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► To cite this version:

K. Zwintz, C. Neiner, O. Kochukhov, T. Ryabchikova, A. Pigulski, et al.. β Cas: The first δ Scuti star with a dynamo magnetic field. *Astronomy & Astrophysics - A&A*, 2020, 643, pp.A110. <10.1051/0004-6361/202038210>. <hal-03254112>

HAL Id: hal-03254112

<https://hal.science/hal-03254112v1>

Submitted on 5 May 2023

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β Cas: The first δ Scuti star with a dynamo magnetic field^{★,★★}

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Received 20 April 2020 / Accepted 10 September 2020

ABSTRACT

Context. F-type stars are characterised by several physical processes such as different pulsation mechanisms, rotation, convection, diffusion, and magnetic fields. The rapidly rotating δ Scuti star β Cas can be considered as a benchmark star to study the interaction of several of these effects.

Aims. We investigate the pulsational and magnetic field properties of β Cas. We also determine the star's apparent fundamental parameters and chemical abundances.

Methods. Based on photometric time series obtained from three different space missions (BRITE-Constellation, SMEI, and TESS), we conduct a frequency analysis and investigate the stability of the pulsation amplitudes over four years of observations. We investigate the presence of a magnetic field and its properties using spectropolarimetric observations taken with the Narval instrument by applying the least-squares deconvolution and Zeeman-Doppler imaging techniques.

Results. The star β Cas shows only three independent p -mode frequencies down to the few ppm-level; its highest amplitude frequency is suggested to be an $n = 3$, $\ell = 2$, $m = 0$ mode. Its magnetic field structure is quite complex and almost certainly of a dynamo origin. The atmosphere of β Cas is slightly deficient in iron peak elements and slightly overabundant in C, O, and heavier elements.

Conclusions. Atypically for δ Scuti stars, we can only detect three pulsation modes down to exceptionally low noise levels for β Cas. The star is also one of very few δ Scuti pulsators known to date to show a measurable magnetic field and the first δ Scuti star with a dynamo magnetic field. These characteristics make β Cas an interesting target for future studies of dynamo processes in the thin convective envelopes of F-type stars, the transition region between fossil and dynamo fields, and the interaction between pulsations and magnetic field.

Key words. stars: individual: β Cas – stars: variables: δ Scuti – stars: atmospheres – stars: magnetic field – stars: abundances

1. Introduction

Stellar evolution is influenced by the interaction of several physical processes such as pulsations, rotation, magnetic fields,

* The BRITE data are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/643/A110>

** Based on data collected by the BRITE Constellation satellite mission, designed, built, launched, operated and supported by the Austrian Research Promotion Agency (FFG), the University of Vienna, the Technical University of Graz, the University of Innsbruck, the Canadian Space Agency (CSA), the University of Toronto Institute for Aerospace Studies (UTIAS), the Foundation for Polish Science & Technology (FNiTP MNiSW), and National Science Centre (NCN). Also based on observations obtained at the Telescope *Bernard Lyot* (USR5026) operated by the Observatoire Midi-Pyrénées, Université de Toulouse (Paul Sabatier), Centre National de la Recherche Scientifique (CNRS) of France.

convection, and diffusion. The lifetimes of stars change depending on how strong the impact of these effects is. The exact description and theoretical representation of all interacting physical processes remains one of the great challenges in stellar astrophysics. Through the analysis of suitable benchmark objects, we aim to learn more about these physical interactions and improve our theoretical understanding.

F-type stars can show four types of pulsations: (i) δ Scuti-type p -modes driven by the κ -mechanism acting in the He II ionisation zone (Pamyatnykh et al. 2000), (ii) γ Doradus-type g -modes that are caused by the convective flux blocking mechanism (Guzik et al. 2000), (iii) gravito-inertial modes or Rossby (r) modes where the Coriolis force is the restoring force (Saió et al. 2018), and (iv) stochastic solar-like oscillations for which pressure is the restoring force (e.g. Kjeldsen & Bedding 1995). In addition, hybrid stars showing both δ Scuti and γ Doradus pulsations have been detected and studied in detail in particular

since the advent of space missions for high-precision photometry (e.g. Grigahcène et al. 2010).

Cool stars typically rotate slowly, while hotter stars mostly show fast rotation. A high rotation rate leads to strong centrifugal forces that make a star oblate. Consequently, the stars' surface temperatures vary across latitudes due to gravity darkening (von Zeipel 1924a,b). Additionally, the distribution of the chemical elements in the stellar atmosphere is affected by high rotation rates (Meynet & Maeder 2000).

In massive and intermediate-mass O, B, and A stars on the main sequence, strong surface magnetic fields are found in ~10% of cases (e.g. Neiner et al. 2017). These are fossil fields that can exist in stars down to effective temperatures of about 6500 K (e.g. Kochukhov 2003). They are usually dipolar with a typical strength of 3 kG (Shultz et al. 2019). At lower effective temperatures up to about 6700 K, observed magnetic fields have a dynamo character (e.g. Marsden et al. 2014). The exact transition between fossil and dynamo fields (Seach et al. 2020), and the possible interaction between these two types of fields (Featherstone et al. 2009), are not well known yet, but it is likely that some early F stars host both a fossil and a dynamo field that are observable at their surface.

The star β Cas (HD 432, HR 21, Caph) has an apparent magnitude of 2.27 in V and a spectral type of F_2 III (Gray et al. 2003). It is located at a heliocentric distance of 16.8 ± 0.1 pc (determined from the HIPPARCOS parallax of 59.58 ± 0.38 mas; van Leeuwen 2007), and its mass is estimated to be $2.09 M_{\odot}$ (Holmberg et al. 2007). During its main sequence lifetime, β Cas was an A-type star that is now considered to be a rather evolved star located near the Terminal Age Main Sequence (TAMS).

Several measurements of β Cas' projected rotational velocity, $v_e \sin i$, can be found in the literature: The first determination dates back to Slettebak (1955), who reported a value of 70 km s^{-1} . This is rather consistent with several recent measurements that lie between 69 and 71 km s^{-1} (e.g. Glebocki et al. 2000; Schröder et al. 2009).

A detailed interferometric study of β Cas (Che et al. 2011) yielded its geometric properties, surface temperature distribution, mass, and age. The star β Cas rotates with more than 90% of its critical velocity, which causes significant radius and temperature differences between the poles and the equator: The radius of β Cas is ~24% greater at the equator than at the poles and the temperature at the poles is ~1000 K higher than at the equator (Che et al. 2011). The authors also determined the inclination angle to be $19.9 \pm 1.9^{\circ}$, the rotation rate to be $1.12_{-0.04}^{+0.03} \text{ d}^{-1}$, the mass to be $1.91 \pm 0.02 M_{\odot}$, and the age to be 1.18 ± 0.05 Gyr.

Millis (1966) discovered the brightness variability of β Cas and identified it as a member of the class of δ Scuti stars as it showed a period of 0.104 d (or 2.5 hours) with an amplitude of 0.04 mag in Johnson V . Yang et al. (1982) confirmed the photometrically discovered period in radial velocity variations of β Cas, which had the highest amplitude in the Ca II line at 8662 \AA . Antonello et al. (1986) refined the period to be 0.10101 days with an amplitude of 0.03 mag in V based on eight nights of observations at Merate Observatory, and speculated that β Cas would be a small-amplitude, mono-periodic δ Scuti star. δ Scuti pulsation and chromospheric variability were detected in the UV using data from the International Ultraviolet Explorer (IUE; Ayres 1991); no hard evidence for a direct connection between both types of variations were found. Based on Strömgren $uvby\beta$ observations, Rodriguez et al. (1992) determined the pulsation frequency to be $9.91 \pm 0.35 \text{ d}^{-1}$ (i.e. a pulsation period of 0.101 d). The authors also determined the effective

temperature, T_{eff} , of β Cas to be 7170 K, its $\log g$ to be 3.62 cgs, and its metallicity $[M/H]$ to be 0.2 from the Strömgren colours. Based on these findings, Rodriguez et al. (1992) calculated the pulsation constant, Q , for the pulsation frequency to be 0.024 indicating first overtone radial pulsation (i.e. a p -mode with $n = 1$). These findings were reviewed by Riboni et al. (1994), who confirmed the presence of a single pulsation frequency at $9.8997 \pm 0.0005 \text{ d}^{-1}$ (i.e. a pulsation period of 0.10101 d); they found T_{eff} of 7000 ± 200 K and a $\log g$ of 3.55 ± 0.3 cgs but reported that a firm mode identification could not be performed.

The chromosphere of β Cas was studied using IUE spectra by Teays et al. (1989) who found that its chromospheric activity is modulated by the pulsation. They also found that the mean level of chromospheric activity is comparable to other F-type stars.

At the beginning of the 20th century, it was speculated that β Cas could be a binary star with an orbital period of 27 days (Mellor 1917). However, a review of over 60 years of radial velocity data conducted by Abt (1965) revealed no sign of binarity. A recent catalogue of δ Scuti stars in binary systems by Liakos & Niarchos (2017) lists β Cas as a "binary with an unspecified orbital period".

In this work, we combine photometric time series obtained by the BRITe-Constellation (where BRITe stands for BRITe Target Explorer; Weiss et al. 2014), Solar Mass Ejection Imager (SMEI; Eyles et al. 2003; Jackson et al. 2004), and Transiting Exoplanet Survey Satellite (TESS; Ricker et al. 2015) space telescopes to investigate the suggested mono-periodicity of β Cas. We also obtained spectropolarimetric observations with the Narval spectropolarimeter at the Telescope Bernard Lyot (TBL) and determine the magnetic properties of β Cas. Based on these data, we also review the fundamental atmospheric parameters and chemical abundances of the star.

2. Observations

2.1. BRITe-Constellation observations and data reduction

The five $20 \times 20 \times 20$ cm nanosatellites of the BRITe-Constellation¹ each carry a 3 cm telescope feeding an uncooled CCD (Weiss et al. 2014). Three BRITe satellites – BRITe-Toronto (BTr), Uni-BRITe (UBr), and BRITe-Heweliusz (BHR) – carry a custom-defined red filter (550–700 nm), and two satellites – BRITe-Austria (BAb) and BRITe-Lem (BLb) – a custom-defined blue filter (390–460 nm). More details on the detectors, pre-launch and in-orbit tests are described by Pablo et al. (2016). Popowicz et al. (2017) describe the pipeline that processes the observed images yielding the instrumental magnitudes which are delivered to the users.

Each BRITe-Constellation nanosatellite observes large fields with typically 15 to 20 stars brighter than $V = 6$ mag including at least three targets brighter than $V = 3$ mag. Each field is observed for at least 15 min each per ~100 min orbit for up to half a year.

The star β Cas was observed during four consecutive seasons with the BRITe-Constellation nanosatellites: (i) in field 11-CasCep-I-2015 from 23 July to 1 November 2015, using four of the five satellites: BAb, BLb, BHR, and BTr, (ii) in field 19-Cas-I-2016 from 7 August 2016 to 1 February 2017 using the satellites BAb and UBr, (iii) in field 30-Cas-II-2017 from 7 August 2017 to 3 February 2018 only using BAb, and (iv) in field

¹ <http://www.brite-constellation.at>

Table 1. Properties of the BRITE-Constellation two-colour observations, the SMEI and TESS data for β Cas.

Satellite	Field ID	Obs _{start}	Obs _{end}	Time base [d]	1/T [d ⁻¹]	N #	Res. noise [ppm]	f_{Nyq} [d ⁻¹]
BAb	11-CasCep-I-2015	29 Aug. 2015	26 Oct. 2015	58.034	0.017	14305	163.1	2117.33
BLb	11-CasCep-I-2015	29 Sep. 2015	17 Oct. 2015	18.067	0.055	8403	217.2	2119.62
<i>BAb + BLb</i>	<i>Combined</i>	<i>29 Aug. 2015</i>	<i>26 Oct. 2015</i>	<i>58.034</i>	<i>0.017</i>	<i>22708</i>	<i>130.8</i>	<i>2133.35</i>
BHr	11-CasCep-I-2015	31 Aug. 2015	17 Oct. 2015	46.950	0.021	4552	215.4	2096.39
BTr	11-CasCep-I-2015	4 Dec. 2015	20 Jan. 2016	43.681	0.023	20609	50.8	1892.47
<i>BHr + BTr</i>	<i>Combined</i>	<i>31 Aug. 2015</i>	<i>20 Jan. 2016</i>	<i>142.096</i>	<i>0.007</i>	<i>25161</i>	<i>62.8</i>	<i>1925.06</i>
BAb	19-Cas-I-2016	7 Aug. 2016	30 Dec. 2016	145.045	0.007	17728	114.4	2085.80
UBr	19-Cas-I-2016	13 Sep. 2016	1 Feb. 2017	141.072	0.007	23494	84.2	2120.99
BAb	30-Cas-II-2017	7 Aug. 2017	3 Feb. 2018	160.170	0.006	7253	227.2	2092.82
BAb	39-Cas-III-2018	8 Aug. 2018	14 Nov. 2018	96.587	0.010	1316	677.3	2075.96
BTr	39-Cas-III-2018	14 Sep. 2018	21 Jan. 2019	129.618	0.008	41757	92.4	2108.16
SMEI				2884.825	0.0003	28742	64.8	7.08
TESS	Sector 17	7 Oct. 2019	2 Nov. 2019	23.081	0.043	13134	–	–
	Sector 18	2 Nov. 2019	27 Nov. 2019	22.873	0.044	14961	–	–
	<i>Combined</i>	<i>7. Oct. 2019</i>	<i>27 Nov. 2019</i>	<i>45.954</i>	<i>0.02</i>	<i>28095</i>	<i>2.4</i>	<i>359.39</i>

Notes. Satellite used to conduct the observations (Satellite), BRITE-Constellation field ID and TESS Sector number (Field ID), corresponding start (Obs_{start}) and end dates (Obs_{end}) of observations, total time base of the reduced data set (Time base), Rayleigh frequency resolution (1/T), number of data points (N), residual noise after pre-whitening all frequencies (Res. noise) which is calculated over the complete frequency range relevant for δ Scuti pulsations from 0 to 100 d⁻¹, and the Nyquist frequency (f_{Nyq}) for each data set. As the TESS data of sectors 17 and 18 were analysed together, no individual values for the residual noise and Nyquist frequency are provided.

39-Cas-III-2018 from 7 August 2018 to 3 February 2019 using BAb and BTr. Table 1 summarises the properties of the BRITE observations.

The BRITE raw data were extracted from the two-dimensional images following the procedure described by Popowicz et al. (2017). The BRITE photometry was subsequently corrected for instrumental effects. The corrections included outlier rejection, and both one- and two-dimensional decorrelations with all available parameters, in accordance with the procedure described by Pigulski (2018). Figure 1 shows the full light curves obtained by UBr (panel a) and BAb (panel b) in 2016 as well as four-day subsets of the data illustrating the pulsational variability. The corresponding light curves of the three other seasons are given in the appendix (Fig. A.1).

2.2. Solar Mass Ejection Imager (SMEI) observations and data reduction

The SMEI experiment (Eyles et al. 2003; Jackson et al. 2004) was placed on board the Coriolis spacecraft and aimed at measuring sunlight scattered by free electrons of the solar wind, but the images are also suitable to extract the photometry of bright stars. The β Cas data were obtained in the years 2003–2010 and are available through the University of California San Diego (UCSD) web page². The SMEI photometry is affected by long-term calibration effects, especially a spurious variability with a period of one year. We corrected the SMEI UCSD photometry of β Cas for this one-year variability by subtracting an interpolated mean light curve. Finally, the individual uncertainties were calculated for each data point using the scatter of the neighbouring data points, and the worst parts of the light curve (i.e. those with an uncertainty higher than 0.013 mag) and outliers were removed. The low-frequency instrumental variability was

filtered out by subtracting detrended residuals of the fit. This procedure removed the intrinsic low-frequency (frequencies below ~ 1 d⁻¹) variability, if present.

The final SMEI data for β Cas comprise 28 742 data points obtained between 6 February 2003 and 31 December 2010 for a total time base of 2884.89537 d (~ 7.9 yr). This corresponds to a Rayleigh frequency resolution, 1/T, of 0.0003 d⁻¹. An overview of the properties of the SMEI data is given in Table 1.

2.3. TESS data

The TESS satellite (Ricker et al. 2015) was launched on 18 April 2018 on board a Falcon 9 rocket and carries four identical cameras. Each camera has an effective aperture size of 10 cm and a 24° × 24° wide field of view. The red-optical TESS bandpass ranges from 600 to 1000 nm. TESS observations are conducted almost across the entire sky in 13 sectors each with a time base of ~ 27 days. Depending on the position of a given target in the sky, TESS data can span between a minimum of ~ 27 and a maximum of 351 days. TESS photometric time series are typically conducted at a cadence of 30 min. For a sub-sample of 200 000 stars, observations are carried out at a 2 min cadence. TESS data are made available to the public through the Barbara A. Mikulski Archive for Space Telescopes (MAST)³.

The primary mission of TESS is the detection of small exoplanets transiting bright, nearby stars. As a secondary science goal, the TESS data is used for asteroseismic studies of all classes of pulsating stars across the Hertzsprung-Russell (HR) diagram.

We combined the photometric time series obtained from BRITE-Constellation and SMEI with observations taken by TESS from 7 October to 27 November 2019 in Sectors 17 and 18. The total time base of the TESS data for β Cas (TIC 396298498, TESS magnitude $T = 2.041$ mag) is 45.954 days

² http://smei.ucsd.edu/new_smei/index.html

³ <http://archive.stsci.edu>

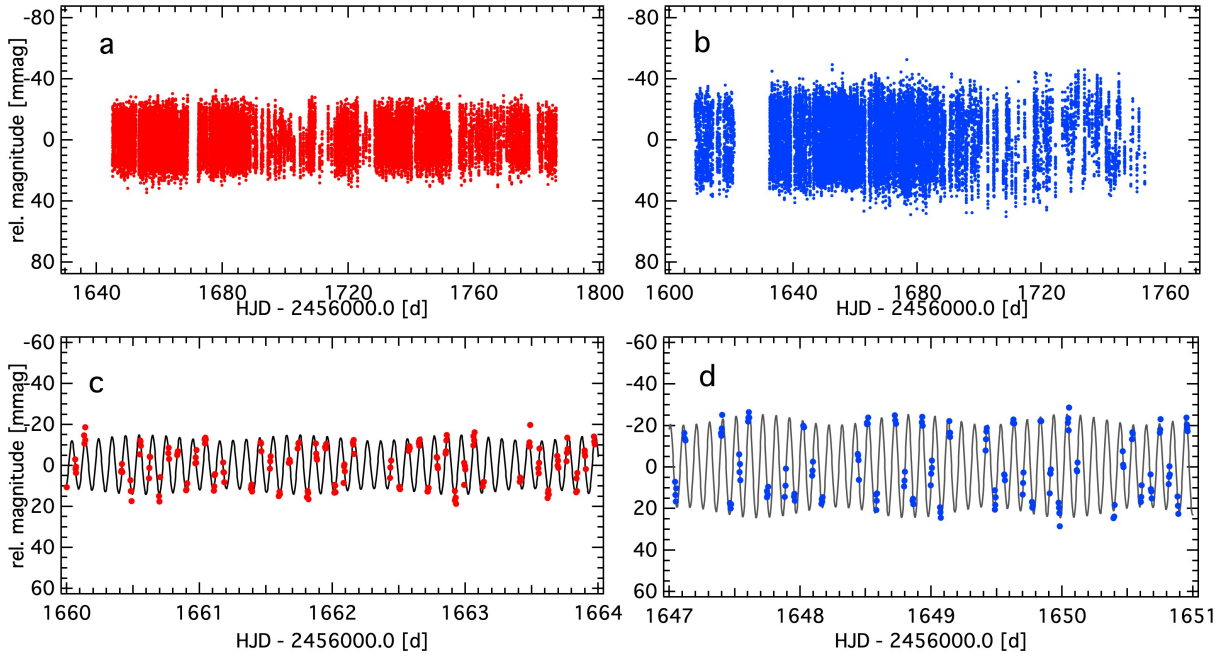


Fig. 1. BRITE photometric time series obtained by UBr (*panel a*) and BAb in 2016 (*panel b*) to the same Y -axis scale and with a time base of 170 days on both X axes. *Panels c and d*: four-day subsets of the UBr and BAb 2016 light curves binned to five-minute intervals and the corresponding multi-sine fit with the two identified pulsation frequencies again to the same Y -axis scale and with a time base of four days on both X axes.

(see Table 1). The star β Cas is one of the pre-selected targets for 2 min cadence observations.

The full TESS light curve and a zoom into a four-day subset are given in Fig. 2. The beginnings and ends of the two Sectors are marked with a vertical dashed line. The obvious gaps within each Sector are caused by the data downlink at the perigee of the TESS orbit. The star β Cas was observed with CCD 1 of Camera 2 in Sector 17 and with CCD 2 of Camera 2 in Sector 18. Just before the end of the first orbit, the Moon entered Camera 1 and 2's field of view. No other instrumental effects were reported (see the TESS Data Release Notes for Sector 17⁴ and 18⁵).

We used the 2 min Simple Aperture Photometry (SAP) flux light curve provided by the MAST archive and the Python packages `lightkurve` (Lightkurve Collaboration 2018) and `SMURFS`⁶ (Müller 2020). We removed all measurements with a non-zero “quality” flag (see Sect. 9 in the TESS Science Data Products Description Document⁷), which marks anomalies like cosmic rays, instrumental issues, or stray light from the Earth or Moon. Furthermore, the outliers were removed by means of 4σ -clipping. In the next step, we subtracted the median flux of the two sectors and combined them. At this point, a first frequency analysis was conducted to check for the presence of a low-frequency signal that might originate from g -modes and of the rotational frequency of 1.12 d^{-1} as found by Che et al. (2011). Figure B.1 shows a zoom into the low-frequency domain of the TESS data at that point in the analysis and illustrates that the rotation frequency cannot be detected. It is also evident that there is an increased noise level in the region between 0.0 and

0.5 d^{-1} that is of instrumental origin. No clear evidence for significant g -mode frequencies can be found. Hence, in the next step, we applied a Gaussian filter using `scipy` (Virtanen et al. 2020) to remove the low-frequency signal that is of instrumental origin. This procedure removed any intrinsic low-frequency (i.e. frequencies below $\sim 2 \text{ d}^{-1}$) variability, if present.

2.4. Narval spectropolarimetric observations

The star β Cas was observed with the Narval spectropolarimeter installed at the 2.03 m *Télescope Bernard Lyot* (TBL) at Pic du Midi Observatory in France. Narval provides spectra covering the wavelength range from 3900 to 10 500 Å with a resolving power of $\sim 65 000$, spread over 40 echelle orders recorded on a single detector. We used Narval in circular polarisation mode to produce Stokes V and Stokes I spectra from a sequence of four sub-exposures. A null polarisation spectrum (N) is also produced by combining the four sub-exposures in a destructive way. N allows us to check for signal due to instrumental effects or stellar phenomena unrelated to magnetism, such as pulsations.

The first observations of β Cas were obtained on 3 November 2013 as a part of the BRITEpol survey (Neiner et al. 2017). BRITEpol measures the potential magnetic field of all stars brighter than $V = 4$ mag, as a ground-based support to BRITE. The possible detection of a magnetic field in this first observation of β Cas led to a series of three additional observations obtained between 24 September and 21 December 2014, to confirm the presence of a magnetic field in β Cas. Finally, a complete series of follow-up observations was acquired between 1 December and 13 December 2015 simultaneously with the BRITE observations. The log of the Narval observations is available in Table 2.

Narval employs the beam-exchange polarimetric modulation procedure (Semel et al. 1993; Donati et al. 1997; Bagnulo et al. 2009), which allows one to compensate most instrumental polarisation artefacts and prevent a temporal variation of stellar

⁴ https://archive.stsci.edu/missions/tess/doc/tess_drn/tess_sector_17_drn24_v02.pdf

⁵ https://archive.stsci.edu/missions/tess/doc/tess_drn/tess_sector_18_drn25_v02.pdf

⁶ <https://github.com/MarcoMuellner/SMURFS>

⁷ <https://archive.stsci.edu/missions/tess/doc/EXP-TESS-ARC-ICD-TM-0014.pdf>

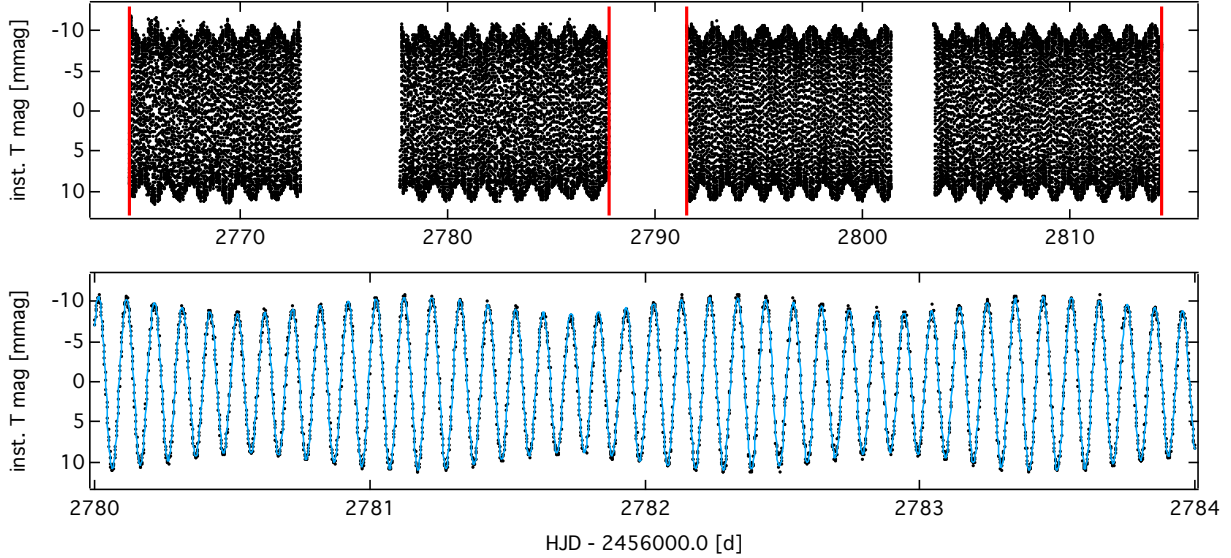


Fig. 2. *Top panel:* complete TESS light curve. Start and end dates of Sectors 17 and 18 are marked with vertical red lines. *Bottom panel:* four-day zoom illustrating the pulsational variability.

spectra to result in spurious polarisation signatures. In any case, due to the brightness of the star the individual sub-exposures could be kept very short (65 s), excluding any possibility of spurious polarisation appearing due to spectral variability associated with δ Scuti pulsations. To obtain a higher signal-to-noise (S/N), several consecutive polarimetric sequences were then recorded and co-added after reduction (see Sect. 5.1).

The data were reduced with the LIBRE-ESPRIT software pipeline available at TBL. Each order of the intensity spectra was then normalised separately using SPENT (Martin et al. 2018) and the normalisation function was also applied to Stokes V and N .

3. Photometric analysis

The frequency analysis of the BRITe, SMEI and TESS photometric time series of β Cas was performed independently of each other using the software package Period04 (Lenz & Breger 2005) that combines Fourier and least-squares algorithms. Frequencies were then pre-whitened and considered to be significant if their amplitudes exceeded 3.9 times the local noise level in the amplitude spectrum (Breger et al. 1993; Kuschnig et al. 1997). Frequency, amplitude, and phase errors were calculated using the formulae given by Montgomery & O’Donoghue (1999). To verify the analysis, we used the frequency extraction tool SMURFS, which automates the search for significant frequencies in time series data by iterative searching for the frequency with the maximum amplitude and removing it using curve fitting tools provided by `lmfit` (Newville et al. 2014) and `scipy` (Virtanen et al. 2020).

All analysed data sets show the presence of two pulsation modes with frequencies F_1 at 9.89708 d^{-1} and F_2 at 9.04369 d^{-1} (see Table 3). In some of the BRITe data sets and the TESS data, an harmonic frequency to F_1 is detected. Only in the TESS data, a third independent δ Scuti-type frequency of F_4 at 8.3847 d^{-1} with an amplitude of only 0.055 mmag and a combination frequency of $F_1 + F_2$ are found.

The harmonic frequency F_3 at 19.79221 d^{-1} is identified to be two times F_1 . It is only significant in those photometric time series that have a low enough noise level (i.e. in the

Table 2. Journal of the spectropolarimetric observations.

#	Date	mid-HJD –2450 000	T_{exp} [s]	S/N
1	Nov. 3, 2013	6600.2627	4×65	818
2	Sep. 25, 2014	6925.6165	$3 \times 4 \times 65$	1206
3	Dec. 19, 2014	7011.2941	$5 \times 4 \times 65$	1258
4	Dec. 21, 2014	7013.2990	$5 \times 4 \times 65$	1122
5	Dec. 1, 2015	7358.3265	$5 \times 4 \times 65$	984
6	Dec. 1, 2015	7358.3891	$5 \times 4 \times 65$	881
7	Dec. 2, 2015	7359.3314	$5 \times 4 \times 65$	723
8	Dec. 2, 2015	7359.3870	$5 \times 4 \times 65$	781
9	Dec. 5, 2015	7362.2862	$5 \times 4 \times 65$	918
10	Dec. 6, 2015	7363.2947	$5 \times 4 \times 65$	1100
11	Dec. 6, 2015	7363.3535	$5 \times 4 \times 65$	1154
12	Dec. 6, 2015	7363.4058	$5 \times 4 \times 65$	1160
13	Dec. 7, 2015	7364.3514	$5 \times 4 \times 65$	1140
14	Dec. 7, 2015	7364.4070	$5 \times 4 \times 65$	1058
15	Dec. 9, 2015	7366.3073	$5 \times 4 \times 65$	1040
16	Dec. 11, 2015	7368.3693	$5 \times 4 \times 65$	1093
17	Dec. 12, 2015	7369.3194	$5 \times 4 \times 65$	991
18	Dec. 12, 2015	7369.3734	$5 \times 4 \times 65$	889
19	Dec. 13, 2015	7370.3799	$5 \times 4 \times 65$	995

Notes. Indicated are the index number of the averaged polarimetric measurement, the date of observations, the Heliocentric Julian Date at the middle of the observations (mid-HJD – 2450 000), the number of polarimetric sequences times the exposure time in seconds, and the average signal-to-noise ratio of a (single) spectropolarimetric sequence per CCD pixel at $\sim 500 \text{ nm}$.

BRITe 2015 and 2016 B & R observations and in TESS data). Similarly, frequency F_5 at 18.9409 d^{-1} is actually F_1 plus F_2 ; due to its small amplitude of 0.038 mmag, it is only detectable in the TESS data. The TESS data also allow us to identify a frequency F_6 at 9.9000 d^{-1} that is the same as F_1 within the Rayleigh frequency resolution. We speculate that it results from the small amplitude changes detected in F_1 (see Sect. 6.2). With the presently available data, we cannot decide unambiguously

Table 3. Pulsation frequencies (F), amplitudes (A), phases (ϕ), and signal-to-noise values (S/N) of β Cas derived from the BRITE-Constellation, SMEI, and TESS data.

	F_1	F_2	$F_3 = 2 \cdot F_1$	F_4	$F_5 = F_1 + F_2$	$F_6 = F_1 \pm (1/T)$	
Freq. BRITE red	9.89708(1)	9.0437(1)	19.7922(6)	–	–	–	d ⁻¹
A_R 2015	13.30(4)	1.51(4)	0.28(4)	–	–	–	mmag
A_R 2016	13.14(6)	1.43(6)	0.40(6)	–	–	–	mmag
A_R 2018	12.57(6)	1.34(6)	–	–	–	–	mmag
ϕ_R 2015	0.1911(5)	0.216(5)	0.4(2)	–	–	–	
ϕ_R 2016	0.1505(7)	0.769(6)	0.4(2)	–	–	–	
ϕ_R 2018	0.1566(7)	0.791(6)	–	–	–	–	
S/N_R 2015	21.47	21.94	4.38	–	–	–	
S/N_R 2016	23.81	17.57	4.98	–	–	–	
S/N_R 2018	32.54	14.46	–	–	–	–	
Freq. BRITE blue	9.89710(1)	9.0434(1)	19.7946(7)	–	–	–	d ⁻¹
A_B 2015	22.2(1)	2.5(1)	0.5(1)	–	–	–	mmag
A_B 2016	22.47(8)	2.62(8)	0.47(8)	–	–	–	mmag
A_B 2017	22.2(2)	2.38(2)	–	–	–	–	mmag
A_B 2018	23.7(4)	–	–	–	–	–	mmag
ϕ_B 2015	0.1719(7)	0.132(7)	0.49(3)	–	–	–	
ϕ_B 2016	0.1469(6)	0.82(5)	0.99(3)	–	–	–	
ϕ_B 2017	0.126(1)	0.78(1)	–	–	–	–	
ϕ_B 2018	0.625(3)	–	–	–	–	–	
S/N_B 2015	17.41	18.67	3.53	–	–	–	
S/N_B 2016	23.15	21.45	3.99	–	–	–	
S/N_B 2017	14.12	10.27	–	–	–	–	
S/N_B 2018	7.49	–	–	–	–	–	
Freq. SMEI	9.8971699(9)	9.044955(8)	–	–	–	–	d ⁻¹
A_{SMEI}	11.25(5)	1.24(5)	–	–	–	–	mmag
ϕ_{SMEI}	0.1301(7)	0.001(7)	–	–	–	–	
S/N_{SMEI}	120.65	21.41	–	–	–	–	
Freq. TESS	9.897098(2)	9.04391(2)	19.7942(1)	8.3847(4)	18.9409(6)	9.9000(5)	d ⁻¹
A_{TESS}	9.749(2)	1.035(2)	0.229(2)	0.055(2)	0.038(2)	0.025(2)	mmag
ϕ_{TESS}	0.77974(4)	0.4214(3)	0.304(2)	0.771(6)	0.260(9)	0.305(8)	
S/N_{TESS}	20.28	153.52	54.77	10.51	10.65	19.365	

Notes. Frequency, amplitude, and phase errors are given as last-digit errors in parentheses and were calculated following [Montgomery & O'Donoghue \(1999\)](#). Frequencies F_3 , F_5 , and F_6 are identified as linear combinations in the top line.

whether F_6 is an independent frequency or is dependent on F_1 . Future additional TESS observations of β Cas will hopefully contribute to finding an unambiguous solution. A summary of the pulsation frequencies, amplitudes, and phases derived from the three seasons of BRITE-Constellation data, SMEI and TESS observations is given in Table 3.

As an example, the amplitude spectra from the 2016 BAB and UBr data are shown in Fig. 3: Blue filter data are shown on the left, red filter data on the right side. The top panels illustrate the amplitude spectra of the original data with F_1 identified as well as two alias frequencies, which appear in the blue and the red filter data. $f_{\text{alias},1}$ can be identified as the corresponding BRITE orbital frequency, f_{orb} , minus F_1 and $f_{\text{alias},2}$ as 2 times f_{orb} minus F_1 . Both alias frequencies disappear after pre-whitening F_1 as can be seen in the middle panels of Fig. 3, which shows the amplitude spectra after subtraction of F_1 , where F_2 and two new alias frequencies $f_{\text{alias},3}$ and $f_{\text{alias},4}$ are marked. $f_{\text{alias},3}$ is generated as f_{orb} minus F_2 , and $f_{\text{alias},4}$ as 2 times f_{orb} minus F_2 . They again disappear when F_2 is pre-whitened. The bottom panels show the amplitude spectra after pre-whitening with F_1 and F_2 with $F_3 = 2 \cdot F_1$ and f_{orb} marked. The residual amplitude spectra for the 2016 blue and red filter data are shown in the bottom panel

of Fig. 3 and illustrate the corresponding average residual noise levels of 114.4 ppm for BAB and 84.2 ppm for UBr. The amplitude spectra for the 2015, 2017, and 2018 BRITE observations, and the spectral window functions are given in Appendix B (Figs. B.2–B.5).

The Nyquist frequency for the SMEI data is at 7.08 d⁻¹ because measurements were taken every ~ 1.7 h. The frequencies of δ Scuti stars are typically higher than this value (e.g. [Aerts et al. 2010](#)). As it was shown for Kepler data by [Murphy et al. \(2013\)](#), it is possible to do super-Nyquist asteroseismology using the SMEI data because the real peaks remain as singlets even if they are above f_{Nyq} . Using the SMEI data, we confirm the pulsation frequencies F_1 and F_2 (see Fig. 4). The residual amplitude spectrum after pre-whitening F_1 and F_2 is shown in the bottom panel of Fig. 4. Figure B.6 shows the SMEI spectral window.

The amplitude spectra obtained from the TESS data are illustrated in Fig. 5: Following the pre-whitening sequence, F_1 to F_6 are identified and marked. The residual amplitude spectrum after pre-whitening the six frequencies is shown in the bottom panel of Fig. 5. For completeness, Fig. B.7 illustrates the spectral window of the TESS data.

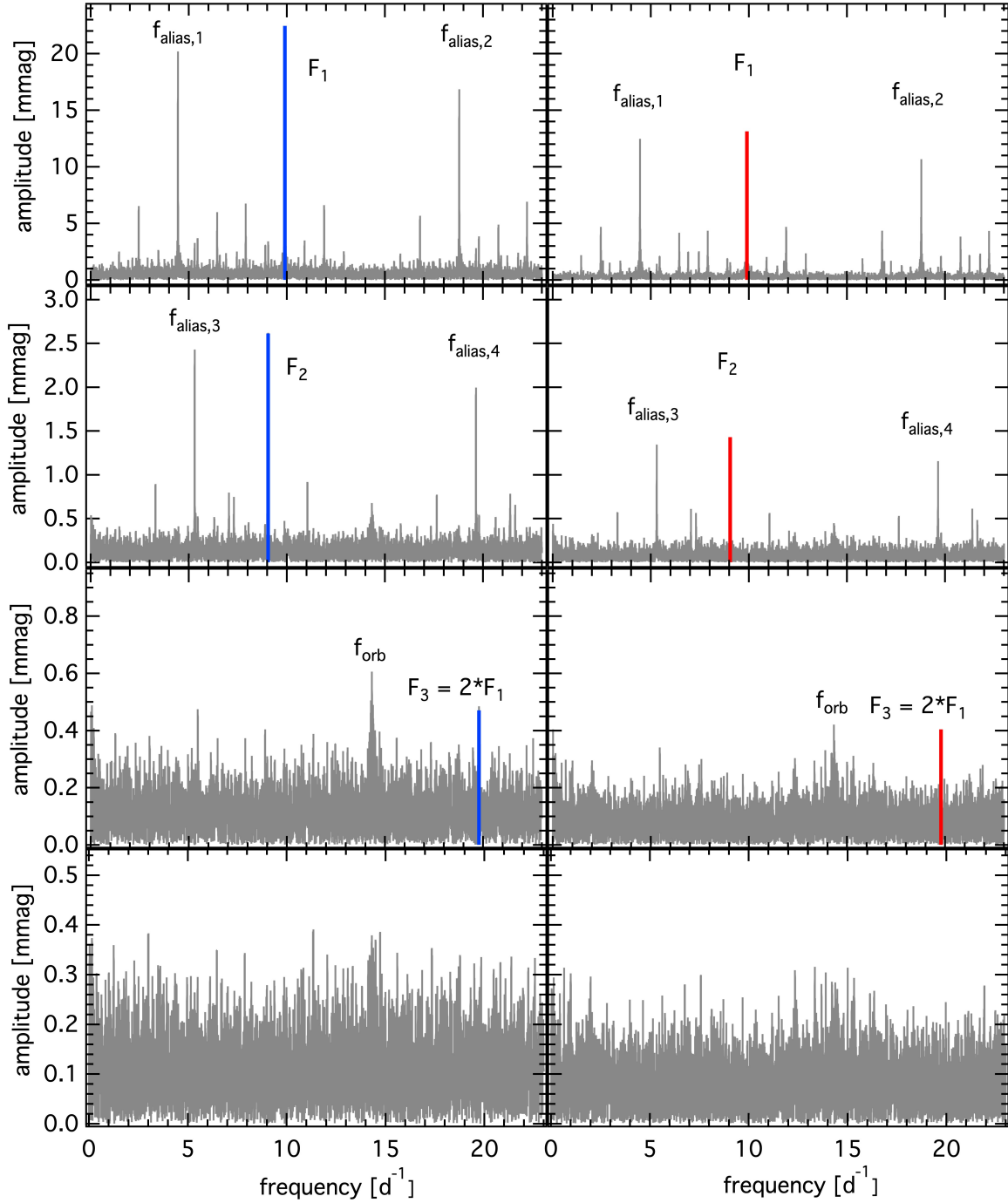


Fig. 3. Amplitude spectra of the BRITE-Constellation data obtained in 2016: BAb blue filter data are shown on the left side, UBr red filter data on the right side. *Top panels:* amplitude spectra of the original data with F_1 identified, *second panels:* amplitude spectra after pre-whitening F_1 , *third panels:* those after pre-whitening F_1 and F_2 , and *bottom panel:* residual amplitude spectra after pre-whitening all significant frequencies. An explanation for the identified alias frequencies is given in the text.

4. Spectroscopic analysis

The spectropolarimetric time-series were averaged to produce one spectrum with $S/N = 1250$ estimated in a small region with only continuum from 6070–6071 Å. This value for the signal-to-noise ratio corresponds to the actual pixel-to-pixel scatter measured in the red. It is not much larger than the values given in Sect. 2.4 due to a fixed-pattern noise affecting the red part of the Narval spectra. This combined spectrum was used for the determination of the apparent atmospheric parameters and for a

detailed abundance analysis conducted using the SME software (Spectroscopy Made Easy – version 503) written in the IDL language (Valenti & Piskunov 1996; Piskunov & Valenti 2017). In our analysis, we did not take into account the non-sphericity and gravity darkening due to rapid rotation, but constrain our investigation to the apparent values.

Following an approach described by Ryabchikova et al. (2016), six intervals are chosen for the fitting of synthetic spectra to the observations: 4400–4700, 5100–5250, 5570–5750, 6000–6220, 6400–6700 and 7700–7900 Å. The 6400–6700 Å

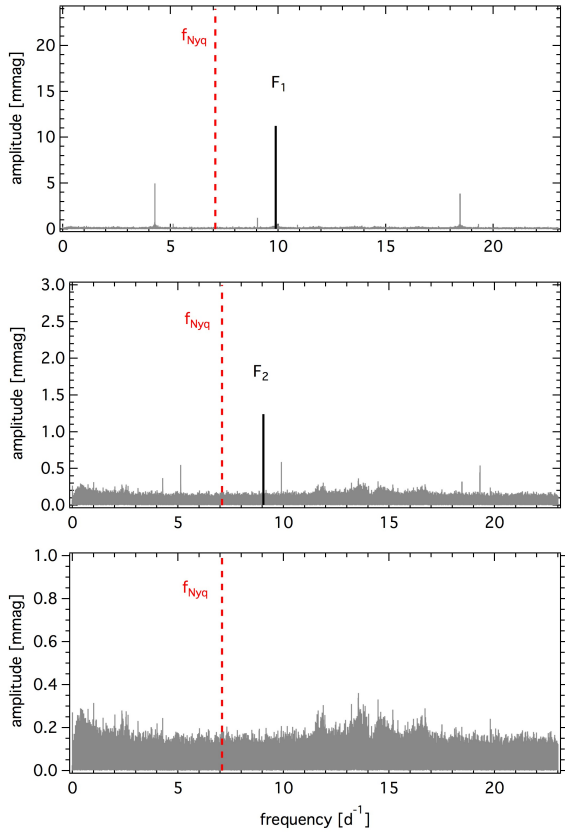


Fig. 4. Amplitude spectra of the SMEI data: Original data with F_1 identified (top panel), amplitude spectra after pre-whitening with F_1 and showing F_2 (middle panel), and residuals after pre-whitening F_1 and F_2 (bottom panel). The position of the Nyquist frequency is marked in red.

region contains the $H\alpha$ line which is a good temperature indicator in the cool stars' domain and is still slightly sensitive to gravity variations at effective temperatures near 7000 K (see Ryabchikova et al. 2016). The 7700–7900 Å region contains the OI triplet which allows an estimation of the oxygen abundance in non-local thermodynamic equilibrium (NLTE). In addition, the small spectral region from 5850–5910 Å with the Ba II line at a wavelength of 5853 Å and the resonance Na I D lines was used for abundance determination. Atomic line parameters were extracted from the third version of the Vienna Atomic Line Database (VALD3; Ryabchikova et al. 2015; Pakhomov et al. 2017). Besides O, NLTE effects were taken into account for Na, Ca, and Ba (Piskunov et al. 2017). Strong observed lines of these elements allow the measurement of accurate abundances even in such a rapidly rotating star. The SME analysis was performed with the grid of plane-parallel MARCS atmospheric models (Gustafsson et al. 2008). The library of the departure coefficients for this grid was calculated based on the model atom developed for O by Sitnova et al. (2013), for Na by Alexeeva et al. (2014), for Ca by Sitnova et al. (2018), and for Ba by Mashonkina et al. (1999).

The SME software implements two methods for estimating parameter uncertainties when fitting stellar spectra. The first is a standard estimate of the confidence interval based on the covariance matrix. This matrix is just the inverse of the Marquardt-Levenberg Hessian matrix approximation computed at the best fit solution (see, e.g. Press et al. 2002, Sect. 15 Modelling of Data). The covariance matrix is stored as part of the SME output

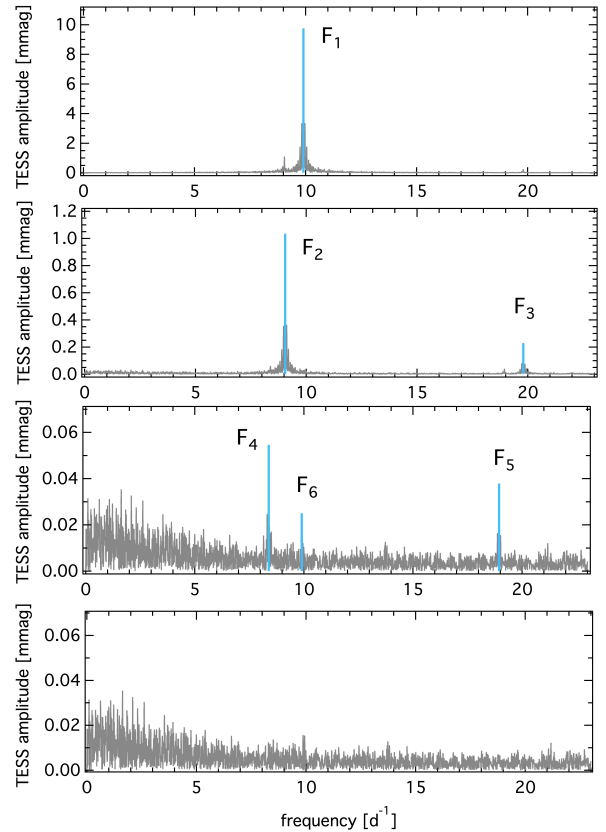


Fig. 5. Fourier analysis of the TESS data: The amplitude spectrum of the original data with F_1 identified (top panel), amplitude spectrum after pre-whitening F_1 (second panel from the top), amplitude spectrum after pre-whitening F_1 , F_2 , and F_3 (third panel from the top), and residual amplitude spectrum after pre-whitening all significant frequencies (bottom panel).

structure. The main diagonal contains the squares of confidence intervals (one σ for normal distribution of uncertainties) for all free parameters of the fit. This is true under the assumption of a perfect model (that is the residuals of the fit gradually go to zero as data accuracy improves). Such a situation will correspond to a reduced χ^2 reaching unity, which is seldom the case in spectral synthesis. In practice, for χ^2 values larger than one this method gives highly underestimated values of uncertainties. In our error estimates using method 1, we account for this effect by multiplying the main diagonal numbers by the reduced χ^2 . The second more heuristic approach described in Piskunov & Valenti (2017) and implemented in Ryabchikova et al. (2016) is based on the statistical analysis of the residuals. In this case, the focus is on the core of the distribution that, given good statistics, resembles a normal distribution. Therefore, the new method provides very reasonable uncertainty estimates for parameters constrained by essentially all spectral lines (e.g. effective temperature, metallicity, velocities). The estimates are less robust in case that few lines are sensitive to the parameter (e.g. surface gravity, individual abundances for species represented by one, or a few lines etc.). For abundance estimates of Sr, Nd, and Eu, we applied the spectrum fitting procedure used in the BinMag6 code (Kochukhov 2018).

Synthetic spectra were calculated with the model atmosphere and abundance table derived by the SME procedure, while Sr, Eu, and Nd abundances were varied to reach the best fit. For the Sr and Eu abundance estimates, a fit of the synthetic

Table 4. Atmospheric parameters of β Cas used for the determination of the abundance of Nd.

Parameter	This paper			Che et al. (2011)		Gray et al. (2003)
	Value	err ₁	err ₂	Model 1	Model 2	
T_{eff} [K]	6920	35	140	6825	6897	6915
$\log g$ [cgs]	3.53	0.16	0.58	3.57	3.59	3.49
[M/H]	-0.11	0.04	0.12	–	–	-0.02
$\nu_e \sin i$ [km s ⁻¹]	73.6	8.1	7.0	72.4	79.8	–
ν_{mic} [km s ⁻¹]	4.1	0.4	0.5	–	–	3.1

Notes. The errors, err₁ and err₂, were calculated using SME and are based on the confidence interval (method 1) and the statistical analysis of the residuals (method 2). Apparent parameters from modelling by Che et al. (2011) are given in Cols. 5–6. The last column contains parameters derived by Gray et al. (2003).

spectrum to the observed spectrum was performed in the 4200–4230 Å region, which contains the Sr II λ 4215.52 Å and Eu II λ 4205.05 Å lines. Additionally, the Eu II line at λ 6645.11 Å was fit. The spectral region 5200–5350 Å was used for the determination of the abundance of Nd. This region contains many Nd II and the strongest Nd III lines, which appear in stars with high overabundance of the rare-earth elements. The error estimates for Sr, Nd, and Eu are obtained using method 1.

The final parameters of β Cas derived from the spectral synthesis are $T_{\text{eff}} = 6920$ K, $\log g = 3.53$ cgs, [M/H] = -0.11, $\nu_e \sin i = 73.6$ km s⁻¹, and microturbulent velocity, $\nu_{\text{mic}} = 4.1$ km s⁻¹. They are listed together with the error estimates from both methods (err₁ and err₂) and a comparison to literature values in Table 4.

As described above, our SME analysis was performed using a grid of plane-parallel atmospheric models. The surface integration implemented in SME assumes a spherical star with a homogeneous surface. However, according to Che et al. (2011), β Cas is a rapidly rotating star spinning close to its critical velocity, and hence has inhomogeneous surface temperature and gravity distributions. The authors modelled β Cas using two methods, and provided apparent effective temperatures, luminosities, and masses. The corresponding effective temperatures and gravities for both models – the modified von Zeipel model (Model 1) and the Lucy model (Model 2) – are given in columns five and six of Table 4. Within the errors, our parameters agree with those obtained by Che et al. (2011). They also agree with the parameters derived by Gray et al. (2003).

The results of the abundance analysis are presented in Table 5. Columns err₁ and err₂ list the errors of the abundances according to the two methods for error determination implemented in SME. The last column shows element abundances relative to solar values. The solar abundances were taken from Scott et al. (2015b,a) and Grevesse et al. (2015).

Chemical species marked by asterisks in Table 5 have few lines in the analysed parts of the spectrum; therefore their abundances are very uncertain. N and Ba also have few lines but they are strong enough to provide a reasonable abundance estimate. Abundances of heavy elements are rather uncertain, too, but are close to the solar values within their errors. The atmosphere of β Cas is slightly metal deficient in iron peak elements and slightly overabundant in both light elements C and O, and heavy elements. Overall, the observed abundance pattern of β Cas is similar to the atmospheric abundances of another δ Scuti-type star HD 261711 (Zwintz et al. 2013). Figures 6 and 7 illustrate our best fitting solution using the derived fundamental parameters and atmospheric abundances in the region around H α and in two selected regions.

Table 5. Abundances in the atmosphere of β Cas.

Element	$\log(N_{\text{el}}/N_{\text{tot}})$	err ₁	err ₂	$[N_{\text{el}}/N_{\text{tot}}]$
C*	-3.52	0.10	0.26	+0.09
O	-3.19	0.02	0.06	+0.16
Na	-5.87	0.03	0.12	-0.04
Mg	-4.57	0.06	0.16	-0.12
Al*	-5.81	0.23	0.11	-0.20
Si	-4.55	0.07	0.19	-0.02
Ca	-5.84	0.05	0.15	-0.12
Sc	-8.93	0.10	0.15	-0.05
Ti	-7.14	0.03	0.17	-0.03
Cr	-6.54	0.05	0.22	-0.12
Fe	-4.76	0.02	0.13	-0.18
Ni	-6.05	0.08	0.29	-0.21
Sr*	-9.13	0.10		+0.08
Y	-9.75	0.09	0.18	+0.08
Zr	-9.40	0.19	0.37	+0.05
Ba	-9.74	0.03	0.06	+0.05
Nd*	-10.57	0.10		+0.05
Eu*	-11.40	0.10		+0.12

Notes. Columns err₁ and err₂ list the errors of the abundances according to the two methods for error determination implemented in SME. The last column shows the abundances relative to solar values. The solar abundances were taken from Scott et al. (2015b,a) and Grevesse et al. (2015). Chemical species marked by asterisks have uncertain abundance values because they have only few weak or blended lines in the analysed parts of the spectrum (see text).

5. Spectropolarimetric analysis

5.1. LSD profiles

We used the least squares deconvolution (LSD) technique (Donati et al. 1997) to create mean Stokes I , Stokes V , and N profiles of each Narval polarimetric sequence. The velocity step used for the LSD profiles is 2.6 km s⁻¹.

To perform LSD, a list of stellar lines present in the spectrum, together with their wavelength, depth, and Landé factor is necessary. We started from a line list extracted from the VALD3 atomic database for the effective temperature, gravity, microturbulence, and chemical abundances of β Cas determined above (Table 4) and restricted it to lines with depths larger than 1% of the continuum level. From this template list we rejected the hydrogen lines, as well as lines blended with the hydrogen line wings, lines that were not present in the spectrum, or that were contaminated by telluric or interstellar features. We then

Table 6. Magnetic field measurements for β Cas.

#	B_l	N_l	Magnetic detection
1	0.6 \pm 6.6	-1.1 \pm 6.6	ND
2	1.3 \pm 2.5	-4.6 \pm 2.5	MD
3	3.9 \pm 1.9	-0.0 \pm 2.0	DD
4	0.8 \pm 2.1	1.4 \pm 2.1	DD
5	-5.9 \pm 2.5	-2.3 \pm 2.5	DD
6	0.6 \pm 2.7	1.6 \pm 2.7	DD
7	-1.6 \pm 3.4	2.1 \pm 3.4	ND
8	-1.4 \pm 3.0	-1.7 \pm 3.0	MD
9	-3.5 \pm 2.6	-1.3 \pm 2.6	MD
10	-3.1 \pm 2.2	-2.6 \pm 2.2	DD
11	1.0 \pm 2.1	0.6 \pm 2.1	MD
12	-0.1 \pm 2.1	0.0 \pm 2.1	DD
13	-3.2 \pm 2.1	1.0 \pm 2.1	ND
14	-3.7 \pm 2.3	0.7 \pm 2.3	DD
15	3.4 \pm 2.6	-3.9 \pm 2.6	DD
16	2.8 \pm 2.2	-1.8 \pm 2.3	DD
17	-0.3 \pm 2.4	-1.4 \pm 2.4	DD
18	-0.9 \pm 2.7	-0.6 \pm 2.7	DD
19	1.7 \pm 2.4	-2.7 \pm 2.4	ND

Notes. Columns indicate the number of the polarimetric measurement, the longitudinal field value with its error bar in Gauss, the corresponding measurement obtained for N , and the formal magnetic field detection status (DD is a Definite Detection, MD is a Marginal Detection, and ND is No Detection) based on Stokes V profile analysis.

We find that the longitudinal field values are very weak, of the order of a few Gauss. All B_l that we derive are compatible with 0, indicating a complex magnetic field topology typical of cool active stars with dynamo fields (e.g. Donati et al. 1997; Donati & Collier Cameron 1997).

5.3. Zeeman Doppler imaging

We used Zeeman Doppler imaging (ZDI, Kochukhov 2016) to infer the magnetic field topology of β Cas and to put constraints on the stellar rotational period. The tomographic mapping was carried out with the help of the magnetic inversion code INVERSLSD (Kochukhov et al. 2014), which was modified to include a non-radial pulsation velocity field using spherical harmonic parameterisation described by Kochukhov (2004). In addition, we lifted the usual approximation of ZDI that each observation corresponds to an instantaneous profile measurement. Instead, the model line profiles were calculated by a numerical integration over appropriate pulsational and rotational phase intervals, which allowed us to properly account for phase smearing. On the other hand, the gravity darkening and non-sphericity resulting from a rapid rotation of β Cas were not included.

A subset of observations obtained in the period from 1 December 2015 to 13 December 2015 was considered for the ZDI modelling. This data set comprises 75 individual Stokes V observing sequences (4×65 s each), in groups of five consecutive observations repeated one to three times per night. In the first analysis step, we modelled all 75 Stokes I LSD profiles in order to optimise $v_e \sin i$ together with the pulsational mode parameters. This was accomplished with the help of a series of forward calculations assuming a single-mode pulsation with $P_{\text{puls}} = 0.1010396$ d (i.e. the average period corresponding to our F_1) and $i = 20^\circ$ (Che et al. 2011). The pulsa-

tional velocity amplitude and phase were adjusted to reproduce the observed radial velocity curve. Based on this analysis, we inferred $v_e \sin i = 75 \text{ km s}^{-1}$, which is close to the value of 73.6 km s^{-1} found in Sect. 4, and found that an axisymmetric quadrupolar mode provides a marginally better description of the pulsational Stokes I profile variability pattern compared to the radial or axisymmetric dipolar pulsation.

In a second step, we used the previously determined broadening and pulsational parameters to reconstruct the magnetic field geometry of β Cas for different trial values of the stellar rotational period. This modelling was based on the 15 Stokes V averaged spectra obtained in 2015 (i.e. numbers #5 to #19 in Table 2).

Che et al. (2011) estimate the rotational frequency to be $1.12^{+0.03}_{-0.04} \text{ d}^{-1}$. This corresponds to $P_{\text{rot}} = 0.89^{+0.03}_{-0.02} \text{ d}$. For the ZDI modelling, we considered a P_{rot} interval of 0.847–1.174 d, which encompasses the $\pm 2\sigma$ rotational period range from Che et al. (2011) and extends all the way to 1.172 d corresponding to the difference between the two main frequencies present in the BRITE data. The resulting relative χ^2 of the fit to Stokes V profiles is illustrated as a function of trial rotation period in Fig. 9. We find that multiple rotation periods provide good descriptions of our Stokes V observations of β Cas. Specifically, the lowest χ^2 of the fit to the observed LSD profiles is achieved with P_{rot} of 0.868, 0.890, and 1.145 d. All three rotation periods result in qualitatively similar magnetic field maps and a non-sinusoidal behaviour of the B_l values. The ZDI field geometry and Stokes V profile fits corresponding to $P_{\text{rot}} = 0.868$ d are illustrated in Fig. 10. The B_l values folded with this period are shown in Fig. 11.

The three rotation periods mentioned above result in a qualitatively different phase distribution of the 15 Stokes V observations. The period $P_{\text{rot}} = 0.868$ d yields three pairs of Stokes V profiles, obtained seven nights apart, with very similar rotational phases. These profiles closely agree with each other both in the observations and in the model (see Fig. 10). This is unlikely to be a coincidence. On the other hand, periods $P_{\text{rot}} = 0.890$ d and $P_{\text{rot}} = 1.145$ d yield no pairs of close rotational phases. These periods might therefore represent aliases appearing due to a relatively sparse rotational phase sampling of our observations. For this reason, we consider $P_{\text{rot}} = 0.868$ d to be the most likely rotational period of β Cas. The ZDI inversion with this period also provides a magnetic map with 14% lower total energy compared to the reconstruction results for the other two periods. Formally, $P_{\text{rot}} = 0.890$ d cannot be excluded as it produces a low χ^2 and is consistent with the results of Che et al. (2011). However, it does not explain the observed repetition of Stokes V profile shapes. The period $P_{\text{rot}} = 1.145$ d has the same problem; in addition it is formally excluded (at the 8.4σ level) by the interferometric results of Che et al. (2011).

For each of the three plausible periods we tested the possibility of the presence of a solar-like differential rotation. In all three cases equally good fits can be obtained with no differential rotation ($\alpha \equiv \Delta\Omega/\Omega_e = 0.0$) and with a combination of a shorter equatorial period and a moderate solar-like differential rotation ($\alpha = 0.01$ – 0.02). In other words, the existing observational data do not allow us to meaningfully constrain differential rotation.

Considering the ZDI results obtained for $P_{\text{rot}} = 0.868$ d, we performed a bootstrapping error analysis by randomly reshuffling residuals between observations and model fit for each rotational phase, adding these residuals back to the model profiles and reconstructing a new magnetic map from simulated data. This procedure was repeated 100 times and the resulting standard deviations of different magnetic parameters were adopted as error estimates. This analysis showed that the local error of

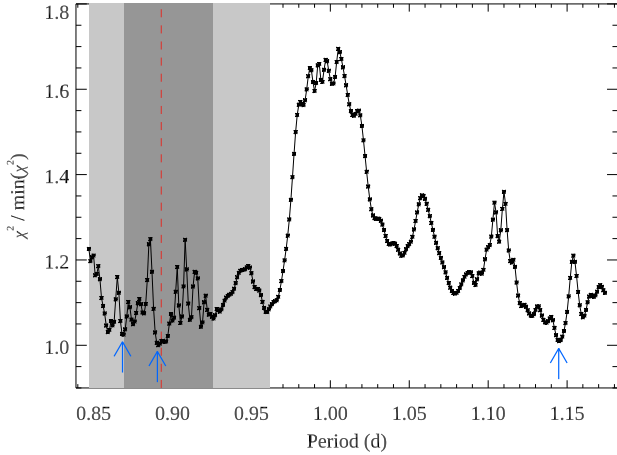


Fig. 9. Relative χ^2 of the fit to Stokes V LSD profiles as a function of rotational period. The vertical dashed line and the shaded regions correspond to the rotational period determined by Che et al. (2011) and the corresponding $1-2\sigma$ error bars. The arrows indicate the three rotational periods discussed in the text.

the magnetic field vector maps shown in Fig. 10 is 6 G for the radial field and 8–9 G for the meridional and azimuthal components. The maximum surface field strength is 87 ± 5 G while the mean field strength (field modulus averaged over the visible hemisphere) is 20 ± 1 G.

The spherical harmonic description of the surface magnetic field implemented in INVERSLSD (see Kochukhov et al. 2014 for details) allows us to assess contributions of different modes to the field geometry of β Cas. We infer that the magnetic field of this star is predominantly poloidal ($65 \pm 5\%$ of the field energy is concentrated in poloidal modes) and contains a comparable contribution of axisymmetric ($|m| < \ell/2$, $60 \pm 5\%$) and non-axisymmetric ($|m| \geq \ell/2$, $40 \pm 5\%$) harmonic components. The distribution of the relative magnetic field energy as a function of ℓ value of harmonic modes is shown in Fig. D.1. We find that the field energy peaks at $\ell = 1$ ($14 \pm 6\%$ of the total energy) and then fluctuates between 3–4% until $\ell = 10$. Then, there is a secondary maximum at $\ell = 12-15$ (energy contributions up to $5.4 \pm 0.7\%$ per ℓ value) corresponding to the small-scale structure seen in the reconstructed magnetic maps. The energy contribution of all modes with $\ell \leq 27$ appears to be non-negligible ($\geq 1 \pm 0.2\%$ of the total magnetic field energy). Given the high $v_e \sin i$ of the star and the resolving power of our spectra, ZDI is potentially sensitive to modes with ℓ up to ≈ 100 (Fares et al. 2012).

6. Discussion

6.1. Pulsations

δ Scuti pulsators are intermediate mass stars located in the lower part of the so-called classical instability strip with spectral types between A2 and F2 (Rodríguez & Breger 2001) that can be in the pre-main sequence, main sequence, or post-main sequence evolutionary stages. δ Scuti stars are typically multi-periodic oscillators that can show very rich pulsation frequency spectra that challenge asteroseismic analyses and the theoretical interpretation of the observed pulsation frequencies.

A- and F-type stars can also show a combination of pressure (p -), gravity (g -), and Rossby (r -) modes (e.g. Uytterhoeven et al. 2011; Saio et al. 2018). Hence, we investigated all available photometric data sets of β Cas for the presence of g - and r -modes in

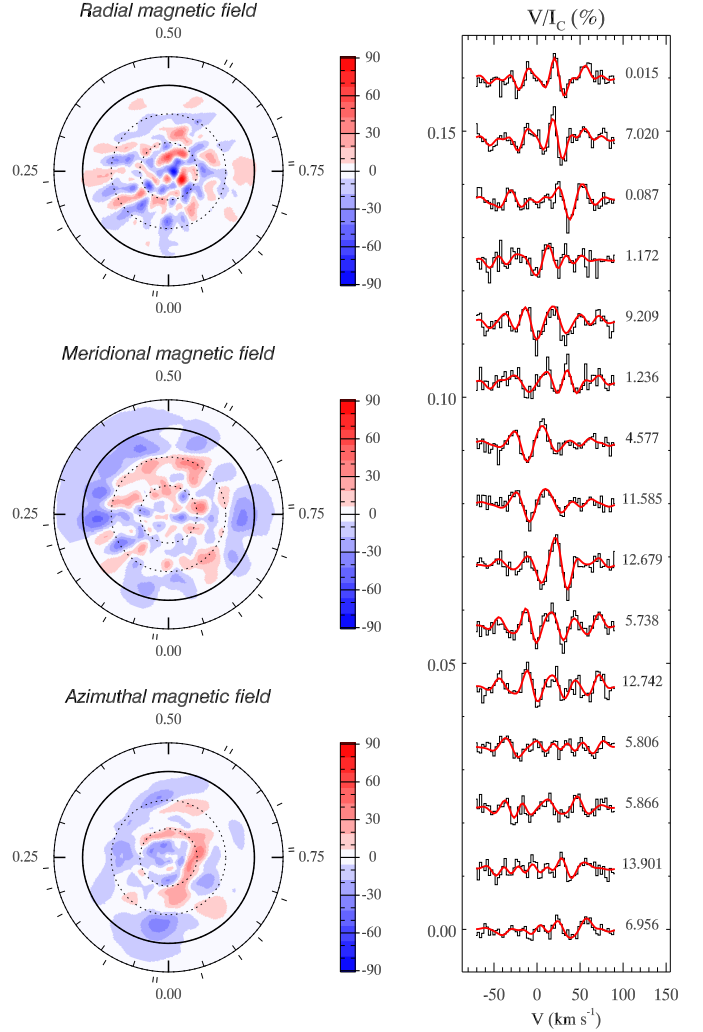


Fig. 10. Magnetic field maps of β Cas and corresponding Stokes V profile fits obtained with ZDI for $P_{\text{rot}} = 0.868$ d. The plots on the left side show the radial, meridional, and azimuthal magnetic field components in the flattened polar projection. The thick circle corresponds to the stellar equator. The numbers next to surface plots correspond to rotational phases while the short bars illustrate rotational phase coverage. The colour bars indicate the field strength in Gauss. The right panel shows the observed (histogram) and model (solid red curves) profiles, shifted vertically with an equidistant step. The rotational phases (calculated relative to $\text{HJD}_0 = 2457358.31370$) are indicated to the right of each line profile.

addition to the already described p -modes. g -modes would be found in the range of ~ 3.3 to 0.3 d^{-1} in frequency (corresponding to ~ 0.3 to 3.0 days in period; Kaye et al. 1999); r -modes appear as a group of peaks below m times the rotational frequency. BRITE-Constellation and SMEI data are known to allow the detection of g -mode pulsations when the standard procedures for data reduction are applied (e.g. Kallinger et al. 2017; Zwintz et al. 2017). The BRITE-Constellation and SMEI data for β Cas do not show any signs for g -mode pulsations. We also checked the TESS data for the potential presence of g -modes before we applied the Gaussian filter to remove the instrumental signal, and also did not find any evidence for them (see Fig. B.1). In all our data sets, we do not detect a frequency that can be attributed to the rotation of β Cas or a group of peaks typical for r -modes.

There are two prominent physical effects that complicate the asteroseismic analysis of δ Scuti stars. One effect is moderate

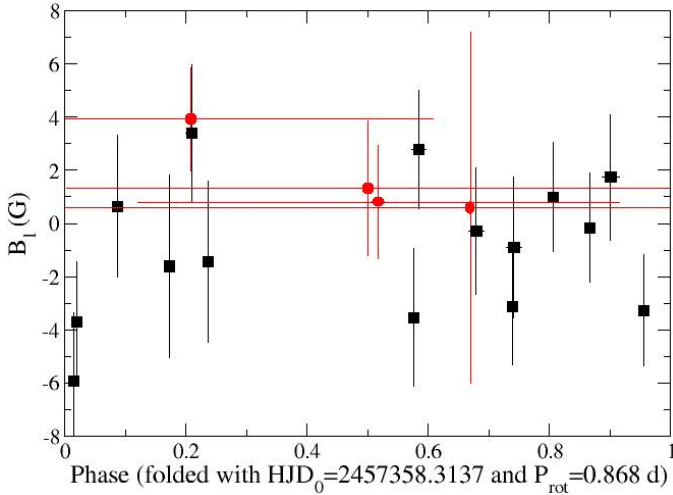


Fig. 11. Longitudinal magnetic field values folded with the rotation period 0.868 d, with phases calculated relative to $HJD_0 = 2457358.3137$ corresponding to the start of the 2015 observations. The red symbols indicate the data obtained in 2013 and 2014, which thus have a much larger phase error compared to the 2015 data set.

to fast rotation, which can cause a splitting of the pulsation modes with the same n and ℓ values but different m values (e.g. Lignières et al. 2006). The second effect is the presence of magnetic fields, which is a rather recent discovery for δ Scuti stars (e.g. Neiner & Lampens 2015; Neiner et al. 2017). In this context, β Cas is a special case because observationally it shows only three independent p -mode pulsation frequencies and not several dozen to hundreds of modes. The reason might be connected to the inclination angle of only 19° (Che et al. 2011) and the presence of the magnetic field. Despite the rather high rotational speed of β Cas, no sign of a rotational splitting can be detected in the present observational material.

We calculated the pulsation constant, Q , based on our values for the three independent frequencies, F_1 , F_2 , and F_4 , and our fundamental parameters, $T_{\text{eff}} = 6920$ K and $\log g = 3.53$ cgs. The pulsation constant Q (Petersen 1976; Stellingwerf 1979) can be expressed as:

$$\log Q = -6.454 + \log P + 0.5 \log g + 0.1 M_{\text{bol}} + \log T_{\text{eff}}, \quad (1)$$

where P is the pulsation period in days and M_{bol} is the bolometric magnitude, which is defined as $M_{\text{bol}} = M_V + \text{BC}$. The absolute magnitude of 1.14 mag is calculated from the distance of 16.8 pc, and the bolometric correction, BC, can be calculated from the relation given by Reed (1998).

$$\text{BC} = -8.499 (\log T_{\text{eff}} - 4)^4 + 13.421 (\log T_{\text{eff}} - 4)^3 - 8.131 (\log T_{\text{eff}} - 4)^2 - 3.901 (\log T_{\text{eff}} - 4) - 0.438. \quad (2)$$

The pulsation constant has a value of 0.033 for fundamental mode pulsation ($n = 0$), 0.025 for the first overtone ($n = 1$), 0.020 for the second overtone ($n = 2$), and 0.017 for the third overtone ($n = 3$).

The corresponding Q values for F_1 at 9.89708 d^{-1} , F_2 at 9.0437 d^{-1} , and F_4 at 8.3847 d^{-1} are 0.018, 0.020, and 0.022, respectively. The calculated Q value for F_4 lies between the first and second overtone pulsation mode; no clear identification of the radial order is therefore possible. F_2 can be identified as second overtone, and F_1 possibly as third overtone pulsation. The latter is in contradiction with earlier reports in the literature that identified F_1 as a first overtone pulsation mode (Rodríguez et al.

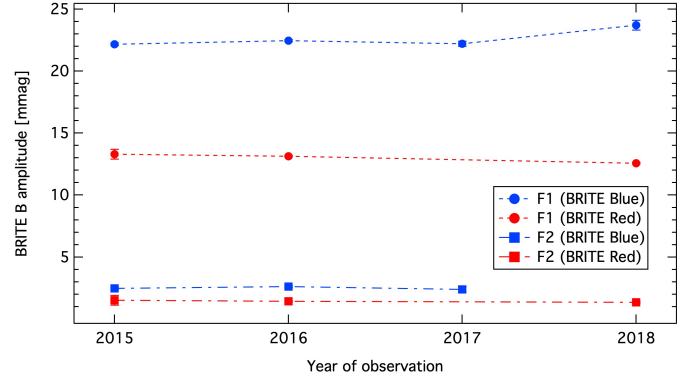


Fig. 12. Annual behaviour of the amplitudes of the two main pulsation frequencies, F_1 (filled circles), and F_2 (filled squares) based on the BRITE-Constellation observations in the B (blue) and R (red) filter conducted every year from 2015 to early 2019. The one-sigma error bars in the figure are mostly smaller than the symbol size.

1992). Together with the results from our Stokes I LSD profile analysis (see Sect. 5.3), F_1 would then be a possible $n = 3$, $\ell = 2$, and $m = 0$ p -mode.

6.2. Amplitude variability

We have used data for β Cas obtained in four specific passbands: the BRITE blue filter (390–460 nm), the BRITE red filter (550–750 nm), the passband of SMEI (450–950 nm), and the passband of TESS (600–1000 nm). For each of the two pulsation frequencies that appear in data from all instruments, it is evident that the by far highest amplitude can be measured from the BRITE blue filter data, followed by the BRITE red amplitude and the amplitude in the SMEI passband. The pulsation amplitudes are smallest in the reddest passband – that of the TESS camera.

It has been reported several times in the past that some of the pulsation amplitudes in δ Scuti stars show time-dependent behaviour (e.g. Breger et al. 1991; Breger & Bischof 2002; Zwintz et al. 2019). The origin of amplitude variability can be either intrinsic due to beating of unresolved frequencies, non-linearity, or mode-coupling, or extrinsic due to binary and multiple systems. A detailed overview of the amplitude modulation in δ Scuti stars is given by Bowman et al. (2016).

We examined the amplitude variability of β Cas by first studying the annual behaviour in the BRITE red and blue filters based on the four years of consecutive observations (see Table 1). It can clearly be seen from Fig. 12 that there is no significant modulation of the amplitudes of F_1 and F_2 in both BRITE filters.

In a second step, we used the longest and best BRITE-Constellation data obtained in single observing seasons to study the behaviour of the pulsation amplitudes on the shorter time scale of a few months. The first season of BRITE observations of β Cas in 2015 yielded too short time bases (i.e. ~ 58 days) for such an analysis. The BAb data obtained in 2017 and in 2018 have insufficient quality for such an analysis. Therefore, we restrained the analysis of shorter period amplitude variability on the BAb and UBr data obtained in 2016 and the BTr data from 2018. For each of the three data sets, we calculated 30-day subsets with 20-day overlaps, and find only very moderate modulations of the pulsation amplitudes of F_1 and F_2 within one-sigma errors (see Fig. 13).

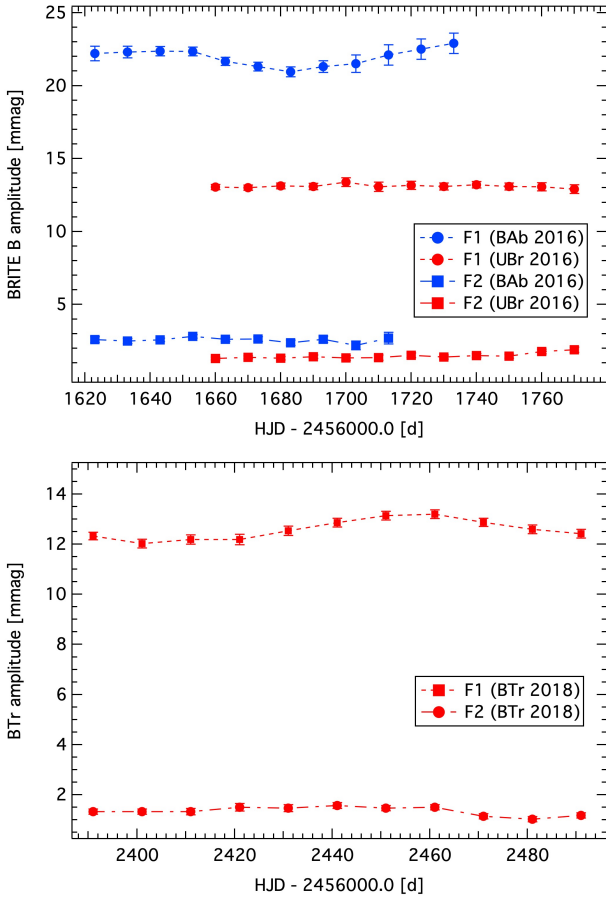


Fig. 13. Seasonal amplitude behaviour of the two main pulsation frequencies, F_1 (filled circles) and F_2 (filled squares). *Top panel:* 30-day subsets with 20-day overlaps for the BAb 2016 (blue) and UBr 2016 (red) data (*top panel*); *bottom panel:* 30-day subsets with 20-day overlaps for the BTr 2018 data (red). The one-sigma error bars in the figure are often smaller than the symbol size.

As a final check, we used the TESS data set, which is considerably shorter in time base, but has significantly less noise compared to the BRITE observations. Consequently, we split the light curve in the four blocks that are introduced by the visible gaps (see the top panel of Fig. 2). The blocks contain 8.24 d, 10.0, 9.9 d, and 10.5 d of uninterrupted data with nearly 100% of duty cycle. For each of the blocks, we determined the corresponding amplitudes of F_1 and F_2 . The third independent pulsation frequency, F_4 , has such a low amplitude that it does not appear in the frequency spectra of separate subsets. Hence, we had to discard it from our study of the pulsation amplitude behaviour. Figure 14 again illustrates that the amplitudes of F_1 and F_2 do not vary much during the 49.686 days of TESS observations even within one-sigma errors. We conclude that no statistically significant variability of the pulsation amplitudes of F_1 , F_2 , and F_4 can be detected.

6.3. Non-binarity of β Cas

In the past, it was speculated several times that β Cas is actually a binary system. Although a detailed analysis by Abt (1965) illustrated the non-detection of a secondary component around β Cas, a recent study by Liakos & Niarchos (2017) again lists the star as a possible binary. Therefore, we applied the time delay method (Murphy & Shibahashi 2015) to our nearly four-years long pho-

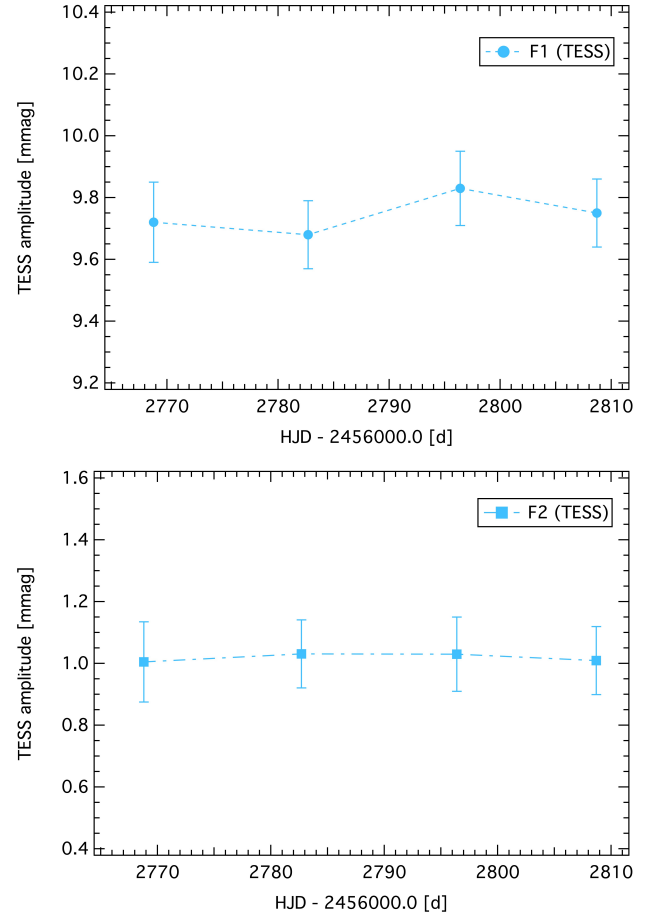


Fig. 14. Amplitude behaviour of the two main pulsation frequencies, F_1 (filled circles, *top panel*) and F_2 (filled squares, *bottom panel*), based on four subsets of TESS data. The error bars display the one-sigma error derived using SMURFS.

tometric time series to check independently if a secondary can be detected.

The orbital movement of two components in a binary system introduces changes in the pulsation signal of δ Scuti pulsators throughout the orbit (Shibahashi & Kurtz 2012). This results in frequency modulation, where the amplitude spectrum shows additional peaks near the intrinsic pulsation frequencies and phase modulation, where the intrinsic pulsation signal arrives earlier (or later) depending on the orbital phase. This phase modulation is equivalent to the concept of light arrival time delays meaning the pulsation signal arrives later if the star is further away and vice versa. These time delays depend on the orbital parameters and it is therefore possible to constrain the orbit if time delays can be measured from the light curve (Murphy & Shibahashi 2015).

We used maelstrom (Hey et al. 2020) to investigate our data sets for any time delay signal. Neither data set shows significant time delays. We therefore exclude a binary signal with $a \sin(i)/c \gtrsim 5$ s (see Fig. 8 of Hey et al. 2020) and periods < 1000 days.

6.4. Evolutionary stage

Using the T_{eff} and $\log g$ values determined from our analysis and the errors taken from the second approach described in Sect. 4 (i.e. the err_2 values in Table 4), the position of β Cas in the Kiel

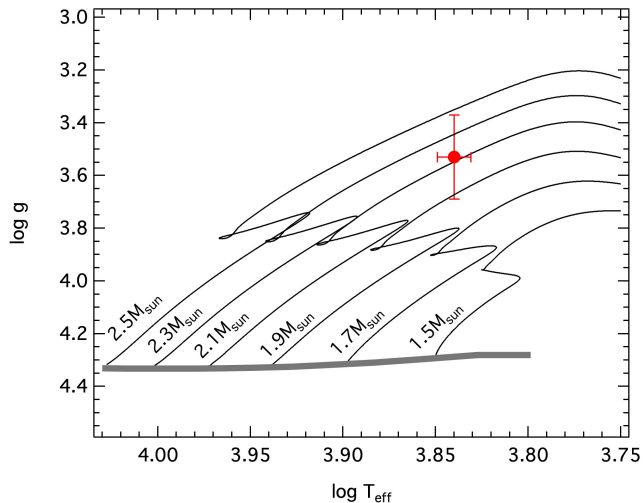


Fig. 15. Position of β Cas in the Kiel diagram based on our final adopted values for T_{eff} and $\log g$ (red square). Post-main sequence tracks have been calculated using MESA version r-12115 (Paxton et al. 2011, 2013, 2015, 2018, 2019). The location of the zero-age main sequence (ZAMS) is given as a thick grey line.

diagram is shown in Fig. 15. From our analysis we can confirm that the mass of β Cas is around $2.1 M_{\odot}$ and that it has to be a rather evolved star moving away from the TAMS.

6.5. Structure of the magnetic field

Following the detection of a complex magnetic field on the surface of β Cas, we attempted to reconstruct the stellar field topology with the ZDI technique. The subset of 15 Stokes V averaged LSD profiles suitable for this analysis extends over about two weeks, corresponding to approximately 14 stellar rotations. These data alone are insufficient for an unambiguous determination of the rotational period and are not suitable for a refined investigation of, for example, latitudinal differential rotation, temporal field evolution, or variation of the field structure with pulsational phase. Nevertheless, we found a plausible rotational period, compatible with the period range suggested by the previous interferometric analysis, which phases the Stokes V profiles convincingly. Using this period we have successfully reproduced the circular polarisation observations with a fairly complex, yet static, magnetic field topology. The longitudinal field values follow a non-sinusoidal behaviour, unlike dipolar fossil fields. Further high-cadence spectropolarimetric observations are required for probing the temporal evolution of this field and exploring its response to the global δ Scuti pulsations.

Finding such a complex surface magnetic field structure in a star with an effective temperature as high as 6920 K is very unusual. It is known that fossil magnetic fields exist in stars as cool as $T_{\text{eff}} \approx 6500$ K (Kochukhov 2003; Shulyak et al. 2010). On the other hand the hottest stars with dynamo magnetic fields are previously found with a temperature up to $T_{\text{eff}} \approx 6700$ K (Marsden et al. 2014; Seach et al. 2020). Judging by its complexity, the field of β Cas is almost certainly of dynamo origin. It is significantly more complex than any fossil fields of magnetic A, B, and O stars. Instead, its structure resembles the surface magnetic field topologies of well-studied cool, young, active stars such as AB Dor (Donati et al. 1999), V410 Tau (Kochukhov 2015), and Tap 26 (Yu et al. 2017). Thus, our study establishes that the dynamo fields can exist in stars with T_{eff} of up to ≈ 6900 K. It is possible that the rapid rotation of β Cas, by

increasing the thickness of the surface convection layer at the equator, facilitates the dynamo action, allowing it to exist to a higher T_{eff} than in slowly rotating stars.

Finally, about $\sim 10\%$ of O, B, and A stars host a fossil field on the main sequence with a typical dipolar field strength of 3 kG. The strength of these fields at the stellar surface has been shown to decrease with time due to magnetic flux conservation as the stellar radius increases (Kochukhov & Bagnulo 2006; Landstreet et al. 2007; Shultz et al. 2019), and probably decrease further due to, for example, Ohmic decay. Since β Cas is evolved, we cannot exclude that it hosts such a fossil field that has reached a faint strength at the surface and is interacting with the dynamo field in the surface layer. Therefore, β Cas is possibly also an interesting target for the study of the evolution of fossil fields and for the interaction between fossil and dynamo fields.

7. Conclusions

For several reasons, β Cas is an unusual star that combines several physical properties:

- (i) It is a δ Scuti pulsator that shows only three independent p -mode pulsation frequencies even in multiple seasons of space photometry down to the few ppm-level. We suggest that its highest amplitude mode, F_1 , can be identified as an $n = 3$, $\ell = 2$, $m = 0$ mode based on the pulsation constant and the ZDI analysis. No g -mode frequencies were detected.
 - (ii) It is one of the handful of δ Scuti stars known to date to show a measurable magnetic field.
 - (iii) Additionally, the magnetic field structure of β Cas is quite complex, which is unusual in a star with an effective temperature as high as 6920 K. According to its complexity, the field of β Cas is almost certainly of dynamo origin, which makes it the first δ Scuti object with a dynamo magnetic field. The rapid rotation of β Cas may lead to a thicker surface convective layer and explain how a dynamo can exist.
- Therefore, β Cas provides an interesting benchmark for the theoretical modelling of dynamo processes in thin convective envelopes of F-type stars and for the study of the transition region between fossil and dynamo fields.

Acknowledgements. KZ acknowledges support by the Austrian Fonds zur Förderung der wissenschaftlichen Forschung (FWF, project V431-NBL) and the Austrian Space Application Programme (ASAP) of the Austrian Research Promotion Agency (FFG). CN acknowledges support from PNPS (Programme National de Physique Stellaire). OK acknowledges research funding from the Swedish Research Council, the Swedish National Space Board, and the Knut and Alice Wallenberg foundation. This research has made use of the SIMBAD database operated at CDS, Strasbourg (France), of NASA's Astrophysics Data System (ADS), and of the VALD database, operated at Uppsala University, the Institute of Astronomy RAS in Moscow, and the University of Vienna. The research of A.F.J.M. has been supported by the Natural Sciences and Engineering Research Council (NSERC) of Canada. Adam Popowicz was responsible for image processing and automation of photometric routines for the data registered by BRITENANOSAT constellation, and was supported by Silesian University of Technology Rector Grant 02/140/RGJ20/0001. GAW acknowledges Discovery Grant Support from the National Science and Engineering Research Council (NSERC) of Canada.

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Appendix A: Additional BRITE and SMEI light curves

The data obtained by BAb and BLb as well as the data obtained by BHr and BTr in 2015 were combined to one blue filter and one red filter light curve. Their properties are described in Table 1.

As can be seen in panels a and b of Fig. A.1, observations of BAb and BLb were conducted simultaneously, while BHr and BTr observed β Cas at distinct times. Figure A.1 also shows the BAb observations in 2017 (panel c) and the BTr and BAb observations in 2018 (panels d and e). Figure A.2 shows the full light curve obtained by SMEI.

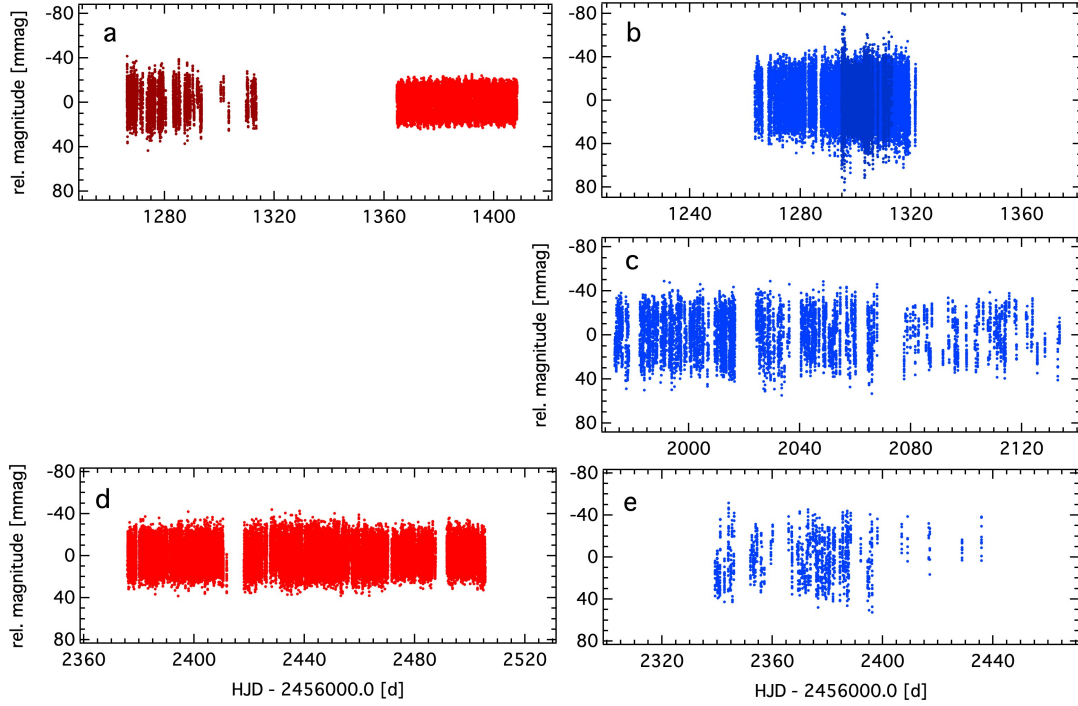


Fig. A.1. BRITE photometric time series obtained by BTr (brighter red in panel a), BHr (darker red in panel a), BAb (brighter blue in panel b), and BLb (darker blue in panel b) in 2015, by BAb in 2017 (panel c), by BTr (panel d) and BAb (panel e) in 2018.

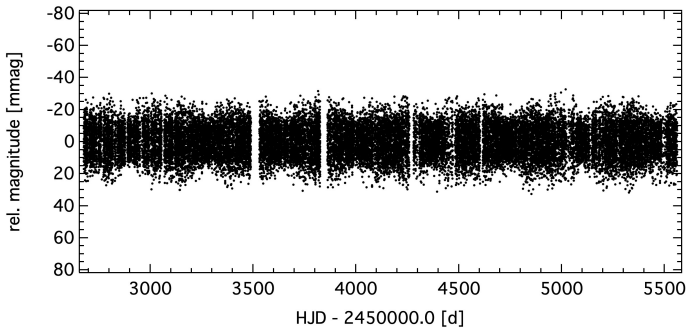


Fig. A.2. SMEI photometric time series.

Appendix B: Amplitude spectra and spectral windows

Below we provide additional figures illustrating the frequency analyses of the TESS and BRITE-Constellation 2015, 2017, and 2018 data as well as the spectral window functions for all data sets used in our analysis. Figure B.1 shows a zoom into the low-frequency domain of the amplitude spectrum of the original TESS data: The rotation frequency at 1.12 d^{-1} cannot be identified, there is increased noise in the region between 0.0 and 0.5 d^{-1} , and no evidence for significant g -mode frequencies.

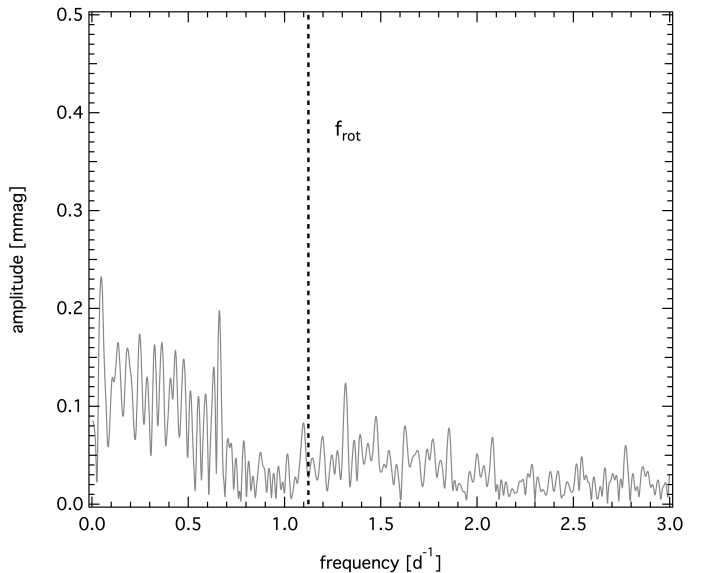


Fig. B.1. Zoom into the low-frequency domain of the amplitude spectrum of the original TESS data before application of a Gaussian filter. The position of the rotation frequency as determined by Che et al. (2011) is indicated with a dashed line.

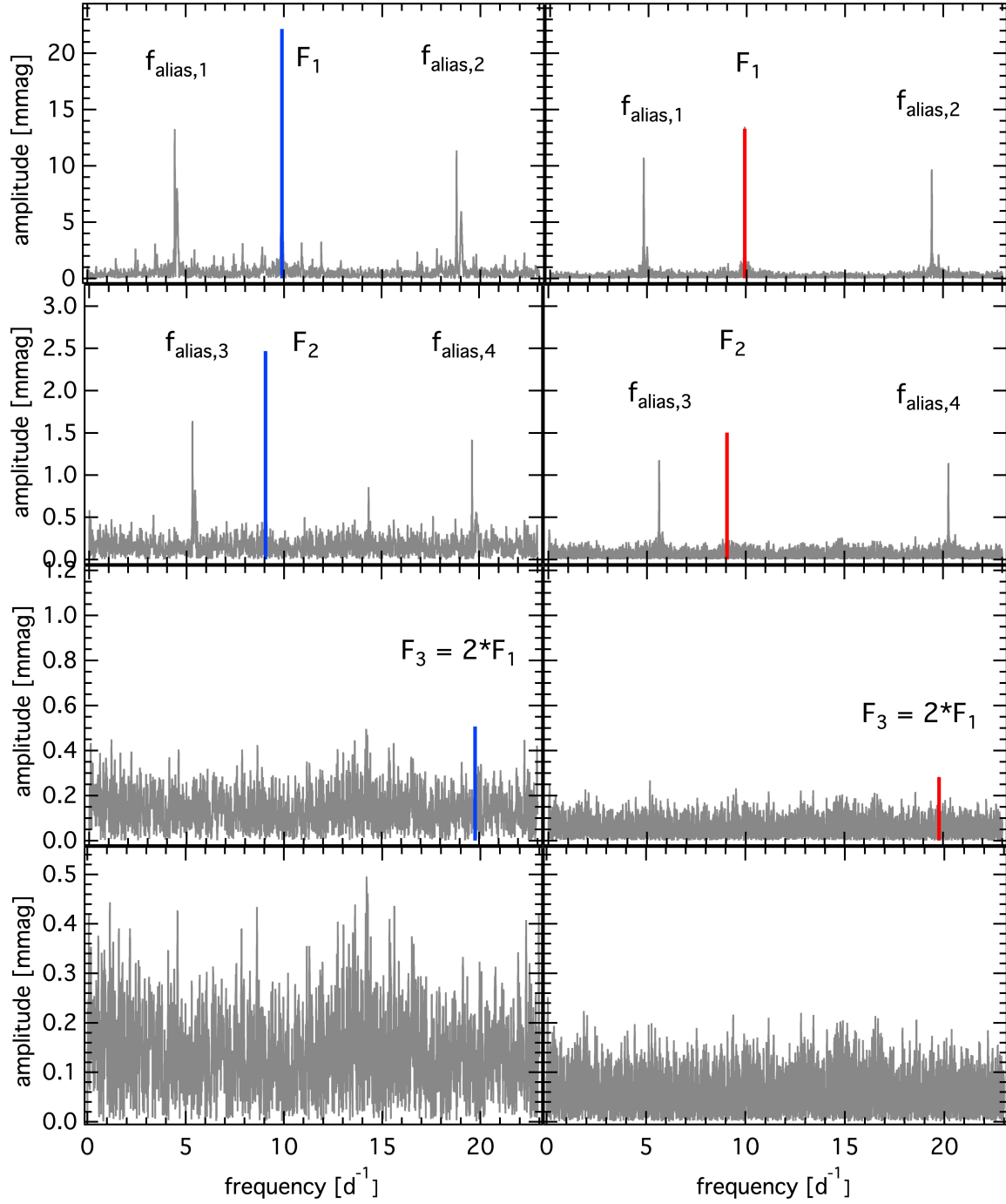


Fig. B.2. Amplitude spectra of the BRITE-Constellation data obtained in 2015: combined blue filter data are shown on the *left side*, combined red filter data on the *right side*. *Top panels*: amplitude spectra of the original data with F_1 identified, *second panels*: amplitude spectra after pre-whitening F_1 , *third panels*: those after pre-whitening F_1 and F_2 , and *bottom panel*: residual amplitude spectra after pre-whitening all significant frequencies. An explanation for the identified alias frequencies is given in the text.

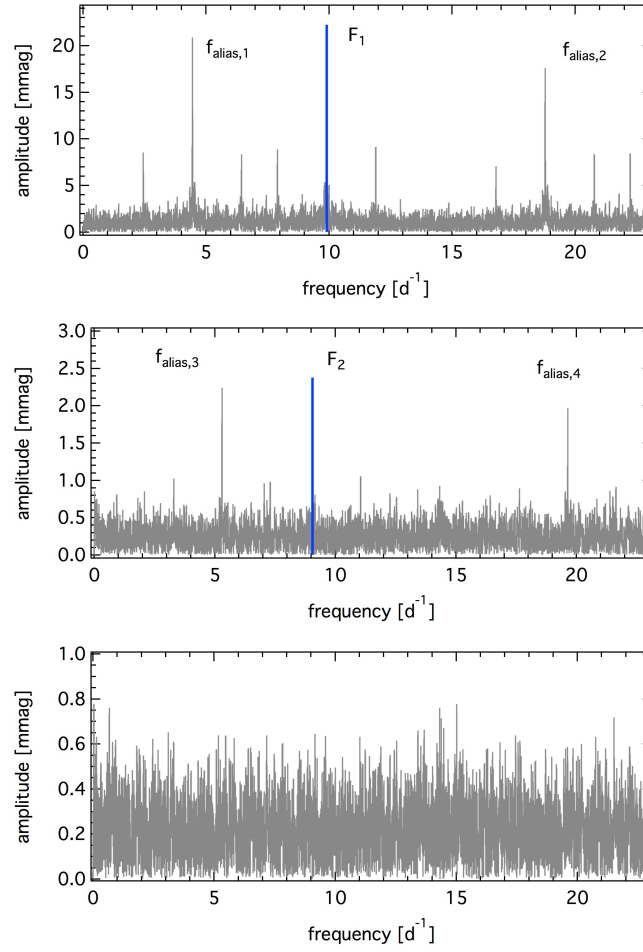


Fig. B.3. Amplitude spectra of the BRITE-Constellation data obtained in 2017 with BAb only: *Top panel:* amplitude spectrum of the original data with F_1 identified, *middle panel:* amplitude spectrum after pre-whitening F_1 , and *bottom panel:* residuals after pre-whitening with the significant frequencies. We note that the noise of the 2017 BAb data is significantly higher than for all the other combined data sets, hence F_3 remains hidden in the noise.

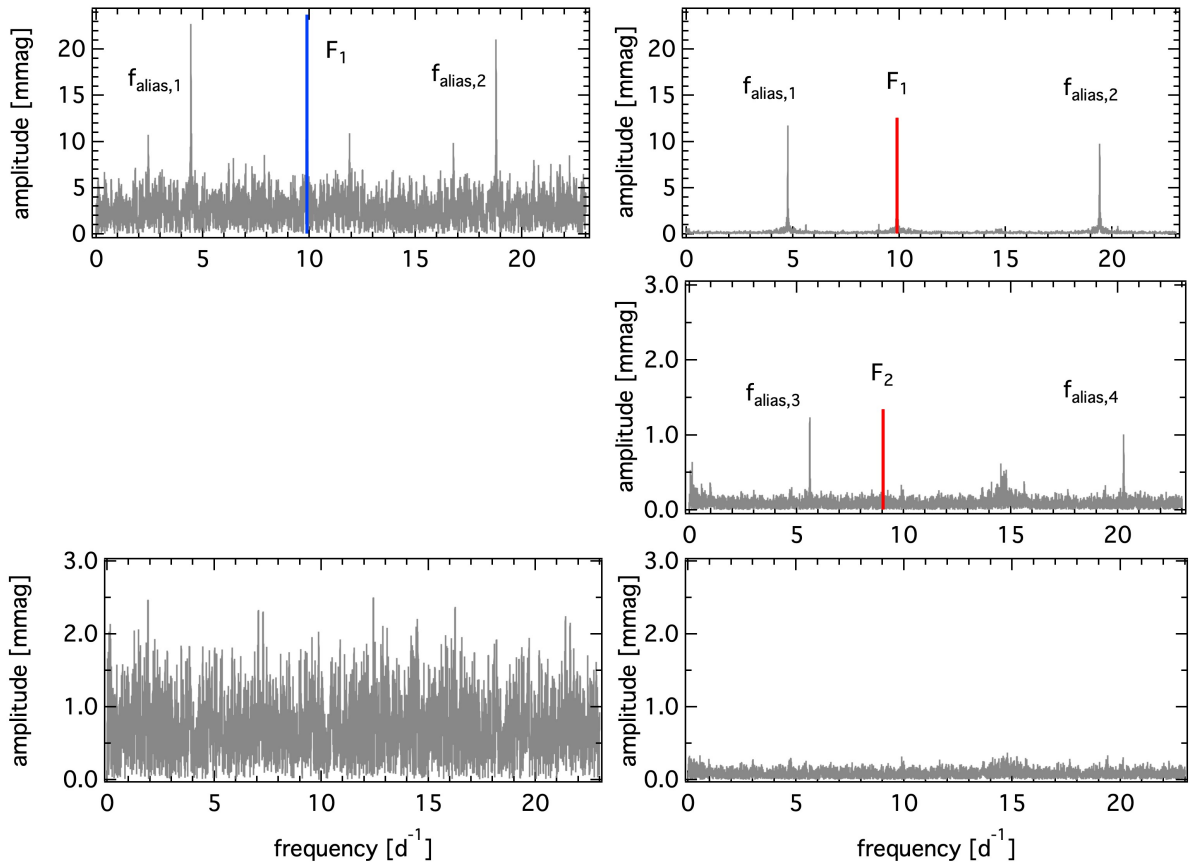


Fig. B.4. Amplitude spectra of the BRITE-Constellation data obtained in 2018: BAb data are shown on the *left side*, BTr data on the *right side*. *Top panels*: amplitude spectra of the original data with F_1 identified, *middle panel* (BTr only): amplitude spectra after pre-whitening F_1 , and *bottom panels*: residuals after pre-whitening all respective significant frequencies. An explanation for the identified alias frequencies is given in the text.

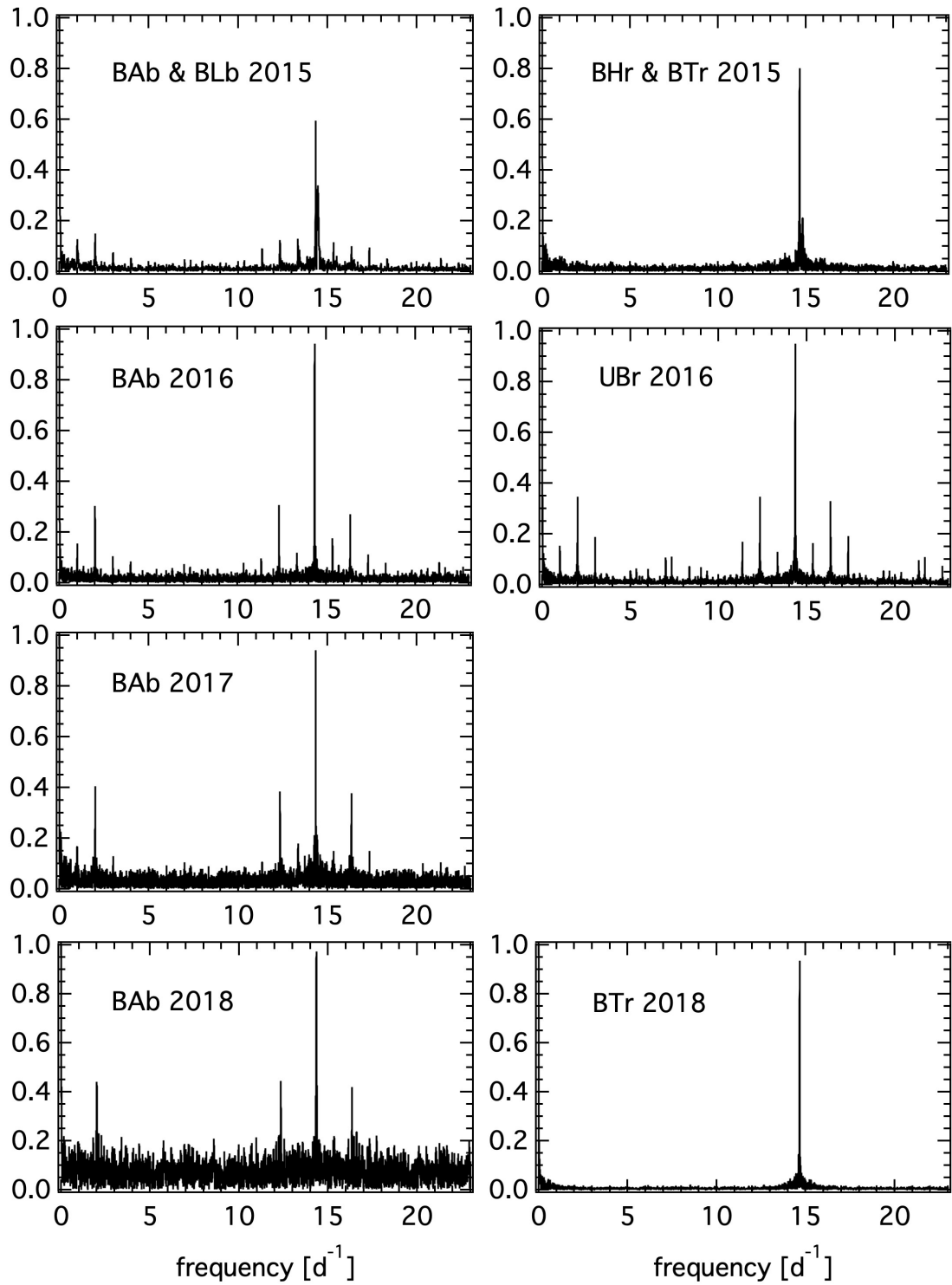


Fig. B.5. Spectral window functions for the BRITE-Constellation data obtained in 2015, 2016, 2017, and 2018 in the blue (*left panels*) and the red filter (*right panels*).

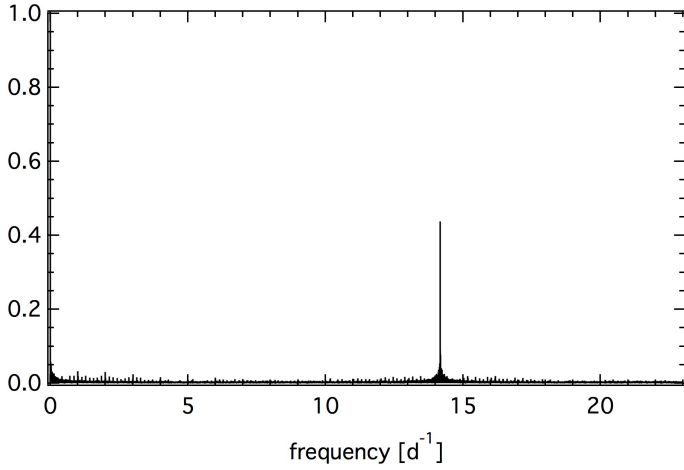


Fig. B.6. Spectral window function for the SMEI data.

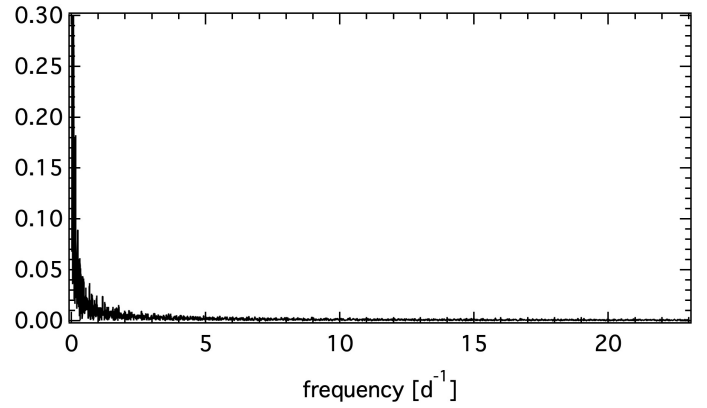


Fig. B.7. Spectral window function for the TESS data. We note the different Y-axis scale compared to the spectral window functions of the BRITE and SMEI data.

Appendix C: LSD profiles

Here we illustrate all LSD Stokes I , V , and null profiles of β Cas derived from the Narval observations obtained in 2013, 2014, and 2015.

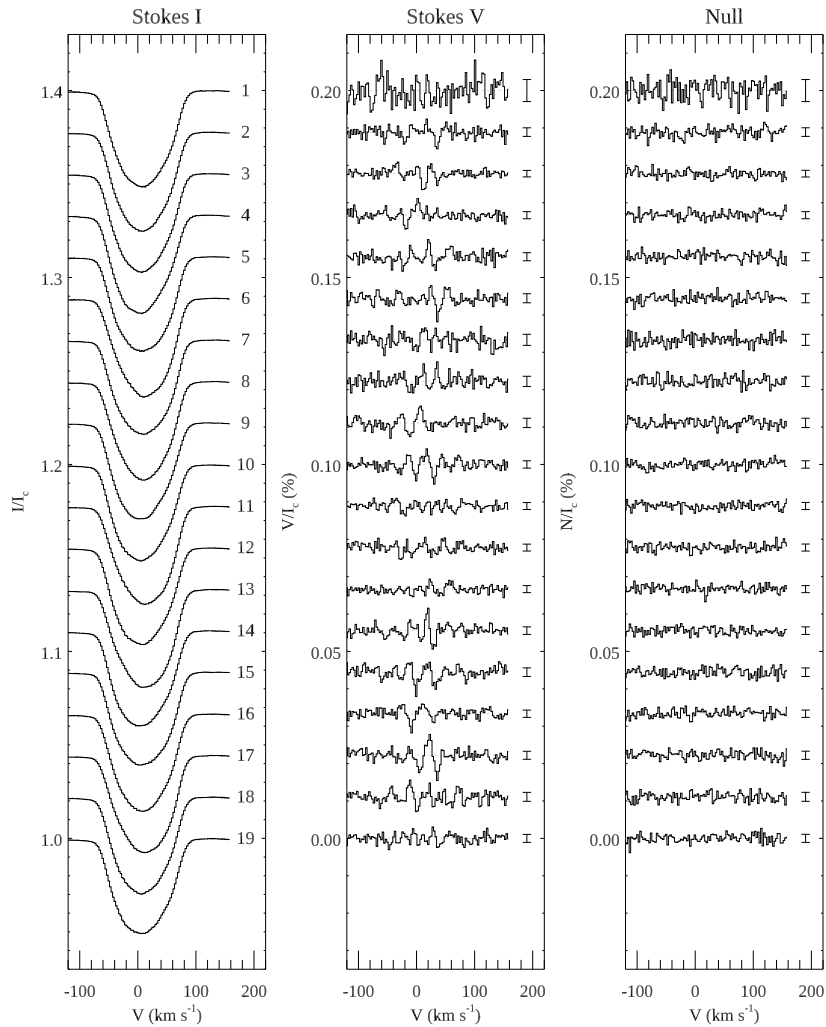


Fig. C.1. Observed LSD Stokes I (left), V (middle), and null (right) profiles of β Cas. Spectra are shifted vertically according to the observing date, from the earliest on top to the latest at the bottom. The numbering of profiles in the Stokes I panel corresponds to the polarimetric measurement number given in Table 2.

Appendix D: Distribution of magnetic energy over spherical harmonic modes

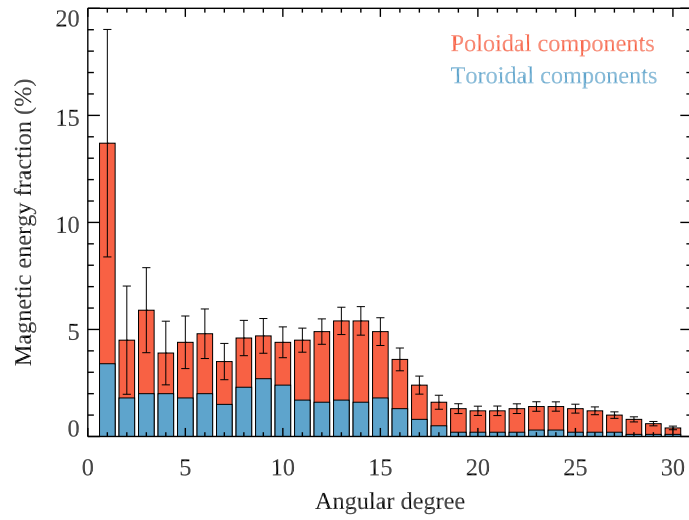


Fig. D.1. Magnetic field energy as a function of angular degree ℓ of the spherical harmonic expansion for the magnetic field topology recovered with ZDI. Different colours show contributions of the poloidal and toroidal components. Error bars correspond to the uncertainties estimated as described in Sect. 5.3.