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# Longitudinal impedance and coherent synchrotron radiation models for ThomX storage ring

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# Abstract

This article deals with the design of an impedance model (including geometric, resistive wall and coherent synchrotron radiation (CSR) wakefields) for ThomX, a 50 MeV electron storage ring designed to work in pulsed mode. The beam dynamics is very different from usual damped storage rings and is strongly dominated by collective effects. The geometric and resistive wall impedance model is obtained using simulation or analytical modelling of the individual elements and is checked using wire measurements on prototypes. The CSR is simulated in a rectangular vacuum chamber to take into account transient effects and resonances. From these models, two distinct regimes of beam dynamics stand out, driven respectively by the CSR and by the geometric impedance. *Keywords:* Beam coupling impedance, Coherent synchrotron radiation, Wire measurement, Wakefield

### 1. Introduction

ThomX is a compact laser-electron storage rings (LESR) [1], a Compton backscattering X-ray source, which is being built at LAL, Orsay, France [2, 3]. ThomX storage ring design parameters are shown in Table 1. In this machine, electrons are accelerated and injected into a storage ring where they interact

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with a laser to produce  $1 \times 10^{13}$  photons per second in the hard X-ray range (50 to 90 KeV). As usual in LESR, such as TTX-II [4], NESTOR [5] or ThomX, the beam can suffer from strong degradation by single, multiple Touschek scattering and Compton interaction. To counter this effect, the machine works in pulsed mode: a new bunch is injected every 20 ms while the older one is extracted [6]. 10 The global aim of the machine is to maximise the X-ray flux produced by tak-11 ing care of the spectral and angular flux [7]. The electron storage ring has been 12 designed with this intent which makes the electron beam dynamics very differ-13 ent from the beam dynamics in usual storage rings dedicated to synchrotron 14 radiation production [8, 6, 9, 10]. The difference results from damping times 15 long compared to the storage time. As the electron dynamics is not damped, 16 it is crucial to manage the collective effects (defined as the interaction of the 17 particles with each other as well as with its environment) as, once the beam is 18 perturbed it will not recover within the storage time. In addition, the beam is 19 injected without longitudinal matching and the lattice has a strong nonlinear 20 dependence on energy of the momentum compaction. Due to the previous con-21 siderations, the bunch undergoes a transient regime of filamentation at injection 22 until it has fully filled the RF bucket [6]. Besides, the injected electron bunch 23 has a low energy, 50 MeV, a relatively high charge, 1 nC, and a short duration, 24 a few ps, which implies very strong collective effects. In particular, the coherent 25 synchrotron radiation (CSR) is expected to play a strong role during the tran-26 signt regime as the injected bunch length is short. After the transient regime, 21 the bunch length is much longer and the CSR impact is expected to be much 28 more reduced compared to the geometric and resistive walls (RW) wakefields. 29

During the design phase of an accelerator project, the different beam coupling impedance sources should be estimated and summarised in an impedance budget. The impedance bugdet can then be used to ensure that the wakefields will not prevent achieving nominal performances, which for ThomX means avoiding any degradation on the X-rays flux or quality. Also, a good knowledge of the machine impedance allows for a better discrimination of possible instability sources. Unfortunately strong discrepancies have been noted between

Table 1: ThomX nominal storage ring design parameters. The range of values given for the emittance, the relative energy spread and the bunch duration correspond to typical beam properties at injection depending on the linac setup.

Parameter	Value	$\mathbf{Units}$
Beam energy $E_0$	50	MeV
Emittance (rms, normalised) $\epsilon_{x,y}$	7 - 9	$\rm mm.mrad$
Rel. energy spread at inj. (rms) $\sigma_{\delta}$	0.2 - 0.6	%
Bunch duration at inj. (rms) $\sigma_s$	6 - 16	$\mathbf{ps}$
Bunch charge $Q$	1	nC
Circumference $L_0$	18	m
Number of bunch	1	
Current I	16.7	${ m mA}$
Trans./long. damping time $\tau_{x,y}/\tau_s$	1/0.5	$\mathbf{S}$
Momentum compaction factor $\alpha_1$	0.0124	
Tune x/y, $Q_x/Q_y$	3.17/1.74	
Storage time before ext./inj. $T_{store}$	20	$\mathbf{ms}$

measured data and prediction based on computed impedance budgets [11]. A 37 way to check the impedance estimations, obtained by numeric simulation or by 38 analytic development, is to use bench measurements [12, 13]. As a basis for 39 future complete analysis of the beam dynamics in the presence of collective ef-40 fects, we present in this paper the simulated and measured impedance models 41 for the geometric, resistive walls and CSR wakefields for ThomX storage ring. 42 We show that the CSR is dominant with respect to impedance during the tran-43 sient regime when the bunch length is short. After the transient regime, the 44 bunch length is much longer and the CSR impact is reduced compared to the 45 geometric and RW wakefields. 46

The geometric and RW model has been obtained using either numerical simulations or an analytical model for each of the different components. It is presented in section 2. The simulations have then been cross-checked against bench measurements using the coaxial wire method, the measurement results are shown in section 3 and the detailed error estimate is presented in appendix. Finally, the CSR has been simulated, taking into account rectangular chamber and drifts, using the CSRZ code [14] and the results are presented in section 4.

# <sup>54</sup> 2. ThomX RW and geometric impedance model

When it was possible, the storage ring elements have been simulated using 55 CST [15] up to 50 GHz corresponding to a bunch length of  $\sigma_z = 2$  mm, which is 56 the bunch length at injection. For higher frequencies, the geometric impedance 57 contribution is much smaller than the CSR one and thus can be neglected in 58 the specific case of ThomX. CST wakefield solver can be used to compute the 59 fields generated by a beam when said beam is going trough 3D structures. It 60 takes into account both of the geometric and the resistive wall wakefields and 61 has been benchmarked multiple times against theory and other codes [15, 16]. 62 When numerical simulation was not possible, due to thin coating on kicker 63 magnets, an analytic model was used. 64

The plots of the real part and of the imaginary part of the longitudinal impedance  $Z_{\parallel}$  are shown in Fig. 1. The contribution of each element type is represented by the different coloured areas. The summary of the impedance budget is shown in Table 2. The loss factor  $k_{\parallel}$  for each individual element is computed for a  $\sigma = 2 \text{ mm}$  bunch and the relative contribution of each type to the total loss factor  $k_{\parallel,T} = 6.73 \text{ V pC}^{-1}$  is shown. We will now go through the contribution of each element.

Table 2: Summary of all the elements composing ThomX storage ring and of their relative contribution to the impedance budget. Loss factor  $k_{\parallel}$  computed for a Gaussian longitudinal distribution of  $\sigma_z = 2 \,\mathrm{mm}$ .

Element	Number	$\boldsymbol{k}_{\parallel}~(\mathrm{V/pC})$	% of $k_{\parallel,T}$
Bellows	18	$1.54 \times 10^{-2}$	4.1 %
BPMs	12	$3.59 \times 10^{-2}$	6.3~%
IP clearing electrodes	2	$1.20 \times 10^{-2}$	0.4~%
IP chamber	1	$1.23 \times 10^{-1}$	$1.8 \ \%$
Pumping ports	15	$4.13  imes 10^{-2}$	9.2~%
Kickers	2	$4.1  imes 10^{-1}$	12.2~%
Septum	1	1.14	17.0~%
FBT	1	$1.52 \times 10^{-1}$	2.3~%
RF Cavity + Tapers	1	3.14	46.7~%
Total		$k_{\parallel,T} = 6.73$	100 $\%$

71



Figure 1: Real and imaginary part of the longitudinal impedance  $Z_{\parallel}$  for ThomX storage ring (without the RF cavity contribution). Each component contribution to the total impedance is represented by a coloured area. The full sum corresponds to the upper limit of the yellow (pumping ports) area.

# 72 2.1. Bellows, BPMs and pumping ports

ThomX beam pipe has an octagonal cross section and most of the elements have the same shape to avoid impedance increase due to tapered sections. The bellows have integrated RF fingers with the same octagonal cross section in order to shield the beam from the irregular surface of the bellows, see Fig. 2. The 18 bellows of the storage ring amount to 4.1 % of the total loss factor  $k_{\parallel,T}$ .



Figure 2: CST model of the bellows with RF fingers.

78

There are different types of beam position monitors (BPMs) in ThomX storage ring. Their design is based on SOLEIL BPMs [17, 18], which is a classic button BPM bloc with four electrodes. In ThomX, some BPMs have double

BPM blocs with six or hight electrodes. The additional buttons are used as 82 ion clearing electrodes to avoid ion trapping by the electron beam [8, 19]. In a 83 button BPM, the electromagnetic fields excited by the beam can be trapped in 84 the structure. There are two main trapped modes, at 8.6 GHz and at 18.0 GHz, 85 which correspond to the modes created between the BPM button and the BPM 86 bloc housing the button. The fields can also propagate and resonate in the 87 dielectric material composing the vacuum insulator and act back on the beam. 88 These resonant modes, located around 14 GHz, have a lower amplitude com-89 pared to the main ones. The loss factor value in Table 2 for the BPMs corre-٩N sponds to a double BPM bloc with six buttons. 91

#### 92 2.2. Interaction point

In addition to BPM, there are also two stand-alone clearing electrodes lo-93 cated at the interaction point (IP) and at the point symmetric to the IP. Each 94 of them is composed of two BPM buttons. The vacuum chamber at the IP is a 95 special design, the interaction laser needs to be able to enter and exit the chamber in order to produce X-rays via Compton interaction with the electron beam. 97 Two windows have then been cut in the curved sections of the IP chamber which 98 contributes to the machine impedance. As it is not possible to simulate curved 99 section in CST, the same windows have been adapted to a straight line geometry 100 similar to the one of the IP chamber to estimate the wakefield generated. 101

## 102 2.3. Pumping ports

ThomX pumping ports consist of a circular opening in the vertical plane 103 behind a grid which continues ThomX typical cross section. There are several 104 types of pumping ports in the storage ring, some of them in bent regions. The 105 bent pumping port impedance is assumed to be the same as the ones in straight 106 sections. As for the bellows, the pumping port impedance is of the broad band 107 type, with a very low amplitude at the lower frequencies but the amplitude 108 slowly increases at higher frequencies. Around 50 GHz, the bellows, the pump-109 ing ports and the BPMs account for more than 50 % of the total broad band 110 impedance. 111

# 112 2.4. Kickers

Kickers are often complex pieces to handle with respect to impedance estima-113 tion, as shown by the high number of publications focusing on kicker impedance 114 evaluation. ThomX kickers are composed of an elliptic ceramic chamber which 115 is coated by a thin ( $\approx 100 \,\mathrm{nm}$ ) layer of titanium which is partially oxidised on 116 surface due to the air contact during the manufacturing process. The chamber 117 has to allow the magnetic field, produced by the fast kicker magnets, to go 118 inside the chamber for the kicker to be effective which is why the ceramic is 119 used as the body of the chamber. In the same time, the chamber is coated by 120 a conductor in order to allow the image current to flow along the coating and 121 limit heating and wakefield emission. 122

But having a ceramic chamber also mean than the beam electromagnetic 123 field can reach outside of the chamber and can interact with outside materials. 124 In particular, the magnet system is composed of rectangular ferrite yokes. The 125 interaction of the beam electromagnetic field with the ferrite is a concern as it is 126 known to produce high impedance for past kickers [20, 21, 22]. But this type of 127 element, with thin coatings and ferrite, is very complex to simulate on software 128 like CST because the huge number of mesh cells needed to take into account 129 the different scales. Even with adaptive mesh cells, the 3D model would still 130 need more than  $10^9$  mesh cells in order to correctly model both the thin coating 131 and the rest of the structure. An eventual simulation this way would take much 132 133 more memory and computation time than what is affordable.

So to evaluate the kicker impedance, an analytical model close to the kicker 134 geometry and allowing to tackle the issues raised was used: the multi-layered 135 cylindrical chamber model [23] computed using IW2D [24]. This model allows to 136 derive the impedance of a 2D (i.e. infinite in the longitudinal direction) axisym-137 metric structure composed of different circular layers. This model is very well 138 adapted to the ceramic chamber, as the ceramic and the coatings have uniform 139 width (supposedly for the titanium and its oxidised part) corresponding well to 140 a layered model. For the magnet system part, which is further from the beam, 141 its geometry is neither axisymmetric nor uniform but it will be approximated 142

as so. The elliptic geometry of ThomX kickers has been taken into account
using Yokoya factors to correct the results given for a circular geometry [25].
Compared to simulations, the advantage of using an analytical model is that it
is very easy to get the impedance up to very high frequency, up to 1 THz for
this study.



Figure 3: Models used in IW2D based on ThomX kicker geometry. The parameter used for the materials are shown in Table 3.

Table 3: Parameter used in IW2D for ThomX kicker materials:  $\rho_{DC}$  is the DC resistivity of the layer,  $\tau$  is the resistivity relaxation time,  $\epsilon_b$  is the real part of the dielectric constant,  $\chi_m$  is the magnetic susceptibility,  $f_m$  is the permeability relaxation frequency and h is the layer thickness.

Materia $p_{DC}$ ( $\Omega$ m)	au (s)	$\epsilon_b$	$\chi_m$	$f_m$ (Hz)	<b>h</b> (m)
Titan <b>i</b> $0$ <sup>13</sup> (10 <sup>11</sup> to 10 <sup>15</sup> )	0	1	0	$\infty$	$10 \times 10^{-9}$
OX-					
ide					
$TiO_2$					
Titanium $5.5 \times 10^{-7}$	$5.7\times10^{-16}\approx0$	1	0	$\infty$	$90 \times 10^{-9}$
Ti					
Aluminium $10^{12}$	0	9.8	0	$\infty$	$5  imes 10^{-3}$
OX-					
ide					
$Al_2O_3$					
Ferrite $10^6$	0	1	2000	$\infty$	$15 \times 10^{-3}$

Using IW2D, several layered models were used to design a more realistic kicker model, see Fig. 3. The first model is composed of layers of vacuum, titanium oxide, titanium and then of alumina ceramic. The second one has two additional layers, a vacuum layer followed by a ferrite layer. The model 1 is used to cover the two kicker extremities where there is no ferrite and the model 2 is used for the central part which houses the magnet system. The longitudinal impedance produced by this realistic kicker model is shown in Fig. 4. The impedance spectrum is composed of an important broad band component with oscillations with a period of 10 GHz. The large value of the broad band maximum is due to the bad conductivity of both the ceramic and the titanium oxide. The oscillations are linked to the high dielectric constant,  $\epsilon_b = 9.8$ , of the ceramic. The high magnetic susceptibility of the ferrite,  $\chi_m \approx 2000$ , leads to the high frequency impedance oscillations seen on the spectrum and on the high amplitude resonance at 58 GHz.



Figure 4: Longitudinal impedance produced by the kicker versus frequency. Real part is in red and imaginary part in blue. The top plot is the full spectrum from DC to 1 THz and the bottom one is a zoom ranging from DC to 80 GHz. This results corresponds to 126 mm of model 1 and 204 mm of model 2.

161

Several approximations were made to obtain the kicker impedance. The 162 actual geometry of the magnet system is neglected, some physical parameters of 163 the materials (i.g.  $\chi_m$ ) are known to be frequency dependent but not considered 164 as such in this model and the value of most of the parameters is subject to large 165 uncertainties. The value of  $\chi_m$  for the ferrite layer which has been used is the 166 DC value, which should lead to overestimate the impedance ( $\chi_m$  is supposed 167 to decrease with f). In order to estimate the error due to large parameter 168 uncertainties, the models 1 and 2 composing the final kicker model have been 169

computed for different parameters within their probable range. Overall, the error  $\Delta Z$  due to the lack of knowledge about material parameter should be  $\Delta Z \approx \pm 5 \Omega$ . This corresponds to a 20 % error on the estimation of the loss factor  $k_{\parallel}$  for the kickers.

# <sup>174</sup> 2.5. Septum, transverse feedback (FBT) and RF cavity

The septum chamber is designed to allow the beam injection and extraction while shielding the stored beam from the septum DC magnet. The main body of the chamber is shielded from the constant magnetic field produced by the septum magnet with a thin layer of mu-metal. Mu-metal is metal with an high relative magnetic permeability  $\mu_r$  which prevent the DC component of the magnetic field to go through it. Thanks to this mu-metal layer, the stored beam is not affected by the septum magnet magnetic field.

The septum chamber is a complex piece with respect to impedance esti-182 mation because it presents many different features impacting the impedance. 183 Firstly, the septum chamber begins with a taper transition from the ThomX 184 cross section to a rectangular cross section. Then, this rectangular cross section 185 is reduced in the horizontal plane to allow for the injection/extraction windows, 186 this transition corresponds to a step in and then to a step out in the horizontal 187 plane. Finally, the central part shows both a pumping grid on one side and 188 the mu-metal shield all around this central region. The mu-metal magnetic 189 permeability is highly frequency dependant,  $\mu_r = 520 \times 10^3$  at DC and  $\mu_r =$ 190  $80 \times 10^3$  at 60 Hz. It is possible to use frequency dependant materials in CST, 191 but in practice the computational cost explodes when trying to use it to model 192 thin layers for a high frequency range. So, as it is known that the magnetic 193 permeability of the mu-metal decreases very quickly with frequency [26], the 194 relative magnetic permeability of the mu-metal has been set to 1 in the wake-195 field simulations. The impedance found for the septum is broad band and very 196 197 characteristic of a step transition with a frequency cut-off around 5.5 GHz.

The transverse feedback (FBT) aims to damp the injection jitter and to suppress transverse instabilities. It uses a stripline kicker composed of four

electrodes, which reproduces ThomX cross section, connected to electrical feed-200 through at both ends. The electrodes are supported by ceramic (marcor) holders 201 and are connected to the feed-through via coper foils. In order to minimise the 202 impedance, 0.5 mm capacitive gaps have been added on each side of the elec-203 trodes. This capacitive gap, combined with the inductance of the feedthroughs 204 and copper foils, and the 50  $\Omega$  electric impedance of the electrodes, creates a low 205 pass filter [27]. The cut-off frequency of this filter depends on the height of the 206 capacitive section h. CST simulations have been done for several values of the 207 height of the capacitive section h, varying h from 0 mm to 15 mm, in order to 208 find the value that would minimise the impedance. The design with h = 10 mm209 is chosen as it allows to reduce the loss factor from  $k_{\parallel,h=0mm} = 0.21 \,\mathrm{V \, p C^{-1}}$  to 210  $k_{\parallel,h=10mm}=0.15\,{\rm V\,pC^{-1}}$  for a  $\sigma_z=2\,{\rm mm}$  bunch length. 211

The RF cavity used in ThomX is a 500 MHz single cell copper cavity of the 212 ELETTRA type [28], tapers are used to adjust its cross section to ThomX vac-213 uum chamber one. As time domain wakefield simulations are not well adapted 214 to compute the impedance of an RF cavity, the cavity has been simulated in 215 the frequency domain. The longitudinal and transverse modes of the cavity 216 have been simulated with eigenmode solvers and measured using a vector net-217 work analyser (VNA) in transmission mode [29]. The impedance of the RF 218 cavity can then be built using the RLC resonator model [30]. The RF cavity 219 contribution to the total impedance is not shown in Fig. 1 as its impedance 220 only corresponds to very high amplitude, narrow resonances. The tapers have 221 been simulated in CST and their impedance is broad band with a frequency 222 cut-off around 10 GHz. The value indicated in Table 2 corresponds to the loss 223 factor of both the RF cavity and its tapers simulated together,  $k_{\parallel,RF+tapers} =$ 224  $3.14 \,\mathrm{V \, pC^{-1}}$ , which is superior to the sum of the loss factor of its two components 225 taken individually  $k_{\parallel,RF} + k_{\parallel,tapers} \approx 2.97 \,\mathrm{V \, p C^{-1}}.$ 226

# 227 3. Impedance measurements using the coaxial wire method

Impedance evaluation is not always a straightforward affair, using analytical models provide an exact solution but the model seldom corresponds to the real

object one wants to evaluate. Nowadays, electromagnetic simulations are very 230 powerful and perfected tools but this often come with an increased difficulty 231 to set the numerous parameters of these "black boxes" like solvers. Because 232 of this difficulty to parameter, it is possible to get a simulation result far from 233 reality if the simulation is incorrectly set. RF measurements have the advantage 234 to allow the component direct measurement, contrary to analytical models and 235 simulations where a model has to be set. But the measurement is difficult, not 236 always easy to interpret and is not possible for every elements. Finally, beam 237 measurements of the impedance allow the accuracy of an existing impedance 238 model to be checked. But, in most cases, it comes too late in the process to 239 allow for the element modification if too big an impedance is detected. 240

For these reasons, when building an impedance model for a machine, com-241 mon wisdom says that, ideally, one should use at least two different methods for 242 each element one wants to evaluate. In order to constitute ThomX impedance 243 model, the main method which was chosen is time domain simulation using 244 CST. Then, when possible, RF measurements were done in order to cross check 245 the simulation results. This section describes the impedance measurements done 246 using the coaxial wire method. It first focuses on the setup used and on the 247 measurement limitations, the measurement of the bellows with and without RF 248 fingers, see Fig. 2, is then presented and compared with simulations. 249

### 250 3.1. Measurement setup

Impedance measurements using the classical coaxial wire method use the 251 fact that electromagnetic field produced by an ultrarelativistic beam is close to 252 the one produced by a coaxial TEM transmission line [31]. It is then possible 253 to measure the impedance using a Vector Network Analyser (VNA) matched to 254 the TEM transmission line created by a Device Under Test (DUT) and a wire 255 inserted inside the DUT. The VNA measures the transmission parameter S21, 256 which corresponds to the ratio of the output power wave to the input power 257 wave. The measurement of the DUT is carried out with respect to an ideal 258 reference line in order to remove any effect coming from the setup. The principle 259

of the measurement is described in more detail in [12, 13]. The log-formula has been chosen for the impedance evaluation from the RF measurements [32]:

$$Z = 2Z_L \ln\left(\frac{S21_{DUT}}{S21_{REF}}\right) \tag{1}$$

where  $Z_L$  is the line impedance of the DUT. The log-formula has the advantage of being able to correctly resolve lumped impedance parts while keeping an acceptable error for distributed impedance parts [12].

The measurement setup is presented in Fig. 5. A half shell flange is used 265 to support the measurement setup, an RF bulkhead going through the half 266 shell links the cable going to the VNA (Vector Network Analyser) to the RF 267 connector. A coaxial cable brazed on the RF connector and stripped on the 268 end tip is used as an antenna. A resistor is brazed on the stripped tip of this 269 coaxial cable in order to match the two coaxial lines. Then the CuBe (Copper 270 Beryllium) wire is brazed on the other end of the resistor. A metallic plate is 271 used to separate the RF connector part from the measurement part. If there 272 is no separation then the TEM modes created between the external conductor 273 of the coaxial conductor can propagate and disrupt the measurement. In order 274 to damp reflections on this plate, RF absorbing foam has been glued to it. In 275 the aim of improving repeatability, the plate and the foam have been glued to a 276 metallic support which can be removed to screw the RF connector and tauten 277 the wire. 278



Figure 5: Measurement setup for longitudinal impedance using the coaxial wire method

A TEM coaxial line is created by the wire going trough the vacuum chamber. In order for the electromagnetic wave from the VNA to propagate without reflections to the system along the wire, the two lines  $Z_0 = 50 \ \Omega$  and  $Z_L$  must be adapted by a matching resistor [13].

The line impedance  $Z_L$  of a ThomX beam pipe has been simulated using 283  $CST^{TM}$  MW for different wire diameters and compared with the analytic for-284 mula for the case of round chambers. In this case, it is necessary to determine an 28 equivalent diameter  $D_{eq}$  for ThomX cross section which is not cylindrical. The 286 value of this equivalent diameter  $D_{eq} = 30.9$  mm is chosen so that the analytical 287 results match the simulations. The material of the wire is chosen to be copper 288 beryllium (CuBe) in order to be able to tauten the wire without stretching it. 280 The half shell flanges have been designed to have a diameter of  $D_{eq} = 30.9 \text{ mm}$ 290 to have the same line impedance  $Z_L$  as the vacuum pipe one. 291

In order to be able to measure high impedance components, it is important 292 to have the highest line impedance  $Z_L$  possible [13]. Ideally the line impedance 293 should be much higher than the DUT impedance. However, there is a com-294 promise to be made between the frequency precision and attenuation of the 295 signal with respect to the wire diameter which will be explain briefly in the 296 measurements section [33, 34]. Firstly, we started to do measurements with a 297 wire diameter of d = 1 mm which gives a line impedance of  $Z_L = 205.7 \pm 6.0$ 298  $\Omega$ . In this case, the matching is done using a resistor of  $R_s = Z_L - Z_0 \approx 150 \Omega$ . 200 To compare the impact of wire thickness, the measurements were also done with 300 thinner wires of 0.1 mm and of 0.025 mm. Using thinner wires increase the line 301 impedance  $Z_L$  and allow for a better precision when measuring high impedance 302 components. These additional measurements will also help to determine the 303 influence of the wire diameter on the signal attenuation. The line impedance 304 corresponding to the 0.1 mm and 0.025 mm wires were calculated with respect 305 to analytic formula and they are equal to 343.76  $\Omega$  and 426.88  $\Omega$  respectively 306 [13]. 307

### 308 3.2. Measurement limitations

The coaxial wire measurement of the impedance has many limitations which can prevent a good measurement. Some limitations come from the setup and other come from the method used to do the measurement.

A first limitation is fixed by the calibration done on the VNA before doing the measurement. Using a calibration kit valid down to -40 dB it is not possible to accurately measure below -40 dB. This means that, using Eq. (1), the maximum impedance value which can be precisely measured using this setup is  $Z_{max} =$  $-2Z_L \ln(-40dB) \approx 1900 \ \Omega$  with 1 mm wire. This limit is further reduced because the measurement of the reference has to be taken into account.

A second limitation would be due to the repeatability of the measurements. 318 When doing coaxial wire measurements many aspects change from measurement 319 to measurement and may increase the uncertainty of the measurement: the 320 brazing and the tautening of the wire, the positioning of the RF absorbing 321 foam, the screwing of the half shell flanges on the DUT, ... In order to decrease 322 the statistical errors, several measurements have been taken and the impedance 323 is computed from the averaged value. Systematic errors include the effect of 324 the wire thickness and the limitations of the log-formula. A support to fix the 325 positioning of the RF foam is used and the measurement is done in a clean room 326 with fixed temperature and pressure. A precise error quantification has been 327 done to estimate this limitation, see Appendix A. 328

Lastly the coaxial wire method has been shown to be inaccurate below the 320 beam pipe cut-off frequency [35]. The stretched wire perturb the behaviour of 330 the electromagnetic field by allowing TEM waves with zero cut-off frequencies 331 332 whereas, in realistic situation with a beam, these modes would not be able to propagate. The cut-off frequency  $(TE_{11})$  for a round pipe is given by  $f_c = \frac{j_{1,1}c}{2\pi R}$ 333 with  $j_{1,1}$  the first root of the Bessel function  $J_1$ , c the speed of light and R the 334 radius of the beam pipe. For ThomX cross section, if the value  $R_{eq} = \frac{D_{eq}}{2}$  is 335 used then,  $f_c=5.7~\mathrm{GHz}.$  The method is known to give good results above 30 %336 of the cut-off [35], for ThomX this would mean above  $1.3f_c \approx 7.4$  GHz. Below 337 7.4 GHz, the amplitude and frequency shift introduced by the wire can be seen 338 as an additional error on the measurement. 339

As the limitations are severe, in our case the coaxial wire method is only used to validate the simulation tools and methods.

### 342 3.3. Measurement of the reference section

In order to measure impedance by the wire method, it is necessary to measure 343 an "ideal reference line" corresponding to  $S21_{REF}$  in Eq. (1). This measurement 344 is used as the reference to take into account the defaults of the setup and the 345 particular geometry of the beam pipe cross section. The reference section used 346 here is a plain vacuum pipe using ThomX cross section. Ideally, the reference 347 section and the DUT should have the same length. But in our case, there are 348 many objects of different length to measure and it does not seem justified to 349 make new reference sections for each object to measure. 350

Two length of reference section were measured, 100 mm and 500 mm. The two S21 measurements give very similar results but the longer section shows small oscillations on top of the general behaviour shown by both sections. As the difference between two sections of very different length is small enough, it is legitimate to use one of these two measurement as reference for a DUT no matter its length. For smaller DUT, which size is around 100 mm, the smaller one is used and for bigger DUT the other is used. The comparison of the 100 mm and 500 mm can be seen in Fig.6.



Figure 6: S21 measurement of ThomX reference section, the 100 mm section is plotted in blue and the 500 mm section in red. The mean value for the set of 5 measurements is plotted in plain line and the 95 % CI is shown in dotted lines.

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#### 359 3.4. Measurements

The RF measurement of the bellows has been done with and without the RF fingers to test the effectiveness of the RF fingers in suppressing the trapped modes. The transmission parameter S21 for these measurements is shown in
Fig. 7. The measurement of bellows with RF fingers is very close to the reference measurement which indicates that the shielding works as intended. The
measurement without RF fingers shows strong resonance peaks which clearly
stand out of the reference measurement.



Figure 7: S21 measurement of ThomX bellows, with RF fingers in blue, without RF fingers in red and the 100 mm reference section in black. The mean value for the set of 5 measurements is plotted in plain line and the 95 % CI is shown in dotted lines.

Figure 8 shows the real part of the impedance obtained using the log formula, Eq. (1). It is compared with CST simulations of the impedance for both cases, in dotted lines with RF fingers for the top plot and without RF fingers for the bottom plot for the 1 mm diameter wire.For the bellows with RF fingers, the measurement agrees very well with the simulation which gives a very low impedance.

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For the bellows without RF fingers, firstly the measurements were done with 373 1 mm wire. The simulation agrees relatively well with the measurement as the 374 four peaks found in simulation also appears in the measurement. The two strong 375 peaks at 2.1 GHz and 3.5 GHz in the simulation are shifted respectively at 2.2 376 GHz and 3.6 GHz in the measurement and have a lower amplitude value by 377 a factor 8 to 10. The two smaller peaks at 4.4 GHz and 4.8 GHz are shifted 378 respectively at 4.3 GHz and 4.6 GHz but have comparable amplitude. The 379 differences in amplitude and the shifts in frequency can be explained by the 380 variable geometry of a real bellows compared to the fixed bellows modelled in 381 CST simulation, the loss in the resistors and the attenuation due to the thickness 382 of the wire [36]. For example, the resistors used for line impedance matching 383 can bring additional noise for high frequency applications. The current density 384

is related to frequency for resistor which creates additional noise and power 385 loss [34]. For comparison, the same measurements were done with the thinner 386 wire of 0.1 mm. The reproducibility error with 0.1 mm wire on the bellow and 387 reference section measurements were reduced nearly half compared to the 1 mm 388 wire measurements and even more in the case of the high resonance peaks as 389 it can be seen in Figure 9. The most likely reason is the change in the wire 390 tension coming from the difficulty in stretching the 1 mm wire. With the 0.1 391 mm wire, the frequency shift with respect to the impedance calculations was 392 reduced significantly as it can be seen in Figure 10 however the attenuation gets 303 bigger with the thinner wire [36]. Also the strong field distortion due to the 394 insertion of the wire creates frequency shifts in impedance spectrum decreasing 395 when the wire diameter gets smaller [33, 34]. In the measurement, the peaks 396 are broader than in the simulations as all the components of the real bellows do 397 not resonate at the same frequency due to small variations in the bellows period 398 which do not exist in the perfect model used for simulations. As a good trade 399 off between the frequency precision and the attenuation, it was decided to use 400 0.1 mm wire for future measurements. It is important to note the effectiveness 401 of the RF fingers in suppressing the high impedance measured without the RF 402 fingers. 403

In addition to the bellows, measurements have also been performed on several prototypes of BPMs, of pumping ports and of the RF cavity and its tapers [8, 29]. Despite the important uncertainty and the limited frequency range of the measurements, they have allowed to check that the elements were correctly represented in CST, and that the element design and manufacture is suited to produce low impedance elements.

#### 410 4. Coherent synchrotron radiation impedance model using CSRZ

In this section, a coherent synchrotron radiation (CSR) impedance model for ThomX storage ring is developed following the same idea as for the geometric and resistive wall impedance. The CSR community usually uses a different convention for the impedance and the wake functions compared to the one use



Figure 8: Real part of the impedance of ThomX bellows : a) Measurement with RF fingers, b) Simulations with RF fingers, c) Measurements without RF fingers, d) Simulations with RF fingers. The mean value for the set of 5 measurements is plotted in plain line and the 95 % CI is shown in thin dotted lines for a) and c).



Figure 9: The real part of the simulated and measured impedances for 1 mm and 0.1 mm wire



Figure 10: The standard deviation on the bellow measurements for 1 mm and 0.1 mm wire

here and used in the literature for the geometric and resistive wall wakefields [15, 30, 37]. In the CSR convention, a positive wake function corresponds to an energy loss and the impedance spectrum is the complex conjugate of the one use here. This section keeps using the same convention used in this paper but plots -Im[Z] in the impedance spectrum in order to keep the usual display of the impedance for the CSR.

The steady-state parallel plate model is often used to estimate the CSR impedance [38, 39, 40]. In this model, an electron (point like charge) moves in between two perfectly conducting plates separated by a distance h on the horizontal direction. As it takes into account the shielding created by the beam pipe walls, this model adds a threshold  $f_{sh}$  below which the CSR impedance is very strongly reduced compared to the free space model [38, 39].

These simple models correspond to a steady-state situation where the elec-427 tron bunch trajectory is perfectly circular. In most real machines, the dipoles 428 are interleaved with drift spaces which introduce transient effects at dipole en-429 trance and exit. The CSR fields emitted in the dipoles are guided by the vacuum 430 chamber, acting as a waveguide, and propagate along the beam in the straight 431 sections, see (c) of Fig. 11. This effect, also called "drift CSR", is more im-432 portant if the machine contains short dipole magnets. Some more complicated 433 analytical models take into account transient effects [41, 42]. 434

In addition to transient effects, the CSR fields can also be reflected, some-435 times multiple times, on the transverse beam pipe walls, as in (b) of Fig. 11. 436 The reflections on the outer walls lead to head-tail effects while the reflections 437 on the inner walls lead to tail-head effects. When the magnet is long compared 438 to the vacuum chamber width a, the CSR fields can resonate within the vacuum 439 chamber and excite the eigenmodes of the vacuum chamber [14]. Furthermore, 440 the CSR fields radiated in a dipole can propagate until the next dipole and 441 interfere with the new CSR fields produced in this second dipole [14]. 442

For now, the only way to consider all these effects is to use numerical methods which allow to simulate the CSR wakefield or CSR impedance for a given beamline and vacuum chamber geometry. The CSRZ code, by Demin Zhou, is a



Figure 11: Schematics of the electron interaction within a bunch due to coherent synchrotron radiation (CSR). White arrows show the propagation direction of the bunch and red arrows the emitted CSR field. The bunch is represented by an ellipse with the black contour with inside an electron of the tail in blue and one of the head in green. (a): effect of CSR in free space, the CSR radiated by the tail affects the head of the bunch. (b): effect of the walls, the CSR radiated by the head is reflected on the walls and affects the tail. (c): transient effect at dipole exit, the CSR field emitted at the dipole exit travels parallel to the bunch and interacts with it during the drift.

FORTRAN 90 code which allows to compute the CSR impedance of a beam 446 by numerical integration of Maxwell's equations in the paraxial approximation 447 [14, 43]. The code considers a beam pipe of constant rectangular cross section 448 with a curvature defined by an arbitrary function of the longitudinal coordinate 449 s. It brings the possibility to simulate CSR with the real disposition of the 450 dipole magnets in a lattice. The code assumes a constant Gaussian bunch in 451 every dimensions. After the geometry defined by the user, an infinite straight 452 section can be added to integrate the CSR fields produced in bends and can 453 take into account additional transient effects.



Figure 12: CSR impedance computed with the parallel plate model  $Z_{PP}$  (steady-state) in red and using CSRZ for a single ThomX ring dipole  $Z_{CSRZ}$ . The real part of the impedance is shown in plain lines and the imaginary part in dotted lines. Parameters: L = 0.2964 m, R = 0.3773 m, h = 28 mm, a = 40 mm.

A ThomX storage ring dipole has been simulated using CSRZ, approximat-455 ing ThomX vacuum chamber with a beam pipe of rectangular cross section with 456 an horizontal dimension of a = 40 mm and a vertical one of h = 28 mm. In fig-457 ure 12, the CSR impedance computed with CSRZ for a single bend in ThomX, 458  $Z_{CSRZ}$ , is compared to the CSR impedance computed using the parallel plate 459 model  $Z_{PP}$ . Both the analytic model and the numerical calculation agree on 460 the frequency value for the CSR threshold, around 11 GHz. Compared to the 461 very smooth impedance of the parallel plate model, the impedance computed 462 using CSRZ shows oscillations corresponding to the resonances of the CSR fields 463 within the rectangular vacuum chamber both in the real and in the imaginary 464 part. The amplitude difference between the curves is due to the transient ef-465 fects which increase the amplitude of the real part and decrease the one of the 466 imaginary part.



Figure 13: CSR wake potential radiated by a Gaussian longitudinal charge density  $\rho$  ( $\sigma_z = 0.5 \,\mathrm{mm}$ ) for a ThomX ring dipole with the parallel plate model  $W_{p,PP}$  and with CSRZ  $W_{p,CSRZ}$ . The head of the bunch corresponds to negative z values and the tail to positive z values.

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The wake potential  $W_{p,CSRZ}$  generated by the  $Z_{CSRZ}$  impedance spectrum 468 for a Gaussian bunch of  $\sigma_z = 0.5 \,\mathrm{mm}$  is shown in Fig. 13. It is compared to the 469 wake potential of the parallel plate model  $W_{p,PP}$ , the amplitude of  $W_{p,CSRZ}$  is 470 slightly more important due to the transient effects. The z < 0 zone is similar 471 for the two wake potentials, which means that the tail-head interaction is not 472 affected by the inner walls of the vacuum chamber in this case. The z > 0 zone is 473 modified compared to the parallel plate case, with a longer wake trailing behind 474 the bunch. This change is brought by the effect of the outer walls, bringing an 475 additional head-tail interaction, and the resonances within the vacuum chamber. 476

The CSRZ simulation has also been performed for multiple bends in order to 477 estimate the effect of the CSR field interference [8]. The interference between the 478 CSR emitted in each bend produces additional oscillations on the real part and 479 imaginary part of the impedance which are amplified as more and more dipoles 480 are added. For the full ring, the impedance spectrum is full of resonant peaks 481 but keeps the same mean amplitude as  $Z_{CSRZ}$ . Unfortunately, this computation 482 is very long, several months of calculation for the full ThomX 18 m ring with 483 a frequency step thin enough to resolve properly these peaks in the impedance 484 spectrum. 485

#### 486 5. Summary and conclusion

An impedance model, for both the geometric wakefields and the coherent synchrotron radiantion (CSR), has been designed for the particular case of ThomX [2, 3], a laser-electron storage rings [1] for X-ray production via Compton backscattering.

The geometric and resistive wall impedance model designed is based on sim-491 ulations of every elements of the storage ring. Then the coaxial wire method 492 has been used to measure prototypes of the storage ring elements to check the 493 simulations. A precise evaluation of the different error sources of these mea-494 surements has been done and highlights the important uncertainty of this type 495 of measurements. Nevertheless, the measurements have allowed to validate the 496 simulations. As the simulation of the kicker impedance was not possible, because 497 of very thin coatings, an analytical model, the multi-layered cylindrical cham-498 ber [23], has been used to evaluate the kicker impedance. The total impedance 499 budget has been presented, corresponding to a loss factor of  $k_{\parallel,T} = 6.73 \,\mathrm{V \, p C^{-1}}$ 500 for a Gaussian bunch of  $\sigma = 2 \text{ mm}$ . To this value, the RF cavity and its tapers 501 contribute for 47 %, the septum chamber for 17 %, the kickers for 12 % and the 502 rest is distributed among the other components of ThomX storage ring. 503

The CSR impedance model has been obtained by simulation of the beam in a rectangular vacuum chamber. It has allowed to take into account transient effects, due to straight sections in between dipoles, and resonances, due to reflections on the beam pipe, using the CSRZ code [14, 43]. The result has been compared with the parallel plate model and has shown the importance of the transient effects and resonances in ThomX dipoles.

These impedance models have been used to extract pseudo wake functions 510 which are used to feed the codes currently used for ThomX beam dynamics stud-511 ies. The analysis of these two models provide important insight on the influence 512 of collective effects in ThomX beam dynamics. The quantity  $Re[Z]|\tilde{\rho}|$  is related 513 to the total energy loss of a bunch of spectrum  $\tilde{\rho}$  due to the impedance Z [30]. 514 This quantity is shown for both impedance models for a short bunch,  $\sigma_s = 2 \text{ mm}$ 515 = 6.6 ps, and for a longer bunch,  $\sigma_s = 6 \text{ mm} = 20 \text{ ps}$ , in Fig. 14. At injection, 516 the bunch corresponds to the short bunch case, for which the dominant effect is 517 the CSR. After some time, the bunch has fully filled the RF bucket due to the 518 filamentation induced by the longitudinal mismatch at injection. For the long 519 bunch obtained, the effect of the CSR is small compared to the geometric and 520 resistive wall wakefields. It confirms that, in ThomX case, simulating the geo-521 metric impedance up to 50 GHz is enough. As, for short bunches for which high 522 frequencies are important, the CSR is the dominant effect. This simple analysis 523 also highlights two distinct regimes for the longitudinal dynamics. A transient 524 regime during which the CSR has a strong impact due both to the injection of 525 a short bunch and to the filamentation [8]. And another regime, which starts 526 after the emittance dilution, which corresponds to the classic potential-well dis-527 tortion. 528

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Figure 14: Plots of the product  $Re[Z]|\tilde{\rho}|^2$  versus the frequency for different bunch length  $\sigma_z$ . The impedance Z corresponds to the CSR impedance of the full storage ring for the red line  $(8 \times Z_{CSRZ}, \text{see Fig. 12})$ . The impedance Z corresponds to the full geometric/RW impedance model, see Fig. 1, for the blue line. The black line shows the modulus squared of the bunch spectrum  $|\tilde{\rho}|^2$  is arbitrary units (arb. unit).

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#### <sup>542</sup> Appendix A. Errors estimate for the coaxial wire measurement

The main source of error in the impedance measurement is due to the S21 measurements, especially the error on the repeatability of the measurements. A bunch of 5 different measurements of each pieces measured have been done to test these bias. After each measurement, the brazing and the tautening of the wire were changed. The typical value for the standard deviation is about  $\sigma_{S21} = 0.4$  dB but it increases with frequency.

As the error is inferred from a small set of repeated measurements, type A uncertainty, a Student t-distribution for the error is assumed [44]. So the standard uncertainty is given by  $u_{S21_M} = \sqrt{\frac{\nu}{\nu-2}}\sigma$ , with  $\nu = N - 1$  degrees of

Variable (Unit)	ErrorTypeProbability distribution		Standard uncertainty $u$
	source		
$S21_{REF/DUT}$ (dB)	Repe <b>at</b> ability	Student	$u_{S_M} = \sqrt{\frac{4}{4-2}}\sigma_{S21} \approx 0.57$ (Variable)
$S21_{REF/DUT}$ (dB)	VNAB	Triangular	$u_{S_C} = \frac{0.2}{\sqrt{6}} \approx 0.082$
,	Cal-		VÜ
	i-		
	bra-		
	tion		
$S21_{REF/DUT}$ (dB)	VNAB	Rectangular	$u_{S_R} = \frac{0.02}{2\sqrt{3}} \approx 0.0082$
	Res-		2 \ 5
	0-		
	lu-		
	tion		
$d \pmod{d}$	ManuBacturing	Gaussian	$u_d = 0.1$
$D_{eq} (\mathrm{mm})$	${ m Mode}Bzation$	Gaussian	$u_D = 0.1$

Table A.4: Sources of errors for impedance measurements. The standard uncertainty for the repeatability of  $S21_{REF/DUT}$  is computed for  $\sigma_{S21} = 0.4$  dB

freedom, N the number of measurement in a set and  $\sigma$  the standard deviation of the measurement set.

Other sources of errors, type B uncertainty, for the S21 measurement are the 554 VNA resolution limit and calibration. The VNA used to do the measurement 555 is an Anritsu MS4624B, last calibration check in a metrology laboratory shown 556 a maximum error of e = 0.2 dB (at -50 dB) when compared to a reference. A 557 triangular distribution of the errors is assumed as this value e is the maximum 558 error and not the most probable error. The resolution limit of the VNA is 559 r = 0.02 dB at maximum. In this case a rectangular distribution of the errors 560 is assumed as all values v are equally likely in  $\left[v - \frac{r}{2}, v + \frac{r}{2}\right]$ . 561

In addition to the error on the S21 measurement there is also an error on the determination of the line impedance  $Z_L$ . The error on the wire diameter dis given by the manufacturer  $u_d = 0.1$  mm. The error for ThomX equivalent diameter  $D_{eq}$  is the fitting error which is about  $u_D = 0.1$  mm. Table A.4 shows the summary of the different error components, their sources and their respective probability distribution.

<sup>568</sup> Using uncertainty propagation on Eq. (1) gives the composed standard un-

certainty of the impedance measurement  $u_Z$  in Eq. (A.1) [44]. The standard uncertainty on the S21 measurement  $u_S$  is given by:  $u_S = u_{S_M} + u_{S_C} + u_{S_R}$ . With  $u_{S_C}$  the standard uncertainty on the calibration,  $u_{S_R}$  the standard uncertainty on the resolution. The standard uncertainty on the repeatability of the measurement  $u_{S_M}$  depends on the object measured and on the frequency considered.

$$u_{Z} = \frac{Z_{v}}{\pi} \sqrt{\ln^{2} \left(\frac{S21_{DUT}}{S21_{REF}}\right) \left(\frac{u_{D}^{2}}{D^{2}} + \frac{u_{d}^{2}}{d^{2}}\right)} + \ln^{2} \left(\frac{D}{d}\right) \left(\frac{u_{S_{DUT}}^{2}}{S21_{DUT}^{2}} + \frac{u_{S_{REF}}^{2}}{S21_{REF}^{2}}\right)}$$
(A.1)

But Eq. (A.1) is not usable in this state as when using uncertainty propagation formulas the standard uncertainties  $u_S$  should be absolute uncertainty. As it is shown in Eq. (A.2) to Eq. (A.4), the absolute uncertainties in dB (with index dB) change into relative uncertainties when changed back in linear scale (with index L). Furthermore the transformation from dB scale to linear scale leads to an asymmetry of the uncertainty boundaries.

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$$S21_{dB} - u_{S_{dB}} < S21_{dB} < S21_{dB} + u_{S_{dB}}$$
(A.2)

$$\frac{S21_L}{u_{S_L}} < S21_L < S21_L u_{S_L} \tag{A.3}$$

$$S21_L + S21_L(\frac{1}{u_{S_L}} - 1) < S21_L < S21_L + S21_L(u_{S_L} - 1)$$
(A.4)

Finally Eq. (A.5) is obtained, in which all the quantities are in linear scale, and gives the upper and lower composed standard uncertainties. For example if the transmission parameter S21 for the reference is measured at -10 dB, for the DUT at -15 dB and that both measurements have a standard deviation of  $\sigma_{S21} = 0.4$  dB at this frequency point then the impedance measured is Z = $237^{+49}_{-46} \Omega$ . In that case, 98 % of the uncertainty on the impedance is due to the uncertainty on S21 measurements and 2 % on the line impedance  $Z_L$ .

$$u_{Z}^{\pm} = \frac{Z_{v}}{\pi} \sqrt{\ln^{2} \left(\frac{S21_{DUT}}{S21_{REF}}\right) \left(\frac{u_{D}^{2}}{D^{2}} + \frac{u_{d}^{2}}{d^{2}}\right)} + \ln^{2} \left(\frac{D}{d}\right) \left(u_{DUT}^{\pm} + u_{REF}^{\pm}\right)^{2}}$$
(A.5)

$$u^{+} = u_{S_{L}} - 1 \tag{A.6}$$

$$u^{-} = \frac{1}{u_{S_{I}}} - 1 \tag{A.7}$$

All measurement results are shown with their 95 % confidence interval (CI) corresponding to the extended uncertainty using Student coefficient k = 2.78(N = 5). In the case of the previous example, the extended uncertainties to 95 % CI gives  $Z = 237^{+137}_{-127} \Omega$ . The important uncertainty found comfort us in the idea that this measurement should only be used to validate the simulation tools and methods.

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