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Influence of the variability of soil profile properties on weak and strong seismic response 1 2 Stefania Gobbi^{a,*}, Luca Lenti^{a,d}, Maria Paola Santisi d'Avila^b, Jean-François Semblat^c, 3 Philippe Reiffsteck^a 4 5 ^a Université Gustave Eiffel, IFSTTAR (GERS/SRO), Marne la Vallée, France 6 ^b Polytech'Lab, EA UNS 7498, Université Côte d'Azur, Sophia Antipolis, France 7 ^c IMSIA (UMR9219), CNRS, EDF, CEA, ENSTA Paris, Institut Polytechnique de Paris, 8 9 France ^c Cerema, Equipe-Projet MOUVGS, Sophia Antipolis, France 10 11 12 Corresponding author: 13 Stefania Gobbi 14 Université Gustave Eiffel, IFSTTAR (GERS/SRO) 15 14-20 Boulevard Newton - 77420 Champs sur Marne - France 16 17 Email: stefania.gobbi@ifsttar.fr 18

ABSTRACT

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20 Characterizing the potential effect of local site conditions on the amplification of ground motions is a critical aspect of seismic hazard and risk assessment. The aim of this study is to 21 investigate the reliability and the limit of using the average shear wave velocity in the upper 22 30m of the soil profile $v_{s,30}$, as single proxy, to characterize seismic site effects for weak and 23 strong events. 24 To this regard, a dataset of 300 one-dimensional soil profiles with a given $v_{s,30}$ are generated 25 through a Monte Carlo approach. Their seismic responses are computed for a set of 40 real 26 accelerograms, with different seismic features. The vertical propagation from the bottom of 27 the generated columns is modeled using a finite element spatial discretization, accounting for 28 29 both linear and nonlinear soil behavior. The site dominant frequency f_0 and the shear wave velocity gradient in the profile B_{30} are 30 proposed as proxies to characterize seismic site effects and the variability of the response 31 spectra for the numerical signals, at the free surface of the set of columns, is discussed. 32 Correlations between site-specific amplification factors deduced using the numerical response 33 spectra and the proposed site proxies are analyzed for different sub-ranges of periods. The 34 obtained amplification factors are then compared to those proposed by different international 35 and national design codes. 36 37 The results, obtained under assumption of linear and nonlinear behavior of soil, emphasize the need to introduce complementary site parameters proxies, in addition to $v_{s,30}$, to characterize 38 39 the expected site effects in design response spectra.

- 41 **Keywords:** Geotechnical properties, site effects, variability, average shear wave velocity,
- 42 impedance contrast, response spectrum, Eurocode 8.

1. Introduction

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Recent and past earthquakes, such as 1985 Mexico City, 1989 Loma Prieta, 45 Northridge, 1995 Kobe events, among others, underline the need to characterize the effect 46 of the local soil conditions on seismic site response prediction. It has been widely recognized 47 that the seismic site effects are generally related to the stratigraphy, the surface topography, 48 49 the impedance contrast and the rheology of the soils involved during the propagation of 50 seismic waves [1]. Current seismic design codes consider the seismic site effects through a ground type 51 classification solely based on the average shear velocity in the upper 30m of the soil profile 52 $v_{s,30}$ proposed by Borcherdt [2], neglecting the depth of the bedrock and the property of the 53 soil below 30m. Nevertheless, it has been recognized that $v_{s,30}$ is a useful parameter to capture 54 55 some features of the local site amplification effects [3–7]. However, several researches [8–15] show that $v_{s,30}$ cannot be used as the single-site proxy to 56 discriminate soils in terms of seismic amplification over the whole frequency range of 57 interest. To this regard, Steidl [16] and Park and Hashash [8] recommended the introduction 58 of a depth-to-bedrock parameter since they found that the previsions based on $v_{s,30}$ are over 59 and under conservative for deep sediments at short and long periods, respectively. Many 60 alternatives to $v_{s,30}$ are proposed to improve site soil characterization accounting for 61 additional information on the shear wave velocity profile with depth, the site dominant 62 63 frequency f_0 , the impedance contrast between sediments and bedrock and the depth to the bedrock. 64 65 Various studies [11,12,17–21] propose new site classification based on a combination of these different proxies. Gallipoli and Mucciarelli [21] and Cadet et al. [11] propose a two-66 parameters site classification approach through the dominant frequency f_0 and the average 67

shear wave velocity $v_s(\overline{z})$ in the shallow soil up to the reference depth \overline{z} . Kotha et al. [17]

introduce a new approach classification characterized by the kernel density distributions of

 $v_{s,30}$, $v_{s,10}$, H_{800} and the predominant period.

Recently, several researchers explore the performance of different site proxies in order to reduce the aleatory variability on the seismic prediction. Derras et al. [14] investigate the performance of four site condition proxies, $v_{s,30}$, f_0 , the topographical slope and the depth H_{800} (the depth where the shear wave velocity v_s reaches $800\,\mathrm{m/s}$) using a neural networks approach, in order to assess their benefits to reduce the uncertainty of the site response. They conclude that the best single-proxy is $v_{s,30}$ for periods below 0.6 s and f_0 or H_{800} at longer periods and that the best pair is $(v_{s,30}, H_{800})$ at short periods and (f_0, H_{800}) at long periods. Stambouli et al. [22] conduct a numerical investigation on 858 soil columns corresponding to

real sites profiles from Japan, USA, and Europe. They show that the best performing site proxy is the impedance contrast between bedrock velocity and minimum surface velocity but even the pair $(v_{s,30}, f_0)$ can reduce significantly the variability of the site response at least around 60%.

Lately, Chuanbin et al. [23] study the best performing site proxies for the linear characterization of the site response using 1840 ground-motion recordings from a KiK-net database. They focus their study on the dominant period of the site T_0 , the site depths $Z_{0.8}$ and $Z_{1.0}$, which are measured site depths to layers having shear-wave velocity 0.8 and 1.0 km/s, respectively. They demonstrate that predictions based on the configuration using T_0 as the primary and $v_{s,30}$ as the secondary proxy can induce a significant reduction in site-to-site amplification variability.

Ciancimino et al. [24] adopt some classical proxies for site characterization in the context of

seismic site effect estimation. Their reliability is evaluated, under the assumption of linear 91 92 regime, and compared to the ground type classification adopted in the Eurocode 8 [25], New Zealand Standard [26] and that suggested by Pitilakis et al. [18]. 93 Following these recent reviews, the prediction of the seismic site response using only a single 94 proxy over the whole period range does not seem satisfactory. Hence, to improve the site 95 amplification estimation, it is advisable to use a combination of site proxies rather than a 96 single site proxy. Based on this idea, the goal of the present research is to assess the 97 correlation with the site amplification of some site parameters used to characterize the site 98 condition, with the aim of improving the expected ground motion prediction. 99 In this research, the site dominant frequency f_0 and the shear wave velocity gradient B_{30} are 100 selected as complementary proxies, in addition to $v_{s,30}$, and applied to a wide variety of soil 101 profiles with given $v_{s,30}$ and H_{800} . The two proposed proxies has been selected because they 102 can be estimated, without excessive cost, by geophysical methods applied to ambient 103 vibrations or seismic motions, recorded using temporary instruments located at the soil 104 surface [27]. 105 106 Then, since the nonlinear behavior of soils has been recognized as an important factor in site 107 response [28,29], the second aim of this work is to explore how these site parameter proxies

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2. Methodology

The stratigraphy of a set of soil profiles with a given average shear wave velocity in the upper $30 \,\mathrm{m} \, v_{s,30}$ is randomly generated, according to the Monte Carlo method. Consequently, all the generated profiles belong to the same ground type in the Eurocode classification [25]. The seismic wavefield along these soil profiles has been computed using the finite element

allow to capture and account for the nonlinear component of site response.

method (FEM) for spatial discretization and the Newmark algorithm for time discretization,

implemented in the SWAP_3C FEM package [30,31]. The highest-amplitude horizontal component of a wide variety of recorded earthquakes, representative of regions of low to moderate intensity, is applied as input motion at the base of each soil profile. These recorded signals are propagated along each soil profile and the ground response at the surface is evaluated in both cases of linear and nonlinear soil behavior.

Results are presented with regard to the amplification factors adopted by Ciancimino et al. [24], in different period ranges, in order to distinguish short-, mid- and long-period amplification factors. Differences between the response spectra of numerical signals at the soil surface and the reference spectrum proposed by European buildings codes [25] are then

quantified and discussed.

2.1 Set of generated soil profiles for the statistical analysis

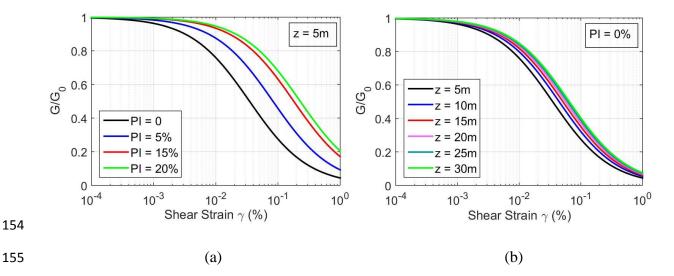
The parameters chosen for the set of soil profiles are the average shear wave velocity $v_{s,30} = 270 \,\mathrm{m/s}$, corresponding to the ground type C according to the Eurocode 8 [25], the soil depth of $30\,m$, the number of layers equal to 4 and the density $\rho\!=\!1850\,kg/m^3$. The geotechnical properties assumed for the bedrock are the density $\rho_b = 2200 \,\mathrm{kg/m^3}$ and the shear wave velocity $v_{sb} = 1000 \,\mathrm{m/s}$. The properties of each layer are generated considering each stochastic parameter uniformly distributed in a given range. The soil layer thickness ranges in [1-15m], the shear wave velocity in [100-800 m/s] and 4 soil types can be randomly targeted. Each soil type from 1 to 4 is associated to a plasticity index PI = 0,5,10 and 20%, respectively. Yokota et al. [32] have shown that normalized shear modulus reduction curve for different types of soils can be expressed by a set of formulas in the absence of available

test data. To this regard, a normalized shear modulus reduction curve, as a function of the

shear strain γ , is derived using the four-parameter model proposed by Darendeli [33] to characterize normalized modulus reduction formulation:

$$G(\gamma)/G_0 = 1/\left[1 + (\gamma/\gamma_r)^{\alpha}\right]$$
 (1)

assuming a normal consolidated soil (over-consolidation ratio OCR = 1). The reference shear strain is defined as $\gamma_r = \left(\phi_1 + \phi_2 \, PI \cdot OCR^{\phi_3}\right) \sigma_{v0}^{r\phi_4}$, where from ϕ_1 to ϕ_4 are parameters that relate the normalized modulus reduction curve to soil type and loading conditions estimated on the basis of statistical analysis ($\phi_1 = 0.0352$, $\phi_2 = 0.001$, $\phi_3 = 0.3246$, $\phi_4 = 0.3483$) and $\alpha = 0.92$. The vertical effective stress σ_{v0}' is calculated each 5m using the chosen soil density $\rho = 1850 \, \text{kg/m}^3$, to account for the variation of the shear modulus decay curve with depth. The normalized shear modulus reduction curves employed for the four soil types, associated to a different plasticity index PI are shown in Fig. 1 (a), for a fixed depth $z = 5 \, \text{m}$. The curves $G(\gamma)/G_0$ at various depths, associated to a related vertical effective stress σ_{v0}' , for the soil



type 1 having plasticity index PI = 0, are shown in Fig. 1 (b).

Fig. 1. Normalized shear modulus reduction curves obtained by Darendeli formulation [33] (a) for the four soil types associated to different plasticity index PI and a given depth $z = 5 \,\mathrm{m}$,

(b) and for increasing depth z and a given plasticity index PI = 0.

A set of 300 soil profiles is randomly generated with different layer thicknesses and impedance contrasts, in order to represent various site conditions and estimate the influence of their uncertainty on the amplification process. Among these 300 soil profiles, for 200 of them, the shear wave velocity profile increases with depth to consider the effect of increasing confining stresses. In the other 100 soil profiles, there is an inversion of the shear wave velocity profile in one of the middle layers. The position and the thickness of the layer with the shear wave velocity inversion are selected randomly. The generated shear wave velocity profiles with depth $v_s(z)$ are shown in Fig. 2, in the cases of increasing v_s and of inversions in the profile (a and b, respectively). It can be noted that the variability in the shear wave velocity profile, according to the same $v_{s,30} = 270 \,\text{m/s}$, can be very large.

2.2 Set of recorded seismic motions

A set of 40 signals, recorded at rock outcrops, is selected as input for the computation of the seismic wave propagation along the 300 generated soil profiles. These seismic motions originate from ITACA, the Italian Strong Motion Database [34], ISESD, European Strong Motion Database [35] or PEER, Pacific Earthquake Engineering Research Center Database [36].

[36]. In the adopted set of seismic signals, 20 of them are representative of low to moderate intensity with magnitudes ranging from 3 to 5.5 (associated to the type 2 response spectrum of Eurocode 8 [25]) and the other 20 are representative of moderate to high seismicity with magnitude ranging from 5.6 to 7.5 (type 1 response spectrum).

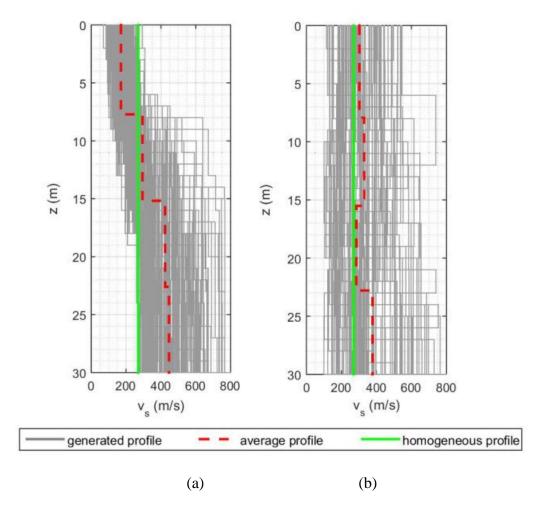


Fig. 2. Generated shear wave velocity profiles with depth $v_s(z)$ in the cases of (a) increasing v_s and (b) shear wave velocity inversion. All the generated soil profiles have the same average shear wave velocity $v_{s,30} = 270 \,\mathrm{m/s}$.

Taking into account the influence of the frequency content on the free-field (FF) ground motion, the selected seismic records are representative of a wide variety of dominant frequencies. The set of recorded seismic motions is sorted in terms of frequency content using the equivalent period T_{VA} , parameter proposed by Cameron and Green [37], defined as

$$T_{VA} = 2\pi \frac{\alpha_V \left(\xi = 5\%\right)}{\alpha_A \left(\xi = 5\%\right)} \frac{v_{gR}}{a_{gR}} \tag{2}$$

where a_{gR} and v_{gR} are the peak ground acceleration and velocity at the outcrop, respectively.

The median spectrum amplification factors for horizontal motion are estimated by Newmark and Hall [38] as $\alpha_A(\xi=5\%)=2.12$ and $\alpha_V(\xi=5\%)=1.65$, for the constant acceleration and constant velocity regions of 5% damped response spectra, respectively.

Fig. 3 shows the equivalent predominant frequency $1/T_{VA}$ related with the peak ground acceleration on rock outcrop a_{gR} for the set of 40 seismic motions. The oblique lines represent uniform values of v_{gR} . The severity of seismic motion increases according to the direction of increasing velocity (from the bottom-right corner toward the top-left one, where the values of a_{gR} and v_{gR} are both higher). Based on the observations in Kobe [39], the values $a_{gR} = 0.8 \, \mathrm{g}$ and $v_{gR} = 100 \, \mathrm{cm/s}$ are considered as risk limits, meaning that the input motions above these values are considered as the most severe ones (Fig. 3). Then the set of the selected seismic motions is made up of a wide variety of frequency content, peak acceleration and peak velocity.

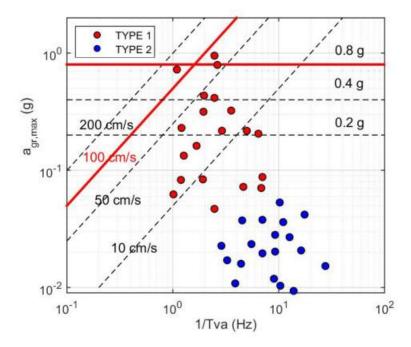


Fig. 3. Equivalent predominant frequency T_{VA} related to the peak ground acceleration at the outcrop a_{gR} for the set of 40 seismic motions. The oblique lines represent uniform values of

209 v_{gR} . The horizontal lines represent constant values of a_{gR} . 210 2.3 Wave propagation model 211 212 Assuming a vertical propagation in a horizontally layered medium, the numerical analysis is undertaken as a one-dimensional approach. The soil is assumed homogeneous and both 213 assumptions of linear and nonlinear constitutive behavior are analyzed. 214 Quadratic line finite elements are adopted for spatial discretization and the Newmark 215 algorithm for time discretization, with some numerical damping. The SWAP_3C finite 216 element software [30,31,40,41] is used for the numerical simulations. 217 At the soil-bedrock interface, an absorbing boundary condition adopted by Joyner and Chen 218 219 [42] is applied in order to take into account the elasticity of the underlying bedrock and allow energy to be radiated back. The mechanical properties characterizing the bedrock are the 220 221 density ρ_b and the shear wave velocity v_{sb} . The largest horizontal component of the signal recorded at the reference outcrop is halved and 222 imposed as the incident wave at the soil-bedrock interface. 223 The finite element size in each soil layer is defined as the minimum between 1m and one 224 225 tenth of the minimum wavelength, related to shear wave velocity in the layer and the maximum frequency assumed equal to 15 Hz, above which the spectral content of the input 226 signal is considered negligible. 227 Details of the finite element model employed in this research are completely described by 228 229 Santisi d'Avila et al. [30,31]. 230 2.4 Hysteretic model for soil 231 The so-called Masing-Prandtl-Ishlinskii-Iwan (MPII) nonlinear constitutive model [43] is 232

used for the soil in a total stress analysis. Its main feature is the satisfactory reproduction of

nonlinear and hysteretic behavior of soils under cyclic loadings [40,41], starting from the knowledge of a small number of parameters characterizing the soil properties, such as elastic parameters and the shear modulus redaction curve.

The MPII model is elasto-plastic with linear kinematic hardening. The plasticity model assumes an associated plastic flow, which allows for isotropic yield. This rheological model has no viscous damping and the soil damping is purely hysteretic and not frequency dependent. The size of the Von Mises yield surface is imposed by the backbone curve in the uniaxial stress case. The tangent constitutive matrix is deduced from the actual strain level and the strain and stress values at the previous time step [43,44].[44] This means that the stress level depends on the strain increment and strain history but not on the strain rate.

2.5 Data analysis

An optimal selection of site parameters is an important tool for the prediction of the expected ground motion. Based on recent results [14,22–24], the site dominant frequency f_0 and the

shear wave velocity gradient B_{30} are chosen as complementary proxies in this study.

As proposed by Regnier et al. [45], the shear wave velocity gradient B_{30} is defined as the slope of the linear regression of the relation between the logarithm of the shear wave velocity profile $v_s(z)$ and the depth z. Thus, it is computed as:

$$\log(v_s(z)) = B_{30}\log(z) + A_{30} \pm \sigma_{30}$$
 (3)

where A_{30} is the vertical intercept of the regression, σ_{30} is the standard deviation associated to the linear regression.

The shear wave velocity gradient B_{30} , estimated by Eq. (3) for all the generated 30m deep soil profiles, quantifies the variation of the shear wave velocity $v_s(z)$ contrast in the superficial layers. Its value is close to zero if the velocity is nearly constant with depth and it

is larger if the shear wave velocity v_s increases rapidly with depth [45].

The results of the numerical simulations of seismic wave propagation in the set of generated soil profiles, are first analyzed in terms of amplification factors, according to Ciancimino et al. [24], in both cases of linear and nonlinear soil behavior.

The soil amplification factor S_s is a local indicator of the site amplification, providing an estimate of the site effect on the FF motion. It is defined as the ratio of the peak ground acceleration at the surface a_g to the peak acceleration at the outcrop a_{gR} :

$$S_s = a_g / a_{gR} \tag{4}$$

The spectral amplification factor SA and the spectral velocity factor SV are used to quantify the ground motion intensity in a given period range. These parameters are proposed by Rey et al. [46]. They are defined as the ratio of I_{soil} to I_{rock} . These are the intensity of the spectrum estimated using the signal at the ground surface and at the outcrop, respectively. The intensities used in the amplification factors SA and SV are calculated by Housner [47] using the spectrum in terms of acceleration PSA(T) and velocity PSV(T), respectively, as follows:

$$SA = \frac{I_{soil}}{I_{rock}} \quad \text{with} \quad I = \int_{T_1}^{T_2} PSA(T) dT$$
 (5)

$$SV = \frac{I_{soil}}{I_{rock}} \quad \text{with} \quad I = \int_{T_1}^{T_2} PSV(T) dT \tag{6}$$

In Eqs (5) and (6), $[T_1 - T_2]$ is the fixed range of vibration period.

In this research, the spectra PSA(T) and PSV(T) are normalized with respect to the peak acceleration at the outcrop a_{gR} . The period range $\begin{bmatrix} 0.05-2.5s \end{bmatrix}$, representative of the fundamental vibration period for more common structures, is divided into three sub-ranges in order to analyze the results for short, middle and long periods of vibration. Spectral

amplification factors for short [0.05-0.5s], middle [0.5-1s] and long [1-2.5s] periods of

vibration are indicated as (SA_S, SV_S) , (SA_M, SV_M) and (SA_L, SV_L) , respectively.

In a second phase, the response spectra of numerical FF motion are compared to those

suggested by Eurocode 8 [25]. Finally, the results in terms of site amplification factors are

compared with the Eurocode 8 [25], the New Zealand Standard [26] building codes, and those

evaluated by Pitilakis et al. [18], Ciancimino et al. [24].

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3. Results and discussion

The variability of the shear wave velocity profiles with depth $v_s(z)$ for the set of generated

soil profiles, having the same average $v_{s,30} = 270 \,\mathrm{m/s}$, is shown in Fig. 2. The FF motion

obtained by numerical simulation, propagating the set of recorded seismic signals along the

291 generated soil profiles is analyzed.

In the following, the influence on site amplification of complementary parameters as the shear

wave velocity profiles with depth $v_s(z)$, the site dominant frequency f_0 and the shear wave

velocity gradient B_{30} is assessed. The fluctuation of amplification factors with the site

parameters f_0 and B_{30} is analyzed.

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3.1 Site parameter variability

The dominant frequency of the site f_0 is obtained by evaluating the FF to bedrock transfer

function (TF) that is the ratio of the Fourier spectrum of the accelerograms at the FF soil

surface and at the outcropping bedrock surface. A low-amplitude signal is used so that the soil

remains in the elastic regime. The frequency corresponding to the peak of this TF corresponds

to the fundamental frequency of the soil column, considered as the dominant frequency of the

site f_0 . In the case of a homogeneous soil, the fundamental frequency of a 30m deep soil

304 profile, having a shear wave velocity $v_s = 270 \,\mathrm{m/s}$, is also deduced [48] as

305 $f_0 = v_s/(4H) = 2.25 \,\mathrm{Hz}$. The homogeneous soil profile is adopted in the following

- 306 comparisons as canonical case.
- Fig. 4 displays the TF obtained for the soil profile with a homogeneous soil, the generated soil
- profiles with increasing shear wave velocity with depth $v_s(z)$ and those with an inversion in
- the $v_s(z)$ profile. The dominant frequency of the site f_0 , obtained for the set of all the
- generated soil profiles ranges from 1.5 to 3.5Hz. For increasing $v_s(z)$ profiles (Fig. 4a), the
- dominant frequency of the site is mostly higher than the frequency for the homogeneous case.
- Whereas the natural frequencies obtained for soil profiles with an inversion in $v_s(z)$ are
- distributed in a frequency range (Fig. 4b). The peaks of the TF obtained for the generated soil
- profiles show a higher amplification compared with the homogeneous soil profile in most
- cases. In particular, the amplification estimated for the soil profiles having increasing $v_s(z)$ is
- larger for higher f_0 (Fig. 4a).
- According to Fig. 4, the site amplification changes depending on the stratigraphy (i.e. shear
- wave profile with depth $v_s(z)$) and the fundamental frequency of the site f_0 . The frequency
- 319 content of the surface motion varies accordingly.
- Fig. 5 illustrates the linear correlation between the shear wave velocity gradient B_{30} and the
- fundamental frequency of the site f_0 , for the set of generated soil profiles with given $v_{s,30}$.
- This correlation is high, with a correlation coefficient $r^2 = 0.85$, for the whole set of 300 soil
- 323 profiles.
- The amplification factors in Eqs (4), (5) and (6) are calculated using the computed FF motion
- and the related response spectrum for all the 24000 samples (set of 40 recorded seismic
- signals applied to 300 generated soil profiles, for linear and nonlinear soil behaviors).

The estimated amplification factors S_s , SA and SV, SA_S , SA_M and SA_L , SV_S , SV_M and SV_L , are shown in Figs 6, 7, 8, and 9 as functions of the dominant period of the site $T_0 = 1/f_0$ and of the shear wave velocity gradient B_{30} , respectively, for both cases of linear (a) and nonlinear (b) behavior. The trend of mean and standard deviation is also displayed by the thick and dashed lines, respectively.

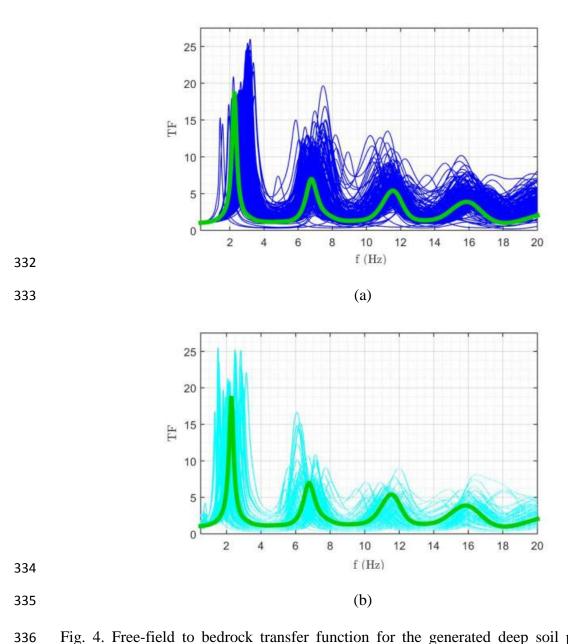


Fig. 4. Free-field to bedrock transfer function for the generated deep soil profiles having increasing shear wave velocity profile (a) and showing a velocity inversion (b). The thick line is the transfer function for the homogeneous soil profile.

Figs 6, 7, 8 and 9 illustrate the amplification factors in the three fixed ranges of period in order to understand if their variation is modified for different periods. It appears that the largest amplifications are reached for short vibration periods (lower than 0.5s).

Figs 6 and 8 display that site amplification is strongly dependent on the site predominant period T_0 , for short vibration periods of the FF motion (SA_S, SV_S) and independent from it for long periods (SA_L, SV_L) . Moreover, site amplification is much more pronounced in soil profiles having T_0 lower than that of the homogeneous profile, for short vibration periods of the FF motion (SA_S, SV_S) . Whereas, for middle periods of vibrations (SA_M, SV_M) , site amplification is more pronounced in soil profiles having predominant period T_0 higher than that of the homogeneous profile.

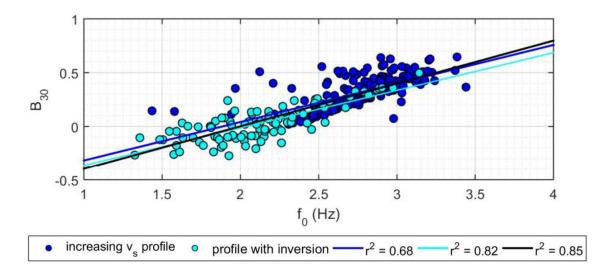
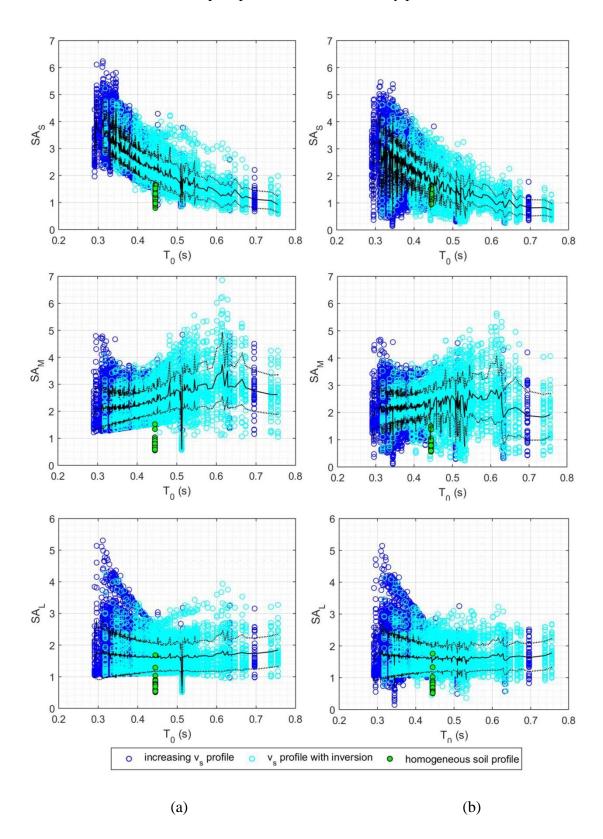
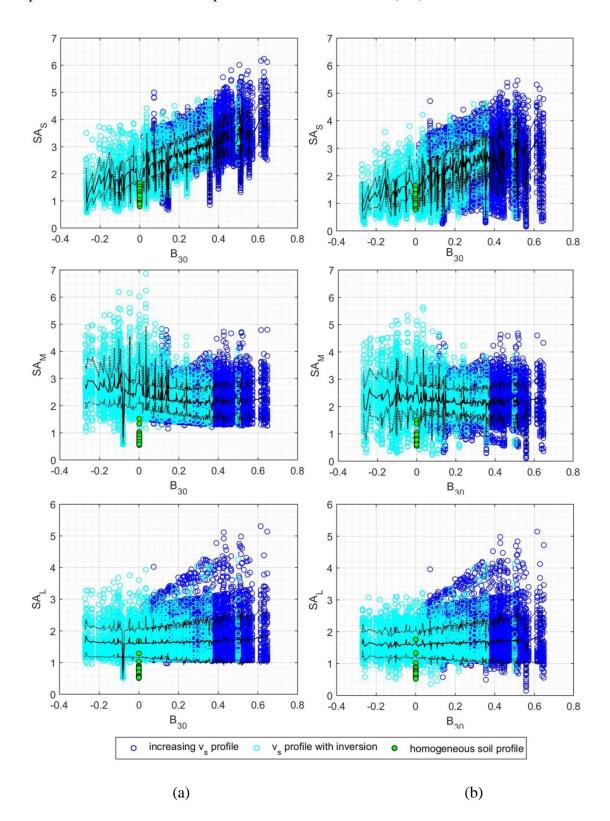
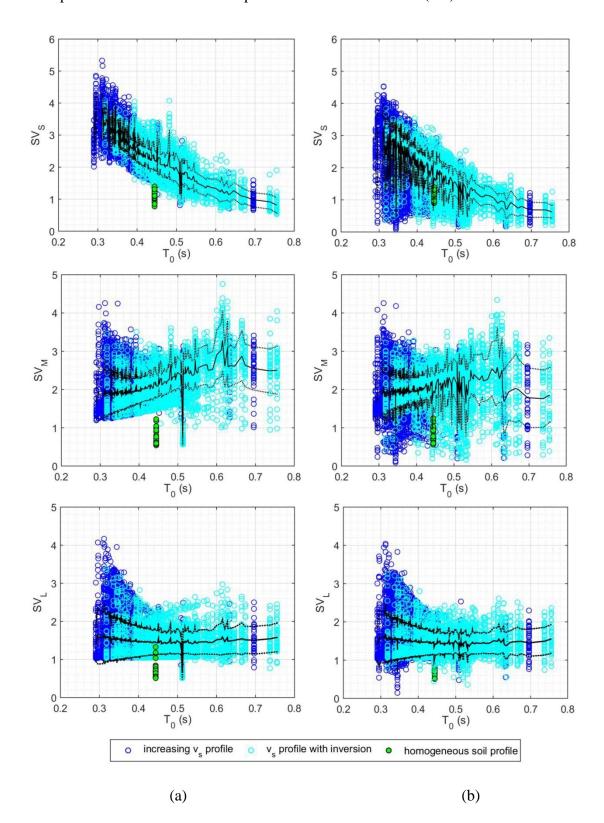


Fig. 5. Linear regression of the shear wave velocity gradient B_{30} with reference to the fundamental frequency of the site f_0 , for the generated deep soil profiles. The thick line is for the set of all 300 generated soil profiles.

Figs 7 and 9 show that the largest values of amplification factors are reached for short







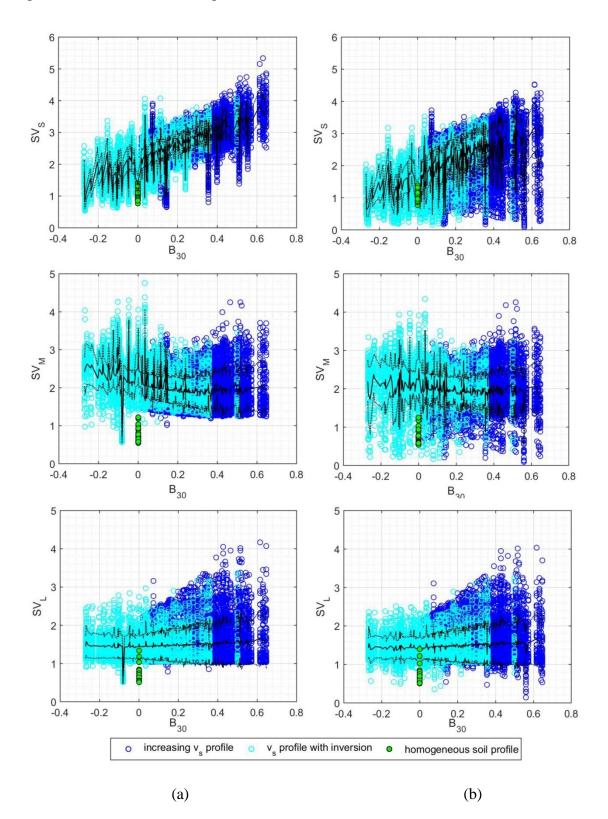


Fig. 9. Amplification factors SV_S , SV_M and SV_L as a function of the shear wave velocity gradient B_{30} , for both cases of linear (a) and nonlinear (b) behaviors. The thick and dashed lines represent the mean and means plus one standard deviation (SD) trend.

The nonlinear soil behavior on the site response induces a reduced amplification effect. Similarly to the case of linear soil behavior, the site amplification is more pronounced in the

site parameters. On the contrary, the site amplification is less pronounced and independent

case of short vibration periods of the FF motion and it is strongly dependent on the proposed

from the proposed site parameters, for longer vibration periods of the FF motion.

3.2 Influence on site effects of the nonlinear soil behavior

In this section, the effects of soil nonlinearities on site response are investigated with reference to the proposed site proxies (predominant period T_0 and shear wave velocity gradient B_{30}). The main goal is to verify the reliability of T_0 and B_{30} even in the range of soil nonlinear behavior. The impact of nonlinear soil response on the site response is characterized in terms of amplification factor SV. The SV factor is estimated in both cases of linear and nonlinear soil response, in the three adopted period ranges. The amplification factor NL/L is computed as the ratio of spectral velocity factors SV_S , SV_M and SV_L in the ranges of short, middle and long period, for nonlinear soil behavior to that for linear soil behavior.

Fig.10 illustrates the average amplification factor as a function of the site dominant period T_0 (Fig. 10a) and shear wave velocity gradient B_{30} (Fig. 10b). Results are distinguished between those for weak earthquakes (associated to the type 2 response spectrum of Eurocode 8 [25]) and strong earthquakes (type 1 response spectrum).

As expected, the effect of nonlinear soil behavior is negligible for small earthquakes (type 2

response spectrum of Eurocode 8 [25]) for the whole range of periods of vibration. In fact, the

NL/L ratio is close to one.

In the case of stronger earthquakes (type 1 response spectrum), the modification in the site response depends on the stratigraphy and varies with the vibration period of the FF motion.

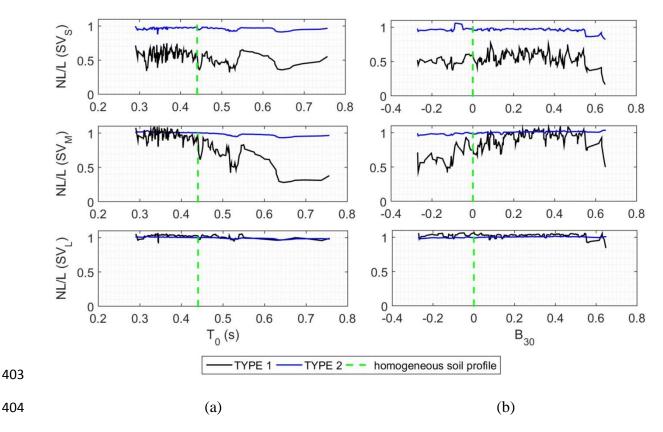


Fig. 10. Computed ratio of spectral velocity factors SV_S , SV_M and SV_L (short, intermediate and long periods of vibration) for nonlinear soil behavior to that for linear soil behavior (NL/L) as a function of the dominant period of the site T_0 (a) and the shear wave velocity gradient B_{30} (b), for the whole set of generated soil profiles. The curves are distinguished between those for small earthquakes (associated to the type 2 response spectrum of Eurocode 8) and strong earthquakes (type 1 response spectrum).

According to Fig. 10, for vibration periods of the strong motion over 1s, the effect of nonlinear soil behavior is negligible (see SV_L). On the contrary, in the range of short periods (see SV_S), the amplitude reduction due to nonlinear effects is up to 60%. Moreover, the

amplification factor in the range of middle periods (see SV_M) show a remarkable amplitude reduction for a site predominant period T_0 higher than 0.44s (period of vibration of the homogeneous soil profile) and a reduction up to 10% for lower periods T_0 (Fig 10a). An important amplitude reduction is obtained for a shear wave velocity gradient B_{30} outside the range [0-0.5], that correspond to soil profiles with significant impedance contrast (high B_{30}) and velocity inversions (negative B_{30}).

3.4 Comparison with building codes

- Fig. 11 displays the comparison of the average pseudo-acceleration response spectrum normalized with respect to the peak acceleration of the outcropping motion, using a damping ratio of 5%.
- The linear and nonlinear computations are separated and, for both, the cases of weak earthquakes (associated to the type 2 response spectrum of the Eurocode 8 [25]) and strong earthquakes (type 1 response spectrum) are distinguished. In each of these combinations, the average pseudo-acceleration response spectra are estimated for the FF motion in the case of increasing shear wave velocity and for profiles with a velocity inversion.
 - The elastic response spectra proposed by Eurocode 8 is conservative, compared to the obtained average response spectra, for higher periods (higher than 0.2s for type 2 and 0.6s for type 1). Conversely, for lower periods, the average response spectrum, obtained for all the generated soil profiles, gives higher acceleration peaks.
 - If the elastic response spectrum proposed by Eurocode 8 [3] is compared for the spectrum in the homogeneous case, with average soil properties, it is conservative for the whole ranges of period for weak earthquakes (type 2) and in most cases for strong earthquakes (type 1).
- 438 The reduction of the site response for the nonlinear soil behavior is negligible for weak

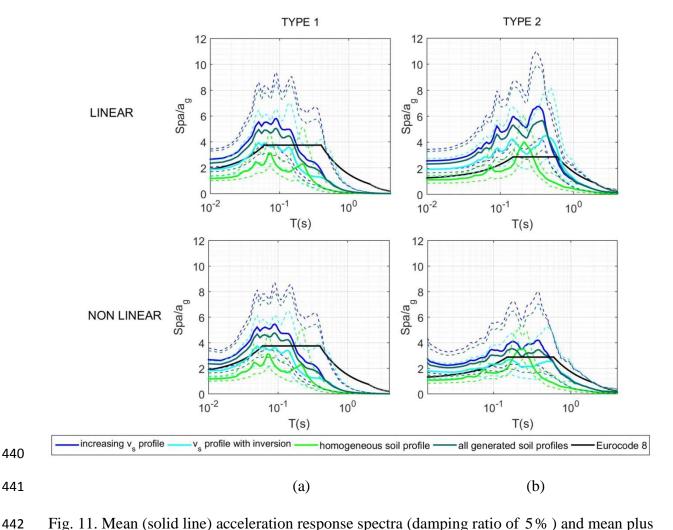


Fig. 11. Mean (solid line) acceleration response spectra (damping ratio of 5%) and mean plus one standard deviation (dashed line), evaluated for the free-field motion of the generated multilayered soil profiles, compared to the homogeneous case and the elastic response spectrum proposed by Eurocode 8 [3]. The cases are distinguished as follows: assumption of linear and nonlinear soil behavior; weak earthquakes (a) and strong earthquakes (b). Following the approach adopted by Ciancimino et al. [24] for the linear regime, the site amplification factors are evaluated for the samples of the present statistical analysis, in the case of linear and nonlinear soil behavior. The computed amplification factors are compared with those suggested by Eurocode 8 [25] and New Zealand Standard [26] building codes, with those proposed by Pitilakis et al. [18] and with those obtained by Ciancimino et al. [24]. The ground type classification used in the Eurocode 8 [25] is only based on the $v_{s,30}$ parameter. In

the New Zealand Standard [26], the fundamental site period is included as a proxy of site 453 454 effects. In addition, Pitilakis et al. [18] classify the ground type using the fundamental period of the site, the depth of the seismic bedrock and the average soil column shear wave velocity 455 are taken into account. The 300 generated soil profiles are identified as ground type C 456 according to Eurocode 8 [25] and as C2 according Pitilakis et al. [18]. Among them, 286 are 457 identified as ground type C according to the New Zealand Standard [26] building codes 458 459 $(T_0 > 0.6s)$. 460 The comparison between the mean value of site amplification factors S_s (Eq. (4)) and SA(Eq. (5)), and the values within one standard deviation of the mean are represented in Fig. 12 461 for weak earthquakes and in Fig. 13 for strong earthquakes. These values are compared to 462 those obtained according to the building codes to analyze their reliability. The coefficient of 463 variation CV of S_s and SA is also calculated. In each figure, the simulations under the 464 assumption of linear and nonlinear soil behavior are separated. The amplification factors are 465 estimated, for both soil behaviors, using only the FF motions of multilayered soil profiles with 466 increasing shear wave velocity with depth, only the FF motions of soil profiles with a velocity 467 468 inversion, the FF motions of all the generated soil profiles and the FF motion of the 469 homogeneous soil profile. The obtained numerical results obtained under the assumption of linear soil behavior are also 470 471 compared to those obtained by Ciancimino et al. [24], that performed analyses on a database of seismic responses of one-dimensional soil profiles having equivalent linear behavior. We 472 can observe that our results under the assumption of linear behavior are in good agreement 473 474 with those obtained by Ciancimino et al. [24]. According to Figs 12 and 13, only the amplification factors obtained for the case of 475 homogeneous soil profile are smaller than those suggested by Eurocode 8 [25] and the same 476 consideration is made comparing with the New Zealand Standard [26] building codes (Fig. 477

478 14).

It is interesting to note that the values proposed by Pitilakis et al. [18] for the site 479 amplification factor SA are close to those computed using the set of generated samples in the 480 present analysis. Conversely, the values proposed by Pitilakis et al. [18] for the site 481 amplification factor S_s are lower than those obtained in the present research. This means that 482 ground classification based on complementary site proxies instead on a single proxy is more 483 484 adequate. But also it is important to understand the best complementary proxies that allow predicting the site response for different ranges of periods. 485 Moreover, the nonlinear effects are negligible in terms of mean values and CV of the 486 amplification factors, for weak earthquakes (Fig. 12) and they are significant for strong 487 earthquakes (Fig. 13). 488 The average amplification factors obtained for soil profiles with a velocity inversion are lower 489 than the ones associated to other soil profiles. 490 Lastly, Fig. 14 shows that the comparison between the computed amplification factors and 491 those deduced by New Zealand Standard [26]. The difference observed could be justified by a 492 493 higher seismicity expected in New Zealand that could increase the effect of nonlinear soil behavior and thus reduce the peak acceleration. 494

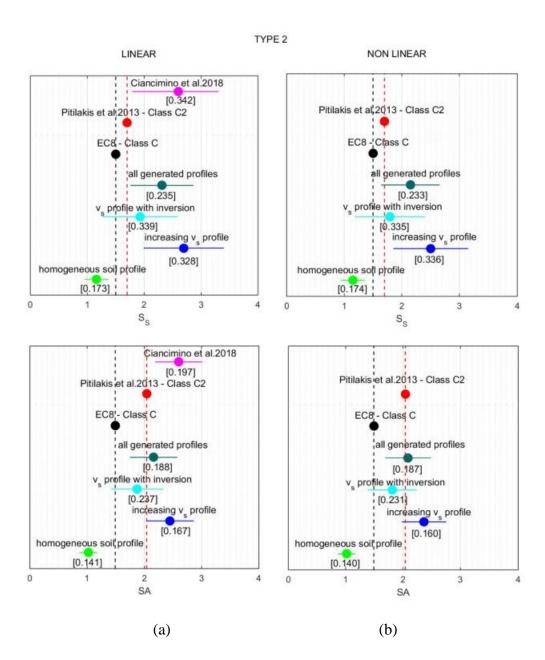


Fig. 12. Mean value of site amplification factors S_s (top) and SA (bottom), the values within one standard deviation of the mean and the coefficient of variation CV (value between brackets) in the case of small earthquakes (type 2 response spectrum of Eurocode 8 [25]), for numerical simulations under the assumption of linear (a) and nonlinear (b) soil behavior. The values suggested by Eurocode 8 [25], Pitilakis et al. [18] and Ciancimino et al [24] are indicated.



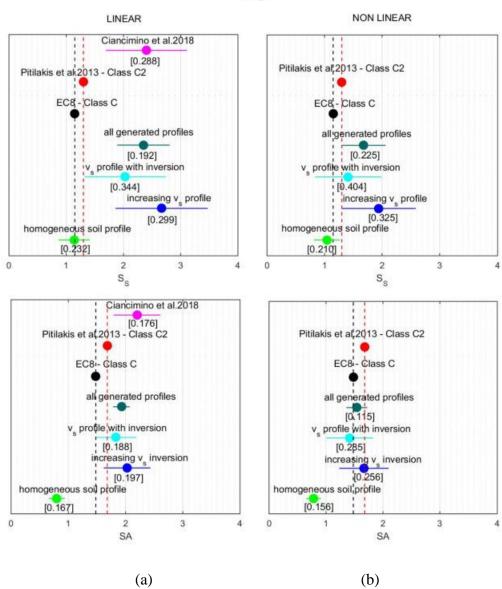


Fig. 13. Mean value of site amplification factors S_s (top) and SA (bottom), the values within one standard deviation of the mean and the coefficient of variation CV (value between brackets) in the case of strong earthquakes (type 1 response spectrum of Eurocode 8 [25]), for numerical simulations under the assumption of linear (a) and nonlinear (b) soil behavior. The values suggested by Eurocode 8 [25], Pitilakis et al. [18] and Ciancimino et al [24] are indicated.

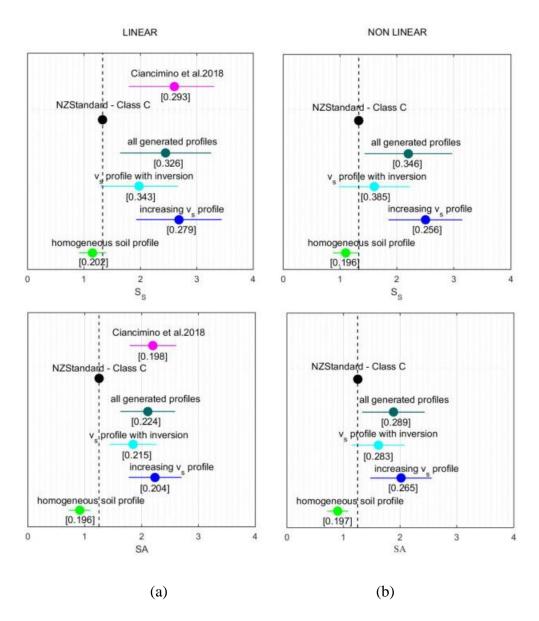


Fig. 14. Mean value of site amplification factors S_s (top) and SA (bottom), the values within one standard deviation of the mean and the coefficient of variation CV (value between brackets) for the whole set of recorded seismic signals. Numerical simulations under the assumption of linear (a) and nonlinear (b) soil behavior are separated. The values suggested by the New Zealand Standard [26] building codes are indicated.

4. Conclusions

The vertical propagation of various recorded seismic signals along stochastically generated soil profiles is numerically simulated to obtain the FF motion, in both cases of linear and

nonlinear soil behavior. The average shear wave velocity in the upper 30m of soil profiles

523 $v_{s,30}$ is fixed and corresponds to the ground type C, according to the Eurocode 8. The soil-

- bedrock interface depth is selected as $H_{800} = 30 \,\mathrm{m}$.
- 525 This research highlights the influence of the layering uncertainty on the site response. It is
- demonstrated that the average shear wave velocity $v_{s,30}$ is not able, as single parameter, to
- 527 characterize the soil profiles in terms of expected amplification level over the whole
- 528 frequency range.

- Two site parameters are proposed as proxies, complementary to $v_{s,30}$, such as the dominant
- frequency of the site $f_{\scriptscriptstyle 0}$ and the shear wave velocity gradient $B_{\scriptscriptstyle 30}$. The site response is
- represented in terms of site amplification factors, deduced using the response spectrum of the
- FF motion, for the 24000 performed simulations (set of 40 recorded seismic signals applied to
- 533 300 generated soil profiles, for linear and nonlinear soil behaviors). The influence on site
- amplification of the shear wave velocity profile, site dominant frequency and shear wave
- velocity gradient are analyzed independently from H_{800} .
- The obtained amplification factors are functions of both site conditions and intensity of rock
- 537 motions and the values could decrease due to soil nonlinearity. The amplification factors
- increase with decreasing site dominant period T_0 and increasing shear wave velocity gradient
- 539 B_{30} , when they are evaluated over a large range of vibration periods [0.05-2.5s].
- Nevertheless, site amplification appears strongly dependent on the site predominant period
- 541 T_0 , for short vibration periods of the FF motion and independent from it for long periods.
- Moreover, site amplification is much more pronounced in soil profiles having T_0 lower than
- that of the homogeneous profile, for short vibration periods of the FF motion.
- 544 The largest values of amplification factors are reached for short vibration periods of the FF
- motion, lower than $0.5 \,\mathrm{s}$, in soil profiles having a high shear wave velocity gradient B_{30} ,

546 which corresponds to sites with a large impedance contrast in the first 30m or with a steep slope in the shear wave velocity profile. 547 The site response is modified when the nonlinear soil behavior is taken into account in the 548 numerical simulations. The nonlinear soil behavior on the site response induces a reduced 549 amplification effect. Similarly to the case of linear soil behavior, the site amplification is more 550 pronounced in the case of short vibration periods of the FF motion and it is strongly 551 dependent on the proposed site parameters. On the contrary, the site amplification is less 552 553 pronounced and independent from the proposed site parameters, for vibration periods of the FF motion higher than 1s. 554 Nonlinear effects are negligible for small earthquakes and for vibration periods of strong 555 ground motions longer than 1s. Whereas, they are significant for short- and middle-periods of 556 strong earthquakes. In particular, soil profiles having dominant period T_0 higher than that of 557 the homogeneous profile exhibit significant nonlinear effects. In addition, soil profiles with 558 negative value of B_{30} (i.e. velocity inversion) and profiles with high value of B_{30} lead to 559 pronounced nonlinear site effects. 560 561 Average amplification factors are compared to those suggested by Eurocode 8 [25] and New Zealand Standard [26] building codes, and by Pitilakis et al. [18]. The obtained results 562 demonstrate that the ground type classification proposed by Eurocode 8 [25], based on $v_{s,30}$ 563 only, is not suitable. The comparison to the amplification factors proposed by Pitilakis et al. 564 565 [18] shows that the introduction of complementary site proxies makes the ground type classification more adequate. In fact, the computed average spectral amplification factors SA 566 are comparable to those estimated by Pitilakis et al. [18]. 567 568 The average amplification factors computed for soil profiles with a velocity inversion are lower than for the profiles having monotonic shear wave velocity profiles. 569 This research confirms that it is possible to improve the current ground type classification 570

taking into account simple and accessible site parameters complementary to $v_{s,30}$. Accounting for complementary site proxies in the ground type classification, such as the dominant frequency of the site f_0 and the shear wave velocity gradient B_{30} , allow a better prediction of the expected amplification, in particular for short vibration periods of the FF motion, up to 1s. Further work should be done to analyze the results for soil profiles having different ground types according to the Eurocode 8 (only ground type C has been discussed in this research) and depth H_{800} .

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6. References

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