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### Density fluctuation analysis very near above and below

- <sup>2</sup> critical point using morphological and spatiotemporal
- **3** information

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Abstract We investigate the fractal nature of critical fluctuations in sulfur hexafluoride 14 (SF<sub>6</sub>) under microgravity conditions. For this purpose, we use the Bidimensional Empiric 15 Mode Decomposition (BEMD) approach to separate the spatial scales of fluctuations in 16 orthogonal Independent Mode Functions (IMFs). Statistical analysis of three morphology 17 measures (area, eccentricity, and orientation of convex objects in recorded images) across 18 different IMFs shows that critical fluctuations obey power-laws across multiple spatial scales. 19 We also perform a spatiotemporal analysis of fluctuations by extracting one line of pixels 20 from each image and creating a temporal stack from successive images, or "waterfalls." 21 The spatiotemporal section analysis along the spatial direction reveals multiple spatial scales 22 present in the original fluctuating image. The analysis of the "waterfalls" along the temporal 23 direction identifies a common power-law temporal behavior across all spatial scales. Our 24 results show that critical fluctuations very near critical temperature  $(T_c)$  have a fractal structure 25 captured by power-laws with multiple critical exponents. The morphology analysis shows 26 that very near  $T_c$ , the fluctuating domains are mostly spherical with some anisotropy. 27

#### 28 1 Introduction

- <sup>29</sup> Many experiments on the critical behavior of gas-liquid and binary fluids systems have been <sup>30</sup> performed, and they go back to over a hundred years [5,7,9,25,26]. Many of them are light
- scattering-based experiments [6,35,53,79] that determine thermophysical parameters close
   to the critical point by relying almost exclusively on Fourier analysis [14,32,58,59]. Fourier
- transform is a convenient method of switching back and forth between the real physical space
- (x, y) of the light scattering in the recorded image and the corresponding conjugated space of
- wavenumbers ( $k_x = 2\pi/x$ ,  $k_y = 2\pi/y$ ). Compared to the Fourier method, there are only a
- <sup>36</sup> few studies on direct observation of the scattered light intensity fluctuations in physical space

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(x, y) of the recorded images [10,23,35,38,39]. Asher and Pankow [2] performed a somewhat similar direct observation of light intensity fluctuations, although they used a laser-induced fluorescence method to measure the timescales of surface concentration fluctuations.

In real space recorded images, light intensity fluctuations appear as domains whose inten-40 sity is different from the image's mean intensity. In equilibrium conditions, these fluctuations 41 have large enough sizes to become detectable with optical cameras only when the system 42 is close to criticality. On the other side, non-equilibrium fluctuations become giant thanks 43 to the coupling of spontaneous fluctuations with the existing gradient [77]. This is increas-44 ingly true if one removes gravity [75]. The direct imaging of critical fluctuations may answer 45 fundamental questions regarding the correlation between thermal fluctuations and critical 46 percolation points [18,70]. This connection rests on a precise criterion to define clusters that 47 emerge from fluctuations during phase separation, and this up to now is still lacking. 48

The fluctuations of light intensity  $\delta i(x, y)$  detected by light scattering experiments are determined by the corresponding order parameter fluctuations. In pure fluids near their critical point, the order parameter is the reduced critical density,  $M = \rho/\rho_c - 1$ , where  $\rho(\rho_c)$  is the (critical) density of the system.

The signature of self-similarity of the fluctuating domains is the existence of a power-law dependence between the number of the convex areas and their "mass," i.e., the number of pixels in the image belonging to a convex domain [24]. Mathematically, the existence of a scaling equation for an observable A(r), which is a function of a variable r, establishes the quantitative connection between the power-laws and fractals:

$$A(\lambda r) = \lambda^n A(r), \tag{1}$$

where  $\lambda$  is a constant factor and n is a scaling exponent, independent of r [48]. Indeed, a 59 power-law such as  $y(r) = \alpha r^n$  is among the functions that obey the above scaling law since 60  $y(\lambda r) = \alpha(\lambda r)^n = \lambda^n y(r)$ . The above scaling equation is identical to the recursion formula 61 of the renormalization group theory when recursively integrating the short distance degrees 62 of freedom of the system to generate a sequence of effective Hamiltonians corresponding to 63 increasing scale [47, 74, 80, 81]. The physical quantity A(r) may not be extensive at the critical 64 point due to the long-range correlation of critical fluctuations. As the system approaches a 65 critical point, the asymptotic behavior of the physical quantity A(r) as the length scale 66 changes  $L \rightarrow L' = L/r$  usually gives a power-law [29, 30, 73]: 67 

58

$$A(L') = A(L/r) \propto r^{-\varphi} A(L).$$
<sup>(2)</sup>

Near the critical points of phase transition, a new order driven by strong and long-range 69 correlations between dynamic events emerges at all the system's spatial scales. Such a 70 (re)organization of the system occurs at all spatial scales and can be best captured math-71 ematically by power-laws and fractal dimensions [69]. A fluid near its critical point is in 72 constant contact with a thermostat with which it exchanges energy that leads to a coher-73 ent macroscopic behavior [17]. Such a process mediated by long-range correlations among 74 fluctuating domains reflects the unity of the physical laws spanning multiple spatiotemporal 75 scales and is captured by scale-free power-law distributions of observables. 76

The first study that identified an experimental power-law was done by Vilfredo Pareto and
modeled the distribution of individuals' incomes, which is called nowadays Pareto law [63].
He found that the relative number of individuals with an annual income larger than a specific
value *x* was proportional to the power of *x*. Since then, fractal structures characterized by
power-law distributions were discovered in the turbulent flow [71], earthquake dynamics

occurrence of an infinite cluster can be associated with the divergence of the fluctuations near

the critical point [36].

Our main result is that critical fluctuations very near critical temperature  $(T_c)$  have a fractal

structure captured by power-laws with multiple critical exponents. Our current approach's

<sup>87</sup> advantages are that (1) data analysis is performed in the spatial domain without using Fourier

transforms, (2) the image analysis is data-driven, i.e., all measures related to spatiotemporal
 behavior of the fluctuations are directly related to observed intensity fluctuations, and (3) the

<sup>90</sup> BEMD-based analysis is valid even for nonlinear and non-stationary processes.

#### 91 2 Experimental setup

Images of large thermal fluctuations near the critical point ( $T_c = 318.733$  K,  $P_c = 37.586$  bar, 92  $\rho_c = 5.0581 \text{ mol } l^{-1}$ ) of sulfur hexafluoride (SF<sub>6</sub>) in microgravity conditions were recorded 93 using ALICE 2 instruments onboard of 1999 MIR space station [15,28,49,51,55]. In this 94 microgravity experiment, SF<sub>6</sub> above its critical temperature  $T_c$  was quenched by quickly 95 decreasing its temperature with steps of  $300 \,\mu$ K. Several sets of thermal quenches (see Fig. 96 1 in [56]) were performed from the one-phase region above critical temperature into the 97 two-phase region below  $T_c$  that resulted in phase separation [55,56]. The temperature was 98 monitored with three thermistors placed inside the SCU. For image analysis, we cropped the 99 most extensive possible rectangular area without including data markers. In this paper, we 100 only discuss image processing results based on the last  $300 \,\mu K$  thermal quench that stepped 101 through the critical temperature [39, 56, 60]. The system was prepared at the critical density 102 with the order parameter  $M = (\rho - \rho_c)/\rho = 0.0 \pm 0.02\%$ . The 300  $\mu$ K temperature quench 103 through  $T_c$  started the phase separation of the fluid (see [39,56,60] for a detailed description 104 of the experimental procedure). Since the phase separation has begun during the last  $300 \,\mu K$ 105 thermal quench, we concluded that  $T_c$  was somewhere between the upper (UP, i.e.,  $T > T_c$ ) 106 and lower (DOWN, i.e.,  $T < T_c$ ) plateaus. The exact location of  $T_c$  measured from the 107 DOWN plateau was determined with the histogram method to be  $46.74 \pm 0.03 \mu K$  [55] and 108 in the range of  $15 \,\mu\text{K}$  to  $42 \,\mu\text{K}$  using Dynamic Differential Microscopy (DDM) [56]. 109

The density fluctuations were visualized through light transmission normal to the sapphire 110 windows using a He-Ne laser with 632.8 nm wavelength and about  $100 \,\mu$ W maximum power 111 (see also [60] for a detailed description). Laser stability after 1 h was estimated to be better 112 than 0.3 %. An optical microscope of 3.1  $\mu$ m resolution was also used to record a small SCU 113 region. We used 166 images (6.64 s) recorded for UP ( $T > T_c$ ) plateau. While the first 71 114 images of the 166 UP series were recorded with the microscope focused on the sapphire 115 window, the rest were recorded with the focal plane at the cell's center. For the DOWN 116  $(T < T_c)$  plateau, we used 479 images (19.16s). All images for the DOWN region were 117 recorded with the focal plane at the center of the cell. The full description of the experiment 118 is presented elsewhere [55,56,60]. 119

#### 120 3 Methods

121 3.1 Bidimensional Empiric Mode Decomposition (BEMD)

We use a new data-driven method for multi-scale analysis of critical fluctuations. The method naturally separates the spatial scales based on the image content. The BEMD method breaks

the original image into different orthogonal spatial scales called Intrinsic Mode Function

(IMF) and one residual quantity [60]. We probe the fractal nature of critical fluctuations by
separating spatial scales with the BEMD method followed by (1) morphological analysis and
(2) spatiotemporal cross sections ("waterfalls") of all IMFs. For this purpose, the BEMD
first separates the fluctuations in orthogonal spatial scales that contrast the morphology and
spatial properties more intuitively. We hypothesize that if critical fluctuations have a fractal
structure, then morphology measures and spatiotemporal structures should observe similar
evolutions across all spatial scales represented by individual IMFs.

In the past, the Empirical Mode Decomposition (EMD) has been applied to earthquake 132 analysis [41,64], structural diagnosis [31,52], characterization of non-stationary biological 133 processes [44], mechanical fault diagnosis [84,85], and ocean waves analysis [72]. One 134 advantage of EMD over traditional spectral analysis methods is that it can be applied even to 135 nonlinear and non-stationary signals and produces linear and stationary IMFs [43]. Intuitively, 136 the EMD is a data-driven adaptive method that allows recursive removal of oscillations (IMFs) 137 by repeated subtraction of an appropriately defined baseline [34, 40–44]. For two-dimensional 138 data sets (images), we used a BEMD algorithm [65] that requires no pre-determined filter or 139 wavelet function [68]. The BEMD has been applied to texture extraction and image filtering 140 [45], finding the gold mineral deposition [40], the discovery of tin-copper polymetallic ore 141 field [16] by gravity anomalies captured by satellite images, image denoising [4,50], content-142 based image retrieval [1], and fusion of multispectral and remote sensing [27, 34, 37]. We 143 recently expanded the application of the BEMD method and combined it with the Dynamic 144 Differential Microscopy (DDM) to the analyses of critical fluctuations [60]. All the details 145 of decomposing fluctuation images based on BEMD are described in [60]. BEMD is a fully 146 adaptive multi-scale decomposition because it operates on the local extremum sequence. The 147 decomposition is carried out by direct extraction of the local energy associated with the signal 148 itself's intrinsic time-scales. This approach is different from the wavelet-based multi-scale 149 analysis that characterizes the scale of a signal event using pre-specified basis functions [82]. 150 For this study, we only considered three IMFs, plus the residual image [60]. Representative 151 examples of the original images, their first three IMFs, and the residual are shown in Fig. 1. 152 The BEMD decomposition contains the fluctuations from finest to coarsest spatial scale. 153 Since the sifting process extracts from the original image (Fig. 1A1 and A2) first the highest 154 spatial frequency (Fig. 1B1 and B2), the first IMF mode corresponds to the short-range 155 fluctuations, which we expect to dominate very close to the critical point. Conversely, the 156 image tendency and the long-range correlations of fluctuations are contained in the next two 157 modes (Fig. 1C1-C2 and D1-D2). The residue (Fig. 1E1 and E2) represents the largest spatial 158 scale of fluctuations obtained from the data. The residual is usually used as a background 159 image to correct for nonuniform illumination. 160

#### 161 3.2 Spatiotemporal cross sections

The spatiotemporal correlations of fluctuations could be captured with the stacked onedimensional sections through individual images, i.e., "waterfalls" [39]. For this purpose, a horizontal line of pixels was extracted from successive images at the same location, which gave the spatial dimension of the image, called "space" in Fig. 2A1. The rows of pixels (one row from each recorded image) were stacked according to the image index (time) along the vertical direction, which gave the temporal dimension called "time" in (see Fig. 2)A1.

To obtain the original spatiotemporal ("waterfall)" images, we first applied the BEMD decomposition to the original images, as shown in Fig. 1. Subsequently, we created for each IMF order the corresponding spatiotemporal ("waterfall") image as described above and shown in Fig. 2A1-A4. An optimum gray-level threshold was selected for each line of pixels,

A1 B1 C1 D1 E1 A2 B2 C2 D2 E2 A2 B2 C2 D2 E2

**Fig. 1** The original images (A1 above  $T_c$  (UP with cell centered focus) and A2 below  $T_c$  (DOWN with cell centered focus)), the first three IMFs (B1-D1 for UP and B2-D2 for DOWN), and the residual image (E1 for UP and E2 for DOWN) for the image index 100 of UP and the image index 200 of DOWN region. Above critical temperature (panels A1-E1), the finest spatial scale (B1) shows small size fluctuations, which correspond to the fluctuations' finest spatial scale. For the DOWN region (B2), the first IMF's characteristic spatial distance seems to be comparable to UP, which is consistent with the early stage phase separation processes. The coarse spatial scales (C and D) show long-range correlation patterns of fluctuations. The residue (E) has a structure that suggests a long-range correlation of fluctuations

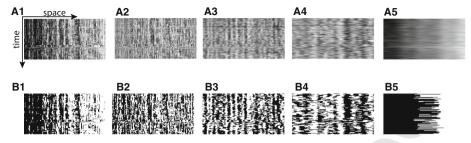
and the "waterfalls" were converted to black and white images (see Fig. 2B1-B4). We chose 172 one threshold per line instead of a single threshold for the entire "waterfall" image because 173 each line belongs to a different fluctuation image. This way, each line of pixels is thresholded 174 based on the correct context it belongs to, i.e., its original image. To binarize the original 175 grayscale images, we computed for each image a threshold based on Otsu's method [62]. 176 Otsu's method chooses a threshold that minimizes the intraclass variance of the thresholded 177 black and white pixels. Although we only show in Fig. 2 the stack of rows through the middle 178 of each image, we repeated the same procedure at 25 % and 75 % of image height and found 179 no statistical difference with the results presented here for the central line of pixels. A similar 180 approach was used for the DOWN region. The black and white thresholded grayscale images 181

were used for edge detection of convex objects during morphology analysis.

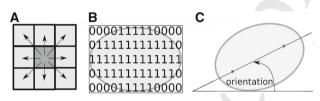
#### 183 4 Results

184 4.1 Morphological analysis of critical fluctuations

We used an in-house Matlab code to compute a set of properties specified by the 8-connected component (object) in the binarized fluctuation images (see Fig. 3B). In a two-dimensional image on a rectangular lattice, any given pixel is connected with eight adjacent pixels if their edges or corners touch, as shown in Fig. 3A. Two adjoining pixels are part of the same object if they are both on and are connected along the horizontal, vertical, or diagonal direction (see Fig. 3A for an 8-connected central pixel). Out of the 25 different properties computed,



**Fig. 2** Stacks of one-dimensional sections through the center of each fluctuation image of the UP region. The original (A1) grayscale images were separated into three IMFs plus a residual image using the BEMD algorithm (A2-A5). The shortest spatial scale is contained in A2 and the longest in A5. The corresponding thresholded black and white images (B1-B5) allow a clear identification of the boundaries of convex domains (black pixels)

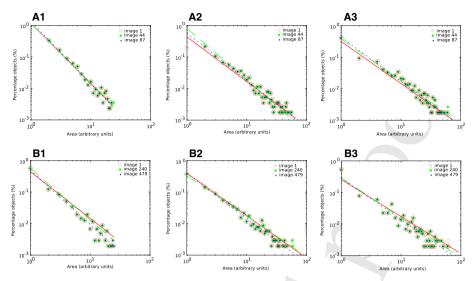


**Fig. 3** (A) In two-dimensional images, an 8-connected central pixel has similar pixels along edges or corners. Two adjoining pixels are part of the same object if they are both on and are connected along the horizontal, vertical, or diagonal direction. (B) The eccentricity of a morphological object is the ratio of the distance between the foci of the ellipse and its major axis length. The value is between 0 (circle) and 1 (line segment). (C) The orientation of an elliptical object is given by the angle between the x-axis and the major axis of the ellipse. The value is in degrees, ranging from  $-90^{\circ}$  to  $90^{\circ}$ . The two dots on the major axis represent the foci of the ellipse

we only present the statistics of the three most relevant measures for the morphology of fluctuations, i.e., area, eccentricity (see Fig. 3B), and orientation (see Fig. 3C).

At least 40% of the compact, i.e., convex, objects with clear boundaries have an area 193 of one arbitrary unit (see Fig. 4A1-B1 for the original image, A2-B2 for IMF1, and A3-194 B3 for IMF2). As expected, large objects are scarce, reflected by a power-law decay of 195 the percentage of compact objects' area versus their size (see Fig. 4A1-B1 for the original 196 images). The statistics of only three representative images are shown in Fig. 4A1-A3 and 197 B1-B3, respectively. The slope of the log-log plots shown in Fig. 4 represents the power-198 law exponents. The UP region has the first 71 images recorded with the focal plane of the 199 microscope on the sapphire window of the SCU and the rest with the focal plane at the center 200 of the SCU. The statistical analysis was performed separately for the two subsets of images 201 recorded above  $T_c$ . Our statistical analysis of the morphology of fluctuation using convex 202 area measure revealed no statistically significant difference between the 71 images and the 203 rest for the UP region (see Fig. 4). As a result, the subsequent statistical analysis for other 204 morphological measures (eccentricity and orientation) lumped together the two subsets of 205 the UP dataset. From the UP region images recorded with the focal plane at the center of the 206 SCU (Fig. 4A1-A3) and from the DOWN region (Fig. 4B1-B3), we only show the log-log 207 plots for a set of three images selected at the beginning of the set, in the middle, and at the 208 end of the respective dataset. 209

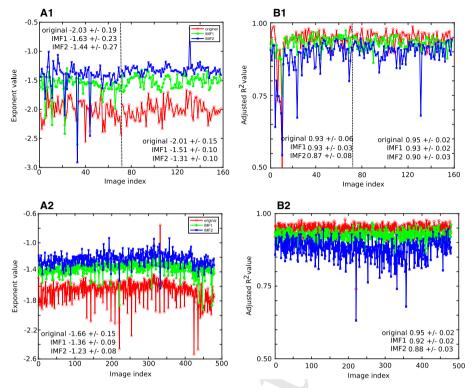
We fitted all area distributions for every image with power-laws given by  $\% objects \propto area^n$ , where the exponent values *n* are shown in Fig. 5A1-A2 for all images and their IMFs.



**Fig. 4** The distribution of the area of the convex objects identified in fluctuations images. The top panels are for the original images (A1) and the first two IMFs (A2 and A3) of the UP region  $(T > T_c)$  with the focal plane in the center of the SCU. The bottom panels (B1-B3) correspond to the DOWN region  $(T < T_c)$  with the focal plane in the center of the SCU. The panels A1-B1 represent the original images, the panels A2-B2 represent the first IMF, and A3-B3 correspond to the second IMF. For each region UP/DOWN, we selected only three images

The area distributions of the third and fourth IMF are not shown, but a numerical summary 212 is presented in Table 1. A summary of the UP plateau's power-law exponents is shown in 213 Fig. 5A1, where the window- and center-focused data are separated by a vertical dashed line. 214 Although we monitored multiple measures of the goodness of fit, e.g., the sum of squared 215 error, the root mean square error, we only show in Fig. 5B1-B2 the adjusted  $R^2$  coefficient 216 as a measure of the goodness of fit. Adjusted  $R^2 \in [-1, +1]$  determines the extent of the 217 dependent variable's variance, which the independent variable can explain. The higher the 218 adjusted  $R^2$ , the better the regression equation captures the dependent variable's variance by 219 the chosen independent variable(s). The average adjusted  $R^2$  coefficient was over 92 % for 220 the original images and the first IMF and over 87% for IMF2. From Fig. 5A1, we notice a 221 significant variance of the power-law exponent for the first 71 images of the UP plateau than 222 the rest of the recording. Since the mean values across all original and IMFs are consistent 223 and statistically identical both for the first 71 images recorded with the window focus and the 224 rest of the images of the UP plateau recorded with the focus plane at the center of the SCU, 225 the observed larger variance for the first subset is not due to the location of the focal plane. 226 A possible explanation for the observed variability is that the first 71 images are recorded 227 closer to when the thermal quench was applied and related to transient phenomena during 228 thermal equilibration. An alternative explanation could reside in the fact that the proximity 229 to the cell border alters the critical fluctuations due to the presence of preferential adsorption 230 on lengthscale  $\xi$  (see [8,83] and references therein). 231

The vertical dashed line in Fig. 5A1 separates the first 71 images of the UP dataset recorded with the focal plane on the sapphire window from the images recorded with the focal plane at SCU center.

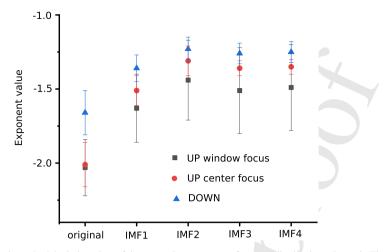


**Fig. 5** Power-law exponents and the goodness of fit. Panel A1 (A2) shows the power-law exponents that best fitted the area distributions in the original image (empty red circles), IMF1 (solid green circles), IMF2 (blue "x" marks) for the UP (DOWN) region. The panels B1 and B2 represent the respective goodness of fit measured by the adjusted  $R^2$  value. The mean values (and the standard deviations) of the power-law exponents (panels A1 and A2) decrease in absolute value from the original images to IMF1 and IMF2. The mean value of the adjusted  $R^2$  also decreases from 95 % for the original images to 92 %-93 % for IMF1 and 88 %-90 % for IMF2. All mean values are given with the corresponding standard deviations

Table 1         Power-law exponents extracted from the log-log plot of the	area distributions shown in Fig. 4
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	original	IMF1	IMF2	IMF3	IMF4
UP window	$-2.03\pm0.19$	$-1.63\pm0.23$	$-1.44 \pm 0.27$	$-1.51\pm0.29$	$-1.49\pm0.29$
UP center	$-2.01\pm0.15$	$-1.51\pm0.10$	$-1.31\pm0.10$	$-1.36\pm0.05$	$-1.35\pm0.05$
DOWN	$-1.66\pm0.15$	$-1.36\pm0.09$	$-1.23\pm0.08$	$-1.26\pm0.07$	$-1.25\pm0.07$

Despite large variabilities and some obvious outliers in the power-low fitting exponents 235 shown in Fig. 4A4-B4, the trends are quite stable. We notice first that the mean values and 236 standard deviations for the first 71 images of the UP region recorded with the focal plane on 237 the sapphire window are within the standard deviation of the next set of images recorded with 238 the focal plane at the center of the SCU (see Table 1). This result has two consequences: 1) 239 supports the ergodic hypothesis that fluctuations have the same structure regardless the focal 240 plane of recordings, and 2) allows us to lump together the first 71 images recorded with the 241 focal plane on the sapphire window with the rest of the UP images recorded with the focal 242 plane at the center of the SCU. 243



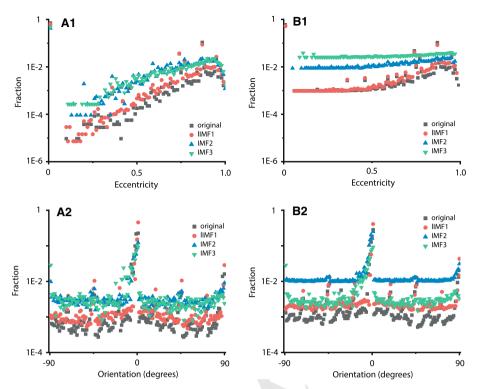
**Fig. 6** Mean and standard deviation plots of the power-law exponents for array distributions shown in Fig. 4. The original images gave the largest (in absolute value) exponents with a steady decrease (in absolute value) for IMF1 and IMF2. The exponents for IMF3 and IMF4 are statistically similar, although the actual images are significantly different (see Fig. 1D for IMF3 and Fig. 1E for IMF4). For the UP region, the exponents obtained with the microscope focused on the sapphire window (solid black squares) are statistically identical to those for the microscope focused at the center of the cell (solid red circles). For the DOWN region, the exponents are significantly smaller (in absolute value) compared to UP region (see solid blue triangles

The average exponents that summarize Fig. 4 are given in Table 1 and the corresponding Fig. 6. As expected, the distribution of areas in the original images (Fig. 4A1-B1) has the smoothest decay and the largest (absolute value) exponent in Table 1 because they contain all IMFs.

The fact that the exponents for the original images and the first two IMFS are statisti-248 cally different suggests that the smoothness of quantitative measures associated with original 249 images could be misleading because it lumps together processes on different spatial and tem-250 poral scales. The similar values of the exponents for IMF3 and IMF4 suggest that, although the 251 actual images look different, the area measure is not sensitive enough to distinguish between 252 these two IMFs. This is because both IMF3 and IMF4 contain the largest spatial scales of the 253 original images, and they do not contain significantly different small-scale convex objects to 254 tilt the array distribution toward one of the two IMFs. 255

Since the original images include convex objects across all spatial scales, they will be 256 separated and smoothened by the BEMD image processing when computing IMF1. As a 257 result, the power-law exponents for IMF1 will reflect the smoothing effect of the BEMD 258 algorithm leading to a smaller (in absolute value) exponent compared to the original image. 259 This is because BEMD smoothing of fast spatial oscillations in the original images will 260 spread the spatial scale over a wider range of sizes. A similar explanation is valid for IMF2. 261 The saturation and plateau observed for the exponents across IMF2, IMF3, and IMF4 (see 262 Fig. 6) suggests that we may not have more than two spatial and temporal scales present 263 in our original image. As a result, adding higher-order IMFs does not add significant new 264 information to our analysis. Therefore, in the subsequent statistical analysis, we will drop 265 the last IMF4 as it does not add significantly more information than IMF3. 266

The eccentricity of convex objects in analyzed images indicates possible anisotropy induced by nucleation [66,67], coalescence-induced coalescence [11,46,54], dimple coalescence [11,57], and other processes that lead to phase separation. The eccentricity of the



**Fig. 7** The eccentricities and orientations of convex areas in fluctuation images. In both UP (left panels A1) and DOWN (right panels B1) regions, the zero-eccentricity (circular cross section) dominates the identified convex objects with larger eccentricities not exceeding 1% of the total objects identified. The orientations of the elliptical areas are dominated by zero degrees (circles plus some ellipses), and the contribution of other orientations is also less than 1% (A2 for UP and B2 for DOWN, respectively). All plots are on the semilogarithmic axis to emphasize that nonzero contribution for eccentricity and orientation is tiny

convex objects identified in fluctuation images is measured as the ratio of the distance between 270 the foci of the ellipse and its major axis length (see Fig. 3B). The value of eccentricity is 271 between 0 (circle) and 1 (a line segment). We show the eccentricity on the semilogarithmic 272 axis (see Fig. 7A1 for UP and Fig. 7B1 for DOWN) to emphasize that although objects with 273 nonzero eccentricity were identified in images, their fraction is very small. Indeed, in all 274 original images and the first three IMFs, the largest percentage of objects are circular (no 275 eccentricity), whereas the largest nonzero eccentricity fraction is around 1%. We summa-276 rized in Table 2 the percentage of circular objects identified in the original images and their 277 IMFs. The fact that about 70 % of objects have a circular shape in the UP region aligns with 278 our hypothesis that above the critical point, we only expect short-range correlations that lead 279 to spherical (circular cross section) objects in the absence of any gradients. The fact that 280 over 60 % of objects have a circular shape in the DOWN region indicates that, although the 281 fluctuations are more anisotropic below  $T_c$ , the fluid is still very close to  $T_c$  in the early stage 282 of phase separation. This suggests that a few tens of  $\mu K$  around  $T_c$ , the local field is still 283 pretty uniform, and there is no significant hydrodynamic anisotropy, such as those induced 284 by coalescence-induced coalescence or dimple coalescence [39,56]. 285

Another measure of the system's anisotropy is the orientation of the convex objects in the fluctuation images (see Fig. 3C). We measured the angle between the x-axis and the major axis

<b>Table 2</b> The percentage ofobjects with zero eccentricity in		original	IMF1	IMF2	IMF3
Fig. 7A1-B1	UP	$71 \pm 11$	$64 \pm 13$	$43 \pm 16$	$48\pm18$
	DOWN	$60\pm 6$	$52\pm 6$	$39 \pm 11$	$45\pm14$

of the elliptical areas identified in fluctuation images, ranging from  $-90^{\circ}$  to  $90^{\circ}$ . For spherical 288 objects, the algorithm selects the major axis along the x-direction, i.e.,  $0^{\circ}$  orientation. We 289 found that the  $0^{\circ}$  orientation of convex areas dominates the distribution of orientations. In 290 other words, all zero eccentricity objects (circular cross-section) plus some ellipses that may 291 have 0° orientation (see Fig. 7A2-B2) dominate critical fluctuations very near  $T_c$ . We used 292 the semilogarithmic axis again to emphasize that the contribution of orientations other than 293  $0^{\circ}$  is below 1 %. The very low eccentricity combined with the high ratio of  $0^{\circ}$  orientation 294 suggests that the fluctuation patterns are relatively homogeneous and mostly spherical very 295 near above and below  $T_c$ . 296

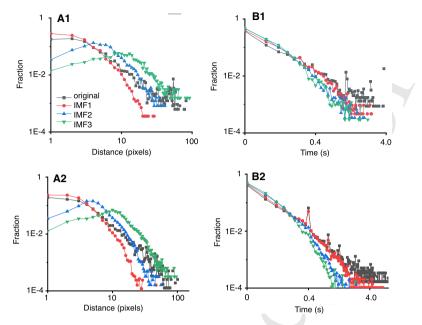
#### 297 4.2 Spatiotemporal cross sections

The phase separation dynamics that take place near  $T_c$  could be captured by the spatiotemporal "waterfalls," i.e., temporal stacks of single-pixel lines. The morphological properties identified in the previous section only capture a few features of critical fluctuations very near above and below the critical temperature.

We determined the distribution of contiguous black pixels along the horizontal (spatial) 302 direction of "waterfalls" shown in Fig. 2. Such a distribution gives information about the 303 spatial size of fluctuations and is shown in Fig. 8A1-A2. For all microscopic images, the 1 304 pixel =  $3.1 \,\mu$ m. The "waterfall"'s spatial dimension statistics contain different information 305 than the distribution of the areas of convex objects identified through morphology analysis. In 306 the spatiotemporal images (see Fig. 2), we analyze the evolution of contiguous linear domains 307 at the same location across all original images and their IMFs. While it is possible for a cross 308 section of an image to contain the same information about the statistics of fluctuations as 309 the whole image, such an ergodic assumption is only valid in the limit of a very large cross 310 section. Due to the finite size of the cross section, i.e., a one-pixel line from each image, we 311 expect slightly different power-law exponents for the spatiotemporal cross sections compared 312 to the morphology analysis. 313

All spatial distributions for all original images and their IMFs have the same general structure: they monotonically increase to a peak and then decay as a power-law (shown as straight-line patterns in a log-log plot of Fig. 8A1-A2). We fitted the spatial distribution data with a power-law over an adjustable range of distances that gave us the best goodness of fit with the maximum possible coefficient of determination. For example, for the original image in Fig. 8A1, the best range was 3 to 24 pixels; for IMF1, the range was 4 to 20 pixels; for IMF2 was 6 to 29 pixels, and for IMF3, it was 14 to 52 pixels.

There are similarities between the spatiotemporal statistics (Table 3) and convex area statistics from morphology analysis (Table 1). In both cases, the power-law exponents increase from the original images as the IMF order increases. Such consistent behavior supports the ergodic hypothesis, i.e., the dynamics of fluctuations is the same whether we analyze the whole image using morphology measures or only a cross section as in the case of "waterfalls." The second conclusion from the power-law exponents' consistent trend is that the fractal hypothesis is supported by the existence of power-laws holds across all IMFs. We noticed



**Fig. 8** Distributions of spatial (A1-A2) and temporal (B1-B2) fluctuation sizes. The spatial size of fluctuations has a peak that depends on the IMF's spatial scale (A1 for UP and A2 for DOWN). Spatial unit is 1 pixel =  $3.1 \,\mu$ m. After the peak, all distributions decay as power laws with quite close exponents (see Table 4). The distribution of temporal correlations for all IMFs follows identical patterns with two different exponents: a relatively small exponent for durations shorter than 0.4s and a much more negative exponent for longer correlation times (B1 for UP and B2 for DOWN). There were 25 frames per second

Table 3 The power law exponent of spatial distribution of objects in Fig. 8A1-A2. The distances are measured in pixels with 1 pixel =  $3.1 \,\mu m$ 

	original	IMF1	IMF2	IMF3
UP	$-1.75\pm0.04$	$-2.19\pm0.08$	$-2.30\pm0.07$	$-2.4\pm0.1$
DOWN	$-0.93\pm0.05$	$-0.94\pm0.10$	$-2.50\pm0.05$	$-2.45\pm0.06$

in both the morphology analysis (Table 1) and the spatiotemporal cross sections (Table 3)
 that the exponents of the original images and IMF1 are very close, which suggests that the
 critical fluctuations are captured for the most part by the finest spatial scale of IMF1.

There are also differences between UP and DOWN plateaus revealed by spatial statistics. 331 For example, the power-law exponents of spatiotemporal cross sections for both the original 332 and IMF1 in the UP region are about twice as large as the exponents for the DOWN region 333 (Table 3). This shows that, although the fractal nature of fluctuations revealed by the power-334 laws is preserved, the DOWN region has a much smoother distribution of linear sizes. Another 335 significant difference is that the power-law exponent increases from the original image to 336 IMF1 only for the UP region (Table 1 and (Table 3), whereas for DOWN, the exponents are 337 almost constant. This means that below  $T_c$ , both the original and IMF1 have similar spatial 338 dynamics. 339

The distribution of temporal correlations measured along the temporal axis (vertical) direction has completely different dynamics than the spatial correlation, as shown in Fig. 8B1-

	original	IMF1	IMF2	IMF3
UP ( $t < 0.4  s$ )	$-1.44\pm0.04$	$-1.48\pm0.02$	$-1.32\pm0.03$	$-1.41 \pm 0.08$
UP ( $t > 0.4$ s)	$-1.6\pm0.1$	$-2.5\pm0.3$	$-3.2\pm0.4$	$-2.4 \pm 0.3$
DOWN ( $t < 0.4  s$ )	$-1.42\pm0.03$	$-1.39\pm0.03$	$-1.33\pm0.04$	$-1.39\pm0.06$
DOWN ( $t > 0.4$ s)	$-1.7\pm0.12$	$-2.26\pm0.10$	$-3.5\pm0.2$	$-3.0 \pm 0.4$

Table 4 The power-law exponent of temporal distribution from Fig. 8B1-B2

B2. All IMFs have almost the same power-law distribution up to 0.4s (the equivalent of 10 342 video frames), and then the power-low exponent drops significantly (see Fig. 8B1-B2 and 343 Table 4). The fact that there are two different exponents for the temporal correlation suggests 344 that indeed the correlation time of fluctuations is best described by a double exponential 345 [39,55,56]. The difference in the two exponents is clear when comparing the fitting for short 346 durations t < 0.4 s against longer durations with t > 0.4 s for all IMFs (see Fig. 8B1-B2 347 and Table 4). The temporal correlation exponent (Table 4) for short durations (below 0.4 s) is 348 statistically identical both for the UP and the DOWN regions. Moreover, the exponents are 349 almost constant across the original images and their IMFs. This suggests that fluctuations in 350 the temporal statistics are not sensitive to spatial scale separation performed with the BEMD. 351 The characteristic times of fluctuations decrease as  $t^{-1.4}$  for the original images. 352

For longer correlation times (above 0.4 s), the distribution scales as  $t^{-1.7}$  and is no longer invariant to BEMD spatial decomposition. The increase in the power-law exponents with the IMF order indicates that larger fluctuations lose temporal correlation much faster than smaller clusters. As expected, the original image's power-law exponents do not show such a large discontinuity because it lumps together multiple spatial and temporal scales (see Table 4). For this reason, in the DDM analysis of fluctuation images the correlation time of fluctuations is represented by a single power-law exponent [3, 19–21, 33, 61, 75, 76].

#### 360 5 Conclusions

The recent extension of the classical theory of fluctuations to non-equilibrium processes 361 [76] showed that the temporal correlation of fluctuations could be directly obtained from 362 fluctuation images. It can lead to experimental advances in measuring diffusion and viscos-363 ity coefficients. The information regarding the evolution and the scaling of the fluctuation 364 correlation time is contained in the Intermediate Scattering Function (ISF). For pure fluid 365 in thermal equilibrium, the ISF is a Gaussian with width proportional to the diffusion time. 366 There are cases when ISF contains multiple time scales, and one approach for mitigating 367 this issue has been the fitting of ISF with multiple exponentials to capture each characteristic 368 time separately [3,61]. This approach allowed, for example, the separation of the thermal 369 diffusivity coefficient from the mass diffusivity [3]. 370

Instead of investigating the fluctuations in Fourier space through their ISFs, we here carried out a direct space analysis of fluctuations. For this purpose, we used the BEMD, data-driven technique to decompose the spatial frequency components into an orthogonal set of Intrinsic Mode Function (IMFs). This method is suitable for analyzing nonlinear and non-stationary data, such as the thermal quench data that stepped through the critical temperature  $T_c$  in our microgravity experiment.

Different physical processes act over different spatial and temporal ranges. Very near the 377 critical point of a phase transition, dynamical fluctuations reach macroscopic magnitude and 378 overrule molecular size, shape, and interactions in dictating bulk behavior [22,78]. These 379 fluctuations are generated by the nonlinear dynamics of classical critical fluids. Recent large-380 scale numerical simulations showed that when approaching the liquid-vapor critical point 381 from the supercritical regime,  $T > T_c$ , the Lyapunov exponents associated with the phase 382 space dynamics of molecules decrease monotonically [22]. This is due to the fact that crit-383 ical fluctuations imply structural organization as opposed to molecular chaos and dynamic 384 instability. The Lyapunov exponents measure how quickly infinitesimally closed phase space 385 points separate over time. Large Lyapunov exponents indicate more unstable phases space 386 dynamics. As the system approaches  $T_c$  from above, the divergence of trajectories "slows 387 down" and allows the formation of spatial regions in the system that will separate into coex-388 isting vapor and liquid phases below  $T_c$ . 389

We found consistent power-laws across all spatial scales, which supports our hypothesis 390 of critical fluctuations' fractal nature. The morphology analysis showed that very near  $T_c$ , the 391 fluctuating domains are mostly spherical with some anisotropy. Spatiotemporal cross sections 392 showed that the distribution of contiguous domains also obeys free-scale power-laws near 393  $T_c$  that support the fractal hypothesis of critical fluctuations. The temporal correlation of 394 fluctuations also follows a power-law with the same exponent across all spatial scales (for 395 correlation times shorter than 0.4s (10 video frames). This surprising result supports the 396 hypothesis of a "slowing down" in the divergence of molecular trajectories [22] across all 397 spatial scales to allow phase separation. 398

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404 **Author contributions** AO and SAO perform image and statistical analysis. YG, CL, and DB conducted the 405 microgravity experiments and contributed to data analysis. All authors wrote the paper together and approved 406 the final manuscript.

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