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Automated fibre placement process for a new hybrid material: A numerical tool for predicting an efficient heating law

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Abstract

An innovative hybrid thermoplastic manufacturing process has been investigated, which consists in carbon fibres reinforced poly(ether-ether-ketone) (PEEK) prepreg sandwiched between two amorphous polyetherimide (PEI) films. By using a laser-assisted automated fibre placement (AFP), a laminate is produced by the deposition of hybrid prepreg tapes, layer-by-layer without using autoclave. The temperature history control is required to ensure good consolidation throughout the part. This depends on the optical behaviour of the hybrid material, which is also subjected to the influence of process parameters. Before determining the optical properties of the new hybrid material, the correlation between these process parameters has been established based on the interaction of laser spot with PEI film and PEEK/carbon fibres tape. Then, the thermal distribution in the laminate is obtained via an optico-thermal model and

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validated with experimental results. Finally, a heating law for the AFP process is established using iterative numerical simulations. *Keywords:* Laser-assisted automated fibre placement, New hybrid

thermoplastic composite, Optico-thermal analysis, Heating law

1. Introduction

The interest of thermoplastic composite materials by using an additive manufacturing (AM) out of autoclave is in continuous evolution due to their promised benefits in terms of work time and costs [1, 2, 3]. In this regard, a new hybrid thermoplastic composite material has been developed to answer to the needs for reduced weight and consequently reduced fuel consumptions 5 and emissions of aircrafts, as well as reduced manufacturing and operational costs, since it does not require the use of an autoclave curing phase. Indeed, the proposed high-performing material is based on a commercial semi-crystalline PEEK-carbon fibre prepreg (called APC-2) embedded in amorphous (PEI) film. Therefore, this hybrid material allows to manufacture 10 advanced composite aerostructures by fast and automated processes, such as automated fibre placement (AFP) machines equipped with high-power laser-diodes, at a temperature just above the glass transition temperature (T_q) of the amorphous layer and lower than the fusion temperature (T_f) of the semi-crystalline APC-2 in order to preserve its optimal degree of 15 crystallinity [3, 4, 5, 6].

The present study aims to improve the productivity of automated laser fibre placement through hybrid material analysis which involve three steps such as heating, melting and solidification to produce good finished

- ²⁰ parts [7, 8, 9, 10, 11]. To control these steps, a complete comprehension of the laser distribution on the heated surfaces and the thermal history of laminate during process is required [9, 12]. Generally, the temperature history control on the tape placement needs to know the energy distribution on the surface and through the thickness of the composite [7]. In the case
- ²⁵ of the thermoplastic composite tape made with continuous unidirectional fibres, near-infrared (NIR) diode lasers are promising sources to melt the thermoplastic and are able to provide higher heat fluxes in near instantaneous response time [13, 14, 15, 16]. The laser interaction with thermoplastic composites can be estimated using a ray-tracing method [13, 16, 7]. For
- instance, Grouve [7] investigated the energy input distribution on the carbon/PPS unidirectional surfaces generated by a laser optic source. A 2D ray-tracing method including the reflectance phenomena was developed to calculate the flux distribution in the substrate and incoming tapes. Stokes-Griffin and Compston [9] evaluated the heat input on APC-2 material
- ³⁵ using a 3D ray-tracing model developed in CAD. Dolo [13] and Baho et al. [17] developed a 2D ray-tracing method by taking into account the reflection phenomena under the roller deformation and the effects of the AFP process parameters. The data from these ray-tracing models are then used as heat input distribution for thermal models in order to determine the temperature
- ⁴⁰ distribution in the material. A knowledge of this distribution helps to establish relevant heating laws in terms of speed and laser power input, and to avoid excessive high temperatures, which can degrade the polymer [4]. Kollmannsberger et al. [18] conducted a more realistic thermal model by considering thermal contact resistances and non-uniform laser heat inputs.

⁴⁵ Analytical solutions have been presented in [19, 20]. For instance, Weiler et al. [19] developed a simplified analytical model to control the temperature distributions and the surface temperature of the substrate. Francesco et al. [20] proposed a semi-empirical thermal model which is used to keep constant the nip-point temperature in terms of laser power and layup speed.
⁵⁰ However, the use of numerical models is still the best method to model the AFP process without reducing the number of assumptions considered in analytical solutions.

In the case of the thermoplastic composite, the optico-thermal models previously developed on the AFP treat standard prepreg tapes. Generally, ⁵⁵ these ribbons consist of a thermoplastic matrix reinforced with carbon fibres. The required temperature applied during the AFP process to join two parts by fusion and consolidation depends on the type of thermoplastic matrix. For amorphous materials, the required temperature will be higher than the transition temperature while the one for semi-crystalline matrice ⁶⁰ will be above the melting temperature [21, 22]. The aim of this work is to characterize and analyze the manufacturing process of a new hybrid thermoplastic composite (HTPC) combining an amorphous material and semi-crystalline reinforced with carbon fibres.

In this paper, the optical and thermal behaviours of a HTPC under the effects of the AFP head parameters are modelled. The HTPC tape is produced by the combination of the aromatic polymer composite (APC-2) embedded in two PEI films. In AFP process, the laminate is produced layer by layer in which the incoming tape and substrate are consolidated by heating their respective surfaces and applying a pressure load. The most

- ⁷⁰ sensitive process parameters to achieve a good consolidation between the different layers without degrading the thermoplastic are the temperature in the consolidation area (i.e., nip-point process), the layup speed and the roller compaction force. These parameters need to be well controlled so that they stay within a specific optimum parameter range. Furthermore,
- ⁷⁵ the laser-heating system is chosen as the heat source in the simulations. In particular, the use of lasers as a heating source puts very high requirements on the process control system. For this reason, a ray-tracing procedure is developed in MatLab software, based on geometric optics to determine the laser heat-flux distribution on the composite. Additionally, the ray-tracing
- ⁸⁰ method requires to know the thermal radiative properties of HTPC, which are characterised and evaluated in terms of the angle of incidence, the wavelength, the head tilt and the roller deformation. After computing the radiative source term, these data are used to calculate the temperature distribution on the surface and through the thickness of the composite by performing finite element analyses with the commercial software Abaqus.

2. Thermo-optical properties

This section deals with some optical properties and thermal characterisations of the HTPC, which represents the main key to investigate the interaction between the laser beam and the laminate during the AFP process.

2.1. The new hybrid material

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Fig. 1 shows the HTPC which consists of two PEI films overlying PEEK/carbon fibres material. PEI is an amorphous polymer with a reported

 $T_g = 217^{\circ}C$, while PEEK is a semi-crystalline polymer with $T_g = 143^{\circ}C$ and a ⁹⁵ melting temperature $T_m = 343^{\circ}C$. The addition of amorphous PEI film to the commercial PEEK/carbon fibres (APC-2) aims to improve the processability of crystalline PEEK [23, 24, 25]. The hybrid material is obtained by heating both a commercial APC-2 and two PEI films over the melting temperature of PEEK. The consolidation step is carried out by a continuous process under ¹⁰⁰ controlled parameters (i.e., temperature distribution, pressure, time, feeding

- speed rate) [23]. The initial thicknesses of the PEI and PEEK/carbon fibres films before this consolidation step are $t_{PEI} = 50 \ \mu m$ and $t_{APC-2} = 127 \ \mu m$, respectively. After consolidation of three layers constituting the hybrid material, the thickness obtained is greater than the sum of the nominal
- thicknesses (Fig. 1). This can be justified by the morphological change of the material occurred during the continuous material production process. Specifically, the mixing between PEEK and PEI phases promotes the growth of the APC-2 / PEI interface, which is caused by a decrease in PEEK crystallinity. This has also been observed by Alvaredo-Atienza et al. [26].
- Finally, the HTPC is split to a width of 6.35 mm and placed on bobbins for feeding the AFP machine.

2.2. Optical properties

One of the most important requirement for accurately controlling laser-material interaction is the optical properties as a function of the laser ¹¹⁵ wavelength and incident angle such as complex refractive index, reflection and penetration depth of laser irradiation. Generally, when a laser beam strikes a material surface, part of its energy is reflected, another absorbed and the rest can be transmitted through material. The amounts of absorption, reflection



Fig. 1: Cross-section of the hybrid thermoplastic composite (HTPC)(a): SEM observation; (b): Schematic representation

and transmission depend on the wavelength λ of the incident beam and the fiber orientations [27, 28]. The spot size, including the laser intensity distribution and profile, is another parameter that should be considered especially in the case of the laser divergence.

For the HTPC material, three materials are in interaction with the laser beam as depicted in Fig. 2.



Fig. 2: Interaction of light with HTPC

¹²⁵ The optical properties of the hybrid material may be deduced from the

complex index of refraction of its constituents $N_{APC-2}(\lambda) = n_{APC-2}(\lambda) - ik_{APC-2}(\lambda)$ and $N_{PEI}(\lambda) = n_{PEI}(\lambda) - ik_{PEI}(\lambda)$, where *n* the real part and *k* is the extinction coefficient. This allows to determine the absorption α of the laser irradiation by the material as a function of the wavelength such as 130 $\alpha = 4\pi k/\lambda$.

Measurements of reflectance R_{PEI} and transmittance T_{PEI} are conducted on the PEI film sample by using a spectrometer with an integrating sphere working from ultraviolet to NIR. Therefore, the complex refractive index is obtained from the following analytical expression [29]

$$n_{PEI}\left(\lambda\right) = \frac{1+R\left(\lambda\right)}{1-R\left(\lambda\right)} \sqrt{4 \frac{R\left(\lambda\right)}{\left[1-R\left(\lambda\right)\right]^2} - \left[k_{PEI}\left(\lambda\right)\right]^2} \tag{1}$$

$$k_{PEI}(\lambda) = \frac{\lambda}{4\pi t_{PEI}} \log \left(\frac{R(\lambda) T_{PEI}(\lambda)}{R_{PEI}(\lambda) - T_{PEI}(\lambda)} \right)$$
(2)

where t_{PEI} is the thickness of the film and R is the corrected reflectance. The refractive indices obtained from Eqs. 1 and 2 for PEI and PEEK are found to be independent on the wavelengths emitted by the laser optics of the AFP machine (800 < λ < 1100 nm) which is 1.6 for PEI and 1.7 for PEEK, respectively. Furthermore, the extinction coefficients are almost zero in this wavelength range, which means that the PEI and the PEEK materials

are not directly heated by absorption of laser irradiation. The refractive index of APC-2 has been computed based on the rule of mixtures (Eq. 3) and the result is reported in Fig. 3.

$$n_{APC-2} = n_f v_f + n_{PEEK} v_{PEEK}$$

$$k_{APC-2} = k_f v_f + k_{PEEK} v_{PEEK}$$
(3)

where $v_{PEEK} = 61\%$ and $v_f = 39\%$ are the volume fraction of the PEEK matrix and carbon fibres, respectively. n_f is the real part of the complex 145 refractive index of the carbon fibres and k_f is its imaginary part. The values of these indices as a function of the wavelength are given by Borghesi and Guizzett [30]. To ensure that the hybrid material is opaque at wavelengths between 500 and 1100 nm, a transmission spectrum is performed with a Bruker Vertex v70 IRTF. The obtained results show that the maximum value 150 of the transmission coefficient as a function of the wavelength does not exceed 0.1%. In addition, the APC-2 is the material which absorbs energy according to its refractive index, as shown in Fig. 3, and given that the extinction coefficient of PEI is zero. The reflectance for the HTPC and PEI is calculated from the Snell's law and Fresnel equations. Then, the Fresnel coefficients (s 155 and p-polarisation) are obtained as a function of the incidence angle θ_a [31]. Fig. 4 depicts the total reflectance for the HTPC, PEI and APC-2 samples obtained from s-polarised and p-polarised lights. It is found that the APC-2 reflectance is most important in light of p-polarisation (see Fig. 5), which means that the light will behave differently depending on the polarisation 160 type. Therefore, a comparative inspection of HTPC reflectance and that reported for APC-2 [9] indicates that the reflectance of the HTPC is slightly higher than that of the APC-2, although the PEI material is semi-transparent and its extinction coefficient is roughly zero. This is because the laser beam

intensity $I(\lambda, t_{HTPC} = 0)$ is initially attenuated by the reflection at the

air/PEI interface. Hence, the real irradiation intensity reaching the opaque portion of the hybrid material (i.e., APC-2) is $(1 - R(\theta_a))I(\lambda, 0)$, where $R(\theta_a)$ is the reflectance of the HTPC material. The attenuation of crossing intensity within the HTPC can be described by the Bouguer's law

$$I(\lambda, t) = (1 - R(\theta_a)) I(\lambda, t_{PEI}) e^{-\alpha(\lambda)t_{HTPC}}$$
(4)

Therefore, the attenuation factor through the HTPC of thickness t_{HTPC} is defined by the ratio $\eta = I(\lambda, t_{HTPC})/I(\lambda, t_{PEI})$. From the refractive index of PEI film and data in Fig. 3, the attenuation factor η is calculated using Eq. 4. Fig. 6 shows the penetration depth of irradiation in the HTPC for $\lambda = 980 \ nm$. For $t_{HTPC} \ge 61.3 \ \mu m$, the irradiation is almost completely absorbed in the APC-2. It is important to note that the penetration depth of APC-2 is 0.3 μm given that 61 μm represents the average thickness of PEI film after joining the PEI film and the APC-2 material. As indicated in Fig. 6, the depth of penetration also depends on the incident angle θ_a . For the AFP process, the incident angle is less than $\theta_a \le 60^\circ$, which means that the attenuation factor does not exceed 0.75.



Fig. 3: Complex refractive index for APC-2



Fig. 4: Angular dependence of the reflectance for HTPC ($\lambda = 980 \ nm$) compared with experimental measurement for APC-2 [14]



Fig. 5: Relative intensity reflectance of APC-2 with s and p-polarisation for $\lambda=980~nm$



Fig. 6: Penetration depth of the irradiation in the HTPC for $\lambda = 980 \ nm$

The measurement of the emissivity is carried out for a temperature of $T = 250^{\circ}C$ and for a broad spectral band $[8 - 12] \ \mu m$. The value of the emissivity of the hybrid material is estimated by minimising the error between the thermocouple temperature and the thermal infrared camera. ¹⁸⁵ The best correlation is obtained with $\varepsilon = 0.87 \pm 0.01$. However, the measured emissivity using a spectrometer ($[8 - 12] \ \mu m$) with integrating sphere is found to be 0.02 upper than the value obtained by IR camera. This difference is explained by the contact between the thermocouple and the heating plate, which causes to overestimate the temperature. Therefore, the emissivity value considered in this study is $\varepsilon = 0.89$ obtained by spectroscopic measurement.

The data in Figs. 3 to 6 represent the main keys to investigate the laser-material interaction such as absorption, reflection and penetration depth of the irradiation into the material in a specific wavelength. The consideration of the incidence angle in this data allows to study the interaction based on parameters of the AFP robot head.

2.3. Thermal properties

To determine the normal absorptance A_n of the HTPC material and coefficients that described the transfer change between table and ²⁰⁰ surroundings air, a 3D transient thermal model is developed and compared with experimental results. The experimental test consists of several static laser shooting during 0.2 s on sample plaque made of HTPC material with a laser power of $P_L = 400 \ W$. The optical device (8F-56-8) used in the present study is that used on the AFP machine. This optics provides a rectangular-shaped spot $(L_x \times L_y)$ measuring 56 × 8 mm^2 . The heat source for the process is a fibre-coupled diode laser system (two diode stacks at $\lambda \approx 980 \ nm$ and two at $\lambda \approx 1030 \ nm$). The energy flow $\Phi(x, y)$ arriving at a given point on the surface is expressed as follows

$$\Phi(x,y) = \frac{A_n \eta_{laser} P_{eff}}{L_x L_y} X(x) Y(y)$$
(5)

where η_{laser} is the loss in optical fibre, P_{eff} is the effective laser power, X(x)and Y(y) are the normalized irradiation length and width profiles of the super-Gaussian beam at the focal distance, respectively. In the case of the (8F-56-8) optics, both X(x) and Y(y) are obtained from super-Gaussian functions fitted to map the laser spot obtained from a static laser shot on a thermal sensitive paper (ZAP-IT paper). Fig. 7 shows the normalized intensity of the laser beam at a focal distance of $w_f = 250 \ mm$.

The temperature at the HTPC interface is measured using an infrared camera with emissivity $\varepsilon = 0.89$. With regard to the numerical simulation, the problem involves to perform a heating and cooling stage. Solving this problem requires the accurate knowledge of the boundary conditions. In the first, the heat exchange between material and surrounding air is prescribed by the Newton's law, $\overrightarrow{\varphi_{conv}} = h_c(T - T_{amb}) \overrightarrow{n}$, in which the ambient temperature is $T_{amb} = 18^{\circ}C$ and h_c is the convective heat transfer coefficient. The thermal exchange between the substrate and the tooling is described by the heat transfer coefficient h_t , while the heat lost by irradiation is defined by the following relationship

$$\overrightarrow{\varphi_{rad}} = h_{rad} \left(T - T_{amb} \right) \overrightarrow{n} \tag{6}$$

where h_{rad} the radiation exchange coefficient isgiven by $h_{rad} {=} \sigma \varepsilon \left(T^2 {+} T_{amb}^2 \right) \left(T {+} T_{amb} \right) . \qquad \sigma {=} 5.67 ~\cdot~ 10^{-8} W/m^2 ~\cdot~ K^4 ~~ {\rm is}$ the To obtain accurate thermal distributions Stefan-Boltzmann constant. in the laminate, the material model must include temperature-dependent physical properties, such as a temperature-dependent specific heat (C_p) , a 230 temperature-dependent density (ρ) and a temperature-dependent thermal conductivity (K). For the APC-2 material, these properties are collected from [13] and summarised in Table 1. Then, the temperature dependence of these physical properties are obtained from a linear regression analysis.

Regarding the PEI material, a capillary rheometer Rheograph 20 is used to perform thermal conductivity and PVT measurements. Fig. 8 shows the curve fitting of the experimental data for both isotropic thermal conductivity and density as a function of temperature under atmospheric pressure. Fig. 9 depicts the temperature-dependent specific heat data obtained by differential scanning calorimetry (DSC).



Fig. 7: Normalized irradiation of super-Gaussian beam at the focal distance w_f

The normal absorptance A_n and the heat transfer coefficients h_c and h_t are determined from numerical simulations by comparing the thermal model with the experimental data. Fig. 10 shows the experimental temperature profile and its result by adjusting the numerical model. A very good correlation is found for $A_n = 0.7$, $h_c = 7 W/m^2/K$ and $h_t = 116 W/m^2/K$.



Fig. 8: Fits of measurement data of density (circle marker) and thermal conductivity (diamond marker) of PEI film

Temperature	Density	Specific heat capacity	Thermal conductivity	
$T \ [^{\circ}C]$	$ ho \; [kg/m^3]$	$C_p \; [J/kg \cdot {}^{\circ}C]$	$K_{xx} [W/m/^{\circ}C]$	$K_{yy} [W/m/^{\circ}C]$
23	1540	1100	4.92	0.61
400	1524	1800	7.68	0.66

Table 1: Physical properties of APC-2 at $23^\circ C$ and $400^\circ C$



Fig. 9: Measurements of specific heat of PEI



Fig. 10: Correlation between experimental and numerical temperature profiles

3. Thermo-optical model

3.1. Ray-tracing method

To model the laser-material interaction during the process, a ray-tracing method has been implemented, which allows computing the laser distribution on the substrate and incoming tape. To simplify the analysis, the specular reflection approach is used based on previously validated models for flat and curved geometries [32, 33, 17]. The AFP head parameters are considered, such as laser power P_L , incident angle β and tilt angle θ of the robot head. Furthermore, the roller deformation under the compaction force F is also taken into account to evaluate the reflection phenomena as function of roller profile. Based on contact mechanics [34], the roller profile of a commercial silicone roller can be written as follow [17]

$$g\left(x,F\right) = \begin{cases} \frac{\left(\delta - R_r\right)}{\left(R_r - w(F)\right)^2} \sqrt{\left(R_r - w(F)\right)^2 - \left(x - \frac{|x|}{x}w(F)\right)^2} & \forall z < 0 \ (a) \\ \delta - R_r & \forall z < 0, \forall |x| < w^F \ (b) \end{cases}$$

$$\begin{pmatrix}
\sqrt{R_r^2 - x^2} & \forall z > 0 \quad (c) \\
(7)
\end{cases}$$

where R_r is the radius of the roller, $w(F) = (4R_rFcos(\theta)/\pi E_{eq}L)^{1/2}$ is the half-contact between the roller and a rigid flat substrate, in which E_{eq} is the equivalent Young modulus of the roller. δ is the the radial deformation given by [35, 36].

In the first step of the ray-tracing method, the laser beam from the optical source onto both tape and substrate is divided into n rays according to the focal distance w_f . Each ray is defined by s and p-polarisation vectors. To consider the super-Gaussian profile Fig. 7, a weight is attribute to each ray from the laser source. The initial ray is assigned a fixed amount of energy depending on the intensity distribution pattern of the beam spot. Then, after setting AFP parameters, both substrate and incoming tape are meshing. The pseudo-code of this ray-tracing algorithm is illustrated in Table 2. In the second step, a mathematical test is carried out to identify the limit incident angle β_l between the substrate and the tape. Therefore, for each light, a logical test is performed to check whether it reaches the substrate or the tape. If the light achieved the substrate or the tape, a portion of its energy is absorbed by carbon fibres depending on its incidence angle. The part

- of the energy reflected by the PEI or APC-2 interfaces could be absorbed by the tape or substrate. The absorbed energy is then calculated using the conservation of energy A+R+T = 1, where A and T are the absorptance and transmittance, respectively. The reflectance R of each ray is calculated using Fresnel coefficients for the s- and p-polarised lights [37]. The path of each
- 270 reflected light from the substrate onto the tape and vice versa is based on the Snell's law. These operations are repeated for all emitted and reflected lights until the amplitude of their energy becomes negligible. Energy from reflected lights that have not reached the substrate or the tape is considered lost. The real reflection phenomenon with standard configuration, i.e., the incident
- angle $\beta = 14.75^{\circ}$, the aperture angle for the laser beam source $\gamma = 2.03^{\circ}$ and the focal distance of the laser optics $w_f = 250 \ mm$, is illustrated in Fig. 11. In the third step, the total laser heat-flux distribution in the substrate and the tape is calculated by computing the amount of energy accumulated on each element.



Fig. 11: Schematic representation of the incoming tape and the substrate reached by direct rays and its reflections according to the limit incident angle β and compaction force F

Algorithm 1: Ray-tracing algorithm

mesh the substrate and the incoming tape **Input** : A list of parameters: $[\beta, w_f, L_{spot}, P_L, F]$ **Output:** Heat flux distribution: $[\varphi_{tape}, \varphi_{substrate}]$ newList = []Divide the laser beam into n_r light and calculate its corresponding incidence angle θ_r ; Search the limit angle tape/substrate β_l ; Set the number of considered reflection N_{ref} ; for $\underline{i \leftarrow 1 \text{ to } N_{ref}}$ do for $\underline{j \leftarrow 1 \text{ to } n_r}$ do if i=1 then Establish the equation of direct light L(i, 1); if $\theta_{\underline{r}} \leq \beta_{\underline{l}}$ then Compute the reflected and the absorbed $E_t(i, 1)$ energy by tape; else Compute the reflected and the absorbed energy $E_s(i, 1)$ by substrate; end if else Establish the equation to reflect light $L_r(i, j)$; Check the interaction between the substrate or the tape; Compute the reflected and the absorbed energy $E_s(i, j)$ or $E_t(i,j);$ end if Update the newList $\leftarrow \{ [E_t(i,j), E_s(i,j) \};$ end for end for Compute the accumulate energy in each element of the substrate and the tape; **return** $\underline{\varphi_{tape}, \varphi_{substrate}}$

Table 2: Ray-tracing algorithm 24

280 3.2. Thermal model

The thermal distribution induced in the substrate during AFP process is represented by a 2D numerical model, given the small thickness of a ply when compared to its width. In addition, the choice of the 2D problem is suitable for establishing the process window. This model is coupled with ²⁸⁵ the non-uniform incident heat flux distributions estimated by ray-tracing method, including the process parameters. In a moving domain, the governing heat transfer equations for the anisotropic hybrid material can be written in a Lagrangian approach as

$$\begin{cases} \rho_{PEI} C_{p,PEI} \dot{T}(x_0, z_0, t) - K_{PEI} \Delta T(x_0, z_0, t) = 0 & z_0 \in t_{PEI} \\ \rho_{APC-2} C_{p,APC-2} \dot{T}(x_0, z_0, t) - div(\overline{\overline{K}}_{APC-2} \cdot \overrightarrow{grad} T(x_0, z_0, t)) = 0 & z_0 \in t_{APC-2} \\ \end{cases}$$

$$(8)$$

where C_p , \overline{K} and ρ are the specific heat capacity, the thermal conductivity ²⁹⁰ tensor (that becomes isotropic for the PEI) and the material density, respectively, which are considered to be temperature-dependent as discussed previously. The various heat losses that occur during the AFP process are described by the following equations

$$\begin{cases} \varphi_{conv} = h_c (T - T_{amb}) & \text{on } D_c \\ \overrightarrow{\varphi_{rad}} = h_{rad} (T - T_{amb}) \overrightarrow{n} & \text{on } D_c \\ \varphi_t = h_t (T - T_t) & \text{on } D_{table} \\ \varphi_r = h_r (T - T_r) & \text{on } D_{roller} \end{cases}$$
(9)

These thermal losses are depicted in Fig. 12. D_c is the convection and ²⁹⁵ surface-ambient radiation domain. h_c and h_t are the convection and the conduction coefficients, respectively. Since one dimension is neglected, the value of h_c and h_t found in the subsection 2.3 are changed from 7 $W/m^2/K$ to 15 $W/m^2/K$ and 116 $W/m^2/K$ to 410 $W/m^2/K$, respectively. These new values are determined numerically by fitting the 2D numerical model to

the experiment data presented in Fig. 10, while the radiation effect adopted for the 3D model is used without any modification. In addition, at t = 0, the initial temperature distribution is assumed to be equal to the ambient temperature $(T_{amb} = 23 \ ^{\circ}C)$. The laser flux distribution is implemented as boundary conditions in the form of the heat flux distribution $\varphi^{i,j} = -P^{i,j}/S^{i,j}$ for each element *i* reached of the substrate or *j* of the incoming tape, which *P* represents the total accumulated energy on the surface *S* of the element.

For a quasi-static analysis, the heat transfer is modelled by an Eulerian approach in which the reference (O, x, z) is related to the head velocity. Then, the steady-state heat transfer problem may be written as

$$\begin{pmatrix}
\rho_{PEI} C_{p,PEI} V \frac{\partial T(x,z)}{\partial x} - K_{PEI} \Delta T(x,z) = 0 & z \in t_{PEI} \\
\rho_{APC-2} C_{p,APC-2} V \frac{\partial T(x,z)}{\partial x} - div(\overline{\overline{K}}_{APC-2} \cdot \overrightarrow{grad} T(x,z)) = 0 & z \in t_{APC-2} \\
\end{cases}$$
(10)

where V = dx/dt is the layup velocity of the process. The advantage of the quasi-static analysis compared to the transient model is the computation time, which can be very useful to control the temperature.



Fig. 12: Boundary conditions

4. Comparison between experiment and numerical predictions

4.1. Experimental setup

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A fibre placement machine developed by Coriolis Composites is used to conduct the experimental tests (see Fig. 13). The placement head is mounted on a six-axis robot, on which is fixed a conformable silicone consolidation roller coated with non-adhesive perfluo-roalkoxy (PFA). The optical device (8F-56-8) is mounted in the robot head to heat both the substrate and the incoming tape according to the incident angle β . This optic generates a 320 constant rectangular spot with an aperture angle of 2.03°. At the focal distance $w_f = 250 \ mm$, the size of laser spot is about $56 \times 8 \ mm^2$ with a super-Gaussian intensity distribution as shown in Fig. 7. A FLIR IR-camera

- is installed next to the optics on the head to monitor the temperature during the layup near the nip-point process. The purpose of the application is to use a laser a diode laser power to heat the HTPC up to a process temperature (between the T_g of PEI and T_m of PEEK). The size of the draping geometry is 500 × 500 mm^2 . At the start of the test, the first layer of HPTC (600 × 600 mm^2) produced by Novotech Aerospace Advanced
- Technology (see Fig. 14) is fixed on the table. Then, a couple of K-type thermocouples (80 μm in diameter) with a rapid response is inserted during the layup according to the arrangement presented in Fig. 15. To avoid excess thickness accumulation, the offset x_0 is taken into account before adding each thermocouple. The temperature was recorded during the process (at a
- frequency of 300 Hz) using a universal QuantumX data acquisition system. The standard process parameters used are reported in Table 3. The laser beam strikes equally the substrate and the incoming tape for this default configuration.



Fig. 13: In-situ AFP process showing the layup of the hybrid material with thermocouples



Fig. 14: The NOVOTECH press which produced the hybrid material

Parameter	Symbol	Value
Laser power	P_L	$3 \ kW$
Laser power efficiency	η_{laser}	80 %
Process speed	V	$0.2 \ m/s$
Tilt of head	θ	7°
Incident laser angle	β	14.75°
Compaction force	F	250 N

Table 3: Experimental process parameters



Fig. 15: Experimental design

4.2. Numerical model implementation

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Fig.16 is a flow diagram illustrating the overall steps for obtaining the thermal results. After identifying the process and robot head parameters, the roller deformation should be calculated based on the roller properties, the compaction force and the tilt of the head. Then, the nip-point process and tape profile can be identified from the roller profile. The tape and the substrate are then discretized, followed by the execution of the ray-tracing 345 algorithm to compute the total energy absorbed on each element. In this step, the laser beam is split into $n_r = 50000$ rays to achieve an accurate heat flux distribution on the tape and the substrate. Thereafter, to describe the orthotropic thermal properties of the HTPC material, the finite element software Abaqus is employed. The moving heat flux distributions at each element of the incoming tape (φ_{tape}) and the substrate (φ_{sub}) are implemented using the DFLUX user subroutine, while the convection and radiation heat losses are developed in the FILM user subroutine. The following assumptions are also made

• The friction between the roller and the tape is negligible.

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- The contact between the PEI and the APC-2 is assumed perfect.
- The incoming tape is considered to be aligned with the laying direction.

The third assumption is used to simplify the thermal problem without affecting the real model. In this case, the incoming tape is placed on the substrate. To avoid the conduction of heat exchange between the incoming tapes and the substrate, an infinite thermal resistance (IRTC in Fig.18) is introduced at this contact from the nip-point process. The inter-ply thermal contact resistance of the substrate is calculated as a function of degree of intimate contact D_{ic} as introduced by Levy et al. [38]. The surface roughness parameters of the PEI film are collected from [39]. Therefore, the evolution of thermal contact resistance is coupled with the heat transfer problem via the user subroutine GAPCON.



Fig. 16: Flow diagram of the thermo-optical model

4.3. Results and discussion

The laser distribution plot for the experimental process parameters is presented in Fig. 17, in which the total incident heat flux on the substrate and the incoming tape from nip-point process computed from the ray-tracing method are depicted. The obtained profile shows that the illuminated area on the tape is larger than the substrate area, despite the standard process parameters in Table 3 are set to obtain an even distribution on the substrate

- and the incoming tape. This is because the reflection phenomenon occurs near the nip-point process. It is found that there are three reflections from the substrate or the incoming tape until the intensity of the light is attenuated by the HTPC. Light is absent at a distance of x = 3 mm due to shadow region starting from the nip-point process to the visible nip-point. The data for the
- total heat flux are then injected on the thermal model. Fig. 18 shows the simulation results for the standard configuration. To facilitate visualization temperature field following the thickness of the plate length of 0.5 m, a ratio 130 is applied in the z_0 direction. From this mapping, the temperatures at the interface melting and between plies are extracted and compared to the experimental results.



Fig. 17: Total incident heat flux on the substrate and the incoming tape for the experimental parameters listed in Table 3. The distance from nip-point process is shown in Fig. 12

Fig. 19 illustrated the evolution of the inter-layer average temperature during draping the fifth layer. The obtained results show the good agreement between the FEM predictions and the experimental data in terms of the timing and average maximum temperature. In addition, the difference
³⁹⁰ between measurements and predictions for the thermal history is less than 6 °C. It is important to note that the temperature measured at the heated

interface between the substrate and the tape by thermocouples is affected by the laser beam which displays error value. This is due to the absorption of irradiation by thermocouples when placed on the substrate. However, ³⁹⁵ the measured temperature at the visible nip-point process is recorded by a IR-camera (mounted on the placement head in parallel with the optical laser) and compared to numerical results. Fig. 20 depicts the numerical temperature history along the interface melting. It is found that the measured average maximum temperature is 295 °C, while the one computed numerically equals 286 °C. This difference is due to the fact that the IR camera measures also the temperature emitted by the APC-2 interface, which

- equals 348 °C at the APC-2 substrate interface and 243 °C at the APC-2 tape interface. On the other hand, in the consolidation region, the interface melting temperature is higher than the glass-transition temperature of the
- ⁴⁰⁵ PEI, which starts from 283 °C for the substrate and 273 °C for the tape. Moreover, the maximum temperature is located in the substrate specifically on the APC-2 interface with a value about 348 °C. This value of temperature exceeds the melting temperature of APC-2 (343 °C), which means that the APC-2 behaviour can be affected using the standard configuration.



Fig. 18: Temperature distribution in the substrate and the incoming tape obtained at $t = 1.75 \ s$ using the standard configuration 3. A ratio 130 is applied according to the thickness of the layers



Fig. 19: Experimental and predicted thermal history between three layers of the laminate



Fig. 20: Thermal history along the melting interface of PEI and APC-2 during welding the fifth layer for the experimental process parameters

- In order to illuminate both substrate and incoming tape surfaces evenly, an optimal configuration is found by setting the incident angle at $\beta = 15.05^{\circ}$ and the tilt of the robot head at $\theta = 4^{\circ}$. These values are found by using the ray-tracing method. Thereafter, the optimal incident heat flux is plotted in Fig. 21 and the corresponding temperature profile is shown in
- ⁴¹⁵ Fig. 22. It can be observed that the incident heat flux on the substrate is increased and more heat is accumulated near the nip-point process. For the optimal configuration, the temperature at the nip point process is shifted

to 297 $^{\circ}C$ on the substrate. This is explained by the depth of penetration which increases with increasing the incident angle (see Fig. 6). Moreover,

- according to Weiler et al. [19], the depth of penetration also depends on the irradiation time, which means that the peak of the incident flux on the tape represented in Fig. 17 has a weak effect on the thermal penetration. This is confirmed by a slight increase at distance $x_0 = 0.38 \ m$ (see Fig. 20) for the maximum distribution of the heat on the tape $\varphi_{tape} = 12.22 \times 10^4 \ W/m^2$.
- From the Fig. 22, the temperature on the APC-2 interface exceeds the melting temperature of PEEK. To minimize this temperature below the PEEK melting temperature, the laser power is reduced to $P_L = 2750 W$. For this update power, the average temperature near the nip point process is approximately 270 °C on the substrate, while the maximum temperature on the APC-2 interface is about 336 °C.



Fig. 21: Optimal incident heat flux on the substrate and the incoming tape. The compaction force and the tilt of the head are $F = 250 \ N$ and $\theta = 4^{\circ}$, respectively. The input laser power is $P_L = 3 \ kW$ with an optimal laser angle of $\beta = 15.05^{\circ}$



Fig. 22: Thermal history along the melting interface of PEI and APC-2 during welding the fifth layer for optimal process parameters

In Fig. 23 and with the optimal process parameters, the maximum temperature in the consolidation region (i.e., in layer 5) is plotted for various speeds and laser power. The obtained curves show a quasi-linear relationship between the laser power and the maximum temperature for each speed. In addition, the slope of each curve decreases with increasing the laser power. This is because the extremely short process time, which considerably affects the penetration depth of the irradiation into the material at higher speed, as demonstrated by Weiler et al. [19]. In order to establish a heating law

for the HTPC material, a linear regression for each curve is used to obtain the correlation between the layup speed and power laser need to maintain a constant temperature at the nip-point process. In the present work, this temperature is set at 250 °C near the nip-point process.

Two main reasons for which this material was developed are the improvement of the adhesion between layers thanks to an amorphous material on the surface and to control the rate of crystallinity of the APC-2. In fact, 445 the aeronautical industry closely monitors the rate of crystallinity of APC-2 processed by additive manufacturing processes. The objective is therefore to melt the PEI in order to achieve good adhesion between layers and not to melt the APC-2 so as not to modify its degree of crystallinity. A serie of calculations was performed to obtain a temperature of 250 $^{\circ}C$ at the nip-point 450 process. For each of these calculations, the temperature of the APC-2 is noted. In Fig. 24 are presented the laser power/process speed operating points to reach 250 $^{\circ}C$ and for each of these points, the temperature of APC-2 is reported. It is noticed that beyond a speed of 0.5 m/s, the APC-2 is melted in the process. In order to avoid the melting temperature of PEEK, 455 the limit interval associated with the nip-point process temperature measured at APC-2 interface is estimated through a series of calculations using the

steady state analysis and the optimal configuration. The results reported in Fig. 24 shown that a limit isothermal (343 °C) melting temprature of APC-2 is closed to the 250 °C at nip-point process.



Fig. 23: Correlation between the laser power and temperature at the nip-point process for the optimal process parameters. The values is computed from the quasi-static analysis



Fig. 24: Correlation between the laser power and layup speed to obtain a constant temperature of 250 $^{\circ}C$ at nip-point process. The shaded area represents the 93% confidence interval.

5. Conclusion

For a AFP process, there are two mainly parameters that control the temperature distribution at the nip-point process, namely, the laser power and the layup speed. To investigate the effect of these parameters along with other parameters related to the robot head, the optical and thermal properties of the hybrid material have been characterised, and provide the basis for the optico-thermal model. For the HTPC material, it was found that the absorption of laser beam is governed by the APC-2, specifically by the carbon fibres. The amount of absorbed energy is affected by the reflectance at the interface between the PEI film and the APC-2. In addition, the reflectance of HTPC increases with increasing the incidence angle, which reduces the penetration area of the heating element. The reflections between the tape and the substrate are modelled using a ray-tracing method including the effects of the compaction force on the deformable roller and the tilt angle of the robot head. It is shown that the reflection occurring between the incoming tape and the substrate increases the laser distribution near nip-point process.

The heat transfer between the substrate and the incoming tape has been investigated using 2D transient finite element models. The non-uniform laser distribution and inter-layer thermal contact resistance are successfully integrated in thermal models. The numerical model predictions are compared with experimental data obtained from thermocouple measurements during the layup process. A very good agreement is observed. A major point of this model is its ability to describe the temperature at the nip-point process more precisely at the interface of the PEI film, which is difficult to know by using an IR camera due to the presence of shadow zone between the visible nip-point and nip-point process. Furthermore, the semi-transparent PEI film is heated by conduction and the maximum temperature is located in APC-2 interface emitted by carbon fibres. From the quasi-static model,

⁴⁹⁰ an imposed temperature at the nip point process is obtained by iterative simulations in terms of laser power and layup velocity. Finally, the present numerical simulation tool can be easily adapted to model other materials with other geometries. Thus, this simulation tool can significantly help to better understand the influence of the process parameters on the heating law for further hybrid materials using AFP process.

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