Möbius strip microlasers

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Direct laser writing [1] enables the fabrication of almost arbitrary three-dimensional (3d) microstructures with feature sizes of less than 1 µm and allows to create 3d organic microlasers such as pyramids with high quality and low surface roughness [2]. Apart from 3d bulk resonators it is also possible to fabricate thin, curved waveguides to investigate how light propagates along a curved surface. We investigate the consequences of such a non-Euclidean geometry on the properties of a microlaser.

We fabricate organic microlasers in the shape of a Möbius strip [see Fig. 1(a)] made of a photoresist doped with a laser dye [3]. The Möbius strip is of particular interest since it exhibits topological properties impossible in two dimensions: it has only one surface and one boundary. We investigate how the topology and non-Euclidean geometry of the Möbius strip influences the structure of the lasing modes. In particular, the formation of whispering gallery modes propagating along the boundary as commonly observed for conventional ring resonators is impossible for the Möbius strip since its boundary features both concave and convex parts.

The spectrum of a Möbius microlaser [Fig. 1(b)] is dominated by a series of equidistant peaks, and its Fourier transform [inset of Fig. 1(b)] reveals the optical length of the underlying periodic ray trajectories. The classical ray trajectories in a resonator are determined by Fermat’s principle, and on a curved surface, the shortest path between two points is a geodesic. We hence surmise that the lasing modes of a Möbius microlaser are localized on periodic geodesics.

We calculate the modes of a Möbius strip resonator with FDTD simulations and its periodic geodesics with a ray tracing code based on Fermat’s principle. Figure 1(c) shows the intensity distribution of a low-loss resonant mode, and its structure is in good agreement with a periodic geodesic with 5 reflections at the boundary. The optical length of this as well as a few other periodic geodesics agrees well with the optical length obtained from the measured lasing spectrum. In conclusion, the experiments and simulations strongly indicate that the lasing modes of the Möbius microlaser are localized on periodic geodesics. These results open the way to further investigations of non-Euclidean photonic devices which can provide new ways of confining and manipulating light in optical microstructures.

References