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F. Galtarossa, M. Pierens, M. Assié, V. Delpech, F. Galet, et al.. HeCTOr: the 3 He Cryogenic Target of Orsay for direct nuclear reactions with radioactive ion beams. Nucl.Instrum.Meth.A, 2021, 1018, pp.165830. 10.1016/j.nima.2021.165830. hal-03235646

HAL Id: hal-03235646 https://hal.science/hal-03235646

Submitted on 9 Feb 2023

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HeCTOr: the ³He Cryogenic Target of Orsay for direct nuclear reactions with radioactive beams

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impinging on the light target at energies ranging from few to several hundreds MeV/u [4]. RIB intensities are several orders of magnitude lower than stable beams, and thus require high

ones are not specifically designed to be employed in experiments with low-energy (~ 10 MeV/u) and low-intensity (~ 10^4 - 10^5 pps) beams for transfer reactions. In particular some are conceived for measurements, like for instance electron scattering or photo-absorption, where temperatures lower than 4 K and/or target thicknesses of few cm are needed to reach areal densities of tens or hundreds of mg/cm² [6, 7, 8, 9, 11]. Others involve measurements with polarized ³He nuclei that can be

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performed also in storage rings, where densities of scattering centers of 10^{16} - 10^{18} atoms/cm² are sufficient [10, 12].

Valid alternatives conceived for low-energy nuclear reactions have been recently developed. Solid targets obtained by implantation [13, 14, 15, 16] have the advantage to be very compact and easy to handle, whereas the employ of windowless and gas jet targets [17, 18, 19] allows to strongly reduce background and stragglings generated in the target windows. In both cases, though, target thicknesses of the order of 1 mg/cm² are hardly reached.

In this paper we report on a ³He cryogenic target where densities of scattering centers of the order of 10²⁰ atoms/cm², normally sufficient to cope with low RIB intensities, are obtained with a target thickness of few mm and an operation temperature higher than 4K. These characteristics make it particularly suited to perform direct transfer reactions, such as (³He,d), $({}^{3}\text{He},p), ({}^{3}\text{He},n)$ and $({}^{3}\text{He},\alpha)$, with radioactive beams in inverse kinematics at bombarding energies ranging from few to tens of MeV/u. These reactions allow to tackle several interesting physics cases, among which we mention shell evolution along neutron shell closures, neutron-proton pairing in unstable nuclei, or proton drip-line physics. The outreach of physics programs dedicated to such studies will strongly profit from the installation of the target in fragmentation or next-generation European post-accelerated ISOL facilities, SPES [20] and HIE-ISOLDE [21], or the low-energy branch of FAIR [22].

2. Constraints on the target design

Properties of the reactions of interest, such as beam intensity and energy, type of reaction and detected reaction products, strongly constrain the design of the target and lead to several specific requirements. In this Section we will report general considerations that should be taken into account in the design of a cryogenic target for our purposes, in Section 3 we will describe in detail the specific design of HeCTOr.

Dimensions. The target has to be coupled to existing detectors which are usually arranged in compact configurations around a traditional foil target of small dimensions. For this reason the dimensions of the target and the associated cryogenic equipment have to be as reduced as possible. At the same time, the target radius must be large enough to give the possibility to deal with both ISOL and fragmentation beams. Typical ISOL beams have dimensions on target $\sigma \sim 2-3$ mm, while fragmentation beams can feature beam spots at least a factor of 2 larger.

Thickness. To measure transfer cross sections usually of the order of few mb with beams of low intensity (< 10^5 pps), the choice of the target thickness must balance the need of sufficient luminosity and good energy resolution. These two requirements go in opposite directions. High luminosity calls for the use of thick targets, of the order of few mg/cm², which can be obtained with a large target cell and operating at cryogenic temperatures. Good energy resolution, which mainly depends on energy losses, stragglings and re-interactions in the target, requires instead thin targets, usually of the order of $100 \,\mu g/cm^2$

or less. The best choice usually depends on the specific physics case.

Window thickness and material. The target windows should be as thin as possible to reduce stragglings, energy losses and contributions coming from background reactions. At the same time they should be thick and elastic enough to withstand considerable deformations due to the high difference in pressure between gas inside the target cell and vacuum around it.

Transparency. The frame surrounding the gas target must have an opening around the target as large as possible to allow the emitted particles to reach the detectors, thus increasing the detection efficiency. Very large openings would require thicker windows and are difficult to obtain due to mechanical constraints. The target can then be designed to have a larger opening in the hemisphere (forward or backward) where the laboratory cross section of the reaction channel of interest is higher. The transparency to electromagnetic radiation (X and γ rays) emitted by the reaction products can be another important requirement. This once again calls for a reduction and an accurate choice of the materials, surrounding the gas target, that might "shadow" the γ -ray detector, absorbing part of the electromagnetic radiation emitted by the reacting nuclei.

Target versatility. A good versatility is an essential property to cover a large number of physics cases without deeply modifying the set-up between different experiments. For instance, the possibility to change the gas inside the target cell, to modify its pressure and temperature and to switch forward and backward sides gives considerable flexibility to the target and allows to perform a large variety of reactions.

3. HeCTOr design and operation

In this Section we will describe the characteristics and operation principles of HeCTOr, the ³He cryogenic target developed at IJCLab and designed to perform direct reactions with radioactive beams in inverse kinematics from few to tens of MeV/u. All the requirements described in Section 2 have been carefully taken into account in its design. In Section 4 we will present the performance during the first in-beam experiment, where the target was coupled to the MUGAST [23] silicon array, the AGATA [24, 25] γ -ray array and the VAMOS [26] large-acceptance magnetic spectrometer.

The target cell. The target cell, shown in Fig. 1, is composed of a main copper frame to which two conic copper flanges are screwed, one on each side of the frame. A thin foil, serving as target window, is then glued to each flange with epoxy resin glue. The diameter of the smaller base of the cone is 16 mm, the frame thickness is 15 mm and the nominal target thickness is 3 mm. The nominal target thickness is defined as the distance between the two windows when ³He gas is at the nominal operation pressure of ~ 1 bar inside the target, neglecting window deformations. An indium wire is placed between the conic flange and the frame to avoid leakages at cryogenic temperatures between the ³He circuit and the vacuum around it.





Figure 2: Magnified view of the target cell. From left to right: conic flange, Havar window, indium wire and target frame. In the forward side the sequence is repeated in inverted order.

Figure 1: (Top) Photographs of the target cell without the thermal shield: a) backward side, from which the beam enters the target; b) forward side. (Bottom) CAD drawings of the target cell where the shield is added as a semitransparent layer: c) backward side; d) forward side. The rod connecting the target cell to the LHe tank is also visible.

The different parts composing the target cell can be seen in the magnified view of Fig. 2.

A coil-shaped copper thermalization block is brazed at the bottom of the frame to ensure good thermal contact and operates as a heat exchanger to cool down the target by means of liquid ⁴He flowing through it. The block contains a pipe with an inner and outer diameter of 4 mm and 6 mm, respectively.

The conic flange has a larger angular opening (130°) in the backward hemisphere to adapt for stripping reactions², like (³He,d) or (³He,p), where the light recoiling particles are mainly scattered at $\theta_{lab} > 90^{\circ}$. The target could also be filled with ⁴He when necessary. For pick-up reactions, where the ejectiles are mainly scattered forward, like (³He,⁴He) but also (⁴He, ⁶He) or (⁴He, ⁸Be), it can be rotated to adapt to the specific reaction.

For the target windows the considerations outlined in Section 2 led to the choice of $3.8-\mu$ m thick foils of Havar, an alloy of cobalt (42 %), chromium (20 %), nickel (2.7 %), tungsten (2.2%) and other materials in smaller percentage. The corresponding areal density of each foil is 3.15 mg/cm². The typical

pressure of gas in the target is 1 bar absolute. The relatively high pressure and the elasticity of Havar induce a deformation of the windows, defined as the maximum distance along the beam direction between the nominal target thickness and the Havar window. Such deformation is measured using a micrometric probe placed in the center of the target window. A first measurement is made with the same (atmospheric) pressure in the gas target and around it. A second one is carried out setting a pressure of 2 bars inside the target and atmospheric pressure around it, in order to have a pressure difference of 1 bar, as in the case of nominal operation. The difference between the two values gives the window deformation, measured to be (0.70 ± 0.05) mm at room temperature. Thanks to the properties of Havar, a similar value is expected also at cryogenic temperatures (5-6K). When it is cooled down to such temperatures, the equivalent areal density of ³He gas is $\sim 2 \text{ mg/cm}^2$ and the density of scattering centers is $\sim 3.5 \cdot 10^{20}$ atoms/cm², about 2-3 orders of magnitude higher than what can be obtained with typical solid ³He-implanted or gas jet targets. Since a small gradient of temperature is present along the cooling circuit in the gas cell region, the target temperature is determined as the average of the temperatures measured by two probes, visible in Fig. 1 (top), placed at the top and bottom of the target cell.

Cryostat description. The small volume of ³He gas contained in the target cell is cooled down to cryogenic temperatures by circulating liquid ⁴He (LHe) around the target region. The LHe is initially injected in the system from the top of the cryostat, defined as the assembly of HeCTOR, visible in Fig. 3, and the MUGAST vacuum chamber (refer also to Fig. 4, where the

²The expressions *stripping* and *pick-up* may be confused when the reaction occurs in inverse kinematics. Here and later in the text we always refer these expressions to the light particle, so in a stripping (pick-up) reaction the light target particle loses (gains) nucleons.

cryostat is enclosed by the dashed gray line). The LHe is then stored in the tank, or phase separator (T1), from which it can finally reach the target. To minimize the consumption and allow the LHe to maintain the cryogenic temperature, a thermal shield is provided by liquid nitrogen (LN₂) at atmospheric pressure and at a temperature of about 77 K, measured with a PT100 (TT02) placed at the bottom of the LN₂ tank (T2).

The target is insulated from the external environment through the outer wall of the cryostat, composed in the upper part of a cylindrical vessel made of AISI 304L stainless steel, with an outer diameter of 450 mm and a length of about 900 mm, and in the lower part of the MUGAST vacuum chamber. The LN_2 and LHe circuits, comprising the LN_2 and LHe tanks and the ³He gas target, are hosted inside the outer wall. The target is supported by a glass-epoxy rod, a heat-insulating material, with a length of 812 mm, an inner diameter of 28 mm and an outer diameter of 30 mm, attached to the LHe tank T1. The total height of HeCTOr, from the top of the vessel to the bottom of the target cell, is approximately 1.73 m.



Figure 3: (Left) Photograph of HeCTOr. (Right) CAD drawing of HeCTOr. The cylindrical vessel is semi-transparent to allow the visualization of the LN_2 tank. The two asymmetric hemicylindrical sheets enclosing the glass-epoxy rod connect the bellow to the target cell.

this figure the outer wall, which can be seen as the first layer of insulation, is represented by the dotted gray line. A second layer, in orange, is maintained at LN_2 temperature and acts as a thermal shield to insulate the cold gas target from radiations from the vacuum vessel at room temperature. This shield is composed at the top of the LN_2 tank and its cover (orange dashed line) and in the central part of two 1.5-mm thick sheets of copper with an asymmetric hemicylindrical-like shape that connect the tank T2 to the target cell and enclose the glassepoxy rod (see Fig. 3 right). These sheets are mechanically and thermally anchored to the tank and cooled by thermal conduction. The bottom of the thermal shield covers the target cell, as shown in Fig. 1 (bottom), to protect the cold mass from the room temperature. A cut of the sheets is made at the level of the target windows to ensure transparency to the beam.

The thermal shield is covered by a multi-layer insulation (MLI), or super-insulation), where each layer acts as a thermal shield, reducing the radiated heat transfer from the vacuum vessel to the shield. MLI consists of stacks of double-aluminized Mylar to reflect heat radiation, separated by low-conduction spacers to limit heat transfer by conduction. The temperature of each layer is left floating and then depends on the global thermal equilibrium of the system. MLI reduces the heat radiated to the cold mass by a factor ~ 200 with respect to the case where it is not present. The upper part of the shield and the cold mass are covered by 30 and 10 layers of MLI, respectively.

The cooling circuit includes the tank T2 with an annular shape and a capacity of about 13 L, a filling and an exhaust line. The tank T2 is supplied with LN_2 flowing out of a Dewar connected via a flexible vacuum-insulated transfer line on top of the cryostat. The cold vapors are warmed at the outlet of the circuit before returning to the atmosphere, avoiding ice formation at the exhaust of the cryostat.

The cold mass, or Helium-4 circuit, shown in blue in Fig. 4 and indicating the ³He gas target and its active cooling circuit, is located at the center of the system. LHe at atmospheric pressure is used to maintain the target temperature below 7 K. The circuit includes the cylindrical phase separator T1 with a useful capacity of about 11 L, filled by a LHe Dewar via a vacuum-insulated and flexible transfer line. The cold vapors return to the atmosphere through the outlet pipe where the presence of an electrical heater avoids the formation of ice. The ³He cryogenic gas target is cooled down by means of LHe coming from T1 and passing through the coil-shaped thermalization block brazed at the bottom of the copper frame. Cold vapors from the boiling helium are returned to the top of the phase separator and flow out of the cryostat via the tank outgassing line.

The Helium-3 circuit includes, outside the cryostat, a setup based on a dry primary vacuum pump to inject or recover the gas in the target inside the cryostat and a tank with a volume of 90 L for the ³He gas storage at sub-atmospheric pressure (28 mbar). To fill the target with ³He gas, the pump is turned on and the valves SV01 and SV02 are opened. The needle valve NV01 moderates the flow to the target to limit sudden pressure changes. For the gas recovering procedure the pump is switched on and the valves SV03 and SV04 are opened. The back-pressure regulator BPR01 prevents the target from over-

The operation scheme of the cryostat is shown in Fig. 4. In



Figure 4: Scheme illustrating the piping and instrumentation diagram of HeCTOr (see text for details).

pressure, while BPR02 protects the pump. The ³He circuit in the cryostat acts as a filling and recovery line to set the pressure in the target.

The isolation vacuum level is measured by means of a combined Pirani and Penning vacuum gauges. We have available a test bench with a dedicated small chamber where the target can be accommodated. In this configuration, the vessel with a volume of about 156 L is pumped by a turbomolecular pump with a pumping speed of 150 L/s in series with a primary rotary vane pump with a pumping speed of 8 m³/h, allowing to reach a vacuum of about 10^{-5} mbar absolute at 300 K. When the system is cold, there is a gain of an order of magnitude on the vacuum level. The LN₂ Dewar is provided with a self-pressurization system and the transfer is controlled by an ON-OFF pneumatic valve (PV600). A high and low thresholds are set on the LN₂ level in the tank to automatically stop and start the transfer procedure. A PT100 thermometer (TT02) is installed at the bottom of the tank to check in particular the first filling during the cooldown process, since it represents the most delicate step. The LHe Dewar is equipped with a heater (EH01), a back-pressure regulator (BPR03) and a solenoid valve (EV01) to pressurize

the Dewar. When a transfer is needed EV01 is closed, forcing the gas to flow through the back-pressure regulator BPR03 with a pressure inside the Dewar set to about 1.1 bar, and the heater is activated to produce vapors. This increases the pressure in the Dewar, allowing a transfer of LHe via the activation of the pneumatic valve PV01. A pressure transmitter (PTLHE) monitors the pressure of the Dewar. A LHe level sensor measures the quantity of LHe remaining in the Dewar while a second one monitors the level of the liquid in the tank inside the cryostat to start and stop the transfer. CernoxTM 1050 AA thermometers are located at the bottom of the LHe tank (TT01), on top and at the bottom of the target (TT04 and TT05), on the thermalization block (TT03) and on the outgassing of the cooling circuit of the target (TT06). The pressure of the ³He storage tank and of the target are measured by piezoresistive pressure sensors (PIPT01 and PIPT02, respectively).

The acquisition and actuators controls are performed by means of a multiplexer Agilent 34970A equipped with two 34901A cards to measure resistances in four-wires mode, LHe level (4-20 mA) and pressure sensors (0-10 VDC). A 34903A relays card is used to activate the heater of the LHe Dewar and the ON-OFF valves. A LabVIEW program communicates with the multiplexer to manage LN_2 and LHe transfers and provides system supervision and data logging.

Cryostat operation. The first step in the procedure to cool down the target is to pump the vacuum vessel below 10^{-5} mbar at room temperature. In the experimental configuration described in Sec. 4 the target is accommodated in the MUGAST reaction chamber, with a volume of 515 L. To make the vacuum we employed a primary pump Agilent IDP-10, two turbomolecular pumps Agilent Turbo-V750 TwisTorr (model 9696018) with a pumping speed of 700 L/s for N₂ and a cryogenic pump, composed of a compressor unity Coolpak 4000 Leybold and a cold head Cryo-plex 8 model 350 Oxford instruments. This pumping system allowed to reach a vacuum level of 10^{-6} mbar.

The LN₂ circuit does not need a specific conditioning. By opening the PV600 valve, LN₂ starts to flow out of the Dewar towards the cryostat and the air remained in the circuit is flushed. For the LHe circuit, the high risk of blocking due to the possible solidification of air in the circuit prevents from carrying out the same simple procedure. The circuit is then conditioned by pumping it below 1 mbar and injecting ⁴He gas slightly above the atmospheric pressure. This operation is then repeated at least three times. The ³He circuit is pumped down to 10^{-6} mbar via the purging port (HV01) with all solenoid valves opened and isolated by closing HV01 and then the solenoid valves.

The thermal shield is cooled down to 77 K by means of LN_2 . When the nominal working mode is reached the temperature is maintained stable keeping the LN_2 level between the high (LS01) and low (LS02) level until the end of the experiment. The ⁴He circuit is cooled down by pressurizing the Dewar and opening the transfer valve PV01 until the tank T1 is filled. The cooling circuit of the target starts and, when the target reaches an equilibrium temperature of about 7 K, the target operation can start. The quantity of LHe needed to cool the target down to this temperature is about 200 L.

Once the cryostat is working in nominal conditions, the hand valve HV02 is opened and the target is filled with ³He gas to atmospheric pressure and maintained during the experiment. The power consumption of the target at equilibrium is ~ 1.7 W.

After the experiment, the LN_2 and LHe supply are stopped simultaneously and the cryostat begins to warm up until the room temperature is reached. The ³He gas is recovered and stored in the tank at low pressure. The ³He gas is not purified after each operation but only when a possible contamination with other gases might have occurred during the target operation. In such a case the tank can be connected to a specific purification tool, composed of a cold trap, to eliminate impurities from the gas.

4. Performance during the experiment

HeCTOr has been employed for the first time in an in-beam experiment in June 2019 at GANIL [27] in Caen, France. The aim of the experiment was the determination of the proton occupancies in the ground state of the N=28 46 Ar isotope,

which can be achieved measuring the differential cross sections of the deuterons emitted in the proton stripping reaction ${}^{46}\text{Ar}({}^{3}\text{He},\text{d}){}^{47}\text{K}$.

In this Section we will describe the experimental set-up employed in GANIL and the performance of HeCTOr. This will allow us to extract and discuss important experimental quantities that must be evaluated when designing and analyzing an experiment with such a target, in particular stability over time (Section 4.1), energy losses (Section 4.2), energy resolution (Section 4.3), and transparency to γ rays (Section 4.4).

4.1. Experimental conditions and beam monitoring

The SPIRAL1 [28] ⁴⁶Ar beam, produced by the fragmentation of ⁴⁸Ca, is re-accelerated at 10 MeV/u and impinges on the ³He gas target with an intensity of approximately $4 \cdot 10^4$ pps. Along the beam line, about 2 m before the target, a beam tracking device, CATS [29], provides beam rate and profile monitoring and a signal for time-of-flight measurement.



Figure 5: A drawing of the experimental set-up at GANIL.

The detection set-up, shown in Fig. 5, is composed of the segmented silicon array MUGAST [23], coupled to the highresolution segmented HPGe array AGATA [24, 25] and the large-acceptance magnetic spectrometer VAMOS [26]. This set-up allows the simultaneous detection in coincidence of both reaction partners and the γ rays emitted by the heavy recoil. The MUGAST array is composed of 12 Double-sided Strips Silicon Detectors (DSSD) surrounding the target: 5 trapezoidal and one annular detector in the backward hemisphere, two square detectors close to 90° and 4 MUST2 [30] detectors at forward angles. The light ejectiles (deuterons in this case) are identified through E-ToF correlation and their scattering angle and energy are measured with an angular resolution better than 1 degree and an intrinsic energy resolution of $\sim 40 \text{ keV}$. The excitation energy of the heavy recoil (47K) is then determined via twobody kinematics. AGATA is placed upstream with respect to MUGAST and detects the γ rays emitted by the reacting nuclei. The typical efficiency of AGATA at 18 cm from the target, with MUGAST installed, is 6-7 % for 1.3-MeV γ rays. VAMOS is placed at 0° for the detection of the heavy residue and its identification in atomic number and mass. The coincidence with VAMOS allows to strongly suppress contributions from other reaction channels, in particular fusion-evaporation reactions on the target windows. Further details on the detection set-up can be found in Ref. [23].

The target system, inserted in the chamber from the top with a crane and secured to a mechanical support attached to the chamber, is placed 25 mm downstream with respect to the nominal target position, due to mechanical constraints, and cooled down to $\sim 6 \text{ K}$ before the beginning of the beam time.

The ⁴⁶Ar beam ions passing through the target are detected in the focal plane detectors of VAMOS and separated depending on their magnetic rigidity $B\rho$, according to:

$$B\rho = 3.105 \cdot \beta \gamma \, \frac{A}{q} \tag{1}$$

where A and q are the mass number and atomic charge of the ions, respectively, $\beta = v/c$ (v is the velocity of the ions) and $\gamma = (1 - \beta^2)^{-1/2}$.

When the target is empty the beam particles lose energy passing through the CATS detector and the two Havar windows. When the target is filled with ³He the energy loss of beam and light ejectiles in the gas has to be considered as well. By monitoring the temperature and pressure of the gas in the target cell during the whole experiment, possible changes in the gas density can be identified and accounted for. Figure 6 shows the trend of the target temperature (in blue) and pressure (in red) as a function of time during 4 days of experiment. The t = 0 reference has been arbitrarily set at the midnight of the day when the experiment started and has been kept the same in Figure 7.



Figure 6: Plot of the temperature in K (blue) and pressure in mbar (red) of the target during 4 days of experiment. The small spikes occurring approximately each 6 hours, and visible mainly in the temperature curve, are in correspondence of the filling of the LHe tank.

We started to fill the target with ³He at t ~ 19 h, reaching the final pressure of 700 mbar at t ~ 27.5 h. During the filling and the rest of the experiment the target temperature remained stable and close to 6 K. At this temperature and pressure the ³He density is 4.5 mg/cm³. The maximum target deformation, measured to be 0.7 mm per side at 1 bar pressure, scales down to 0.5 mm for a pressure of 700 mbar. The corresponding areal density is ~ 2 mg/cm² and the density of ³He scattering centers is ~ $3.5 \cdot 10^{20}$ atoms/cm². The level of vacuum in the chamber,

stable during the whole experiment, was $1.5 \cdot 10^{-6}$ mbar. The small increases in temperature and pressure occurring approximately each 6 hours, visible in Fig. 6, are due to the change of pressure occurring in the thermalization block when the LHe transfer process starts. Such change temporarily interrupts the LHe circulation in the pipe, causing a small increase of the temperature. Then, when LHe starts to flow again, the temperature eventually decreases.

The target thickness can be determined and monitored over time during the experiment by measuring the change in beam ion velocity after the target with VAMOS, according to Eq. 1, and computing the corresponding energy loss in the target. The top panel of Fig. 7 shows the experimental $B\rho$ for a time interval of ~ 40 h after the target filling procedure has been completed. Six main structures are visible, corresponding to the most intense charge states of beam ions detected in VAMOS (from 13⁺ to 18⁺). The intervals where no $B\rho$ information is available represent periods of time where the beam was not delivered. The $B\rho$ is clearly not constant over time but decreases smoothly, in turn indicating a progressive decrease of the velocity of beamlike ions reaching the VAMOS focal plane. This behavior might be explained assuming that the target thickness, instead of being constant, slightly increases over time. Since the temperature and pressure in the target are stable (see Fig. 6), the increase of target thickness could be associated to the thickening of layers of ice forming on the target windows through the deposit of frozen gas, probably coming from the MUGAST cooling system. The presence of other contaminants, like air coming from out of the reaction chamber or small quantities of gas coming from the gas detectors of the VAMOS focal plane, cannot be a priori excluded.

A rough estimation of the expected rate of ice growth can be obtained through simple considerations of kinetic theory of gases, in the approximation of ideal gas. Under the assumption that the velocity of the gas particles in the surroundings of the target follows the Maxwell's distribution, it can be shown that the number of collisions per unit time and unit area is given by:

$$N_c = \frac{1}{4}n\bar{\nu} = \frac{P}{\sqrt{2\pi mk_B T}}$$
(2)

where $n = P/(k_BT)$ is the volumic density of molecules, $\bar{v} = \sqrt{8k_BT/(\pi m)}$ is the mean velocity of the Maxwell distribution, k_B is the Boltzmann constant, T and P the gas temperature and pressure, respectively, and m the mass of the gas molecules. Due to the very low temperature of the surface, the molecules will stick to it after the collision. A monolayer of thickness d₀ is then formed in a time:

$$t_m = \frac{1}{AN_c} = \frac{4}{d_0^2 n\bar{\nu}} \tag{3}$$

where $A = d_0^2$ is the area of a molecule. The volume of a molecule in the ice can be approximated as $d_0^3 = M/(N_A\rho)$ where M is the molar mass, N_A the Avogadro number and $\rho \sim 10^3 \text{ kg/m}^3$ the ice density. The resulting monolayer thickness is $d_0 \sim 3 \text{ Å}$. With the appropriate substitutions, Eq. 3 can



Figure 7: (Top) Experimental B ρ as a function of time for ~ 40 h after the filling of the target with ³He. (Bottom) Same as the top panel but with the simulated B ρ distribution superimposed in black.

be rewritten as:

$$t_m = \frac{\sqrt{2\pi k_B T}}{P} \rho^{2/3} \left(\frac{N_A}{M}\right)^{1/6} \tag{4}$$

For the present experiment $P = 1.5 \cdot 10^{-6}$ mbar, T = 300 K. Assuming in a first approximation that the gas is coming only from the cooling system of MUGAST, its composition is 50% water ($M_{H_2O} = 18.02$ g/mol) and 50% ethyl alcohol ($M_{C_2H_6O} = 46.07$ g/mol), so an average value M ~ 32 can be considered. A detailed study of the gas composition would require a dedicated measurement and is beyond the aim of this simple calculation. Substituting these values in Eq. 4, we obtain a monolayer formation time $t_m \sim 1.6$ s, corresponding to a rate of thickness growth per window of ~ 22 µm/day. This value is not expected to change dramatically if some impurities are added to the gas. Different inputs for M and ρ , to account for varied gas compositions, result in values of thickness growth per day which do not deviate by more than 50% from the present value.

The ice formation rate can be monitored experimentally by measuring the $B\rho$ of beamlike ions in VAMOS and computing the correspondent energy loss in the target. To this aim, we performed simulations with the Zgoubi code [31], where the incoming ions are propagated through the optics of the spectrometer and the energy losses in the different materials along the ion path are taken into account using SRIM [32]. In the simulation we can vary the ice thickness, under the assumption that the ice forms at the same rate on the front and back window, until a good matching between simulation and data is found. The result is shown in the bottom panel of Fig. 7, where the simulated $B\rho$ for the different charge states is superimposed in black on the experimental data. The ice thickness at the beginning of this plot (t ~ 35 h) has been set to $37 \,\mu m$ to reproduce the $B\rho$ value after all the other energy losses of the beam (in CATS, target windows and gas) have been considered as well. The experimental trend is correctly reproduced by setting in the simulation a rate of ice formation on the target windows of a total of $22 \,\mu$ m/day (11 μ m per window), in fair agreement with the simple calculation discussed above. The total ice thickness at t ~ 75 h is then approximately 74 μ m. The simulation also shows that the B ρ structures for t > 65 h are the expected extension of those at t < 46 h, when the proper energy loss in the target is considered.

4.2. Impact of the ice formation

The energy spectrum of the deuterons emitted in the present reaction extends down to 2.5 MeV at the most backward laboratory angles, which is also the angular region where the transfer cross sections are higher. This feature can be common to other stripping reactions at similar bombarding energies, of course depending on the reaction Q value. These particles lose part of their energy passing through the gas composing the target, the Havar window and the ice layers on the window and may eventually reach the detector with not enough energy to overcome the detection threshold. For this reason the increase of ice thickness on the target windows over time turns out to be a highly undesired effect.

To give some numbers, 2.5-MeV deuterons lose about 1 MeV of energy in 40 μ m of ice, the same amount of energy that they lose in about $9\,\mu\text{m}$ of Havar or in 5.5 mm of ³He at the temperature and pressure reached in the present experiment (energy losses computed with LISE++ [33]). These numbers also help to highlight the importance of the correct balance between target thickness and energy losses for this kind of reactions. Higher density of scattering centers (~ 30 times more) could be obtained, for instance, operating the target with liquid ³He at ~4 K, condition that would allow to perform experiments similar to the one presented in this article with beam intensities of less than 10^4 pps. However, in such a case, the deuterons would not have enough kinetic energy to exit the target or to be detected. In this sense, the temperature, pressure and target thickness at which HeCTOr is operated represent an ideal compromise between the two opposite requirements.

Future developments of the system should foresee dedicated tests to better evaluate the rate at which the ice grows and how it depends on variables such as the vacuum level and the gas composition. A possible solution to overcome the problem, however, is to reheat the target each 2-3 days during the experiment. Such operation would allow to strongly reduce the ice thickness, though at the expense of the LHe consumption. For the experiment the target has been kept cold for about 11 days. In this time interval the consumption of LHe was 2400 L, or $\sim 200 \text{ L/day}$. This value could be significantly reduced by installing a system to recover the exhaust LHe.

4.3. Excitation energy resolution

An important observable in direct transfer reactions is represented by the excitation energy, E^* , of the heavy reaction partner. The E^* distribution is a measure of the strength of population of the levels in the heavy residue, 47 K in this case, in the transfer process. Such strength is proportional to the cross section for each specific transfer channel. With the present setup this information can be obtained from two-body kinematics, by measuring the energy and scattering angle of the light recoiling particles in MUGAST. The excitation energy resolution depends on many factors (target thickness, energy of the light ejectiles, angular and energy stragglings, intrinsic resolution of the detectors, beam dimensions, ...) and represents a relevant parameter for the design and analysis of an experiment.

The expected energy resolution for the present case has been determined through simulations performed with *nptool* [34], an open-source data analysis and Monte Carlo simulation framework developed for low-energy nuclear physics experiments and based on the Geant4 [35] simulation toolkit and the ROOT [36] data analysis framework. In *nptool* the target is created by specifying, besides the thickness, density and type of gas, the characteristics of the front and back windows (material, radius, thickness and possible deformations) and of the frame. A possible parametrization for the target and window deformation is represented by a hyperbolic cosine function. Given the cylindrical symmetry of the target cell with respect to the beam axis z, in the forward hemisphere (z > 0) this function has the form:

$$f(r) = z_0 + (d+1) - \cosh\left[\frac{r}{R}\operatorname{acosh}(d+1)\right]$$
(5)

where r represents the distance from the beam axis, R is the target radius, d the deformation at the center of the target and z_0 half of the target thickness (refer to Fig. 8, where R = 8 mm, d = 0.5 mm and $z_0 = 1.5$ mm). In the backward hemisphere the profile is described by -f(r).



Figure 8: (Left) A simplified drawing of the target cell where the different parameters of Eq. 5 are indicated. The red curves represent the target deformation. (Right) An expanded view of the target generated in the Geant4 simulations.

We simulated the transfer reaction ${}^{46}\text{Ar}({}^{3}\text{He,d}){}^{47}\text{K}$ to the ground state of ${}^{47}\text{K}$, in inverse kinematics at the bombarding energy in the laboratory frame $E_b = 460 \text{ MeV}$ (10 MeV/u). In a first simulation we assumed a perfectly collimated point-like beam impinging on the target in (x,y) = (0,0). In this way we

can determine the contributions to the excitation energy resolution coming only from the target and the detectors. The experimental set-up here considered is composed of HeCTOr, placed 25 mm downstream with respect to the nominal target position, and the MUGAST array. For the target configuration we set a thickness of 3 mm of ³He gas. In the backward hemisphere, covered by MUGAST, we set a deformation of 0.5 mm, a 3.8- μ m thick Havar window and an ice layer of 35 μ m. The gas pressure, temperature and density are 700 mbar, 6K and 4.5 mg/cm³, respectively, corresponding to an areal density of ~ 2 mg/cm² of ³He. We assumed an isotropic angular distribution of emitted deuterons in the center-of-mass frame. The top panel of Fig. 9 shows the matrix where the energy of the deuterons right after the reaction, E_{lab} , reconstructed by accounting for all the energy losses in the target and in the detector dead layers, is plotted versus their scattering angle in the laboratory frame, θ_{lab} . The theoretical kinematic line is plotted in green. The inset shows the resulting excitation energy distribution of ⁴⁷K, centered in 0 as expected for the transfer to the ground state. The obtained excitation energy resolution is ~ 1.3 MeV FWHM.

The relative contributions to this resolution can be computed performing different simulations considering, in each of them, only the effect of a single target "layer". We obtained for the target thickness $\Delta E_t \sim 0.8$ MeV, for the target deformation $\Delta E_d \sim 0.4$ MeV, for the Havar window $\Delta E_w \sim 0.6$ MeV, for the ice layer $\Delta E_l \sim 0.6$ MeV (all values are FWHM). The intrinsic resolution of the detectors is $\Delta E_{Si} \sim 40$ keV. The total resolution is given by $\Delta E_{tot} = \sqrt{\Delta E_t^2 + \Delta E_d^2 + \Delta E_w^2 + \Delta E_l^2 + \Delta E_{Si}^2} \sim 1.3$ MeV, in agreement with the result of the simulation where all the effects are considered at the same time.

The experimental E* distribution can be obtained by gating on the ⁴⁷K ions detected in VAMOS and on the deuterons detected in MUGAST. Careful considerations need to be made when comparing it with the result of the simulation. The experimental E* distribution is expected to contain contributions from the different levels of ⁴⁷K populated in the transfer. The $1/2^+$ ground state of 47 K can be populated with an orbital angular momentum transfer L = 0 from ⁴⁶Ar, while the first excited states $3/2^+$ at 360 keV and $(7/2^-)$ at 2020 keV can be populated via L = 2 and L = 3 transfer, respectively. Assuming the spectroscopic factors for the different L transfers to be comparable, at the most backward scattering angles in the laboratory frame, which correspond to the forward angles in the center-ofmass frame, the L=0 transfer to the ground state should have higher cross section than higher L transfer and the width of the E* distribution should reflect the experimental energy resolution. In the bottom panel of Fig. 9 we plot in black the E* distribution obtained with a gate only on the annular detector of MUGAST, which covers the most backward laboratory angles $(\theta_{\rm lab} > 160^{\circ}).$

To directly compare simulation and data one has to consider that the characteristics of the beam can significantly affect shape and width of the E* distribution. For this reason we performed a second simulation considering more realistic beam parameters, leaving the target characteristics unchanged from the first simulation. The beam profile on the xy plane is now represented by a two-dimensional gaussian function with centroid in (x,y) = (0,0) and $\sigma_x = \sigma_y = 3$ mm. Typical spots of SPIRAL1 beams are of the order of ~ 2 mm, but we have to consider the effect of the angular straggling of 0.9 mrad (computed with LISE++) occurring in the four 1.5- μ m thick Mylar windows of the CATS detector placed 2 m before the target. Such angular straggling has been taken into account in the simulation. The number of events was reduced to adapt to the experimental statistics for a more direct comparison. The resulting E* spectrum is shown in red in the bottom panel of Fig. 9, superimposed to the experimental one.



Figure 9: (Top) Two-dimensional plot energy vs scattering angle of the deuterons obtained in the simulation of the reaction ${}^{46}\text{Ar}({}^{3}\text{He},\text{d}){}^{47}\text{K}$ at $\text{E}_{\text{b}} = 10 \,\text{MeV/u}$ for the transfer to the ground state of ${}^{47}\text{K}$. The assumed angular distribution of the emitted deuterons is isotropic in the center-of-mass frame. The green line represents the theoretical kinematic line. The inset shows the resulting simulated excitation energy distribution of ${}^{47}\text{K}$ and the value of resolution FWHM. (Bottom) Comparison between simulated (red) and experimental (black) E* distributions of ${}^{47}\text{K}$. The number of simulated events and the binning have been adapted for a clearer comparison with the experimental spectrum.

The two spectra are in reasonable agreement, though the experimental resolution is slightly larger (~ 30 %) than the simulated one. This discrepancy can be explained considering that, in the experimental data, contributions from the low-lying $3/2^+$ state at 320 keV in 47 K, very close in energy to the ground state, may be present. Moreover the simulation does not consider other beam parameters which could not be precisely determined experimentally with a single beam profiler (CATS) detector, such as, for instance, possible impact positions on target dif-

ferent from (0,0) or slight tilts in the beam direction. The small number of counts at negative excitation energy in the experimental distribution mainly comes from contributions from the deuteron break-up channel after the transfer. Due to the high cross section of the process and the limited resolution in particle identification in MUGAST, few protons, in coincidence with ⁴⁷K in VAMOS, can be tagged as deuterons and treated as such in the analysis. Their energy loss in the target is then overestimated, resulting in a negative excitation energy.

The complete experimental E* distribution and its physical implications will be further discussed in a forthcoming publication [37].

4.4. Transparency to γ radiation

In experiments where absolute cross sections are extracted via γ -particle coincidence, the γ -ray efficiency of the detection set-up plays an important role in the determination of the relevant physical quantities. While MUGAST is nearly transparent to γ radiation [23], the thick frame and shield of the target, if intercepted by γ rays before they reach AGATA, might absorb part of them and lower the effective γ -ray efficiency. When the nucleus produced in the reaction de-excites instantaneously through the emission of γ radiation, the absorption of γ rays by HeCTOr is minimum, since they can pass through the entire large opening of the conic flange facing AGATA in the backward hemisphere. In the case that the decaying level has a long lifetime, of the order of the nanosecond or more, the nucleus might travel a few centimeters before de-exciting. Part of the γ rays will then be absorbed by the target frame before they reach AGATA and the efficiency of the γ -ray detector will be consequently reduced.

Even though transparency to γ rays was not one of the main constraints in the design of HeCTOr, it represents an important parameter to consider when designing and analyzing experiments involving long-lived nuclear excited states. In the present experiment, the 3/2⁺ state at 320 keV in ⁴⁷K, which decays to the ground state, has a lifetime $\tau \sim 1.6$ ns. Since the average β for ⁴⁷K ions is ~0.14, in a time interval of the order of τ the nucleus travels approximately 6 cm and the γ -ray absorption due to the target can become significant. Such effect can be quantified by computing the loss of efficiency of AGATA when a calibration source is placed downstream with respect to the nominal target position, thus simulating the decay of a long-lived excited state. Therefore we placed a ¹⁵²Eu source at 85 mm from the target and acquired the corresponding γ -ray energy spectrum. A simulation was then performed with the AGATA simulation code [38], with the ¹⁵²Eu source placed in the same position, including HeCTOr and the reaction chamber. Figure 10 shows the comparison of the efficiency of the cores of the AGATA crystals as a function of the γ -ray energy between simulation (red squares) and data (black circles). The curves are fits obtained following the prescription of Ref. [39]. The absolute value and trend of the efficiency as a function of E_{γ} are in excellent agreement with the simulation. Significantly wrong parameters for the target materials and dimensions would in fact result not only in a different offset but

also very different shapes of the efficiency curve. As an example, the efficiency curve obtained in a simulation where the entire volume of HeCTOr was removed is shown in Fig. 10 with a dashed green line. The large difference, as compared to the other curves, clearly reflects the effect of γ -ray absorption by the target, which turns out to be, as expected, larger for γ rays of lower energies. This result confirms the importance of carefully accounting for the effect of γ -ray absorption by the target when analyzing the decay of isomeric excited states.



Figure 10: Comparison of the AGATA core efficiency as a function of the γ -ray energy between simulation (red squares) and data (black circles) for γ rays emitted by a ¹⁵²Eu calibration source placed at 85 mm downstream from the target. The green triangles and dashed line represent a second simulation where HeCTOr is not present. The curves are fits obtained following the prescription of Ref. [39].

5. Conclusions

In this paper we reported on HeCTOr, a thick ³He cryogenic target specifically designed to be employed for direct nuclear reactions in inverse kinematics. Among the strengths of the target are the high purity and density of scattering centers attainable at cryogenic temperatures, where thicknesses of the order of few mg/cm² (~ 10^{20} atoms/cm²) can be obtained. These characteristics make it particularly suited for experiments with low-intensity radioactive beams in fragmentation and ISOL facilities. The target has been integrated in a compact experimental set-up consisting of three coincident detectors for a first in-beam experiment. It showed a correct operation of its components and an excellent stability of temperature and pressure over time. Dedicated Geant4 simulations have demonstrated to provide good control over different relevant experimental parameters, such as total target thickness, energy resolution and γ -ray absorption. Foreseen improvements of the set-up will focus on the reduction of both the thickness of ice layers forming on the target windows and the consumption of LHe needed to maintain the target at cryogenic temperatures.

Acknowledgments

The authors acknowledge the GANIL staff for the invaluable support in the phases of installation of the target and during the experiment. We also wish to thank Emmanuel Dartois for his help with the kinetic theory of gases.

This work was supported by the European Union's Horizon 2020 research and innovation program under grant agreement No 654002. A. Gottardo acknowledges financial contribution from the MIUR PRIN 2017 call for funding, project 2017P8KMFT.

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