

Theory of temperature-dependent consumer-resource interactions

Alexis Synodinos, B. Haegeman, Arnaud Sentis, José Montoya

► To cite this version:

Alexis Synodinos, B. Haegeman, Arnaud Sentis, José Montoya. Theory of temperature-dependent consumer-resource interactions. Ecology Letters, 2021, pp.1539-1555. 10.1111/ele.13780. hal-03223982

HAL Id: hal-03223982 https://hal.science/hal-03223982v1

Submitted on 12 Oct 2021

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

1	Title: Theory of temperature-dependent consumer-resource interactions	
2		
3	Running head: Temperature-dependence of consumer-resource interactions	
4		
5	Keywords: climate change, consumer-resource dynamics, food webs, community stability,	
6	biomass distributions, interaction strength, temperature dependence.	
7		
8	Article Type: Ideas and Perspectives	
9		
10	Authors: Alexis D. Synodinos ^{1*} , Bart Haegeman ¹ , Arnaud Sentis ² , José M. Montoya ¹	
11		
12	¹ Theoretical and Experimental Ecology Station, CNRS, Moulis, 09200, France	
13	² INRAE, Aix Marseille Univ., UMR RECOVER, 3275 route Cézanne, 13182 Aix-en-	
14	Provence, France.	
15		
16	* Correspondence to	
17	Alexios Synodinos, Theoretical and Experimental Ecology Station, UMR 5321, 2 Route du	
18	CNRS, Moulis, 09200, France, Tel : +33 561 04 05 89, email :	
19	alexios.synodinos@sete.cnrs.fr	
20		
21	Author emails:	
22	Bart Haegeman: bart.haegeman@sete.cnrs.fr	
23	Arnaud Sentis: arnaud.sentis@inrae.fr	
24	José M. Montoya: josemaria.montoyateran@sete.cnrs.fr	
25		

Author contributions: ADS, BH, AS and JMM conceived the approach. ADS and BH developed the method, AS and JMM guided its application. ADS led the writing of the manuscript; BH, AS and JMM provided crucial input and guidance throughout the writing process. JMM obtained the funding and managed the project. The authors declare no competing interests. Data accessibility statement: This study produced no new data. Any data used was taken from existing publication and is detailed in the Supplementary Information. Number of words in Abstract: 191 Number of words in main text (excluding abstract, figure and table legends, acknowledgments and references): 7,441 Number of references: 73 Number of figures: 7 Number of tables: 1

48 Changes in temperature affect consumer-resource interactions, which underpin the 49 functioning of ecosystems. However, existing studies report contrasting predictions regarding 50 the impacts of warming on biological rates and community dynamics. To improve prediction accuracy and comparability, we develop an approach that combines sensitivity analysis and 51 52 aggregate parameters. The former determines which biological parameters impact the 53 community most strongly at a given temperature. The use of aggregate parameters (i.e., 54 maximal energetic efficiency, ρ , and interaction strength, κ), that combine multiple biological 55 parameters, increases explanatory power and reduces the complexity of theoretical analyses. 56 We illustrate the approach using empirically-derived thermal dependence curves of biological 57 rates and applying it to consumer-resource biomass ratio and community stability. Based on 58 our analyses, we generate four predictions: 1) resource growth rate regulates biomass 59 distributions at mild temperatures, 2) interaction strength alone determines the thermal boundaries of the community, 3) warming destabilises dynamics at low and mild 60 61 temperatures only, 4) interactions strength must decrease faster than maximal energetic 62 efficiency for warming to stabilise dynamics. We argue for the potential benefits of directly working with the aggregate parameters to increase the accuracy of predictions on warming 63 64 impacts on food webs and promote cross-system comparisons.

- 65
- 66

69 Temperature strongly regulates consumer-resource interactions that constitute the 70 fundamental blocks of ecosystems (O'Connor et al. 2009; Montoya & Raffaelli 2010; 71 Petchey et al. 2010; Rall et al. 2012; Amarasekare 2019), and anthropogenic climate change 72 will, in most cases, increase mean temperatures (IPCC 2013). Therefore, understanding and 73 predicting the impacts of warming on consumer-resource interactions has attracted much 74 interest (Vasseur & McCann 2005; Binzer et al. 2012; Thakur et al. 2017). A breakthrough 75 occurred with the postulation that metabolic rate increases exponentially with temperature, 76 with the slope (often referred to as activation energy) conserved across levels of organisation 77 (Gilooly et al. 2001; Brown et al. 2004). However, activation energies can vary significantly 78 among organisms and biological rates (Dell et al. 2011; Réveillon et al. 2019). In addition, 79 the thermal response curve of biological rates can decrease at high temperatures, producing a 80 unimodal thermal dependence shape (Deutsch et al. 2008; Pörtner & Farrell 2008; Englund et 81 al. 2011; Uiterwaal & DeLong 2020). This lack of consensus regarding the exact shape of the 82 temperature-dependence of physiological rates (e.g. ingestion rates), behavioural traits (e.g. 83 consumer search or attack rates) or production (carrying capacity) has contributed to 84 diverging, sometimes contradicting, predictions of how consumer-resource interactions will 85 respond to warming (e.g. Vucic-Pestic et al. 2011; Sentis et al. 2012).

86

87 A dual approach to address the divergence in predictions

88

89 Two community properties describing important features of the community are consumer-90 resource biomass ratio and stability, defined with respect to the occurrence of oscillations. 91 Their importance is reflected in their prevalence in the literature on the effects of warming on

92 consumer-resource communities and food webs (Rall et al. 2010, 2012; Uszko et al. 2017; 93 Barbier & Loreau 2019; Bideault et al. 2020). However, predictions vary about the impacts 94 of warming on both these community properties. Biomass ratios have been theorised to 95 increase (Rip & McCann 2011; Gilbert et al. 2014) or decrease (Vasseur & McCann 2005) 96 monotonically with warming, though experimentally-derived data have mainly yield 97 unimodal responses (Fussmann et al. 2014; Uszko et al. 2017). Likewise, the effects of 98 warming on stability remain unclear. Using data on specific rates (e.g. consumer ingestion 99 and metabolism), studies have inferred that stability either increases monotonically (Rall et 100 al. 2010, 2012; Vucic-Pestic et al. 2011; Fussmann et al. 2014) or responds unimodally 101 (Sentis et al. 2012; Betini et al. 2019) to warming. Theoretical work on stability, in particular 102 on the mechanisms causing the onset of oscillations, expands decades (Rosenzweig & 103 MacArthur 1963; May 1972). Vasseur and McCann (2005) showed that warming will 104 destabilise consumer-resource communities when the consumer metabolic rate increases 105 slower than the ingestion rate. Johnson and Amarasekare (2015) demonstrated the pivotal role of the temperature-dependence of carrying capacity - rather than metabolism and 106 107 ingestion — in determining warming-stability relationships. All these examples demonstrate 108 that the mixed predictions, whether empirically-derived or theoretical, originate from two 109 distinct sources: the different parameters hypothesised to be driving community responses 110 and the thermal dependence shapes of these parameters. To improve the accuracy of 111 predictions regarding the effects of warming on consumer-resource communities, we need to 112 establish which biological parameters drive community properties (biomass distribution, 113 stability) and to acquire a mechanistic understanding of how their thermal dependence shapes 114 affect community properties.

116 A dual approach utilising sensitivity analysis and the application of aggregate parameters can 117 address both these issues (Fig. 1). On the one hand, sensitivity analysis establishes the 118 parameters that most strongly influence the community property of interest: it quantifies the 119 incremental increase in a response variable with respect to a small incremental increase in a 120 parameter. It has been extensively used in population ecology and demography (Caswell 121 2019), with important applications in applied ecology (Manlik et al. 2018). Since the relative 122 importance of parameters can change along the temperature gradient, a sensitivity analysis 123 allows us to determine the temperatures at which changes in the values of the different 124 parameters have the strongest relative impact (Zhao et al. 2020).

125

126 On the other hand, we can aggregate groups of the primary parameters into fewer, 127 biologically meaningful and empirically measurable quantities. The use of such aggregate parameters reduces the complexity of theoretical analyses, provides a mechanistic 128 129 interpretation for the difference in predictions and facilitates the comparison among 130 predictions (Barbier & Loreau 2019; Bideault et al. 2020). Experimentally, replacing multiple 131 measurements of individual parameters with measurements of the aggregates could also 132 restrict the room for divergent findings. The seminal work of Yodzis and Innes (1992) 133 reduced the analysis of consumer-resource interactions to two principal aggregate parameters; 134 consumer maximal energetic efficiency and a measure of resource abundance. A variation of 135 maximal energetic efficiency (termed energetic efficiency) has been widely used by empirical studies. However, rather than being measured directly, it has been derived from 136 137 measurements of its principle components, i.e., feeding and metabolic rates (Rall et al. 2010; 138 Vucic-Pestic et al. 2011; Sentis et al. 2012). Gilbert et al. (2014) posited that a single aggregate parameter — interaction strength defined as the impact of the consumer on the 139 140 resource population density — could capture the effects of warming on the stability of 141 consumer-resource interactions. However, their approach was based on a type I (nonsaturating) functional response, whereas most consumer-resource species pairs typically 142 143 produce type II or III (saturating) functional responses (Jeschke et al. 2004). Moreover, the 144 thermal dependence of interaction strength did not match the impact of warming on stability 145 for type II or III functional responses (Uszko et al. 2017), pointing to a more complex 146 relationship between interaction strength, warming and stability. We use two aggregate 147 parameters: the maximal energetic efficiency of the consumer population, defined as the ratio 148 of energetic gains through ingestion with no resource limitation (i.e., maximal energetic 149 gains) over energetic losses associated to metabolic demand (Yodzis & Innes 1992) and 150 interaction strength, measured as the ratio of resource population density without consumers 151 to resource population density with consumers (Gilbert et al. 2014).

152

153 Thus, our dual approach identifies the parameters causing the divergence in predictions 154 through the sensitivity analysis and simplifies complex theoretical explorations and empirical 155 measurements through the two aggregate parameters (Fig. 1). By expressing the sensitivities 156 and the community dynamics in terms of the aggregate parameters, analyses collapse into two 157 dimensions. This creates a simple and mechanistic tool to increase the accuracy and improve comparability of theoretical and empirically-driven predictions on the impact of temperature 158 159 changes on consumer-resource communities. The dual approach of sensitivity analysis and 160 parameter aggregation is not tailored to a specific model of consumer-resource interactions as 161 both are often used independently for different ecological models (e.g. Barbier et al., add a 162 ref for sensitivity). Here, we apply this general approach to the Rosenzweig-MacArthur 163 model (Rosenzweig & MacArthur 1963), a model frequently used to study the effects of 164 temperature on consumer-resource interactions (Fussmann et al. 2014; Uszko et al. 2017; Daugaard et al. 2019; Dee et al. 2020). Moreover, our approach can be applied to both static 165

166 and dynamic properties of consumer-resource interactions. We illustrate this application 167 using consumer-resource biomass ratio and a stability metric quantifying the proximity to 168 oscillations, respectively; these two variables dominating the literature on the effects of 169 warming on consumer-resource communities (Vasseur & McCann 2005; Rall et al. 2008; 170 Uszko et al. 2017; Betini et al. 2019). We implement different thermal parameterisations 171 from the literature to elucidate how the relative importance of different parameters and their 172 varying thermal dependence shapes impact predicted effects of temperature on consumer-173 resource interactions. Based on our results, we make four predictions that can be theoretically 174 and empirically tested.

175

176 **The dual approach**

177

In this study we illustrate the application of the dual approach (i.e. parameter sensitivity and aggregation) using the Rosenzweig-MacArthur model with a type II functional response (Rosenzweig & MacArthur 1963). This model describes the rate of change in resource and consumer biomass densities:

182

183
$$\frac{dR}{dt} = r(1 - \frac{R}{K})R - \frac{aR}{1 + ahR}C$$
 (1)

184

185
$$\frac{dC}{dt} = \left(e\frac{aR}{1+ahR} - m\right)C$$
 (2)

186

187 *R* and *C* are the resource and consumer species biomass densities, respectively. Resource 188 growth is logistic, with an intrinsic growth rate, r, and carrying capacity, *K*. Resource 189 biomass density is limited by the consumer through a saturating Holling type II functional 190 response with attack rate, a, and handling time, h. Consumer growth is proportional to the 191 assimilated consumed biomass, with e the dimensionless assimilation efficiency; losses occur 192 due to metabolic costs, m. Below we present the formulas most relevant to our study; an 193 extensive analysis of the model is available in the supplementary information (SI 1). We 194 chose a type II response due to its prevalence in many natural consumer-resource interactions 195 (Jeschke et al. 2004), though our approach works for the general form of the functional 196 response (SI 2). Additionally, the functional response can be defined with respect to attack rate and handing time, $f(R) = \frac{aR}{1+ahR}$, or maximum consumption rate, J, and half-saturation 197 density, R_0 , $f(R) = \frac{JR}{R_0 + R}$ (SI 3). 198

- 199
- 200 Stability and aggregate parameters
- 201

As demonstrated through the 'paradox of enrichment' (Rosenzweig 1971), the Rosenzweig-202 MacArthur model produces population cycles (oscillations) with increasing energy fluxes 203 204 (Rip & McCann 2011). Therefore, the coexistence equilibrium can be stable or unstable, 205 where dynamics oscillate around the unstable equilibrium (i.e., a limit cycle). The switch from stable to unstable dynamics occurs at a Hopf bifurcation. Theoretical studies have 206 207 analysed this qualitative change (Yodzis & Innes 1992; Vasseur & McCann 2005; 208 Amarasekare 2015) because these distinct stability regimes translate to different temporal 209 dynamics, with oscillations leading to greater variability over time. We applied a stability 210 metric that quantifies the tendency of the dynamics to oscillate (Johnson & Amarasekare 211 2015).

212

For our analyses we assumed dynamics had converged to the stable equilibrium or the limit cycle and determined the coexistence equilibria and the biomass ratio analytically (SI 1). Equilibrium means zero rate of change for both consumer and resource population biomasses. For the limit cycle, this yields the unstable equilibrium which is approximately equal to the time-averaged biomass values along the limit cycle. Thus, we set equations (1) and (2) to zero, solved to yield the coexistence equilibrium and retrieved the biomass ratio:

219

220
$$\mathcal{B} = \frac{c_s}{R_s} = er \frac{aK(e-mh)-m}{amK(e-mh)}$$
 (3)

221

222 In the model analysis we observed certain repeated parameter groupings (i.e., aggregate parameters) governed the dynamics (SI 1). Such aggregates have been previously used for the 223 224 analysis of the Rosenzweig-MacArthur model (Yodzis & Innes 1992; Vasseur & McCann 225 2005). The aggregates we selected represent ecological mechanisms which can be empirically measured. These are maximal energetic efficiency, $\rho = \frac{e}{mh}$, and interaction strength, 226 $\kappa = ahK\left(\frac{e}{mh} - 1\right)$. A closer look at ρ and κ elucidates their biological meaning. $\frac{1}{h}$ is the 227 saturation value of the functional response and thus represents the maximum consumption 228 229 rate, J. Hence, ρ can be written as:

230



231

 ρ quantifies the energetic gain-to-loss ratio of the consumer population biomass assuming its maximum feeding rate is realised (i.e. unlimited resources). ρ was introduced by Yodzis and Innes (1992) as a key aggregate parameter to understand food web dynamics. In empirical studies, a variant of ρ termed energetic efficiency, *y*, has been often applied (Rall *et al.* 2010; Sentis *et al.* 2012, 2017). Unlike ρ , *y* is a function of the full functional response term and hence also depends on resource density, $y = \frac{e * f(R)}{m}$, where $f(R) = \frac{aR}{1 + ahR}$ at a specified resource density, *R*.

239

240 The second aggregate parameter, κ , can be rewritten in terms of the resource population 241 density:

242

$$\kappa = ahK\left(\frac{e}{mh} - 1\right) = \frac{K}{R_S}$$

243

 κ is the ratio of the resource equilibrium density without consumers (carrying capacity) to the resource equilibrium density with consumers. κ quantifies the effect of the consumer population on the resource population and measures interaction strength (Berlow *et al.* 1999; Gilbert *et al.* 2014).

248

249 Using ρ and κ we determine the conditions for positive resource (eq. 4) and consumer (eq. 5) 250 densities, as well as the Hopf bifurcation (eq. 6) (SI 1):

- 251
- 252 $\rho > 1$ (4)
- 253
- 254 $\kappa > 1$ (5)
- 255
- 256 $\kappa \rho 1 = 0$ (6)
- 257

To determine stability, we adjusted the metric of Johnson and Amarasekare (2015) so that it vanished at the Hopf bifurcation (SI 4). This metric, S, defines stability solely in relation to the Hopf bifurcation.

265

$$\mathcal{S} = -\frac{(\kappa - \rho - 1)}{\rho - 1}$$

266

267 S>0 corresponds to a stable equilibrium and S<0 to oscillations.

268

269 *Sensitivity analysis*

270

271 We performed a sensitivity analysis of the biomass ratio (B) and the stability metric (S) with 272 respect to the original model parameters (i.e., r, a, h, e and m). A sensitivity analysis 273 quantifies the effect of an infinitesimal change in a parameter on the response variable. 274 Typically, while one parameter is being perturbed, all others are assumed to remain constant 275 and correlations between the parameters are not explicitly considered. However, this 276 approach can be applied in cases of correlated parameter change without a loss of accuracy. 277 As many environmental conditions (e.g. temperature) induce correlated changes in the 278 parameters, then the sensitivity of the response variable (e.g. B or S) with respect to the 279 environmental conditions can be reconstructed by combining the sensitivities of the individual parameters (SI 5.1). Different types of sensitivity indices exist such as simple 280 281 sensitivity and elasticity (Manlik et al. 2018; Caswell 2019). Here we used elasticity for biomass ratio (*B*) and an adjusted elasticity for stability (S) (SI 5.1), both dimensionless to facilitate direct comparisons between parameter sensitivities.

284

Elasticity is a proportional sensitivity, quantifying how a relative change in a parameter translates into a relative change in the variable; otherwise known as the log-scaled sensitivity (Manlik *et al.* 2018). Thus, the elasticity of B with respect to parameter x is given by: 288

$$\partial_x \mathcal{B} = \frac{\frac{\partial' \mathcal{B}}{\mathcal{B}}}{\frac{\partial x}{x}} = \frac{\partial \ln(\mathcal{B})}{\partial \ln(x)}$$

289

If $\partial_x B = 1$, a relative increase of 10% in parameter *x* causes a relative increase of 10% in variable *B*. Conversely, $\partial_x B = -1$ implies that a relative increase of 10% in parameter *x* results in relative decrease of 10% in *B*.

293

For the sensitivity of the stability metric, S, we used a variation of the elasticity. We defined the sensitivity of S as the incremental change in S induced by a relative change in parameter x. Our adjustment was possible due to S being dimensionless and it prevents sensitivities from diverging to infinity close to the Hopf bifurcation without altering the outcome of our analysis (SI 5.1).

299

$$\partial_x S = \frac{\partial S}{\frac{\partial x}{x}} = \frac{\partial S}{\partial \ln(x)}$$

301 $\partial_x S = 1$ implies that a relative increase in parameter x of 10% translates into an absolute 302 increase of 0.1 in S and has a stabilising effect. If, conversely, $\partial_x S = -1$, the same relative 303 increase in x would lead to decrease of 0.1 in S with a destabilising effect.

304

The magnitude and sign of each sensitivity determine how strongly and in what direction the parameter perturbation impacts the variable, respectively. We used the magnitudes to rank the relative importance of all parameters. The sign provided qualitative information regarding the direction of change (increasing or decreasing the response variable).

309

310 All sensitivities could be expressed in terms of ρ and κ . Hence, sensitivities are fully 311 determined in a plane with of ρ and κ as axes (Fig. SI 5.1, 5.2). In this ρ - κ plane the 312 sensitivities of all parameters can be ranked by magnitude, splitting the parameter space into regions where different parameters have the highest, second highest, etc. sensitivity 313 314 magnitude. Here, we present figures where the regions are determined by the top-two ranked 315 sensitivities; we do not portray changes in the rankings of the lowest sensitivities (see Fig. SI 316 5.4 and SI 5.5 for the complete biomass ratio and stability metric regions, respectively). The 317 biomass ratio and stability metric have different sensitivity expressions and, therefore, 318 produced different regions. For each variable, the regions remain fixed irrespective of the 319 parameterisation used, because the sensitivity expressions stem from the model equations. 320 The ρ - κ plane provides additional information, such as the feasibility boundary (eq. 5) and 321 the position of the Hopf bifurcation (eq. 6).

322

323 *Temperature parameterisations*

325 To demonstrate the impacts of different parameter thermal dependencies, we implemented 326 temperature parameterisations from the literature. Maintenance respiration rates, m, have 327 been shown to increase exponentially with temperature (Brown et al. 2004). The Arrhenius equation is most often used to describe this thermal dependence (Vasseur & McCann 2005; 328 329 Sentis et al. 2017; Uszko et al. 2017). However, the thermal response curves of resource 330 growth rate, r, attack rate, a, and handling time, h, have been represented either through the 331 Arrhenius equation (Vasseur & McCann 2005; Binzer et al. 2016) or as unimodal functions 332 (Amarasekare 2015; Uszko et al. 2017; Zhang et al. 2017; Uiterwaal & DeLong 2020; Zhao et al. 2020). Carrying capacity, K, and consumer assimilation efficiency, e, have a less clear 333 334 connection to temperature (Uszko et al. 2017; Dee et al. 2020). We selected two 335 parametrisations related to the ongoing debate surrounding the importance of including the 336 decreasing part of the biological rates beyond the optimal temperature (Pawar et al. 2016) and used these as an illustrative comparison. The 'unimodal' model had a unimodal 337 338 parameterisation for r, a (both hump-shaped) and h (U-shaped), the Arrhenius equation for m339 (increasing), and constant K and e (Uszko et al. 2017). We compared this to a 'monotonic' 340 parameterisation where all thermal dependencies (r, a, m increasing; h, K decreasing) follow 341 the Arrhenius equation and e is constant (Fussmann et al. 2014). Following this comparison, 342 we plotted four additional parameterisations from the literature onto the ρ - κ plane to broaden 343 the comparison and demonstrate the simplicity of applying the approach to empirically-344 derived measurements. These consisted of two similar monotonic parameterisations (Vucic-Pestic et al. 2011; Binzer et al. 2016), one where only a was hump-shaped (Sentis et al. 345 346 2012) and one which though monotonic, included some distinctive thermal dependencies -347 exponentially increasing K(T) and e(T) and constant h (Archer et al. 2019). We provide a 348 description of the studies and details of their parameterisations in the supplementary material 349 (SI 6).

351 We should note that not all parameterisations included the resource growth rate, r, so the 352 biomass ratio could not be calculated in these cases. However, we could calculate ρ and κ and, hence, the biomass ratio elasticities for all parameterisations. Thus, we could determine 353 354 how biomass ratio sensitivities to individual parameters changed with warming regardless of 355 the actual biomass ratio values. By including studies which had not measured resource growth or estimated the biomass ratio we broadened the scope of the comparison of the 356 biomass ratio sensitivities. Though this does not represent an exhaustive list of 357 358 parameterisations, we were restricted to parameterisations which could be used to parametrise 359 the Rosenzweig-MacArthur model with a type II response and whose available parameters 360 could yield ρ and κ . 'Mild' and 'extreme' temperatures, as well as 'close' or 'far' from 361 consumer extinction, are defined relative to each parameterisation's temperature range and feasibility boundaries, respectively. The feasible temperature range was determined by 362 363 interaction strength ($\kappa > 1$) with the temperature extremes corresponding to the point of 364 consumer extinction. This condition assumes that resources have a broader thermal range 365 than consumers (e.g., Rose & Caron 2007; West & Post 2016). If resources go extinct at temperatures consumers could withstand, then the feasibility boundary becomes dependent 366 367 on resource growth rate, r (Amarasekare 2015). The parameterisations we present come from 368 ectotherms, where environmental temperatures correspond to the organisms' temperatures. 369 However, our approach can be transferred to endotherms as it does not depend on a specific 370 thermal parametrisation.

371

372 Sensitivities depend on proximity to thermal boundaries

373

374 Biomass ratio: always most sensitive to e and m

376 We analytically obtained four groups of biomass ratio elasticity magnitudes, $\partial_e B = |\partial_m B|$, 377 $\partial_K B = \partial_a B$, $\partial_r B$ and $\partial_h B$. e and m always have the largest elasticity and hence the strongest 378 relative impact on the biomass ratio $(\partial_e B = |\partial_m B| > \partial_K B, \partial_a B, \partial_r B, |\partial_h B|, \text{ Table 1})$. Increasing e 379 increases the biomass ratio $(\partial_e B > 0)$, increasing *m* reduces it $(\partial_m B < 0)$. *K* and *a* have equal 380 and positive elasticities ($\partial_K B = \partial_a B > 0$), both increasing the biomass ratio. The elasticity of r 381 is constant, $\partial_r B = 1$; a directly proportional positive effect on B. Increasing h reduces the 382 biomass ratio, $\partial_h B < 0$. These are general results, independent of any model parameterisation 383 (with temperature or otherwise) following directly from the Rosenzweig-MacArthur model's 384 equations.

385

386 Biomass ratio: high r elasticity far from thermal boundaries

387

388 Both the 'unimodal' and 'monotonic' temperature parameterisations produced a unimodal 389 biomass ratio thermal dependence (Fig. 2). The unimodal parameterisation induced thermal 390 boundaries to the community at both low $(1^{\circ}C)$ and high $(33^{\circ}C)$ temperatures (Fig. 2a). The 391 biomass ratio exceeded 1 for most temperatures (higher consumer than resource biomass), 392 peaked at 14°C around $B \approx 5.5$ and decreased rapidly to 0 as it approached both thermal 393 boundaries (low and high temperature extremes). The biomass ratio of the monotonic 394 parameterisation (Fig. 2b) increased with warming from low temperatures, peaked at $B \approx 0.19$, before decreasing to 0 at high temperatures $(27.5^{\circ}C)$. The two parameterisations are derived 395 396 from different systems, hence the different temperature ranges.

397

In both parameterisations, sensitivity to e and m was highest throughout (Fig. 2c, d) - as expected from the analytical findings. Elasticities were split into two groups at mild 400 temperatures: *e*, *m* and *r* had the highest elasticity with $\partial_e B = |\partial_m B| \approx \partial_r B = 1$, while *a*, *h* and *K* 401 elasticities were very low. Approaching the temperature extremes all elasticities besides $\partial_r B$ 402 diverged; $\partial_h B$ diverged faster than $\partial_K B = \partial_a B$ in the unimodal parameterisation (Fig. 2c), 403 while the opposite occurred in the monotonic one (Fig. 2d).

404

405 Expressing the elasticities in terms of ρ and κ (Table 1) reduces the sensitivity analysis to two 406 dimensions. Ranking the elasticity magnitudes creates distinct regions in the ρ - κ plane which 407 correspond to different elasticity ranking orderings and provide a mechanistic overview of which elasticities dominate where (Fig. 3a). *e* and *m* always have the highest elasticity, so the 408 409 three regions reflect changes in the second highest-ranked elasticity. Regions adjacent to 410 consumer extinction (κ =1) have high sensitivity to either h (red region) or to a and K (yellow 411 region). r elasticity is highest in the region farthest from consumer extinction (orange region). 412 The two temperature parameterisations were mapped onto this plane by calculating their ρ 413 and κ values (Fig 3b and c). Despite the two trajectories being markedly different, both 414 occupied the region where r ranked second highest for most temperatures. The unimodal 415 parameterisation produced a unimodal trajectory, crossing the consumer extinction threshold 416 at low and high temperatures (Fig. 3b). The monotonic parameterisation's trajectory 417 converged monotonically towards consumer extinction with increasing temperature (Fig. 3c).

418

All other parameterisations from the literature also occupied the region of high *r* elasticity for most temperatures, far from their thermal boundaries (Fig. 4). Three monotonic parameterisations produced monotonic trajectories (Fig. 4a, b, c) which started in the region of high *r* elasticity and converged monotonically towards consumer extinction (κ =1). With a hump-shaped thermal dependence of attack rate, a unimodal trajectory emerged (Fig. 4d). At low temperatures it occupied the region of high *r* elasticity but moved away from consumer 425 extinction. With further warming, the trajectory switched direction and followed the same 426 path as the monotonic parameterisations, crossing the consumer extinction boundary. A 427 unimodal thermal dependence for attack rate (hump-shaped) and handling time (U-shaped) 428 (Fig. 4e), induced extinctions at low and high temperatures imposing a unimodal trajectory. 429 Unlike all previous parameterisations, the trajectory crossed the extinction threshold in the 430 region of high h elasticity. The final parameterisation, though monotonic, yielded unimodal 431 trajectories (Fig. 4f). A monotonically increasing K(T) (as opposed to decreasing in the other 432 monotonic parameterisations and constant in the unimodal ones) initially forced the trajectory 433 away from consumer extinction, albeit within the region of high r elasticity. Consumer 434 energetic efficiency ρ decreased, pushing consumers towards extinction, thus forcing an 435 abrupt decline towards the consumer boundary.

436

437 Stability most sensitive either to e and m or to a and K

438

Similarly to the biomass ratio, the analytical approach for the stability sensitivities yielded results conserved independently of the temperature parameterisations (Table 1): equal sensitivity magnitudes pairwise for *e* and *m* and for *a* and *K* (i.e., $|\partial_e S| = \partial_m S$ and $|\partial_K S| = |\partial_a S|$), negative stability sensitivities of *e*, *a* and *K* ($\partial_e S$, $\partial_a S$, $\partial_K S < 0$) implying they destabilise dynamics, a positive sensitivity of *m* ($\partial_m S > 0$) indicating a stabilising effect. *h* can be either stabilising or destabilising and *r* does not affect the stability regime ($\partial_r S = 0$).

445

446 The unimodal temperature parameterisation exhibited oscillations (S < 0) over most 447 temperatures (Fig. 5a). Only at low and high thermal extremes did dynamics briefly stabilise 448 prior to consumer extinction. The monotonic temperature parametrisation produced 449 oscillations at low temperatures (S < 0), crossed a Hopf bifurcation at 17°C and dynamics

were stable (S>0) thereafter (Fig. 5b). In both cases, stability close to consumer extinction 450 451 was most sensitive to consumer assimilation efficiency, e, and metabolism, m, $(|\partial_e S| = \partial_m S)$ followed by handling time, h (Fig. 5c, d). Moving away from the thermal boundaries, attack 452 453 rate, a, and carrying capacity, K, increased in relative importance. Furthest away from the 454 thermal boundaries, stability was most sensitive to changes a and K, followed by h. Even 455 though $\partial_h S$ did not rank highest in any temperature range, it was a close second both at the temperature extremes (second to $|\partial_e S| = \partial_m S$) or furthest away from them (second to 456 457 $|\partial_K S| = |\partial_a S|$). Additionally, h switched from destabilising at mild temperatures ($\partial_h S < 0$) to stabilising $(\partial_h S > 0)$ close to the temperature extremes (Fig. 5c, d, Fig. S5.2). 458

459

460 The ρ - κ plane for the stability metric was split into four regions; in two regions closest to 461 consumer extinction, $|\partial_e S| = \partial_m S$ were the largest sensitivities (Fig. 6a, red and yellow regions) and in the two regions furthest from consumer extinction, $|\partial_K S| = |\partial_a S|$ ranked highest 462 463 (Fig. 6a, green and blue regions). Additionally, the Hopf bifurcation (Fig. 6a, dashed curve) 464 split the plane into stable equilibrium and oscillation regions. Corresponding to the general 465 findings, stability in the two reference ('unimodal' and 'monotonic') parameterisations was most sensitive to changes in e and m at the thermal extremes - close to consumer extinction -466 467 and to a and K at milder temperatures – far from consumer extinction (Fig. 6b, c). The unimodal trajectory occupied the region of oscillations for most temperatures, crossing the 468 Hopf bifurcation twice close to consumer extinction, once at low and once at high 469 470 temperatures (Fig. 6b, blue region). The monotonic trajectory started in the region of 471 oscillations and moved into the stable region with warming, crossing the Hopf bifurcation far 472 from the thermal extreme (Fig. 6c, yellow region).

473

474 Parameter thermal dependencies impact warming-stability relationships

476 Plotting the other temperature parameterisations' trajectories onto the ρ - κ plane reproduced 477 the same patterns with respect to the stability metric's sensitivity (Fig. 7): stability was most 478 sensitive to e and m at the thermal extremes and to a and K far from the extremes. 479 Significantly, the trajectories revealed the impact of the thermal dependence shape of 480 individual parameters on the warming-stability relationship. In three monotonic 481 parameterisations, warming stabilised the dynamics (Fig. 7 a, b, c). In the cases, when 482 oscillations did take place, these occurred at low temperatures (Fig 7a resident prey, b, c) and 483 dynamics crossed the Hopf bifurcation far from the thermal boundary. In the case with two 484 enrichment levels (Fig. 7c), the high enrichment scenario required higher temperatures to 485 stabilise the dynamics. For the unimodal trajectory with hump-shaped attack rate (Fig. 7d), 486 warming at low temperatures pushed the dynamics towards (low enrichment) or deeper into 487 (high enrichment) the region with oscillations (i.e., destabilised dynamics). Here too, the 488 destabilising impact of enrichment was evident. However, further warming switched the 489 direction of the trajectory. Subsequently, both ρ and κ decreased. κ declined much faster, 490 forcing the dynamics towards the stable region and eventually consumer extinction. Both the 491 switch in the trajectory direction and the Hopf bifurcation (high enrichment scenario) 492 occurred at mild temperatures, in the region of high a and K sensitivity. In the 493 parameterisation with both a (hump-shaped) and h (U-shaped) unimodal (Fig. 7e), the Hopf 494 bifurcation occurred close to the thermal boundaries, where κ increased (low temperatures) or 495 decreased (high temperatures) much faster than ρ . The dynamics were oscillatory for most 496 temperatures, with the switch in the trajectory's direction occurring in the region of highest 497 sensitivity to a and K. The final parameterisation's trajectories were characterised by a 498 negative relationship between ρ and κ (Fig. 7f). Driven by the positive thermal dependence of 499 carrying capacity, warming increased κ and destabilised dynamics which oscillated for most 500 temperatures.

501

502 **Discussion**

503

504 Research on the impacts of warming on consumer-resource interactions has yielded mixed 505 results (Vasseur & McCann 2005; Englund et al. 2011; Rall et al. 2012; Gilbert et al. 2014; 506 Uszko et al. 2017). Resolving this debate and improving predictions has become even more 507 pressing as most ecosystems face increased temperatures (Easterling et al. 2000; Walther et 508 al. 2002; Root et al. 2003; Parmesan 2006). Here, we developed an approach to improve and 509 simplify predictions on the impacts of warming on consumer-resource interactions. This 510 approach integrates two pathways: (1) a sensitivity analysis to identify the key biological 511 parameters whose variations have the largest relative impact on community properties at a given temperature, and (2) aggregate parameters (maximal energetic efficiency, ρ , and 512 interaction strength, κ) to increase explanatory power. We used the Rosenzweig-MacArthur 513 514 model with a type II functional response, and applied the approach to consumer-resource 515 biomass ratio and a stability metric quantifying the propensity for oscillations (Johnson & Amarasekare 2015). Therefore, our insights apply to study systems well-described by the 516 517 Rosenzweig-MacArthur model. Our analyses revealed that the relative significance of 518 different parameter groupings is determined by the proximity of the consumer to its thermal boundaries. We, further, elucidated how differences in the shape of the thermal dependence 519 520 curves of individual parameters qualitatively impact predictions. We used empirically-521 derived thermal dependence curves of biological parameters from the literature to illustrate 522 this.

We focus our discussion on the formulation of four testable predictions arising from our results. For each prediction, we present its implications and rationale. Then, we discuss the empirical measurement of the aggregate parameters and present important subtleties and potential extensions of our approach.

528

529 Prediction 1: Resource growth rate regulates biomass distribution at mild temperatures

530

531 Implications: We showed that the relative dominance of consumer assimilation efficiency, 532 metabolism and resource growth rate in driving changes in biomass distributions should 533 manifest itself in any consumer-resource community far from its feasibility boundaries, 534 assuming these communities are well-described by the Rosenzweig-MacArthur model (Fig. 535 3a). Due to the agreement about the thermal dependence of metabolism (Rall et al. 2010; 536 Fussmann et al. 2014; Uszko et al. 2017) and the negligible -if any- change of assimilation 537 efficiency with warming (Dell et al. 2011), differences in the thermal performance curve of resource growth rate will strongly impact biomass ratio predictions. Therefore, improved 538 539 predictions about the impacts of warming on biomass distributions at mild temperatures 540 necessitate the accurate description of the thermal dependence of resource growth rate.

541

Reasoning: Far from the community thermal boundaries, consumer assimilation efficiency, metabolism and resource growth rate always had the greatest elasticity with an almost equal relative impact on biomass ratio ($\partial_e B = |\partial_m B| \approx \partial_r B = 1$, Fig. 2c, d and Fig. S5.1). Increasing metabolism reduced biomass ratios (Table 1), which is likely to be a universal response across ecosystems, given the positive exponential dependence of metabolism on temperature across organisms (Gilooly *et al.* 2001; Brown *et al.* 2004; Rall *et al.* 2012 but see Ehnes *et al.* 2011). Conversely, assimilation efficiency increased biomass ratios but has either been 549 assumed to be unaffected by temperature changes (Vasseur & McCann 2005; Sentis et al. 550 2017; Uszko et al. 2017) or has yielded a weak temperature-dependence (Wurtsbaugh & 551 Davis 1977; Handeland et al. 2008; Lang et al. 2017; Daugaard et al. 2019) with negligible 552 change compared to other parameters. Increasing resource growth rate also increased the 553 biomass ratio. However, evidence on the shape of resource growth's thermal response remains inconclusive: it can either increase exponentially with temperature (Savage et al. 554 555 2004) or decrease abruptly beyond the thermal optimum (Dannon et al. 2010; Thomas et al. 556 2012). Since the biomass ratio is directly proportional to the resource growth rate ($\partial_r B = 1$, 557 Table 1), it will be strongly affected by the values and shape of the resource growth rate 558 thermal performance curve. Given the consensus surrounding the temperature-dependence of 559 metabolism and the minor scale of potential change in assimilation efficiency with 560 temperature, our findings emphasise the significance of correctly parameterising the resource 561 growth rate when aiming to predict biomass distribution changes due to warming at mild 562 temperatures.

563

564 Prediction 2: Interaction strength determines consumer survival with increasing 565 temperatures.

566

Implications: If resources have a broader thermal range compared to consumers (Rose & Caron 2007; West & Post 2016), the thermal boundaries of the community can be determined by measuring solely the thermal dependence of interaction strength, κ . This quantity — the ratio of the resource equilibrium density without consumers (carrying capacity) to the resource equilibrium density with consumers — can be determined experimentally (Berlow *et al.* 2004) or through observations, facilitating predictions and cross-system comparisons thereof.

575 *Reasoning*: Close to the consumer extinction boundary, consumer survival becomes 576 extremely sensitive to all parameters apart from resource growth (Fig. 2, S5.1), making 577 accurate predictions challenging. Currently, consumer survival has been inferred through 578 energetic efficiency — the effective energetic gain of consumers at a certain resource density 579 — which requires determining the thermal dependence of the functional response (Vucic-580 Pestic et al. 2011; Archer et al. 2019). Not only is the functional response's thermal 581 dependence hotly contested (Uszko et al. 2017; Uiterwaal & DeLong 2020), but this 582 uncertainty will be exacerbated by its extremely high sensitivity at the community's thermal 583 boundaries. We showed there exists an alternative, empirically more direct and theoretically 584 more robust metric to determine consumer survival, and hence community feasibility. 585 Interaction strength — the relative values of resource equilibrium without and with 586 consumers (Berlow et al. 1999, 2004; Gilbert et al. 2014) - provides the necessary condition 587 for consumer survival (κ >1), when resources are thermal generalists compared to consumers. 588 This provides an accurate threshold and represents a measurable quantity that can be 589 standardised across experimental designs and study systems (Berlow et al. 2004).

590

591 *Prediction 3: Warming reduces community stability at low and mild temperatures*

592

Implications: This prediction rests on important assumptions: that resources have a broader thermal range, that organisms currently experience temperatures below their optima (Pawar *et al.* 2016) and that the functional response is of type II with a unimodal thermal dependence (Rall *et al.* 2012; Sentis *et al.* 2012; Kuiters 2013; West & Post 2016; Uszko *et al.* 2017; Uiterwaal & DeLong 2020). We deem these assumptions realistic based on the literature; 598 therefore, we argue that consumer-resource interactions at low and mild temperatures will be 599 destabilised by warming. At higher temperatures, warming should always enhance stability.

600

601 *Reasoning*: Stability in the context of consumer-resource interactions has predominantly 602 referred to a qualitative distinction between stable and oscillating dynamics (Rosenzweig & 603 MacArthur 1963; Yodzis & Innes 1992; Vasseur & McCann 2005). We based our analysis on 604 an adjusted stability metric which quantifies the tendency of dynamics to oscillate (Johnson 605 & Amarasekare 2015, SI 4). When comparing existing temperature parameterisations, we 606 found that in most monotonic parameterisations (increasing metabolism and attack rate, 607 decreasing handling time and carrying capacity, assimilation efficiency constant), warming 608 always (i.e., monotonically) stabilised dynamics (Fig. 7a, b, c). The single exception arose 609 when warming and carrying capacity increased simultaneously, which destabilised dynamics 610 (Fig. 7f). Carrying capacity has been described as a proxy for enrichment and its destabilising 611 effect has been established whether independently of temperature (Rosenzweig 1971) or as antagonistic to warming (Binzer et al. 2016). When at least one parameter in the functional 612 613 response had a unimodal thermal dependence (i.e., hump-shaped attack rate or U-shaped 614 handling time), this yielded a unimodal warming-stability relationship (Fig. 7d, e). Significantly, the divergence between the unimodal and (most) monotonic parameterisations 615 in the predicted effect of warming on stability manifested itself at low or mild, rather than 616 617 high temperatures (Fig. 6, 7). This pattern originates in the impact of the parameters with 618 unimodal thermal dependencies on stability. Attack rate is destabilising (Table 1, McCann 619 2011). Thus, a hump-shaped thermal dependence of attack rate destabilises dynamics with 620 warming below the thermal optimum and stabilises dynamics beyond it. Handling time is stabilising close to the thermal extremes (Fig. 6c, S5.2). A U-shaped handling time will 621 622 rapidly decrease with warming from low temperatures, which is strongly destabilising; a 623 corresponding steep increase at high temperatures produces a strong stabilising effect. Thus, 624 warming at high temperatures will always be stabilising. However, at lower temperatures, 625 unimodal and monotonic thermal dependencies produce contrasting warming-stability 626 relationships. Therefore, the thermal dependence shape of the functional response combined 627 with the temperatures currently experienced by communities relative to their optimal 628 temperature will determine the impact of warming on stability (Betini *et al.* 2019).

629

630 Prediction 4: Warming stabilises dynamics only when interaction strength decreases faster631 than maximal energetic efficiency

632

Implications: The combination of ρ — the energetic gain-to-loss ratio of consumers given 633 unlimited resources — and κ — interaction strength — accurately describes the warming-634 635 stability relationship with no recourse to the thermal dependence shapes of individual parameters, the current temperatures relative to the thermal optima, or the proximity to the 636 thermal boundaries of the community. Therefore, differential responses of resources and 637 638 consumers to warming (Dell et al. 2014) will be encompassed by the thermal dependence of the aggregates - assuming the consumer-resource system is well-described by the 639 640 Rosenzweig-MacArthur model. The Hopf bifurcation condition (eq. 6) dictates that κ should 641 decrease faster than ρ for warming to stabilise consumer-resource interactions. Thus, measuring ρ and κ directly can increase the accuracy of warming-stability predictions and 642 643 simplify cross-system comparisons.

644

Reasoning: Decreasing energetic efficiency or interaction strength have been considered
equivalent to increasing stability (Rall *et al.* 2008, 2010; Sentis *et al.* 2012). Thus, estimates
of consumer energetic efficiency or interaction strength based on empirically-derived thermal

648 dependence curves of individual rates (e.g. ingestion rate, attack rate, metabolic rate) have 649 been used to infer the impacts of warming on stability (Rall et al. 2010, 2012; Vucic-Pestic et 650 al. 2011; Fussmann et al. 2014). However, this raises two significant issues. On the one hand, 651 even subtle changes in the thermal dependence shapes of individual parameters can yield all 652 possible outcomes (Amarasekare 2015). On the other hand, reducing the analysis of stability 653 to a single aggregate parameter has limitations. Gilbert et al. (2014) described the warming-654 stability relationship with a single aggregate, interaction strength, but their approach was 655 based on a type I functional response and its predictions do not work well in type II or III 656 scenarios (Uszko et al. 2017). Johnson and Amarasekare (2015) and Amarasekare (2015) 657 attained a single aggregate parameter to reduce the complexity of their explorations; 658 however, this lacks descriptive power of the dynamics close to the community's thermal 659 boundaries (SI 4). Our analysis in the ρ - κ plane suggests that stability cannot be reduced to a 660 single aggregate parameter nor does a decrease in either one or both of ρ and κ suffice to 661 stabilise dynamics. In fact, both ρ and κ can decrease with warming while dynamics become destabilised. A stabilising effect of warming requires not only a concurrent reduction in ρ and 662 663 κ , but also the latter to decrease faster. Critically, both ρ and κ represent biological quantities which can be consistently measured across study systems. 664

665

666 *Working with the aggregate parameters*

667

Working directly with the two aggregate parameters, maximal consumer energetic efficiency, ρ , and interaction strength, κ , can simplify empirical measurements and improve the accuracy of theoretical predictions, particularly for field data and experiments, as we argue below. To determine the thermal dependence of maximal consumer energetic efficiency and interaction strength, one can measure consumer population growth given unlimited resources and 673 resource population density in presence and absence of consumers at different temperatures, 674 respectively. These measurements can be performed in the lab and the field. Interaction 675 strength is commonly determined in field experiments where consumers are excluded 676 (Berlow et al. 2004; Wootton & Emmerson 2005; Novak 2010; Estes et al. 2011). Consumer 677 energetic gain-to-loss ratio under effectively unlimited resources is more rarely estimated. 678 However, it can be derived from consumer population net growth and metabolism and 679 mortality, quantities measured commonly in the field and in the lab (Hanson & Peters 1984; 680 Stemberger & Gilbert 1985; Lampert et al. 1986). Moreover, confounding factors in field 681 measurements of the population-level aggregates should generate less uncertainty compared 682 to that of measuring multiple individual parameters, where uncertainty propagates and often 683 generates large uncertainty in model predictions (e.g. Sentis et al. 2015). Therefore, working 684 directly with the aggregate parameters can be both simpler and lead to more accurate 685 predictions in the field. On the other hand, measuring the individual parameters in the lab has 686 well-established protocols and a history of reliable outputs, with measurements requiring only 687 short-term experiments as opposed to the aggregates.

688

689 The choice between measuring the aggregate or the individual parameters will be informed 690 by the questions and objectives of each study. The aggregates describe population-level mechanisms of consumer-resource interactions, while the individual parameters correspond 691 692 to physiological or behavioural processes of individual organisms scaled up to the population 693 level. As we argued, the aggregates can provide more accurate predictions for field 694 measurements whereas individual parameters can be accurately measured in the lab. This 695 does raise the question whether measurements in a controlled laboratory environment can 696 represent noisier conditions in the field. It would be useful to compare directly measured aggregate parameters to aggregate parameter values derived from the individual parameters to determine how well predictions based on individual rates capture the dynamics of the system. Regardless of the choice, our approach provides the tools for both pathways: studies working with individual parameters will benefit from identifying the most important parameters to measure, while aggregate parameter datapoints can be directly mapped onto the ρ -κ landscape.

- 703
- 704 Subtleties and extensions
- 705

The sensitivity analysis quantified the sensitivity of the model variables to infinitesimal parameter changes. Therefore, applying its insights to data should take into consideration the scales of parameters in the temperature range of interest and potential uncertainties in the parameter estimates (Manlik *et al.* 2018, Fig. Sx). Hence, our argument for the reduced significance of the thermal dependence of assimilation efficiency in driving changes in biomass distributions, despite its high sensitivity.

712

Regarding the stability of consumer-resource interactions, the ρ - κ plane helped visualise the stabilising effect of a type III functional response (Fig. S2.1), which has both theoretical and empirical support (Sarnelle & Wilson 2008; Kalinkat *et al.* 2013; Uszko *et al.* 2017; Daugaard *et al.* 2019). For the type II response, the defining role of the functional response (attack rate) and the carrying capacity has been widely documented (Rosenzweig 1971; Amarasekare 2015; Johnson & Amarasekare 2015; Binzer *et al.* 2016); we add the important caveat that this is the case only far from consumer extinction (Fig. 6a).

721 Finally, relaxing certain assumptions can extend our approach. Considering the scenario 722 where the consumer has a broader thermal niche relative to that of the resource will make the 723 thermal limits of coexistence dependent on resource growth (Amarasekare 2015). 724 Considering the extinction of populations with very low abundances to account for stochastic 725 extinctions can define a realisable coexistence range within the feasible parameter space. 726 Breaking down the original model parameters (e.g. handling time includes the handling and 727 ingestion of prey) could facilitate our understanding of the role of more fundamental 728 physiological processes in the dynamics. Finally, climate change will lead to stronger 729 fluctuations in temperatures (IPCC 2013), which have been shown to alter predictions in 730 consumer-resource dynamics (Vasseur et al. 2014; Dee et al. 2020). This makes the inclusion 731 of temperature variability an important next step.

732

733 Conclusions

734

Warming will have significant, but as yet uncertain impacts on consumer-resource 735 736 interactions which underpin the structure and functioning of ecosystems. We presented an 737 approach that will help to improve the accuracy of predictions and reconcile divergent results by facilitating cross-system comparisons. This approach first determines the parameters 738 739 whose variations have the largest effect on community properties. Second, it simplifies 740 analyses to a two-dimensional plane of mechanistically tractable aggregate parameters; maximal consumer energetic efficiency and interaction strength. Applying it to consumer-741 742 resource biomass ratio and stability, we showed that close to the consumer extinction 743 boundary (i.e., at temperature extremes) both variables are most sensitive to changes in consumer assimilation efficiency and metabolism. Far from the boundary (i.e., mild 744 temperatures), biomass ratio is most sensitive to resource growth rate, consumer assimilation 745

746 efficiency and metabolism. This yielded our first prediction, that resource growth rate 747 regulates biomass distributions at mild temperatures. The consensus around the thermal 748 dependence of metabolism and the limited potential impact of warming on assimilation 749 efficiency, underscore the importance of correctly measuring the thermal dependence of resource growth rate. Using the two aggregate parameters also simplified the study of 750 751 important properties of consumer-resource interactions. From this followed our second 752 prediction, that the thermal boundaries of the community are defined by interaction strength 753 alone. In terms of stability, we demonstrated that a unimodal thermal dependence of attack 754 rate or handling time alters predictions of warming-stability relationships below the thermal optimum, where many organisms may be currently living. Hence our third prediction, that 755 756 initial increases in mean temperatures will destabilise consumer-resource interactions. 757 Significantly, our approach elucidates how the thermal dependence of stability can be comprehensively characterised by maximal energetic efficiency and interaction strength 758 759 values. This produced our fourth prediction; a faster reduction of interaction strength than of 760 maximal energetic efficiency with warming is necessary for dynamics to stabilise. Finally, we 761 demonstrated the potential for targeted experiments to measure the thermal dependencies of 762 maximal energetic efficiency and interaction strength to improve predictions. Ultimately, we show that any temperature parameterisation fitted to the Rosenzweig-MacArthur model can 763 764 be mapped onto the aggregate parameter plane, revealing its stability landscape, providing a 765 mechanistic interpretation for its predictions and allowing for the cross-system comparison of 766 these predictions.

767

⁷⁶⁸ Acknowledgments

We thank three anonymous reviewers and the editor for their constructive feedback. This
research is supported by the FRAGCLIM Consolidator Grant, funded by the European
Research Council under the European Union's Horizon 2020 research and innovation
programme (Grant Agreement Number 726176), and by the "Laboratoires d'Excellences
(LABEX)" TULIP (ANR-10-LABX-41).

- 775
- 776 **References**
- 777
- Amarasekare, P. (2015). Effects of temperature on consumer-resource interactions. *J. Anim. Ecol.*, 84, 665–679.
- Amarasekare, P. (2019). Effects of Climate Warming on Consumer-Resource Interactions: A
 Latitudinal Perspective. *Front. Ecol. Evol.*, 7.
- 782 Archer, L.C., Sohlström, E.H., Gallo, B., Jochum, M., Woodward, G., Kordas, R.L., et al.
- (2019). Consistent temperature dependence of functional response parameters and their
 use in predicting population abundance. *J. Anim. Ecol.*, 88, 1670–1683.
- Barbier, M. & Loreau, M. (2019). Pyramids and cascades: a synthesis of food chain
 functioning and stability. *Ecol. Lett.*, 22, 405–419.
- Berlow, E.L., Navarrete, S.A., Briggs, C.J., Power, M.E. & Menge, B.A. (1999). Quantifying
 Variation in the Strengths of Species Interactions. *Ecology*, 80, 2206.
- 789 Berlow, E.L., Neutel, A.M., Cohen, J.E., De Ruiter, P.C., Ebenman, B., Emmerson, M., et al.
- 790 (2004). Interaction strengths in food webs: Issues and opportunities. J. Anim. Ecol.
- 791 Betini, G.S., Avgar, T., McCann, K.S. & Fryxell, J.M. (2019). Temperature triggers a non
- ⁷⁹² linear response in resource–consumer interaction strength. *Ecosphere*, 10.
- 793 Bideault, A., Galiana, N., Zelnik, Y.R., Gravel, D., Loreau, M., Barbier, M., et al. (2020).
- 794 Thermal mismatches in biological rates determine trophic control and biomass

- 795 distribution under warming. *Glob. Chang. Biol.*, gcb.15395.
- Binzer, A., Guill, C., Brose, U. & Rall, B.C. (2012). The dynamics of food chains under
 climate change and nutrient enrichment. *Philos. Trans. R. Soc. B Biol. Sci.*, 367, 2935–
 2944.
- Binzer, A., Guill, C., Rall, B.C. & Brose, U. (2016). Interactive effects of warming,
 eutrophication and size structure: impacts on biodiversity and food-web structure. *Glob. Chang. Biol.*, 22, 220–227.
- Brown, J.H., Gillooly, J.F., Allen, A.P., Savage, V.M. & West, G.B. (2004). TOWARD A
 METABOLIC THEORY OF ECOLOGY. *Ecology*, 85, 1771–1789.
- 804 Caswell, H. (2019). *Sensitivity Analysis: Matrix Methods in Demography and Ecology*.
 805 Demographic Research Monographs. Springer International Publishing, Cham.
- BioControl, 55, 363–378.
 Dannon, E.A., Tamò, M., van Huis, A. & Dicke, M. (2010). Functional response and life
 history parameters of Apanteles taragamae, a larval parasitoid of Maruca vitrata.
- Daugaard, U., Petchey, O.L. & Pennekamp, F. (2019). Warming can destabilize predator–
 prey interactions by shifting the functional response from Type III to Type II. *J. Anim. Ecol.*, 88, 1575–1586.
- B12 Dee, L.E., Okamtoto, D., Gårdmark, A., Montoya, J.M. & Miller, S.J. (2020). Temperature
 813 variability alters the stability and thresholds for collapse of interacting species. *Philos.*814 *Trans. R. Soc. B Biol. Sci.*, 375, 20190457.
- Dell, A.I., Pawar, S. & Savage, V.M. (2011). Systematic variation in the temperature
 dependence of physiological and ecological traits. *Proc. Natl. Acad. Sci. U. S. A.*, 108,
 10591–10596.
- 818 Dell, A.I., Pawar, S. & Savage, V.M. (2014). Temperature dependence of trophic interactions
- 819 are driven by asymmetry of species responses and foraging strategy. J. Anim. Ecol., 83,

820 70–84.

- Beutsch, C.A., Tewksbury, J.J., Huey, R.B., Sheldon, K.S., Ghalambor, C.K., Haak, D.C., *et al.* (2008). Impacts of climate warming on terrestrial ectotherms across latitude. *Proc. Natl. Acad. Sci.*, 105, 6668–6672.
- Easterling, D.R., Meehl, G.A., Parmesan, C., Changnon, S.A., Karl, T.R. & Mearns, L.O.
- 825 (2000). Climate extremes: observations, modeling, and impacts. *Science*, 289, 2068–
 826 2074.
- Ehnes, R.B., Rall, B.C. & Brose, U. (2011). Phylogenetic grouping, curvature and metabolic
 scaling in terrestrial invertebrates. *Ecol. Lett.*, 14, 993–1000.
- Englund, G., Öhlund, G., Hein, C.L. & Diehl, S. (2011). Temperature dependence of the
 functional response. *Ecol. Lett.*, 14, 914–921.
- 831 Estes, J.A., Terborgh, J., Brashares, J.S., Power, M.E., Berger, J., Bond, W.J., *et al.* (2011).
 832 Trophic downgrading of planet earth. *Science (80-.)*.
- Fussmann, K.E., Schwarzmüller, F., Brose, U., Jousset, A. & Rall, B.C. (2014). Ecological
 stability in response to warming. *Nat. Clim. Chang.*, 4, 206–210.
- 835 Gilbert, B., Tunney, T.D., McCann, K.S., DeLong, J.P., Vasseur, D.A., Savage, V., et al.
- 836 (2014). A bioenergetic framework for the temperature dependence of trophic
 837 interactions. *Ecol. Lett.*, 17, 902–914.
- Gilooly, J.F., Brown, J.H., Geoffrey, B.W., Savage, V.M. & Charnov, E.L. (2001). Effects of
 Size and Temperature on Metabolic Rate. *Science (80-.).*, 293, 2248–2251.
- 840 Handeland, S.O., Imsland, A.K. & Stefansson, S.O. (2008). The effect of temperature and
- fish size on growth, feed intake, food conversion efficiency and stomach evacuation rate
 of Atlantic salmon post-smolts. *Aquaculture*, 283, 36–42.
- 843 Hanson, J.M. & Peters, R.H. (1984). Empirical prediction of crustacean zooplankton biomass
- and profundal macrobenthos biomass in lakes. *Can. J. Fish. Aquat. Sci.*, 41, 439–445.

- 845 IPCC, 2013: Climate Change 2013: The Physical Science Basis. Contribution of Working
- 846 Group I to the Fifth Assessment Report of the Intergovernmental Panel on Climate
- 847 Change [Stocker, T.F., D. Qin, G.-K. Plattner, M. Tignor, S.K. Allen, J. Boschung, A.
- 848 Nauels, Y. Xia, V. Bex and P.M. Midgley (eds.)]. Cambridge University Press,
- 849 Cambridge, United Kingdom and New York, NY, USA, 1535 pp.Jeschke, J.M., Kopp,
- M. & Tollrian, R. (2004). Consumer-food systems: Why type I functional responses are
 exclusive to filter feeders. *Biol. Rev. Camb. Philos. Soc.*
- Jeschke, J.M., Kopp, M. & Tollrian, R. (2004). Consumer-food systems: Why type I
 functional responses are exclusive to filter feeders. *Biol. Rev. Camb. Philos. Soc.*
- Johnson, C.A. & Amarasekare, P. (2015). A metric for quantifying the oscillatory tendency of consumer-resource interactions. *Am. Nat.*, 185, 87–99.
- Kalinkat, G., Schneider, F.D., Digel, C., Guill, C., Rall, B.C. & Brose, U. (2013). Body
 masses, functional responses and predator-prey stability. *Ecol. Lett.*, 16, 1126–1134.
- Kuiters, A. t. (2013). Diversity–stability relationships in plant communities of contrasting
 habitats. *J. Veg. Sci.*, 24, 453–462.
- Lampert, W., Fleckner, W., Rai, H. & Taylor, B.E. (1986). Phytoplankton control by grazing
 zooplankton: A study on the spring clear water phase. *Limnol. Oceanogr.*, 31, 478–
 490.
- Lang, B., Ehnes, R.B., Brose, U. & Rall, B.C. (2017). Temperature and consumer type
 dependencies of energy flows in natural communities. *Oikos*, 126, 1717–1725.
- Manlik, O., Lacy, R.C. & Sherwin, W.B. (2018). Applicability and limitations of sensitivity
 analyses for wildlife management. *J. Appl. Ecol.*, 55, 1430–1440.
- May, R.M. (1972). Limit cycles in predator-prey communities. *Science (80-.).*, 177, 900–
 902.
- 869 McCann, K.S. (2011). Food Webs (MPB-50) | Princeton University Press. Monograpsh Pop

- *Bio.* Available at: https://press.princeton.edu/books/paperback/9780691134185/foodwebs-mpb-50. Last accessed 10 September 2020.
- Montoya, J.M. & Raffaelli, D. (2010). Climate change, biotic interactions and ecosystem
 services. *Philos. Trans. R. Soc. B Biol. Sci.*, 365, 2013–2018.
- Novak, M. (2010). Estimating interaction strengths in nature: experimental support for an
 observational approach. *Ecology*, 91, 2394–2405.
- 876 O'Connor, M.I., Piehler, M.F., Leech, D.M., Anton, A. & Bruno, J.F. (2009). Warming and
 877 Resource Availability Shift Food Web Structure and Metabolism. *PLoS Biol.*, 7,
 878 e1000178.
- Parmesan, C. (2006). Ecological and Evolutionary Responses to Recent Climate Change. *Annu. Rev. Ecol. Evol. Syst.*, 37, 637–669.
- Pawar, S., Dell, A.I., Savage, V.M. & Knies, J.L. (2016). Real versus artificial variation in
 the thermal sensitivity of biological traits. *Am. Nat.*, 187, E41–E52.
- Petchey, O.L., Brose, U. & Rall, B.C. (2010). Predicting the effects of temperature on food
 web connectance. *Philos. Trans. R. Soc. B Biol. Sci.*, 365, 2081–2091.
- 885 Pörtner, H.O. & Farrell, A.P. (2008). Ecology: Physiology and climate change. *Science (80-.*886).
- Rall, B., Guill, C. & Brose, U. (2008). Food-web connectance and predator interference
 dampen the paradox of enrichment. *Oikos*, 117, 202–213.
- 889 Rall, B.C., Brose, U., Hartvig, M., Kalinkat, G., Schwarzmüller, F., Vucic-Pestic, O., et al.
- 890 (2012). Universal temperature and body-mass scaling of feeding rates. *Philos. Trans. R.*891 *Soc. B Biol. Sci.*, 367, 2923–2934.
- Rall, B.Ö.C., Vucic-Pestic, O., Ehnes, R.B., EmmersoN, M. & Brose, U. (2010).
 Temperature, predator-prey interaction strength and population stability. *Glob. Chang. Biol.*, 16, 2145–2157.

- Réveillon, T., Rota, T., Chauvet, É., Lecerf, A. & Sentis, A. (2019). Repeatable inter
 individual variation in the thermal sensitivity of metabolic rate. *Oikos*, 128, 1633–1640.
- Rip, J.M.K. & McCann, K.S. (2011). Cross-ecosystem differences in stability and the
 principle of energy flux. *Ecol. Lett.*, 14, 733–740.
- Root, T.L., Price, J.T., Hall, K.R., Schneider, S.H., Rosenzweig, C. & Pounds, J.A. (2003).
 Fingerprints of global warming on wild animals and plants. *Nature*, 421, 57–60.
- 901 Rose, J.M. & Caron, D.A. (2007). Does low temperature constrain the growth rates of
 902 heterotrophic protists? Evidence and implications for algal blooms in cold waters.
 903 *Limnol. Oceanogr.*, 52, 886–895.
- Rosenzweig, M.L. (1971). Paradox of Enrichment: Destabilization of Exploitation
 Ecosystems in Ecological Time. *Science (80-.).*, 171, 385–387.
- Rosenzweig, M.L. & MacArthur, R.H. (1963). Graphical Representation and Stability
 Conditions of Predator-Prey Interactions. *Am. Nat.*, 97, 209–223.
- Sarnelle, O. & Wilson, A.E. (2008). Type III Functional Response in Daphnia. *Ecology*, 89,
 1723–1732.
- Savage, V.M., Gilloly, J.F., Brown, J.H., Charnov, E.L. & Charnov, E.L. (2004). Effects of
 body size and temperature on population growth. *Am. Nat.*, 163, 429–41.
- 912 Sentis, A., Binzer, A. & Boukal, D.S. (2017). Temperature-size responses alter food chain
 913 persistence across environmental gradients. *Ecol. Lett.*, 20, 852–862.
- 914 Sentis, A., Hemptinne, J.L. & Brodeur, J. (2012). Using functional response modeling to
- 915 investigate the effect of temperature on predator feeding rate and energetic efficiency.
- 916 *Oecologia*, 169, 1117–1125.
- 917 Sentis, A., Morisson, J. & Boukal, D.S. (2015). Thermal acclimation modulates the impacts
- 918 of temperature and enrichment on trophic interaction strengths and population dynamics.
- 919 *Glob. Chang. Biol.*, 21, 3290–3298.

- Stemberger, R.S. & Gilbert, J.J. (1985). Body Size, Food Concentration, and Population
 Growth in Planktonic Rotifers. *Ecology*, 66, 1151–1159.
- 922 Thakur, M.P., Künne, T., Griffin, J.N. & Eisenhauer, N. (2017). Warming magnifies
 923 predation and reduces prey coexistence in a model litter arthropod system. *Proc. R. Soc.*924 *B Biol. Sci.*, 284, 20162570.
- Thomas, M.K., Kremer, C.T., Klausmeier, C.A. & Litchman, E. (2012). A global pattern of
 thermal adaptation in marine phytoplankton. *Science (80-.).*, 338, 1085–1088.
- 927 Uiterwaal, S.F. & DeLong, J.P. (2020). Functional responses are maximized at intermediate
 928 temperatures. *Ecology*.
- Uszko, W., Diehl, S., Englund, G. & Amarasekare, P. (2017). Effects of warming on
 predator-prey interactions a resource-based approach and a theoretical synthesis. *Ecol. Lett.*, 20, 513–523.
- 932 Vasseur, D.A., DeLong, J.P., Gilbert, B., Greig, H.S., Harley, C.D.G., McCann, K.S., et al.
- 933 (2014). Increased temperature variation poses a greater risk to species than climate
 934 warming. *Proc. R. Soc. B Biol. Sci.*, 281.
- Vasseur, D.A. & McCann, K.S. (2005). A mechanistic approach for modeling temperaturedependent consumer-resource dynamics. *Am. Nat.*, 166, 184–98.
- Vucic-Pestic, O., Ehnes, R.B., Rall, B.C. & Brose, U. (2011). Warming up the system: higher
 predator feeding rates but lower energetic efficiencies. *Glob. Chang. Biol.*, 17, 1301–
 1310.
- Walther, G.-R., Post, E., Convey, P., Menzel, A., Parmesan, C., Beebee, T.J.C., *et al.* (2002).
 Ecological responses to recent climate change. *Nature*, 416, 389–395.
- West, D.C. & Post, D.M. (2016). Impacts of warming revealed by linking resource growth
 rates with consumer functional responses. *J. Anim. Ecol.*, 85, 671–680.
- 944 Wootton, J.T. & Emmerson, M. (2005). Measurement of Interaction Strength in Nature.

- 945 Annu. Rev. Ecol. Evol. Syst., 36, 419–444.
- Wurtsbaugh, W.A. & Davis, G.E. (1977). Effects of temperature and ration level on the
 growth and food conversion efficiency of Salmo gairdneri, Richardson. *J. Fish Biol.*, 11,
 87–98.
- 949 Yodzis, P. & Innes, S. (1992). Body size and consumer-resource dynamics. *Am. Nat.*, 139,
 950 1151–1175.
- Zhang, L., Takahashi, D., Hartvig, M. & Andersen, K.H. (2017). Food-web dynamics under
 climate change. *Proc. R. Soc. B Biol. Sci.*, 284, 20171772.
- 953 Zhao, Q., Liu, S. & Niu, X. (2020). Effect of water temperature on the dynamic behavior of
- 954 phytoplankton–zooplankton model. *Appl. Math. Comput.*, 378, 125211.

Tables and Figures

957 Table 1. Sensitivities of the biomass ratio $(\partial_x B)$ and of the stability metric $(\partial_x S)$ with respect

958 to the six original model parameters. All sensitivities are expressed in terms of ρ and κ .

	Consumer-resource biomass	Stability matria C
Parameter	ratio, B	Stability metric, 3
x	$\partial_x \mathcal{B} = \frac{\partial \ln(\mathcal{B})}{\partial \ln(x)}$	$\partial_x \mathcal{S} = \frac{\partial \mathcal{S}}{\partial \ln(x)}$
r	1	0
K	$\frac{1}{\kappa-1}$	$-rac{\kappa}{ ho-1}$
а	$\frac{1}{\kappa-1}$	$-\frac{\kappa}{ ho-1}$
h	$-\frac{1}{(\rho-1)(\kappa-1)}$	$\frac{\kappa(1-\rho)+2\rho}{(\rho-1)^2}$
е	$\frac{\rho}{(\rho-1)(\kappa-1)}+1$	$-\frac{2\rho}{(\rho-1)^2}$
т	$-\frac{\rho}{(\rho-1)(\kappa-1)}-1$	$\frac{2\rho}{(\rho-1)^2}$





assimilated

dC

dt

962

963 Figure 1. Illustration of the current and new dual approaches to predict the impact of global 964 change drivers on community properties. 1) Predictions require a consumer-resource model; 965 the Rosenzweig-MacArthur model (Rosenzweig & MacArthur 1963) or its bioenergetic 966 equivalent (Yodzis & Innes 1992) have been used most commonly for ectotherm consumerresource pairs. 2a) The current approach is to experimentally measure the response of 967 968 parameters along an environmental gradient, e.g. the thermal dependence of the resource 969 population maximal growth rate with critical temperatures, CT_{min} , CT_{max} , and the thermal

970 optimum, T_{opt} . These measurements are used to parameterise the model. Importantly, not all 971 parameters are measured, but rather those which are considered significant (e.g. consumer 972 feeding and metabolic rates for warming-stability relationships). Assuming the remaining 973 parameter values, the model is then used to generate predictions. 2b) Our new dual approach 974 aims to increase the accuracy of predictions and facilitate their comparison. First a sensitivity 975 analysis determines which parameters have the greatest relative impact on the community 976 property of interest along the environmental gradient. Then, aggregate parameters which 977 represent biologically measurable quantities are used to express all sensitivities and 978 determine the dynamics. Collapsing analyses to the two aggregate parameters reduces 979 complexity and increases mechanistic tractability. This facilitates the choice of which 980 parameters need to be measured. 3) Through the empirical determination of the most 981 appropriate parameters (either from the original model parameters of the aggregate parameters themselves) and the reduction in the number of measurements required, prediction 982 983 accuracy improves. The advantages of the new dual approach are twofold. First, as the 984 sensitivity analysis will have identified the most impactful parameters, the source of 985 divergence in predictions can be isolated. Second, the aggregates represent standardised measurable population-level indicators across systems, making theoretical or empirical 986 987 predictions directly comparable.



Figure 2. Consumer-resource biomass ratios for the (a) unimodal and (b) monotonic parametrisations along the temperature gradient. Feasible temperature ranges are constrained by the condition of positive biomass densities for both consumer and resource (grey areas correspond to consumer extinction). The different background colours correspond to different elasticity rankings of model parameters (see legend). Panels (c) and (d) provide the values of the six parameter elasticities along the temperature gradient for the unimodal and monotonic parameterisations, respectively.



999 Figure 3. (a) Biomass ratio elasticity rankings in the ρ - κ plane. The plane is split into regions 1000 (different colours) which correspond to different parameters having the top-two largest 1001 elasticities. These regions have been derived from the analytic expressions of the elasticities 1002 (Table 1). e and m elasticities always rank first. Close to consumer extinction h ranks second 1003 highest at low ρ ($\rho < 2$, red region) and a and K at higher ρ ($\rho > 2$, yellow region). r ranks 1004 second highest far from consumer extinction (orange region). The plane includes the 1005 feasibility boundary (κ =1) and the Hopf bifurcation (dotted curve splitting the plane into 1006 stable equilibrium and oscillations). For the (b) unimodal and (c) monotonic parameterisations from the literature, the thermal dependencies of $\rho = \frac{e}{mh}$ and $\kappa = \frac{\kappa}{Rs}$ were 1007 calculated. This yielded a trajectory for each parameterisation (solid black line). The paths of 1008 1009 the trajectories demonstrate the elasticity of the biomass ratio along the temperature gradient 1010 for each parameterisation.



1012 Figure 4. Trajectories of the six empirical temperature parameterisations in the ρ - κ plane: a) 1013 Vucic-Pestic et al. (2011) with six different experiments - three predator size-classes and two 1014 types of prey, b) Fussmann et al. (2014), c) Binzer et al. (2016) with two levels of 1015 enrichment, d) Sentis et al. (2012), with two levels of enrichment, e) Uszko et al. (2017), f) 1016 Archer *et al.* (2019) with two prey types and three measurements. (a), (b) and (c) have 1017 monotonic thermal dependences for a, m (increasing) and h, K (decreasing), and a constant e. 1018 (d) has a unimodal thermal performance curve for a (hump-shaped), constant e and K, 1019 monotonic h (decreasing) and m (increasing). (e) has a unimodal (U-shaped) h and a (hump-1020 shaped) thermal dependence, constant e and monotonic K, m (increasing). (f) has monotonic 1021 a, K, m, e (increasing) and h constant. All parameter values are detailed in SI 4. The coloured 1022 regions demonstrate the different biomass ratio sensitivity rankings (see legend in Fig. 3a). 1023 The trajectories (solid black lines) for each parameterisation are derived from calculating the thermal dependence of $\rho = \frac{e}{mh}$ and $\kappa = \frac{K}{R_S}$ (see Temperature dependencies and 1024 1025 parameterisations for details).



1028 Figure 5. The thermal dependence of the stability metric, S, for the (a) unimodal and (b) 1029 monotonic parameterisations. S > 0 corresponds to stable dynamics, S < 0 to oscillations. S1030 =0 (dotted line) corresponds to the Hopf bifurcation. The coloured temperature ranges 1031 highlight regions of different sensitivity rankings. For temperatures beyond the community 1032 feasibility boundaries the areas are greyed out. In (c) and (d) the sensitivity to each parameter 1033 is plotted along the temperature gradient for the unimodal and monotonic parameterisations, 1034 respectively.





1036 Figure 6. (a) Stability metric sensitivity rankings in the ρ - κ plane. The plane is split into 1037 regions (different colours) which correspond to different parameters having the top-two 1038 largest sensitivities. These regions have been derived from the analytic expressions of the 1039 elasticities (Table 1). e and m rank first close to consumer extinction; h ranks second highest 1040 closest to consumer extinction (red region). The sensitivity of stability to a and K increases 1041 moving away from consumer extinction. a and K sensitivity ranks second (yellow region), 1042 and then first moving further away. Initially e and m rank second (green region) before h1043 becomes significant (blue region). The plane includes the feasibility boundary (κ =1) and the 1044 Hopf bifurcation (dotted curve splitting the plane into stable equilibrium and oscillations). 1045 For the (b) unimodal and (c) monotonic parameterisations from the literature, the thermal dependencies of $\rho = \frac{e}{mh}$ and $\kappa = \frac{K}{R_S}$ were calculated. This yielded a trajectory for each 1046 1047 parameterisation (solid black line). The paths of the trajectories demonstrate the dynamical 1048 regime and the sensitivity of the stability metric along the temperature gradient for each 1049 parameterisation.





1052 Figure 7. Trajectories of the six empirical temperature parameterisations in the ρ - κ plane: a) 1053 Vucic-Pestic et al. (2011) with six different interaction experiments - three predator size-1054 classes and two types of prey, b) Fussmann et al. (2014), c) Binzer et al. (2016) with two 1055 levels of enrichment, d) Sentis et al. (2012), with two levels of enrichment, e) Uszko et al. (2017), f) Archer et al. (2019) with two prey types and three measurements. (a), (b) and (c) 1056 1057 have monotonic thermal dependences for a, m (increasing) and h, K (decreasing), and a 1058 constant e. (d) has a unimodal thermal performance curve for a (hump-shaped), constant e 1059 and K, monotonic h (decreasing) and m (increasing). (e) has a unimodal (U-shaped) h and a 1060 (hump-shaped) thermal dependence, constant e and monotonic K, m (increasing). (f) has 1061 monotonic a, K, m, e (increasing) and h constant. All parameter values are detailed in SI 4. 1062 The coloured regions demonstrate the different biomass ratio sensitivity rankings (see legend 1063 in Fig. 6a). The trajectories (solid black line) for each parameterisation are derived from calculating the thermal dependence of $\rho = \frac{e}{mh}$ and $\kappa = \frac{\kappa}{R_s}$. Therefore, trajectories do not 1064 1065 change with the variable of interest; the sensitivity regions do.