

Correct Instantiation of a System Reconfiguration Pattern: A Proof and Refinement-Based Approach

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Correct instantiation of a system reconfiguration pattern: a proof and refinement-based approach

Abstract—System substitution can be defined as the capability to replace a system by another one that preserves the specification of the original one. It may occur in different reconfiguration situations like failure management or maintenance. When substituting a system at runtime, a key requirement is to correctly restore the state of the substituted one. This paper proposes a correct by construction generic model for system reconfiguration defined using formal methods, based on a system substitution operator. Systems are seen as state transition systems. This proposal relies on refinement and proofs. The formal development is conducted with the Event-B method. It consists in defining system substitution as a system composition operator associated to proof obligations. A generic formal model is developed using Event-B. Specific systems instantiate this generic model using a particular use of refinement-based on the definition of witnesses. This proposal is illustrated with an electronic commerce service.

Keywords—system substitution, system reconfiguration, proof and refinement-based methods, Event-B

I. INTRODUCTION

Several formal system development approaches have proved the efficiency and the scalability of formal methods for realistic systems using deductive verification, model checking and abstract interpretation. These approaches have been integrated into system engineering life cycles and are currently set up in many engineering domains like aeronautic and space, transportation systems, medical systems or energy production. Checking that systems behave correctly is a key requirement in system engineering. Moreover, the capability to assert that families of systems behave correctly is often used for certification purposes to avoid system specific activities. Formal methods were shown to be good candidates to handle such verification processes and to supply well-founded argumentation for certification. One of the key properties studied in system engineering is the capability of a system to react to changes (e.g. failures, quality of service change, context evolution, maintenance, etc.). In this context, the objective of this proposal is twofold: first, to address the design of adaptive, resilient, dependable, self-* systems etc. which require the capability to reconfigure running systems (more precisely, reconfiguration can be seen as the substitution of a system by another one); second, to put formal methods (more precisely proof and refinement-based methods) into practice to model a system substitution operation for a family of systems whose behavior is characterized by transition systems. The Event-B method is used to perform the formal developments. Two different substitution relations are studied. The first one is a static substitution (corresponding to a *cold start*) that relies on refinement to characterize the set of systems that conform to the same specification. A class of potential implementation systems are thus characterized by refinement. The second one addresses the dynamic substitution (substitution at runtime or *warm start*). It relies on a composition operator that combines two systems that refine the same specification. This composition operator is parameterized by the *substitution* or *reparation property* ensuring that the current state (the state where the source system is halted) is correctly restored in the substitute system. Moreover, we identify three substitution modes for the composition operator: equivalent, degraded or upgraded substitute systems.

This paper proposes a generic system reconfiguration formal model developed using correct-by-construction stepwise refinement and proof-based formal methods. Event-B supports the whole formal development of the system substitution operator. The developed generic model can be instantiated to any number of systems to be substituted. The proposed approach is generic and an instantiation mechanism, based on a specific refinement with witnesses, is proposed to overcome the state space explosion problem usually encountered when model checking-based verification techniques are set up.

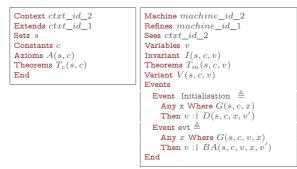
We have structured this paper as follows. First, the next section gives an overview of the Event-B method. Then, section III describes the proposed substitution operator through the definition of a parameterized composition operator for which proof obligations are synthesized, and section IV describes an application of this generalized approach. The mathematical setting describing the generalization of this approach is presented in section V. Then, the corresponding Event-B models handling this generalized model are described in section VI and the associated instantiation mechanism is described in section VII. The same case study is used to instantiate this generic model in section VIII. Then, an assessment of the proposed approach is shown in section IX, and section X gives some related work. Finally, a conclusion summarizes our contribution and some future research paths are discussed in the last section.

II. EVENT-B: A CORRECT-BY-CONSTRUCTION METHOD

An Event-B¹ model [1] (see Listing 1) is defined in a *MACHINE*. It encodes a state transition system which contains: variables, declared in the *VARIABLES* clause, that represent the states; and events, declared in the *EVENTS* clause, that

¹http://www.event-b.org/

represent the transitions (defined by a Before-After predicate BA) from one state to another (: | for the *becomes* operator).



Listing 1. Structures of Event-B contexts and machines

A model also contains *INVARIANTS* and *THEOREMS* that represent its relevant properties. A decreasing *VARIANT* introduces mandatory convergence properties. An Event-B machine is related through the *SEES* clause to a *CONTEXT* that contains the relevant sets, constants, axioms and theorems required to build an Event-B model. The refinement capability, introduced by the *REFINES* clause, builds a new model (thus a new transition system) that contains more design decisions representing the changes from an abstract level to a less abstract one. In a refinement, new variables and new events may be introduced. Gluing invariants are defined to link the variables of the refined machine with the ones of the refining machine. This refinement process ensures the preservation of proved properties and supports the definition of new refined models.

TABLE I. GENERATED PROOF OBLIGATIONS FOR AN EVENT-B MODEL

Theorems	$A(s,c) \Rightarrow T_c(s,c)$
	$A(s,c) \land I(s,c,v) \Rightarrow T_m(s,c,v)$
Invariant preservation	$A(s,c) \wedge I(s,c,v) \wedge G(s,c,v,x)$
	$\wedge BA(s, c, v, x, v') \Rightarrow I(s, c, v')$
Event feasibility	$A(s,c) \wedge I(s,c,v) \wedge G(s,c,v,x)$
	$\Rightarrow \exists v'.BA(s,c,v,x,v')$
Variant progress	$A(s,c) \wedge I(s,c,v)$
	$\wedge G(s, c, v, x) \wedge BA(s, c, v, x, v')$
	$\Rightarrow V(s, c, v') < V(s, c, v)$

Once an Event-B machine is defined, a set of proof obligations is generated. They are passed to the prover embedded in the Rodin platform [2]. Proof obligations associated to an Event-B model are listed in Table I. The prime notation is used to distinguish between pre (x) and post (x') variables. More details on proof obligations can be found in [1].

III. OUR APPROACH FOR SYSTEM SUBSTITUTION

Studied systems are formalized as the state-transition systems. According to Figure 1, a system is initialized, then it evolves (progress) relying on state changes. A failure can occur during state change. The system may then be repaired, or isolated (complete failure).

Two main requirements are identified to allow the substitution of Sys_S by Sys_T (e.g. in case of failure) :

[**Req1.**] *Static substitution.* Sys_S and Sys_T are two systems implementing the same specification Spec.

[Req2.] Dynamic substitution. In case of failure of Sys_S , the system Sys_T is activated at runtime. The state of Sys_T will be initialized according to the current state of Sys_S .

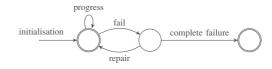
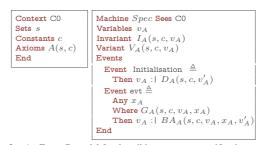


Fig. 1. Studied system behavior pattern

A. The global system specification

Systems are formalized, within Event-B, as state-transition systems. Listing 2 shows a generic model representing the Spec machine for the global system specification. States are defined as a set of variables. Their correct values are constrained by invariants. States are initialized, and transitions are modeled as events (e.g. evt) that may affect state variables. These transitions model progress. An inductive invariant (I_A) ensures the correct behavior (safety) of the defined state-transition system, and an optional variant (V_A) ensures reachability.



Listing 2. An Event-B model for describing a system specification: a context co and a machine Spec

B. Static substitution

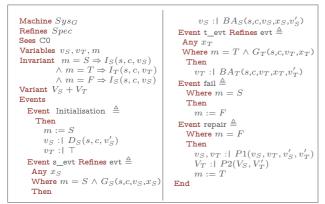
Every system refining the global specification is a candidate for system substitution. Listing 3 depicts two Event-B refinements of the specification *Spec*. They correspond to two systems Sys_S and Sys_T that implement the *same* specification *Spec*. A variable *m* (for mode) has been added to express which system is used. Invariants I_S and I_T define relevant properties and ensure the preservation of the specification properties. This refinement fulfills requirement *Req1*.

Machine Sys_S	Machine Sys_T
Refines Spec Sees C0	Refines Spec Sees C0
Variables v_S, m	Variables v_T, m
Invariant $m = S \Rightarrow I_S(s, c, v_S)$	Invariant $m = T \Rightarrow I_T(s, c, v_T)$
Variant V_S	Variant V_T
Events	Events
Event Initialisation \triangleq	Event Initialisation \triangleq
Then $m := S$	Then $m := T$
$\wedge v_S :\mid D_S(s, c, v'_S)$	$\wedge v_T :\mid D_T(s, c, v'_T) \mid$
Event evt Refines evt \triangleq	Event evt Refines evt \triangleq
Any y_S	Any y_T
Where $m = S$	Where $m = T$
$\wedge G_S(s,c,v_S,y_S)$	$\wedge G_T(s,c,v_T,y_T)$
With $y_S: x_S = y_S$	With $y_T : x_T = y_T$
Then	Then
$v_S :\mid BA_S(s,c,v_S,y_S,v'_S)$	$v_T : BA_T(s,c,v_T,y_T,v_T')$
End	End

Listing 3. Event-B models for Sys_S and Sys_T system substitutes for Spec

C. Dynamic substitution

Two events are introduced (see Listing 4): the first one records the occurrence of a failure (fail) and halts the currently running system by setting the variable m to F; the second one (repair) transfers the control at runtime from Sys_S to Sys_T by 1) setting the variables of Sys_T with values derived from the ones of the interrupted state of Sys_S . This assignment is possible and safe thanks to the definition of an *horizontal invariant* P1 gluing the state variables of systems Sys_S and Sys_T and 2) initializing the variant for Sys_T using a property P2. The variable m is then set to T to transfer the control to Sys_T .



Listing 4. The resulting global system Sys_G

D. Resulting global system

The resulting system composes systems Sys_S and Sys_T and the events fail and repair into one single Event-B machine as depicted on Listing 4. The obtained Event-B model encodes the substitution pattern of Figure 1. The mode m is set to the initial system (here S). The invariants I_S and I_T of each system are preserved, and when a failure occurs, the failing state preserves invariant I_S . Req2 is thus satisfied.

E. System substitution as a composition operator

This proposal can be seen as a parameterized (with the P1 and P2 parameters) system composition written as $Sys_S \circ Sys_T$. It defines the substitution of a system Sys_S by another system Sys_T . Let us study the properties of this operator, i.e. the associated proof obligations. First, the events corresponding to Sys_S and Sys_T preserve the invariant because they preserved their respective invariants I_S and I_T in the static substitution. Second, the event fail also satisfies the invariant, since no state variable is modified by this event. The repair event is the only event concerned by the modification of the variables. It shall maintain the invariant. According to Table I, the associated proof obligation is defined as follows.

$$\begin{split} A(s,c), \ m &= S \Rightarrow I_S(s,c,v_S) \land m = T \Rightarrow I_T(s,c,v_T) \\ \land m &= F \Rightarrow I_S(s,c,v_S), \ m = F, \ P1(v_S,v_T,v'_S,v'_T) \land m' = T \\ \vdash m' &= S \Rightarrow I_S(s,c,v'_S) \land m' = T \Rightarrow I_T(s,c,v'_T) \land m' = F \Rightarrow I_S(s,c,v'_S) \end{split}$$

The proof obligation for the preservation of the invariant in the repair event are obtained after simplifications.

$$A(s,c) \vdash I_S(s,c,v_S) \land P1(v_S,v_T,v'_S,v'_T) \Rightarrow I_T(s,c,v'_T)$$

$$(1)$$

To conclude, the proof obligation corresponding to equation (1) is associated to the composition $Sys_S \underset{P1,P2}{\circ} Sys_T$. This equation defines the proof obligation associated to the substitution pattern we studied.

IV. A CASE STUDY

This method has been applied to a case study of a basic electronic commerce system for web services compensation. The provided Event-B models are borrowed from [3].

A. The system

The system enables the purchase of a set of products from a single supplier. A user selects some products in a cart, pays the corresponding fees, receives an invoice and then the products are delivered by the logistics part of the system (see Figure 2).

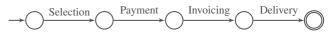


Fig. 2. High level view of the case study system

We suppose that during the *selection* step, a failure occurs due to an error on the supplier side. A failure signal is triggered. It enables the substitution of the supplier website by a new system composed of two other suppliers on two different websites. The two corresponding carts are filled such that the user does not lose or gain any products in the carts (corresponding to an equivalent system substitution case).

B. The specification

The model encodes the state-transitions system of Figure 2.

1) The context: The context C_1 introduces STOCKS a relation associating the available products for each site.

Context C_1	
Sets	
PRODUCTS // all the products in the world	
SITES // all the sites in the world	
Constants STOCKS	
Axioms	
Axm1 : finite(PRODUCTS)	
Axm2 : finite(SITES)	
$Axm3: card(SITES) \ge 2$	
Axm4: STOCKS = SITES × PRODUCTS	
End	

Listing 5. The context C_1

2) The top level specification: corresponds to an Event-B machine (Listing 6) with the events of the state-transitions system of Figure 2. Only the details of the selection event are given. It fills a variable carts with an arbitrary cart which contains the desired products (Grd3), each one of these products being selected on a single site (Grd4).

```
Events

Event initialisation \triangleq

Then

seq := 4

P :\in \mathbb{P}(PRODUCTS)
```

```
\begin{array}{l} carts:=\varnothing\\ \textbf{Event selection}\triangleq\\ \textbf{Any someCarts Where}\\ Grd1:seq=4\\ Grd2:someCarts\subseteq SITES\times P\\ Grd3:ran(someCarts)=P\\ Grd4:\forall p. p\in ran(someCarts)\Rightarrow card(someCarts^{-1}[\{p\}])=1\\ \textbf{Then}\\ seq:=3\\ carts:=someCarts\\ \textbf{Event payment}\triangleq \textbf{Where }Grd1:seq=3 \textbf{ Then }seq:=2\ldots\\ \textbf{Event billing}\triangleq \textbf{Where }Grd1:seq=1 \textbf{ Then }seq:=1\ldots\\ \textbf{Event delivery}\triangleq \textbf{Where }Grd1:seq=1 \textbf{ Then }seq:=0\ldots\\ \textbf{End} \end{array}
```

Listing 6. The events encoding the activities of the case study of Figure 2

C. Possible implementations

We define two systems, *WS1* and *WS2*, implementing (refining) this specification. The two refinements of the selection event are given in Listings 7 and 8. The first system, *WS1*, uses one single cart and one website. It offers the possibility to add items individually to the cart.

```
Event addItem_WS1 \triangleq

Any item

Where item \in P \setminus ran(cart_{WS1})

Then cart_{WS1} := cart_{WS1} \cup \{site_1 \mapsto item\}

Event selection_WS1 \triangleq

Refines selection

Where ran(cart_{WS1}) = P

Then cart := cart_{WS1}
```

Listing 7. Refinement of the selection event for one site (WS1).

The second system, *WS2*, uses two websites with one cart on each website. A user may add items, one by one, to each of the carts, by choosing products on both websites. The cart of the specification is the union of the carts of both websites.

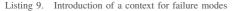
```
 \begin{array}{l} \textbf{Event addItemA_WS2} \triangleq \\ \textbf{Any item} \\ \textbf{Where item} \in P \setminus ran(cart_{WS2}^A \cup cart_{WS2}^B) \\ \textbf{Then } cart_{WS2}^A := cart_{WS2}^A \cup \{site_{2A} \mapsto item\} \\ \textbf{Event addItemB_WS2} \triangleq \\ \textbf{Any item} \\ \textbf{Where } item \in P \setminus ran(cart_{WS2}^A \cup cart_{WS2}^B) \\ \textbf{Then } cart_{WS2}^B := cart_{WS2}^B \cup \{site_{2B} \mapsto item\} \\ \textbf{Event selection_WS2} \triangleq \\ \textbf{Refines selection} \\ \textbf{Where } ran(cart_{WS2}^A \cup cart_{WS2}^B) = P \\ \textbf{Then } cart := cart_{WS2}^A \cup cart_{WS2}^B \\ \textbf{Then } cart := cart_{WS2}^A \cup cart_{WS2}^A \\ \textbf{Then } cart_{WS2}^A \cup cart_{WS2}^A \\ \textbf{Then } cart_{WS2}^A \cup cart_{WS2}^A
```

Listing 8. Refinement of the selection event for two sites (WS2).

D. Failure and substitution

According to the presented methodology, the next step consists in introducing the failure and the substitution events. The basic definitions for failure modes are defined in the context C_{11} .

```
Context C_11 Extends C_1
Sets FAILURE_MODES
Constants OK, NOK
Axioms
axm1:partition(FAILURE_MODES, {OK}, {NOK})
End
```



1) Introduction of failures: the failure_WS1 event introduces failures on the first site WS1. It halts the system.

```
Listing 10. Failure event for WS1
```

2) System substitution: the correctness of the substitution between the two systems relies on the correct restoration of the carts. Correctness is preserved by the *horizontal invariant* defined as $cart_{WS1} = cart_{WS2}^A \cup cart_{WS2}^B$. It guarantees that the products contained in the cart $cart_{WS1}$ already purchased on WS1 (one website) are split in the carts $aCart_{WS2}^A$ and $aCart_{WS2}^B$ of WS2 (two websites).

```
 \begin{array}{l} \textbf{Event Repair_WS1\_WS2} \triangleq \\ \textbf{Any} \\ aCart^{M}_{MS2}, aCart^{B}_{WS2} \\ \textbf{Where} \\ Grd1: sys = WS1 \\ Grd2: failureStatus = NOK \\ \textbf{Grd3}: aCart^{A}_{WS2} \cup aCart^{B}_{WS2} = cart_{WS1} \\ \textbf{Grd4}: aCart^{A}_{WS2} \cap aCart^{B}_{WS2} = \varnothing \\ \textbf{Then} \\ Act1: sys := WS2 \\ Act2: failureStatus := OK \\ Act3: cart^{A}_{WS2} := aCart^{A}_{WS2} \\ Act4: cart^{B}_{WS2} := aCart^{B}_{WS2} \\ \end{array}
```

Listing 11. The substitution event exploiting the horizontal invariant

The Event-B models we presented are borrowed from [3]. This simple case study will be used to illustrate the generalization of system substitution.

V. MATHEMATICAL SETTING FOR SUBSTITUTION

The formal development sketched in the previous section shall be conducted every time a substitution case needs to be considered. In this sense, the previous approach provides a correct substitution mechanism, but it is not generic. Neither the development nor the verification processes can be reused. We advocate the use of a generic correct-by-construction approach. The proposed generalization consists in manipulating the described systems where systems become first-order objects manipulated by the Event-B models. States, transitions, invariants, variants, etc. become objects of the proposed model, and the described system behavior conforms to Figure 1.

This proposal first expresses the system substitution strategy at a higher level, and then reuses this development for each specific system substitution. The specific system is obtained by instantiation of the generic model. Instantiation is defined by a particular use of refinement. Specific systems, defining instances, are witnesses of the generic development.

A. Variables and states

Variables, that represent states, belong to a set Variables. Their values are taken in the set ValueElements. Variables are associated to their values by the $Valuations \subseteq Variables \leftrightarrow \mathbb{P}(ValueElements)$ function.

B. Initialization and progress

The initialization of the global system selects the first system to run. The progress event models the assignment of a new valuation for the system state variables.

C. Systems

Systems belong to the set *Systems* of all the systems. A system is a tuple that is defined as $system = \langle variables, variant, invariant, init, progress \rangle$, where:

• variables is a set of variables representing the state of the system: variables \subseteq Variables

• *variant* is a function producing the natural value of the variant from a valuation of the variables: *variant* \in *Valuations* $\rightarrow \mathbb{N}$

• *invariant* is a predicate defined on the variables values: *invariant* \in Valuations \rightarrow BOOL

• *init* and *progress* are two before-after predicates recording the state changes.

D. Systems substitution relation

System substitution requires the definition of a relation associating the source system states with the target system ones. As defined in equation 2, this relation is given by the definition of an invariant, named *horizontal invariant*.

$\forall S_S, S_T \in Systems.$	
$\forall Inv_H(S_S, S_T) \in$	
$states(S_S) \times states(S_T) \rightarrow BOOL.$	
$substitute_states(S_S, S_T) =$	
$\{(s_S, s_T) \in states(S_S) \times states(S_T) \mid$	
$Inv_H(S_S, S_T)(s_S, s_T)$	$_{T})\}$ (2)

where² states is a function returning the possible valuations of a given system: $states \in System \rightarrow Valuations$, and Inv_H is a predicate defining the horizontal invariant involving the values of the variables of the source and target systems: $Inv_H \in System^2 \rightarrow Valuations^2 \rightarrow BOOL$

The invariant Inv_H links the source and target states. It fulfills the role of P1 in the proof obligation defined in equation (1). In the generic model, its definition is given by an equivalence relation. Its definition entails the definition of the reparation relation $repair \in Systems^2 \times (Valuations \rightarrow BOOL)^2$. It is parameterized by two predicates ψ and φ .

```
\begin{aligned} \forall S_S, S_T \in Systems. \quad \forall \psi \in states(S_S) \to \text{BOOL.} \\ \forall \varphi \in states(S_T) \to \text{BOOL.} \\ repair(S_S, S_T, \psi, \varphi) = \\ & \{(s_S, s_T) \in substitute\_states(S_S, S_T) \mid \\ & Inv_S(S_S)(s_S) \land \psi \Leftrightarrow Inv_S(S_T)(s_T) \land \varphi \} \end{aligned} (3)
```

where $Inv_S(S_X)(s_X)$ is the value (satisfied or not) of the system invariant of the system S_X in the state s_X .

The predicates ψ and $\varphi \ (\neq false)$ define different reparation or substitution modes.

• $\psi = True \land \varphi = True$ in the case S_T is an equivalent system substitute,

- $\psi \neq True \land \varphi = True$ in the case S_T upgrades S_S
- $\psi = True \land \varphi \neq True$ in the case S_T degrades S_S

```
^2\mathrm{If}\;E is a set, then E^2 denotes the Cartesian product E\times E
```

E. Substitution property

The condition to substitute a system S_S by a system S_T is given by the *repairable_equiv* predicate characterizing the set of substitute systems.

$repairable_equiv(S_S) =$	
$\exists S_T \in Systems \cdot repair(S_S, S_T, True, True) \neq \emptyset$	(4)

According to equation (3), here the predicates ψ and φ are set to True in equation (4) to obtain equivalence.

Finally, the generic system of systems setting is given by a graph characterized by the pair SoS = (Systems, repair)where Systems is the set of available systems (nodes) and *repair* is the relation among the available systems (edges). The obtained graph of systems may be constrained by additional properties. For example, a property could be that each system has at least two substitute systems. This is out of the scope of this contribution.

VI. AN EVENT-B MODEL FOR SYSTEM SUBSTITUTION

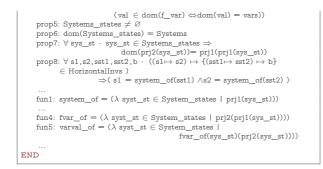
The mathematical setting described above has been completely formalized³ within the Event-B method. This formalization led to the definition of a context CO and of two machines M0 and M1, the latter being the refinement of the former.

A. Required definitions

The context CO (Listing 12) implements the theory associated to the system substitution relation. It defines Systems, Variables and their possible Valuations. Systems are sets characterizing the potentially available systems involved in a substitution. States and Variables are manipulated by the defined recovery mechanism. Note the introduction of the system_of function returning the system a state belongs to. Moreover, it also defines in type10 the type of the *horizontal invariant* which associates corresponding repair states in systems. Property prop8 ensures that this invariant is well-defined on the states to be recovered. The variant expression is accessed by the fvar_of function in fun4 which returns, for a given state, the function which computes the value of the variant, while the varval_of function fun5 returns, for a given state, the value of this variant.

CONTEXT C0 SETS Variables, ValueElements CONSTANTS Valuations, VariablesSets, Systems, Systems_states, system_of, HorizontalInvs, varval_of
AXIOMS
set1: finite (Variables)
set2: finite (ValueElements)
type1: Valuations \subseteq Variables $\rightarrow \mathbb{P}$ (ValueElements)
type2: VariablesSets $\subseteq \mathbb{P}$ (Variables)
type3: Systems \subseteq VariablesSets \times (Valuations $\rightarrow \mathbb{N}$)
type4: Systems_states \subseteq Systems $ imes$ Valuations
type10: HorizontalInvs \in (Systems $ imes$ Systems) $ o$
$((Systems_states \times Systems_states) \rightarrow BOOL)$
prop1: VariablesSets $\neq \emptyset$
prop2: $\forall v1, v2 \cdot (v1 \in VariablesSets \land v2 \in VariablesSets \land v1 \neq v2)$ $\Rightarrow v1 \cap v2 = \emptyset$
prop3: finite (Systems) \land Systems $\neq \varnothing$
prop4: \forall vars,f_var \cdot (vars \mapsto f_var) \in Systems \Rightarrow
$(\forall \ \texttt{val} \ \cdot \ \texttt{val} \in \texttt{Valuations} \Rightarrow$

³The complete Event-B development is available on http://babin.perso. enseeiht.fr/r/HASE_2016_Models.pdf



Listing 12. Context C0 containing basic definitions and properties

B. Systems recovery behavior

The definition of the final obtained model conforms to the system behavior pattern depicted by the transition system of Figure 1.

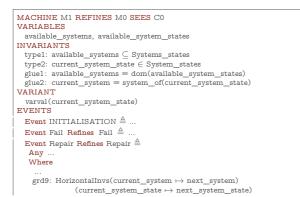
1) The top level specification: The first abstract machine, M0 manipulates systems without considering system states yet. The available_systems and current_system variables define respectively all the available healthy systems for substitution and the current running system.

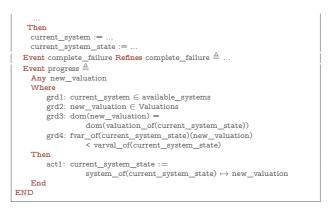
MACHINE MO SEES CO VARIABLES
current_system, current_system_state INVARIANTS
type1: available_systems ⊆ Systems type2: current system ∈ Systems
EVENTS
Event INITIALISATION $\triangleq \dots$
Event Fail \triangleq
Event Repair $\triangleq \dots$
Event Complete_failure $\triangleq \dots$
END

Listing 13. Squeleton of machine M0

This machine only defines system modes and the failure together with the associated reparation. It models the fact that a system fails, is possibly repaired or isolated (complete_failure) in the treatment of the failure.

2) First refinement: Machine M1 below refines M0 to define the final complete generic substitution model. It introduces the variables and the states of the manipulated systems through two new variables available_systems_states and current_system_state.





Listing 14. Extract of the machine M1

Two important gluing invariants are defined. The first one glue1 denotes that the states of the available systems are effectively states of the available systems and the second one glue2 asserts that the current state is a state of the current running system. Here, the events are refined to handle the notion of system states. This refinement, 1) defines varval (current_system_state) as a variant to record the progress of the running system, 2) introduces the important event progress to record the behavior of the current running system. It defines the next state of the running system and ensures that the variant decreases (grd4), and 3) refines the repair event by choosing the next system and its state. Note that the guard grd9 defined in this event guarantees that the substitute system fulfills the horizontal invariant corresponding to the substitution property. Depending on this horizontal invariant, the system is substituted in equivalent, degraded or upgraded mode.

VII. INSTANTIATION WITH EVENT-B: BY REFINEMENT

A. The instantiation context: the principle

A context CO_instance extending CO (Listing 12) is defined with concrete values for sets (Variables, ValueElements) and constants (Valuations, VariablesSets, Systems and System_states).

B. Refinement and witnesses for instantiation: the principle

M1 of the generic model is instantiated by CO_instance context values. It is defined by M2 refining M1. The event progress is itself refined by the events progress_sysXY corresponding to the transitions in the specific system defined in CO_instance. Each transition of the instantiating system refines the progress event of the machine M1. Concrete event variables of M2 and abstract variables of M1 are glued with a witness On Listing 15, the variable new_state is instantiated by the witness new_state_sysA representing a concrete system variable for sysA.

Event eventA ≜	Event eventC Refines eventA \triangleq
Any new_state	Where current_system = sysA \land sysA_ok()
Where current_system_ok()	With new_state = new_state_sysA
Then state := new_state	Then state := new_state_sysA

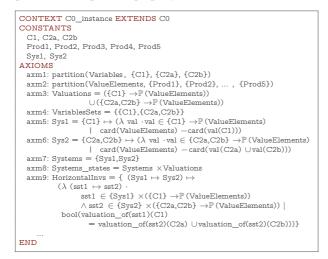
Listing 15. Instantiation through refinement with witness

VIII. APPLICATION TO THE CASE STUDY

The previous approach applies on the defined case study.

A. The instantiation context: application to the case study

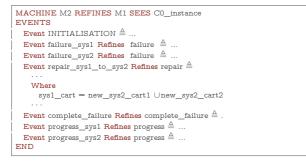
The instantiation context provides concrete values for the deferred sets of the context CO. Variables, systems, states, etc. are valued accordingly. Note the presence of the fundamental axiom axm9 to ensure the correct system substitution. It corresponds to the reparation property introduced in section IV-D2.



Listing 16. The instantiation context

B. Use of refinement and witnesses for instantiation : application to the case study

The events of the M1 machine are refined (by machine M2) for instantiation according to the principle of section VII-B.

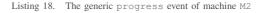


Listing 17. The instantiation machine obtained by refinement

For instance, the progress event is refined by the progress_sys1 event describing the progress for system WS1. It corresponds to the event addItem_WS1 of Listing 7. The witness (with clause) of the event progress_sys1 consists in adding a product in the cart C1 of the website *site*₁ as done in event addItem_WS1.



```
grd3: new_prod ∈ ValueElements
grd4: new_prod ∉ sys1_cart
WITH
    new_valuation: new_valuation = {C1 → (sys1_cart ∪{new_prod}))
THEN
    act1: sys1_cart := sys1_cart ∪{new_prod}
    act2: current_system_state :=
        Sys1 → {C1 → (sys1_cart ∪{new_prod}))}
END
```



IX. Assessment

A. Proof statistics

TABLE II. RODIN PROOFS STATISTICS

Event-B	Generated proof	Automatic	Interactive
Model	Obligations	proofs	proofs
Context C0	7	5	2
Machine M0	5	5	0
Machine M1	28	22	6
Instantiation context C0_context	3	2	1
Instantiation machine M2	54	39	15
Total	97	73	24

B. Model checking or proof-based verification

Note that model checking techniques can be applied to automatically check the correctness of the instantiation. State exploration is possible since the sets have finite number of values in the context CO_instance. The instantiation mechanism defined above is based on refinement. The approach is scalable and does not face the state explosion problem. The key point for scalability concerns the instantiation of specific systems. Indeed, the development presented above is a generic one, defined at a meta-level, where the proof obligation associated to the correctness of the system substitution obtained in section III-E act as meta-theorem.

Event of the model	Instantiation by a witness
Event $evt \triangleq$	Event ref_of_evt ≜
Any x	Refines evt
Where	Where grd1: $G(s, c, v, y)$
grd1: $G(s, c, v, x)$	With x: $x = y //$ witness

Then

End

act1: v :| BA(s, c, v, y, v')

Listing 19. Proof based instantiation

act1: v :| BA(s, c, v, x, v')

Then

End

The use of the ANY generalized substitutions shows that the development considers any transition system described by a template corresponding to Figure 1 together with the associated invariants expressed in the corresponding Event-B models. According to the proof obligation associated to the ANY substitution described in Table I, one proof strategy is to exhibit a witness for the parameter x. Two proof techniques, experimented in this paper have been developed. 1) The first one uses model checking with the ProB [4] model checker. We did not give the details of this approach in this paper. 2) The second technique relies on a proof-based approach (can be used if model checking fails) to check instance correctness. Such an approach consists in defining another model which refines the one presented in section V. Like in section VII, each ANYevent is refined by an event with a witness for each parameter. The event refinement strategy is shown in Listing 19. The witnesses can be any transition system matching the pattern of Figure 1 whatever its size is. This second verification technique requires interactive proof efforts and ensures scalability.

C. Correct-by-construction formal methods

The proposed approach is a generic one. The context CO describes the manipulated systems concepts (systems, variables, HorizontalInvs, etc.). The concepts are manipulated as first-order objects in the machines M0 and M1 in order to encode the behavior pattern described with the events Initialization, progress, fail, repair and complete_failure. Let's note that the concept of transition is not manipulated as first order objects and thus not defined within the context CO. One may wonder why the transitions between states are not defined in this context CO. There are two main reasons for that: first, transitions are not explicitly manipulated by the substitution mechanism introduced in this paper. Second, the Event-B method provides a powerful built-in inductive proof technique based on invariant preservation by the events (see table I). The only proof effort relates to the correct event refinement. Note that in traditional correct-by-construction techniques like Coq [5] or Isabelle [6], classical inductive proof schemes are offered. One has first to describe the inductive structure associated to the formalized systems, then to give a specific inductive proof scheme for this defined inductive structure and finally to prove the correct instantiation. In the kernel definition of these techniques, the inductive process associated to transition systems corresponding to the pattern of Figure 1 and the refinement capability are not available as a built-in inductive proof process. transition together with corresponding inductive proof principles and the instantiation of transitions because event refinement is not available. Unlike Event-B, another meta-level is needed.

X. RELATED WORK

Formal modeling of system reconfiguration has been studied by several authors. Regarding proof and refinement-based methods, the Event-B method has been applied to model fault-tolerance mechanisms in the field of critical multi-agent system by [7]. The authors used refinement at the heart of the approach. State-based formalisms illustrated by Event-B were also exploited by [8] in order to develop fault-tolerant system by modeling fault tolerance requirements, fault assumptions and modes of the system behavior through an additional viewpoints. In [9] Abstract State Machines (ASMs) model a combination of state-transition models with architectural descriptions. Other approaches studied system re-configuration as well. Model checking of timed automata has been used by [10] to model and study the robustness of self-adaptive decentralized systems. Some approaches used process algebras. Analysis of unplanned reconfiguration in dependable systems has also been modeled with process algebra [11]. Behavioral matching between substitute systems was defined by a bisimulation relation. Finally, there exists other approaches, offering an evolving number of systems, to define reconfigurable Byzantine-fault-tolerant distributed system [12].

XI. CONCLUSION

This paper addresses the problem of *correct* system reconfiguration, where systems are described as state-transition sys-

tems. It provides a stepwise correct-by-construction approach that generalizes ad hoc system reconfigurations. This one relies on 1) the definition of a system that implements (i.e. refine) the same specification and 2) a system reconfiguration operator parameterized by a reparation property, namely a horizontal invariant. This one ensures that, when a failure occurs, the state of the source system is correctly restored to the state of the target system. Moreover, the approach is generic and it can be instantiated to any number of systems, thus it ensures scalability. An instantiation mechanism based on the definition of witnesses has been defined. Note that, since instantiation is performed by refinement, solely the last refinement step shall be proved at each instantiation. It corresponds to checking that the witnesses belong to the set of systems. From a methodological point of view, when instantiation by model checking does not scale up, one may use the defined instantiation mechanism based on witnesses. The whole proposed approach has been modeled within the Event-B method. Finally, the approach developed in this paper has been defined for system reconfiguration, but it can be deployed for other cases like redundancy with dissimilar systems or system monitoring.

REFERENCES

- [1] J.-R. Abrial, *Modeling in Event-B: System and Software Engineering*, 1st ed. New York, NY, USA: Cambridge University Press, 2010.
- [2] J.-R. Abrial, M. Butler, S. Hallerstede, T. S. Hoàng, F. Mehta, and L. Voisin, "Rodin: an open toolset for modelling and reasoning in Event-B," *International Journal on Software Tools for Technology Transfer*, vol. 12, no. 6, pp. 447–466, 2010.
- [3] G. Babin, Y. Aït-Ameur, and M. Pantel, "Formal verification of runtime compensation of web service compositions: A refinement and proof based proposal with Event-B," in *Services Computing (SCC), 2015 IEEE International Conference on*, June 2015, pp. 98–105.
- [4] J. Bendisposto, J. Clark, I. Dobrikov, P. Karner, S. Krings, L. Ladenberger, M. Leuschel, and D. Plagge, "Prob 2.0 tutorial," in *Proceedings* of the 4th Rodin User and Developer Workshop, ser. TUCS Lecture Notes, 2013.
- [5] Y. Bertot and P. Castéran, Interactive theorem proving and program development: Coq'Art: the calculus of inductive constructions, ser. Texts in Theoretical Computer Science. Springer Verlag, 2004.
- [6] T. Nipkow, L. C. Paulson, and M. Wenzel, *Isabelle/HOL A Proof Assistant for Higher-Order Logic*, ser. Lecture Notes in Computer Science. Springer, 2002, vol. 2283.
- [7] I. Pereverzeva, E. Troubitsyna, and L. Laibinis, "A refinement-based approach to developing critical multi-agent systems," *International Journal of Critical Computer-Based Systems*, vol. 4, no. 1, pp. 69–91, 2013.
- [8] I. Lopatkin and A. Romanovsky, "Rigorous development of faulttolerant systems through co-refinement," School of Computing Science, University of Newcastle upon Tyne, Tech. Rep., January 2014.
- [9] R. Mirandola, P. Potena, and P. Scandurra, "Adaptation space exploration for service-oriented applications," *Science of Computer Programming*, vol. 80, Part B, pp. 356 – 384, 2014.
- [10] M. U. Iftikhar and D. Weyns, "A case study on formal verification of self-adaptive behaviors in a decentralized system," vol. 91, 2012, pp. 45–62.
- [11] A. Bhattacharyya, "Formal modelling and analysis of dynamic reconfiguration of dependable systems," Ph.D. dissertation, Newcastle University School of Computing Science, January 2013.
- [12] R. Rodrigues, B. Liskov, K. Chen, M. Liskov, and D. Schultz, "Automatic reconfiguration for large-scale reliable storage systems," *Dependable and Secure Computing, IEEE Transactions on*, vol. 9, no. 2, pp. 145–158, March 2012.