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Nucleon decay in the deuteron

F. Oosterhof,¹ J. de Vries,^{2,3,4,5} R. G. E. Timmermans,¹ and U. van Kolck^{6,7}

¹Van Swinderen Institute for Particle Physics and Gravity,

University of Groningen, 9747 AG Groningen, The Netherlands

²Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics,

University of Amsterdam, Science Park 904,

1098 XH Amsterdam, The Netherlands

³Nikhef, Theory Group, Science Park 105,

 $1098 \ XG, \ Amsterdam, \ The \ Netherlands$

⁴Amherst Center for Fundamental Interactions,

Department of Physics, University of Massachusetts Amherst,

Amherst, Massachusetts 01003, USA

⁵RIKEN BNL Research Center, Brookhaven National Laboratory,

Upton, New York 11973-5000, USA

⁶Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France

⁷Department of Physics, University of Arizona, Tucson, Arizona 85721, USA

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Abstract

We calculate the lifetime of the deuteron from dimension-six quark operators that violate baryon number by one unit. We construct an effective field theory (EFT) for $|\Delta B| = 1$ interactions that give rise to nucleon and $\Delta B = 1$ deuteron decay in a systematic expansion. Nucleon decay introduces imaginary parts in the low-energy constants of the $\Delta B = 0$ nuclear interactions in Chiral EFT. We show that up to and including next-to-leading order the deuteron decay rate is given by the sum of the decay rates of the free proton and neutron. The first nuclear correction is expected to contribute at the few-percent level and comes with an undetermined low-energy constant. We discuss its relation to earlier potential-model calculations. In the Standard Model (SM) of particle physics the observed stability of the proton is attributed to an accidental global U(1) symmetry. The associated, classically conserved quantity, baryon number B, is, however, broken by small quantum effects that preserve B - L, where L denotes lepton number. If it is not associated to a local, gauge symmetry, B is expected to be violated in extensions of the SM to higher energies. In fact, proton decay is an outstanding prediction of Grand Unified Theories, in which the strong, weak, and electromagnetic interactions unify at an ultrahigh scale of the order of 10^{16} GeV [1]. At present, the lower bounds on the proton lifetime for the two important decay channels $p \to \pi^0 + e^+$ and $p \to \pi^+ + \bar{\nu}$ are $1.6 \cdot 10^{34}$ y and $3.9 \cdot 10^{32}$ y at 90% confidence level, respectively [2, 3]. Such processes violate baryon number by one unit ($\Delta B = 1$).

Experiments that search for nucleon decay aim to detect it inside nuclei. The lifetime of a nucleon bound in a nucleus may differ from that of a free nucleon due to nuclear interactions, which make theoretical estimates difficult. We examine here the effect of these interactions on the lifetime of the deuteron, the simplest nucleus consisting of more than one nucleon, in effective field theory (EFT). EFT allows for systematic and model-independent calculations of low-energy processes. Recently, EFT was applied to processes in which baryon number is violated by two units [4–7], in particular neutron-antineutron oscillations in free space and in the deuteron. We follow Ref. [6], in which the $\Delta B = 2$ deuteron decay rate was calculated in a systematic expansion.

We restrict ourselves to the lowest-dimension $|\Delta B| = 1$ operators in the SM EFT that satisfy the full SM gauge symmetry and construct an EFT with pions and nucleons describing nucleon and deuteron decay. These operators mediate the decay of the deuteron to a nucleon, an antilepton, and one or more mesons. We distinguish between two classes of $\Delta B = 1$ deuteron decay, which are illustrated in Fig. 1. In processes of the first class, Fig. 1(a), one of the nucleons decays to an antilepton and one or more mesons, while it may interact with the other nucleon via long-range interactions. In this class, we can directly relate the deuteron decay rate to $\Delta B = 1$ decay in the one-nucleon sector via known SM physics. In processes of the second class, Fig. 1(b), the two nucleons in the deuteron are converted to an antilepton and a nucleon and possibly mesons via a short-range $\Delta B = 1$ interaction. Since the produced mesons and antileptons have high momenta, they cannot be treated explicitly in the EFT. We therefore introduce imaginary parts in the low-energy constants of $\Delta B = 0$ interactions, which generate inclusive decay widths. We show that the power counting that is, the ordering of the EFT interactions according to the expected magnitude of their contributions to observables — dictates that deuteron decay is dominated by free-nucleon decay, which is described by the first class. The first nuclear correction is expected to come from the second class at the few-percent level.

The lowest-dimension $|\Delta B| = 1$ operators that satisfy the full $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$ SM gauge symmetry are dimension-six operators constructed from three quark fields and one lepton field. We focus on the operators with *u*- and *d*-quark fields and at most one *s*-quark field, because conservation of energy does not allow the deuteron to decay via a $\Delta B = 1$ process to a final state with two strange quarks or two strange antiquarks. The Lagrangian of the $|\Delta B| = 1$ dimension-six operators can be written as [8–11]

$$\mathcal{L}_{|\Delta B|=1} = \sum_{i=1}^{4} \sum_{d=1}^{2} \mathcal{C}_{d}^{(i)} \mathcal{Q}_{d}^{(i)} + \sum_{i=1}^{6} \sum_{d=1}^{2} \tilde{\mathcal{C}}_{d}^{(i)} \tilde{\mathcal{Q}}_{d}^{(i)} + \text{H.c.} , \qquad (1)$$

where $C_d^{(i)}$ and $\tilde{C}_d^{(i)}$ are Wilson coefficients that depend on physics beyond the SM, $Q_d^{(i)}$ are



FIG. 1. The two classes of deuteron decay. The crossed circle denotes the deuteron, the solid line a nucleon (N) or a lepton (l), the dashed black line a pion (π) , and the gray dashed lines denote possible more pions. The black diamond stands for a $|\Delta B| = 1$ interaction, while the gray blob represents the propagation and strong interaction of two nucleons, and the dashed blob the possibility of additional pion interactions.

operators with u- and d-quark fields,

$$\mathcal{Q}_{d}^{(1)} = (d_{R_{\alpha}}^{T} C u_{R_{\beta}}) \left[(u_{L_{\gamma}}^{T} C e_{L_{d}}) - (d_{L_{\gamma}}^{T} C \nu_{L_{d}}) \right] \varepsilon_{\alpha\beta\gamma} ,$$

$$\mathcal{Q}_{d}^{(2)} = (d_{L_{\alpha}}^{T} C u_{L_{\beta}}) (u_{R_{\gamma}}^{T} C e_{R_{d}}) \varepsilon_{\alpha\beta\gamma} ,$$

$$\mathcal{Q}_{d}^{(3)} = (d_{L_{\alpha}}^{T} C u_{L_{\beta}}) \left[(u_{L_{\gamma}}^{T} C e_{L_{d}}) - (d_{L_{\gamma}}^{T} C \nu_{L_{d}}) \right] \varepsilon_{\alpha\beta\gamma} ,$$

$$\mathcal{Q}_{d}^{(4)} = (d_{R_{\alpha}}^{T} C u_{R_{\beta}}) (u_{R_{\gamma}}^{T} C e_{R_{d}}) \varepsilon_{\alpha\beta\gamma} ,$$
(2)

and $\tilde{\mathcal{Q}}_{d}^{(i)}$ operators with one strange-quark field,

$$\tilde{\mathcal{Q}}_{d}^{(1)} = (s_{R_{\alpha}}^{T} C u_{R_{\beta}}) \left[(u_{L_{\gamma}}^{T} C e_{L_{d}}) - (d_{L_{\gamma}}^{T} C \nu_{L_{d}}) \right] \varepsilon_{\alpha\beta\gamma} ,$$

$$\tilde{\mathcal{Q}}_{d}^{(2)} = (s_{L_{\alpha}}^{T} C u_{L_{\beta}}) (u_{R_{\gamma}}^{T} C e_{R_{d}}) \varepsilon_{\alpha\beta\gamma} ,$$

$$\tilde{\mathcal{Q}}_{d}^{(3)} = (s_{L_{\alpha}}^{T} C u_{L_{\beta}}) \left[(u_{L_{\gamma}}^{T} C e_{L_{d}}) - (d_{L_{\gamma}}^{T} C \nu_{L_{d}}) \right] \varepsilon_{\alpha\beta\gamma} ,$$

$$\tilde{\mathcal{Q}}_{d}^{(4)} = (s_{R_{\alpha}}^{T} C u_{R_{\beta}}) (u_{R_{\gamma}}^{T} C e_{R_{d}}) \varepsilon_{\alpha\beta\gamma} ,$$

$$\tilde{\mathcal{Q}}_{d}^{(5)} = (d_{R_{\alpha}}^{T} C u_{R_{\beta}}) (s_{L_{\gamma}}^{T} C \nu_{L_{d}}) \varepsilon_{\alpha\beta\gamma} .$$
(3)

In these operators the subscript d = 1, 2 indicates the lepton generation, the subscript L, R indicates the chirality of the fermion field, C is the charge-conjugation matrix, α, β, γ are color indices, and $\varepsilon_{\alpha\beta\gamma}$ is the Levi-Civita tensor. The Wilson coefficients are expected to be suppressed by the scale of new physics $\Lambda_{|\Delta B|=1}$, *i.e.* $C_d^{(i)} = \mathcal{O}(c_d^{(i)}\Lambda_{|\Delta B|=1}^{-2})$ and $\tilde{C}_d^{(i)} = \mathcal{O}(\tilde{c}_d^{(i)}\Lambda_{|\Delta B|=1}^{-2})$, where $c_d^{(i)}$ and $\tilde{c}_d^{(i)}$ are dimensionless constants. We use C to denote the values of $C_d^{(i)}$ and $\tilde{C}_d^{(i)}$.

At low energies QCD is non-perturbative, which complicates the calculation of the effects of these interactions on observables. We therefore use Chiral EFT (χ EFT) [12, 13], which is a low-energy EFT of QCD with nucleons and pions as the relevant degrees of freedom. χ EFT is based on the approximate $SU(2)_L \otimes SU(2)_R$ chiral symmetry of QCD, spontaneously broken to the isospin subgroup $SU(2)_I$ and explicitly broken by the *u*- and *d*-quark masses. The pions appear naturally in the theory as pseudo-Goldstone bosons with a mass well below the chiral-symmetry-breaking scale, $m_{\pi} \simeq 140 \text{ MeV} \ll \Lambda_{\chi} \sim 2\pi F_{\pi}$, where $F_{\pi} \simeq 185 \text{ MeV}$ the pion decay constant. The chiral Lagrangian is constructed from all terms consistent with the symmetries of QCD and ordered in the number of derivatives and quark masses. Observables at typical momenta $Q \lesssim m_{\pi}$ are calculated in an expansion in Q/Λ_{χ} . Since nucleons have a mass $m_N \simeq 940 \text{ MeV} \sim \Lambda_{\chi}$, they are treated as non-relativistic in the regime of validity of the theory. Terms in the chiral Lagrangian contain the so-called low-energy constants (LECs), which have to be calculated with non-perturbative methods, in particular lattice QCD, or determined from experiment. Under an assumption of naturalness, they can be estimated by naive dimensional analysis (NDA) [14]. (For a review of the form and limitations of NDA in nuclear systems, see Ref. [15].)

We first discuss the one-nucleon sector. The Lagrangian for non-relativistic nucleon fields $N = (p n)^T$ interacting with pion fields π^a (a = 1, 2, 3) is

$$\mathcal{L}_{N} = N^{\dagger} \left(i\partial_{0} + \frac{\nabla^{2}}{2m_{N}} \right) N - \frac{1}{2} \pi^{a} \left(\partial^{2} + m_{\pi}^{2} \right) \pi^{a} + \frac{g_{A}}{F_{\pi}} N^{\dagger} \sigma_{k} \tau^{a} N \nabla_{k} \pi^{a} + \frac{1}{2} N^{\dagger} \left(\alpha_{0} + \alpha_{1} \tau^{3} \right) N + \frac{1}{F_{\pi}} N^{\dagger} \left[\alpha_{2} \left(\tau^{a} - \delta^{a3} \tau^{3} \right) + \alpha_{3} \varepsilon^{3ab} \tau^{b} \right] N \pi^{a} + \dots , \qquad (4)$$

where σ_k (k = 1, 2, 3) are Pauli spin matrices, τ^a (a = 1, 2, 3) are Pauli isospin matrices, and ε^{abc} is the Levi-Civita tensor in isospin space. Here and below the dots denote terms that do not contribute to the order of our calculation. The first line in Eq. (4) is the standard *B*-conserving Lagrangian, with $g_A \simeq 1.27$ the axial-vector coupling constant. Before they are expanded in powers of π^2/F_{π}^2 , these operators transform as tensor products of scalars and vectors under $SO(4) \sim SU(2)_L \otimes SU(2)_R$, reflecting the pattern of explicit chiral-symmetry breaking in the QCD Lagrangian. The terms with the complex LECs $\alpha_{0,1,2,3}$ are induced by $|\Delta B| = 1$ physics and contribute to the inclusive proton and neutron decay rate. These operators, before they are expanded in powers of pion fields, transform under chiral symmetry as the Kronecker products of each combination of two $|\Delta B| = 1$ operators in Eqs. (2) and (3) that have zero net baryon number, lepton number, and strangeness. From NDA we expect

$$\alpha_{0,1,2,3} = \mathcal{O}\left(\frac{\Lambda_{\chi}^5 \mathcal{C}^2}{(4\pi)^4}\right) .$$
(5)

We do not write explicit $|\Delta B| = 1$ interactions, because the mesonic final states in Fig. 1 contain hard pions with momenta outside the regime of validity for χ EFT. Instead, we calculate the imaginary part of the pole in the nucleon and deuteron propagators to determine their inclusive widths. These imaginary parts stem from the imaginary parts of the newly introduced LECs, which therefore enable nucleon and nuclear decay.

The fully dressed propagator for a nucleon i = p, n of energy E and three-momentum \vec{p} can be written in the form

$$G_i(E, \vec{p}) = \frac{iZ_i}{E - \vec{p}^2/2m_N + \ldots + i\Gamma_i/2} , \qquad (6)$$

where Z_i is the wavefunction renormalization factor, and

$$\Gamma_p = \operatorname{Im}(\alpha_0 + \alpha_1) + \dots , \qquad (7)$$

$$\Gamma_n = \operatorname{Im}(\alpha_0 - \alpha_1) + \dots \tag{8}$$

are the proton and neutron decay rates, respectively. The dots indicate higher-order corrections coming from loop diagrams and contact interactions with insertions of the quark masses and/or derivatives. These corrections start at relative $\mathcal{O}(Q^2/\Lambda_{\chi}^2)$ and are discussed in detail in a separate paper [16]. From the NDA estimate in Eq. (5) we have

$$\Gamma_{p,n} = \mathcal{O}\left(\frac{\Lambda_{\chi}^5 \mathcal{C}^2}{(4\pi)^4}\right) \sim 10^{-4} \mathcal{C}^2 \,\mathrm{GeV}^5 \,\,. \tag{9}$$

This estimate of the inclusive proton and neutron decay rate is consistent with lattice QCD calculations of the decay to a meson and a positron or antimuon, where the largest contribution to the decay rate is $\simeq 3 \cdot 10^{-4} C^2 \text{ GeV}^5$ [17].

To calculate the deuteron decay rate we need to include two-nucleon (NN) interactions. The scattering length in the ${}^{3}S_{1}$ channel is unnaturally large, which is related to the small binding momentum of the deuteron, $\kappa = \sqrt{m_{N}B_{d}} \simeq 45$ MeV, with $B_{d} \simeq 2.225$ MeV the deuteron binding energy. This translates in χ EFT to NN LECs with magnitudes larger than expected by NDA [18, 19]. With this enhanced scaling the leading-order (LO) NNinteraction must be iterated to all orders, resulting in an S-matrix pole associated with the deuteron bound state. Subleading contact interactions and pion exchange between nucleons can be treated perturbatively in an expansion Q/Λ_{NN} , where $Q \sim m_{\pi} \sim \kappa$ and $\Lambda_{NN} \equiv 4\pi F_{\pi}^{2}/g_{A}^{2}m_{N} \sim F_{\pi}$. The same scheme has been used to successfully compute the electromagnetic form factors of the deuteron [20–23] and NN scattering up to center-of-mass momenta around 100 MeV [24].

The Lagrangian for NN contact interactions is

$$\mathcal{L}_{NN} = -\left(C_0 + D_2 m_\pi^2\right) \left(N^T P_i N\right)^{\dagger} \left(N^T P_i N\right) + \frac{C_2}{8} \left\{ \left(N^T P_i N\right)^{\dagger} \left[N^T P_i (\vec{\nabla} - \vec{\nabla})^2 N\right] + \text{H.c.} \right\} + \dots , \qquad (10)$$

where $P_i \equiv \sigma_2 \sigma_i \tau^2 / \sqrt{8}$ projects an NN pair onto the isospin-singlet 3S_1 state and C_0 , D_2 , and C_2 are LECs. The operator with the LEC Re $C_0 = \mathcal{O}(4\pi/m_N\kappa)$ is the LO interaction that is iterated to all orders. It produces a bound state with binding momentum κ if [18]

$$\operatorname{Re} C_0 = \frac{4\pi}{m_N(\kappa - \mu)} + \dots , \qquad (11)$$

where μ is the renormalization scale. Re $C_2 \sim \text{Re } D_2 = \mathcal{O}(4\pi/m_N\kappa^2\Lambda_{NN})$ are LECs contributing to NN scattering at next-to-leading order (NLO) in the Q/Λ_{NN} expansion. The imaginary part of the NN LECs is produced by two insertions of $|\Delta B| = 1$ physics. With a Λ_{NN}^2/κ^2 enhancement over NDA due to renormalization by the LO NN interaction,

$$\operatorname{Im} C_0 = \mathcal{O}\left(\frac{\Lambda_{NN}^4 \mathcal{C}^2}{\kappa^2}\right) \,. \tag{12}$$

By requiring NN scattering amplitudes to be independent of the renormalization scale, we find that $\text{Im } C_0$ must satisfy the renormalization-group equation

$$\frac{\mathrm{d}}{\mathrm{d}\mu}\mathrm{Im}\,C_0 = \frac{m_N}{2\pi}\mathrm{Re}(C_0)\,\mathrm{Im}\,C_0 + \dots \,. \tag{13}$$

The deuteron decay rate is obtained from the imaginary part of the deuteron propagator. Following Ref. [20], the propagator of a deuteron with four-momentum p^{μ} = $(2m_N + \vec{p}^2/4m_N + \bar{E} + \dots, \vec{p})$ can be written in terms of the irreducible two-point function $\Sigma(\bar{E})$, which consists of all diagrams that do not fall apart when cutting any Re C_0 vertex,

$$G_d(\bar{E}) = \frac{\Sigma(\bar{E})}{1 + i \operatorname{Re}(C_0) \Sigma(\bar{E})} = \frac{iZ_d}{\bar{E} + B_d + i\Gamma_d/2} + \dots, \qquad (14)$$

where we expanded around $\overline{E} = -B_d$. Z_d is the deuteron wavefunction renormalization factor and

$$\Gamma_d = \frac{2 \operatorname{Im}(i\Sigma(\bar{E}))}{\operatorname{Re}(\operatorname{d}i\Sigma(\bar{E})/\operatorname{d}\bar{E})}\Big|_{\bar{E}=-B_d} + \dots$$
(15)

is the deuteron decay rate. Up to NLO [20],

$$\operatorname{Re}\left(\frac{\mathrm{d}i\Sigma(\bar{E})}{\mathrm{d}\bar{E}}\right)\Big|_{\bar{E}=-B_d} = \frac{m_N^2}{8\pi\kappa} \left\{ 1 + \frac{m_N}{2\pi}(\kappa-\mu)\left[\kappa(\mu-2\kappa)\operatorname{Re}C_2 + m_\pi^2\operatorname{Re}D_2\right] + \frac{2}{\Lambda_{NN}}\left(\kappa-\mu + \frac{m_\pi^2}{m_\pi+2\kappa}\right) \right\}.$$
(16)

The diagrams that contribute to $\text{Im}(i\Sigma(\bar{E}))$ up to NLO are shown in Fig. 2. Each loop counts as $Q^5/4\pi m_N$, each nucleon propagator as m_N/Q^2 , and each pion propagator as $1/Q^2$. The diagrams in Fig. 2 describe deuteron decay as illustrated in Fig. 1(a). Figure 2(a) contributes at LO and Fig. 2(b,c) at NLO. They amount to

$$\operatorname{Im}(i\Sigma(-B_d)) = \frac{m_N^2}{8\pi\kappa} \operatorname{Im} \alpha_0 \left\{ 1 + \frac{m_N}{2\pi} (\kappa - \mu) \left[\kappa(\mu - 2\kappa) \operatorname{Re} C_2 + m_\pi^2 \operatorname{Re} D_2 \right] + \frac{2}{\Lambda_{NN}} \left(\kappa - \mu + \frac{m_\pi^2}{m_\pi + 2\kappa} \right) \right\}.$$
(17)

Substituting Eqs. (16) and (17) into Eq. (15) we find for the decay rate up to NLO

$$\Gamma_d = 2 \operatorname{Im} \alpha_0 = \Gamma_p + \Gamma_n , \qquad (18)$$

where in the last equality we used Eqs. (7) and (8).

The contributions to Γ_d from the NLO diagrams in Fig. 2(b,c) cancel against the Re C_2 , Re D_2 , and pion terms in Eq. (16). This cancellation is not accidental. The derivative with respect to \bar{E} acts on the nucleon propagators and effectively adds an additional propagator with the same momentum. The resulting term then cancels against the corresponding diagrams contributing to Fig. 2. This cancellation also works at higher orders. For example, additional insertions in Fig. 2 of Re C_2 and Re D_2 vertices and/or pion exchanges proportional to g_A^2 before or after the Im α_0 vertex cancel against similar corrections to the two-point function in Re $(di\Sigma(\bar{E})/d\bar{E})|_{\bar{E}=-B_d}$.

The first non-zero correction to the deuteron decay rate arises from the diagram shown in Fig. 3(a). This diagram describes deuteron decay via a short-range interaction between the nucleons, as illustrated in Fig. 1(b). Following the power counting rules and using the NDA estimate for Im C_0 in Eq. (12), it is expected to contribute at relative $\mathcal{O}(\kappa \Lambda_{NN}/\Lambda_{\chi}^2) \sim 10^{-2}$.

Long-range nuclear effects in which one or more low-energy pions are emitted from the vertex describing nucleon decay can also affect the deuteron decay rate. The lowest-order diagram of this type is shown in Fig. 3(b), which is expected at relative $\mathcal{O}(\kappa^2/\Lambda_{\chi}\Lambda_{NN}) \sim$



FIG. 2. Diagrams contributing to the deuteron decay rate up to NLO. The solid square denotes an $\text{Im }\alpha_0$ vertex, the solid circle a g_A vertex, and the encircled circle a $\text{Re }C_2$ or $\text{Re }D_2$ vertex. Other notation as in Fig. 1.



FIG. 3. Higher-order diagrams contributing to the deuteron decay rate. The squared square denotes an $\text{Im } C_0$ vertex. Other notation as in Figs. 1 and 2.

 10^{-2} — that is, comparable to the diagram in Fig. 3(a). However, the diagram in Fig. 3(b) vanishes: the integrand of the loop integral is odd in three-momentum because the nucleon decay vertex emitting a pion has no derivative (see Eq. (4)) while the g_A vertex has one spatial derivative. Replacing one of the pion-nucleon vertices by a subleading vertex with one additional derivative leads to a suppression of $\mathcal{O}(\kappa/\Lambda_{\chi})$. Long-range nuclear effects affecting the deuteron decay rate are therefore expected at $\mathcal{O}(\kappa^3/\Lambda_{\chi}^2\Lambda_{NN}) \sim 10^{-3}$ or higher.

The part of the Lagrangian in Eq. (4) that comes from $|\Delta B| = 1$ physics has at the next order terms with a time derivative that cannot be removed by a field redefinition without the appearance of time-derivative terms beyond LO in the *B*-conserving part [16]. The corrections to the deuteron decay rate due to these terms appear at relative $\mathcal{O}(\kappa^2/\Lambda_{\chi}^2)$ and are thus of higher order than our estimate for the correction from the diagram in Fig. 3(a).

We conclude that the deuteron decay rate is dominated by the sum of the proton and neutron decay rates, Γ_p and Γ_n , with a correction at relative $\mathcal{O}(\kappa \Lambda_{NN}/\Lambda_{\chi}^2)$, viz.

$$\Gamma_d = \Gamma_p + \Gamma_n - \frac{\kappa}{\pi} (\kappa - \mu)^2 \operatorname{Im} C_0 , \qquad (19)$$

where further corrections are expected at relative $\mathcal{O}(\kappa^2/\Lambda_{\chi}^2)$. The contribution from the LEC Im C_0 is independent of the renormalization scale μ , as can be seen from Eq. (13). It represents the first nuclear correction to the deuteron decay rate. It is presently unknown, but it is expected to be small, of the order of a few percent.

That nucleon decay rates dominate the deuteron decay rate agrees with earlier, modelbased calculations [25, 26]. However, Refs. [25, 26] found larger nuclear corrections than we do. The reason for this discrepancy is not clear because the theoretical frameworks are very different. While we describe *B*-conserving and *B*-violating interactions within the same EFT, Refs. [25, 26] use phenomenological wavefunctions to represent the deuteron and pion interactions for two-nucleon B-violating corrections. The strong-interaction pionnucleon vertex is assumed to be pseudoscalar instead of pseudovector. The latter conforms to chiral symmetry directly, as it gives a derivative pion interaction appropriate for a (pseudo) Goldstone boson. The former vertex satisfies chiral symmetry only when it is accompanied by a seagull vertex, as can be seen by a field redefinition — see, for example, Ref. [27]. The seagull ensures "pair suppression" of the so-called Z diagrams. When the seagull is not included, pseudoscalar coupling can give anomalously large results, for example in pion-nucleon scattering and the closely related pion production in nuclear collisions [28]. An explicit example of this spurious enhancement involving BSM physics is the neutron electric dipole moment [29]. Not surprisingly, the result of Ref. [26] is very sensitive to the introduction of a form factor in the pion-nucleon vertex: a reduction factor ~ 5 for phenomenological forms. Moreover, in the absence of a form factor the result of Ref. [25] depends sensitively on the deuteron wavefunction at small distances: a reduction of ~ 20 when a hard core is added to a Hulthén-type wavefunction.

In contrast, our result Eq. (19) is free of these inconsistencies, but our estimate of the magnitude of nuclear corrections relies on Eq. (12). Since it connects two S waves, this LEC contains an enhancement of two powers of Λ_{NN}/κ associated with the shallowness of the deuteron. Apart from this low-energy enhancement, its size estimate is based on NDA. At the one-nucleon level NDA is not inconsistent with lattice data, see Eq. (9), but it has not been tested for B violation at the two-nucleon level. Eventually Im C_0 can be determined by matching Eq. (19) to the deuteron decay rate calculated in lattice QCD. The same value of the LEC can then be used in the calculation of the decays of heavier nuclei.

The low binding energy of the deuteron allowed for a perturbative treatment of pion exchange and, as a consequence, for an analytical calculation in EFT. This calculation is based on an enhanced scaling of NN couplings — which absorb the effect of pions with momentum above the scale Λ_{NN} — with respect to NDA. The same framework can be used for other light nuclei, where the binding energy per particle is relatively small for a review, see Ref. [30]. For heavier nuclei, with a larger binding energy per nucleon, pion exchange might not be amenable to perturbation theory. Even though the calculation with non-perturbative pions cannot be done analytically, we can still apply power counting arguments to get an estimate of the relative importance of various contributions. In this case the typical momentum is $Q \sim \Lambda_{NN}$ and there is no low-binding enhancement in contact interactions. With NDA, we find that the decay is still dominated by free-nucleon decay. Non-zero corrections from Im C_0 and from one-pion exchange are now expected to appear at the same order, that is, relative $\mathcal{O}(\Lambda_{NN}^2/\Lambda_{\chi}^2) \sim 10^{-2}$. Therefore, to a good accuracy, experiments attempting to detect $\Delta B = 1$ nuclear decay rates can be interpreted as $\Delta B = 1$ nucleon-decay measurements.

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- [1] K. S. Babu *et al.*, arXiv:1311.5285 [hep-ph].
- [2] K. Abe et al. [Super-Kamiokande Collaboration], Phys. Rev. D 95, 012004 (2017).
- [3] K. Abe et al. [Super-Kamiokande Collaboration], Phys. Rev. Lett. 113, 121802 (2014).
- [4] F. Oosterhof, MSc Thesis, University of Groningen (2016).
- [5] J. Bijnens and E. Kofoed, Eur. Phys. J. C 77, 867 (2017).
- [6] F. Oosterhof, B. Long, J. de Vries, R. G. E. Timmermans, and U. van Kolck, Phys. Rev. Lett. 122, 172501 (2019).
- [7] J. Haidenbauer and U.-G. Meißner, Chin. Phys. C 44, 033101 (2020).
- [8] S. Weinberg, Phys. Rev. Lett. 43, 1566 (1979).
- [9] F. Wilczek and A. Zee, Phys. Rev. Lett. 43, 1571 (1979).
- [10] L. F. Abbott and M. B. Wise, Phys. Rev. D 22, 2208 (1980).
- [11] M. Claudson, M. B. Wise, and L. J. Hall, Nucl. Phys. B195, 297 (1982).
- [12] S. Weinberg, Physica A **96**, 327 (1979).
- [13] S. Weinberg, Phys. Lett. B **251**, 288 (1990).
- [14] A. Manohar and H. Georgi, Nucl. Phys. **B234**, 189 (1984).
- [15] U. van Kolck, Eur. Phys. J. A 56, 97 (2020).
- [16] F. Oosterhof, J. de Vries, R. G. E. Timmermans, and U. van Kolck, in preparation.
- [17] Y. Aoki, T. Izubuchi, E. Shintani, and A. Soni, Phys. Rev. D 96, 014506 (2017).
- [18] D. B. Kaplan, M. J. Savage, and M. B. Wise, Phys. Lett. B 424, 390 (1998).
- [19] P. F. Bedaque and U. van Kolck, Ann. Rev. Nucl. Part. Sci. 52, 339 (2002).
- [20] D. B. Kaplan, M. J. Savage, and M. B. Wise, Phys. Rev. C 59, 617 (1999).
- [21] M. J. Savage and R. P. Springer, Nucl. Phys. A686, 413 (2001).
- [22] J. de Vries, E. Mereghetti, R. G. E. Timmermans, and U. van Kolck, Phys. Rev. Lett. 107, 091804 (2011).
- [23] E. Mereghetti, J. de Vries, R. G. E. Timmermans, and U. van Kolck, Phys. Rev. C 88, 034001 (2013).
- [24] S. Fleming, T. Mehen, and I. W. Stewart, Nucl. Phys. A 677, 313 (2000).
- [25] C. B. Dover, M. Goldhaber, T. L. Trueman, and L.-L. Chau, Phys. Rev. D 24, 2886 (1981).
- [26] R. F. Alvarez-Estrada and J. L. Sanchez-Gomez, Phys Rev. D 26, 175 (1982).
- [27] S. A. Coon and J. L. Friar, Phys. Rev. C 34, 1060 (1986).
- [28] T. D. Cohen, J. L. Friar, G. A. Miller, and U. van Kolck, Phys. Rev. C 53, 2661 (1996).
- [29] C. Y. Seng, J. de Vries, E. Mereghetti, H. H. Patel, and M. Ramsey-Musolf, Phys. Lett. B 736, 147 (2014).
- [30] H. W. Hammer, S. König, and U. van Kolck, Rev. Mod. Phys. 92, 025004 (2020).

Declaration of interests

 $X\square$ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: