

# Experimental and numerical highlighting of water vapor sorption hysteresis in the coupled heat and moisture transfers

M. Maaroufi, F. Bennai, Rafik Belarbi, K. Abahri

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1	<b>Experimental</b>	l and numerical	l highlighting of	f water vap	or sorption
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2	hysteresis in	the coupled hea	t and moisture	transfers
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3	M. Maaroufi <sup>1,2</sup> , F. Bennai <sup>4</sup> , R. Belarbi <sup>2,3*</sup> , K. Abahri <sup>1</sup>
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4 <sup>1</sup> LMT, ENS Paris-Saclay, CNRS, Université Paris-Saclay, 61 avenue du Président Wilson, 94235

- 5 Cachan, France
- <sup>6</sup> <sup>2</sup> University of La Rochelle, CNRS, LaSIE UMR 7356, Avenue Michel Crépeau, 17042 La Rochelle
- 7 Cedex 1, France
- 8 <sup>3</sup> 4ev Lab, EDF R&D, CNRS, LaSIE, Université de La Rochelle, Avenue Michel Crépeau 17042 La
- 9 Rochelle cedex1, France
- <sup>4</sup> Université de Lorraine, CNRS, Arts et Métiers ParisTech, LEM3, F-57000, Metz, France
- 11 \*Corresponding author: Rafik Belarbi
- 12 Email address: rbelarbi@univ-lr.fr
- 13 Phone Number: +33 (0)5 46 45 72 39
- 14 Postal Address : LaSIE, La Rochelle Université, Avenue Michel CREPEAU 17042, La Rochelle
- 15 Cedex 1, France
- 16

## 17 Highlights

- 18 Experimental and numerical study of water vapor sorption hysteresis.
- Development of a coupled heat and mass transfer model with consideration of sorptionhysteresis.

Sorption hysteresis model allows a better adequacy of simulated results with experimental
ones.

- Non-hysteresis model shows various discrepancies and relative gaps between experimental
and numerical results reached 28%.

25 Abstract

Heat, air and moisture transfers have a significant influence on indoor ambience and affect both temperature and hygrometry values and energy performance of buildings. Furthermore, high levels of humidity may lead to severe pathologies in building walls in addition to tamper indoor air quality and hygrothermal comfort. Sorption hysteresis phenomenon is responsible for the moisture accumulation in porous building materials, and leaving it out in hygrothermal modelling would result in an incorrect water content value.

32 The present work aims to highlight the influence of the sorption hysteresis 33 phenomenon on heat and moisture transfer in expanded polystyrene concrete. In order to 34 achieve this, a coupled heat and mass transfer model will be elaborated, taking consideration of sorption hysteresis phenomenon. Experimental protocols will be conducted to highlight the 35 hysteresis in the materials, and the results will be compared to those of the numerical 36 37 simulations. A simple hygrothermal transfer model without including hysteresis will also be used in the numerical simulations so that it is compared to the developed model. Experimental 38 39 results show that considering the hysteresis phenomenon allows to better apprehend the hygrothermal behavior of building materials, and neglecting it leads to important differences 40 sometimes reaching 28%. 41

#### 42 Key words

43 Sorption hysteresis; Coupled heat and moisture transfers; Hygrothermal modelling;
44 Experimental characterization; Numerical simulations.

### 45 List of symbols

U: Volume water content (kg/m <sup>3</sup> )	RH: Relative humidity (%)	
ω: Mass water content (kg/kg)	P <sub>vsat</sub> : Saturation vapor pressure (Pa)	
U <sub>v</sub> : Water vapor content (kg/m <sup>3</sup> )	$\rho_s$ : Density (kg/m <sup>3</sup> )	
U <sub>l</sub> : Liquid water content (kg/m <sup>3</sup> )	K <sub>m</sub> : Moisture diffusion coefficient (kg/m.s)	
m: phase change ratio	$\delta_a$ : Water vapor permeability of air (kg/m.s.Pa)	
j <sub>v</sub> : Water vapor flux density (kg/m <sup>2</sup> .s)	μ: Water vapor diffusion resistance	
j <sub>l</sub> : Liquid water flux density (kg/m <sup>2</sup> .s)	H: Enthalpy (J/kg)	
j <sub>m</sub> : Total mass flux (kg/m <sup>2</sup> .s)	φ: Total heat flux (W/m <sup>2</sup> )	
$\delta_v$ :Water vapor permeability	ψ: Internal energy (J)	
(kg/m.s.Pa)		
$\delta_l$ :Liquid water permeability	C <sub>p</sub> : Specific heat (J/g.K)	
(kg/m.s.Pa)		
P <sub>v</sub> : Water vapor pressure (Pa)	$\lambda$ : Thermal conductivity (W/m.K)	
P <sub>c</sub> : Capillary pressure (Pa)	L <sub>v</sub> : Latent heat of vaporization (J/kg)	
$C_{pv}$ : Specific heat of water vapor (J/g.K)	R: Gaz constant (J/K.mol)	
T : Temperature (K)	M : Molar mass (kg/mol)	

46 **1. Introduction** 

Indoor air humidity is as important as indoor air temperature, since moisture can significantly influence the energy performance of households [1,2], and is one of the main causes of its deterioration [3,4]. Moisture in porous building materials can also greatly affect the indoor air quality and comfort of occupants, given that excessive low or high humidity can cause multiple respiratory pathologies and allergies [5]. To predict those effects, moisture transfer has been studied for a long time, especially in unsaturated porous media based on Darcy and Fick's laws [6,7]. To avoid moisture condensation, insulation failure or mold 54 growth in building materials, coupled heat and moisture transfers should be studied together 55 for a better prediction of the hygrothermal behavior of the building, and thus optimize its 56 design [8 – 10]. Hygrothermal transfers are often expressed using mainly phenomenological 57 models [11,12] or models that consider the materials microstructure through porosity or pore 58 size distribution [13,14].

59 Adsorption and desorption isotherms are among the most important hydric properties of porous building materials, since they describe the equilibrium water content as a function 60 of the ambient relative humidity, at a certain temperature. Cement based materials often 61 exhibit a hysteresis loop, meaning the moisture content at the same relative humidity is 62 63 different whether the material experiences wetting or drying. Therefore, the moisture content also depends on the hydric history of the material [15], and the water content follows the 64 intermediate scanning curves (fig.1, curves B and D) located between the two main adsorption 65 and desorption curves (fig.1, curves A and C) [16]. 66



67

68

**Fig.1** Sorption hysteresis curves [17]

69 Sorption hysteresis should then be taken into consideration in any hygrothermal
70 transfers research, since it illustrates the fact that it is easier for water to get in than to get out

of a porous medium [18] and is highly correlated to capillary forces [19]. In the past few decades, the interest about this phenomenon has highly increased, and researchers began developing hygrothermal models considering the effect of sorption hysteresis. However, it remains unknown and less studied in the literature, unlike other conventional phenomena such as hydration or carbonation.

76 Some researches exhibited sorption hysteresis experimentally and considered it in the 77 heat and mass transfers modelling. In his work, Zhang [20] studied cement pastes initially saturated, then subjected to hydric cycles varying from 33% to 80% and finally 53,5% of 78 79 relative humidity. He then validated his hygrothermal model using experimental saturation 80 profiles. However, he only subjected the samples to only one cycle of wetting and drying, which is not representative of buildings. Ait Oumeziane [21] also studied sorption hysteresis 81 phenomenon in a hemp concrete, a very hygroscopic material. Samples were subjected to 82 many cycles of 75% of relative humidity during 8h, then 33% during 16h, corresponding to 83 the NORDTEST protocol for the determination of Moisture Buffer Value [22]. However, 84 85 some input parameters were only taken from literature and not measured for the studied material, and thermal conductivity dependency was modeled based on its values at the dry and 86 saturated state only. The evolution of the water content in the material was compared to 87 88 numerical simulations. In line with this work, Lelièvre [23] also studied hysteresis in hemp concrete through three different experimentations. The difference lies in the duration of the 89 relative humidity levels, which varies from few hours to few days. Nevertheless, thermal 90 properties of the material were considered constant regardless of its water content, and most 91 of the input parameters were taken from previous works in literature. 92

Other researches designed sorption hysteresis modelling using a physical approach, based on the microstructure of the materials. Schiller et al. [24] recently proposed a hysteresis model in hardened cement pastes with consideration of the sorption in the interlayer space

between the C-S-H sheets, which is supposed to be responsible for low-pressure hysteresis of 96 97 water sorption isotherms. Their work is based on a macroscopic approach using a simple mathematical model coupled to volume change diagrams. Only computed hysteresis loops 98 99 were compared to those observed experimentally. Jiang et al. [25] developed a model to predict water vapor sorption hysteresis of cement-based materials based on pore size 100 distribution obtained from adsorption isotherms. No suited experimental campaign was led to 101 validate the model, which was verified using water vapor sorption isotherms from literature. 102 103 However, sorption isotherms are determined at equilibrium, while materials in buildings undergo dynamic humidity variations. 104



105

106

Fig.2 Main and average sorption curves for hemp concrete [26]

In most of the numerical studies of hygrothermal transfers, sorption hysteresis is often 107 neglected. Some works prefer to overestimate the water content and consider that it varies 108 109 according to the evolution of the main desorption curve for each variation of the daily relative humidity, whether it is a wetting or a drying [27 - 29]. Some researchers assume that the 110 111 water content rather follows the path of the main adsorption curve and do not consider sorption hysteresis [18], and others even consider a mean curve between the main sorption 112 isotherms, introducing some weighting coefficients [20]. These choices are difficult to justify, 113 114 given that water content in a porous material follows different paths whether it is subjected to

a wetting or drying. In fact, at the same relative humidity, water content has two different
values, and the relative gap between them is very high. In the case of very hygroscopic
materials such as hemp concrete [26], the difference can go from 50% to 100%, as shown in
figure 2.

119 The water content depends then on the relative humidity of the environment in 120 addition to the previous hydric states of the material. Therefore, sorption hysteresis must be 121 taken into account in the modelling of coupled heat and mass transfers in building materials, 122 because it allows determining a more precise value of water content at any given time.

In this context, we propose a hygrothermal transfer model considering the sorption 123 hysteresis phenomenon using the sorption isotherms. The heat and mass transfer model is 124 based on Luikov's equations [30], including some improvements in the hypotheses. Indeed, 125 126 input parameters were not supposed constant, and their temperature and water content dependency were considered. Sorption hysteresis phenomenon is also considered, and an 127 128 adequate experimental campaign was carried on in order to validate the computed results. 129 Moreover, in order to reduce the environmental footprint of building sector, a recycled expanded polystyrene mortar will be the material of interest. It is an eco-friendly material that 130 helps reuse the expanded polystyrene waste and has improved thermal insulation properties. It 131 132 is a highly heterogeneous material with a complex microstructure, and is composed of two materials whose hygrothermal behavior highly varies. 133

In what follows, the hygrothermal model will be presented, along with its implementation on Matlab and Comsol multiphysics. The experimental setup allowing the highlight of hysteresis will be presented, and the obtained results will be compared to the ones from the numerical calculations using the hysteresis model. A non-hysteresis model will also be used in order to enhance the influence of the sorption hysteresis phenomenon. It is

139	implemented using the main adsorption isotherm only, and it aims to show the importance of
140	sorption hysteresis consideration in hygrothermal transfers modelling.

## 141 **2. Modelling**

#### 142 **2.1. Heat and mass transfers modelling**

In this study, the implemented model is a coupled heat and mass transfers model using respectively temperature and water content as driving potentials. Afterwards, it will be coupled to a physical model that allows calculating the water content inside the pores from the ambient relative humidity with the consideration of sorption hysteresis.

147 The mass balance equations for the water vapor and liquid water phases respectively are148 written below:

149 
$$\frac{\partial U_v}{\partial t} + \operatorname{div}(j_v) = -m \tag{1}$$

150 
$$\frac{\partial U_l}{\partial t} + \operatorname{div}(j_l) = m$$
 (2)

151 By adding the two equations, we obtain the equation (3) that simplifies into equation (4).

152 
$$\frac{\partial U_{v}}{\partial t} + \frac{\partial U_{l}}{\partial t} + \operatorname{div}(j_{v}) + \operatorname{div}(j_{l}) = 0$$
(3)

153 
$$\frac{\partial U}{\partial t} + \operatorname{div}(j_v + j_l) = 0$$
 (4)

Given that the volume water content is function of the mass water content and the materialsdensity (equation (5)), the mass balance equation becomes equation (6).

156 
$$\mathbf{U} = \boldsymbol{\rho}_{s} \times \boldsymbol{\omega} \tag{5}$$

157 
$$\rho_{s} \frac{\partial \omega}{\partial t} + \operatorname{div}(j_{v} + j_{l}) = 0$$
 (6)

158 Flux densities of water vapor and liquid water can be expressed using adequate diffusion159 coefficients, which depend on the hydric state of the material as:

160 
$$j_v = -\delta_v \cdot \nabla P_v$$
 (7)

161 
$$j_l = -\delta_l \cdot \nabla P_c \tag{8}$$

162 In order to simplify the boundary conditions, water vapor content is considered the only 163 driving force of the mass transfers. Moreover, both the water vapor pressure and the capillary 164 pressure are related to relative humidity through the saturated vapor pressure and Kelvin law.

165 
$$P_v = RH \times P_{vsat}$$
(9)

166 
$$P_{c} = \frac{RT\rho_{l}}{M} \ln(RH)$$
(10)

167 Given the dependency of relative humidity on the temperature, the derivative of equation (10)168 is expressed as follows [31]:

169 
$$\nabla P_{c} = \left[\frac{RT\rho_{l}}{M}\frac{1}{RH}\nabla RH\right] + \left[\frac{RT\rho_{l}}{M}\left(\frac{\partial \ln(RH)}{\partial T}\right) + \frac{R\rho_{l}}{M}\ln(RH)\right]\nabla T$$
(11)

The thermal diffusion is negligibly small, and considered of no importance in building scienceapplications [32,33]. Therefore, the total mass flux can be expressed in the equation (12).

172 
$$j_{\rm m} = -\left[\delta_{\nu} P_{\rm vsat} + \delta_l \frac{RT\rho_l}{M} \frac{1}{RH}\right] \nabla RH$$
(12)

The moisture storage capacity  $C_m$  is defined as the slope of the sorption isotherm curves [34]. It is then a function of relative humidity and water content. It is an important property of the material as it represents the water accumulation in the pores due to sorption hysteresis.

176 
$$C_m = \frac{\partial \omega}{\partial RH}$$
(13)

177 The final expression of the mass balance equation is then explicated in equation (14).

178 
$$\rho_{s} \frac{\partial \omega}{\partial t} - \operatorname{div} \left[ \frac{K_{m}}{C_{m}} (\nabla \omega) + \frac{\delta_{l}}{C_{m}} \frac{\text{R.T}_{ref} \cdot \rho_{l}}{\text{M.RH}} (\nabla \omega) \right] = 0$$
(14)

179 We set  $K_l = \frac{\delta_l}{c_m} \frac{\text{R.T}_{ref} \cdot \rho_l}{\text{M.RH}}$  to simplify the mass balance equation.

180 
$$\rho_{\rm s} \frac{\partial \omega}{\partial t} - \operatorname{div} \left[ \frac{K_m}{c_m} (\nabla \omega) + K_l (\nabla \omega) \right] = 0 \tag{15}$$

181 The moisture diffusion coefficient that appeared in the mass balance equation is defined as182 below [23, 35, 36]:

183 
$$K_m(\omega) = \frac{\delta_a}{\mu(\omega)} P_{\text{vsat}} = \delta_v(\omega) P_{\text{vsat}}$$
(16)

The heat balance equation is expressed in the equation (17) [36]. We only consider heat transfers due to conduction, convection and phase change, and we neglect the radiation phenomenon. The final conservation of energy equation is then as:

187 
$$C_{p}\rho_{s}\frac{\partial T}{\partial t} - \operatorname{div}(\lambda \nabla T) - K_{m}C_{pv}\nabla T - m L_{v}\omega = 0 \qquad (17)$$

### 188 **2.2. Initial and boundary conditions**

189 The boundary conditions in this paper are Dirichlet type, and the temperatures and relative190 humidities are directly applied to the exterior surfaces of the sample.

191 
$$\begin{cases} \omega(x = 0, t) = \omega_1(t) \\ T(x = 0, t) = T_1 \end{cases} \text{ and } \begin{cases} \omega(x = L, t) = \omega_2(t) \\ T(x = L, t) = T_2 \end{cases}$$
(18)

Where L is the thickness of the sample. The initial conditions are considered uniform in thematerial and expressed as follows:

194 
$$\begin{cases} \omega(x, t = 0) = \omega_0 \\ T(x, t = 0) = T_0 \end{cases}$$
(19)

#### 195 **2.3. Input parameters**

196 The input parameters of the heat and mass transfers model are the hygrothermal properties of 197 the material, that were determined using an experimental campaign. The moisture storage 198 capacity Cm is obtained through the water vapor sorption isotherm curves presented later. 199 The thermal conductivity of the material depends on the temperature and the water content of 200 the material, and it was experimentally determined based on the guarded hot plate method 201 [37]. The thermal conductivity of the polystyrene mortar can be expressed as a function of 202 temperature as follows:

$$\lambda = 0,0005.\,\mathrm{T} + 0,1472 \tag{20}$$

The thermal conductivity was also measured depending on the hydric state of the material. Its dependency on the water content is expressed in equation 21.

206 
$$\lambda = 0,3663.\omega + 0,1413$$
 (21)

The water vapor permeability of polystyrene concrete depends on the materials water content, and it was experimentally determined following the cup test method based on the standards NF EN ISO 12572 [38]. This method allows determining the water vapor permeability at a low and a high relative humidity (3% and 93%). Hence, water vapor permeability will have two different values whether the ambient relative humidity is high or low.

$\rho_{s}$ (kg/m3)	537	C <sub>p</sub> (J/kg.K)	971
Tref (K)	273,15	C <sub>pv</sub> (J/kg.K)	1860
δ <sub>v</sub> (kg/m.s.Pa)	3,22.10 <sup>-12</sup> at low RH 1,2.10 <sup>-11</sup> at high RH	m (-)	0,3
L <sub>v</sub> (J/kg)	2,5.10 <sup>6</sup>		

212 **Table 1**. Input parameters

## 213 **2.4. Sorption hysteresis modelling**

The coupled heat and mass transfers model will be coupled to a sorption hysteresis model. Therefore, in addition to taking into account the moisture accumulation inside the pores through the moisture storage capacity, it will be able to calculate the real value of water content from the ambient relative humidity. The sorption hysteresis model chosen for this
work is the one developed by Carmeliet [39], which is a physical model based on the theory
of the independent domains and the ink-bottle pore effect, elaborated by Mualem [40,41]. In
previous works, this model was proven to be the most representative to the hysteretic behavior
of cement based materials [21,23].

The use of empirical hysteresis models often leads to a hysteretic behavior called "pumping effect". It reflects the fact that the numerical scanning curves do not respect the closing principle. In other words, this means that during a succession of adsorption and desorption cycles, there is a unique water content value for each extremum of relative humidity. Therefore, a material undergoing several cycles of wetting /drying should normally return to its initial relative humidity and water content.

Some researches [20,42,43] consider that the pumping effect is not a physical characteristic specific to the material, but that it is entirely artificial. It is then considered as errors generated by the calculation algorithms. Mualem model – and therefore Carmeliet model – respects the closing principle and makes it possible to avoid pumping errors, confirming its accuracy in hysteresis modelling [29,23].

The sorption hysteresis model developed by Carmeliet allows calculating modelled hysteresis loops from the main adsorption and desorption isotherm curves. It is based on the theory of independent domains, considering the ink-bottle shaped pores. It expresses the water content in the scanning curves in different expressions, whether it is a wetting or a drying, in terms of water content in the main sorption isotherms, and some specific values such as saturation point.

239 The equation describing the water content in adsorption scanning curves is recalled below.

240 
$$\omega_{ads,hyst}(RH,i) = \omega_{i-1} + (1 - A(RH_{i-1}))(\omega_{ads}(RH) - \omega_{ads}(RH_{i-1})).$$
 (22)

The "i" indicates the inversion point which is the exact time of going from an adsorption to a desorption (and vice versa). In equation (22), the "i" here marks the inversion between the i-1<sup>th</sup> desorption scanning curve and the i<sup>th</sup> adsorption scanning curve.

The equation describing the water content in desorption scanning curves is expressed in (23). In this case, the "i" marks the inversion between the i-1<sup>th</sup> adsorption scanning curve and the i<sup>th</sup> desorption scanning curve, as explicated in figure 3.

247 
$$\omega_{\text{des,hyst}}(\text{RH, i}) = \omega_{i-1} - (1 - A(\text{RH}))(\omega_{\text{ads}}(\text{RH}_{i-1}) - \omega_{\text{ads}}(\text{RH})), \quad (23)$$



248 Where  $A(RH) = \frac{\omega_{des}(RH) - \omega_{ads}(RH)}{\omega_{sat} - \omega_{ads}(RH)}$  (24)

249



# Fig.3 Schematic representation of the i<sup>th</sup> inversion point

The water content associated to each varying value of relative humidity is calculated whether it is a wetting or a drying. For that, we need to know and memorize the inversion points. It is then necessary to indicate a transition criterion between the different phases of wetting/drying, along with a list of the inversion points [21]. Equation (25) expresses the condition of the transition from the adsorption curve to the desorption curve, and vice versa. When the inversion criterion is less than zero, there is a transition from a sorption phase to the other, and the new inversion point is added to the list.

$$L_{inv} = (RH(n) - RH(n-1)) \times (RH(n-1) - RH_{i-1})$$
(25)

RH(n) represents the relative humidity of the material at the time n, RH(n-1) at the time n-1, and RH<sub>i-1</sub> corresponds to the relative humidity of the last identified inversion point. The iterations in the program stand for the time. There is an inversion if the inversion criterion is less than zero. In this case, this new point is saved and becomes the last identified inversion point. The values of relative humidity and water content are therefore calculated at each time, and the water capacity is calculated differently whether it is an adsorption or a desorption.

As shown in figure 4, MATLAB software was used to compute the hysteresis model, 265 coupled to COMSOL Multiphysics where the hygrothermal model was implemented. The 266 experimental values of ambient relative humidity and the main adsorption and desorption 267 curves are first introduced in MATLAB where the hysteresis model allows the calculation of 268 269 the corresponding values of water content, in addition to the moisture storage capacity. These values are then imported into COMSOL along with the input parameters consisting in the 270 hygrothermal properties of the material of interest. The resolution in Comsol is based on the 271 272 finite elements method following three basic steps, namely pre-processing, solver, and postprocessing. It generates a set of equations for all the involved physical models and 273 implements them in a single iteration scheme, which is repeated until convergence is reached. 274 Comsol has several solvers all based on finite elements method, then chooses the most 275 suitable one to ensure stability and convergence of the solutions. The time dependent solver is 276 277 computing the solution to a possibly nonlinear system of equations at each time step via a set of iterative techniques based upon Newton's method. These Newton's method techniques for 278 solving a nonlinear system of equations evaluate a function, as well as its derivative, at every 279

time step. This derivative is also known as the Jacobian and is relatively expensive to compute. Therefore, the software will try to minimize reevaluating the Jacobian, by default. If the nonlinear solver has difficulty converging, it will reduce the requested time step size and try to compute the solution.



284

285

Fig.4 Hysteresis modelling steps

## 286

#### 3. Materials and methods

In this study, the coupled heat and moisture transfers model developed is based on 287 phenomenological modelling, where the relevance of the prediction is conditioned by a 288 reliable evaluation of the input data. The hygrothermal properties that constitute the input 289 290 parameters of the implemented model were experimentally determined using standard laboratory methods. A part of this section was dedicated to a fine, experimental 291 characterization of the intrinsic hydric and thermal properties of the material. The material of 292 293 interest in this work is a polystyrene mortar made of recycled expanded polystyrene granules and a CEMII cement as a binder [44,45]. 294

295 Computing the coupled heat and mass transfers involves the experimental 296 determination of the hygrothermal properties of the material. The experimental campaign 297 aimed to measure the water vapor permeability using the wet cup/dry cup method based on 298 the EN ISO 12572 norm [46], the thermal conductivity using the Guarded Hot Plate method 299 based on the NF EN 12667 norm [47], and the heat capacity using a 3D sensors calorimeter.

In addition, the implementation of the hysteresis model requires the determination and modelling of the main adsorption and desorption curves of the material. The experimental isotherm curves were determined using the gravimetric technique that is based on continuous successive weightings. The test was performed on a very recent vapor sorption analyzer that allows measuring the mass evolution of the samples. For the polystyrene mortar, the main isotherms are modelled using the equation below [39], which proves a good adequacy between the experimental and the modelled curves, as shown in figure 5.

307 
$$\omega(\text{RH}) = \omega_{\text{sat}} \left(1 - \frac{\ln(\text{RH})}{A}\right)^{-1/n}$$
(26)

A and n are empirical calibration coefficients. These parameters were adjusted using the experimental data presented in figure 5. The fitting parameters are presented in table 2, and are different whether it is adsorption or desorption. The root mean squared error between the experimental data and the adjustment curves is 0,2%.







**Fig.5** Main adsorption and desorption isotherm curves of polystyrene mortar

This model precisely reproduces the sorption isotherms of the polystyrene mortar in adsorption phase, and is less accurate in desorption phase. This is due to the sudden decrease of water content in the main desorption curve between 30% and 40% of relative humidity, that is very difficult to model.

	Α	n	R <sup>2</sup>
Adsorption	0,033	1,796	0,996
Desorption	0,399	1,35	0,965

**Table 2.** Fitting coefficients for the main sorption isotherms

During the daily variations of relative humidity and temperature, the water content 319 320 inside building materials varies according to the intermediate sorption isotherms. In order to characterize experimentally the intermediate curves of the expanded polystyrene mortar, the 321 total water content is measured at the equilibrium when subjecting the material to different 322 relative humidity levels. The experimental method used here was the gravimetric technique 323 that is based on continuous successive weightings. The test was performed on three cubic 324 samples of 10x10x10 mm<sup>3</sup> dimensions previously dried at 60°C. The temperature was fixed at 325 23°C and the relative humidity variations are presented in figure 6. 326



327

328

Fig.6 Relative humidity variation during the determination of the intermediate isotherms

A second experimental campaign dedicated to the validation of the model was 329 performed. The objective is to assess the relevance of the coupled heat and moisture transfers 330 model by confronting it to experimental results on the one hand, and on the other hand to 331 highlight the influence of considering the hysteresis of water content in the developed model. 332 The experimentation consists of imposing a unidirectional transfer through cylindrical 333 samples by applying a thermal and hydric insulation on all the surfaces but one, as 334 335 schematized in figure 6. Hygrothermal sensors are introduced inside the samples in order to 336 record the temperature and relative humidity evolution. The sensors were positioned 1,5cm away from the surface of the sample, as shown in figure 7. The samples were then be 337 subjected to cyclic solicitations in temperature and relative humidity applied on the exposed 338 surface. Samples are initially conditioned at 50% of RH and 25°C. 339





Fig.7 Samples dimensions (left) and sensors disposition (right)

The experimental setup is presented in figure 8, and is composed of a climatic 342 chamber in charge of the ambient conditions and a high accuracy ambiance sensor ensuring 343 compliance with the ambient conditions imposed on the sample in terms of temperature and 344 relative humidity. High precision sensors are also put inside the samples in order to obtain the 345 temperature and water content profiles at different positions in the material. Each sample is 346 put on a scale so that it can measure the total water content during the experimentation. The 347 climatic chamber is of type Memmert HCP240 and the ambience sensor is a psychrometer of 348 high precision ( $\pm 1\%$  in the whole relative humidity range). The hygrothermal sensors used 349 inside the samples are capacitive humidity sensors FHA 646 R, characterized by ± 2% of 350 precision in relative humidity range and  $\pm 0.2$ K for a temperature from 0 to 70°C. 351



352

353

#### Fig.8 Experimental setup diagram

For us, to study the materials response to long and short cyclic solicitations, three different hygrothermal conditions were tested. The first protocol is set in a way to consider the reaction of the material to hydric solicitations with low drying kinetics, at a constant temperature. The two other protocols aim to simulate the daily variations of climatic 358 conditions, but one is at a constant temperature, and in the other one it varies along with the

relative humidity. The detailed solicitations and their durations are presented in table 3.



360 **Table 3.** Experimental hydric and thermal conditions

## 361 **4. Results and discussion**

In the following, the experimental and numerical results are presented. First, the intermediate adsorption and desorption curves of the polystyrene mortar are presented, in addition to the experimental and modelled moisture storage capacity curve. Afterwards, the experimental water content profiles inside the samples, along with the simulated water content profiles are presented simultaneously in order to compare both. The three different 367 experimental protocols presented in table 3 are treated separately, in order to compare368 between the experimental and simulated profiles in each case.

369

#### 4.1. Main and intermediate sorption curves

The experimental adsorption and desorption curves of the polystyrene mortar are 370 presented in the figure 9. Given that the sample was initially at a dry state, the first curves are 371 the main adsorption and desorption isotherms, while all the others represent the intermediate 372 373 curves. The scanning curves are all located between the main curves, which represent an envelope curve. They have the same look and vary in the same way, they even present the 374 abrupt decrease in desorption around 30% of relative humidity. After four cycles of the 375 wetting and drying cycles presented in figure 6, the intermediate curves overlap, thus the 4th 376 adsorption curve and the 3rd desorption curve are imbricating. These results come from the 377 378 water accumulation in the materials porosity and the sorption hysteresis phenomenon, since the relative humidity conditions are narrowed down after each cycle. 379



380



**Fig.9** Main and intermediate sorption isotherm curves of the polystyrene mortar

The intermediate curves represent the variations of water content of the material under cyclic varying relative humidity. The hysteresis model developed by Carmeliet [39] should be able to model the water content so that it can follow the same path. In the figure 10, the

experimental and modelled intermediate curves are compared, and show a better adequacy in 385 386 adsorption phases. On the other hand, in the desorption phases, the modelled curves underestimate the experimental curves and almost overlap. This is due to the sudden decrease 387 of water content in the main desorption curve between 30% and 40% of relative humidity. 388 Indeed, the sudden variation is very difficult model, and the modelled main desorption curve 389 tend to underestimate the experimental one. Therefore, all the following intermediate curves 390 are underestimating the water content values. Moreover, Carmeliet model ensures the closing 391 principle that helps avoiding pumping errors and each scanning adsorption and desorption 392 curve meet at the same value of water content. 393



394

Fig.10 Experimental and modelled main and intermediate sorption curves of the polystyrene
 mortar

The hysteresis model is also used to model the moisture storage capacity of the material in order to evaluate its accuracy. Moisture storage capacity is defined as the derivative of the water content in relation to the relative humidity; it can then be obtained from the sorption curves. In order to verify the accuracy of the hysteresis model, modelled moisture storage capacity of polystyrene mortar is compared to the experimental in figure 11. During the adsorption phase, the modelled moisture capacity shows very good concordance with the experimental curve, since the highest difference is only 8%. In desorption, the model
give less adequate results and display bigger differences up to 30%. However, the variations
of the modelled curves look like the experimental ones, and the model allows preserving the
shape of the experimental curve.



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## 9 **4.2.** Water content evolution through time

In the following, the experimental water content profiles inside the samples are presented. They are compared to the numerical profiles obtained through simulations using the hysteresis model presented in the previous parts. A non-hysteresis model will also be used in order to assess the importance of the phenomenon consideration in the hygrothermal transfers modelling in building materials. The results of each experimentation is presented apart from the others below.

## 416 **4.2.1.** Long lasting cycles at constant temperature

417 Numerical and experimental results of the water content profiles in the samples submitted to 418 long lasting cycles at constant temperature are presented in figure 12. Using the non-419 hysteresis model, the evolution of water content represents a curve below the experimental results and underestimates the actual values. In the adsorption phase, the difference between the experimental and simulated curves is relatively low, and the highest relative gap observed is 5%. On the contrary, during desorption, the non-hysteresis model underestimates the real water content values. The difference in this case is highly significant and the simulated values show relative gaps reaching 28%.

The profiles obtained with the hysteresis model show a good adequacy with the experimental results, except the first adsorption cycle where the difference is relatively high. Indeed the numerical values of water content are lower than the experimental ones, and a 7% relative difference is recorded at the peak of the first cycle. Concerning the remaining cycles, the numerical curves are in good concordance with the experiments and the relative differences do not exceed 2%.



431

432

**Fig.12** Experimental and numerical water content profiles in the first test

The discrepancy in the first cycle could result from a delay of the model, due to the initial conditions. In fact, the material is initially conditioned at 60% of relative humidity, which corresponds to a water content of 2.8% kg/kg before going through the first adsorption. In the model, the initial water content put in the input parameters corresponds to that. Afterwards, at the end of each desorption cycle, the sample has a water content of about 3.5% kg/kg. Therefore, during humidification where the relative humidity is at 85%, it is easier for the material to reach the maximum water content (4.7% kg/kg) when it is at 3.5% kg/kg than when it is at its initial value. In reality, polystyrene mortar is not very hygroscopic, and so it quickly reaches the maximum water content even when it is at the initial water content.

442

## 4.2.2. Short lasting cycles at constant temperature

The second experiment consists of short lasting cycles at constant temperature, and the water content profiles are presented in figure 13. The water content curve simulated with the nonhysteresis model has the same shape as the experimental curve, and their amplitudes are similar. The real water content values are underestimated since the numerical curve is below the experimental, and the relative gap increases a little more with each cycle, until reaching a maximum value of 7% in the last cycle.

449 Using a non-hysteresis model in simulating the hygrothermal behavior of building materials is 450 not a wise choice. Indeed, it is not advised to underestimate the water content in building 451 walls in hygrothermal transfer simulations, because of water accumulation that could degrade 452 the construction if not taken into consideration.

In a second time, the numerical curves acquired using the hysteresis model show the effect of the sorption hysteresis phenomenon. This latter is less apparent in the experimental results because of the drying period that is higher than the humidification. The numerical profiles have the same amplitude as the experimental, but show a slight increase in time. However, the displayed relative difference is only of 2.5% corresponding to barely 0.07% kg/kg, and the simulated curves are in good agreement with the experimental.

The hysteresis model uses the main adsorption and desorption isotherm curves as input parameters, which are based on equilibrium measurements. On the other hand, the 461 measurements in this test are carried out in dynamic regime, which may explain the462 differences between the experimental and numerical results.



463

464

**Fig.13** Experimental and numerical water content profiles in the second test

465 Consequently, the water content profiles obtained with the hysteresis model have a better 466 concordance with the real water content profiles, in comparison with the profiles obtained 467 with the non-hysteresis model. The simulated curves have the same shape as the experimental 468 curves, as well as the same variations and amplitudes, and an admissible difference.

## 469 **4.2.3.** Short lasting cycles at varying temperature

The third experimentation is based on short lasting cycles at a varying temperature, corresponding to the daily variations of temperature and relative humidity. As can be seen in figure 14, the experimental curve shows a discrepancy in the first cycle, where the water content is lower than in the others. This is due to a malfunctioning of the climatic chamber, which did not secure the required temperature and relative humidity during the first cycle. Given that the real climatic conditions recorded inside the chamber are used in the numerical simulations, the simulated water content profiles display the same behavior in the first cycle.





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Fig.14 Experimental and numerical water content profiles in the third test

In this experimentation, the simulated water content curve using the non-hysteresis model is not located below the experimental curve, contrary to the two previous tests. In fact, the water content values are overestimated, and the high values obtained could be due to the varying temperature and its effect on moisture transfers. In addition to that, the amplitude of the simulated curve is significantly lower and corresponds to only 40% of the real one. The relative difference gradually increases as cycles progress, and attain a maximum value of 16%.

The curve obtained using the hysteresis model shows a very good concordance with the experimental one. Although the water accumulation due to hysteresis is slightly greater in simulated curves, only a small difference is observed. Indeed, the highest relative gap is about 5%, which can be considered as included in the precision range of the sensors. The hysteresis model also allows to maintain the shape and the amplitude of the experimental water content profiles, unlike the non-hysteresis model.

### 492 **5.** Conclusion

In this paper, we presented an experimental and numerical study of the water vapor sorption hysteresis phenomenon in expanded polystyrene mortar. First, a coupled heat and mass transfer model was presented allowing the sorption hysteresis consideration through the physical model of Carmeliet. Afterwards, the experimental setup was presented, along with the protocols and hygrothermal conditions. The experimental profiles were then compared to the simulated ones in order to assess the influence of hysteresis consideration in hygrothermal modelling of building materials.

The developed experimentations aim to highlight the sorption hysteresis phenomenon via submitting the samples to multiple cyclic conditions, varying in temperature and relative humidity. High precision sensors were inserted in the samples in order to record the water content evolution during the time of the experiment. The experimental profiles were later compared to simulated ones, obtained using the hysteresis model coupled to the hygrothermal transfer model, and also a non-hysteresis model used to evaluate the influence of considering hysteresis in numerical simulation.

The three different experimentations showed the same conclusion: Sorption hysteresis consideration allows obtaining a better adequacy between simulated and experimental results. In fact, the simulated curves using the hysteresis model had the same shape and amplitude as the experimental ones, and the difference did not exceed 7%. On the other hand, the nonhysteresis model showed numerical curves that either highly underestimated or overestimated the real water content values. Moreover, their amplitude did not match the experimental one, and the relative gaps were significantly important and reached 28%.

The water vapor sorption hysteresis phenomenon highly affects the hygrothermal transfers in building materials, as it causes water accumulation in the pores. Its consideration allows to a better apprehension of the real water content in porous materials and thus a better understanding of the hygrothermal behavior of buildings.

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519	CRediT authorship contribution statement
520	Maroua Maaroufi: Investigation, Methodology, Validation, Writing - original draft, Writing
521	- review & editing.
522	Fares Bennai: Validation, Writing - review & editing, Visualization.
523	Rafik Belarbi: Conceptualization, Writing - review & editing, Supervision, Validation.
524	Kamilia Abahri: Supervision, Validation.
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