

Experimental and numerical highlighting of water vapor sorption hysteresis in the coupled heat and moisture transfers

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Experimental and numerical highlighting of water vapor sorption

2 hysteresis in the coupled heat and moisture transfers

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Highlights

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- Experimental and numerical study of water vapor sorption hysteresis.
- Development of a coupled heat and mass transfer model with consideration of sorption
- 20 hysteresis.

- 21 Sorption hysteresis model allows a better adequacy of simulated results with experimental
- 22 ones.

- Non-hysteresis model shows various discrepancies and relative gaps between experimental
- and numerical results reached 28%.

Abstract

Heat, air and moisture transfers have a significant influence on indoor ambience and affect both temperature and hygrometry values and energy performance of buildings. Furthermore, high levels of humidity may lead to severe pathologies in building walls in addition to tamper indoor air quality and hygrothermal comfort. Sorption hysteresis phenomenon is responsible for the moisture accumulation in porous building materials, and leaving it out in hygrothermal modelling would result in an incorrect water content value.

The present work aims to highlight the influence of the sorption hysteresis phenomenon on heat and moisture transfer in expanded polystyrene concrete. In order to achieve this, a coupled heat and mass transfer model will be elaborated, taking consideration of sorption hysteresis phenomenon. Experimental protocols will be conducted to highlight the hysteresis in the materials, and the results will be compared to those of the numerical simulations. A simple hygrothermal transfer model without including hysteresis will also be used in the numerical simulations so that it is compared to the developed model. Experimental results show that considering the hysteresis phenomenon allows to better apprehend the hygrothermal behavior of building materials, and neglecting it leads to important differences sometimes reaching 28%.

Key words

- 43 Sorption hysteresis; Coupled heat and moisture transfers; Hygrothermal modelling;
- 44 Experimental characterization; Numerical simulations.

45 List of symbols

U: Volume water content (kg/m³) RH: Relative humidity (%)

ω: Mass water content (kg/kg) P_{vsat}: Saturation vapor pressure (Pa)

 U_v : Water vapor content (kg/m³) ρ_s : Density (kg/m³)

U₁: Liquid water content (kg/m³) K_m: Moisture diffusion coefficient (kg/m.s)

m: phase change ratio δ_a : Water vapor permeability of air (kg/m.s.Pa)

 j_{v} : Water vapor flux density (kg/m².s) μ : Water vapor diffusion resistance

j_l: Liquid water flux density (kg/m².s) H: Enthalpy (J/kg)

 j_m : Total mass flux (kg/m².s) ϕ : Total heat flux (W/m²)

 δ_v : Water vapor permeability ψ : Internal energy (J)

(kg/m.s.Pa)

 δ_l :Liquid water permeability C_p : Specific heat (J/g.K)

(kg/m.s.Pa)

 P_v : Water vapor pressure (Pa) λ : Thermal conductivity (W/m.K)

P_c: Capillary pressure (Pa) L_v: Latent heat of vaporization (J/kg)

C_{pv}: Specific heat of water vapor (J/g.K) R: Gaz constant (J/K.mol)

T : Temperature (K) M : Molar mass (kg/mol)

1. Introduction

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Indoor air humidity is as important as indoor air temperature, since moisture can significantly influence the energy performance of households [1,2], and is one of the main causes of its deterioration [3,4]. Moisture in porous building materials can also greatly affect the indoor air quality and comfort of occupants, given that excessive low or high humidity can cause multiple respiratory pathologies and allergies [5]. To predict those effects, moisture transfer has been studied for a long time, especially in unsaturated porous media based on Darcy and Fick's laws [6,7]. To avoid moisture condensation, insulation failure or mold

growth in building materials, coupled heat and moisture transfers should be studied together for a better prediction of the hygrothermal behavior of the building, and thus optimize its design [8-10]. Hygrothermal transfers are often expressed using mainly phenomenological models [11,12] or models that consider the materials microstructure through porosity or pore size distribution [13,14].

Adsorption and desorption isotherms are among the most important hydric properties of porous building materials, since they describe the equilibrium water content as a function of the ambient relative humidity, at a certain temperature. Cement based materials often exhibit a hysteresis loop, meaning the moisture content at the same relative humidity is different whether the material experiences wetting or drying. Therefore, the moisture content also depends on the hydric history of the material [15], and the water content follows the intermediate scanning curves (fig.1, curves B and D) located between the two main adsorption and desorption curves (fig.1, curves A and C) [16].

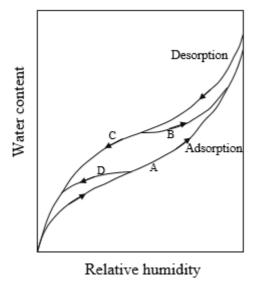


Fig.1 Sorption hysteresis curves [17]

Sorption hysteresis should then be taken into consideration in any hygrothermal transfers research, since it illustrates the fact that it is easier for water to get in than to get out

of a porous medium [18] and is highly correlated to capillary forces [19]. In the past few decades, the interest about this phenomenon has highly increased, and researchers began developing hygrothermal models considering the effect of sorption hysteresis. However, it remains unknown and less studied in the literature, unlike other conventional phenomena such as hydration or carbonation.

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Some researches exhibited sorption hysteresis experimentally and considered it in the heat and mass transfers modelling. In his work, Zhang [20] studied cement pastes initially saturated, then subjected to hydric cycles varying from 33% to 80% and finally 53,5% of relative humidity. He then validated his hygrothermal model using experimental saturation profiles. However, he only subjected the samples to only one cycle of wetting and drying, which is not representative of buildings. Ait Oumeziane [21] also studied sorption hysteresis phenomenon in a hemp concrete, a very hygroscopic material. Samples were subjected to many cycles of 75% of relative humidity during 8h, then 33% during 16h, corresponding to the NORDTEST protocol for the determination of Moisture Buffer Value [22]. However, some input parameters were only taken from literature and not measured for the studied material, and thermal conductivity dependency was modeled based on its values at the dry and saturated state only. The evolution of the water content in the material was compared to numerical simulations. In line with this work, Lelièvre [23] also studied hysteresis in hemp concrete through three different experimentations. The difference lies in the duration of the relative humidity levels, which varies from few hours to few days. Nevertheless, thermal properties of the material were considered constant regardless of its water content, and most of the input parameters were taken from previous works in literature.

Other researches designed sorption hysteresis modelling using a physical approach, based on the microstructure of the materials. Schiller et al. [24] recently proposed a hysteresis model in hardened cement pastes with consideration of the sorption in the interlayer space

between the C-S-H sheets, which is supposed to be responsible for low-pressure hysteresis of water sorption isotherms. Their work is based on a macroscopic approach using a simple mathematical model coupled to volume change diagrams. Only computed hysteresis loops were compared to those observed experimentally. Jiang et al. [25] developed a model to predict water vapor sorption hysteresis of cement-based materials based on pore size distribution obtained from adsorption isotherms. No suited experimental campaign was led to validate the model, which was verified using water vapor sorption isotherms from literature. However, sorption isotherms are determined at equilibrium, while materials in buildings undergo dynamic humidity variations.

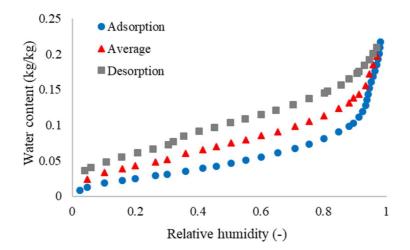


Fig.2 Main and average sorption curves for hemp concrete [26]

In most of the numerical studies of hygrothermal transfers, sorption hysteresis is often neglected. Some works prefer to overestimate the water content and consider that it varies according to the evolution of the main desorption curve for each variation of the daily relative humidity, whether it is a wetting or a drying [27 – 29]. Some researchers assume that the water content rather follows the path of the main adsorption curve and do not consider sorption hysteresis [18], and others even consider a mean curve between the main sorption isotherms, introducing some weighting coefficients [20]. These choices are difficult to justify, given that water content in a porous material follows different paths whether it is subjected to

a wetting or drying. In fact, at the same relative humidity, water content has two different values, and the relative gap between them is very high. In the case of very hygroscopic materials such as hemp concrete [26], the difference can go from 50% to 100%, as shown in figure 2.

The water content depends then on the relative humidity of the environment in addition to the previous hydric states of the material. Therefore, sorption hysteresis must be taken into account in the modelling of coupled heat and mass transfers in building materials, because it allows determining a more precise value of water content at any given time.

In this context, we propose a hygrothermal transfer model considering the sorption hysteresis phenomenon using the sorption isotherms. The heat and mass transfer model is based on Luikov's equations [30], including some improvements in the hypotheses. Indeed, input parameters were not supposed constant, and their temperature and water content dependency were considered. Sorption hysteresis phenomenon is also considered, and an adequate experimental campaign was carried on in order to validate the computed results. Moreover, in order to reduce the environmental footprint of building sector, a recycled expanded polystyrene mortar will be the material of interest. It is an eco-friendly material that helps reuse the expanded polystyrene waste and has improved thermal insulation properties. It is a highly heterogeneous material with a complex microstructure, and is composed of two materials whose hygrothermal behavior highly varies.

In what follows, the hygrothermal model will be presented, along with its implementation on Matlab and Comsol multiphysics. The experimental setup allowing the highlight of hysteresis will be presented, and the obtained results will be compared to the ones from the numerical calculations using the hysteresis model. A non-hysteresis model will also be used in order to enhance the influence of the sorption hysteresis phenomenon. It is

implemented using the main adsorption isotherm only, and it aims to show the importance ofsorption hysteresis consideration in hygrothermal transfers modelling.

2. Modelling

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2.1. Heat and mass transfers modelling

In this study, the implemented model is a coupled heat and mass transfers model using respectively temperature and water content as driving potentials. Afterwards, it will be coupled to a physical model that allows calculating the water content inside the pores from the ambient relative humidity with the consideration of sorption hysteresis.

The mass balance equations for the water vapor and liquid water phases respectively are written below:

$$\frac{\partial U_{v}}{\partial t} + \operatorname{div}(j_{v}) = -m \tag{1}$$

$$\frac{\partial U_l}{\partial t} + \operatorname{div}(j_l) = m \tag{2}$$

By adding the two equations, we obtain the equation (3) that simplifies into equation (4).

$$\frac{\partial U_{v}}{\partial t} + \frac{\partial U_{l}}{\partial t} + \operatorname{div}(j_{v}) + \operatorname{div}(j_{l}) = 0$$
(3)

$$\frac{\partial U}{\partial t} + \operatorname{div}(j_{v} + j_{l}) = 0 \tag{4}$$

Given that the volume water content is function of the mass water content and the materials density (equation (5)), the mass balance equation becomes equation (6).

$$U = \rho_{\rm S} \times \omega \tag{5}$$

$$\rho_{s} \frac{\partial \omega}{\partial t} + \operatorname{div}(j_{v} + j_{l}) = 0 \tag{6}$$

Flux densities of water vapor and liquid water can be expressed using adequate diffusion coefficients, which depend on the hydric state of the material as:

$$j_{v} = -\delta_{v}. \nabla P_{v} \tag{7}$$

$$j_l = -\delta_l \cdot \nabla P_c \tag{8}$$

In order to simplify the boundary conditions, water vapor content is considered the only driving force of the mass transfers. Moreover, both the water vapor pressure and the capillary pressure are related to relative humidity through the saturated vapor pressure and Kelvin law.

$$P_{v} = RH \times P_{vsat} \tag{9}$$

$$P_{c} = \frac{RT\rho_{l}}{M} \ln(RH) \tag{10}$$

- Given the dependency of relative humidity on the temperature, the derivative of equation (10)
- is expressed as follows [31]:

$$\nabla P_{c} = \left[\frac{RT\rho_{l}}{M} \frac{1}{RH} \nabla RH \right] + \left[\frac{RT\rho_{l}}{M} \left(\frac{\partial \ln(RH)}{\partial T} \right) + \frac{R\rho_{l}}{M} \ln(RH) \right] \nabla T$$
 (11)

- 170 The thermal diffusion is negligibly small, and considered of no importance in building science
- applications [32,33]. Therefore, the total mass flux can be expressed in the equation (12).

$$j_{m} = -\left[\delta_{v} P_{vsat} + \delta_{l} \frac{RT\rho_{l}}{M} \frac{1}{RH}\right] \nabla RH$$
 (12)

- The moisture storage capacity C_m is defined as the slope of the sorption isotherm curves [34].
- 174 It is then a function of relative humidity and water content. It is an important property of the
- material as it represents the water accumulation in the pores due to sorption hysteresis.

$$C_m = \frac{\partial \omega}{\partial RH} \tag{13}$$

177 The final expression of the mass balance equation is then explicated in equation (14).

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$$\rho_{s} \frac{\partial \omega}{\partial t} - \operatorname{div} \left[\frac{K_{m}}{C_{m}} (\nabla \omega) + \frac{\delta_{l}}{C_{m}} \frac{R.T_{ref}.\rho_{l}}{M.RH} (\nabla \omega) \right] = 0$$
 (14)

We set $K_l = \frac{\delta_l}{C_m} \frac{\text{R.T}_{ref} \cdot \rho_l}{\text{M.RH}}$ to simplify the mass balance equation.

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$$\rho_{s} \frac{\partial \omega}{\partial t} - \operatorname{div} \left[\frac{K_{m}}{C_{m}} (\nabla \omega) + K_{l} (\nabla \omega) \right] = 0$$
 (15)

The moisture diffusion coefficient that appeared in the mass balance equation is defined as below [23, 35, 36]:

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$$K_m(\omega) = \frac{\delta_a}{\mu(\omega)} P_{\text{vsat}} = \delta_{\text{v}}(\omega) P_{\text{vsat}}$$
 (16)

The heat balance equation is expressed in the equation (17) [36]. We only consider heat transfers due to conduction, convection and phase change, and we neglect the radiation phenomenon. The final conservation of energy equation is then as:

$$C_{p}\rho_{s}\frac{\partial T}{\partial t} - \operatorname{div}(\lambda \nabla T) - K_{m}C_{pv}\nabla T - m L_{v}\omega = 0$$
(17)

2.2. Initial and boundary conditions

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The boundary conditions in this paper are Dirichlet type, and the temperatures and relative humidities are directly applied to the exterior surfaces of the sample.

$$\begin{cases} \omega(x=0,t)=\omega_1(t)\\ T(x=0,t)=T_1 \end{cases} \quad \text{and} \quad \begin{cases} \omega(x=L,t)=\omega_2(t)\\ T(x=L,t)=T_2 \end{cases} \tag{18}$$

Where L is the thickness of the sample. The initial conditions are considered uniform in the material and expressed as follows:

$$\begin{cases}
\omega(x, t = 0) = \omega_0 \\
T(x, t = 0) = T_0
\end{cases}$$
(19)

2.3. Input parameters

The input parameters of the heat and mass transfers model are the hygrothermal properties of the material, that were determined using an experimental campaign. The moisture storage capacity Cm is obtained through the water vapor sorption isotherm curves presented later.

The thermal conductivity of the material depends on the temperature and the water content of the material, and it was experimentally determined based on the guarded hot plate method [37]. The thermal conductivity of the polystyrene mortar can be expressed as a function of temperature as follows:

$$\lambda = 0,0005.T + 0,1472 \tag{20}$$

The thermal conductivity was also measured depending on the hydric state of the material. Its dependency on the water content is expressed in equation 21.

$$\lambda = 0.3663. \omega + 0.1413 \tag{21}$$

The water vapor permeability of polystyrene concrete depends on the materials water content, and it was experimentally determined following the cup test method based on the standards NF EN ISO 12572 [38]. This method allows determining the water vapor permeability at a low and a high relative humidity (3% and 93%). Hence, water vapor permeability will have two different values whether the ambient relative humidity is high or low.

ρ_s (kg/m3)	537	C _p (J/kg.K)	971
Tref (K)	273,15	C _{pv} (J/kg.K)	1860
δ _v (kg/m.s.Pa)	3,22.10 ⁻¹² at low RH 1,2.10 ⁻¹¹ at high RH	m (-)	0,3
L _v (J/kg)	$2,5.10^6$		

 Table 1. Input parameters

2.4. Sorption hysteresis modelling

The coupled heat and mass transfers model will be coupled to a sorption hysteresis model. Therefore, in addition to taking into account the moisture accumulation inside the pores through the moisture storage capacity, it will be able to calculate the real value of water

content from the ambient relative humidity. The sorption hysteresis model chosen for this work is the one developed by Carmeliet [39], which is a physical model based on the theory of the independent domains and the ink-bottle pore effect, elaborated by Mualem [40,41]. In previous works, this model was proven to be the most representative to the hysteretic behavior of cement based materials [21,23].

The use of empirical hysteresis models often leads to a hysteretic behavior called "pumping effect". It reflects the fact that the numerical scanning curves do not respect the closing principle. In other words, this means that during a succession of adsorption and desorption cycles, there is a unique water content value for each extremum of relative humidity. Therefore, a material undergoing several cycles of wetting /drying should normally return to its initial relative humidity and water content.

Some researches [20,42,43] consider that the pumping effect is not a physical characteristic specific to the material, but that it is entirely artificial. It is then considered as errors generated by the calculation algorithms. Mualem model – and therefore Carmeliet model – respects the closing principle and makes it possible to avoid pumping errors, confirming its accuracy in hysteresis modelling [29,23].

The sorption hysteresis model developed by Carmeliet allows calculating modelled hysteresis loops from the main adsorption and desorption isotherm curves. It is based on the theory of independent domains, considering the ink-bottle shaped pores. It expresses the water content in the scanning curves in different expressions, whether it is a wetting or a drying, in terms of water content in the main sorption isotherms, and some specific values such as saturation point.

The equation describing the water content in adsorption scanning curves is recalled below.

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$$\omega_{ads,hvst}(RH,i) = \omega_{i-1} + (1 - A(RH_{i-1}))(\omega_{ads}(RH) - \omega_{ads}(RH_{i-1})).$$
 (22)

The "i" indicates the inversion point which is the exact time of going from an adsorption to a desorption (and vice versa). In equation (22), the "i" here marks the inversion between the i-1th desorption scanning curve and the ith adsorption scanning curve.

The equation describing the water content in desorption scanning curves is expressed in (23). In this case, the "i" marks the inversion between the i-1th adsorption scanning curve and the ith desorption scanning curve, as explicated in figure 3.

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$$\omega_{\text{des,hyst}}(RH, i) = \omega_{i-1} - (1 - A(RH))(\omega_{\text{ads}}(RH_{i-1}) - \omega_{\text{ads}}(RH)),$$
 (23)

248 Where
$$A(RH) = \frac{\omega_{des}(RH) - \omega_{ads}(RH)}{\omega_{sat} - \omega_{ads}(RH)}$$
 (24)

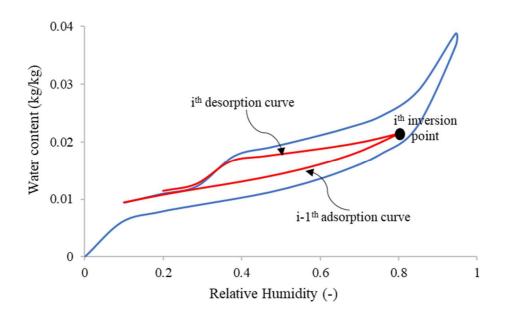


Fig.3 Schematic representation of the ith inversion point

The water content associated to each varying value of relative humidity is calculated whether it is a wetting or a drying. For that, we need to know and memorize the inversion points. It is then necessary to indicate a transition criterion between the different phases of wetting/drying, along with a list of the inversion points [21]. Equation (25) expresses the condition of the transition from the adsorption curve to the desorption curve, and vice versa.

When the inversion criterion is less than zero, there is a transition from a sorption phase to the other, and the new inversion point is added to the list.

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$$L_{inv} = (RH(n) - RH(n-1)) \times (RH(n-1) - RH_{i-1})$$
 (25)

RH(n) represents the relative humidity of the material at the time n, RH(n-1) at the time n-1, and RH_{i-1} corresponds to the relative humidity of the last identified inversion point. The iterations in the program stand for the time. There is an inversion if the inversion criterion is less than zero. In this case, this new point is saved and becomes the last identified inversion point. The values of relative humidity and water content are therefore calculated at each time, and the water capacity is calculated differently whether it is an adsorption or a desorption.

As shown in figure 4, MATLAB software was used to compute the hysteresis model, coupled to COMSOL Multiphysics where the hygrothermal model was implemented. The experimental values of ambient relative humidity and the main adsorption and desorption curves are first introduced in MATLAB where the hysteresis model allows the calculation of the corresponding values of water content, in addition to the moisture storage capacity. These values are then imported into COMSOL along with the input parameters consisting in the hygrothermal properties of the material of interest. The resolution in Comsol is based on the finite elements method following three basic steps, namely pre-processing, solver, and post-processing. It generates a set of equations for all the involved physical models and implements them in a single iteration scheme, which is repeated until convergence is reached. Comsol has several solvers all based on finite elements method, then chooses the most suitable one to ensure stability and convergence of the solutions. The time dependent solver is computing the solution to a possibly nonlinear system of equations at each time step via a set of iterative techniques based upon Newton's method. These Newton's method techniques for solving a nonlinear system of equations evaluate a function, as well as its derivative, at every

time step. This derivative is also known as the Jacobian and is relatively expensive to compute. Therefore, the software will try to minimize reevaluating the Jacobian, by default. If the nonlinear solver has difficulty converging, it will reduce the requested time step size and try to compute the solution.

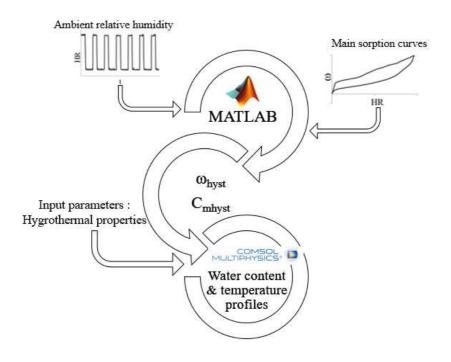


Fig.4 Hysteresis modelling steps

3. Materials and methods

In this study, the coupled heat and moisture transfers model developed is based on phenomenological modelling, where the relevance of the prediction is conditioned by a reliable evaluation of the input data. The hygrothermal properties that constitute the input parameters of the implemented model were experimentally determined using standard laboratory methods. A part of this section was dedicated to a fine, experimental characterization of the intrinsic hydric and thermal properties of the material. The material of interest in this work is a polystyrene mortar made of recycled expanded polystyrene granules and a CEMII cement as a binder [44,45].

Computing the coupled heat and mass transfers involves the experimental determination of the hygrothermal properties of the material. The experimental campaign aimed to measure the water vapor permeability using the wet cup/dry cup method based on the EN ISO 12572 norm [46], the thermal conductivity using the Guarded Hot Plate method based on the NF EN 12667 norm [47], and the heat capacity using a 3D sensors calorimeter.

In addition, the implementation of the hysteresis model requires the determination and modelling of the main adsorption and desorption curves of the material. The experimental isotherm curves were determined using the gravimetric technique that is based on continuous successive weightings. The test was performed on a very recent vapor sorption analyzer that allows measuring the mass evolution of the samples. For the polystyrene mortar, the main isotherms are modelled using the equation below [39], which proves a good adequacy between the experimental and the modelled curves, as shown in figure 5.

$$\omega(RH) = \omega_{sat} \left(1 - \frac{\ln(RH)}{A}\right)^{-1/n}$$
 (26)

A and n are empirical calibration coefficients. These parameters were adjusted using the experimental data presented in figure 5. The fitting parameters are presented in table 2, and are different whether it is adsorption or desorption. The root mean squared error between the experimental data and the adjustment curves is 0,2%.

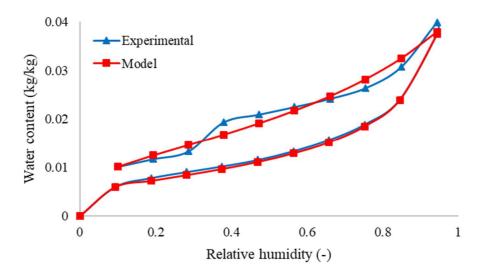


Fig.5 Main adsorption and desorption isotherm curves of polystyrene mortar

This model precisely reproduces the sorption isotherms of the polystyrene mortar in adsorption phase, and is less accurate in desorption phase. This is due to the sudden decrease of water content in the main desorption curve between 30% and 40% of relative humidity, that is very difficult to model.

	A	n	R ²
Adsorption	0,033	1,796	0,996
Desorption	0,399	1,35	0,965

Table 2. Fitting coefficients for the main sorption isotherms

During the daily variations of relative humidity and temperature, the water content inside building materials varies according to the intermediate sorption isotherms. In order to characterize experimentally the intermediate curves of the expanded polystyrene mortar, the total water content is measured at the equilibrium when subjecting the material to different relative humidity levels. The experimental method used here was the gravimetric technique that is based on continuous successive weightings. The test was performed on three cubic samples of $10x10x10 \text{ mm}^3$ dimensions previously dried at 60° C. The temperature was fixed at 23° C and the relative humidity variations are presented in figure 6.

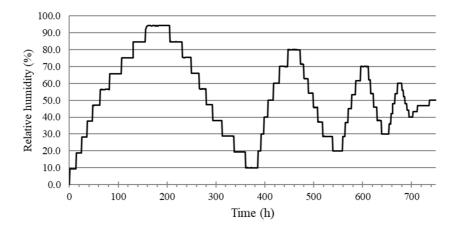


Fig.6 Relative humidity variation during the determination of the intermediate isotherms

A second experimental campaign dedicated to the validation of the model was performed. The objective is to assess the relevance of the coupled heat and moisture transfers model by confronting it to experimental results on the one hand, and on the other hand to highlight the influence of considering the hysteresis of water content in the developed model. The experimentation consists of imposing a unidirectional transfer through cylindrical samples by applying a thermal and hydric insulation on all the surfaces but one, as schematized in figure 6. Hygrothermal sensors are introduced inside the samples in order to record the temperature and relative humidity evolution. The sensors were positioned 1,5cm away from the surface of the sample, as shown in figure 7. The samples were then be subjected to cyclic solicitations in temperature and relative humidity applied on the exposed surface. Samples are initially conditioned at 50% of RH and 25°C.

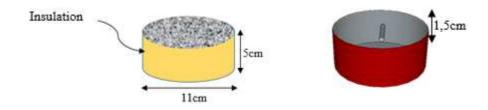


Fig.7 Samples dimensions (left) and sensors disposition (right)

The experimental setup is presented in figure 8, and is composed of a climatic chamber in charge of the ambient conditions and a high accuracy ambiance sensor ensuring compliance with the ambient conditions imposed on the sample in terms of temperature and relative humidity. High precision sensors are also put inside the samples in order to obtain the temperature and water content profiles at different positions in the material. Each sample is put on a scale so that it can measure the total water content during the experimentation. The climatic chamber is of type Memmert HCP240 and the ambience sensor is a psychrometer of high precision (\pm 1% in the whole relative humidity range). The hygrothermal sensors used inside the samples are capacitive humidity sensors FHA 646 R, characterized by \pm 2% of precision in relative humidity range and \pm 0,2K for a temperature from 0 to 70°C.

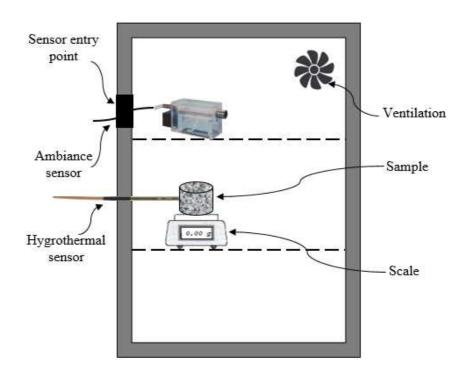


Fig.8 Experimental setup diagram

For us, to study the materials response to long and short cyclic solicitations, three different hygrothermal conditions were tested. The first protocol is set in a way to consider the reaction of the material to hydric solicitations with low drying kinetics, at a constant temperature. The two other protocols aim to simulate the daily variations of climatic

conditions, but one is at a constant temperature, and in the other one it varies along with the relative humidity. The detailed solicitations and their durations are presented in table 3.

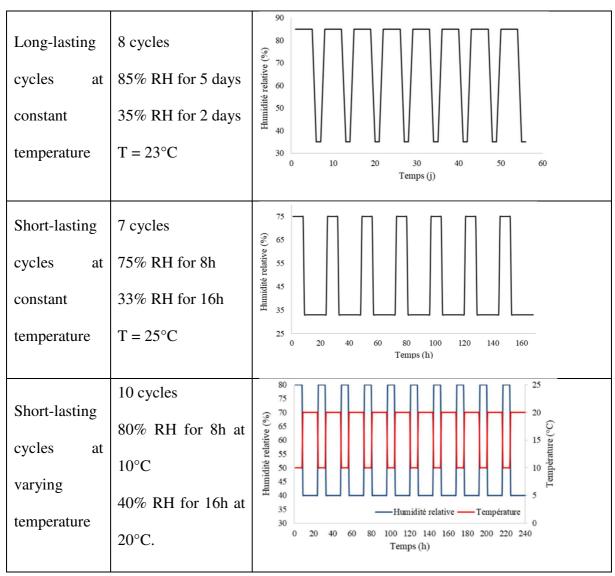


Table 3. Experimental hydric and thermal conditions

4. Results and discussion

In the following, the experimental and numerical results are presented. First, the intermediate adsorption and desorption curves of the polystyrene mortar are presented, in addition to the experimental and modelled moisture storage capacity curve. Afterwards, the experimental water content profiles inside the samples, along with the simulated water content profiles are presented simultaneously in order to compare both. The three different

experimental protocols presented in table 3 are treated separately, in order to compare between the experimental and simulated profiles in each case.

4.1. Main and intermediate sorption curves

The experimental adsorption and desorption curves of the polystyrene mortar are presented in the figure 9. Given that the sample was initially at a dry state, the first curves are the main adsorption and desorption isotherms, while all the others represent the intermediate curves. The scanning curves are all located between the main curves, which represent an envelope curve. They have the same look and vary in the same way, they even present the abrupt decrease in desorption around 30% of relative humidity. After four cycles of the wetting and drying cycles presented in figure 6, the intermediate curves overlap, thus the 4th adsorption curve and the 3rd desorption curve are imbricating. These results come from the water accumulation in the materials porosity and the sorption hysteresis phenomenon, since the relative humidity conditions are narrowed down after each cycle.

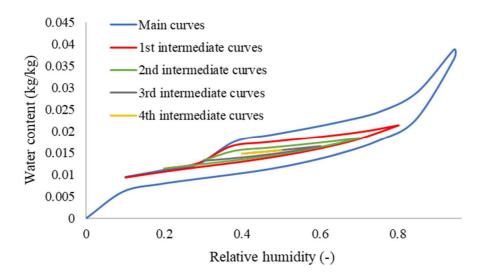


Fig.9 Main and intermediate sorption isotherm curves of the polystyrene mortar

The intermediate curves represent the variations of water content of the material under cyclic varying relative humidity. The hysteresis model developed by Carmeliet [39] should be able to model the water content so that it can follow the same path. In the figure 10, the

experimental and modelled intermediate curves are compared, and show a better adequacy in adsorption phases. On the other hand, in the desorption phases, the modelled curves underestimate the experimental curves and almost overlap. This is due to the sudden decrease of water content in the main desorption curve between 30% and 40% of relative humidity. Indeed, the sudden variation is very difficult model, and the modelled main desorption curve tend to underestimate the experimental one. Therefore, all the following intermediate curves are underestimating the water content values. Moreover, Carmeliet model ensures the closing principle that helps avoiding pumping errors and each scanning adsorption and desorption curve meet at the same value of water content.

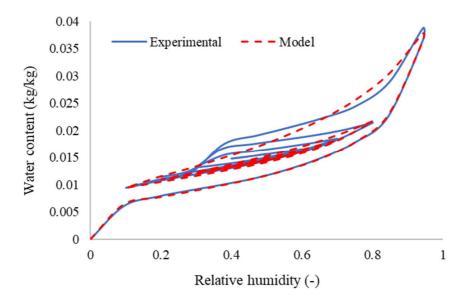


Fig.10 Experimental and modelled main and intermediate sorption curves of the polystyrene

mortar

The hysteresis model is also used to model the moisture storage capacity of the material in order to evaluate its accuracy. Moisture storage capacity is defined as the derivative of the water content in relation to the relative humidity; it can then be obtained from the sorption curves. In order to verify the accuracy of the hysteresis model, modelled moisture storage capacity of polystyrene mortar is compared to the experimental in figure 11. During the adsorption phase, the modelled moisture capacity shows very good concordance

with the experimental curve, since the highest difference is only 8%. In desorption, the model give less adequate results and display bigger differences up to 30%. However, the variations of the modelled curves look like the experimental ones, and the model allows preserving the shape of the experimental curve.

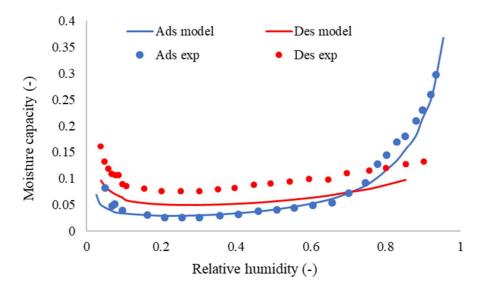


Fig.11 Experimental and modelled moisture storage capacity of polystyrene mortar

4.2. Water content evolution through time

In the following, the experimental water content profiles inside the samples are presented. They are compared to the numerical profiles obtained through simulations using the hysteresis model presented in the previous parts. A non-hysteresis model will also be used in order to assess the importance of the phenomenon consideration in the hygrothermal transfers modelling in building materials. The results of each experimentation is presented apart from the others below.

4.2.1. Long lasting cycles at constant temperature

Numerical and experimental results of the water content profiles in the samples submitted to long lasting cycles at constant temperature are presented in figure 12. Using the non-hysteresis model, the evolution of water content represents a curve below the experimental

results and underestimates the actual values. In the adsorption phase, the difference between the experimental and simulated curves is relatively low, and the highest relative gap observed is 5%. On the contrary, during desorption, the non-hysteresis model underestimates the real water content values. The difference in this case is highly significant and the simulated values show relative gaps reaching 28%.

The profiles obtained with the hysteresis model show a good adequacy with the experimental results, except the first adsorption cycle where the difference is relatively high. Indeed the numerical values of water content are lower than the experimental ones, and a 7% relative difference is recorded at the peak of the first cycle. Concerning the remaining cycles, the numerical curves are in good concordance with the experiments and the relative differences do not exceed 2%.

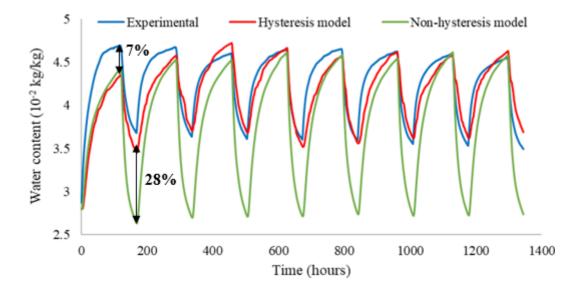


Fig.12 Experimental and numerical water content profiles in the first test

The discrepancy in the first cycle could result from a delay of the model, due to the initial conditions. In fact, the material is initially conditioned at 60% of relative humidity, which corresponds to a water content of 2.8% kg/kg before going through the first adsorption. In the model, the initial water content put in the input parameters corresponds to that. Afterwards, at

the end of each desorption cycle, the sample has a water content of about 3.5% kg/kg. Therefore, during humidification where the relative humidity is at 85%, it is easier for the material to reach the maximum water content (4.7% kg/kg) when it is at 3.5% kg/kg than when it is at its initial value. In reality, polystyrene mortar is not very hygroscopic, and so it quickly reaches the maximum water content even when it is at the initial water content.

4.2.2. Short lasting cycles at constant temperature

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The second experiment consists of short lasting cycles at constant temperature, and the water content profiles are presented in figure 13. The water content curve simulated with the nonhysteresis model has the same shape as the experimental curve, and their amplitudes are similar. The real water content values are underestimated since the numerical curve is below the experimental, and the relative gap increases a little more with each cycle, until reaching a maximum value of 7% in the last cycle. Using a non-hysteresis model in simulating the hygrothermal behavior of building materials is not a wise choice. Indeed, it is not advised to underestimate the water content in building walls in hygrothermal transfer simulations, because of water accumulation that could degrade the construction if not taken into consideration. In a second time, the numerical curves acquired using the hysteresis model show the effect of the sorption hysteresis phenomenon. This latter is less apparent in the experimental results because of the drying period that is higher than the humidification. The numerical profiles have the same amplitude as the experimental, but show a slight increase in time. However, the displayed relative difference is only of 2.5% corresponding to barely 0.07% kg/kg, and the simulated curves are in good agreement with the experimental. The hysteresis model uses the main adsorption and desorption isotherm curves as input

parameters, which are based on equilibrium measurements. On the other hand, the

measurements in this test are carried out in dynamic regime, which may explain the differences between the experimental and numerical results.

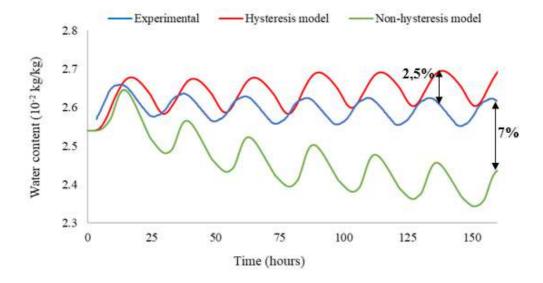


Fig.13 Experimental and numerical water content profiles in the second test

Consequently, the water content profiles obtained with the hysteresis model have a better concordance with the real water content profiles, in comparison with the profiles obtained with the non-hysteresis model. The simulated curves have the same shape as the experimental curves, as well as the same variations and amplitudes, and an admissible difference.

4.2.3. Short lasting cycles at varying temperature

The third experimentation is based on short lasting cycles at a varying temperature, corresponding to the daily variations of temperature and relative humidity. As can be seen in figure 14, the experimental curve shows a discrepancy in the first cycle, where the water content is lower than in the others. This is due to a malfunctioning of the climatic chamber, which did not secure the required temperature and relative humidity during the first cycle. Given that the real climatic conditions recorded inside the chamber are used in the numerical simulations, the simulated water content profiles display the same behavior in the first cycle.

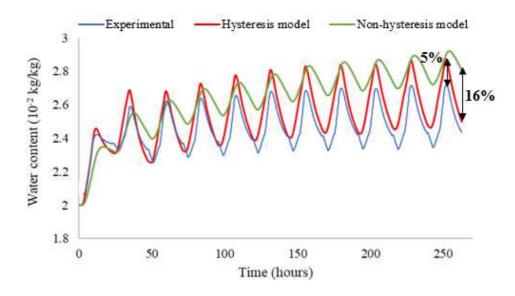


Fig.14 Experimental and numerical water content profiles in the third test

In this experimentation, the simulated water content curve using the non-hysteresis model is not located below the experimental curve, contrary to the two previous tests. In fact, the water content values are overestimated, and the high values obtained could be due to the varying temperature and its effect on moisture transfers. In addition to that, the amplitude of the simulated curve is significantly lower and corresponds to only 40% of the real one. The relative difference gradually increases as cycles progress, and attain a maximum value of 16%.

The curve obtained using the hysteresis model shows a very good concordance with the experimental one. Although the water accumulation due to hysteresis is slightly greater in simulated curves, only a small difference is observed. Indeed, the highest relative gap is about 5%, which can be considered as included in the precision range of the sensors. The hysteresis model also allows to maintain the shape and the amplitude of the experimental water content profiles, unlike the non-hysteresis model.

5. Conclusion

In this paper, we presented an experimental and numerical study of the water vapor sorption hysteresis phenomenon in expanded polystyrene mortar. First, a coupled heat and mass transfer model was presented allowing the sorption hysteresis consideration through the physical model of Carmeliet. Afterwards, the experimental setup was presented, along with the protocols and hygrothermal conditions. The experimental profiles were then compared to the simulated ones in order to assess the influence of hysteresis consideration in hygrothermal modelling of building materials.

The developed experimentations aim to highlight the sorption hysteresis phenomenon via submitting the samples to multiple cyclic conditions, varying in temperature and relative humidity. High precision sensors were inserted in the samples in order to record the water content evolution during the time of the experiment. The experimental profiles were later compared to simulated ones, obtained using the hysteresis model coupled to the hygrothermal transfer model, and also a non-hysteresis model used to evaluate the influence of considering hysteresis in numerical simulation.

The three different experimentations showed the same conclusion: Sorption hysteresis consideration allows obtaining a better adequacy between simulated and experimental results. In fact, the simulated curves using the hysteresis model had the same shape and amplitude as the experimental ones, and the difference did not exceed 7%. On the other hand, the non-hysteresis model showed numerical curves that either highly underestimated or overestimated the real water content values. Moreover, their amplitude did not match the experimental one, and the relative gaps were significantly important and reached 28%.

The water vapor sorption hysteresis phenomenon highly affects the hygrothermal transfers in building materials, as it causes water accumulation in the pores. Its consideration allows to a better apprehension of the real water content in porous materials and thus a better understanding of the hygrothermal behavior of buildings.

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CRediT authorship contribution statement

- 520 Maroua Maaroufi: Investigation, Methodology, Validation, Writing original draft, Writing
- 521 review & editing.
- Fares Bennai: Validation, Writing review & editing, Visualization.
- **Rafik Belarbi:** Conceptualization, Writing review & editing, Supervision, Validation.
- 524 Kamilia Abahri: Supervision, Validation.

525 **Declaration of Competing Interest**

- 526 The authors declare that they have no known competing financial interests or personal
- relationships that could have appeared to influence the work reported in this paper.

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