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Karunesh Kant, Pascal Henry Biwole, A. Shukla, Atul Sharma, Shiva Gorjian. Heat transfer and energy storage performances of phase change materials encapsulated in honeycomb cells. *Journal of Energy Storage*, 2021, 38, pp.102507. 10.1016/j.est.2021.102507 . hal-03180672

HAL Id: hal-03180672

<https://hal.science/hal-03180672>

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1 **Heat Transfer and Energy Storage Performances of Phase Change**
2 **Materials Encapsulated in Honeycomb Cells**

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14

Abstract

15 Thermal energy storage devices are vital for reducing the inconsistency between energy
16 supply and demand as well as for enhancing the performance of solar thermal systems. The
17 present study investigates the melting process in metallic honeycombed heat exchangers
18 filled with n-octadecane as phase change material (PCM). Further, a parametric study is
19 conducted for four different honeycomb cell sizes, fin thicknesses, and angles of inclinations
20 of the computational domain. The findings are described in the form of heated surface
21 average temperature variation, melt fraction of the PCM, and thermal energy stored. Results
22 show that the honeycomb fin structure considerably improves the heat transfer in the PCM.
23 Further, it was observed that the honeycomb cell size and fin thickness greatly influence the
24 variation of the average front surface temperature, melt fraction, and energy storage rate,
25 whereas the inclination angle doesn't have a significant effect when cell size is less than 0.01
26 m. From the study, it was also observed that when the computational domain is horizontal
27 without honeycomb cells, the pure conduction in the PCM results in much higher front
28 surface temperature, which is greatly reduced in presence of the honeycomb cells.

29 Keywords: Phase change materials; Thermal energy storage; Numerical simulation; Heat
30 transfer; Melt fraction

31	Nomenclature	
32	C_p	specific heat [J/(kgK)]
33	h_{∞}	heat transfer coefficient on the front and back surface [W/(m ² K)]
34	H	height of computational domain [m]
35	k	thermal conductivity [W/(mK)]
36	L_c	cell length [m]
37	L_f	latent heat of PCM [J/kg]
38	P	pressure [Pa]
39	Pe	peclet number [1]
40	q_0	incident heat flux on the front surface [W/m ²]
41	t	time [s]
42	T	temperature [K]
43	T_{∞}	ambient temperature [K]
44	T_{ini}	initial temperature [K]
45	u	velocity field of melted PCM[m/s]
46	W	width of the computational domain [m]
47	δ_{fin}	fin thickness [m]
48	θ	tilt angle from horizontal [°]
49	ρ	density [kg/m ³]
50	ρ_l	density of liquid PCM [kg/m ³]
51	ρ_s	density of solid PCM [kg/m ³]
52	β	thermal expansion coefficient of PCM [1/K]
53	μ	viscosity of melted PCM [Pa.s]
54	Subscript	
55	s	solid
56	l	liquid

57 1. INTRODUCTION

58 Solar energy is an abundantly available, clean, and sustainable energy source therefore it is
59 accepted as one of the most favorable alternative energy sources for sustainable development
60 [1–5]. Due to the intermittency by its nature, unreliability is the major impeding factor for the
61 massive use of solar energy in agriculture and food processing. The unreliability of solar
62 energy utilization can be diminished by stowing solar energy when it is excess compared to
63 the demand and consuming the stowed energy whenever required. The energy storage system
64 is, consequently, important to any system that is based largely on solar energy. Solar energy
65 can be stored in the form of thermal energy in thermal energy storage (TES) devices. During
66 the past few decades, the latent heat TES devices using PCM have gained larger attention due
67 to their favorable thermophysical properties. However, these materials show poor thermal
68 conductivity, which restricts the thermal transport in the storage medium and alleviates the
69 melting/solidification process. To evade this shortcoming and enhance thermal transport
70 throughout the solid-liquid phase transition, multitudinous approaches have been
71 recommended in past studies. These approaches are the addition of highly thermal conductive
72 nanoparticles [6–8], incorporation of metal matrix [9], addition porous matrices [10], and use
73 of multiple PCMs [11,12]. Amid these approaches, the incorporation of the metal matrix in
74 PCM is the focus of the present study because it is cheap and easy to integrate with the
75 system.

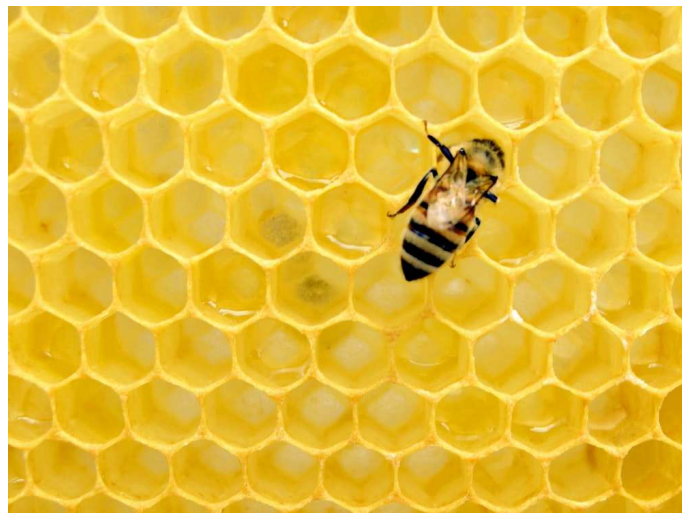
76 In recent years, several studies have been executed to assess the heat transfer behavior of
77 metal matrices integrated PCMs. In this regard, Biwole et al. [13] conducted a numerical
78 simulation of RT-25 PCM filled in a rectangular enclosure to assess the effect of fin size and
79 distribution. The effective fin configuration was investigated and it was perceived that the fin
80 surface area is an important factor that guides the melting of PCM and the rate of heat
81 transfer between the PCM and the front hot surface, while the fin structures advance greater
82 natural convection, leading to an advanced heat flux. Groulx et al. [14] conducted a
83 numerical simulation to assess the influence of fin placement and angle of inclination on the
84 melting of RT25 PCM in a rectangular enclosure. Based on the study it was concluded that
85 the convection heat transfer causes a significant acceleration in the melting process of the
86 PCM. Also, a negligible effect for the computational domain's inclination angle smaller than
87 75° from vertical on the heat transfer behavior of all considered configurations was reported.
88 Darzi et al. [15] studied the melting and solidification behavior of PCM considering radial

89 fins and thermally conductive nanoparticles to enhanced thermal transport. The phase change
90 process was accelerated by increasing the nanoparticle concentration and the elliptical tube
91 decreases the melting time as compared to the circular tube. Further, increment the fin
92 number show system deficient due to the suppression of natural convection. A numerical
93 study of PCM solidification was conducted by Abidi et al [16] to investigate the best
94 configuration that minimizes the melting and solidification time of PCM in a triplex tube heat
95 exchanger with both external and internal fins. In continuation with the thermal transport
96 enhancement using fin structure, a novel snowflake crystal fin structure was investigated by
97 Sheikholeslami et al. [17] to enhance the thermal efficiency of the latent heat thermal energy
98 storage (LHTES) device during the heat discharging process. The obtained results were
99 indicated that the discharging process of the LHTES is improved by applying Snowflake
100 shaped fin structure, in comparison with the nanoparticle diffusion, while it does not
101 considerably reduce the maximum thermal energy storage capacity. Wu et al. [18] performed
102 numerical analysis and improved the thermal transport behavior of the LHTES device with
103 spiderweb-like fins. From the obtained results it is observed that the spiderweb-like fins
104 decrease melting and solidification time by reducing the heat transfer hysteresis region.

105 In the recent past, several investigators have made substantial efforts to improve the thermal
106 performance of LHTES devices by using different thermally conductive fin structures. The
107 researchers had paid their most attention toward modified rectangular and annular fin
108 structures. Conversely, several studies have shown that proposed conventional fins have a
109 simple structure with a small specific surface area which makes it tough to realize reasonable
110 thermal transport performance of LHTES devices. Consequently, some fins with mixed
111 structures and a high specific surface have been found to enhance the thermal transport
112 effectiveness of LHTES devices. Recently, bionics are advanced in the field of fluid flow and
113 heat transfer applications including chemical reactor [19], biomedical equipment [20,21], and
114 electronic cooling [22–26]. The fin structures made by natural assortment encourages the
115 improvement of the LHTES device. By realizing natural structures, the fins with bionic
116 structures for instance tree-shaped fins [26,27], Koch fractal fins [28], and snowflake-shaped
117 fins [17,29] have been recently proposed by researchers to the enhanced thermal performance
118 of PCM thermal energy storage devices.

119 The bionic fins provide an effective means for thermal transport, therefore increasing the
120 thermal transport effectiveness of LHTES devices. Though the hysteresis exists during

121 melting and solidification of PCM with various ranges depends on the gaps between fins. The
122 presence of hysteresis impedes the additional enhancement of the thermal efficiency of such
123 devices. The extensive existence of honeycomb meshed structure in nature offers an idea to
124 solve the hysteresis problem. As shown in *Figure 1*, the honeycomb has a compact and
125 uniformly distributed structure over the entire structure. Based on this quality, the use of
126 honeycomb-like fin introduces a high interest for improved efficiency of charging and
127 discharging processes of LHTES devices.



128

129 *Figure 1 Honey bee honeycomb*

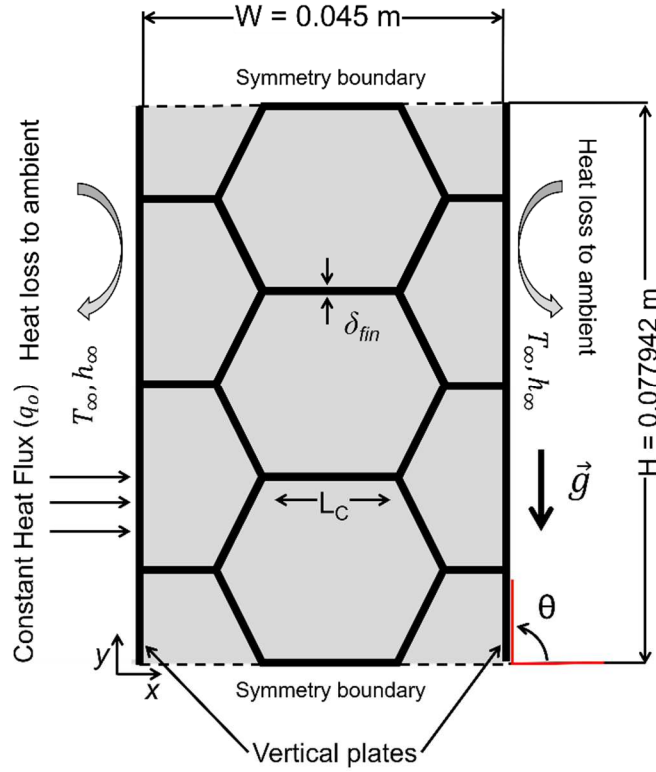
130 Through a comprehensive literature assessment, it can be chronicled that not much
131 investigation has been dedicated to investigating the charging efficiency of LHTES devices
132 with honeycomb meshed fins. The melting behavior of PCM and interstitial thermal energy
133 absorption process between honeycomb meshed fin structures and PCM is still imprecise.
134 Further, the effect of the honeycomb meshed fin structure on the charging efficiency of
135 LHTES devices has not been exposed so far. The effect of natural convection on the melting
136 progression has been highlighted by numerous researchers; however, no known study has
137 been found in the literature on the melting and energy storage behavior of PCM in the
138 honeycomb structure and limited works have focused on the effect of the container's tilt
139 angle on the melting behavior of the PCM process. Consequently, the current analysis
140 provides an advanced insight into how the thorough nature of honeycomb meshed fins
141 influence the heat absorption behavior of LHTES devices while can be considered as an
142 important work to enhance the thermal storage and discharge effectiveness.

143 The article is structured as follows: In the introduction section, the overall background and
144 the goal of the current study are presented. After the introduction, the computational model
145 with all the simulation details including the dimensions and constants used in the study are
146 described. Next to the computational model, the mathematical formulation, boundary
147 conditions, and computational technique with model validation are presented. Further,
148 detailed discussions on the results of the present study are presented, trailed by a summary of
149 the key conclusions.

150 2. COMPUTATIONAL MODEL

151 The geometry of the computational domain considered in the present work has been
152 presented in Figure 2. The computational domain is poised of two vertical metallic plates
153 connected with hexagonal honeycomb cells; the fin thickness of each hexagonal cell, as well
154 as the vertical plate, is δ_{fin} . The height (H) and width (W) of the container are fixed, with
155 values 0.077942 m and 0.045 m respectively and the inclination angle of the computational
156 domain from horizontal is θ ° as shown in Figure 2. Each cell in the container has the same
157 length (L_C) and uniform thickness. Internal fins are also made of the same material as front
158 and back vertical plates. The cell length L_C , the inclination angle of the container from
159 horizontal θ and the fin thickness are given in Table 2. The thermo-physical properties of
160 metallic fins and PCM considered in the present study are shown in Table 1. The
161 computational domain is primarily set at a temperature $T_{ini} = 23.2$ °C and the front metallic
162 plate is subjected to a continuous heat flux of $q_0 = 1000 W/m^2$ perpendicular to the front
163 surface for the period of the numerical simulation. As the present study is only focused on the
164 influence of honeycomb structure on the heat transfer behavior in PCM, the convective heat
165 transfer coefficient on the front and back surface is fixed. The front and back surface of the
166 container is opened to convection cooling with an ambient temperature of $T_\infty = 23.2$ °C as
167 well as the convection heat transfer coefficient $h_\infty = 2 W/m^2K$. The top and bottom of the
168 computational domain are subjected to symmetry boundaries (adiabatic). The acceleration
169 due to gravity is always working in the downward direction for the entire tilt angle range. To
170 conduct numerical simulation the following assumptions has been considered in the present
171 study: (i) the liquated PCM is incompressible and Newtonian, (ii) the melted PCM's flow is
172 laminar, radiation and three-dimensional convection are neglected, (iii) volume expansion
173 due to the melting of PCM is neglected.

174 In the present study, n-octadecane is considered as PCM and its thermo-physical properties
175 are given in Table 1. Four different angles of inclination and fin thicknesses are studied for
176 four different honeycomb cell sizes. The study has also been conducted without honeycomb
177 cells in the rectangular plane of the container considered. The studied combinations of the fin
178 thickness and inclinational angles are given in Table 2, where L_C is the honeycomb cell
179 length, δ_{fin} is the fin thickness of the honeycomb cells and θ is the angle of inclination of the
180 computational domain from horizontal as shown in Figure 2. The numerical simulation was
181 conducted at 4 different angles of inclination θ without honeycomb cells as well as at 4
182 different L_C (i.e. $L_C = 0.005$ m, $L_C = 0.0075$ m, $L_C = 0.010$ m and $L_C = 0.015$ m) considering
183 $\delta_{fin} = 0.0005$ m to investigate the effect of inclination angle as well as honeycomb cell length
184 on front surface temperature, melt fraction, and energy storage content. Further, to investigate
185 the effect of the honeycomb fin thickness, the studies are conducted at 4 different honeycomb
186 fin thickness δ_{fin} with 4 honeycomb cell length L_C while the angle of inclination of the
187 computational domain is fixed at 60° . Through the change in honeycomb cell size, fin
188 thickness, tilt angle from horizontal, initial, and boundary conditions to the mathematical
189 model are described in the next section and thermal energy storage behavior of computational
190 domain is described arrangements are described.



191

192 *Figure 2 Geometry and boundary conditions of the system considered for the numerical*
 193 *simulation*

194 *Table 1 Thermophysical properties of PCM and metallic fin*

Properties /Material	PCM	Metallic fin
Melting temperature ($^{\circ}C$)	28.2	NA
Specific heat ($J/kg.K$)	1934 (s), 2196 (l)	900
Latent heat of fusion (kJ/kg)	245	NA
Density (kg/m^3)	814 (s), 775 (l)	2700
Thermal conductivity ($W/m.K$)	0.350 (s), 0.149 (l)	238
Thermal expansion coefficient ($1/^{\circ}C$)	9.1×10^{-4}	NA
Kinematic viscosity (m^2/s)	5×10^{-6}	NA

195

196 *Table 2 Parameters considered in the present study*

	θ $^{\circ}$ (at $\delta_{fin} = 0.0005$ m)				δ_{fin} [m] (at $\theta = 60$ $^{\circ}$)			
Without cells	0	30	60	90	NA	NA	NA	NA
$L_C = 0.005$ m	0	30	60	90	0.00025	0.0005	0.001	0.0015
$L_C = 0.0075$ m	0	30	60	90	0.00025	0.0005	0.001	0.0015

$L_c = 0.010 \text{ m}$	0	30	60	90	0.00025	0.0005	0.001	0.0015
$L_c = 0.015 \text{ m}$	0	30	60	90	0.00025	0.0005	0.001	0.0015

197 3. MATHEMATICAL FORMULATIONS

198 3.1. Numerical simulation model description

199 The following equations (1) and (2) with the boundary conditions are applied on the heated
200 front and back external surface correspondingly:

$$201 \quad -k \left. \frac{\partial T}{\partial x} \right|_{x=0} = q_0 + h_{\infty}(T_{\infty} - T) \quad (1)$$

$$202 \quad -k \left. \frac{\partial T}{\partial x} \right|_{x=\delta_{fin}+W+\delta_{fin}} = h_{\infty}(T - T_{\infty}) \quad (2)$$

203 Further, the equation of heat transfer diffusion realized within the fins and PCM domain is:

$$204 \quad \rho C_p \frac{\partial T}{\partial t} + \nabla(-k\nabla T) + \rho C_p \vec{u} \cdot \nabla T = 0 \quad (3)$$

205 where ρ , C_p and k represents density, specific heat, and thermal conductivity respectively. For
206 the PCM, the value of ρ , k and C_p varies with temperature as given by eq. (7), (8) and (9)
207 respectively. The fluid velocity \vec{u} is always zero in the metallic fins as well as on the surface
208 of metallic fins, and is given in the PCM domain by numerically solving the Navier-Stokes
209 and continuity equation; the equation of modified momentum conservation for the PCM
210 domain can be given [14]:

$$211 \quad \rho \frac{\partial \vec{u}}{\partial t} + \rho(\vec{u} \cdot \nabla)\vec{u} = -\nabla P + \rho_l(1 - \beta(T - T_m))\vec{g} + \mu_l \cdot \nabla^2 \vec{u} - \frac{C(1-B(T))^2}{B^3(T)+\varepsilon} \vec{u} \quad (4)$$

212 where ρ_l and μ_l are respectively the density and dynamic viscosity is of melted PCM, β is the
213 thermal expansion coefficient of PCM and \vec{g} is the acceleration because of gravity constant.
214 The value of constant C (Kozeny-Carman permeability) can be determined by the inherent
215 characteristics of the PCM material. Increasing its value causes a decrease in the melted
216 PCM's flow in the transition zone, and consequently to a smoother nature of the liquidus
217 melting front while decreasing its value will have the contrary influence. The value of
218 constant C in the present study is $10^5 \text{ kg/ (m}^3 \cdot \text{s)}$. Here, ε is constant with a given value of

219 10^{-3} as in [30] to evade dividing by zero. The melted fraction function $B(T)$ of PCM is
 220 defined as:

$$221 \quad B(T) = \begin{cases} 0, & T < \left(T_m - \frac{\Delta T}{2}\right) \\ \frac{T - T_m + \Delta T/2}{\Delta T}, & \left(T_m - \frac{\Delta T}{2}\right) < T < \left(T_m + \frac{\Delta T}{2}\right) \\ 1, & T > \left(T_m + \frac{\Delta T}{2}\right) \end{cases} \quad (5)$$

222 Here ΔT is transition temperature and its value is taken 2°C in the present study. The varying
 223 thermo-physical properties of PCM are modeled as a function of temperature through Eqs.
 224 (6)-(10). The viscosity μ of PCM is adjusted to ensure a very high value when the PCM is in
 225 the solid-state [13].

$$226 \quad \mu(T) = \mu_l \left(1 + \frac{C(1-B(T))^2}{C_0(B^3(T)+\varepsilon)}\right) \quad (6)$$

$$227 \quad \rho(T) = \rho_s + (\rho_l - \rho_s) \cdot B(T) \quad (7)$$

$$228 \quad k(T) = k_s + (k_l - k_s) \cdot B(T) \quad (8)$$

229 where the value of C_0 is taken $1 \text{ kg}/(\text{m}^3 \cdot \text{s})$ to make sure unit consistency, ρ_s and ρ_l are the
 230 density of the solid and liquid phases of PCM, respectively. Similarly, the k_s and k_l are the
 231 PCM's thermal conductivity for solid and liquid phases respectively. The specific heat of
 232 PCM which is temperature-dependent modeled including an extra term which accounts for
 233 the latent heat of fusion stored or released in the melting or solidification process,
 234 consequential in an adjusted heat capacity of PCM can be given by [13]:

$$235 \quad C_p(T) = C_{p_s} + (C_{p_l} - C_{p_s}) \cdot B(T) + L_f D(T) \quad (9)$$

236 where

$$237 \quad D(T) = \frac{e^{-\frac{(T-T_m)^2}{(\Delta T/4)^2}}}{\sqrt{\pi(\Delta T/4)^2}} \quad (10)$$

238 The reason for considering the Gaussian function $D(T)$ in eq. (9) is conserve the latent heat of
 239 PCM all over the transition period, because the integral of function $D(T)$ over the whole
 240 range of transition temperature ΔT is always 1 [31]. The consideration of ΔT produces a

241 numerical mushy region. The mushy region thickness grows with the growth in the value of
242 ΔT . The value of ΔT depends on the nature of the materials and can be fixed empirically if
243 one has previous information on the melting behavior of PCM. The deformation of geometry
244 owing to the PCM's thermal expansion is not considered in the present study.

245 *3.2. Computational method, meshing and validation of the model*

246 The above-mentioned equations are implemented in a fluid and laminar flow module of
247 COMSOL Multiphysics 5.5. The present study used fixed-grid approaches similar to the one
248 labeled in this section that consents to evade the necessity to solve the Stefan problem at the
249 varying melting front. Furthermore, the melting front tracing method necessitates an already
250 existed liquid layer, which is not the situation for the present study. Through fixed-grid
251 approaches, the standard method for the liquid flow and energy for instance the finite element
252 numerical resolution of N-S equations can be applied with partial modifications.

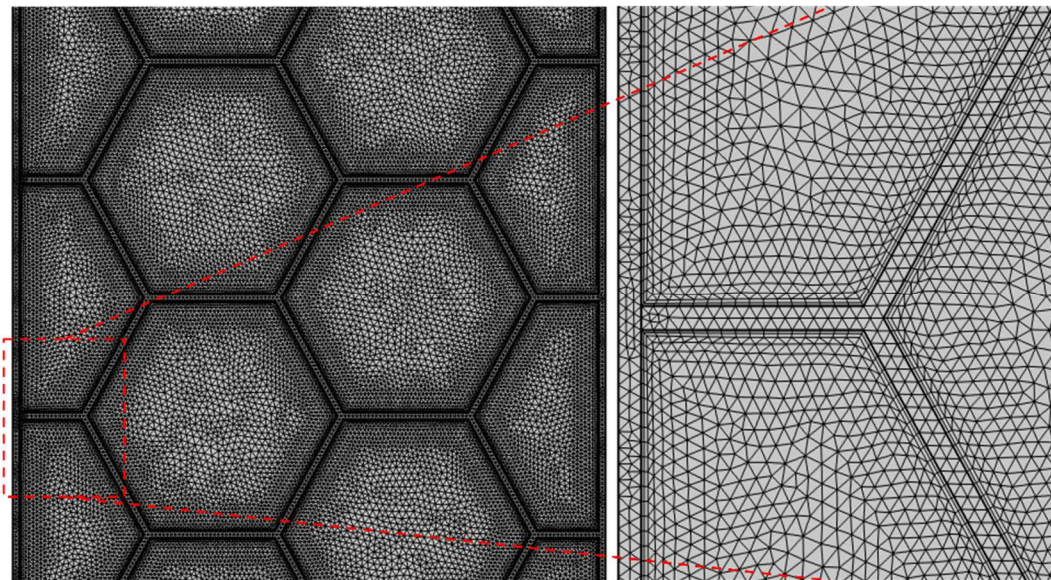
253 To solve the problem, an extremely fine mesh is chosen with a maximum and minimum size
254 of the element of value 5.98×10^{-4} m and 6.9×10^{-6} m respectively, which results in the total
255 number of 62716, 72050, 80806, and 95166 linear free triangular mesh elements for $L_C =$
256 0.015 m, $L_C = 0.01$ m, $L_C = 0.0075$ m and $L_C = 0.0075$ m respectively. The maximum mesh
257 size is defined using a condition on the mass mesh Peclet number [31]:

$$258 \quad Pe = \frac{\bar{u}\Delta x}{\vartheta} < 2 \quad (11)$$

259 where Δx is the maximum length of mesh cell in a unit 2D surface. From numerical
260 simulations, the maximum velocity in the honeycomb cell is taken as 5×10^{-3} m/s. Therefore,
261 Eq. (11) gives $\Delta x \approx 2 \times 10^{-3}$ m. In the present study, Pe is kept lower than 1 to increase
262 numerical stability. Consequently, the maximum mesh size is 1×10^{-3} m. The mesh is refined
263 at the borders of the PCM domain (see Figure 3). The first layer thickness of the boundary
264 layer is 5.22×10^{-5} m. Mesh sensitivity tests were also conducted at three increasing mesh
265 element sizes and the transient average temperature of the container's front surface was
266 observed at 38202, 50836, and 62716 mesh elements, as presented in Figure 4 for $L_C = 0.015$
267 m. For the other L_C , the maximum and minimum mesh sizes are the same, therefore the
268 change in the mesh size will not affect the output results from the model. From this figure, it
269 is observed that there is a negligible change in the variation of the front surface temperature

270 when increasing the number of mesh elements. Therefore, for the sake of accuracy, maximum
271 numbers of mesh elements were selected for the present study.

272 The numerical model presented above has been experimentally validated with our previous
273 experimental study by Biwole *et al.* [31] and a comparison of the temperature variation is
274 presented in *Figure 5*. For more details about the experimental setup and PCM properties,
275 etc. please refer to Biwole *et al.* [31]. The model explained above has also been validated
276 with the experimental results reported by Shokouhmand and Kamkari [32] on the Lauric
277 acid's melting in another previous study conducted by Biwole *et al.* [13]. The verification of
278 the model with previous experimental results provides the confidence for the detailed
279 systematic parametric studies of honeycomb geometry for enhanced thermal transport in
280 PCM.

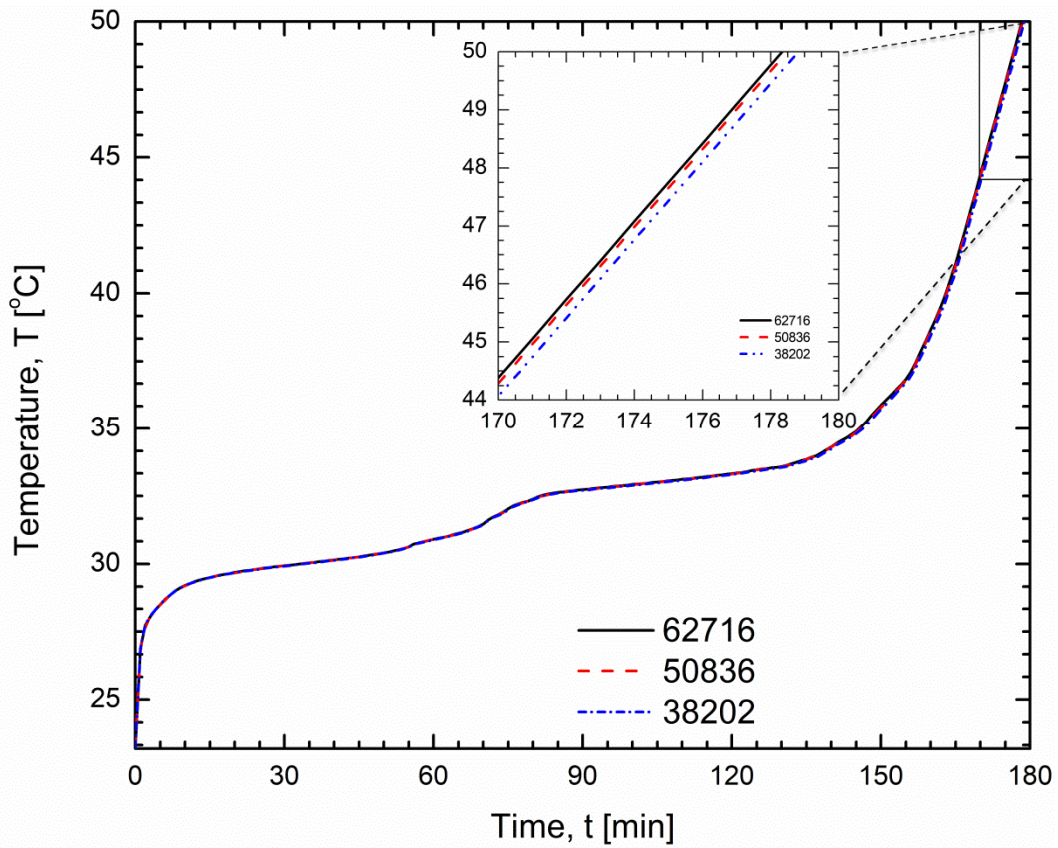


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Figure 3 Meshing of the computational domain

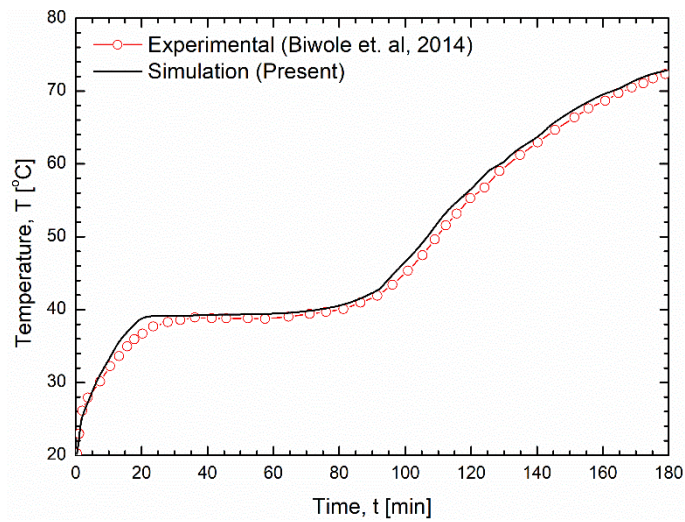
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Figure 4 Mesh sensitivity test of the model



285

286

Figure 5 Validation of numerical model with experimental study of Biwole et al [31]

287

4. RESULTS AND DISCUSSION

288

The findings of this study are described in four different subsections. In the first one, the

289

temperature variation in each cell and the whole computational domain, as well as the

290 observed evolution of the melt fraction are discussed, for a single honeycomb cell size and
 291 container's angle of inclination. In the next subsections, the effect of honeycomb cell size,
 292 container tilt angle, and honeycomb fin thickness are discussed. In the present study three
 293 factors are used to evaluate the efficiency of charging and discharging of PCM: (i) the
 294 average temperature of the front surface, which must keep on the lowest possible value for
 295 the longest possible time, (ii) the melt fraction of the PCM with time, (iii) the time-dependent
 296 energy storage content with a 1,000 W/m² constant heat flux on the front surface of the
 297 computational domain.

298 The melt fraction of the PCM in the computational domain is defined as:

$$299 \quad \phi = \frac{\text{Volume of the melted PCM } (T > (T_m + \Delta T/2))}{\text{Total volume of PCM}} \quad (11)$$

300 The energy stored in the PCM is calculated based on the temperature of the PCM.

$$301 \quad \text{for } T < T_m: E = mC_p(T - T_{ini}) \quad (12)$$

$$302 \quad \text{for } T = T_m: E = m\{C_p(T_m - T_{ini}) + L_f\} \quad (13)$$

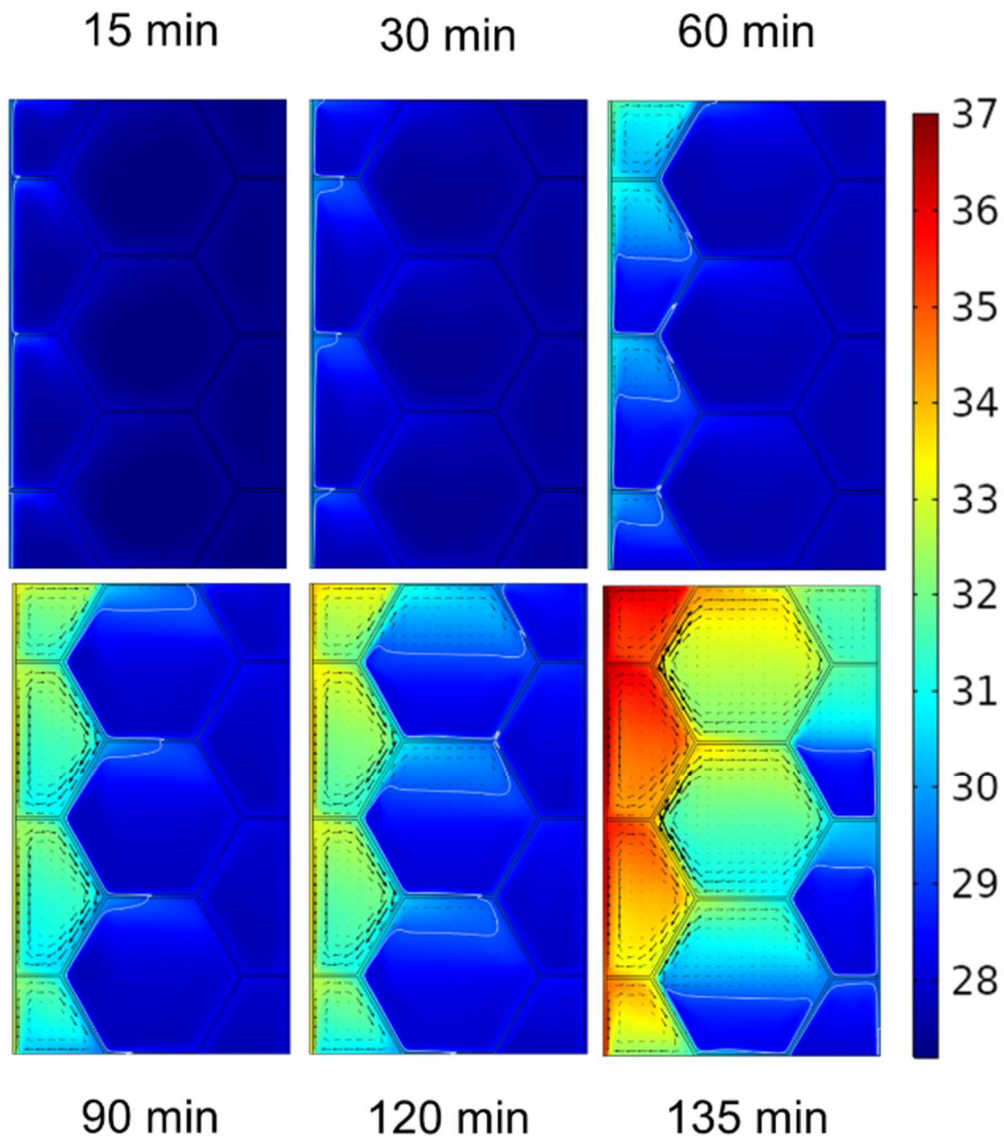
$$303 \quad \text{for } T > T_m: E = m\{C_p(T_m - T_{ini}) + L_f + C_p(T - T_m)\} \quad (14)$$

304 Here E is energy storage content and m is the mass of the PCM filled in the computational
 305 domain. The amount of energy stored in the melted PCM is computed as the energy stowed
 306 in entire numerical elements plus the computational domain.

307 *4.1. Melting of PCM in honeycomb cells*

308 The PCM's melting in honeycomb cells is presented in Figure 6, at different time intervals
 309 with 0.015 m cell length and 0.0005 m honeycomb fin thickness. The color contours
 310 represent the variation of temperature, arrows show the velocity field, and the white line
 311 denotes the melting front of the PCM. The heat flux applied to the front (left) surface of the
 312 computational domain heats the PCM filled in the cells near the front surface. The PCM starts
 313 melting and melted PCM moves upward due to the buoyancy force and collects at the top of
 314 each cell. It can also be noted that the thermal behavior on each cell is related to that of its
 315 vertical neighbors. Despite the fact that they receive the same normal heat flux from the left,

316 the cells situated at the top of the container heat up faster than the cells situated at the bottom.
 317 The warmer liquid PCM collected at the top of each cell, thus warming the cell directly
 318 above, also explains this. For all these reasons, a double temperature gradient is observed
 319 from top to bottom both in each cell and in the PCM container. As expected, a horizontal
 320 temperature gradient in the container is also noted as the heat propagates from the heated
 321 plate.



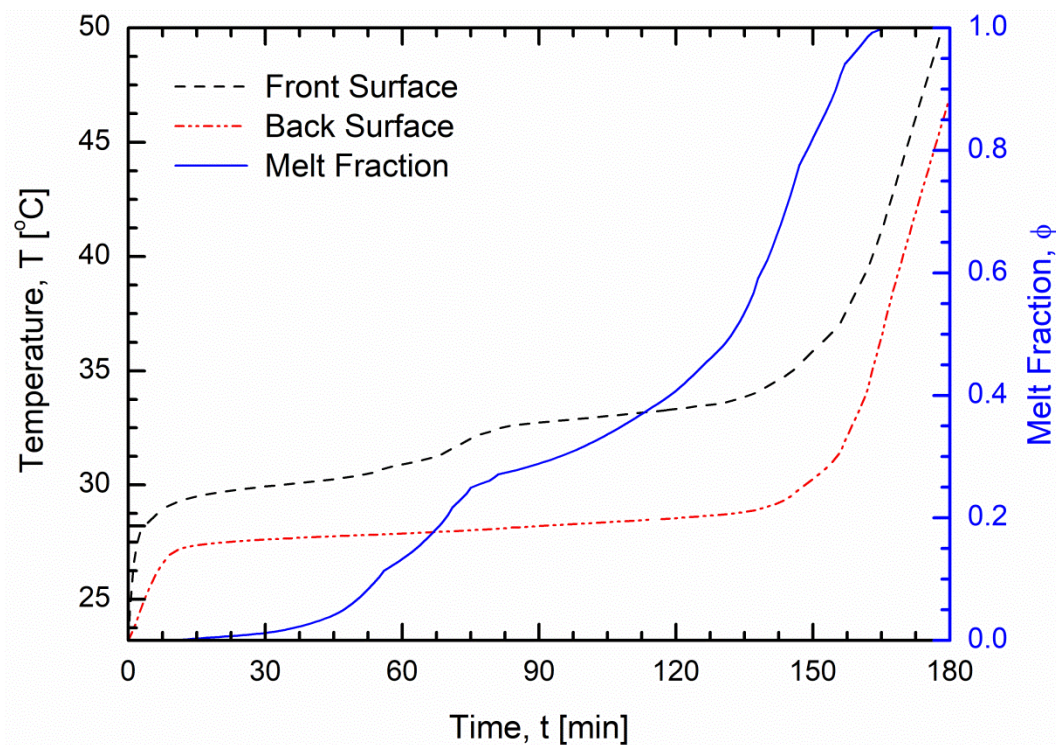
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323 *Figure 6 Temperature field, melting front (white contours) and moving direction (black*
 324 *arrows) of n-octadecane in honeycomb cells at different times*

325 The average temperature variation of the front and back surfaces, as well as the variation of
 326 melt fraction (ϕ) with time, are presented in Figure 7. The two inflexion points noted on the

327 curves of each surface average temperature are explained by the start and end of the PCM
328 melting in the container, as obvious when comparing with the melt fraction curve. At first,
329 the average front surface temperature increases sharply up to the melting temperature of the
330 PCM. Then, it increases more gradually until the melt fraction of the PCM reaches its
331 maximum value (i.e. 1). It resumes increasing sharply again as the heat storage is done in the
332 form of sensible heat.

333 From $t = 60$ min to $t = 90$ min, a sudden increase in the front surface temperature of the
334 computational domain is observed because of the complete melting of the cell near the front
335 surface, which affects the melting of the PCM in the other cells of the container. At the same
336 time, it was observed that there is a gradual increment in the melt fraction of the PCM
337 compared to the initial stage of melting. The average back surface temperature gradually
338 increases from the start of melting until the complete melting of PCM. Except at the start and
339 end of PCM melting, there is no sudden increment or decrement in its temperature variation.

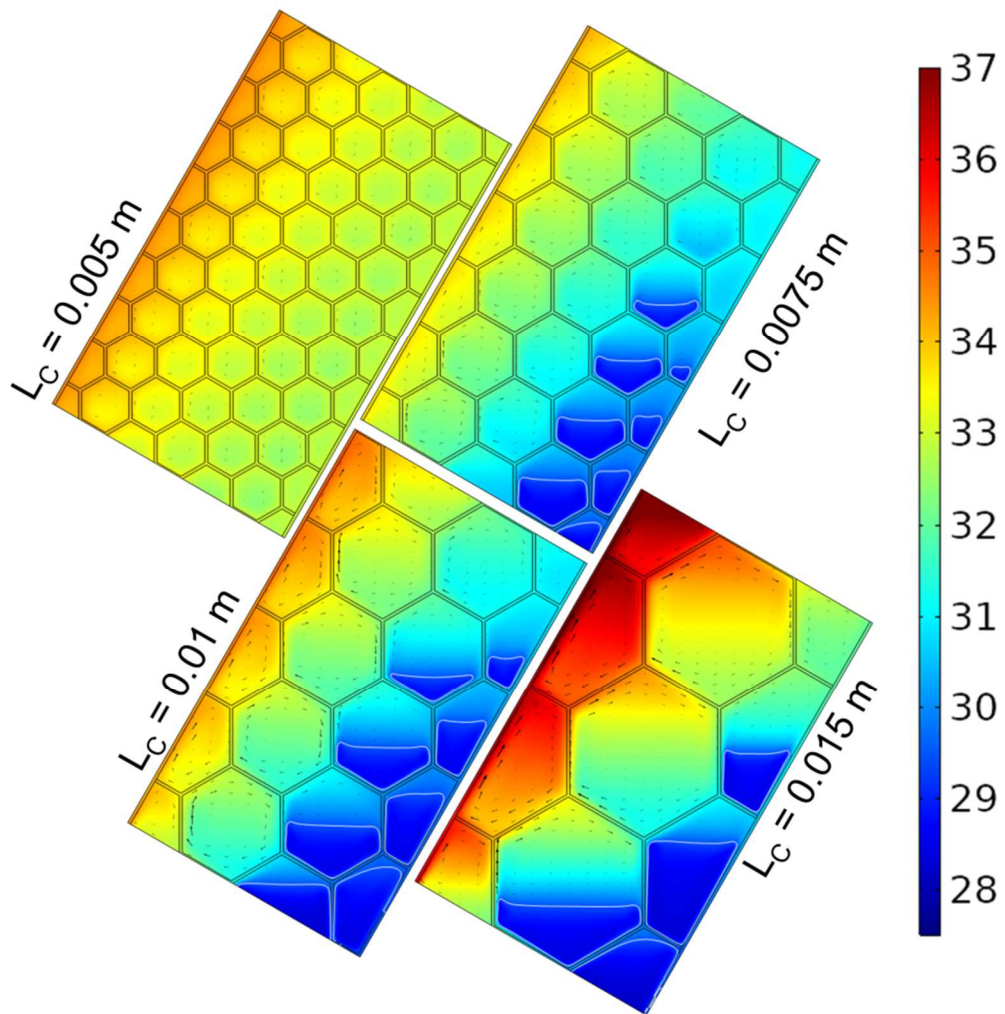


340

341 *Figure 7 Variation of melt fraction (ϕ) and average front and back surface temperature of*
342 *the container*

343 4.2. Effect of honeycomb cell size

344 Figure 8 represents the temperature field, the melting front and shows the moving direction of
345 the molten PCM in the computational domain for four different honeycomb cell sizes, at $t =$
346 150 min for $\delta_{fin} = 0.0005$ m and $\theta = 60^\circ$. For the smallest honeycomb cell size ($L_c = 0.005$
347 m), the PCM is completely melted, whereas for $L_c = 0.0075$ m, 0.01 m and 0.015 m, some
348 un-melted PCM remains. For the smaller cell sizes, the temperature gradient in the
349 computational domain is reduced as compared to the larger cell sizes.

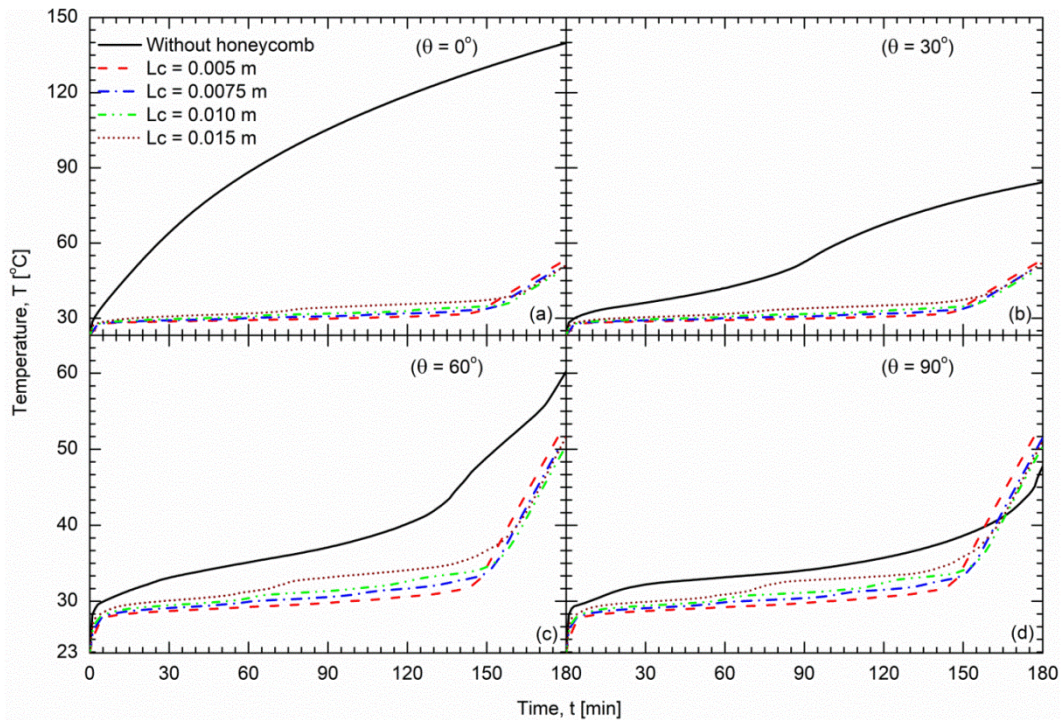


350

351 *Figure 8 Temperature field, melting front (white contours) and moving direction (black*
352 *arrows) of n-octadecane in honeycomb container for different cell size at 150 min ($\delta_{fin} =$*
353 *0.0005 m and $\theta = 60^\circ$)*

354 4.2.1. Effect of honeycomb cell size on the average front surface temperature

355 The average temperature variation of the front surface with time for different cell sizes and
356 angles of container inclination is presented in *Figure 9*. The comparison includes a case
357 without hexagonal cells in the computational domain. When the computational domain is
358 horizontal (*Figure 9(a)*, $\theta = 0^\circ$), the average temperature of the front surface without
359 hexagonal cells increases sharply and reaches around 135°C at 180 min because of pure
360 conduction in the PCM. The effect of PCM is hardly noticeable. However with the
361 honeycomb heat exchanger at $L_c = 0.005\text{ m}$, 0.0075 m , 0.01 m and 0.015 m the average front
362 surface temperature increases sharply only up to 30°C at $t = 5\text{ min}$, and then increases much
363 more gradually with time until $t = 150\text{ min}$. This behavior is due to the presence of
364 hexagonal cells in the container that facilitates a smooth heat transfer in the PCM. The fin
365 structure transports heat all over the computational domain efficiently, thanks to its higher
366 thermal conductivity. An increment in the tilt angle results in an enhancement of the
367 convective heat transport in the PCM, which in turn further reduces the average front surface
368 temperature. It is also observed that the angle of inclinations have a minor effect when the
369 cell size is small ($L_c = 0.005\text{ m}$, $L_c = 0.01\text{ m}$ and $L_c = 0.015\text{ m}$). From *Figure 9(a)-(d)* it is
370 noted that the inclination angle only affects the average front surface temperature when the
371 cell size is large. A major influence of the inclination angle on average front surface
372 temperature is only observed when there are no hexagonal cells in the computational domain.
373 Due to the addition of honeycomb cells, it is possible to keep the front surface temperatures
374 at 32°C , which is around 90°C below as compared to the horizontal case (i.e. $\theta = 0^\circ$, pure
375 conduction), 50°C lower as compared to $\theta = 30^\circ$ case, 15°C lower as compared to $\theta = 60^\circ$
376 case and 8°C lower as compared to $\theta = 90^\circ$ case. It is also probable to keep an approximately
377 constant temperature of the front surface for up to 140 min.



378

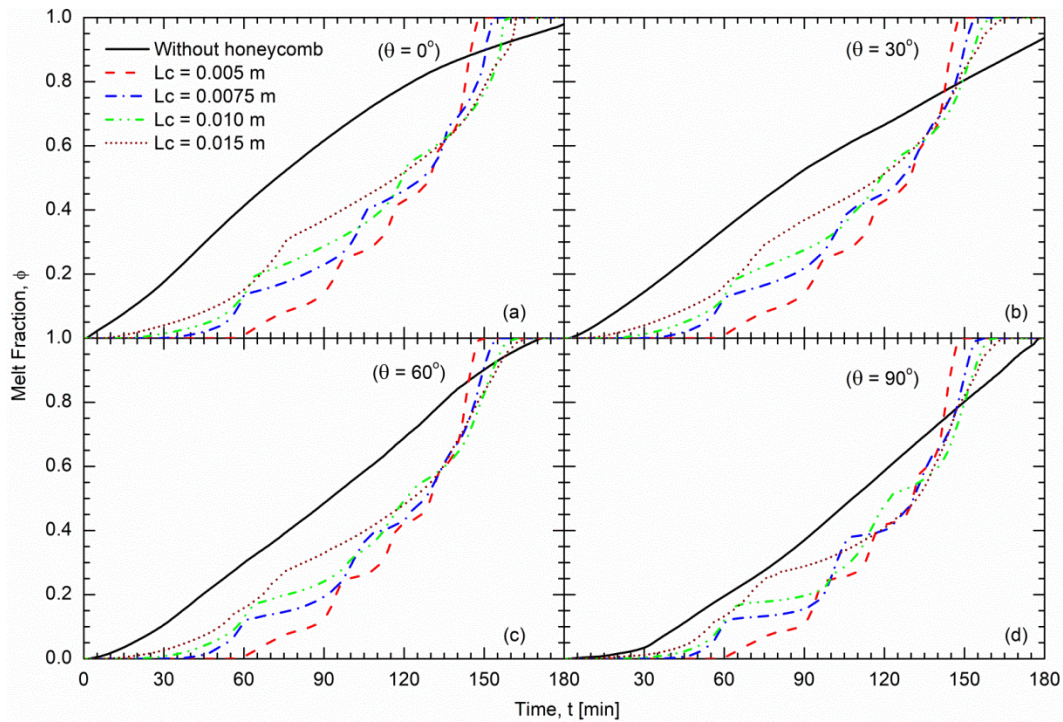
379 *Figure 9 Average front surface temperature variation with time for different honeycomb cell*
 380 *sizes: (a) at $\theta = 0^\circ$, (b) $\theta = 30^\circ$ (c) $\theta = 60^\circ$ and (d) $\theta = 90^\circ$*

381 *4.2.2. Effect of honeycomb cell size on the melt fraction*

382 The variation of melt fraction in the computational domain for different cell sizes and various
 383 inclination angles is shown in Figure 10. Four disparate inclination angles (i.e. 0° , 30° , 60° ,
 384 and 90°) are considered in the present study. The melt fraction without honeycomb cells is
 385 advanced as compared to that with honeycomb cells up to 140 min, regardless of the cell
 386 sizes. This behavior is observed because of two reasons. Firstly, the presence of honeycomb
 387 cells transfers heat to the entire computational domain, not only to the PCM available near
 388 the front heating surface. Due to the absorption of heat as sensible heat by the computational
 389 domain, the melt fraction of the PCM without cells is higher for a certain time and melting
 390 starts later for the smallest cell size as compared to larger cell size. Secondly, in the
 391 beginning, the convection heat transfer is accentuated in the configuration without cells, since
 392 the melt PCM has more room for movement. After a certain amount of time (140 min here),
 393 the latter convection process fails to achieve fast melting of the solid PCM situated as the
 394 bottom left of the container and becomes less efficient than that of celled configurations
 395 where heat is transported everywhere, as shown in Figure 8.

396 The latter reasoning holds when comparing meshed configurations. One can observe that for
397 cases with higher cell sizes, melting starts earlier but ends later than for smaller cell sizes. As
398 the heat which is transferred from the heated surface to the entire computational domain is
399 reduced with larger cells, their initially higher melting rate decreases, and they finally take a
400 longer time to achieve complete melting. For all the inclination angles it is observed that the
401 melting starts at around 60 min, 35 min, 20 min, and 10 min for $L_c = 0.005$ m, $L_c = 0.0075$ m,
402 $L_c = 0.01$ m, and $L_c = 0.015$ m respectively, meaning that the finer the mesh, the later the
403 melting start.

404 There are several inflection points observed in the melt fraction variation for all the cell sizes
405 and inclination angles. The first inflection point for $L_c = 0.005$ m, $L_c = 0.0075$ m, $L_c = 0.01$
406 m, and $L_c = 0.015$ m is observed when melt fraction reaches around 0.1, 0.15, 0.2 and 0.3
407 respectively. The second inflection point in the melt fraction is not observed when $L_c =$
408 0.015 , however for $L_c = 0.005$ m, $L_c = 0.0075$ m, $L_c = 0.01$ m the inflection point is observed
409 when the melt fraction reaches 0.225, 0.45, and 0.55 respectively. The number of inflection
410 points in the melt fraction variation depends on the number of cells in the direction of the
411 heat flux application. The inflections in the melt fraction are because of the uneven heat
412 transfer that happened simultaneously by the additional contact resistance at the surface of
413 each cell and to convection in the melted PCM within the cells. Regarding the latter cause,
414 the heat transfer to the honeycomb cell is faster when the PCM filled in the previous cell is
415 completely melted. If the PCM filled in the previous cell is not completely melted, the heat is
416 absorbed by the solid PCM and a reduced amount of energy is transferred to the next cell
417 which reduces the melting rate in that cell, resulting in a reduced melt fraction.

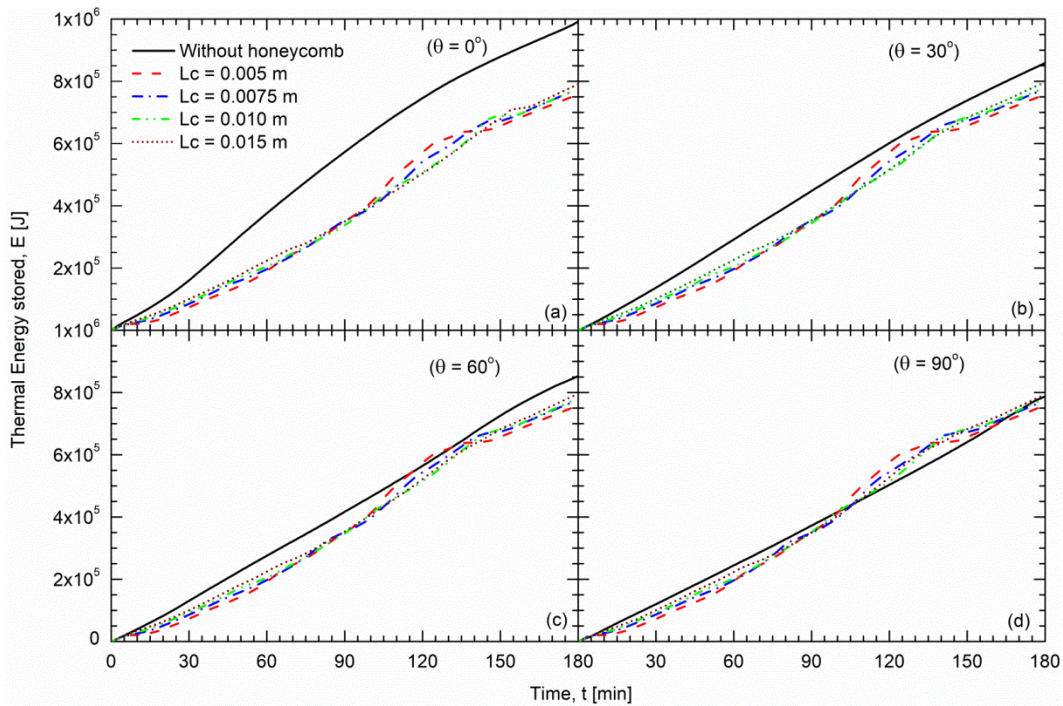


418

419 *Figure 10 Melt fraction variation with time for different honeycomb cell sizes: (a) at $\theta = 0^\circ$,*
 420 *(b) $\theta = 30^\circ$ (c) $\theta = 60^\circ$ and (d) $\theta = 90^\circ$*

421 *4.2.3. Effect of honeycomb cell size on the energy stored*

422 The energy stored is calculated for different cell sizes and tilt angles, as presented in Figs.
 423 Figure 11(a)-(d). The maximum energy is stored for the computational domains that have no
 424 hexagonal cells because, without honeycomb cells, the temperature of the computational
 425 domain is higher as compared to other configurations, which results in additional energy
 426 stored in as sensible heat. The honeycomb cells facilitate the heat transfer to the backplate
 427 and the environment beyond, thus reducing the thermal energy remaining in the container.
 428 The decrease in the cell size causes an increased number of cells in the computational
 429 domain, which reduces the actual volume of the PCM in the container. Therefore, finer mesh
 430 configurations exhibit a lower heat storage capacity. For meshed configurations, it is also
 431 observed that the inclination angle does not significantly affect the energy content in the
 432 PCM.



433

434 *Figure 11 Energy stored in PCM with time for different honeycomb cell sizes: (a) at $\theta = 0^\circ$,*
 435 *(b) $\theta = 30^\circ$ (c) $\theta = 60^\circ$ and (d) $\theta = 90^\circ$*

436 4.3. Effect of the inclination angle

437 The melting of PCM in a rectangular container also depends on the inclination angle due to
 438 the convection effect. The effect of the tilt angle of the computational domain from horizontal
 439 on the average temperature of the front surface, melt fraction, energy stored in the container
 440 is presented for two different cell sizes, $L_C = 0.015\text{ m}$ and $L_C = 0.0075\text{ m}$.

441 4.3.1. Influence of inclination angle on the average front surface temperature

442 Figure 12(a) and (d) show the average front surface temperature variation at different angles
 443 of inclination for two different cell sizes $L_C = 0.015\text{ m}$ and $L_C = 0.0075\text{ m}$, respectively.
 444 For both cell sizes, the minimum average front surface temperature is obtained with $\theta = 90^\circ$
 445 because of higher convective heat transfer in the computational domain. The impact of the
 446 angle of inclination on the average front surface temperature is negligible with smaller cell
 447 sizes because of the enhanced thermal transport due to the existence of the fin structure. The
 448 presence of the fin structure reduces the velocity field; however, it enhances thermal transport
 449 via the metallic structure.

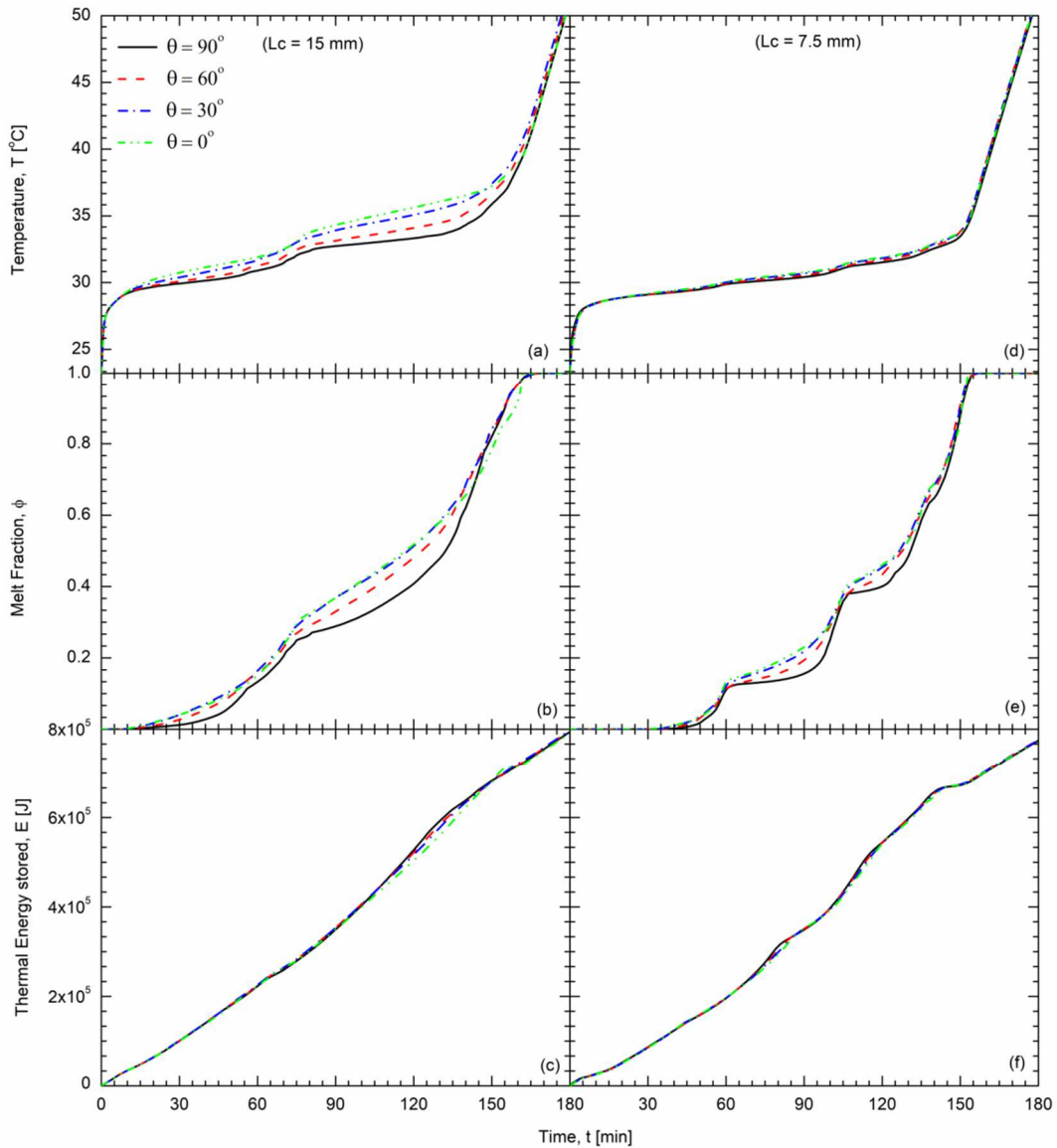
450 *4.3.2. Influence of inclination angle on the melt fraction*

451 The Influence of the tilt angle of the computational domain on the melt fraction for two
452 different cell sizes is presented in Figures 12(b) and (e). For a certain time duration, the melt
453 fraction is advanced when the computational domain is completely horizontal ($\theta = 0^\circ$) for
454 both cell sizes. Further, there are inflection points in the melting curve of both cell sizes. As
455 previously mentioned, this is due to the uneven heat transfer that happened because of the
456 additional contact resistance at the surface of each cell and to convection in the melted PCM
457 within the cells. The number of inflection points in the melt fraction depends on the number
458 of hexagonal cells present in the computational domain.

459 *4.3.3. Influence of inclination angle on the energy stored*

460 The energy storage content in the PCM with time at different inclination angles is presented
461 in Figure 12(c) and (f) for $L_C = 0.015$ m and $L_C = 0.0075$ m, respectively. There is a small
462 variation are observed for the different angle of inclination during energy storage with $L_C =$
463 0.015 m, however, there is no variation with $L_C = 0.0075$ m. for given cell size and fin
464 thickness the overall rate of energy storage is the same, regardless of the angle of inclination.
465 This is due to the hypothesis of normal heat flux on the front surface in all configurations.
466 The results might be different in real applications where the amount of solar radiation
467 received depends on the container's tilt angle.

468



469

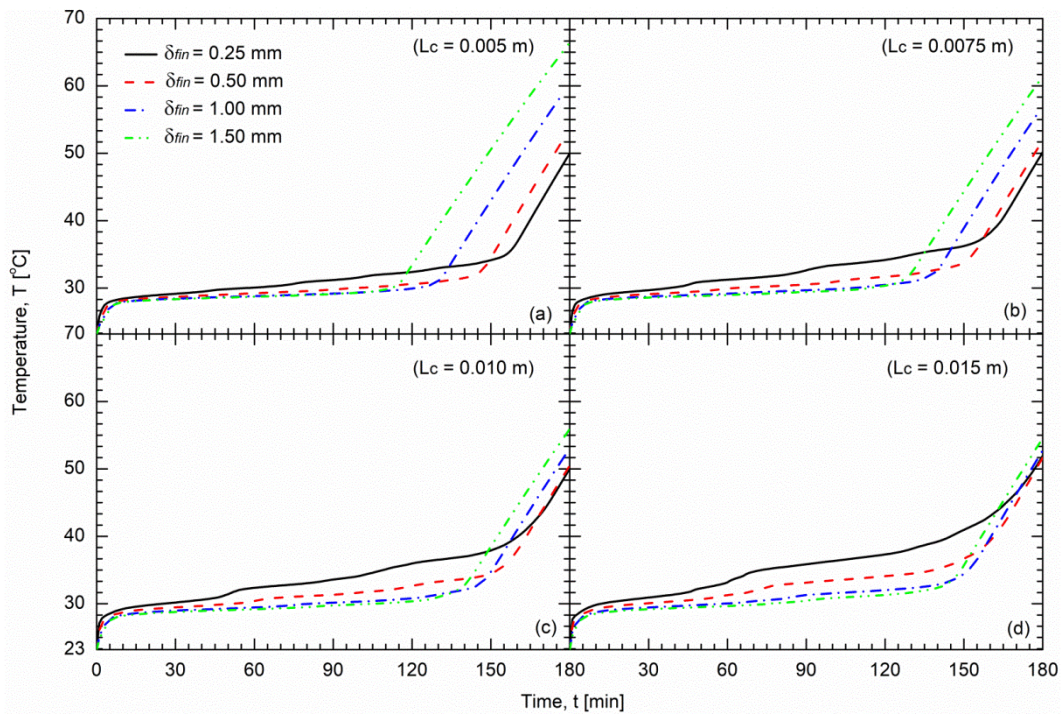
470 *Figure 12 Effect of tilt angle on average front surface temperature, melt fraction and energy*
 471 *stored in the PCM: (a)-(c) $L_C = 0.015$ m, (d)-(f) $L_C = 0.0075$ m*

472 4.4. Effect of the honeycomb cell fin thickness

473 4.4.1. Effect of the honeycomb cell fin thickness on the average front surface temperature

474 *Figure 13* represents the average front surface temperature variation for four different
 475 honeycomb cell fin thicknesses (i.e. $\delta_{fin} = 0.25$ mm, 0.5 mm, 1 mm and 1.5 mm). Four
 476 different cell sizes are also considered. *Figure 13* (a) represents the average temperature
 477 variation for $L_C = 0.005$ m. At first, the minimum temperature is obtained with a thicker fin
 478 because of higher heat transmission to the backplate. But due to enhanced heat transfer to the
 479 PCM and reduced volume of PCM in the container, the thicker fin configuration is also the

480 one with a shorter melting time and its average front surface temperature becomes highest
 481 after the complete melting of PCM. The same behavior is observed for all fin thicknesses,
 482 with the inversion depending on the fin thickness, except before the end of melting where
 483 there is a very small temperature difference for $\delta_{fin} = 0.5 \text{ mm}, 1 \text{ mm}$ and 1.5 mm . As
 484 shown in *Figure 13* (b)-(d) the cell size does not significantly change the above-described
 485 pattern. However larger cell sizes reduce thermal transport to the PCM and therefore, the
 486 average front surface temperature is higher for the higher cell size.



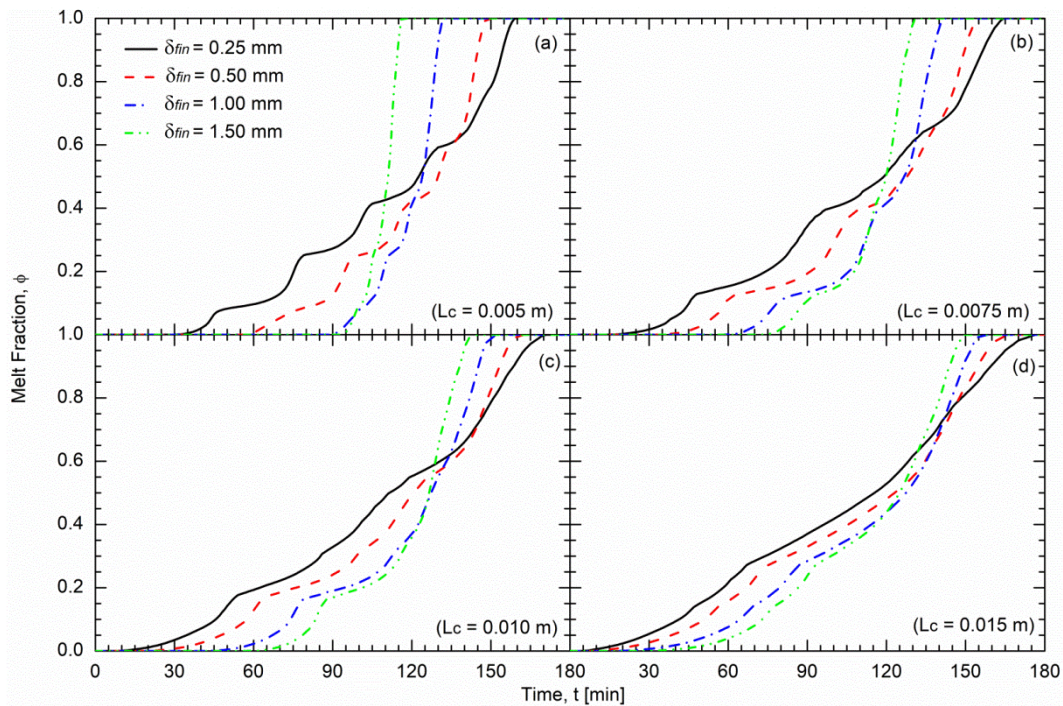
487

488 *Figure 13* Average front surface temperature variation with time at different honeycomb fin
 489 thickness: (a) at $L_C = 0.005 \text{ m}$, (b) $L_C = 0.0075 \text{ m}$ (c) $L_C = 0.010 \text{ m}$ and (d) $L_C = 0.015 \text{ m}$

490 4.4.2. Effect of the honeycomb cell fin thickness on the melt fraction

491 The effect of honeycomb cell fin thickness on melt fraction for different cell sizes is shown in
 492 *Figure 14*(a)-(d). *Figure 14*(a) represents the melt fraction at $L_C = 0.005 \text{ m}$ for different fin
 493 thicknesses. The melting of PCM starts later for higher fin thicknesses as compared to lower
 494 ones, because of the higher fin thickness transport to the backplate and higher storage of
 495 sensible heat in the fins. Due to sensible heating below the melting temperature, the melting
 496 of PCM starts later which can be visible in *Figure 14*(a). Similar to the previous subsection,
 497 after fin sensible heating, the heat transfer is enhanced with higher fin thickness, with less
 498 volume of PCM, which explains the end of melting, earlier than that of lower fin thicknesses.

499 A similar pattern is obtained with all other cell sizes; however, the complete melting time is
 500 higher for higher cell sizes.

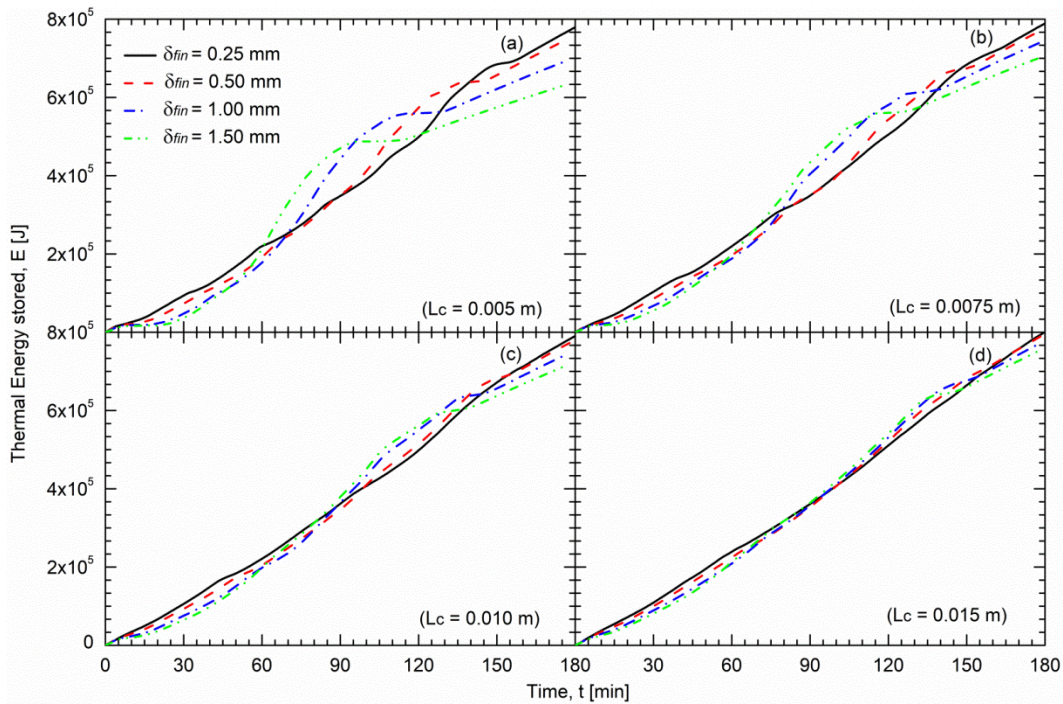


501

502 *Figure 14 Melt fraction variation with time at different honeycomb fin thickness: (a) at $L_c =$*
 503 *0.005 m, (b) $L_c = 0.0075$ m (c) $L_c = 0.010$ m and (d) $L_c = 0.015$ m*

504 *4.4.2. Effect of the honeycomb cell fin thickness on the energy stored*

505 The variation of energy storage content in the computational domain with time for different
 506 fin thicknesses for four different cell sizes is presented in Figure 15(a)-(d). Initially, the
 507 energy storage rate in the PCM is higher for smaller fin thicknesses, as the energy is quickly
 508 transported to the PCM (reduced sensible heat accumulation in the fins). After the melting of
 509 PCM starts, it becomes lower for lower fin thicknesses, as previously explained. The overall
 510 energy storage content after complete melting is higher for lower fin thickness and minimum
 511 for highest fin thickness because of the reduction in the actual volume of PCM filled in the
 512 computational domain. Increasing the cell size tends to reduce the effect of fin thickness, as
 513 the rate of energy storage becomes similar for all cases (Figure 15 (c)-(d)).



514

515 *Figure 15 Energy stored in PCM with time at different honeycomb fin thickness: (a) at $L_c =$*
 516 *0.005 m, (b) $L_c = 0.0075$ m (c) $L_c = 0.010$ m and (d) $L_c = 0.015$ m*

517 **5. Conclusions**

518 In the current study, the influence of honeycomb meshed fins on the heat transport
 519 performance of a rectangular PCM container inclined at different angles from horizontal has
 520 been numerically studied. A 2D numerical model of the rectangular container with
 521 honeycomb structure considering conduction and convection modes of heat transfer in the
 522 melted PCM is developed. The heat transfer and energy storage behavior without honeycomb
 523 cells was looked up to that of four other configurations where the PCM is filled in
 524 honeycomb cells of four different lengths, thicknesses, and tilted at four different inclination
 525 angles. The evaluation of the charging and discharging efficiency of the PCM-filled in
 526 honeycomb fins structures were based on the melting time, the regulation of the front plate
 527 temperature to retain it as low as possible for the longest possible duration, as well as the
 528 energy storage rate.

529 Results have shown that natural convection plays an important role in maintaining the
 530 average temperature of the front surface to a constant value and for continuous thermal
 531 transport in PCM. Further, optimized honeycomb cell length and fin thickness choices would
 532 be vital for a rapid heat transfer to the rear end of the computational domain. It was also

533 found that a tilt angle of the honeycomb cells has a minor influence on the heat transfer
534 behavior of all studied patterns when the cell size is small. The total melting time is minimum
535 for lower cell sizes and higher fin thickness regardless of the orientation of the computational
536 domain. With such a configuration, it is possible to keep the front surface temperatures at 32
537 °C, which is around 90°C lower compared to the horizontal case (pure conduction, $\theta = 0^\circ$).
538 The energy storage behavior of the PCM with varying time is also investigated for the range
539 of parameters selected in the present study and it is found that the total energy content is
540 higher without honeycomb mesh because of the higher amount of PCM, while the tilt angle
541 has a marginal effect on the energy storage rate in cases where the heat flux remains normal
542 to the heated surface. Finally, it is concluded that this type of fin structure leads to enhanced
543 thermal transport in the PCM to maintain the front surface temperature constant. Besides, the
544 charging and discharging time of PCM is reduced as compared to without meshed
545 configuration. Overall, such studies for PCM encapsulated in honeycomb cells may be
546 utilized for appropriate thermal management and to optimize heat transfer and energy
547 storage.

548

549 Declaration of competing interest

550 The authors have no conflict of interest regarding this work.

551 Acknowledgment

552 The authors want to acknowledge the Université Clermont Auvergne postdoctoral grant
553 2020-2021.

554

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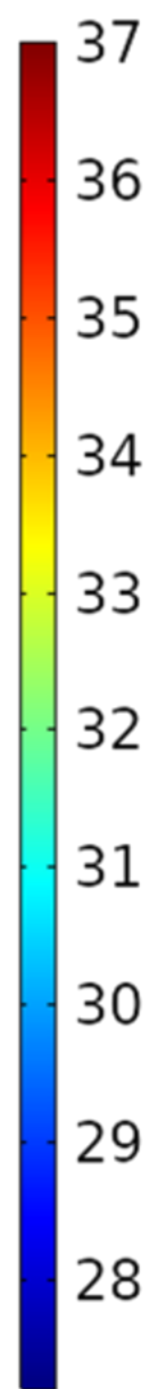
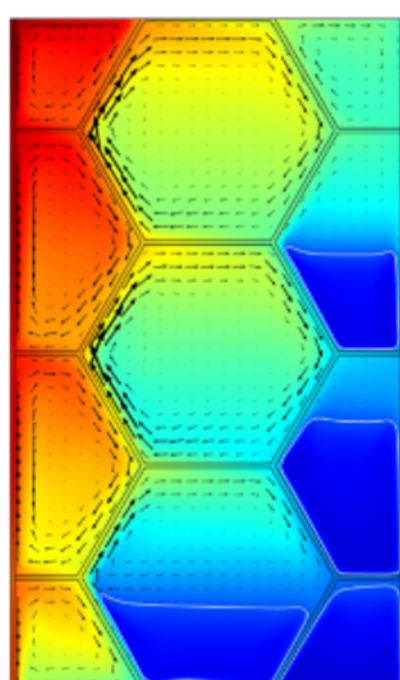
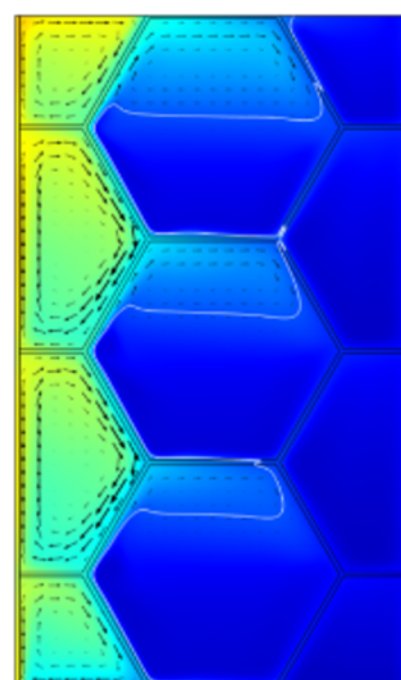
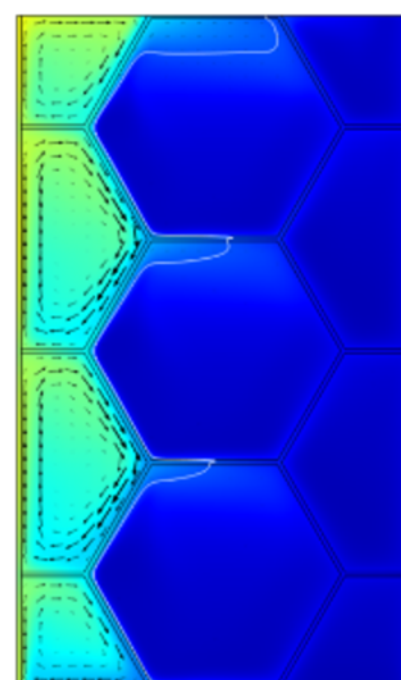
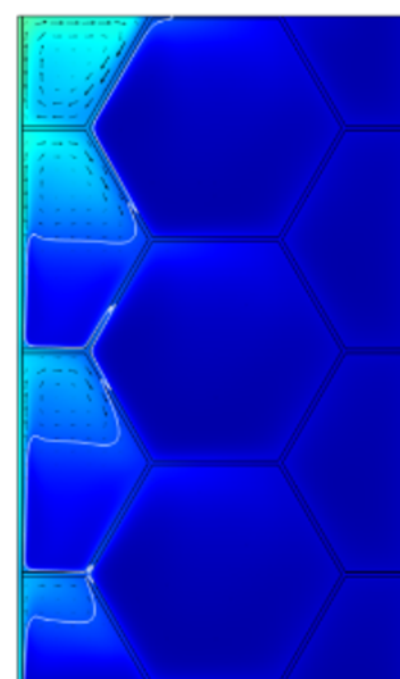
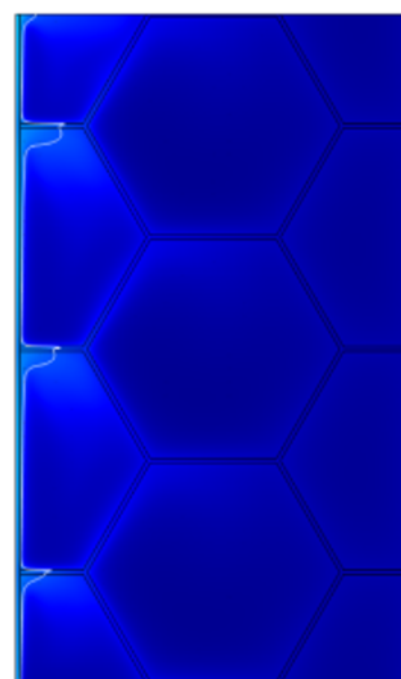
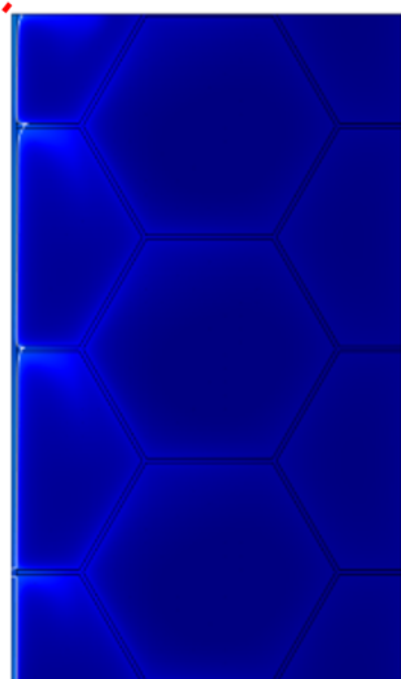
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15 min

30 min

60 min



90 min

120 min

135 min