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Generation of spherical vortex beams to trap large particles for enhanced axial force

Zhao D.^{a,b}, Thomas J.-L.^a, Marchiano R.^b

^a*Sorbonne Université, CNRS, Institut des Nanosciences de Paris, INSP, F-75005 Paris, France*

^b*Sorbonne Université, CNRS, Institut Jean le Rond d'Alembert, d'Alembert, F-75005 Paris, France*

Abstract

Recent studies have shown the possibility to manipulate small elastic spheres in 3D with a single-sided beam. Acoustical tweezers are very appealing because they provide a fine spatial control of the motion of a single particle in space. Their main limitations are due to the weak restoring axial force and improving this force is still a challenge. We show theoretically that the spherical vortex beams can trap large particles and enhance the axial force. Indeed, the special features of these unusual beams look like the bottle beams in optics. Nevertheless, their spatial complexity presupposes that they can be produced with sufficient precision. Therefore, attention is paid to the synthesis of the spherical vortices. A method based on the inverse filter method is proposed. It allows to synthesize them with a very good precision since the theoretical force is recovered experimentally with an error smaller than 10%. Then, the spherical vortices are used to trap polyethylene beads with radii between 500 and 590 μm . Experiments show that the radial trap is working while no beads have been trapped in the axial direction. This failure is analyzed in detail and is shown to be mainly due to sensitivity to the properties of the materials which influences the resonance modes of the elastic sphere. This study paves the way to the optimization of acoustical tweezers for the manipulation of large objects.

Keywords: Radiation pressure, Acoustical tweezers, Single beam tweezers, spherical vortex beam, Resonating spherical target

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1. Introduction

Contactless manipulation using radiation pressure is widely used in biological, chemistry and medical applications. Among available tools, optical tweezers [4] stand out for their selectivity, the ability to pick up a selected particle among others, and accuracy. They have been used to trap various kinds of targets such as cells, viruses and molecules [40, 1, 24, 3, 36]. Meanwhile, the shortcomings of optical tweezers: the photo-damage due to photochemistry [9] and unavoidable heating [23] with highly focused optical beam restrict the range of force in practical situations (from 0.1 to 100 pN [30]). Magnetic tweezers are safe for biological samples but have their limitations in terms of forces and trap stiffness. In this context, the noninvasive and deep-tissue-penetration properties of ultrasound are very attractive for complex manipulations in biological and biomedical domains.

Acoustical traps based on standing waves were proved to be feasible and can provide stable traps for spheres, droplets, living animals [39, 43, 42]. In these setups, the standing waves are made with a single transducer and a mirror or two transducers in opposite directions. Hence the targets must be located in between and thus forbid three-dimensional manipulation in many practical situations. Moreover, a single location of equilibrium is achieved only if the cavity length is one half of wavelength. Indeed, all pressure nodes (or anti-nodes depending on the object density and compressibility) act as potential traps. Such a constraint means that submillimetric wavelengths much larger than the micrometric targets are usually used even in microfluidic channels. Standing wavefields are of significance in collective manipulation of multiple objects or for particle sorting. On the contrary, single-beam optical tweezers achieve selective traps with a single position of equilibrium of size comparable to the particles. Diffraction in the far-field limits the focal spot to a size larger than about one wavelength, therefore achieving acoustical tweezers with optimal selectivity means trapping object of about the size or larger than one wavelength. Moreover, they afford three-dimensional manipulations with nanometer accuracy. Regarding the advantage of three-dimensional manipulation, single beam acoustical tweezers consisting of single-sided transducer or transducers array are developed [5, 11, 21]. For such single-sided configurations, the most important parts are the beamforming and transducer design. To date, different beamforming of single beam acoustical tweezers have been investigated: focused Gaussian beam [34, 19, 20], Bessel beam [15, 13, 26, 12], fraxicon beam [22] and focused vortex beam [7].

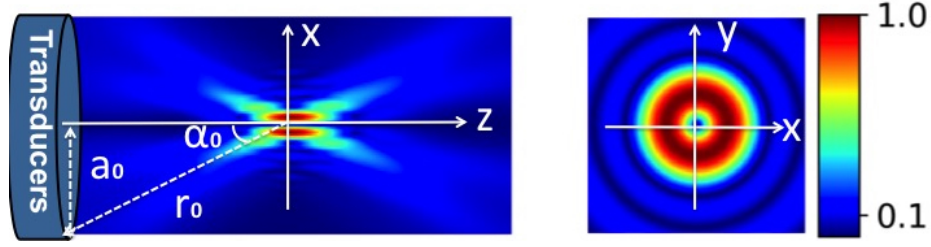
The major challenge of acoustic single beam trapping is to achieve the axial restoring force since there is a competition between the gradient forces and axial expelling force induced by the back-scattering. One way to overcome this difficulty is to increase the axial pressure gradient. A recent study has proposed another type of vortex beam, namely, the spherical vortex beam [5]. This special beam has a dark focus that is surrounded by regions of higher amplitude, features reminiscent of the bottle beam used in optical traps [2]. For these waves, the minimum energy density is achieved without phase singularity. This black zone is surrounded by a shiny shell, but the amplitude is not uniform and therefore the trap is anisotropic. Optimizations have been proposed [10, 29, 18] and realized [35] in the context of optical tweezers and high-resolution imaging. These solutions are interesting alternatives but without the phase singularity, the wave has no pseudo kinetic moment and therefore the tweezers cannot apply any controllable torque and rotation to the particle [8]. The spherical vortex beam was theoretically estimated to be able to trap large elastic spheres, i.e. a size comparable to the wavelength, with the potential to achieve optimal selectivity. Nevertheless, the experimental realization of acoustical tweezers requires good field synthesis design. For focused vortex beams, the synthesis systems have been developed using either multi-elements, i.e. arrays of transducers, [38, 25, 28, 7] or mono-element like spiral grating, spiraling transducers and metasurface [16, 33, 17]. As the beam shape of a spherical vortex become more complicate, attention should be paid to find a suitable system for the field synthesis. At the same time, as the target sphere becomes larger, the resonances of the scattering coefficients may probably appear and will influence the trapping. So the question arises: is it possible to trap spherical beads with a spherical vortex? In this paper, we will answer this question by first presenting the theoretical background about spherical vortices with special attention to the predictions of the forces exerted by this kind of beams and by comparing them to the ones exerted by a focused vortex. Then the wavefield synthesis of such beams will be presented and used to manipulate polyethylene beads (Sec. 3.2). Finally, the analysis of the resonances of large spheres, as well as their influence on the trapping, are discussed.

2. Methods

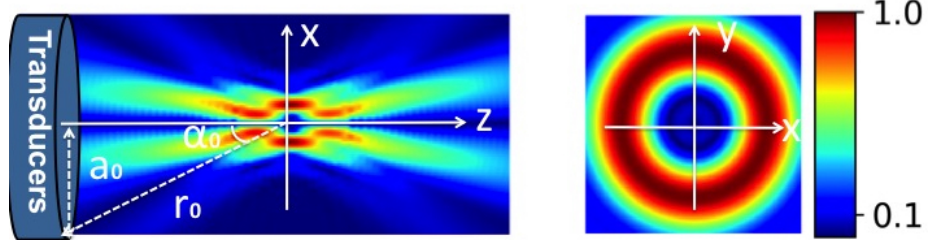
2.1. Theoretical predictions of the forces exerted by a spherical vortex on an elastic sphere

Spherical vortex, as suggested by its name, is a vortex beam whose associated pressure field has a spherical pattern at the central beam core. As is shown in Fig. 1(b), the high amplitude has a ‘candy’

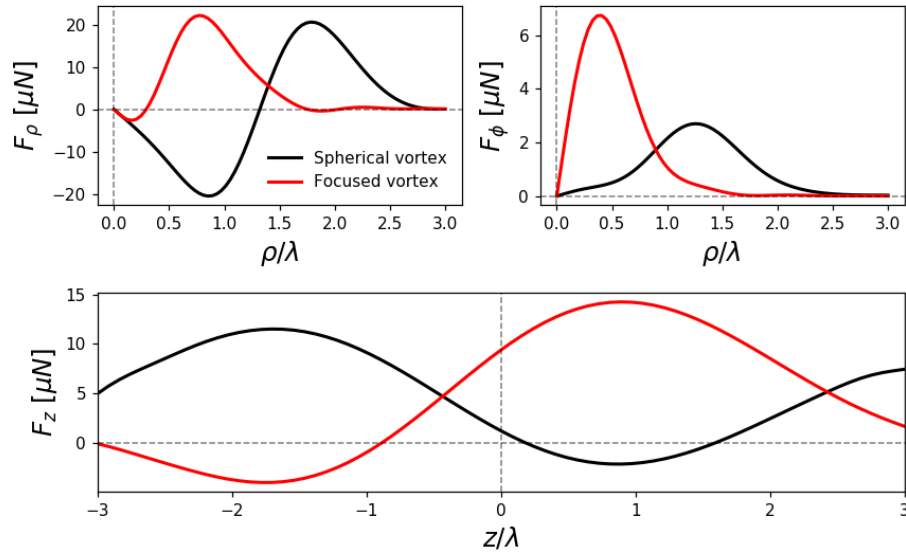
form, the zero amplitude region is like a spherical ‘candy’ wrapped up by the high-pressure field. This kind of vortex has a high-amplitude gradient both radially and axially and forms a spherical trapping zone with zero amplitude at the center. Compared to a focused vortex beam with the same topological charge (Fig. 1(a)), the spherical vortex has a higher pressure gradient in the wave propagation direction and a larger trapping zone (Fig. 1(b)). According to this configuration of the pressure field, the spherical vortex is supposed to be able to trap large spheres radially and axially (with radius $a \simeq 0.5\lambda$).



(a) Theoretical pressure field of a focused vortex



(b) Theoretical pressure field of a spherical vortex



(c) Theoretical radiation forces

Figure 1: (Color online) Modulus of the complex pressure field at frequency $f_0 = 1.2$ MHz for (a) a focused vortex beam and (b) a spherical vortex beam with topological charge $m' = 1$, radial degree $l = 8$ generated with a concave spherical transducer: aperture angle $\alpha_0 = 49^\circ$, geometrical focus $r_0 = 7.5$ cm, the spherical basis is centered at the focus of the incident beam; (c) Radiation forces on a polyethylene sphere with radius $a = 0.45\lambda$ exerted by a focused vortex beam with topological charge $m' = 1$ and aperture angle $\alpha_0 = 49^\circ$ and a spherical vortex beam of same topological charge and aperture angle with radial degree $l = 8$.

In a spherical basis, the incident wavefield can be decomposed with spherical functions and described

by the incident beam shape coefficients (BSC) A_n^m :

$$p_i(r, \theta, \phi, t) = p_a \sum_{n=0}^{+\infty} \sum_{m=-n}^n A_n^m j_n(kr) Y_n^m(\theta, \phi) \exp(-i\omega t) \quad (1)$$

where p_a is the characteristic amplitude, j_n is the spherical Bessel function and Y_n^m are the spherical harmonics.

65 The BSC for a focused vortex are [5]:

$$A_n^m = \delta_{m,m'} N_n^{m'} (kr_0)^2 h_n^{(1)}(kr_0) (-1)^{n+m'} \int_{\cos \alpha_0}^1 P_n^{m'}(x) dx, \quad (2)$$

and for a spherical vortex:

$$A_n^m = \delta_{m,m'} 4\pi N_n^{m'} (kr_0)^2 h_n^{(1)}(kr_0) (-1)^{n+l} \int_{\cos \alpha_0}^1 \tilde{P}_l^{m'}(x) P_n^{m'}(x) dx, \quad (3)$$

where the coefficients $N_n^{m'}$ are:

$$N_n^{m'} = \sqrt{\frac{(2n+1)}{4\pi} \frac{(n-m')!}{(n+m')!}}.$$

Function $h_n^{(1)}$ is the spherical Hankel function of the first kind, the wavenumber is $k = 2\pi/\lambda$, functions P_n^m and $\tilde{P}_l^{m'}$ are the associated Legendre polynomials and associated Legendre polynomials normalized to unity, respectively, $x = -\cos(\theta) = \cos(\alpha)$, with $\alpha = \pi - \theta$, (r, θ, φ) the spherical coordinates. With $\delta_{m,m'}$ the Kronecker delta, m' the topological charge of the vortex and α_0, a_0, r_0 are respectively the aperture angle, the radius of the transducer array and the focal distance as illustrated in Fig. 1(b). Comparing the beam shape coefficients of the two vortex beams, the spherical vortex is obtained by using the associated Legendre polynomial to tailor the focused vortex beam. Thus, for a spherical vortex of topological charge $m' = 1$, the shape is mainly determined by the aperture angle α_0 and the degree l of the associated Legendre polynomial $\tilde{P}_l^{m'}(x)$ in Eq. (3). Among these factors, the aperture angle α_0 is limited by the directivity pattern of the transducers and the lens used to focus the field. The maximum angle of the aperture is generally fixed by the experimental setup (for instance in our experimental system, it is 49°). Thus, to achieve the desired forces acting on an elastic sphere, the optimal topological charge m' and the degree l should be chosen. First, the degree l of the associated Legendre polynomial $\tilde{P}_l^{m'}(x)$, is chosen

to have an amplitude that varies smoothly in the range of $x = [\cos \alpha_0, 1]$ and gently drops near zero at $\cos \alpha_0$ to minimize the secondary lobes in the radiated field that would be induced by a sharp truncation. As depicted in Fig. 2, the topological charge m' is fixed at 1, $\tilde{P}_l^{m'}(x)$ as a function of α is plotted for different degrees l . According to the figure, the degree $l = 4$ and $l = 8$ are both close to zero at $\alpha_0 = 49^\circ$. Actually, $l = 4$ is closer to zero than $l = 8$. However, comparing the pressure field for $l = 4$ and $l = 8$ (Fig. 3), we find that in plane (x, z) , the axial pressure gradient for $l = 8$ is larger than $l = 4$. And in plane (x, y) , the size of the trapping region (the blue zone inside the high intensity ring) for $l = 8$ is also larger than $l = 4$. Therefore, a compromise should be made to obtain the optimal beam shape. As our aim is to trap large particles, which need a large trapping zone and a high pressure gradient in the axial direction, the degree $l = 8$ is the best suited with $m' = 1$.

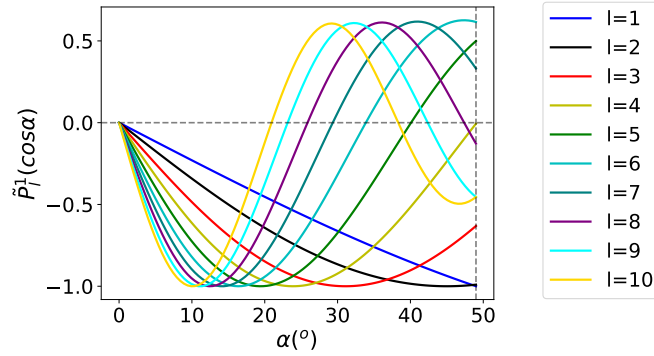


Figure 2: (Color online) Normalized associated Legendre polynomial $\tilde{P}_l^{m'}(\cos \alpha)$ as a function of α . A vertical grey line is drawn to mark $\alpha_0 = 49^\circ$.

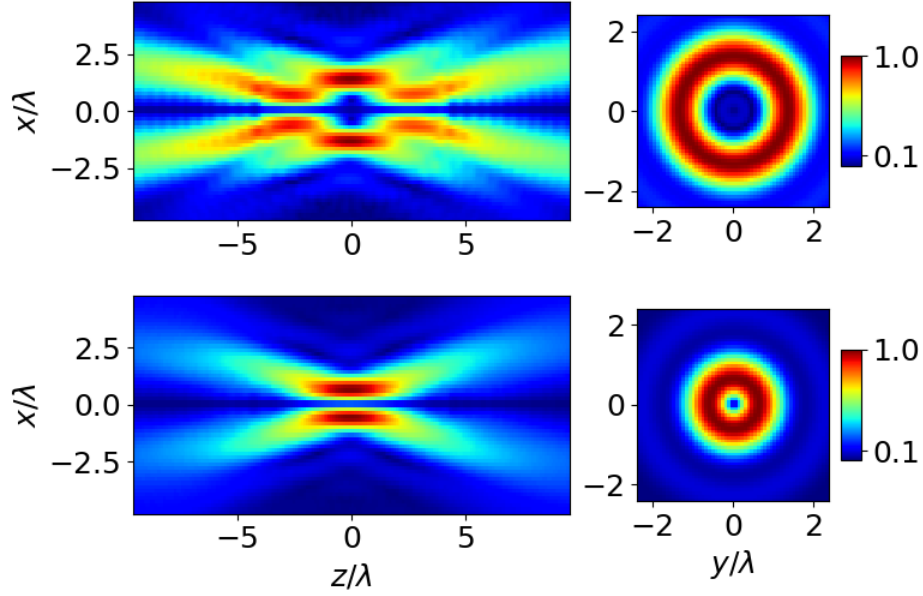


Figure 3: Modulus of the pressure field in plane (x, y) and (x, z) with $l = 8$ (top) and $l = 4$ (bottom).

90 The trapping effect of a focused vortex and a spherical vortex beam are assessed by computing the radiation forces. To do so, an efficient model established recently [6] is applied. According to this model, the three-dimensional radiation force acting on an elastic sphere in an arbitrary wavefield can be computed using the BSC and scattering coefficients. As illustrated in Fig. 1(c), a polyethylene bead (density $\rho = 1000 \text{ kg/m}^3$, transverse velocity $c_t = 1000 \text{ m/s}$, longitudinal velocity $c_l = 2400 \text{ m/s}$) with
95 radius $a = 0.45\lambda$, immersed in water ($\rho_0 = 1000 \text{ kg/m}^3$, $c_0 = 1480 \text{ m/s}$) can be trapped by the forces exerted by a spherical vortex but not by a focused vortex beam at frequency $f_0 = 1.2 \text{ MHz}$. Consequently, by tailoring the spherical vortex with proper topological charge and radial degree, it is possible to trap a large elastic sphere while it is not possible with a focused vortex.

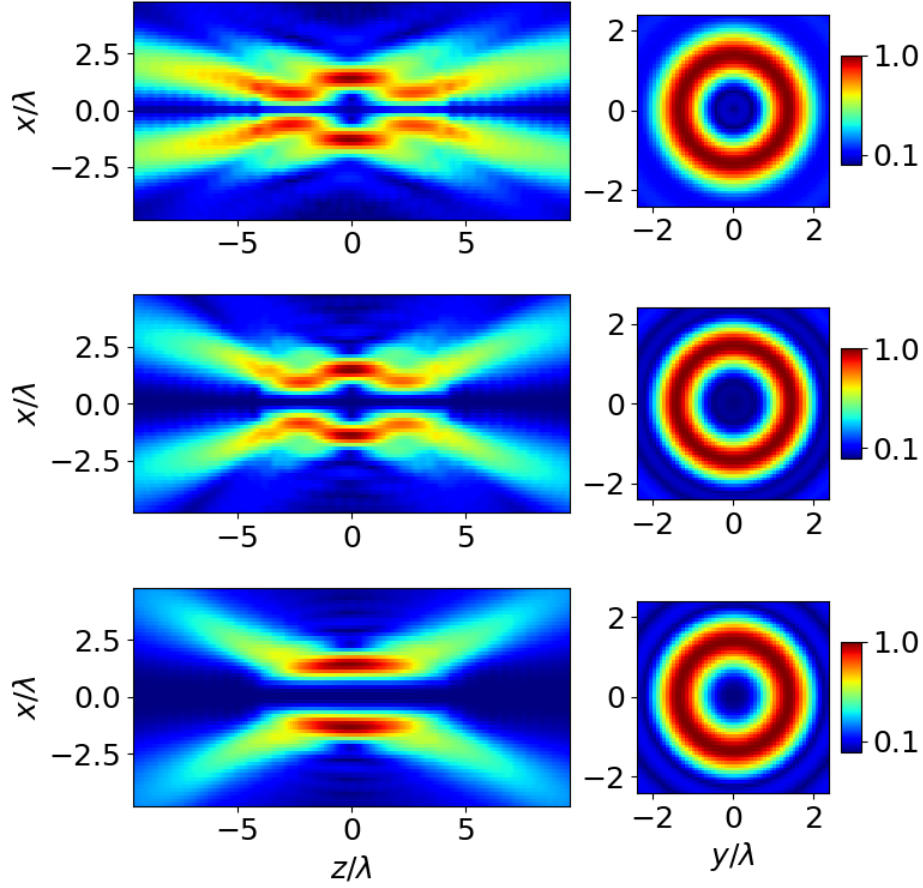


Figure 4: (Color online) Modulus of the pressure field in plane (x,y) and (x,z) with different topological charges: $m' = 1$, $m' = 2, m' = 3$.

Regarding the topological charge m' , we have compared the amplitude of the pressure field with $m' = 1, m' = 2, m' = 3$ in plane (x,y) and (x,z) (see Fig. 4). In plane (x,y) , the high-amplitude ring keeps almost the same shape and the area of zero amplitude has a radius of about 0.5λ . Meanwhile, the pressure gradient in plane (x,z) varies a lot from $m' = 1$ to $m' = 3$. When $m' = 1$, the high amplitude has a ‘candy’ form, the zero amplitude region is like a spherical ‘candy’ wrapped up by high pressure field (see Fig. 4). By increasing m' to 2, the zero amplitude region remains roughly spherical at the center, but the high pressure surrounding it begins to open at the two sides. For $m' = 3$, the zero amplitude region turns completely into a cylindrical shape. These variations of the beam shape change the pressure gradient and therefore, intuitively impacts the radiation forces. Computing the forces varying the charge m' from 1 to 3, the amplitude of the axial force decreases as a result of the decrease of the pressure field

amplitude. For $m' = 3$, no axial trap is predicted due to the lack of pressure gradient at the center of the
 110 vortex in the axial direction. The axial force with $m' = 1$ is the largest owing its beam shape giving rise
 to the greatest pressure gradient. Therefore, the topological charge $m' = 1$ and radial degree $l = 8$ are
 selected to generate a spherical vortex with a good capability for trapping the target sphere.

Note that, in this study the scattering between several particles is not taken into account and we
 are considering the scattering of only one particle in the model. Indeed, the goal is to improve the
 115 spatial selectivity of the tweezers and as a corollary to minimize the number of particles insonified.
 Nevertheless, if more than one particle are initially located in the spatially focused trap, these particles
 may reach configurations where multiple scattering may be of importance and equilibrium configurations
 with several particles have already been observed [8]. For these cases, resonances may appear in the wave
 scattering process of bouncing back and forth between the particles. Theoretical modeling of these cases
 120 is still an open issue.

2.2. Experimental setup

The experimental setup is shown in Fig. 5. An array of 127 piezoelectric transducers (Vernon,
 France) with a central frequency at 1.2 MHz is held by a vertical support in a large water tank. The
 corresponding wavelength is $\lambda = 1.23$ mm in water at 20 °C where the speed of sound is about 1480 m/s.
 125 The surface of each transducer is a hexagon of 62.82 mm² and they fill a spherical cap with a focal
 distance equal to 45 cm. The total aperture of the transducer array is 110 mm. A high numerical aperture
 bi-concave lens machined in PMMA allows to reduce the focal distance to about 6 cm (see Fig. 5).
 Each transducer is driven independently by a multichannel electronic (Lecoeur, France). The 127 electric
 signals used to synthesize the ultrasonic beam are computed by inverse filter method (see section 3.1). A
 130 very thin polyethylene film (with thickness ≈ 15 μ m) that ensures minimal acoustic reflection is stretched
 on a bracket and is mounted on a three-axis motorized positioning system. The motors (ILS250, Newport)
 are powered and controlled by a remote command (Newport, MM-4006) with an accuracy of 5 μ m.
 Behind an optical window, an optical zoom image the area of interest and the image is recorded by a
 CMOS camera (Pointgrey Flea3). At the bottom of the vertical support, four wheels are fixed to move
 135 the array of transducers. The pressure field is measured with a hydrophone of 0.2 mm diameter (Precision
 Acoustics Ltd, UK).

Two kinds of polyethylene spheres were tested in our experiments: spheres with radii between $500\mu\text{m}$ and $590\mu\text{m}$ ($0.4\lambda - 0.47\lambda$) with density 1000 kg/m^3 (990 kg/m^3 - 1010 kg/m^3) and 960 kg/m^3 (960 kg/m^3 - 980 kg/m^3). The transverse and longitudinal velocities are estimated to be : $c_t = 1000\text{ m/s}$ and $c_l = 2400\text{ m/s}$ [31, 32].

Figure 5 shows the experimental setup in a configuration where the array of transducers is on the top oriented downwards. A second experimental configuration has also been used where the array of transducers is at the bottom and is oriented upwards. This second configuration is used to trap beads with density 960 kg/m^3 . In this case the polyethylene film prevents the bead from rising up.

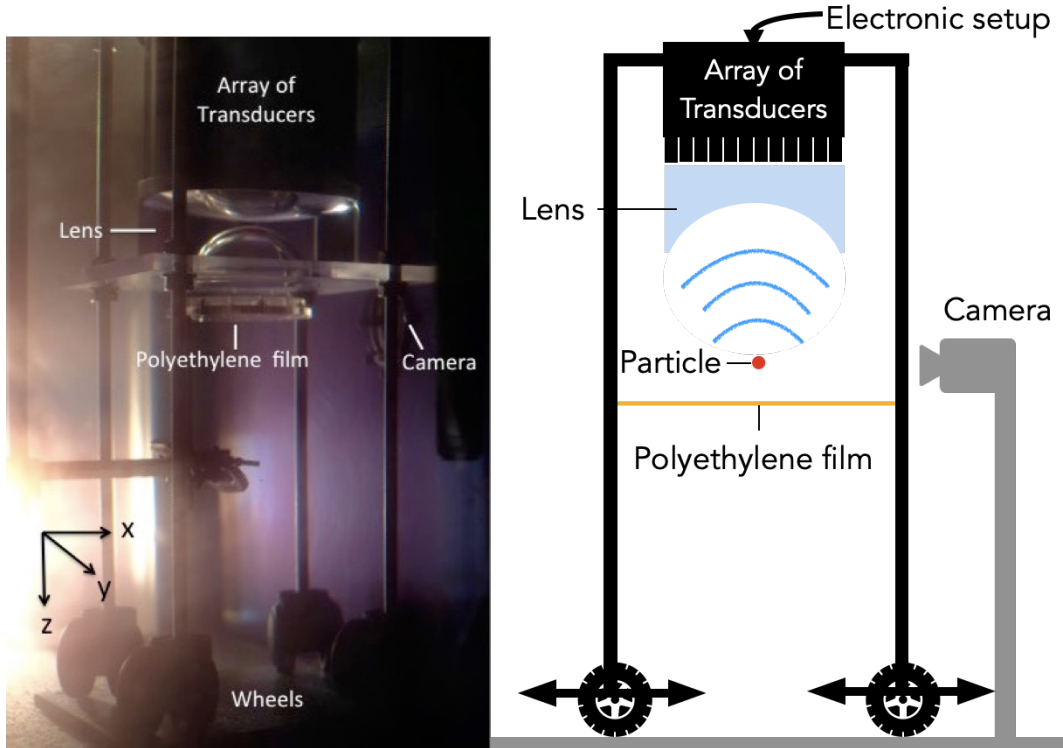


Figure 5: (color on line)Experimental setup: an array of transducers is positioned vertically with an acoustic lens to help the focusing; a polyethylene film is stretched on a bracket that is connected to a motorized positioning system.

3. Experimental results

3.1. Experimental synthesis of a spherical vortex

According to the analysis of section 2.1, a spherical vortex with topological charge $m' = 1$, radial degree $l = 8$ is chosen to trap the elastic spheres. An accurate synthesis of the wavefield is required to

achieve the desired trapping forces, especially the axial restoring force. With an array of transducers, multiple methods can be applied to synthesize the desired acoustic field, including time reversal [14], inverse filtering [38, 37] and integrative angular spectrum technologies [41]. Among these methods, inverse filtering is a very general technique for analyzing and synthesizing complex signals that propagate through an arbitrary linear medium. This method provides the optimal input signals to get a target wave-field. It consists of three steps: the first is recording the propagation operator of the propagation medium which completely characterizes the medium and the geometry of the experiment; the second is calculating the inversion of the propagation operator; and finally computing the optimal input for the transducer array.

We consider N control points whose positions are distributed in the volume of the medium. Let $f_j(t)$ be the signal received at the j th control point ($1 \leq j \leq N$) and $e_i(t)$ ($1 \leq i \leq M$) the signal emitted by the i th transducer. As the medium can be thought as a linear and time invariant system, these two signals are related by:

$$f_j(t) = \sum_{i=1}^M h_{ji}(t) * e_i(t), \quad (4)$$

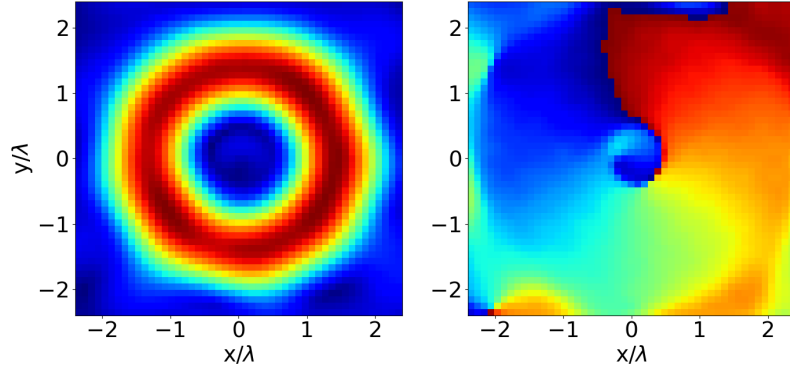
where $h_{ji}(t)$ is the impulse response between transducer i and control point j . The symbol ‘*’ denotes the convolution product. In the Fourier domain, this equation is transformed into a matrix/vector product: $\underline{F}(\omega) = \underline{\underline{H}}(\omega)\underline{E}(\omega)$, where $\underline{\underline{H}}$ is the frequency response of the system (size: $N \times M$), which describes the propagation of signals from the array of transducers to the control points and thus is called the propagation operator. The vectors $\underline{E}(\omega)$ (length: M) and $\underline{F}(\omega)$ (length: N) contain the spectra of the transmitted and received signals respectively. We aim to find the optimal signals to send ($\underline{E}$) by the array of transducers to generate the target field $\underline{F}$ on the control points after propagation. A naive approach consists in inverting directly this relation. However, the matrix $\underline{\underline{H}}$ is not square and cannot be inverted directly. Instead, the pseudo inverse is computed with a singular value decomposition, which allows adding a step of regularization through the choice of a cut-off in the singular values. Then, it is straightforward to get the emission vector to synthesize the target field $\underline{F}(\omega)$:

$$\underline{E}(\omega) = \underline{\underline{\hat{H}}}^{-1}(\omega)\underline{F}(\omega). \quad (5)$$

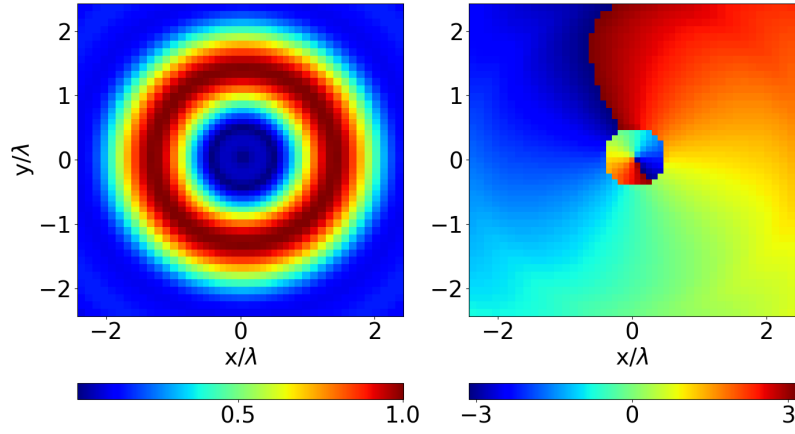
with $\underline{\underline{\hat{H}}}^{-1}(\omega)$ the regularized inverse propagation operator.

The spatial distribution of the control points is the key parameter determining the efficiency of the inverse filter method. To get a propagation operator that completely characterizes the medium, it is essential to over-sample the field in the area of interest. Among various trial distributions, we found that a regular distribution with 2500 points located in the focal plane (x, y) gives the best result. For this distribution, the sampling points are evenly distributed on a square surface with side length 6 mm (4.9λ) and with a step of 0.14 mm (0.11λ). At the center, inside a square of side length 2 mm (1.62λ), we refined the mesh and the step is decreased to 0.1 mm (0.08λ). This small step is required to properly sample the pressure field which varies rapidly in the center (see Fig. 6(b)).

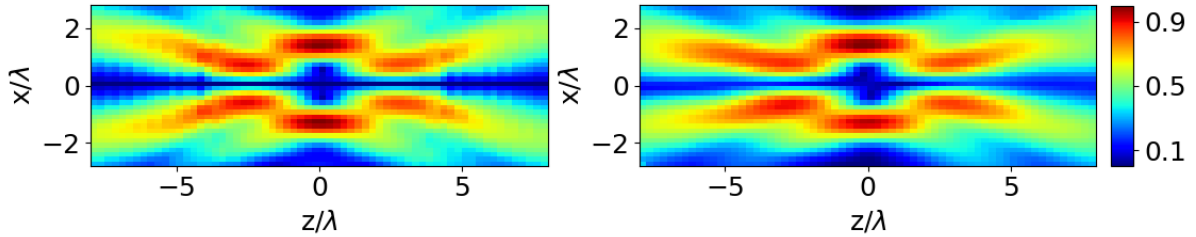
Once the emission vector is obtained, the associated pressure field is measured in the focal plane (x, y) and the axial plane (x, z) and then compared to the theoretical field (see Fig. 6). For the selected spherical vortex of charge $m' = 1$, radial order $l = 8$ and aperture angle $\alpha_0 = 49^\circ$, it appears from the figure that the high-amplitude ring is well recovered with good uniformity of amplitude. Inside the ring, the field is at zero amplitude and again is in agreement with the target theoretical one. Even though the variation of phase inside the small circle in the center is smeared out in the measured field, the global variation of the phase is in good agreement with the theoretical one. The modulus in axial plane (x, z) is similar to the theory as expected.



(a) Modulus and phase of the complex pressure field in plane (x, y) (experimental measurements).



(b) Modulus and phase of the complex pressure field in plane (x, y) (theoretical pressure field).



(c) Modulus of the complex pressure field in plane (x, z) : theoretical (left) and experimental (right).

Figure 6: (Color online) Experimental and theoretical modulus and phase of the complex pressure field in plane (x, y) and (x, z) for a spherical vortex beam with $m' = 1$, $l = 8$ and $\alpha_0 = 49^\circ$

175 Furthermore, from the measurement of the field in focal plane (x, y) , we can also compute the BSC and thus obtain the radiation forces by the angular spectrum method [44]. The radiation forces computed from the measurements are given in Fig. 7. We find a good agreement with the theoretical forces,

especially for the axial force F_z for which the discrepancy is less than 10%. The latter confirms the high quality of the synthesis of spherical vortex beams for this distribution of control points.

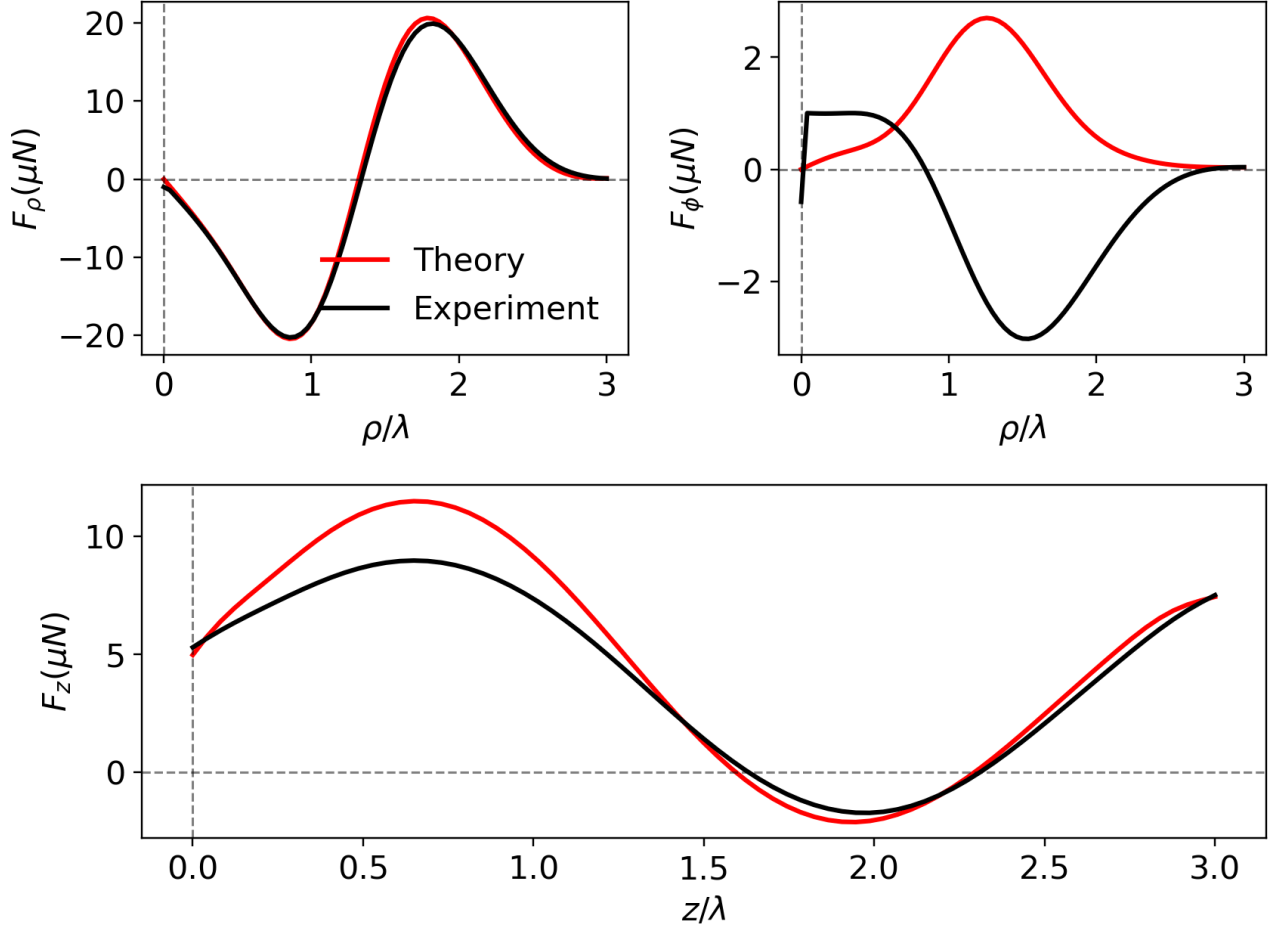


Figure 7: (Color online) Theoretical and experimentally estimated radiation force exerted on a polyethylene sphere of radius $a = 0.45\lambda$ by a focused spherical vortex beam of topological charge $m' = 1$, $l = 8$.

Nevertheless, regarding the emission vectors obtained by the standard inverse filter method, the energy is mainly distributed on the first 20 transducers located in the middle and the other 100 transducers have barely no contribution to the pressure field. Each electronic channel can deliver high power, 25 W, but for pulse signals only. Experiments of trapping and manipulation require tens of seconds of duration and hence the emitted power must be decreased. Taking into account the weight of our large targeted spheres, the applied axial force has to be as large as possible. For this reason, the emission vector is modified to increase the axial force in order to make optimal use of all the transducers and, at the same

time, increase the amplitude of the high-amplitude ring.

Thus the following modifications are made: first of all, for each transducer, the emitted signals are normalized $e_i(t_n)/\max_n(e_i(t_n))$, where i is the index of the transducer (from 1 to 127) and n is the index of the time sample. Then, each signal is scaled by a new amplitude factor equal to:

$$\left(\max_n(e_i(t_n)) / \max_i\left(\max_n(e_i(t_n))\right)\right)^\beta \quad (6)$$

with β equal to 1, 0.5 or 0.25. By applying these modifications, the number of signals with significant amplitude increases. Meanwhile, the pressure field radiated and measured is also changed. In Fig. 8, the
190 top row is the field measured with the original emission vector, $\beta = 1$ and then going downward $\beta = 0.5$ and finally $\beta = 0.25$. In plane (x, y) , the high-amplitude rings keep the same pattern. While inside the rings, the pressure modulus is no longer zero and the phases have also been modified. Moreover, the differences between the pressure field measurements in plane (x, z) are also clearly visible.

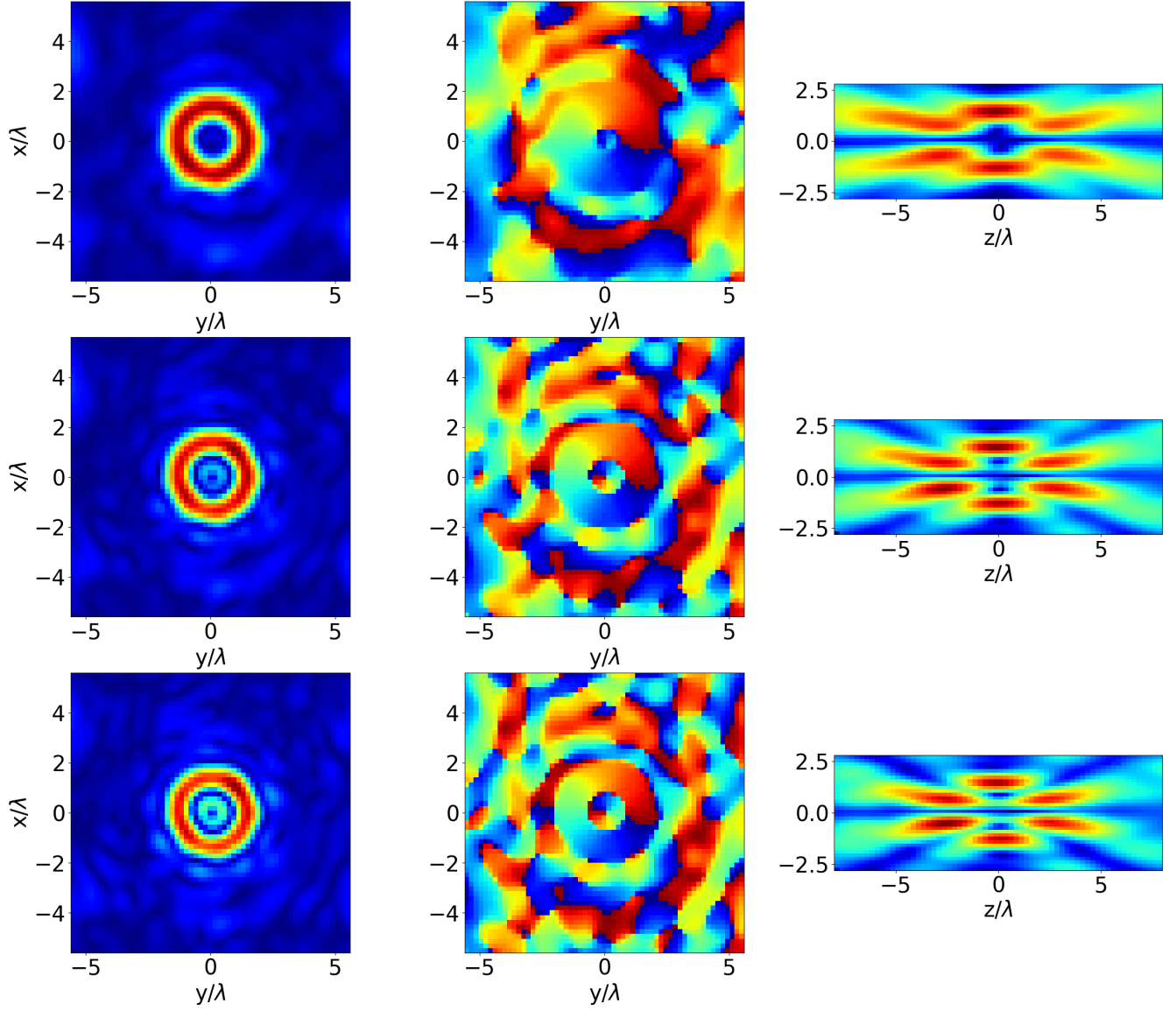


Figure 8: (Color online) Modulus (Left) and phase (Middle) of the complex pressure field in plane (x, y) with modulus (Right) of the pressure field in plane (x, z) for a spherical vortex beam with $l = 8$, $\alpha_0 = 49^\circ$. From top to bottom: $\beta = 1, 0.5, 0.25$.

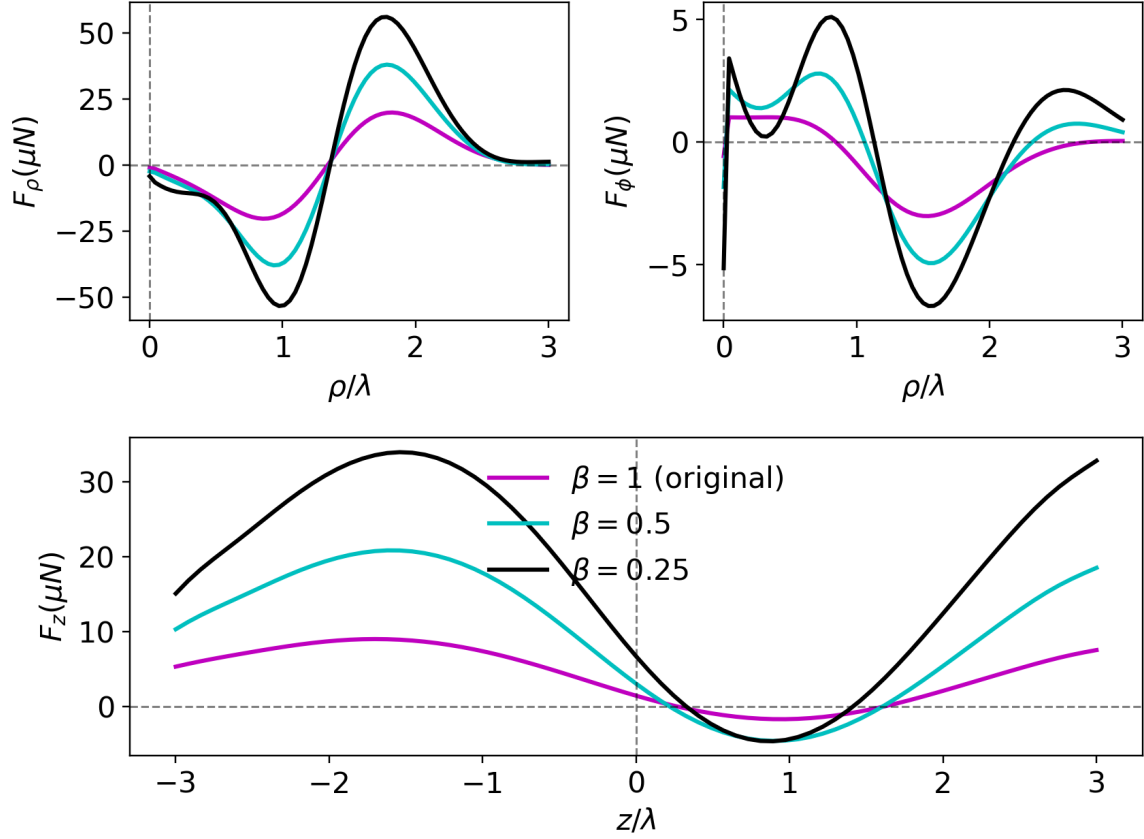


Figure 9: (Color online) Experimentally estimated radiation force exerted on a polyethylene sphere of radius $a = 0.45\lambda$ by a focused spherical vortex beam of topological charge $m' = 1$, $l = 8$ synthesized by different emission vectors with $\beta = 1$ (original), 0.5, 0.25.

In order to evaluate the impact of these modifications on the radiation forces quantitatively, we use again a calculation method based on the angular spectrum method which allows to estimate the radiation forces from the measured pressure fields [44]. As depicted in Fig. 9, by modifying the emission vector $\underline{E}$ from the origin up to $\beta = 0.25$, the amplitude of the radial force increases and the trap in radial direction remains always. For the axial force, when $z < 0$, the force is positive and increases notably with the decrease of the coefficient β . The maximum positive force with $\beta = 0.25$ is four times larger than the original one. However, when the sphere is located behind the focus ($z > 0$), the maximum amplitude of the restoring force increases until $\beta = 0.25$ and then decreases. Thus, according to the trapping performance illustrated by the radiation forces, the exponent $\beta = 0.25$ is optimum and should be sufficient to overcome the weight of light spheres. This modification is used in the trapping experiments

presented in the next section.

3.2. *Experimental trapping with a spherical vortex*

3.2.1. *Localization of the trapping zone*

One feature of the single side acoustical tweezers is to have a tight trapping zone. It means that the object can be trapped only in a very small region of the space, which is a very appealing property ensuring a very good selectivity of the device. Therefore, prior to any manipulation task, the trapping zone has to be found accurately. This is done with the hydrophone. The pressure field of the vortex in transverse plane (x, y) has a zero amplitude zone at the center surrounded by a high-amplitude ring as shown in Fig. 1(b). At the focal plane, the amplitude of the ring reaches its maximum amplitude. The focal position of the vortex can be found by these characteristics. Once the hydrophone is successfully positioned at the focus, we then adjust the position of the camera to get a clear picture of the hydrophone, and at the same time make sure that the hydrophone is at the center of the image. This step of fixing the focal position allows later to locate the sphere at the trapping area of the vortex.

3.2.2. *Axial and radial traps*

Once the trapping zone is located by the hydrophone, the target beads are placed on the acoustically transparent membrane. By moving the membrane with the motorized positioning system, it is easy to move the target bead in the trapping zone of the spherical vortex beam. Once the bead is positioned inside the trapping zone, the spherical vortex is emitted to trap it. It should be noticed that since two types of polyethylene beads with different densities are used, two experimental setups are used. To trap the beads with density higher than water, the experimental setup used is the same as in Fig. 5. However, for the beads which float, the transducer array is placed under the membrane. During the experiments, once the field is activated, the membrane is moved transversely and axially. Particles could be selected individually and relatively to the membrane moved transversely. Fig. 10 shows three snapshots of such an experiment, see also video of the bead trapped and moved by the acoustic tweezers. We can see that the selected bead located in the center is radially trapped. Indeed while moving the polyethylene film, this particle doesn't move with the film and stays in the same position while other beads located in the surrounding and not trapped are moving with the membrane and appear in the camera field of view. On the contrary, no axial trap was observed during the experiments: when the membrane is moved in the

direction of propagation of the waves, the bead also moves. The reasons responsible for the failure of the axial trap have caught our attention and are discussed in the following sections.

Figure 10: Snapshots of a polyethylene sphere trapped radially by a spherical vortex. A movie is available on line showing the bead trapped and moved laterally by the tweezers.

4. Discussion and conclusions

235 4.1. *The resonance of the spheres*

Despite the theoretical predictions and the good wavefield synthesis, only the radial trap has been observed and no evidence of the axial trap have been found. Even though the emission vectors have been modified to ensure a negative axial force larger than the sphere weight, this was not strong enough to take off the sphere. In the following section, we revisit the numerical evaluation in order to detail the
240 choice of parameters (material, size) selected to ensure an efficient trapping. According to our estimation of the axial forces for a polyethylene sphere of different radii, the trapping capability of the spherical vortex, especially the axial trap, is not constant. As depicted in Fig. 11, among the radii tested for the polyethylene spheres $a = 0.41\lambda$, $a = 0.45\lambda$ and $a = 0.48\lambda$, the radial trap exists always. On the contrary, only the sphere with $a = 0.45\lambda$ can be trapped axially.

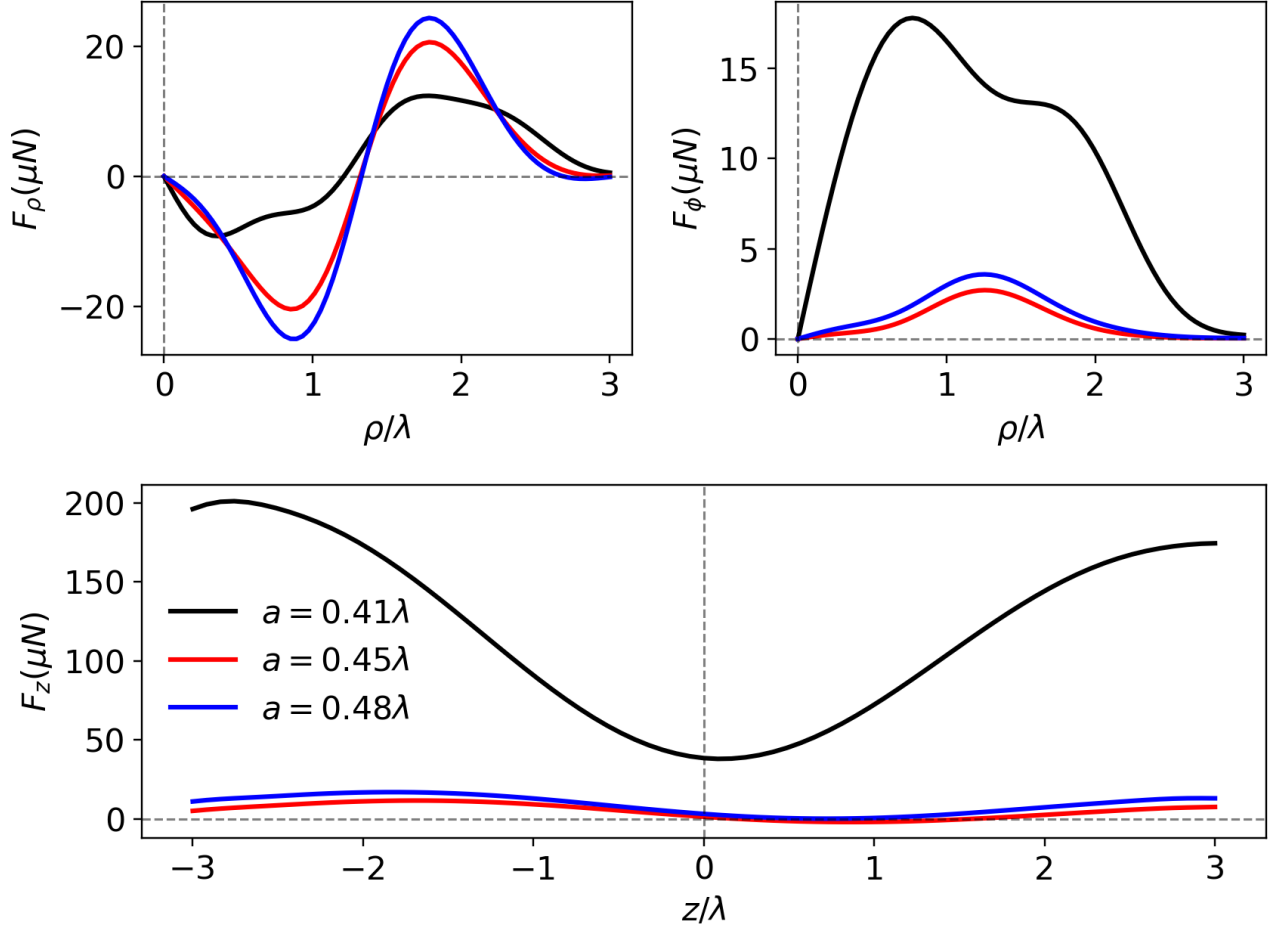


Figure 11: (Color online) Radial F_ρ , azimuthal F_ϕ , axial F_z forces exerted on a polyethylene sphere of radii $a = 0.41\lambda$, $a = 0.45\lambda$, $a = 0.48\lambda$ by a spherical vortex beam.

Therefore, to succeed in trapping the particles experimentally, it is important to test the range of sizes and materials that can be trapped, especially in the axial direction of a spherical vortex. The negative force in the axial direction is the key to trap the particles. Thus, the determination of the suitable range of sphere sizes requires only to compute the axial force at a position where the negative force is most likely to appear. This kind of analysis on negative axial force was first demonstrated for a Bessel beam [27]. Note that the maximum axial restoring force exerted by a spherical vortex at frequency 1 MHz is about $5\mu\text{N}$ (see Fig. 11), however the volume of the sphere is about 1mm^3 which limits the choice of sphere materials to light polymer spheres with density comparable to water. Therefore, only light spheres like polyethylene and polystyrene are analyzed in this section. According to Fig. 11, for instance, at $z = 0.9\lambda$

the axial force is negative with a maximum amplitude for a polyethylene sphere of $a = 0.45\lambda$. In Fig. 12(a), the axial force at $z = 0.9\lambda$ as a function of sphere radius is represented. As illustrated in the figure, from $a = 0.2\lambda$, the resonances begin to appear in the axial force and thereafter regions for which the axial force is negative alternates with regions where the force is positive. In the figure, the zone where $F_z < 0$ represents the range of sphere radius that can be trapped. Only the spheres with radii between $(0.42\lambda$ and $0.47\lambda)$ or $(0.5\lambda$ and $0.54\lambda)$, $(0.59\lambda$ and $0.64\lambda)$ have a negative force and therefore can be trapped by the spherical vortex. This result agrees with the force estimation in Fig.11, since the spheres of radii $a = 0.41\lambda$ and $a = 0.48\lambda$ are at the resonances of the axial force, it is impossible to trap them axially. These resonances of the force come from the resonances of the scattering coefficients R_n . The expression of the axial force [6] can be calculated with :

$$F_z = -2 \frac{\langle V \rangle}{k_0^2} \sum_{n=0}^{\infty} \sum_{|m| \leq n} \Im(G_n^m A_n^{m*} A_{n+1}^m C_n). \quad (7)$$

With:

$$\begin{aligned} V &= p_a^2 / (4\rho_0 c_0^2), \\ C_n &= R_n^* + R_{n+1} + 2R_n^* R_{n+1}, \\ G_n^m &= \sqrt{(n+m+1)(n-m+1)} / \sqrt{(2n+1)(2n+3)}. \end{aligned}$$

where A_n^m are the BSC defined by Eq. 3, C_n is a function of the scattering coefficients R_n ; p_a is the linear component of the acoustic pressure; ρ_0 and c_0 are the fluid density and speed of sound at rest respectively. In Fig. 12(b), the modulus of C_n is plotted for a polyethylene sphere as a function of radius. Comparing Fig. 12(a) and Fig. 12(b), the resonances in C_n locate at the same positions as the resonances observed in the axial forces. The figure also illustrates that for $a < 0.6\lambda$, the coefficients C_n with $n > 6$ can be neglected since from $n = 6$ the amplitudes become weak. As the force is a sum on degree n of function:

$$\hat{f}_z^n = -\Im(G_n^m A_n^{m*} A_{n+1}^m C_n). \quad (8)$$

245 The contribution of $\hat{f}_z^n$ to the negative force at each degree n can be computed by Eq. (8). In Fig. 12(c), the $\hat{f}_z^n$ until degree $n = 6$ are depicted. Taking the trapping region between 0.42λ and 0.47λ as an example, according to the figure, $\hat{f}_z^n$ with negative amplitudes that contribute to the final negative force

are at degrees $n = 2$, $n = 3$ and $n = 4$.

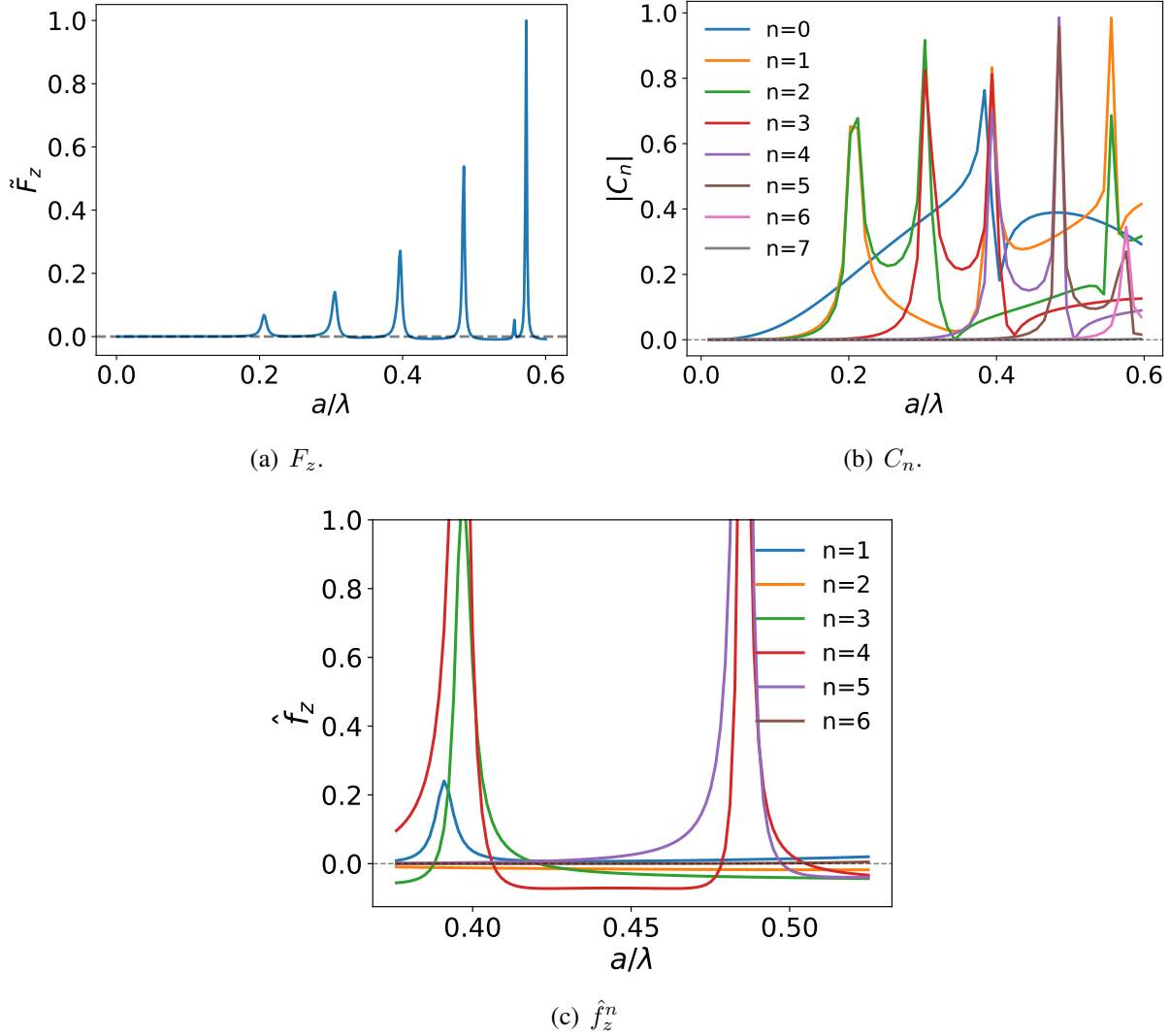


Figure 12: (Color online) (a) Normalized axial forces $\tilde{F}_z$ exerted on a polyethylene sphere positioned at $z = 0.9\lambda$ as a function of sphere radius by a spherical vortex ; (b) Modulus of C_n as a function of sphere radius for a polyethylene sphere; (c) $\hat{f}_z^n$ as a function of sphere radius for different degrees until $n = 6$ for a polyethylene sphere.

In order to find the relation between the coefficients C_n and its contribution to the negative force, the coefficients C_n of polyethylene sphere at degree $n = 2$, $n = 3$ and $n = 4$ are depicted in Fig. 13(a) and 13(b). In the figure, the region within which the negative force appears is highlighted by two gray dashed curves. In the trapping region, the modulus of C_n as well as the phase are constant and located between two resonances. The phase inside the trapping region is approximately $\frac{\pi}{2}$. As the axial force component

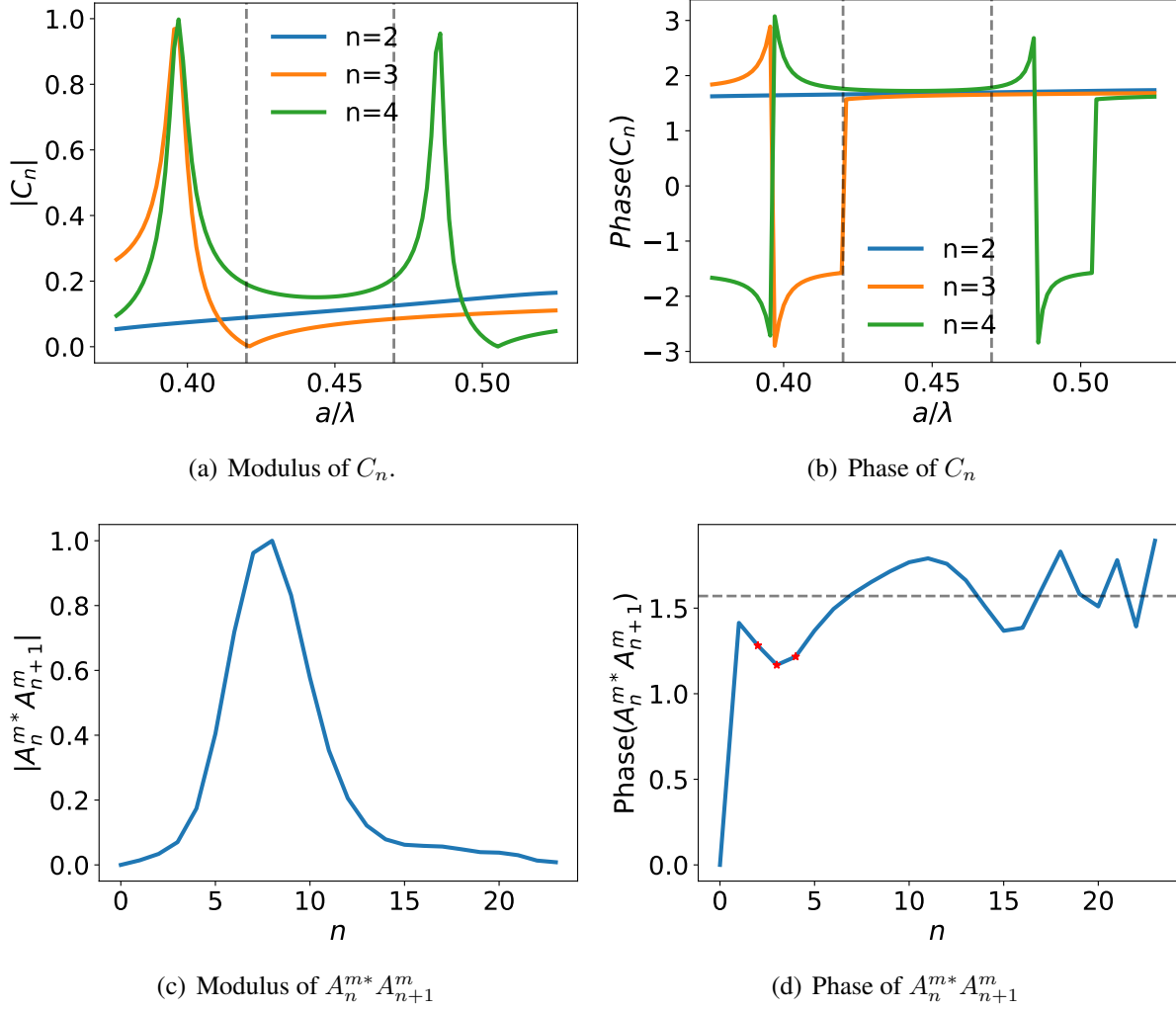


Figure 13: (Color online) (a) Modulus and (b) phase of C_n as a function of radius at degrees $n = 2, n = 3, n = 4$ for a polyethylene sphere; (c) Modulus and (d) phase of $A_n^{m*} A_{n+1}^m$ as a function of degree n .

for each n is the opposite of the imaginary part of the product of $A_n^{m*} A_{n+1}^m$ and C_n , the axial force is negative when the phase is inferior to π . In Fig. 13(c) and 13(d), the modulus and phase of $A_n^{m*} A_{n+1}^m$ are plotted. Even though the maximum of the modulus is at $n = 8$, the corresponding phase is however above $\frac{\pi}{2}$ (the gray dashed line represents the position where the phase is $\pi/2$), since the phase of C_n is equal to $\frac{\pi}{2}$, the phase of the product is then equal or superior to π and does not contribute to the axial restoring force at all (for a value of π) and will, on the contrary, push away the sphere for values superior to π . Meanwhile, at degree $n = 2, n = 3$ and $n = 4$, the phases of $A_n^{m*} A_{n+1}^m$ are the smallest and located below $\frac{\pi}{2}$ which finally contributes to the negative restoring forces.

The trap capability of the spherical vortex on a polystyrene sphere can be examined in the same way. The axial force exerted on a polystyrene sphere at position $z = 0.9\lambda$ as a function of the polystyrene sphere radius is computed and shown in Fig. 14(a). According to the figure, the negative force appears
 265 at some of the radii but the amplitude is very weak. For one of the regions between $a = 0.46\lambda$ and 0.49λ , the $\hat{f}_z^n$ are plotted in Fig. 14(b). The $\hat{f}_z^n$ contributing to the negative force are at degrees $n = 2$, $n = 3$, $n = 4$ again. Then we plot the coefficients C_n as shown in Fig. 14(c) and 14(d). Similar to the polyethylene sphere, inside the trapping zone, the modulus and phase of C_n are constant. The phases at degree $n = 2$, and $n = 3$ are close to $\frac{\pi}{2}$ while at degree $n = 4$, the phase is larger and is equal to $\frac{2\pi}{3}$. As
 270 the sum of C_n phase and $A_n^{m*} A_{n+1}^m$ phase at $n = 4$ is close but less than π this results in a small negative force. Moreover, since the sinus function (the imaginary part) decreases linearly around π , a decrease of phase thus results in a proportional increase of the modulus of the negative force.

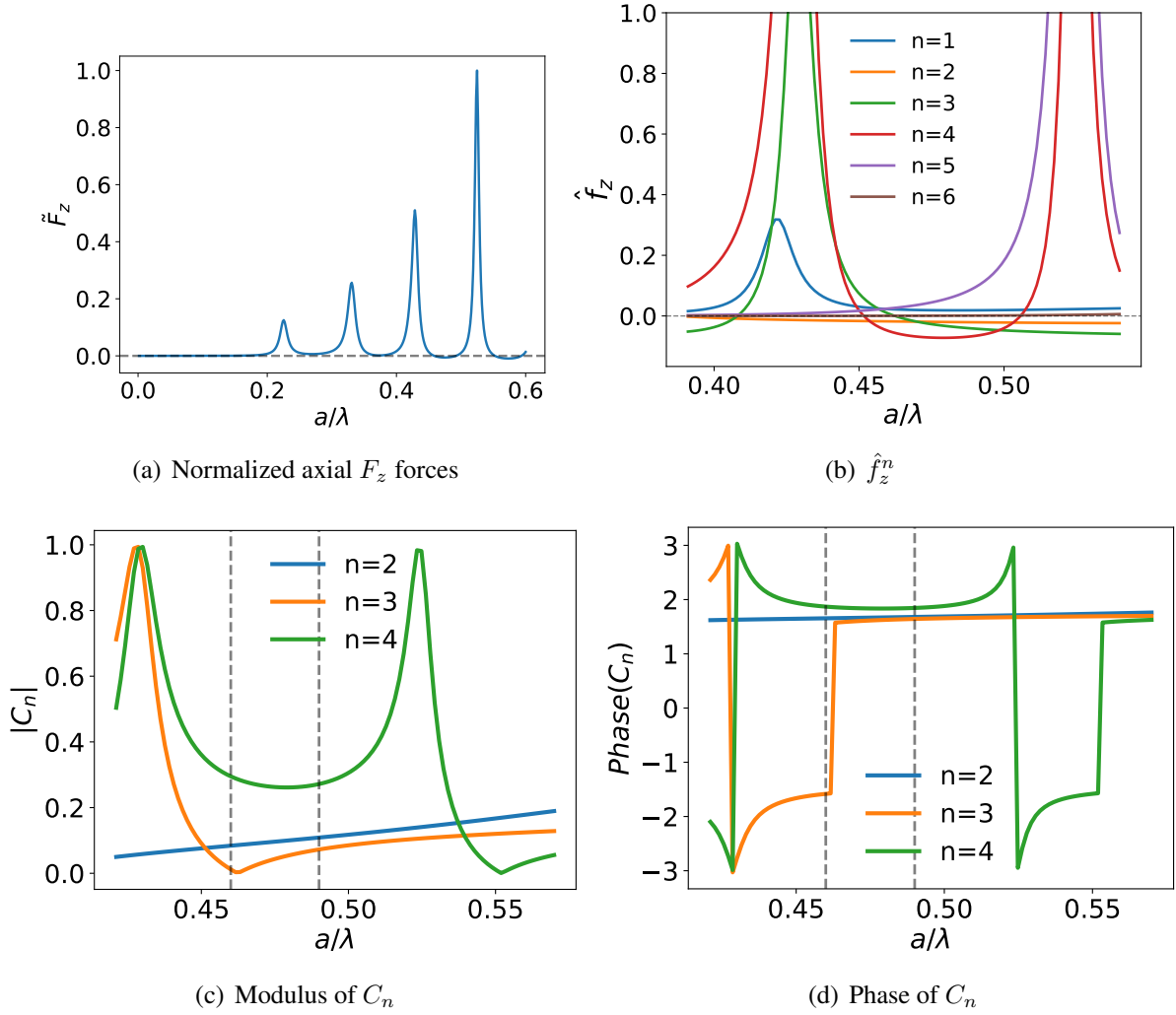


Figure 14: (Color online) (a) Normalized axial F_z forces exerted on an polystyrene sphere positioned at $z = 0.9\lambda$ as a function of sphere radius; (b) $\hat{f}_z^n$ as a function of sphere radius for different degrees until $n = 6$; (c) Modulus and (d) phase of C_n as a function of sphere radius at degrees $n = 2, n = 3, n = 4$ for a polystyrene sphere.

4.2. Influence of the BSC

As the scattering coefficients C_n of a polystyrene sphere depends only on its physical properties, the only way to trap a polystyrene sphere is to adjust the BSC of the spherical vortex beam to give rise to the negative force. The BSC of a spherical vortex, as demonstrated in the previous section, can be modified by changing the aperture angle α_0 , the radial degree l , or topological charge m' . Taking the radial degree l as an example, in Fig. 15(a) and 15(b), the modulus and phase of $A_n^{m*} A_{n+1}^m$ with different radial degrees are shown. The gray dashed lines highlight the radial degrees of interest. Looking at the phases of

280 each radial degree, the $l = 8$ gives rise to a phase significantly below $\pi/2$ in the region of interest and
 hence potentially to a large negative force. However, the modulus of the $A_n^{m*} A_{n+1}^m$, at the same degree n ,
 decrease when l increases and this trend is in favor of the smallest l . Therefore the impact of changing
 the radial degree l on the negative force is not obvious. In Fig. 15(c), $\hat{f}_z^n$ as a function of polystyrene
 sphere radius with different radial degrees l selected to compute the the BSC are shown. From the figure,
 285 the BSC with radial degree $l = 8$ lead to the most significant negative force. In spite of the fact that
 the modulus of $A_n^{m*} A_{n+1}^m$ at $n = 2, 3, 4$ with $l = 8$ are smaller than those computed with $l = 6$, and
 $l = 7$, they have a smaller phase at the same time. Thus again, this result emphasizes that the phase of
 the scattered waves relative to the incident one is the main feature leading to a large enough negative
 restoring force and hence a 3D trapping.

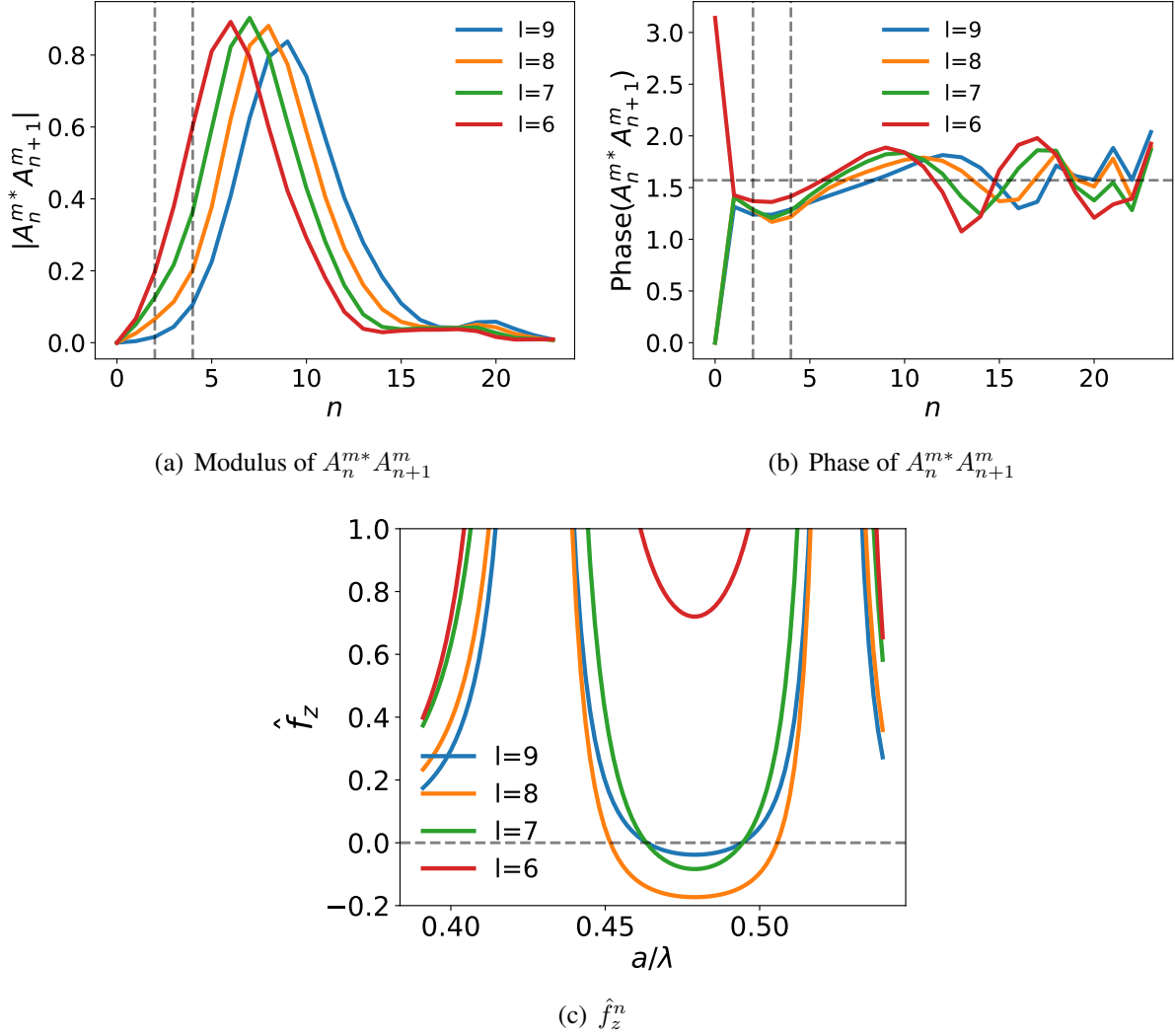


Figure 15: (Color online) (a) Modulus and (b) phase of $A_n^{m*} A_{n+1}^m$ as a function of degree n for different radial degrees l ; (c) $\hat{f}_z^n$ at degree $n = 4$ as a function of sphere radius for different radial degrees l .

4.3. Conclusions

In conclusion, diffraction in the far-field limits the focal spot to a size larger than about one wavelength, therefore achieving acoustical tweezers with optimal selectivity means trapping object of about the size of the tweezers and hence of about one wavelength also. However for such large objects, the modes have resonances due to creeping waves or anti-resonances around which the phase and the amplitude of the modal reflection coefficient vary rapidly. Since the trapping ability of a spherical vortex is strongly dependent on the phase of the scattered wave relative to the incident one, this effect leads to

a reversal of the radiation force direction. Different kinds of acoustical vortices were assessed. As anticipated, the so-called spherical vortices with their peculiar energy density that seems to bypass a zone where ultrasound is canceled give the best results. The sharp energy density gradient in both radial and axial directions are favorable for a strong restoring force in all directions. With such fields, we predict that 3D trapping can be achieved between two resonance peaks for spheres of about one wavelength in diameter and with an axial force strong enough to exceed the sphere weight. While we observed radial trapping, the axial force obtained experimentally was not sufficient to lift the sphere. Several explanations are possible for this partial failure. First the physical properties of the polymer sphere are not well characterized. A change of the speed of sound for either shear or longitudinal waves will result in a variation of the speed of sound of the creeping waves and hence a shift in frequency of the resonances. Moreover, these polymers are visco-elastic and the acoustic attenuation will contribute to pushing the sphere and hence the axial restoring force is decreased. Since this parameter is not known, we did not try to estimate the amplitude of this effect. Second, there are electrical static forces between polyethylene spheres and a surfactant must be used to disperse them in water. Since our membrane is also in polyethylene, we did observe that a static force occurs between the spheres and the membrane. The amplitude of this static force is difficult to estimate and to mitigate but has to be overcome by the axial radiation force to take off the sphere. So, it may be possible that the force is enough to compensate the weight but too small to compensate the weight and overcome the short ranged static force that exists when the sphere lies on the membrane. In this study, the relatively low frequency and hence relatively large wavelength leads to polymer materials for which the density contrast with the fluid is weak to mitigate the weight of the object. Such constraint will not exist if we scale down the experimental conditions. Indeed, the sphere weight is proportional to its volume and hence decreases with the cube of the wavelength and hence faster than the radiation force amplitude. Denser materials are generally much more stiffer than polymers and therefore the speed of sound is higher. Such conditions are favorable since the resonances will be shifted to a higher ratio between the radius and the wavelength in water. Moreover material like glass are well characterized, the attenuation can be neglected and no electrical force with the membrane is expected. A numerical method efficient enough to search for the parameters (numerical aperture, elastic constants, frequency...) allowing to obtain a trap in the three directions must be developed to carry out this task.

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