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Monitoring the Greater Agulhas Current with AIS Data Information

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Key Points:

- The high density of vessel traffic and associated AIS messages provide means to derive the oceanic surface current.
- A two-step strategy is applied with a first guess obtained from the collective behavior of vessels in a given space-time interval.
- Ocean currents along vessel trajectories are then re-analyzed and interpolated before being projected onto a regular grid.
- An Helmholtz-Hodge decomposition of the obtained optimally interpolated field is performed
- In the core of the Greater Agulhas Current, analysis confirms that interpolated altimeter-derived estimates largely underestimate actual surface current velocities.

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Abstract

Over the core region of the Agulhas Current, new estimations of ocean surface velocities are reported using the increasing dataset from the Automatic Identification System (AIS), initially designed to monitor vessel traffic. A two-step strategy is suggested. A first guess is evaluated from the collective behavior of vessels for a given space-time interval. Individual vessel trajectories are then re-analyzed and interpolated. Applied during year 2016, these ocean surface current estimates are demonstrated to well determine the intensity of surface currents. The improved spatial resolution helps the decomposition of the optimally interpolated surface current vector field between irrotational and divergence-free component, e.g. Helmholtz-Hodge decomposition. Comparisons are performed between *in-situ* drifting-buoys and data collected during the ACT experiment (Agulhas Current Time-series), as well as mean Doppler-derived surface currents obtained from satellite synthetic aperture radar (SAR) measurements. Comparisons with the Sea Surface Temperature from MODIS sensors confirm the occurrence of meandering events for the current path. For the Agulhas Current region, the high density of vessel traffic can provide new means to study and monitor intense upper ocean currents with more detailed resolution and precision.

Plain Language Summary

Today, for security reasons, merchant ships transmit location, speed, heading and course-over-ground information through the Automatic Identification System (AIS). These messages are a new source of information to complement ocean surface current measurements. In this paper, the intense traffic off the South African coast can result in a selection of more than 150 ships per day. Daily analyses and correlations are reported and illustrate links with observed changes in sea surface temperature. In view of the existing need to establish a more comprehensive monitoring system for the Agulhas Current, these results encourage the systematic usage of the increasingly available amount of AIS data as complementary to traditional *in situ* and altimeter measurements for routine quantitative monitoring of heat and mass transport in this region.

1 Introduction

Before the altimetry era, ocean surface current estimates were based on the logs of both military and merchant ships [Richardson and McKee, 1984; Richardson and Walsh, 1986; Richardson and Reverdin, 1987]. Indeed, in the presence of intense currents, ships may be pushed off-course and their speed be modified. Subtracting the predicted vector, based on dead reckoning, from the vector representing the ship's actual speed and direction, surface current estimates can then be derived. This method may have lacked accurate positioning and time sampling. However, precision in geo-positioning has been largely improved. Moreover, today, merchant ships systematically transmit their position, bearing and speed through AIS messages, increasing the number of estimates. Early studies have shown the relevance of using AIS information and ship trajectory analysis to estimate surface currents [Guichoux, 2015; van der Neut, 2016]. Some comparisons between high-frequency radar (HFR) measurements and AIS-derived surface currents have shown excellent concordance, particularly over tidal currents in coastal regions. These first efforts also revealed capabilities to detect mesoscale structures such as eddies and filaments in the Sicily Channel, Italy [Guichoux *et al.*, 2016]. [Inazu *et al.*, 2018] also exploited AIS data messages to reveal the presence of a passing tsunami event, further demonstrating that associated AIS derived currents quantitatively captured the speed of the tsunami's current. Accordingly, AIS data messages can thus provide opportune new sources of information to complement and improve current ocean observation systems.

In certain oceanic regions, i.e., off the South African coast, marine traffic is so intense that data from more than 150 ships can be used each day. As discussed in the

73 present paper, such a wealth of information can be combined with all available *a priori*
 74 surface current estimates, particularly those derived from satellite altimetry and drifting-
 75 buoys, in order to develop an improved spatio-temporal surface current monitoring system.

76 The present demonstration focuses on the northern part of the Agulhas Current,
 77 between 32° S and 36° S, where marine traffic is most intense all year round. The flow,
 78 along the eastern coast of South Africa, is steered by and essentially follows the very steep
 79 continental shelf break. In this core part of the current, surface velocities up to 2 ms^{-1} are
 80 commonly reported [Bryden *et al.*, 2005] and likely impact ship trajectories. Such extreme
 81 values are generally not reported in interpolated gridded fields from altimeters. Besides
 82 inherent smoothing induced by the interpolation of sparse satellite measurements, this un-
 83 derestimation of current velocities may also be due to the presence of non-geostrophic
 84 components of the real current [Beal and Donohue, 2013; Krug *et al.*, 2018].

85 In the present study we developed a methodology in 2 steps. The first consisted
 86 in calculating a first guess of the oceanic surface current. As explained in section 2, as-
 87 suming that all vessels, within a given space-time interval, encounter the same sea sur-
 88 face conditions, a surface current estimate can be found as the solution of a linear sys-
 89 tem. However this method suffers from large errors. We therefore filtered the data using
 90 physical considerations regarding the variance of the different velocities associated to each
 91 vessel. This first method requires a substantial number of AIS messages from different
 92 vessels to converge. We considered this result our first guess. In the second step, we filled
 93 in the gaps inherent to this first method by returning to the vessels' individual data over
 94 time and interpolating their navigation characteristics. We then provided the associated
 95 currents along the vessel trajectories, correcting the first guess and projected them on to a
 96 regular grid. We consider these fields our second guess. Finally, we applied an optimal in-
 97 terpolation to fulfill the gaps of the regular grid. The improved spatial resolution helps the
 98 application of the Helmholtz-Hodge decomposition between rotational- and divergence-
 99 free components.

100 *In-situ* and remote sensing data used for the validation of the derived surface current
 101 field are presented in section 3. Results are presented and discussed in section 4.

102 2 Data and Methods

103 2.1 AIS Messages

104 In the Agulhas current, marine traffic is particularly intense. In 2016, off the coast
 105 of Port Elisabeth, 23° E- 29° E and 32° S- 36° S, up to 1000 vessels transmitted their AIS
 106 messages each day. Messages are obtained from ORBCOMM and gathered using satel-
 107 lites. These messages include static and dynamic information. The static information in-
 108 cludes the MMSI (Maritime Mobile Service Identity), the ship's name and type, its length
 109 and its draft. The dynamic information includes longitude/latitude, speed over ground
 110 (SOG), course over ground (COG) and the ship's heading (true heading or TH). It must
 111 be noted that, the emission period of the AIS messages is around 10 seconds and the sam-
 112 pling rate of the data obtained from Satellite AIS is around a few minutes.

113 However, all messages may not be useful. Indeed, all vessels do not necessarily
 114 have a continuous course over ground, or are simply not in transit, (e.g., fishing vessels).
 115 Thus, from the reported trajectories and speeds, only messages corresponding to vessels in
 116 transit were kept. To illustrate data availability, the mean daily number of AIS messages,
 117 per 0.125° square box, is shown in figure 1 (a). We can clearly see that marine traffic fol-
 118 lows the coast closely, at a maximal distance of around 100 kilometers. At its peak inten-
 119 sity, the mean number of AIS data messages per grid cell and per day can be as high as
 120 180 for approximately 15 vessels (figures 1 (a) and (b)).

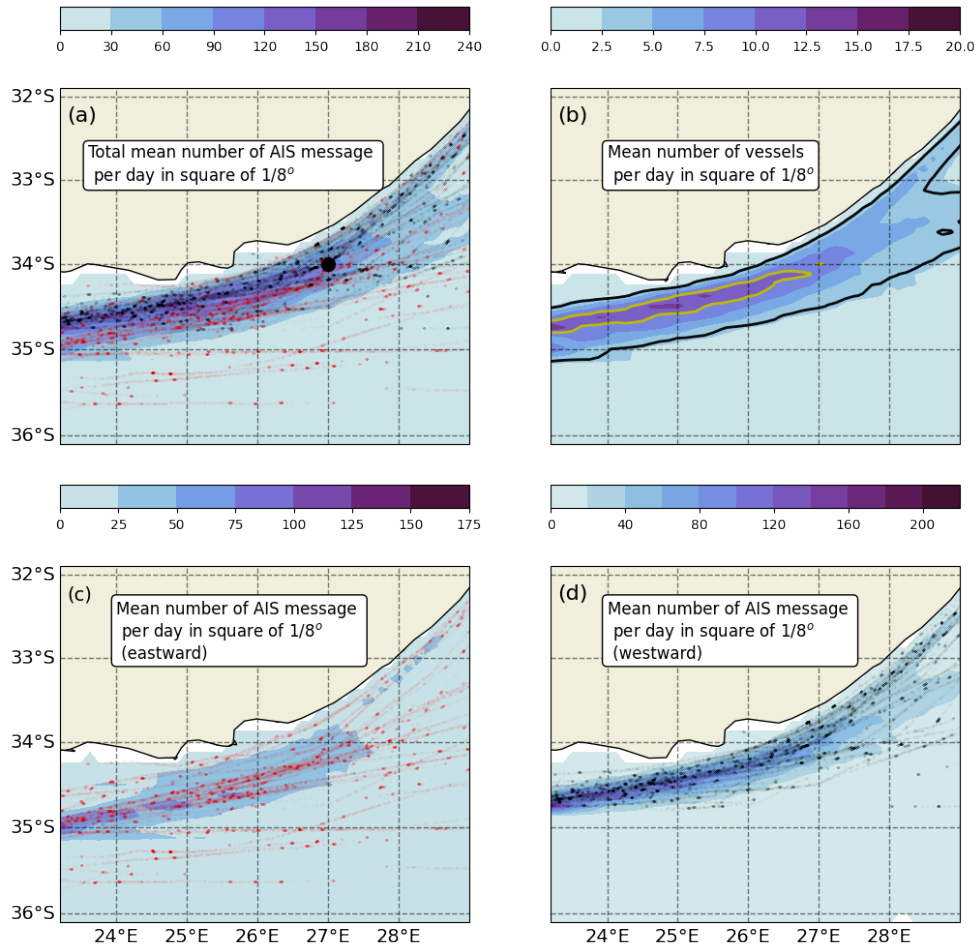


Figure 1: Mean daily number of AIS related messages in a grid of 0.125° . (a) Total number of AIS messages. (b) Total number of vessels. (c) Number of AIS messages related to Eastward bound vessels. Trajectories are represented by a red dot and correspond to a given day. (d) Same as (c) but for Westward bound vessels. Trajectories are represented in black. The dot corresponds to the location where maritime traffic and wind were analysed (see figure 4).

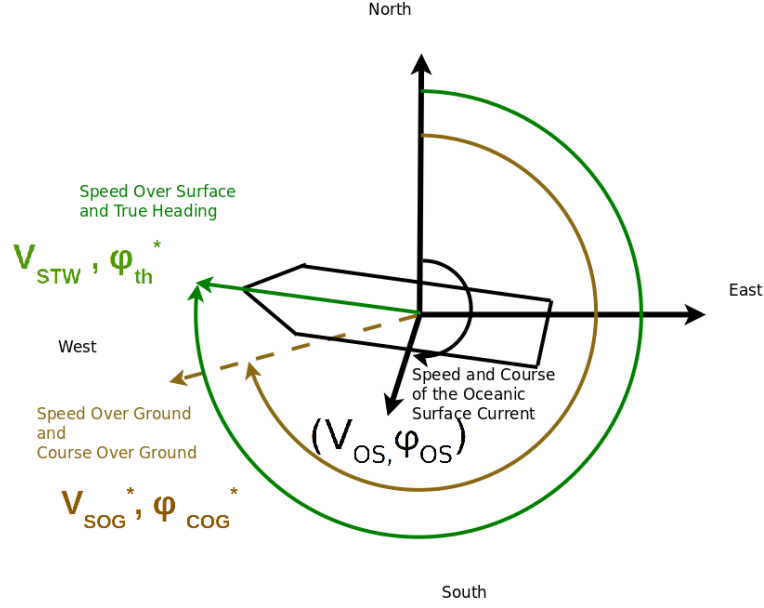


Figure 2: Measurement diagram and definitions. Variables with an asterisk are known and transmitted via the AIS message. The other variables are calculated. When projected over the zonal and meridional axes V_{OS} and φ_{OS} become u_{os} and v_{os} .

121 As also illustrated in figure 1, ships in transit generally follow straight lines between two way points. In the presence of sea surface currents, the true heading (direction pointed to by the vessel) then adjusts to best follow the prescribed route. The vocabulary and a diagram are presented in figure 2. As a basic principle, the composition of the different velocity vectors is given by:

$$\overrightarrow{V_{Boat/Ground}} = \overrightarrow{V_{Boat/Sea}} + \overrightarrow{V_{Sea/Ground}} \quad (1)$$

126 $\overrightarrow{V_{Boat/Ground}}$ is measured using the ground distance traveled during a fixed time, with its associated magnitude (SOG) and direction (COG) provided in the AIS message.
 127 $\overrightarrow{V_{Boat/Sea}}$ is the vector velocity of the boat relative to the sea surface, with its associated direction (TH) also provided in the AIS message. The magnitude of $\overrightarrow{V_{Boat/Sea}}$ stays unknown. As such, $\overrightarrow{V_{Sea/Ground}}$ is a completely unknown oceanic surface current vector. By
 128 projection, in this case on the horizontal and vertical axes associated with the zonal and meridional velocity components, we obtain two equations and three unknown variables
 129 (i.e., direction and magnitude of the oceanic current and magnitude of the boat's speed relative to the sea):

$$\begin{cases} V_{sog}^* \sin(\varphi_{cog}^*) = V_{stw} \sin(\varphi_{th}^*) + u_{os} & \text{(zonal)} \\ V_{sog}^* \cos(\varphi_{cog}^*) = V_{stw} \cos(\varphi_{th}^*) + v_{os} & \text{(meridional)} \end{cases} \quad (2)$$

135 For each AIS data message, V_{sog} is the speed over ground, φ_{cog} the course over ground, V_{stw} the speed through water and φ_{th} the true heading of each ship considered. u_{os} and v_{os} represent the zonal and meridional component of the ocean surface current. As in figure 2, the asterisk indicates variables obtained from the AIS messages.

139 It is important to note that all basic assumptions are valid so long as the equation of motion of the vessel yields to $m \frac{dv}{dt} \approx 0$. This also helps with discarding stormy
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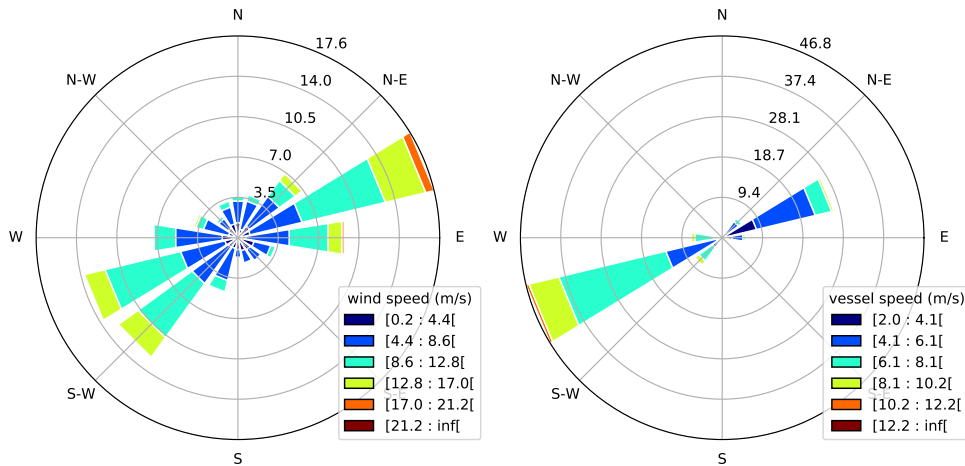


Figure 3: (a) ECMWF wind rose diagram at point ($27^{\circ}\text{E}, 34^{\circ}\text{S}$), located in the Agulhas current. (b) Wind rose diagram showing the mean direction and speed of vessels travelling with the flow (South-westerly) and against the flow (North-easterly) for all vessels located inside a square 0.5° around coordinates ($27^{\circ}\text{E}, 34^{\circ}\text{S}$).

141 weather conditions or maneuvering operations. In [Inazu *et al.*, 2018], the characteris-
 142 tic time response of the vessel was estimated to be around 40 to 120 s. This timescale is
 143 small compared to the timescale of the oceanic surface current. For this reason, comput-
 144 ing the oceanic current seems feasible as long as the motion of the vessel reaches a steady
 145 state, as we will further see.

146 2.1.1 Impact of the wind - Leeway Drift

147 Wind directions in the Agulhas typically flip between SW and NE as shown in fig-
 148 ure 3 (a) for the year 2016, in a region located near the longitude latitude point ($27^{\circ}, -34^{\circ}$).
 149 The wind data was obtained from the ECMWF ERA-Interim reanalysis product available
 150 at <http://apps.ecmwf.int/datasets/>. For the same area, the mean direction and the mean
 151 speed of the vessels in transit for both destinations (Indian or Atlantic Ocean) are reported
 152 in figure 3 (b). The wind is likely to affect vessel speed through water by blowing either
 153 from the front or from behind. The vessel may thus accelerate or decelerate rather than
 154 being pushed off course (no lateral effect). Strong winds with an orientation perpendicu-
 155 lar to the course of the boat could modify the true heading thus hindering surface current
 156 estimations. However, considering a standard boat, Richardson [Richardson, 1997] demon-
 157 strated that the wind-induced drift is small compared to that of the oceanic current. The
 158 leeway drift of a boat enduring complete lateral wind of magnitude 6ms^{-1} would amount
 159 to around 3.5cms^{-1} , only 0.6% of the wind's magnitude. The fact that the wind is not
 160 always lateral further weakens this percentage. Given the results of these analyses, the lee-
 161 way drift is not considered in the present evaluation in the Agulhas region. Nevertheless,
 162 the wind does play a crucial role in vessel behavior in an indirect manner, as further ex-
 163 plained below.

164 2.2 First guess calculation of the oceanic surface current

165 2.2.1 Linear system

166 Vessels and associated AIS messages, are first considered to be in homogeneous
 167 surface conditions in both space and time. Given that solving the linear system requires

168 a sufficient amount of data, the AIS messages are aggregated within 3 different spatio-
 169 temporal boxes. Figure 1(b) shows black and yellow contours corresponding to densities
 170 of 3 and 10 vessels per day, per $1/8^\circ$ square box, respectively. For densities superior to
 171 10, we considered cells of $1/8^\circ \times 1/8^\circ$ over a 1-day period. For densities between 3 and
 172 10, we changed this time interval to a 3-day period and for densities inferior to 3, we con-
 173 sidered cells of $1/4^\circ \times 1/4^\circ$ within a 5-day period. For each AIS message, we have two
 174 equations and three unknowns, the magnitude of V_{stw} and the two current components.
 175 For n AIS messages, we therefore have $2n$ equations. However, using the space-time ho-
 176 mogeneity assumption, this leaves only $n+2$ unknowns to be solved. The following system
 177 is thus considered:

$$\begin{cases} V_{sog_1}^* \sin(\varphi_{cog_1}^*) = V_{stw_1} \sin(\varphi_{TH_1}^*) & +u_{os} \\ V_{sog_1}^* \cos(\varphi_{cog_1}^*) = V_{stw_1} \cos(\varphi_{TH_1}^*) & +v_{os} \\ \vdots & \vdots \\ V_{sog_n}^* \sin(\varphi_{cog_n}^*) = V_{stw_n} \sin(\varphi_{TH_n}^*) & +u_{os} \\ V_{sog_n}^* \cos(\varphi_{cog_n}^*) = V_{stw_n} \cos(\varphi_{TH_n}^*) & +v_{os} \end{cases} \quad (3)$$

178 Although seemingly overdetermined, this system still requires a significant number of AIS
 179 messages and suffers from almost three sources of error. To illustrate the main source of
 180 error, we can write the equation to be solved as follows:

$$Ax = b \quad (4)$$

181 with A being the matrix to invert in order to calculate the oceanic surface current such as:

$$A = \begin{pmatrix} 1 & 0 & \sin(\varphi_{TH_1}^*) & 0 & \dots & 0 \\ 0 & 1 & \cos(\varphi_{TH_1}^*) & 0 & \dots & 0 \\ \vdots & \vdots & & \ddots & & \\ 1 & 0 & 0 & \dots & 0 & \sin(\varphi_{TH_n}^*) \\ 0 & 1 & 0 & \dots & 0 & \cos(\varphi_{TH_n}^*) \end{pmatrix}, x = \begin{pmatrix} u_{os} \\ v_{os} \\ V_{stw_1} \\ \vdots \\ V_{stw_n} \end{pmatrix}, b = \begin{pmatrix} V_{sog_1}^* \sin(\varphi_{cog_1}^*) \\ V_{sog_1}^* \cos(\varphi_{cog_1}^*) \\ \vdots \\ V_{sog_n}^* \sin(\varphi_{cog_n}^*) \\ V_{sog_n}^* \cos(\varphi_{cog_n}^*) \end{pmatrix} \quad (5)$$

182 where A and b correspond to the observations and x corresponds to the unknowns. Con-
 183 sidering matrix A, one may note a particular case in which all the vessel headings (φ_{TH_i})
 184 are similar or equal. Mathematically this would correspond to a badly conditioned matrix
 185 and a solution to this system would be difficult to obtain. In practice, it would correspond
 186 to an area where all the vessels have approximately the same true heading. This situa-
 187 tion is clearly illustrated in figures 1 (c) and (d) where the densities of the AIS messages
 188 from vessels going westwards and vessels going eastwards are plotted separately. It may
 189 be noted that in the north-eastern part, there is no preferred maritime route. This leads to
 190 diverse headings for the different vessels and facilitates the calculation of the current by
 191 inverting the linear system 3. Nevertheless, considering the south-western part, traffic is
 192 far more organized and we can easily identify three lanes of traffic. Clearly, the diversity
 193 of vessel headings is small in these areas and a solution of the system 3 may lead to con-
 194 siderable errors. More detailed explanations are provided in the supporting information
 195 S1. For this same reason, we only invert the system when a minimum of three vessels are
 196 present inside our spatio-temporal cell. Indeed, if such is the case, the redundancy of the
 197 heading concerning a unique vessel is high and does not allow for a successful inversion
 198 of the system.

199 Although a badly conditioned matrix may be considered a major source of error in
 200 our investigation, additional sources are traffic density and bad weather conditions. Stormy
 201 weather impacts the fluctuation of the variables provided by the the AIS data messages,
 202 preventing the system from finding a correct solution.

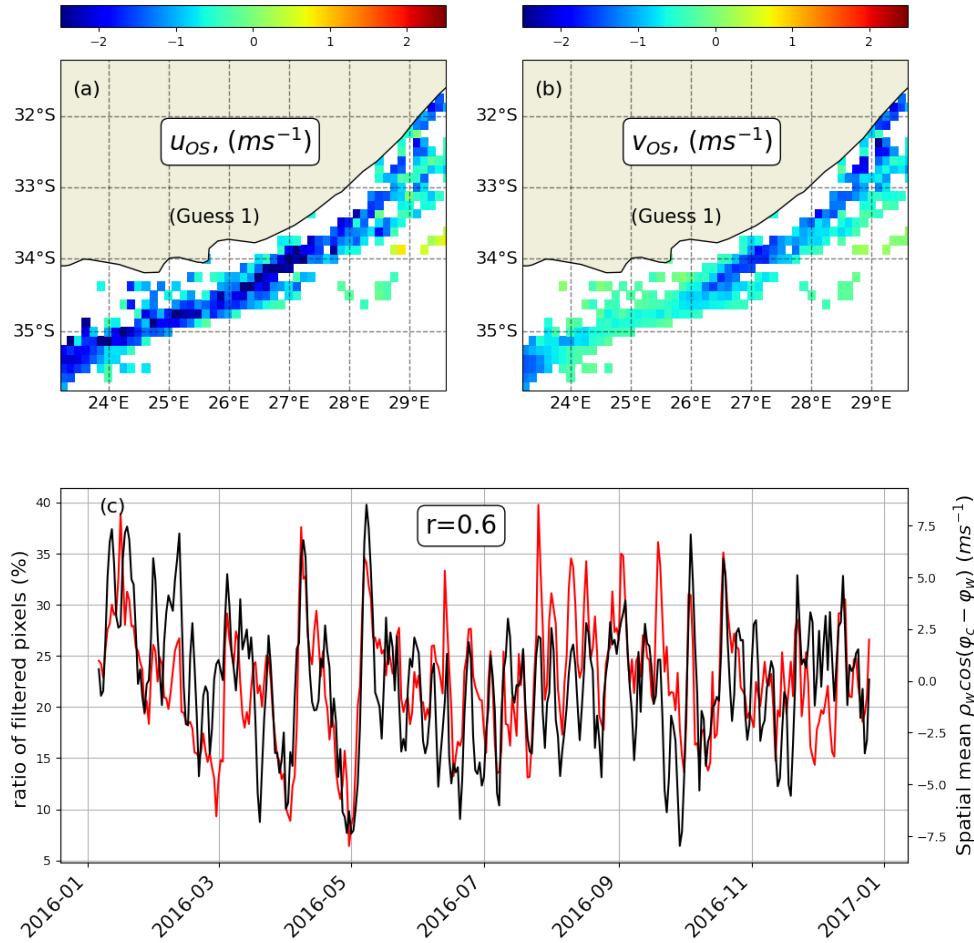


Figure 4: Maps of the filtered oceanic surface current for (a) the zonal component and (b) the meridional component for January 16th, 2016. (c) In black, percentage of the number of filtered boxes over the total number of boxes as a function of time (day). In red, the mean scalar product of the wind and geostrophic ocean current as a function of time (day).

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2.2.2 Filtering

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Direct calculation of surface currents thus leads to considerable errors. An example of the direct estimates found by solving the linear system and explanations are given in the supporting information S1. To improve the results we used additional information regarding the speed through water (V_{stw}), also obtained when solving the linear system. The idea of this filtering technique is to consider each result associated to each spatio-temporal box (pixel) and to assign a binary quality index to it. The technical details are given in supporting information S2.

Figure 4 shows the pixels with a good quality index, the maps (a) and (b) correspond to the zonal and the meridional oceanic surface components. Figure 4 (c) indicates the amount of points retained, i.e., the ratio between the number of pixels with a good quality index over the total number of pixels for which a calculation was carried out. By repeating this operation for each day, we obtained a corresponding time-series. To qualify the main variability of the signal we calculated the mean magnitude of the wind in the direction of the geostrophic current (averaged over the whole domain). In polar coor-

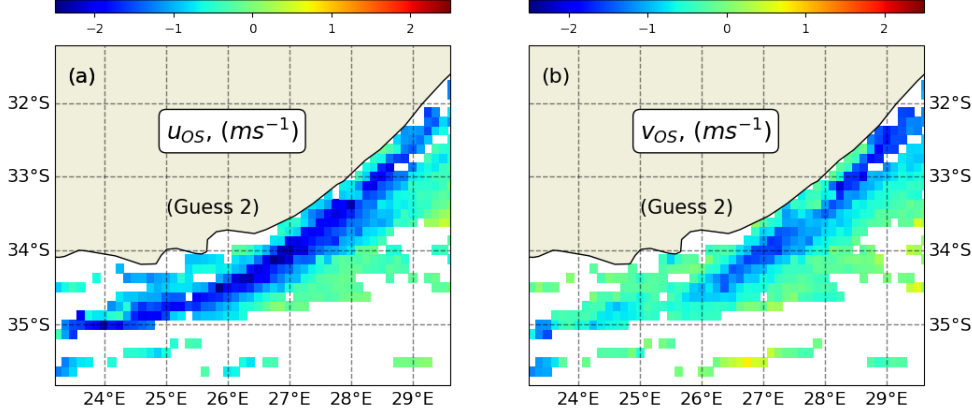


Figure 5: Second guess of the zonal (a) and meridional (b) components of the oceanic surface current for January 16th, 2016.

218 dinates this term corresponds to $\rho_w \cos(\varphi_c - \varphi_w)$, ρ_w being the magnitude of the wind,
 219 φ_c and φ_w being the direction of the current and wind respectively. In figure 4 (c), we
 220 clearly note the significant correlation between the two signals $r = 0.6$. This result indi-
 221 cates that our filter, explained above, successfully discards environmental conditions
 222 such as stormy weather, that interact with the current. Indeed, the situation in which the
 223 wind blows against the current is known to cause very difficult sea conditions for ves-
 224 sels and quite logically prevents calculation of the oceanic current. Other sources of error
 225 may come from the refraction of the waves by the current which leads to large amplifica-
 226 tion of the significant wave height [Quilfen et al., 2018; Ardhuin et al., 2017; Quilfen and
 227 Chapron, 2018; Kudryavtsev et al., 2017a].

228 2.3 Second guess calculation of the oceanic surface current

229 A first guess of the oceanic surface current gathers information shared by the ves-
 230 sels within a given space-time interval. This method involves the aggregation of data, thus
 231 lowering the spatial and temporal resolution. Moreover, while our filtering technique based
 232 on the variance of the different speeds V_{sog} and V_{stw} of the vessels enables us to better
 233 discard outliers, one can easily observe on figures 4 (a) and (b) that the results and the
 234 corresponding maps still exhibit notable noise levels. To improve the first-guess estimates,
 235 the basic idea consists in regularising and augmenting the spatio-temporal resolution using
 236 the time continuity of the vessels' speed through water. To do so, we consider the vessels
 237 along their entire journey and collect all their calculated speeds though water obtained by
 238 solving the system 3.

239 2.3.1 Filtering the speed through water

240 Having obtained the time-series of the speed through water, we then filter our results
 241 using the Empirical Mode Decomposition. For this, we only keep the trend of the EMD
 242 [Huang et al. [1998]; Kopsinis and McLaughlin [2009];). From this filtered estimate of
 243 speed through water we then use the set of equations 2 and calculate the zonal and merid-
 244 ional components of the oceanic surface current as follows:

$$\begin{cases} u_{os} = \mathcal{F}(V_{stw})\sin(\varphi_{TH}) - V_{sog}\sin(\varphi_{cog}) & \text{(Zonal Guess 2)} \\ v_{os} = \mathcal{F}(V_{stw})\cos(\varphi_{TH}) - V_{sog}\cos(\varphi_{cog}) & \text{(Meridional Guess 2)} \end{cases} \quad (6)$$

245 where $\mathcal{F}(V_{stw})$ represents the filter for the speed through water. Examples and more de-
 246 tailed explanations are given in the supporting information S3.

247 2.3.2 Results of the second guess

248 The results obtained from the second guess are illustrated in figure 5 where the
 249 zonal (a) and the meridional (b) velocities are plotted on the map for the same day as
 250 for the first guess, i.e., January 16th 2016. As expected, the global spatial coverage is
 251 higher as the individual information for each vessel is now used systematically to infer
 252 the oceanic surface current. As previously mentioned, this method is not accurate every
 253 time and everywhere and, essentially, is incorrect when the wind blows against the current
 254 (figure 5). Before projecting the estimates from the daily available vessels onto the same
 255 regular grid as done previously, we thus select the periods when the wind was not blowing
 256 against the current, i.e., when $\rho_w \cos(\varphi_c - \varphi_w) > 0$. Where φ_c and φ_w are the direction of
 257 the current and wind and ρ_w is the wind magnitude.

258 2.4 Optimal interpolation

259 Once a clean dataset obtained for both the zonal and the meridional velocity com-
 260 ponents, we apply a classic optimal interpolation in order to smooth and map the results
 261 in space and time [Bretherton *et al.*, 1976]. The results of the interpolations are Gaussian,
 262 defined by their mean fields u_{os}^s, v_{os}^s , and associated covariance $P_{u_{os}^s}^s, P_{v_{os}^s}^s$. Here, the in-
 263 dex s indicates the smoothing results (i.e., the interpolation using all available data along a
 264 given region and time period).

265 Optimal interpolation is a mathematical tool used to merge background information
 266 (x^b) from *a priori* knowledge, in this case, the annual average of the zonal and meridional
 267 current estimates and observations (y). The result of the optimal interpolation is Gaussian
 268 with a mean x^s and a covariance P^s given by:

$$\begin{aligned} x^s &= x^b + K(y - Hx^b), \\ P^s &= B - KHB, \end{aligned} \quad (7)$$

$$\text{with the gain } K = BH^T (HBH^T + R)^{-1},$$

269 where H is the observation operator, thus creating the link between the observation and
 270 the background. Here, H is the identity matrix.

271 The background B and observation R covariances defined in Eq. (7) significantly im-
 272 pact the interpolation results and consequently must be estimated. These two covariances
 273 depend on important parameters: noise levels and spatio-temporal correlation lengths. Vari-
 274 ograms are classic statistical tools used to estimate these parameters from available mea-
 275 surements [Tandeo *et al.*, 2014]. The variograms were calculated empirically in both space
 276 and time and results are shown in figure 6. We then fitted the empirical variograms using
 277 an exponential spatio-temporal shape, defined by:

$$\gamma(\Delta_s, \Delta_t) = R + \sigma^2 \left(1 - \exp\left(-\frac{\Delta_s}{L}\right) \exp\left(-\frac{\Delta_t}{T}\right) \right) \quad (8)$$

278 where R corresponds to the observation error variance, σ^2 to the stationary variance of
 279 the process, L to the spatial correlation length, and T to the temporal correlation length.
 280 The fitted variograms using the formula given in Eq. (8) are also shown in figure 6. The
 281 variance parameters, for both zonal and meridional components of the current, are $R_u =$
 282 0.1 and $R_v = 0.05$ for the observation variance, $\sigma_u = 0.4$ and $\sigma_v = 0.25$ for the sta-
 283 tionary variance. The correlation lengths were equal for two components of the current,
 284 $L_u = L_v = 0.6$ degrees for space, and $T_u = T_v = 20$ days for time. These correlation
 285 length values are consistent with those normally used in the interpolation of altimeter data
 286 [Le Traon *et al.*, 1998].

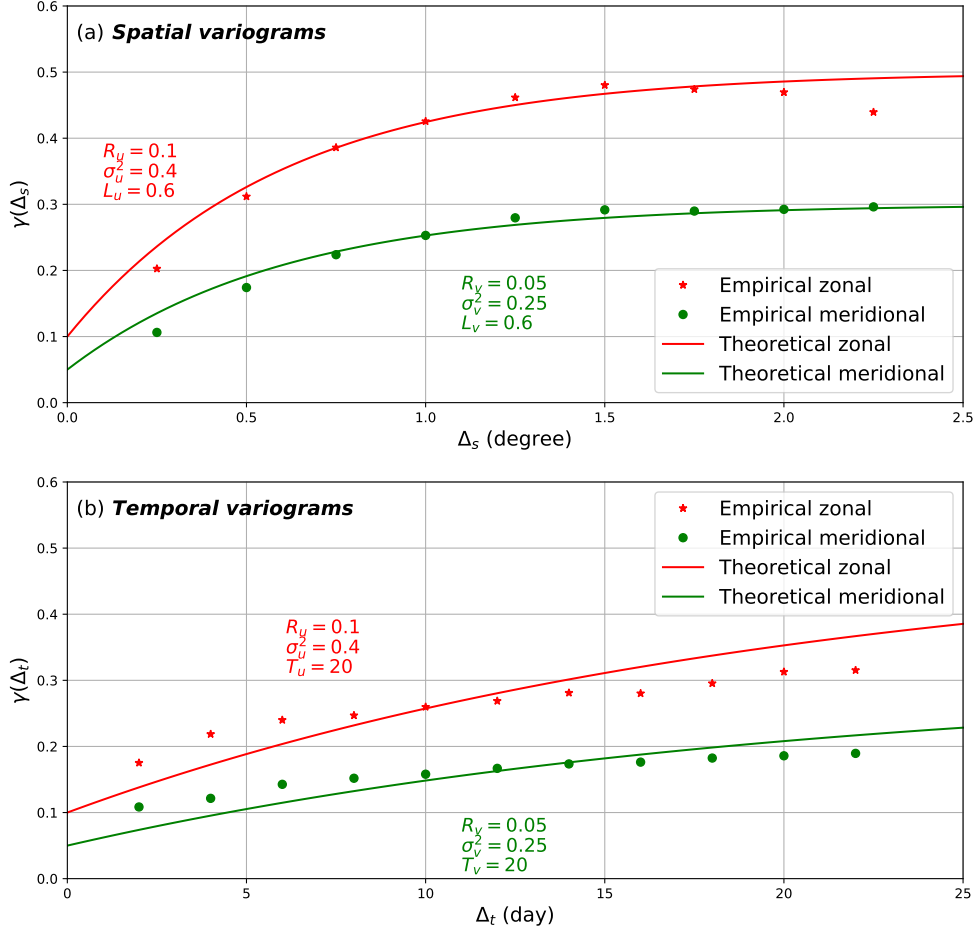


Figure 6: (a) Empirical and theoretical spatial variograms of the zonal and meridional current components. (b) Corresponding temporal variograms.

287 The corresponding optimally interpolated fields of the zonal and meridional components of the oceanic current are presented in figures 7 (a) and (b). The associated square root covariances $\sqrt{P_{u_{os}}^s}$, $\sqrt{P_{v_{os}}^s}$ are presented in figures 7 (c) and (d). These terms can be considered estimates of the errors associated to optimal interpolation. Not surprisingly, we note that these maps are very similar to those of maritime traffic presented in figure 1.

292 2.5 Helmholtz-Hodge decomposition of the optimally interpolated field

293 Oceanic currents are the result of different physical mechanisms at different scales. Among these are differences in sea level (Geostrophy balance), wind (Ekman transport) and waves (Stoke Drift) etc. While a geostrophy balance leads to a divergent-free flow, this is generally not the case for the other mechanisms and their interactions. Moreover, ocean flow is always considered incompressible which means that the divergence obtained from the analysis of the oceanic surface flow must be related to the vertical motion of the ocean, and more generally to ageostrophic processes. In order to study and identify these different physical mechanisms, we can use the Helmholtz-Hodges decomposition, briefly described here. This decomposition describes the flow as the sum of rotation-free, divergent-free and harmonic vector fields. Considering a smooth vector field $\vec{\xi}$ as the re-

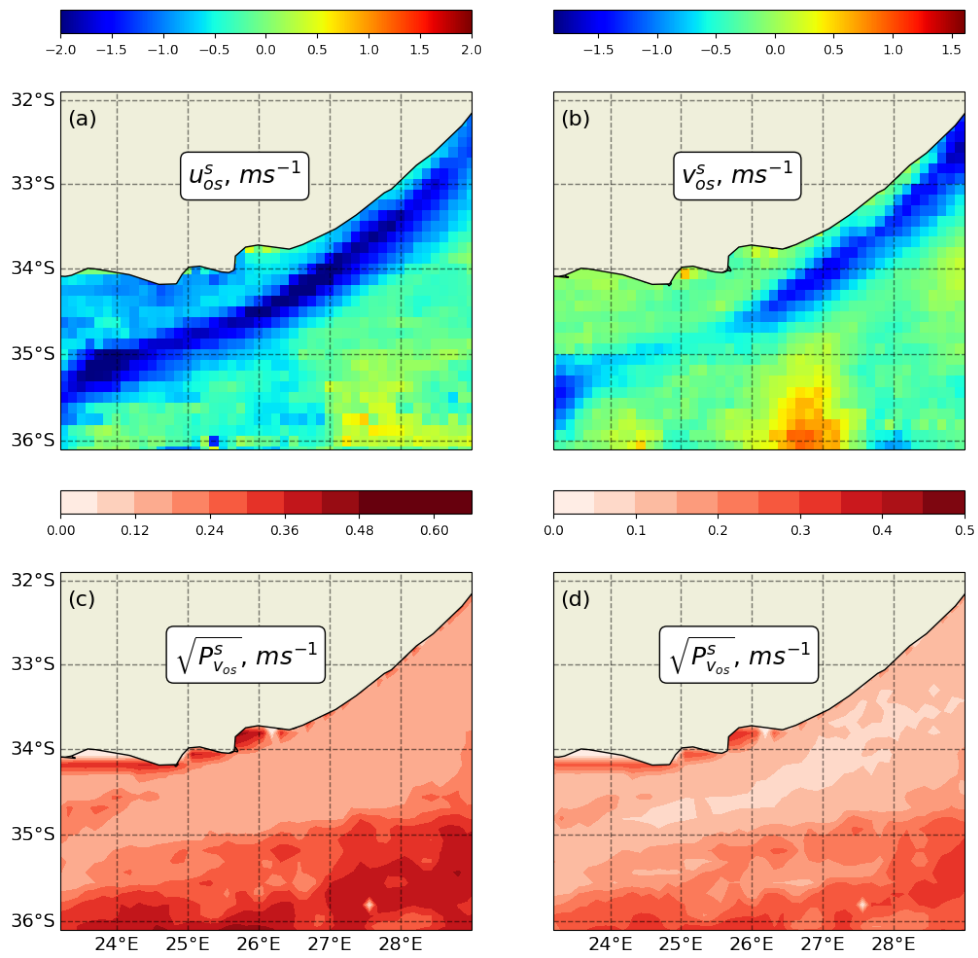


Figure 7: Zonal (a) and meridional (b) oceanic surface current components obtained from the optimal interpolation for January 16th, 2016. (c) and (d) show the covariances associated to the zonal and meridional means respectively

303 sult of the optimally interpolated fields then,

$$\vec{\xi} = \vec{r} + \vec{d} + \vec{h} \quad (9)$$

304 where \vec{r} is the divergent-free ($\nabla \cdot \vec{r} = 0$), \vec{d} is the rotation-free ($\nabla \times \vec{d} = 0$) and \vec{h} is harmonic
305 ($\nabla \times \vec{h} = 0$ and $\nabla \cdot \vec{h} = 0$). This leads to the following equations:

$$\nabla \cdot \vec{d} = \nabla \cdot \vec{\xi} \quad (10)$$

$$\nabla \times \vec{r} = \nabla \times \vec{\xi} \quad (11)$$

306 When substituting $d = \nabla D$ and $\vec{r} = \nabla \times \vec{R}$ the above equations become two Poisson's equa-
307 tions. Nevertheless, the above system is under-specified, given that for any harmonic flow
308 added to the solution, the resulting sum is still a solution. This raises the problem of the
309 uniqueness of the solution when the domain is bound (in an infinite domain the harmonic
310 flow disappears). Most related studies use the NP (Normal parallel) boundary conditions
311 which forces the rotational (divergent) flow to be normal (parallel) to the boundaries.
312 Here, we used the so-called Natural Helmholtz-Hodges Decomposition (nHHD)[*Bhatia*
313 *et al.*, 2014]. The basic idea is to consider the domain under external and internal influ-
314 ences. As such, the rotational and divergent flows are under the internal influences (in the
315 domain) and the harmonic flow is under the external influence (at the boundaries). An
316 advantage of applying this method is the non-use of boundary conditions to obtain the
317 uniqueness of the solution. The sole limitation of the nHHD is that it is not guaranteed to
318 be L2-orthogonal between the divergent, d and the rotational, r flows. For visualization
319 and analysis this property is not required. Further details and explanations are provided
320 in [*Bhatia et al.*, 2014]. The subscripts ξ , r and d refer to the optimal velocity field, the
321 divergent-free flow field and the rotational-free flow field.

322 3 Validation data

323 3.1 Remote Sensing

324 3.1.1 Geostrophic velocity gridded field and Along-Track altimetry

325 The geostrophic velocities are derived from the altimeter products, using both the
326 gridded geostrophic velocity and the Along-Track estimates.

327 For the gridded geostrophic velocity, we used the SLA (Sea Level Anomaly) ob-
328 tained through the altimeter-gridded products, [http://marine.copernicus.eu/services-portfolio/](http://marine.copernicus.eu/services-portfolio/access-to-product)
329 [access-to-product](http://marine.copernicus.eu/services-portfolio/access-to-product) together with the new Mean Dynamic Topography called MDT_CNES-CLS18
330 available at [https://www.aviso.altimetry.fr/en/data/products/auxiliary-products/](https://www.aviso.altimetry.fr/en/data/products/auxiliary-products/mdt.html)
331 [mdt.html](https://www.aviso.altimetry.fr/en/data/products/auxiliary-products/mdt.html). The new MDT is derived from the CNES-CLS15 MSS, the GOCO05S geoid
332 model together with the latest versions of altimetric (for the period 1993-2012) and *in-situ*
333 data. The spatial resolution is $1/8^\circ$. As the SLA is available at $1/4^\circ$, we linearly interpo-
334 lated the SLA to $1/8^\circ$ in order to calculate the current under the geostrophic approxima-
335 tion.

$$u_{geo} = -\frac{g}{f} \frac{\delta(SLA + MDT)}{\delta y}, \quad \text{and} \quad v_{geo} = \frac{g}{f} \frac{\delta(SLA + MDT)}{\delta x} \quad (12)$$

336 For the Along-Track estimates and due to the fact that the Agulhas current has a strong
337 SSH-gradient signature, we also inferred the geostrophic current perpendicular to the or-
338 bital tracks of the altimeter Jason-2. The Along-Track altimetry dataset was obtained
339 from the AVISO Geophysical Data Records (GDR) available at [https://www.aviso.](https://www.aviso.altimetry.fr)
340 [altimetry.fr](https://www.aviso.altimetry.fr). We used the 1 Hz (5.8 km) Jason-2 SSH corresponding to tracks #20 and
341 #96 and derived geostrophic velocities from the Along-Track ADT obtained by subtracting
342 the mean sea surface height and adding the mean dynamic topography. This methodology
343 is basically the same as that used by [*Krug and Tournadre*, 2012].

3.1.2 Synthetic Aperture Radar-derived surface current field and Sentinel-1 SAR roughness

Although the geostrophic current estimates are derived from the sea level height which results from an integration over the water column, they only represent an estimate of the geostrophic current and do not represent the total surface current. In order to compare with an estimate of the total surface current we used the radial velocity map estimated from the Advanced Synthetic Aperture Radar (ASAR) measurements on the ENVISAT satellite mission (2002-2012) [Chapron *et al.*, 2005; Johannessen *et al.*, 2008; Rouault *et al.*, 2010] available at <https://cersat.ifremer.fr>. The basic principle involves using the Doppler centroid information in the radar signal to extract the ocean surface velocity. In the Agulhas region, e.g., [Johannessen *et al.*, 2014], quantitative estimation of the current's speed can be reliably calculated along the radar line-of-sight which coincides closely with the main current direction 15° from the north (anti-clockwise). For ASAR measurements, the resulting average map at $1/8^\circ$ resolution builds on 329 ascending acquisitions, accumulated during the 2007-2011 period. As the time period for the ASAR measurements does not overlap with the time period for the present study, we compared only the average ocean surface velocity over each time period.

To characterise our spatially and temporally co-located results, we used the SAR imagery and one image in particular from the Sentinel-1 mission taken on December 5th, 2016, thus coinciding with our study period. Oceanic fronts are often revealed by high resolution products such as sea surface temperature or ocean color but also by sea surface roughness. The sea surface current gradients generally impact the roughness of the ocean and provide a means to study the sharp oceanic front [Kudryavtsev *et al.*, 2012; Raschle *et al.*, 2020]. The nominal resolution is about 20m and data are available at <https://scihub.copernicus.eu/>.

3.1.3 Sea Surface Temperature and Ocean Color

The sea surface temperature (SST) and ocean color (Chlorophyll-A) data used here were derived from Aqua and Terra MODIS sensors with a resolution of approximately 1km at nadir. We used Level-2 (L2) data which represents the measurements at full swath resolution. Both SST and ocean color data were obtained from the NASA Ocean Biology Processing Group (OBPG).

3.2 In-situ data

3.2.1 ACT experiment

To further test the retrieved estimates, we also considered surface velocities from the Agulhas Current Time-series (ACT) experiment. We use the gridded cross-sectional velocities based on *in situ* current meter measurements [Beal *et al.*, 2015]. Data can be downloaded at <https://beal-agulhas.rsmas.miami.edu/data-and-products/index.html>. Moorings, located beneath the altimeter Jason-2, track 96, all include ADCP instruments oriented towards the surface enabling the estimation of the near-surface current. Vessels generally have a draft inferior to 20 meters. From the ACT products, we then used the mean cross-sectional velocity over the 3-year experimental period at two different depths: 0 and 20 meters. Small differences were found, indicating a weak vertical shear. To compare the current estimates obtained from the different sensors, we systematically rotated the zonal and meridional velocity components by 64° to coincide with the cross-track velocity directions of both the ACT experiment and Jason-2, track #96. The ACT array deployment and the Jason-2, track #96 were oriented 15° clockwise from the perpendicular of the continental slope in order to align with the core direction of the main path of the Agulhas current. The cross-track velocities of both the ACT and Jason-2 track #96 were thus very close to the total velocity of the current.

3.2.2 Drifting-buoys

When possible, comparisons with Lagrangian estimates from drifting-buoys were also considered. Data from a total of 15 drifting-buoys, passing through the region of interest in 2016, were available at <http://www.aoml.noaa.gov/envids/gld/> [Lumpkin *et al.*, 2013]. Lagrangian drifters are surface floats equipped with a holey-sock drogue centered at 15m.

4 Results and Discussion

4.1 Annual Average

Time averages are of interest for several reasons. Firstly, it provides the exact match observed between the Mean Dynamic Topography (MDT) and the mean geostrophic current. Geostrophic current estimates are obtained from the equations 12. As the time average of the anomaly (SLA) must equal zero, deriving the MDT gives access to the mean geostrophic current. Secondly, the period of data availability from different instruments does not always coincide. Finally, the time average does not suffer from bias and smoothing linked to interpolation techniques.

4.1.1 ASAR and MDT

Data from the ASAR corresponds to a radial velocity in a direction oriented 15° clockwise from the zonal component. When both components of the current are available, we applied a rotation to conform to the radial direction of the ASAR and then compared the result with the appropriate rotated component. Results are presented in figure 8. Plot (a) illustrates the time average of the ASAR radial velocity estimates obtained from the 329 ascendant paths during the 2007-2011 period. The current's core is clearly distinguishable and the maximum current in the radial line of sight is observed between 26° E and 28.5° E. The current reaches up to $\approx 1.7 \text{ ms}^{-1}$ in this area. Plot (b) shows that the magnitude of the mean geostrophic current in the same radial line of sight and corresponding to the last available MDT (2018), is similar to the ASAR radial velocity estimates. The maximum current is, however, located more westward, i.e., between 25° E and 27° E. Regarding the estimates of the ocean surface current represented in plot (c) for the first guess and (d) for the second guess, we note a more faithful similarity with the ASAR estimates. Nevertheless, it seems that the current estimates from the AIS are weaker in the south-western area. It may be noted that the difference between the first and second guesses clearly shows the difference in noise level.

4.1.2 ACT, MDT and Along-Track Altimetry

The area covered in this study has been intersected by both the Jason-2 altimeter tracks 96 and 20, and the corresponding *in situ* ACT deployment. Comparisons are reported between the reconstructed AIS surface current, the Along-Track geostrophic velocities, and those estimated from the different MDT data (2018 and 2013). As the time periods do not overlap, only the mean gridded cross-track surface current velocities from the ACT experiment (2010-2013) are considered [Beal *et al.*, 2015]. Figure 9 shows maps of the surface current magnitudes for (a) the oceanic surface current from the AIS messages and (b) the mean geostrophic current obtained from the MDT (2018). Obtained as described in the previous paragraph, the current's core is shown very close to the coast and seems strongly steered by the continental slope. Estimates from the new MDT are slightly weaker than the estimates of the oceanic surface current derived from AIS messages. We note the opposite effect in the south-western part where the current flows farther from the coast. These observations are quantified in figure 9 where we compare (c) the along cross-track velocity for the Jason-2 track 96 associated with the ACT time series experiment and (d) the along cross-track velocity for the Jason-2 track 20. On both graphs, although

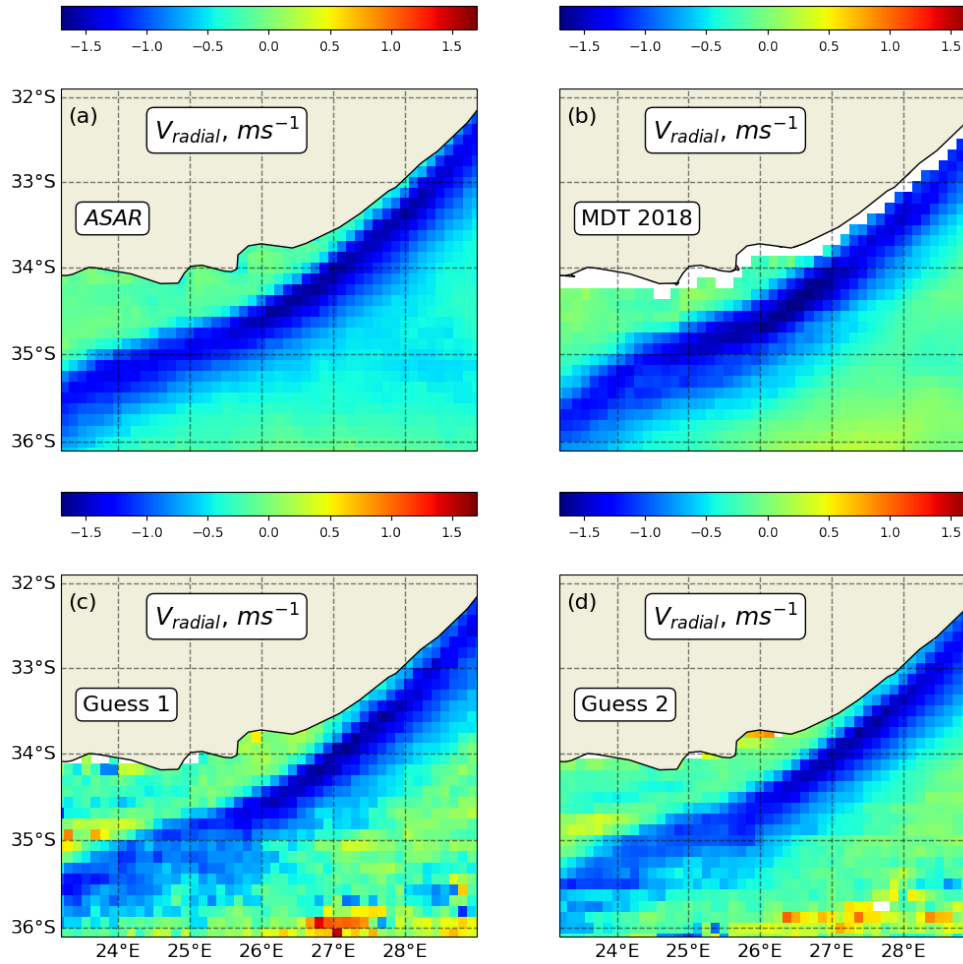


Figure 8: Time average maps of surface velocity from: (a) ASAR based range-Doppler velocity from 2007-2011. (b) Surface geostrophic current derived from MDT 2018. (c) First guess of the oceanic surface current. (d) Second guess of the oceanic surface current. The velocities in (b),(c) and (d) are rotated by 15° to conform with the ASAR radial range velocities. All maps have a spatial resolution of $1/8^\circ$. The color bar indicates surface speed in ms^{-1}

the previous Mean Dynamic Topography (MDT 2013, dashed grey line) was clearly much weaker than all others estimates, the more recent Mean Dynamic Topography (MDT 2018, full grey line) is much closer to both the ACT experiment and the mean cross-track velocity from track 96 (blue line) but seems rather high in comparison to track 20. It is interesting to note that both the geostrophic velocities and the AIS reconstructed velocities are close to the ACT measurements, though both slightly weaker.

4.1.3 Sea Surface Temperature, Ocean Color and nHHD flows

Among the key variables in ocean dynamics are vorticity and divergence. Obviously these quantities are linked to the divergent-free flow field OS_r and the divergence to the rotational-free flow field OS_d . For example, in the Quasi-Geostrophic model, the derivative of the surface vorticity is modified by the surface divergence when the fluid is considered incompressible. Moreover, the oceanic surface divergence is often associated to the oceanic front and can be easily detected from sea surface temperature, ocean color and SAR imagery. In figures 10 (a) and (b) the average annual SST from the MODIS Aqua Sensor is presented together with the average annual Chlorophyll-a concentration for the the year 2016. The region is clearly divided between the warm, poor (in terms of Chlorophyll-a) and the cold, rich waters. From the average annual OS_ξ current, in these regions we can attribute positive and negative vorticity to the warm, poor waters and the cold, rich waters respectively (figure 10 (c)). The same can be seen with the divergence calculation presented in figure 10 (d). Here, the cold, rich waters correspond to positive divergence (up-welling), whereas the warm, poor waters correspond to negative divergence (down-welling). It is important to note that the Chlorophyll-a concentration is in log-scale and the level corresponding to the value -1 is plotted in figure 10 (b). This line approximately corresponds to the level of zero divergence in figure 10 (d). In figures 10 (e) and (f) the average annual magnitude of the divergent-free (OS_r) and rotational-free (OS_d) flows are shown. The first field shares the same mathematical property of being a divergent-free field as the velocity field derived from the MDT (figures 8 (b) and 9 (b)). When compared, we notice a similar value $\approx 1.5ms^{-1}$ in the north-eastern part but a notable difference arises in the south-western part where the current derived from the MDT is stronger. Interestingly, this part corresponds to the highest magnitudes of the average annual rotational-free (OS_d) field. Indeed, this magnitude can be as high as $25cms^{-1}$ and is essentially oriented southwards. Therefore, we suggest that the meridional component of the total current estimates (OS_ξ) will have a more significant part of rotational-free flow (OS_d) than will the zonal component. Moreover, the oceanic current estimates derived from the altimetry are better solved in the zonal direction than in the meridional one. Most often, this is due to the north-south orientation of the nadir-looking altimeter ground tracks, allowing more accurate zonal surface currents to be derived via the geostrophic approximation. Nevertheless, this approximation does not take into account the ageostrophic processes present in the total estimates of the current (OS_ξ) represented in our study by the rotational-free flow. For this particular region, this may be another source of error relating to the meridional component of the geostrophic current.

4.2 Space-time co-location synergy and validations

In this part we analyse and compare three different situations at three different times before testing our estimates with the spatially and temporally co-located velocity estimates from the drifting-buoys.

4.2.1 Sentinel-1 SAR Roughness

Contrary to the average annual current which strictly follows the continental shelf, the Agulhas current is sometimes disrupted by cyclonic events, also known as meanders or natal pulses [Lutjeharms *et al.*, 1989; Beal and Elipot, 2016]. These events are, occurring

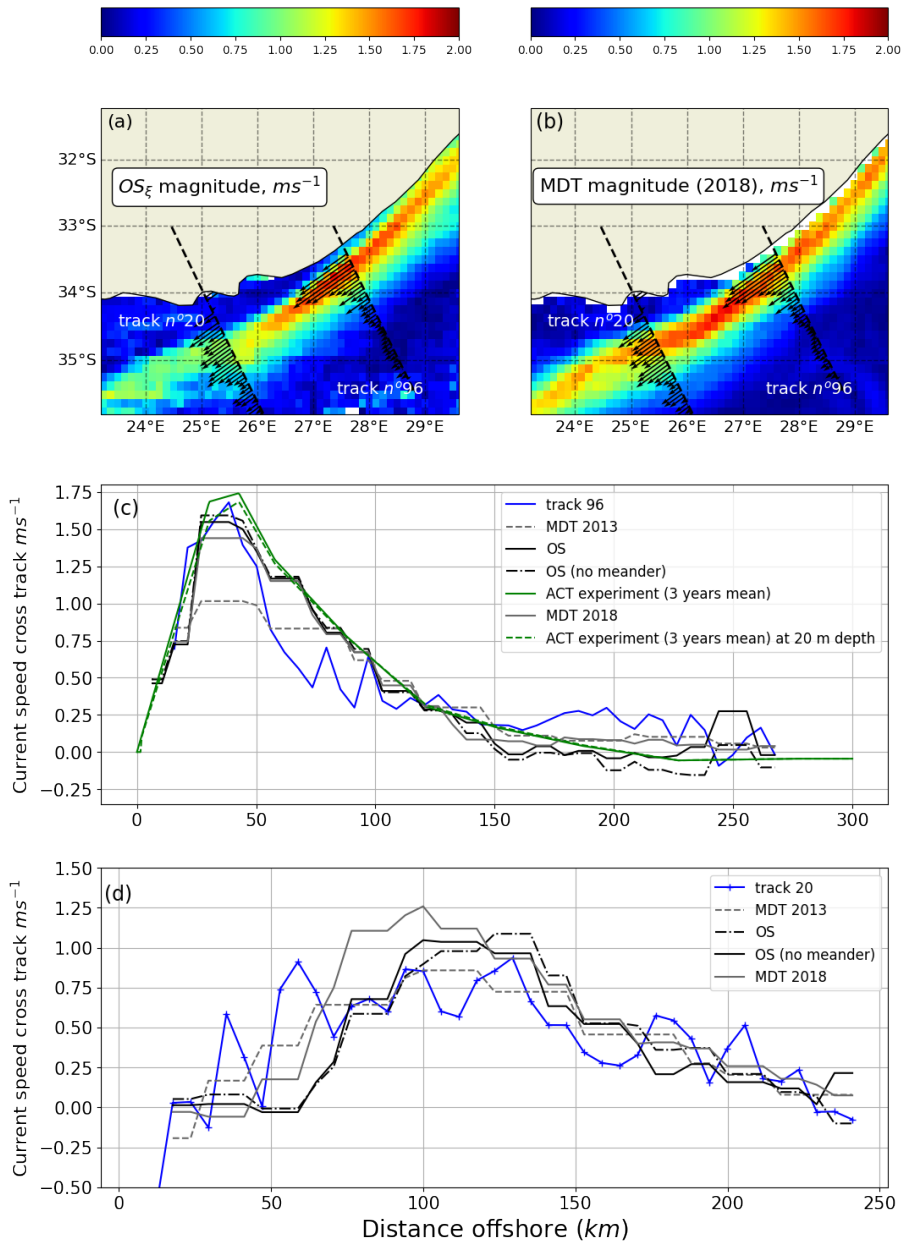


Figure 9: (a) Time average of the magnitude of our ocean surface current estimates. (b) Time average of the magnitude of the oceanic current derived from the MDT 2018. Quivers represent the time average for the Along-Track geostrophic velocities for the Jason-2 tracks 20 and 96. (c) In blue, the cross-track velocity from Jason-2 track 96 for the year 2016 (mean of 20 altimeter geostrophic velocities). In green, the cross-track surface velocities from the gridded dataset of the ACT experiment averaged over 3 years for the surface (full line) and at 20 meters depth (dashed line). The oceanic surface current velocity is represented by a black full line for the year 2016 and current velocities associated to the two MDT estimates are shown in gray (full line for 2018, dashed line for 2013). (d) Same as (c) but for the altimeter Jason 2 track 20.

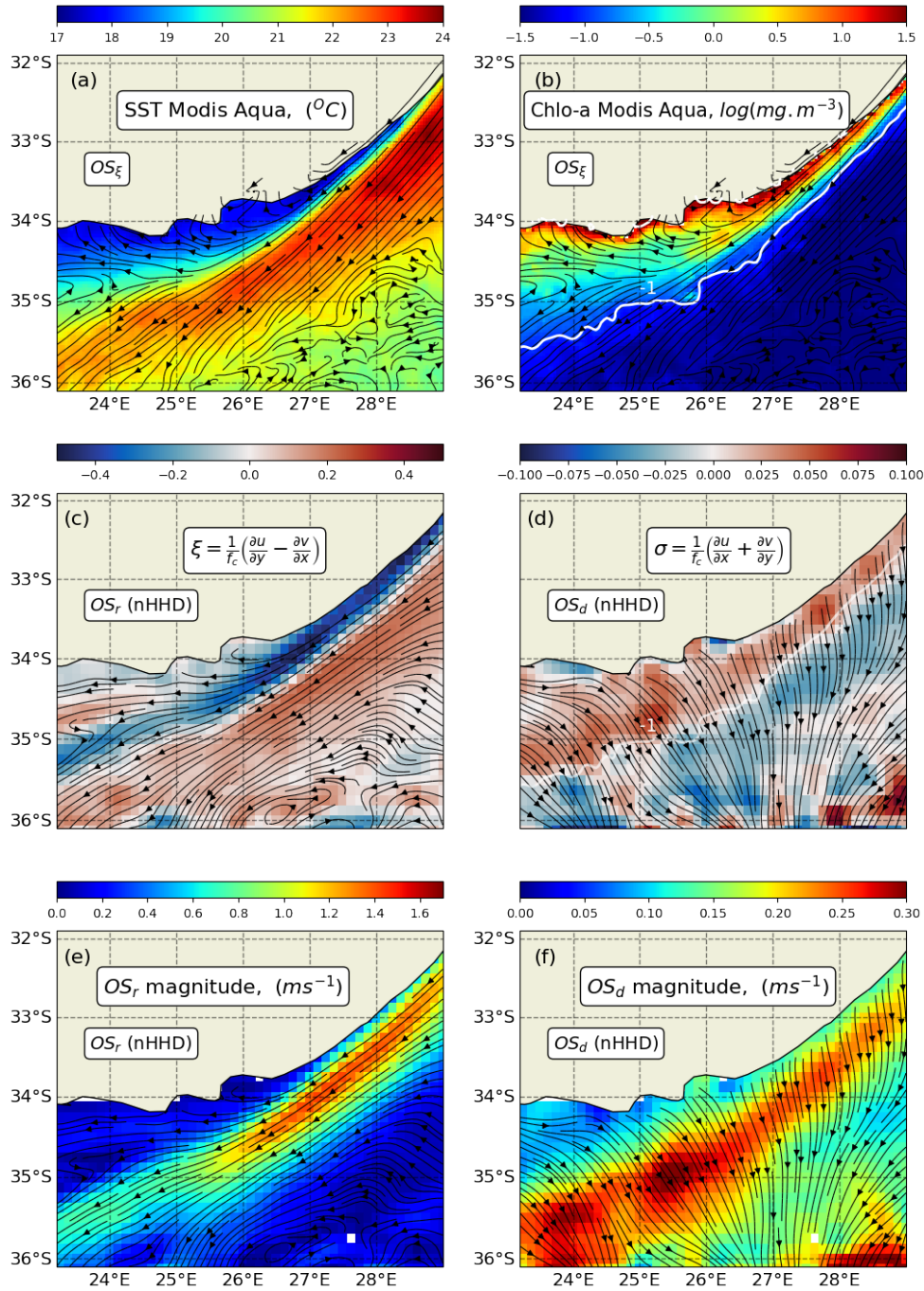


Figure 10: All maps correspond to annual mean (2016). (a) SST MODIS with the streamlines of the total oceanic surface current field. (b) Chlorophyll-a also with the streamlines of the total oceanic surface current field. (c) Vorticity with the divergent-free flow field (OS_r). (d) Divergence with the streamlines of the rotational-free flow field (OS_d). (e) and (f) represent the magnitude of the divergent-free flow field and the rotational-free flow field associated with their own streamlines.

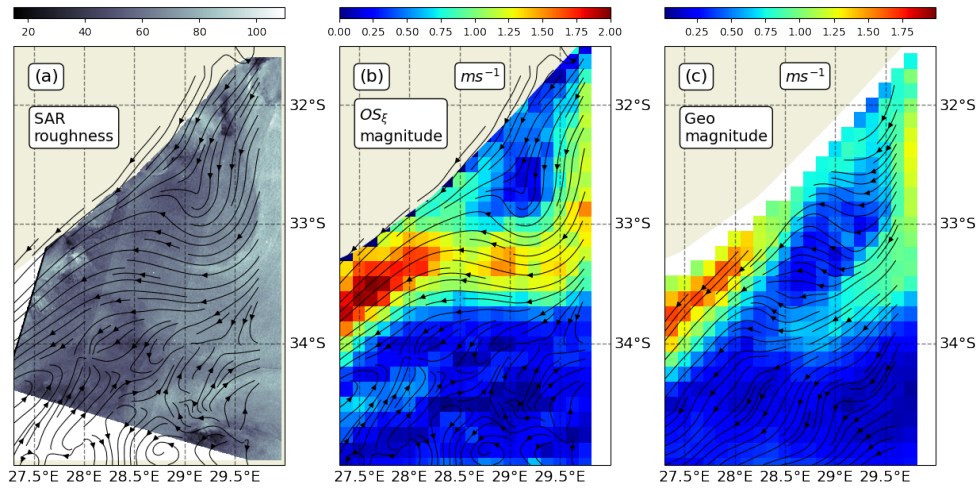


Figure 11: (a) SAR Roughness December 5th, 2016, streamlines correspond to the ocean surface current. (b) Magnitude and associated streamlines of the oceanic surface current. (c) Magnitude and associated streamlines of the geostrophic gridded current.

490 around 1.6 year^{-1} [Rouault and Penven, 2011]. Such a propagating natal pulse can be
 491 clearly observed on the SAR image obtained from the Sentinel-1 mission on December
 492 5th, 2016, presented in figure 11 (a). To compare the OS and geostrophic gridded current
 493 estimates, their magnitudes with associated streamlines are shown in figures 11 (b) and
 494 (c) respectively. We clearly note that the streamlines associated to the OS_{ξ} current follow
 495 the shape of the meander present in the SAR Roughness image more closely than do the
 496 streamlines issued from the geostrophic gridded current. In this specific case, it may be
 497 argued that this is caused by the fast evolving shape of the meander in contrast to the time
 498 resolution of the altimeter-derived geostrophic current estimates.

499 4.2.2 SST and Ocean Color

500 Here we illustrate two situations of interest where the MODIS Terra sensors captured
 501 the SST signature and ocean color. The first occurred during a meander event on
 502 April 11th, 2016. As previously shown in figure 11, a propagating natal pulse is clearly
 503 expressed on the SST field. In this case, however, the meander was located in the south-
 504 western part of the region (figure 12 (a)). The total oceanic surface OS_{ξ} streamlines obtained,
 505 closely follow the SST iso-lines and thus the meander. Such circulation is likely
 506 to cause vertical velocity and induce up-welling [Goschen et al., 2015; Leber et al., 2017].
 507 Indeed, these authors' findings demonstrate that two mechanisms are responsible for in-
 508 duced up-welling events: the presence of a meander and northeasterly winds. As an il-
 509 lustration of the up-welling sites, figure 12 (b) shows the concentration of chlorophyll-a.
 510 The streamlines associated to the divergent component (OS_d) of the velocity field clearly
 511 originate in the highest chlorophyll-a concentration areas as is the case for the maps show-
 512 ing annual average illustrated in figures 10 (d) and (f). The areas of highest concentration
 513 are always located near the shore, on the continental shelf. During a meander event, how-
 514 ever, higher concentrations are present over a larger geographical area. As previously, the
 515 line corresponding to the value -1 in the log scale of the chlorophyll-a concentration is
 516 reported on the map in figure 12 (c). As was the case for the annual average, we clearly
 517 observe that the line separating the areas of high and poor chlorophyll-a concentration co-
 518 incides quite well with the areas of positive and negative divergence.

519 The second situation of interest occurred on May 18th, 2016. This period was meander-
 520 free but showed the presence of northeasterly winds. Results are shown in figures 12 (d),
 521 (e) and (f). In this situation, the SST gradient is more pronounced between the current's
 522 core and the continental shelf which concentrates the highest levels of Chlorophyll-a. The
 523 area is smaller than in the first situation (meander). Roughly the same observations can be
 524 made regarding the separation between rich and poor regions (in terms of Chlorophyll-a)
 525 and the correspondence with the positive and negative divergence. An interesting phe-
 526 nomenon can be observed in the south-western area where a thin filament of Chlorophyll-a
 527 follows the Agulhas current along its inner side. This thin filament clearly corresponds to
 528 an area of high positive divergence (figures 12 (e) and (f)).

529 4.2.3 Drifting-buoys

530 For the year 2016, we could select 15 drifting-buoys within our study site from the
 531 AOML catalogue. Their trajectories are presented in the subplot of figure 13 (a). Fig-
 532 ures 13 (a) and (b) show maps corresponding to the oceanic current estimates OS_{ξ} and
 533 geostrophic estimates (Geo) during a meander event in the beginning of March. A week
 534 before the date represented on these maps, on February 24th, a drifting-buoy entered the
 535 area in the north-eastern part and drifted northwards before interacting with the main
 536 current and being advected south-west following the current caused by the meander. Al-
 537 though the correlation and Root Mean Square Error (RMSE) between the OS_{ξ} or Geo
 538 velocities and the velocities issued from this drifter in particular are close, some differ-
 539 ences do exist between the two maps. Firstly, near the coast and between the longitudes
 540 27°E and 28° the south-westward current is much stronger when considering the OS_{ξ} es-
 541 timates. The same phenomenon exists if we consider the divergent-free flow field (OS_r)
 542 instead. Secondly, the south geographical extension of the meander is larger with the OS_{ξ}
 543 estimates.

544 To study the difference between the two products and considering the velocities of
 545 the drifters as a ground truth, we systematically co-located (in both time and space) the
 546 velocities associated to the drifting-buoys with our estimates and those from the Geo. Fig-
 547 ure 11(c) shows the comparison between the total zonal surface current (U_{ξ}) (in blue) and
 548 the divergent-free (U_r) (in red) with the zonal velocities of the drifting-buoys. We note
 549 a better correlation ($r = 0.83$ versus $r = 0.76$) and lower RMSE (0.32 versus 0.38)
 550 when considering the zonal divergent-free component (U_r) with the zonal velocities of
 551 the drifting-buoys. It is important to note that figure 10 (f) shows the annual average of
 552 the rotational-free flow field and though weaker than the meridional component, a posi-
 553 tive zonal component appears. It seems logic that the total zonal current estimates U_{ξ} are
 554 weaker (in absolute value) than the divergent-free zonal estimates U_r . This is somewhat
 555 what is observed when looking at figure 13 (c). Moreover, the scatter plot shown in figure
 556 13 (d) comparing the zonal Geo estimates to the zonal velocities of the drifting-buoys is
 557 very similar to that obtained with the divergent-free flow field. ($r = 0.85, rmse = 0.3$).
 558 The drifting-buoy drogues are at 15m depth which is very similar to the draft of vessels.
 559 Why the divergent-free component U_r is closer to the zonal velocity of the drifting-buoys
 560 remains unanswered. One explanation may come from the errors which are larger in the
 561 zonal direction than in the meridional one, as demonstrated in the optimal interpolation
 562 section 2.4

563 When we compare the meridional velocities V_{ξ} and V_r to the meridional velocity
 564 of the drifting-buoys we find quite the opposite result, which is definitively far easier to
 565 interpret. Indeed, the analysis of the scatter plot in figure 13 (e) shows a stronger corre-
 566 lation with the total V_{ξ} in blue ($r = 0.84, rmse = 0.28$) than with the divergent-free V_r
 567 in red ($r = 0.8, rmse = 0.32$). Moreover, a clear bias is observed when comparing the
 568 total meridional component with the meridional divergent-free component (≈ -0.05 for
 569 the total current versus ≈ -0.13 for the divergent-free current). This indicates that the
 570 meridional divergent-free component underestimates the real current represented by the

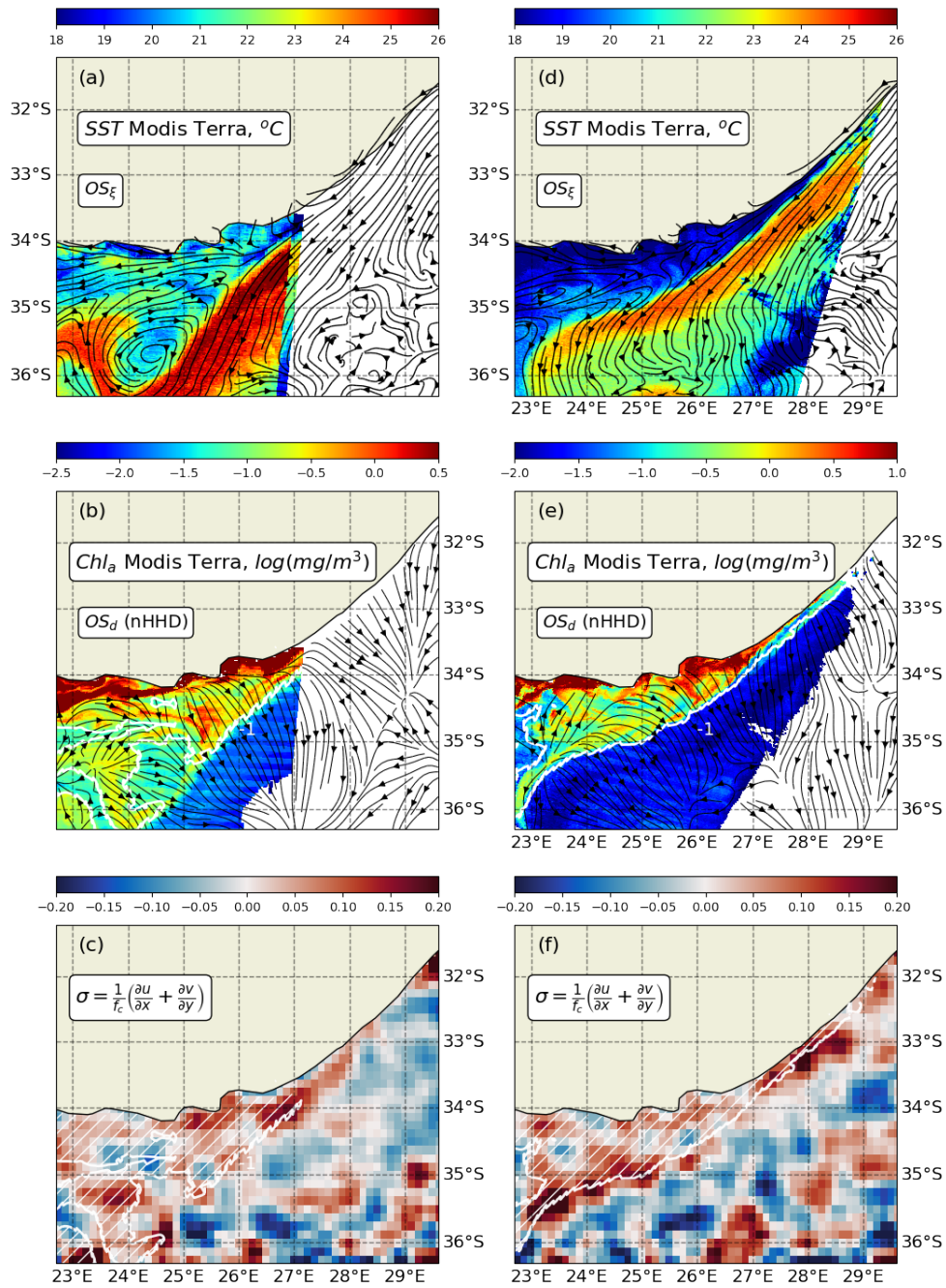


Figure 12: (a) Sea Surface Temperature in degrees Celsius obtained from the MODIS Terra sensor for April 11th, 2016. Streamline represents the total AIS current estimates. (b) Ocean color (Chlorophyll-a) in a logarithmic scale obtained from the MODIS Terra sensor, same day as (a). Streamline represents the divergence component of the current. (c) Same as (a) but on May 18th, 2016. (d) Same as (b) but on May 18th, 2016

571 drifting-buoys. The same can be observed with the meridional Geo velocities where the
 572 lowest absolute values never exceed -1.5ms^{-1} as is the case for the meridional divergent-
 573 free current V_r . This, however, is clearly not the case for the total estimates V_g , the ab-
 574 solute values of which quite regularly exceed -1.5ms^{-1} . In terms of the annual average,
 575 figure 10 (f) shows magnitude values around 25cm.s^{-1} oriented almost southward for the
 576 rotational-free current. This is in line with the bias found between the meridional veloc-
 577 ity of the divergent-free current and the meridional velocity of the drifting-buoys. Given
 578 that the drifting-buoys' drogues are at a depth of 15 meters and that the draft of vessels is
 579 of the same order but integrated from the surface to the draft, we guess that our current
 580 estimates correspond to a depth inferior to 15 meters. This could be the reason for the dif-
 581 ference observed between the bias of 0.13 cm.s^{-1} and the magnitude of the rotational-free
 582 current of $\approx 0.25\text{ cm.s}^{-1}$. Another possible explanation could be the spatio-temporal spar-
 583 sity of the drifting-buoys. For this part, however, it seems reasonable to conclude that the
 584 extremes values in the meridional velocity of the drifting-buoys are out of the geostrophic
 585 equilibrium.

586 **5 conclusion**

587 In this paper, we have demonstrated that improved estimations of upper ocean sur-
 588 face velocities can be obtained over the core region of the Agulhas Current, when using
 589 selected AIS messages.

590 The AIS data do not directly provide vessel speeds with respect to the moving ocean.
 591 To overcome this lack of information and in order to directly derive the upper ocean cur-
 592 rent, the interpretation framework can be built on a homogeneity assumption: that is, all
 593 vessels, chosen within a given space-time interval, encounter the same sea surface condi-
 594 tions. In the Agulhas region of interest, this space-time interval can be adjusted follow-
 595 ing the density of the maritime traffic. A second guess reduces the space-time resolution
 596 to one day and $1/8^\circ$. During transient events the differences between our estimates and
 597 geostrophic current estimates are notable. These transient events may move relatively fast
 598 and not be sufficiently sampled by altimeter measurements.

599 Further comparisons performed using data from *in situ* drifting-buoys, ADCP
 600 measurements (ACT experiment), as well as average Doppler-derived surface current from
 601 satellite SAR measurements, all reveal a general (anticipated) underestimation of the sur-
 602 face current estimates obtained by interpolated altimeter products.

603 In view of the existing need for a more comprehensive monitoring system for the
 604 Agulhas Current, these results are encouraging to consider the ever-increasing availability
 605 of AIS messages for routine quantitative monitoring of surface current conditions, and to
 606 better evaluate the leakage of warm, saline waters from the Indian Ocean into the Atlantic
 607 Ocean [*de Ruijter et al.*, 1999; *Beal et al.*, 2011]. Combining surface information with *in*
 608 *situ* information can directly serve to more accurately represent Agulhas ring transport and
 609 exchanges [*Nencioli et al.*, 2018]. Modeling surface current interactions in standard wave
 610 numerical models is also an active area of research [*Ardhuin et al.*, 2017]. In the Agulhas
 611 current region, strong currents cause significant swell ray deflection and localized trapping
 612 phenomena (e.g., [*Quilfen et al.*, 2018; *Quilfen and Chapron*, 2018]). A direct benefit of
 613 the increased availability and accuracy of combined satellite observations, including imag-
 614 ing [*Kudryavtsev et al.*, 2017b,a] and AIS messages would be a significant improvement in
 615 navigation safety in the region.

616 **Acknowledgments**

617 The raw AIS data were obtained from ORBCOMM. Underlying raw AIS data (i.e., indi-
 618 vidual vessel tracks) are publicly available from source data providers and may or may not
 619 require a fee to be accessed, depending on user affiliation and terms of use. The SST and

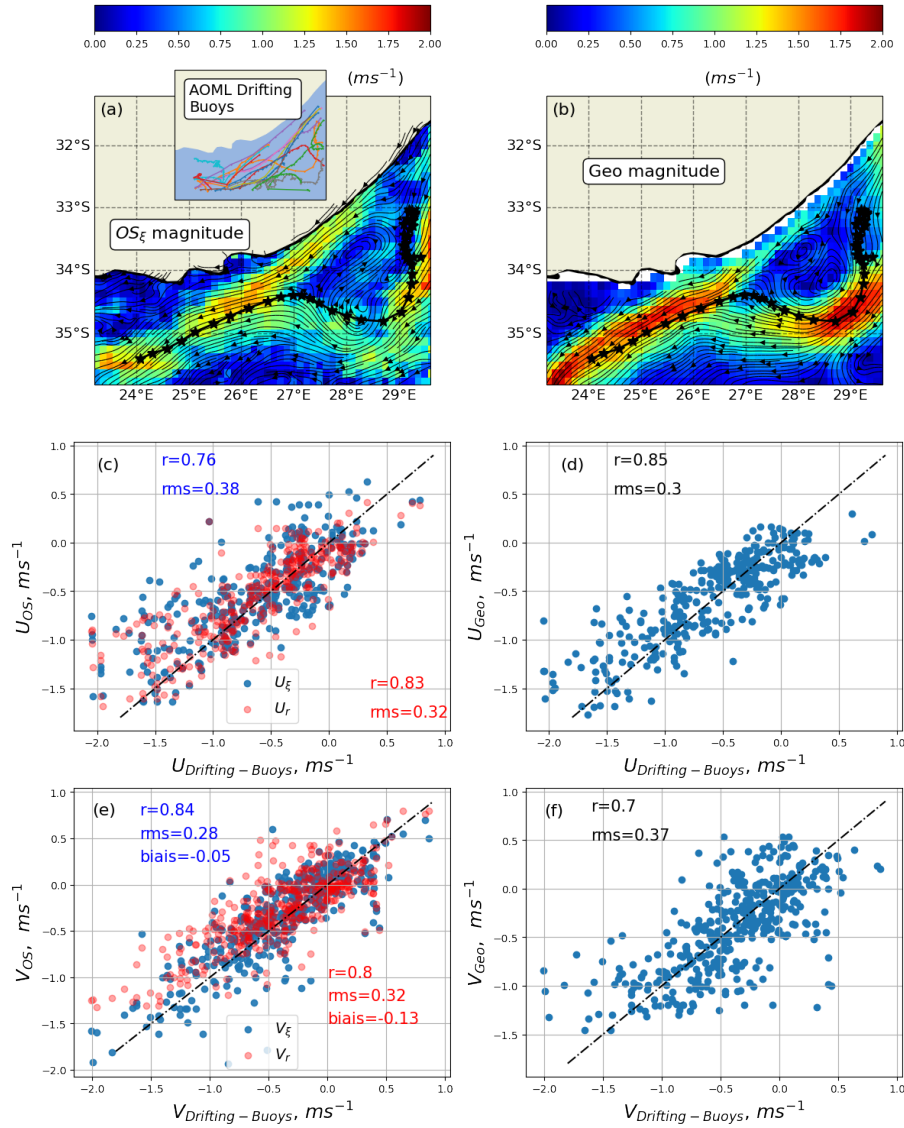


Figure 13: (a) Ocean Surface current magnitude for March 1st, 2016. The black dotted line shows an example trajectory of one of the drifting-buoys between February 24th and March 6th. The trajectories of the 15 drifting-buoys considered in this study are represented in the sub-graph. (b) Same as (a) but for the geostrophic estimates (Geo) of the current. (c) Scatter plot of the zonal component of the total velocity field versus the zonal velocity of the drifting-buoys (in blue). In red, the zonal component of the total velocity field is substituted by the zonal curl component. (d) Scatter plot of the zonal component of the geostrophic velocity field versus the velocity of the drifting-buoys. (e) Scatter plot of the meridional component of the total velocity field versus the meridional velocity of the drifting-buoys (in blue). In red, the meridional component of the total velocity field is substituted by the meridional curl component. (f) Scatter plot of the meridional component of the geostrophic velocity field versus the meridional velocity of the drifting-buoys

620 mean Doppler-derived surface current (SAR) products are available at [http://cersat.
621 ifremer.fr/](http://cersat.ifremer.fr/). The data from the drifting-buoys is available at [http://www.aoml.noaa.
622 gov/envids/gld/](http://www.aoml.noaa.gov/envids/gld/). The gridded reprocessed absolute geostrophic velocities from AVISO,
623 distributed by CMEMS are available at [http://marine.copernicus.eu/services-portfolio/
624 access-to-products/](http://marine.copernicus.eu/services-portfolio/access-to-products/). The data from the JASON-2 altimeter tracks 96 and 20 are
625 available at <https://www.aviso.altimetry.fr>. Regarding the ACT experiment, the
626 data can be downloaded at [https://beal-agulhas.rsmas.miami.edu/data-and-products/
627 index.html](https://beal-agulhas.rsmas.miami.edu/data-and-products/index.html)

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