

# Absolute cross sections and asymmetry parameters for photodetachment of $C^--({}^4S^o)$

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Raphaël Marion, Kevin Dunseath, Mariko Terao-Dunseath, Xavier Urbain. Absolute cross sections and asymmetry parameters for photodetachment of  $C^-(^4S^o)$ . Physical Review A, 2021, 103 (2), pp.023115. 10.1103/PhysRevA.103.023115. hal-03154120

## HAL Id: hal-03154120 https://hal.science/hal-03154120v1

Submitted on 5 Mar 2021

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Absolute total cross sections and asymmetry parameters for the photodetachment of the  $^4S^o$  ground state of  $C^-$  are reported for photon energies ranging from threshold to 6 eV. The total cross sections were measured using the Animated Crossed Beam technique incorporating corrections for saturation, while the asymmetry parameters were obtained using Velocity Map Imaging spectrometry. The measured values are in good agreement with theoretical results obtained from an R-matrix calculation using polarized pseudostates.

#### PACS numbers: 32.80.Gc, 31.10.+z, 33.60+q

#### I. INTRODUCTION

The study of the photodetachment of negative ions, especially of open-shell systems such as carbon and oxygen, presents a double interest: they play an important role in astrophysics and atmospheric physics [1], and provide stringent tests for the description of electron correlation. The electron affinity, or energy difference between the ground states of the negative ion and the residual atom, is indeed much smaller than the ionization energy of atoms and cations. While the variational principle applies independently for each system, it is much more difficult to guarantee a well-balanced calculation for both systems, and hence an accurate value for the electron affinity.

A comprehensive review of the knowledge of the structure and dynamics of atomic anions has been compiled by Andersen [2], who focused in particular on the decade between 1994 and 2004. In the case of  $O^-$ , there was a long-standing discrepancy between experiment and theory, which was only recently resolved by new measurements using the Animated Crossed Beam technique to determine absolute total cross sections [3]. These are about 17% larger than the earlier data, and are in very good agreement with new theoretical results presented in the same publication. Since the most extensive set of experimental near-threshold photodetachment cross sections for  $C^-({}^4S^o)$  dates back to 1962 and was normalized using the earlier data for  $O^-$  [4], a direct measurement appears timely.

The carbon anion exists in two bound states: the ground state  $C^-(1s^22s^22p^3 \, ^4S^o)$ , which has an affinity of 1.2621226(11) eV with respect to the  $C(1s^22s^22p^2 \, ^3P_0)$  ground level [5], and an excited state  $C^-(1s^22s^22p^3 \, ^2D^o)$  which is very weakly bound by about 33 meV [6]. In this work, we consider only photodetachment from the  $^4S^o$  ground state. At low energy, this results in the ejection of a  $^2P$ 0 bound electron into the  $^2S^o$ 1 residual atom in its ground state:

$$C^{-}(1s^{2}2s^{2}2p^{3} {}^{4}S^{o}) + \gamma \rightarrow C(1s^{2}2s^{2}2p^{2} {}^{3}P) + e^{-}(\ell = 0, 2).$$

<sup>44</sup> Above 4eV, it becomes possible to leave the resid-<sup>45</sup> ual atom in its first spin-allowed excited state, <sup>46</sup>  $C(1s^22s2p^3{}^5S^o)$ , while ejecting a *p*-wave photoelectron:

$$C^{-}(1s^{2}2s^{2}2p^{3} {}^{4}S^{o}) + \gamma \rightarrow C(1s^{2}2s2p^{3} {}^{5}S^{o}) + e^{-}(\ell = 1).$$

<sup>47</sup> As the photon energy increases, more final excited states of the residual atom become accessible. In work pub<sup>48</sup> lished just after the review by Andersen [2], Zhou et<sup>50</sup> al. [7] computed the photodetachment cross section up 
<sup>51</sup> to 13 eV, including the excitation of the residual atom 
<sup>52</sup> up to the  $C(1s^22s2p^3 \, ^5P^o)$  state. At yet higher pho<sup>53</sup> ton energies, core-hole ionization opens up and multi<sup>54</sup> ple photodetachment of  $C^-$  takes place, as studied by 
<sup>55</sup> Gibson et al. [8], and more recently, in the comprehen<sup>56</sup> sive work on inner-shell photodetachment conducted by 
<sup>57</sup> Perry-Sassmannshausen et al. [9].

The structure of the paper is as follows: the experise mental method used to determine the absolute cross sections and the asymmetry parameter  $\beta$  for photodetachment is described in Sec. II; Sec. III explains how carbon wave functions were optimized in view of new *ab initio* R-matrix calculations; results and comparison with previous data are detailed in Sec. IV. The conclusions and perspectives for future work are presented in Sec. V.

#### II. EXPERIMENT

Our experimental method has been presented in detail 68 in previous publications [3, 10, 11]. We will therefore only describe the main features of the different techniques vi used in the current work, in particular the novel approach used to determine corrections for saturation effects when using pulsed lasers.

#### A. Experimental Setup

The experimental setup can operate in two independent modes and is shown schematically in Fig. 1. The atomic beam is produced by a duoplasmatron source  $^{77}$  filled with  $\rm CO_2$  gas, at a potential of 4 kV. A permanent

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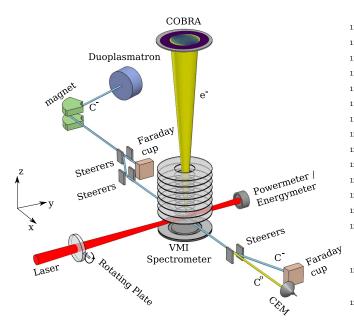


FIG. 1. Experimental setup

Photon energies up to  $6\,\mathrm{eV}$  are reached using an external 142 statistics) carried out at each offset Z: beta barium borate (BBO) crystal.

In the first mode, based on the Animated Crossed 91 Beam technique, a polarizing beam splitter combined 92 with a half-wave plate selects the horizontal polarization  $_{93}$  and tunes the energy of the laser pulses. The animation 94 of the laser beam is carried out by rotating a 12 mm 95 thick antireflection coated plate whose axis lies perpen-96 dicular to the laser beam propagation axis. The pulse  $_{97}$  energy, tuned to about  $20\,\mu\mathrm{J}$ , is measured by a Thorlabs 98 ES111C pyroelectric energy sensor while the continuous 99 power is measured by a Thorlabs S310C thermal power 100 sensor and varied between 40 and 100 mW depending on 101 the solid state laser. During experiments with continu-102 ous light, the anion beam current is also continuous while ton beams cross at right angles. The neutrals follow a 106 straight trajectory and are counted with a channel elec-107 tron multiplier (CEM, KBL 25RS from Sjuts Optotech-108 nik) with a high detection efficiency. The anion beam 109 is deflected by an electrostatic field and the current is 110 measured with a Faraday cup.

112 on while working at a higher pulse energy (250  $\mu$ J) with 154 factorized into a normalized distribution  $\hat{\rho}(x, y, z)$  valid

much shorter anion packets  $(1 \mu s)$  in order to increase 114 the signal-to-noise ratio (SNR). The photoelectrons are extracted perpendicularly by an electrostatic plate and directed to the electrostatic lens designed following [12]. The repeller electrode is split to correct the trajectory of the anions as explained in [13]. Photoelectrons are detected using a COBRA system [14], comprising three stacked microchannel plates (MCP), a phosphor screen, a 121 metal-oxide semiconductor (CMOS) camera and a waveform digitizer.

Data acquisition as well as fast digital control are achieved using a field-programmable gate array (FPGA) board while the whole setup is supervised by a LabVIEW 126 application.

#### Absolute cross section measurements

#### 1. The ACB technique

The absolute measurement of the cross section is based on the Animated Crossed Beam (ACB) technique [10], in 131 which the laser beam is periodically swept through the 78 magnet performs a mass selection and the cleaned and 132 perpendicular anion beam. The laser is characterized by  $_{79}$  collimated beam (diameter 1 mm) is then bunched by an  $_{133}$  its frequency  $\omega$ , pulse duration  $T_p$  and, in a reference 80 electrostatic deflector in front of an aperture to limit de- 134 frame whose origin is fixed at the beam intersection in 81 tector ageing. After interaction, residual anions are col- 135 the center of the interaction zone, by the flux density 82 lected in a Faraday cup in order to measure the current 136 of photons  $\phi_p(x,y,z-Z,t)$  in the direction of propaga- $_{83}$   $I_0$ , which is typically 100 pA. Continuous light sources are  $_{137}$  tion. Z is the offset of the laser beam as it is swept  $^{84}$  provided by different solid-state lasers at  $778\,\mathrm{nm}$ ,  $532\,\mathrm{nm}$   $^{138}$  across the anion beam. The normalized photon flux den-<sub>85</sub> and  $405\,\mathrm{nm}$  wavelengths. The pulsed light source is from  $_{139}$  sity,  $\hat{\phi}(x,y,z,t)$ , is assumed to be constant from pulse to 86 an OPO laser system (NT342A-30 from Ekspla), tunable 140 pulse while the energy  $E_{p,Z}$  may substantially vary for from 2600 nm to 225 nm, with a repetition rate of  $30 \,\mathrm{Hz}$ . <sup>141</sup> each pulse p of the  $n_Z$  laser shots (typically 120 for good

$$\phi_p(x, y, z - Z, t) = \frac{E_{p, Z}}{\hbar \omega} \hat{\phi}(x, y, z - Z, t).$$

The C<sup>-</sup> anions, produced in a duoplasmatron source with a bias potential  $-V_S$ , have a nominal velocity v= $_{145}$   $\sqrt{2 eV_S/M_{C^-}}$ , where  $M_{C^-}$  is the mass of  $C^-$  and e is the elementary charge. At any instant during pulse p, 147 as the velocity  $v \ll c$ , the laser illuminates an almost static distribution of anions  $\rho(x,y,z,t)$ , governed by the 149 equation

$$\vec{\nabla} \cdot \vec{j} + \frac{\partial \rho}{\partial t} = -\sigma \phi \rho,$$

with pulsed light, the anions are bunched at 30 Hz in 3.3 where  $\vec{j} = \rho \vec{v}$  is the anion current density and  $\sigma$  the pho-104 ms packets. In the interaction zone, the anion and pho- 151 todetachment cross section. The solution of this equation 152 for the pulse starting at  $t = t_{p,Z}$  is formally given by

$$\rho_p(x, y, z, t; Z) = \rho(x, y, z; t_{p,Z})$$

$$\times \exp\left\{-\sigma \int_{-\infty}^x \frac{dx'}{v} \phi_p(x', y, z - Z, t - \frac{x - x'}{v})\right\}.$$

In the second mode, the VMI spectrometer is turned 153 The initial distribution of anions,  $\rho(x, y, z; t_{p,Z})$ , can be

155 for all pulses and a fluctuating magnitude related to the 156 total current  $I_{p,Z} = \iint e\rho v dy dz$  delivered by the source 157 to the entrance of the interaction zone at the time of the 158 laser shot:

$$\rho(x, y, z; t_{p,Z}) = \frac{I_{p,Z}}{ev} \hat{\rho}(x, y, z).$$

For a detector of neutrals located at a position  $x_d$  far after the interaction zone, with an efficiency  $\eta$  and an active surface  $S_{\rm d}$  larger than the cross-sectional area of 162 the anion beam, we can express the count of neutrals for p a pulse p as

$$\begin{split} N_{p,Z} &= \eta \int dt \iint_{S_{d}} dy dz \ v \ \rho(x_{d}, y, z; t_{p,Z}) \\ &\times \left[ 1 - \exp \left\{ -\sigma \int_{-\infty}^{x_{d}} \frac{dx'}{v} \phi_{p}(x', y, z - Z, t - \frac{x_{d} - x'}{v}) \right\} \right]. \end{split}$$

If the argument of the exponential in Eq. (1) is small 165 enough so that a first order expansion is sufficient, the <sub>166</sub> neutral count  $N_{p,Z}$  is proportional to the cross section  $\sigma$ . After normalizing  $N_{p,Z}$  with respect to the current  $I_{p,Z}$ and energy  $E_{p,Z}$  and integrating over all laser offsets Z, the remaining integrals involve only  $\hat{\phi}$  and  $\hat{\rho}$ , which result 170 in a constant scale factor whose determination does not require any further assumptions about the beam profiles. We obtain the ACB expression for the photodetach-173 ment cross section:

$$\sigma_{\text{pulsed}}^{\text{ACB}} = \frac{1}{\eta} \sum_{Z} \frac{\Delta Z}{n_Z} \sum_{p=1}^{n_Z} \frac{\hbar \omega}{E_{p,Z}} \frac{\text{e}v}{I_{p,Z}} N_{p,Z}.$$
 (2)

This highlights the major advantage of the ACB tech-175 nique; the experimental cross section does not depend 199 Inserting this in Eq. (2) yields a self-consistent expression beam interaction experiments.

For continuous lasers, the integration over pulse dura-180 tion is irrelevant and the production rate  $R_Z$  of neutrals 181 is directly measured by the CEM and normalized to the 182 power  $P_Z$  of the laser beam at position Z instead of the 183 pulse energy  $E_{p,Z}$ , and to the anion current  $I_Z$ :

$$\sigma_{\rm cont}^{\rm ACB} = \frac{1}{\eta} \sum_{Z} \Delta Z \frac{\hbar \omega}{P_Z} \frac{ev}{I_Z} R_Z.$$
 (3)

#### Saturation effects from a pulsed laser

The ACB technique has been successfully implemented 186 and used to determine absolute cross sections for many 187 electron-ion [15–17] and electron-atom [18, 19] interac-188 tions as well as for the photodetachment of H<sup>-</sup> [20] and 189 O<sup>-</sup> [3, 11]. The few necessary assumptions that are satis-190 fied in the case of continuous lasers however do not always 191 hold for pulsed lasers: as the peak intensity may become

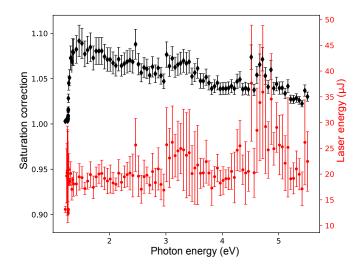


FIG. 2. Correction of saturation for the cross section at each wavelength, and fluctuations of the pulse energy of the laser. Full lozenge: correction of saturation; full circle: pulse energy.

192 high even for pulses of relatively low energy, the first-193 order approximation for the exponential function appear-194 ing in Eq. (1) may be no longer valid, particularly in the 195 infrared domain or when the cross section becomes large. 196 Higher order terms in the expansion of the exponential in Eq. (1) contribute an extra term  $s_p$  representing the 198 phenomenon of saturation:

$$\int dt \sum_{Z} \frac{\hbar \omega}{E_{p,Z}} \left[ 1 - \exp \left\{ -\sigma \int_{-\infty}^{x_{\rm d}} \frac{dx'}{v} \phi_p \right\} \right]$$

$$\equiv \frac{\sigma}{v} \left[ 1 - s_p(\sigma) \right].$$

on the geometrical overlap of the beams, which is critical 200 for  $\sigma$  which must be solved by iteration, starting from and difficult to measure accurately in standard beam-  $\sigma_0 = \sigma^{ACB}$ , until a stationary value of the cross section

$$\sigma_{i+1} = \frac{\sigma^{ACB}}{1 - s(\sigma_i)},\tag{4}$$

where  $s(\sigma)$  is the correction for saturation averaged over 204 the  $n_Z$  laser pulses, taking into account the fluctuations 205 of energy shown in Fig. 2.

Unfortunately, assumptions concerning the beam profiles are now unavoidable. Provided that the Rayleigh 208 length is greater than the diameter of the circular an-209 ion beam, which has a waist  $w_0 \in [250, 300] \mu m$  and 210 a pulse duration  $T_p \in [7,9]$  ns, we can expand the  $_{\mbox{\scriptsize 211}}$  laser profile about the coordinates of its maximum  $t_M$  $(-T_p/2 \le t - t_M \le T_p/2)$  as

$$\hat{\phi}(x, y, z, t) = \frac{2}{T_p} \frac{2}{\pi w_0^2} \cos^2 \left( \pi \, \frac{t - t_M}{T_p} \right) \times \exp \left\{ -2 \, \frac{x^2 + z^2}{w_0^2} \right\}. \tag{5}$$

The factor by which  $\sigma^{ACB}$  must be multiplied to cor- 263 214 rect for saturation effects is shown in Fig. 2. Its effect 215 is to slightly increase the apparent cross section, par-216 ticularly at lower photon energies. Since assumptions 217 concerning the beam profiles are needed to estimate the 218 saturation correction, it may seem that the main advan-219 tage of the ACB technique is somehow lost. The cor-220 rections however remain small and the whole procedure 221 can be validated by comparison with measurements us-222 ing a continuous laser, which is not subject to saturation, 223 or obtained with a pulsed laser at lower energy and/or 224 higher frequency, as will be shown in Sec. IV.

#### Differential cross section measurements

In the case of detachment by linearly polarized light, 227 in the dipole approximation, additional information pro-228 vided by the angular distribution of photoelectrons can 229 be conveniently summarized using the asymmetry pa-230 rameter  $\beta$ ,

$$\frac{d\sigma}{d\Omega} = \frac{\sigma}{4\pi} \left[ 1 + \beta P_2(\cos \theta) \right],\tag{6}$$

 $_{231}$  relating the differential cross section  $d\sigma/d\Omega$  to the total  $_{280}$  ciency of another CEM detector, older and smaller, and 232 cross section  $\sigma$ , where  $P_2$  is the second-order Legendre 281 obtained a value of  $\eta = 90 \pm 1\%$ . 233 polynomial and  $\theta$  is the angle between the photoelectron 282  $^{234}$  momentum and the laser polarization axis. The parame-  $^{283}$  events detected during the same laser-neutral coincidence  $_{235}$ ter  $\beta$  can be measured by means of a Velocity Map Imag-  $_{284}$  time window will be counted as one. Under normal con-236 ing (VMI) spectrometer: photodetachment occurs inside 285 ditions, with a weak anion current and low photodetach- $_{237}$  an electric field perpendicular to both the anion beam  $_{286}$  ment rates, the probability of such a counting loss is  $_{238}$  and the direction of the laser polarization. This elec-  $_{287}$  small. We expect the number  $m_p$  of neutrals effectively  $_{239}$  tric field slightly bends the trajectory of the anion beam  $_{288}$  produced in a pulse to follow Poisson statistics, characwhile totally separating out the less energetic photoelec-241 trons. Following [21], this almost perpendicular photo-242 electron beam is then guided through a thick electrostatic 243 lens formed by stacking biased circular electrodes whose 244 voltages have been optimized by simulation in order to 246 tor is placed at the focal plane where the image formed is 291 mial statistics: 247 the Fourier transform of the transverse momentum of the photoelectron cloud which, in the absence of aberrations, 249 is independent of the location where photodetachment 250 took place.

Outside the lens, the velocity of the photoelectrons de-252 pends on the kinetic energy release (KER) of the pho-253 todetachment channel and on the bias potential applied to the repeller electrode. The photoelectrons therefore travel on expanding Newton spheres that are projected 256 onto the detector screen. Assuming an azimuthal sym-257 metry, it is possible to reconstruct from the 2D image 258 the 3D angular distribution of the photoelectrons by 259 an inverse Abel transform, for which many computa-260 tional techniques are available. In this work, we use the 261 MEVELER algorithm based on a Bayesian approach, de-262 velopped in [22].

#### Analysis of experimental uncertainties

#### 1. Absolute cross sections

By detecting both products of the photodetachment 266 in coincidence, the efficiency  $\eta$  of the CEM can be esti-267 mated. Using the logical conjunction symbol  $\wedge$ , we de-268 note by  $(e \wedge l)$  the detection of a photoelectron in coin-269 cidence with a laser pulse, and by  $(n \wedge e \wedge l)$  the simul-270 taneous detection of a neutral. Provided all the detected 271 electrons are produced by photodetachment, the bino-272 mial statistical estimate of  $\eta$  and its variance are

$$\hat{\eta} = \frac{\#(n \wedge e \wedge l)}{\#(e \wedge l)};$$

$$\operatorname{Var}[\hat{\eta}] = \frac{\hat{\eta}(1 - \hat{\eta})}{\#(e \wedge l)},$$

273 where the symbol # stands for the number of coinci-274 dences of a given type. This estimate can be used to cal-275 ibrate new detectors or to compensate for ageing, with an 276 accuracy of about one percent, depending on the number (6) 277 of events. For the present experiment we have observed 278 a quite stable value of  $\eta = 95 \pm 0.5\%$  during the whole 279 process. To test the method, we have analysed the effi-

In ACB measurements with pulsed lasers, two or more 289 terized by a mean value  $\hat{m}$ :

$$P[m_p|\hat{m}] = \frac{\hat{m}^{m_p}}{m_p!} \exp(-\hat{m}),$$

achieve the best resolution. The position sensitive detec- 200 and the number of detected neutrals  $m_d$  to follow bino-

$$P[m_d = y | \eta, m_p] = {m_p \choose y} \eta^y (1 - \eta)^{m_p - y}.$$

292 The value of  $\hat{m}$  may be deduced from the total number  $293 m_T$  of counted neutrals for n pulses by noting that the <sup>294</sup> apparent rate per pulse  $\bar{m} = m_T/n \, (\bar{m} < 1)$  is the com-295 plement of the probability of no detection, yielding the 296 relation:

$$\begin{split} \bar{m} &= {\rm P} \left[ m_d \geq 1 \right] = 1 - {\rm P} \left[ m_d = 0 \right] \\ &= 1 - \sum_{m_p} {\rm P} [m_d = 0 \, | \eta, m_p ] \, {\rm P} [m_p | \hat{m}] \\ &\Longrightarrow \bar{m} = 1 - e^{-\eta \hat{m}}. \end{split}$$

In the following, the quantity  $\eta \hat{m}$  will be denoted by  $\hat{m}_d$ .

The background contribution to  $\hat{m}_d$  is estimated by duplicating the coincidence time window with an arbitrary 300 delay and applying the same Poisson correction to the  $_{301}$  total number  $b_T$  of neutrals detected out of coincidence  $_{302}$  during the same  $n_Z$  pulses. With these definitions, the  $_{303}$  mean rate and variance for neutral detection per pulse 304  $N_Z$  entering Eq. (2) is given by

$$\hat{N}_Z = \hat{m}_{d,Z} - \hat{b}_{d,Z};$$

$$\operatorname{Var}\left[\hat{N}_Z\right] = \frac{\hat{m}_{d,Z} + \hat{b}_{d,Z}}{n_Z}.$$

305 with  $\hat{m}_{d,Z} = -\ln(1 - \bar{m}_Z)$  and  $\hat{b}_{d,Z} = -\ln(1 - \bar{b}_Z)$ .

For continuous light, we have improved the estimate 307 of the background compared to our previous setup [3] 308 by implementing a mechanical shutter to measure al $n_s$  times at  $_{310}$  each offset Z of the laser beam during the whole sweep 311 time, rather than only at the beginning and at the end of  $_{312}$  each experimental run. With a switching delay  $T_s$  lead-313 ing to durations of direct and background measurements  $T_m = T_b = n_s T_s$ , during which  $T_T$  and  $T_T$  neutrals are 315 respectively counted, the detection rate  $R_Z$  entering Eq. 316 (3) is estimated by

$$\hat{R}_Z = \hat{R}_{m,Z} - \hat{R}_{b,Z};$$

$$\operatorname{Var}\left[\hat{R}_Z\right] = \frac{\hat{R}_{m,Z} + \hat{R}_{b,Z}}{n_c T_c};$$

317 with  $\hat{R}_{m,Z} = m_{T,Z}/T_m$  and  $\hat{R}_{b,Z} = b_{T,Z}/T_b$ .

The contribution of the variance of the signal to the 319 variance of the experimental cross section is given by

$$\operatorname{Var}[\hat{\sigma}_{\text{pulsed}}] = \sum_{p,Z} \left( \frac{1}{n_Z} \frac{\Delta Z}{\eta} \frac{\hbar \omega}{E_{p,Z}} \frac{\text{e}v}{I_{p,Z}} \right)^2 \operatorname{Var}[\hat{N}_{p,Z}]$$
$$\operatorname{Var}[\hat{\sigma}_{\text{cont}}] = \sum_{Z} \left( \frac{\Delta Z}{\eta} \frac{\hbar \omega}{P_Z} \frac{\text{e}v}{I_Z} \right)^2 \operatorname{Var}[\hat{R}_Z].$$

320 Sufficient internal statistical precision is usually obtained <sub>321</sub> by one Z-scan for a continuous laser and by 5 Z-scans 322 for pulsed light.

A final source of uncertainties arises from the ob-324 served fluctuations of measured cross sections over different runs, which might be due to variations of spatial  $_{326}$  distributions, especially in the laser beam. Fortunately,  $_{343}$  where p(v) is the radial velocity distribution normalized 327 these variations average to zero so that increasing the 344 so that  $\int p(v)dv = 1$  and  $P_{\ell}$  is the Legendre polynomial 328 number of runs (a repeatability test) is sufficient to im-329 prove the external statistics and reach the objective of 330 2% uncertainty for a pulsed laser and 0.5% for a contin-331 uous laser. The final values are obtained by calculating 332 the weighted average over several runs:

TABLE I. Typical values for experimental uncertainties using the ACB technique.

the Neb teeninque.	
Uncertainties Type A (statistical):	
Detector efficiency	0.5~%
Correction for saturation	1 %
Statistical uncertainties with pulsed laser	2%
Statistical uncertainties with CW laser	0.5~%
Combined uncertainties type A:	
Pulsed laser	2.3 %
CW laser	0.7~%
Uncertainties Type B (systematic):	
Powermeter / Energymeter	3.1 %
Resolution	0.5~%
Calibration	3 %
Electrometer	1.1 %
Resolution	0.5~%
Calibration	1 %
Vertical displacement Z	2 %
Combined uncertainties type B:	3.8~%
Final combined uncertainties:	
Pulsed Laser	4.5~%
Continuous Laser	3.9~%

$$\hat{\sigma}_{\text{pulsed}}^{ACB} = \sum_{i} \frac{\hat{\sigma}_{j}}{\text{Var}[\hat{\sigma}_{j}]} / \sum_{i} \frac{1}{\text{Var}[\hat{\sigma}_{j}]}; \quad (7)$$

$$\operatorname{Var}[\hat{\sigma}_{\text{pulsed}}^{ACB}] = 1 / \sum_{j} \frac{1}{\operatorname{Var}[\hat{\sigma}_{j}]}.$$
 (8)

A summary of typical uncertainty values is presented 334 in Table I, following [23] for the classifications and rules 335 for combining experimental uncertainties.

#### Asymmetry parameters

To the best of our knowledge, there are no reliable statistical estimators for asymmetry parameters. Here we propose one such estimator for N events.

We start from a general probability distribution in spherical coordinates with azimuthal symmetry:

$$P(v,\theta,\phi) = \frac{p(v)}{4\pi v^2} \left( \sum_{\ell=0}^{L} \beta_{\ell} P_{\ell}(\cos\theta) \right), \tag{9}$$

342 normalized so that

$$\int_0^\infty \int_0^\pi \int_0^{2\pi} dv \, d\theta \, d\phi \, v^2 \sin \theta \, P(v, \theta, \phi) = 1,$$

of degree  $\ell$ . The coefficients  $\beta_{\ell}$  are then given by

$$\beta_{\ell} = (2\ell + 1) \int_0^{\infty} \int_0^{\pi} \int_0^{2\pi} dv \, d\theta \, d\phi \, v^2 \sin \theta$$
$$\times P_{\ell}(\cos \theta) P(v, \theta, \phi). \quad (10)$$

 $_{346}$  The right hand side of this equation can be interpreted as the expectation value  $E[X^{[\ell]}]$  of  $X^{[\ell]} = (2\ell+1)P_{\ell}(\cos\theta)$ 348 with respect to the probability distribution  $P(v, \theta, \phi)$ . We can also define the variance of  $X^{[\ell]}$  as

$$Var[X^{[\ell]}] = E[(X^{[\ell]})^2] - \left(E[X^{[\ell]}]\right)^2$$
$$= (2\ell + 1)^2 \sum_{\ell'=0}^{L} \begin{pmatrix} \ell & \ell & \ell' \\ 0 & 0 & 0 \end{pmatrix}^2 \beta_{\ell'} - \beta_{\ell}^2. (11)$$

We now consider an experiment providing N independent observations  $\theta_i$ ,  $i \in \{1, ..., N\}$ , of the polar angle 352  $\theta$ . The sample mean

$$\hat{\beta}_{\ell} = \frac{1}{N} \sum_{i=1}^{N} X_i^{[\ell]} = \frac{2l+1}{N} \sum_{i=1}^{N} P_l(\cos \theta_i), \qquad (12)$$

353 is then an unbiased estimator which, following the Central Limit Theorem, converges to  $\beta_{\ell}$  as  $N \to \infty$ . The experimental variance for large sample sizes is  $Var[X^{[\ell]}]/N$ , which vanishes as  $N \to \infty$  so that the estimator is consis-357 tent. We note that the presence of the Wigner 3-j symbol 358 in Eq. (11) implies that the precision of  $\hat{\beta}_{\ell}$  is blurred by 359 all the even distributions  $P_{\ell'}(\cos\theta)$  with  $\ell'$  even between  $_{360}$  0 and  $2\ell$ .

In the specific case of photodetachment by linearly polarized light, the dipole selection rules lead to the expres-363 sion (6) for the differential cross section, which involves 364 only  $\ell=0$  and 2. Since  $\beta_0=1,\,\beta_2$  is known as the asym- $_{365}$  metry parameter commonly denoted  $\beta$ . For the same 366 reasons, the upper limit of the summations over  $\ell$  or  $\ell'$ 367 in Eqs. (9) and (11) is L=2. The statistical precision 368 for the estimation of  $\beta$ , from Eq. (11) with  $\ell=2$ , only 369 contains contributions from  $\ell'=0$  and 2, leading to

$$\frac{5}{N} + \frac{10\hat{\beta}}{7N} - \frac{\hat{\beta}^2}{N}.$$
 (13)

These results, however, cannot be directly applied to 371 our data since the spherical distribution itself is not 372 known experimentally, only its projection. The Abel in-373 version provided by the maximum entropy (MAXENT) <sup>374</sup> approach[22] gives an estimate of the distribution in an 375 un-normalized form:

$$\mathcal{P}(v,\theta,\phi) = \frac{1}{4\pi v^2} \left[ Q_0(v) + Q_2(v) P_2(\cos\theta) \right].$$
 (14)

376 Integrating Eq. (14) over the velocity space gives the total 411 number of events  $N = \int Q_0(v) dv$ , while direct compari-378 son with Eq. (9) yields an estimate  $\hat{\beta}(v) = Q_2(v)/Q_0(v)$ . The dependency of  $\hat{\beta}$  on v, which arises from the unavoid- 413 rameters were calculated using standard, non-relativistic 380 able dispersion associated with the limited precision of 414 R-matrix theory as implemented in the UK APAP 381 the experimental setup, prevents a direct determination 415 (Atomic Processes for Astrophysical Plasmas) suite of 382 of the best and unique value of the asymmetry parameter 416 computer codes [24]. In this approach, initially devel-<sub>383</sub> and its precision from  $Q_0(v)$  and  $Q_2(v)$ , even for cases <sub>417</sub> oped in order to study resonances in nucleon-nucleus col-384 with a single detachment channel.

TABLE II. Typical values for experimental uncertainties in the asymmetry parameters.

Systematic errors:	
Circularization and Abel inversion	$\Delta \beta = 0.01$
Background filtering	$\Delta \beta = 0.01$
Statistical uncertainties:	$\Delta \beta = 0.007$

Following Eq. (10), we define the experimental estimate of  $\hat{\beta}$  as the expectation value of  $X^{[2]}$  with respect to the probability distribution (14) normalized by the 388 factor 1/N:

$$\hat{\beta} = E[5P_2(\cos\theta)]$$

$$= \frac{5}{N} \int_0^\infty \int_0^\pi \int_0^{2\pi} dv \, d\theta \, d\phi \, v^2 \sin\theta$$

$$\times P_2(\cos\theta) \mathcal{P}(v, \theta, \phi),$$

389 which yields

$$\hat{\beta} = \frac{1}{N} \int Q_2(v) dv = \frac{\int Q_2(v) dv}{\int Q_0(v) dv}.$$
 (15)

In practice, the definition of the limits of the integrals over v requires some prior information about the phys-392 ical process in order to define for example the number 393 of peaks expected and their energy range. In this work, 394 where all the peaks are clearly identified, we select the 395 range  $\Delta v$  of v such that  $Q_0(v)$  is greater than 10% of the local maximum. The number of events,  $\int_{\Delta v} Q_0(v) dv$ , 397 is of the order of 10<sup>5</sup>, leading to an uncertainty, given by Eq. (13), of  $\Delta \hat{\beta} \approx 0.007$ . To these statistical uncer-399 tainties, we add an absolute error  $\Delta\beta = 0.01$  to take 400 into account the systematic errors of circularization of 401 the data and the internal uncertainties arising from the 402 MEVELER algorithm. For photon energies larger than 3.4 eV, where background noise starts to appear, we include an additional  $\Delta\beta = 0.01$  in the absolute error to 405 account for filtering in the background procedure. Above 406 4 eV, the increasingly large background noise renders the 407 filtering procedure less effective and the parameter  $\beta$  be-408 comes inaccessible.

Typical values for experimental uncertainties in the 410 asymmetry parameters are summarized in Table II.

#### III. THEORY

Photodetachment cross sections and asymmetry pa-418 lisions [25], configuration space is naturally divided in

419 two parts: the inner region, where all (N+1) electrons 420 interact strongly and the solution is expanded in a basis 421 of discrete functions analogous to bound states in a finite 422 box, built using a set of N-electron target wave functions  $_{423}$  coupled to R-matrix continuum orbitals describing the 424 projectile electron; the outer region, where the solution 425 can be written as the simple product of target and projec-426 tile wave functions. In atomic physics, all potentials are 427 known but long-range couplings in the outer region must 428 be fully taken into account. The collisional approach 429 can be extended to photoionization and photodetache-430 ment by considering these processes as half-collisions: 431 the asymptotically vanishing initial bound state is the solution of the close-coupling problem with all channels closed. Such a solution only exists for a negative energy 434 that must be found numerically by an iterative approach. 435 In the weak field regime considered here, the photode-436 tachment cross section can be evaluated using perturba-437 tion theory: it is proportional to the modulus square of 438 the dipole matrix element between the initial bound state 439 of C<sup>-</sup> and a final continuum state of the neutral atom and 440 an ejected photoelectron. This collisional wave function 441 is determined at each photoelectron energy by matching 442 at the boundary a the amplitude of the solutions of the 443 inner and outer regions using the inverse log-derivative matrix. Full details of the R-matrix method are given in [26], in particular chapter 8 which treats photoionization.

In the spectral range covered by our experiment, we 447 consider photodetachment of  $C^{-}(1s^22s^22p^3 {}^4S^o)$ , leav-448 ing the residual atom in one of the target states  $C(1s^22s^22p^2\,^3P)$  and  $C(1s^22s2p^3\,^5S^o)$ . The key point is to determine a set of atomic orbitals suitable, in a configuration interaction approach, for describing electron correlations in the inner region, delimited by the spatial extension of the most diffuse target state. The inner 454 region therefore does not need to encompass the entire 455 charge distribution of  $C^-(1s^22s^22p^3 {}^4S^o)$ . The orbitals 456 must of course reproduce as accurately as possible not 457 just the energy levels of the residual atom but also its 458 electron affinity, which is very sensitive to the polariza-459 tion of the target in the presence of the extra electron. 460 The challenge is to optimize a finite set of orthonormal 461 orbitals while taking into account all these physical ef-462 fects.

 $^{465}$  matrix calculations. The  $^3P$  and  $^5S^o$  configurations aris- $^{479}$  combined with the Variable Phase Method (VPM) in the 466 ing from the main configuration  $1s^22s^22p^2$  with excita-480 asymptotic region. The energy of the  ${}^5S^o$  level with re-467 tion of up to two electrons from the n=2 shell are 481 spect to that of the ground state differs by 2.6% from  $_{468}$  included in the basis and the respective hamiltonian ma-  $_{482}$  the observed value and can be considered as sufficiently  $_{469}$  trices are diagonalized. The spectroscopic 1s, 2s and 2p  $_{483}$  good for the purpose of this work. The full average polarorbitals are Hartree-Fock orbitals [27]. The other orbitals  $^{484}$  <u>izability</u>  $\bar{\alpha}$  of  $C(1s^22s^22p^2\,^3P)$  obtained by including  $^{\bar{3}}S^{o}$ , 471 are optimized using the CIVPOL computer code [28]:  $\bar{3}s$ ,  $_{485}$   $^{3}P^{o}$  and  $^{3}D^{o}$  pseudostates is 11.58  $a_{0}^{3}$ , close to the value  $\bar{a}_{72}$   $\bar{3}p$ ,  $\bar{3}d$  and  $\bar{4}f$  are optimized on the ground state energy of  $\bar{a}_{86}$  of 11.67  $a_0^3$  from an extensive coupled cluster calculation <sup>473</sup>  $C(^3P)$ ,  $\bar{4}s$ ,  $\bar{4}p$  and  $\bar{4}d$  are optimized on the ground state <sup>487</sup> [30]. 474 polarizability.

TABLE III. Parameters of the ten Slater orbitals optimized on the energy and polarizability of the  $C(1s^22s^22p^{2\,3}P)$  ground state using the computer code CIVPOL [28].

	$C_{jn\ell}$	$I_{jn\ell}$	$\zeta_{jn\ell}$		$C_{jn\ell}$	$I_{jn\ell}$	$\zeta_{jn\ell}$
1s	23.64032	1	5.43599	2p	0.31061	2	0.98073
	4.04776	1	9.48256		1.58145	2	1.44361
	0.00110	2	1.05749		2.92085	2	2.60051
	-0.00583	2	1.52427		1.27982	2	6.51003
	0.07620	2	2.68435				
	0.15955	2	4.20096	$\bar{3}\mathrm{p}$	5.75621	2	1.55007
					-2.37862	3	1.36859
2s	-5.27596	1	5.43599				
	-0.62547	1	9.48256	$\bar{4}\mathrm{p}$	2.34572	$^{2}$	0.51316
	0.10754	2	1.05749		-3.28476	3	0.68909
	2.48567	2	1.52427		1.03114	4	0.85291
	4.57346	2	2.68435				
	-6.16698	2	4.20096	$\bar{3}d$	3.94743	3	1.89468
$\bar{3}s$	6.92570	1	2.34033	$\bar{4}\mathrm{d}$	2.78398	3	1.99721
00	-20.83502	2	2.37260	10	-0.17968	4	1.07874
	2.68194	3	1.54022		-0.11300	7	1.01014
$\bar{4}s$	3.86042	1	1.25514	$ar{4}\mathrm{f}$	5.90852	4	2.41065
	-16.39226	2	1.23475				
	17.35377	3	1.61817				
	-0.05982	4	0.91968				

TABLE IV. Energies of the  $1s^22s^22p^2$   $^3P$  and  $1s^22s2p^3$   $^5S^o$ terms of carbon, together with those of the three polarized pseudostates included in the R-matrix calculations. observed values are taken from the NIST Atomic Spectra Database [29].

	Absolute (a.u.)	Relative (eV)	Zhou <i>et al.</i> [7] (eV)	Observed (eV)
${}^{3}P_{{}^{5}S^{o}}$	-37.77831 $-37.62867$	0.0 4.07191	0.0 3.97679	0.0 4.17895
$\frac{{}^{3}P^{o}}{{}^{3}D^{o}}$ $\frac{{}^{3}S^{o}}{{}^{3}S^{o}}$	-37.40867 $-37.31503$ $-37.26368$	10.05842 12.60649 14.00380		

In Table III, we present the parameters of the ten 477 values from NIST and those of an earlier calculation by Slater-type orbitals chosen to describe carbon in our R- 478 Zhou et al. [7], who used a similar R-matrix approach

The electron affinity of the carbon ground state is cal-In Table IV, the energy of  $C(1s^22s^22p^2^3P)$  and 489 culated using the program STGB in the UK APAP suite  $_{476}$  C(1s<sup>2</sup>2s2p<sup>3</sup>  $_{5}$ S°) are compared with the recommended  $_{490}$  of codes [24]. This uses a perturbative treatment of the

491 long-range potentials in the R-matrix outer region com- 545 and the theoretical cross section is of the order of 1.5%, bined with an iterative search over negative energies to 546 less than the experimental uncertainty. find bound state solutions for the (N+1)-electron system. 547 497 continuum orbitals to ensure convergence). In addition, 551 small dip in the vicinity of the  $C(1s^22s2p^3 \, {}^5S^o)$  thresh-499 at least two electrons from the  $1s^22s^22p^3$  base configu-553 the  $C(^5S^o)$  +  $e^-(\ell=1)$  channel. 500 ration in order to obtain a bound state of C<sup>-</sup>. For the results reported below, we in fact included excitation of up to 3 electrons. For an inner region size varying between  $25 a_0$  and  $35 a_0$  and the number of continuum orbitals between 25 and 50, we obtained values of the electron affinity ranging from 1.2575 eV to 1.2613 eV, which 506 compare favourably with the value of 1.2658 eV corre-507 sponding to the energy difference between the weighted <sup>508</sup> average of the experimental fine structure levels of  $C(^3P)$ and the  $C^{-}(^{4}S^{o})$  ground state [5]. The electron affinity 510 in the calculation by Zhou et al. [7] is 1.21 eV.

#### RESULTS AND DISCUSSION

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512

#### Total cross sections

The absolute cross sections for photodetachment of

 $^{-}(^{4}S^{o})$  from our experiment are presented in Fig. 3 and 515 compared with those by Seman and Branscomb [4] and 516 Haeffler et al. [31]. Other data in the threshold region by Feldmann [6], Hall et al. [32] and Brandon et al. [33] are not reproduced here as they are not absolute and cover a very limited range of photon energies. Further discussion of their work can be found in the review by Andersen [2]. We first note that the cross section does not fall to 522 zero below the photodetachment threshold of  $C^{-}(^{4}S^{o})$ , which indicates that some anions are produced in the  $^2D$  554 529 range, except around 1.38 eV, just above threshold, where 560 of both sets of cross sections are relatively constant. The <sub>535</sub> by Zhou et al. [34], which suggests that the cross section <sub>566</sub> rent results, except for the first two values at about 1.5 eV  $_{536}$  for photodetachment of  $C^{-}(^{2}D)$  is of a similar order of  $_{567}$  which are then too large. magnitude to that for photodetachment of  $C^{-}(^{4}S^{o})$  over 568 The steep rise of the photodetachment cross section 538 the energy range considered, with a small peak above 569 above the  $C(^5S^o)$  threshold contrasts with the nearly <sub>540</sub> gests that the population of  $C^{-}(^{2}D)$  in our anion beam <sub>571</sub> et al. [31]. Their results were also normalized to the 541 is very small and that the measured cross sections are 572 earlier photodetachment cross sections of O<sup>-</sup> [36], but 542 relatively unaffected by the presence of this state. Even 573 renormalization with the absolute values by Génévriez et <sub>543</sub> in the worst case, near threshold, the estimate of the er-<sub>574</sub> al. [3] is inconclusive as the energy dependence is very 544 ror obtained by combining the measured branching ratio 575 different and the values are very dispersed.

Just above threshold, the cross section increases as The value of the electron affinity will thus depend of the 548  $\sqrt{E}$ , where E is the photoelectron energy, since the domsize of the R-matrix inner region and the number of con- 549 inant channel is  $C(1s^22s^22p^2\,^3P) + e^-(\ell=0)$ . Beyond tinuum orbitals used (a larger inner region requires more 550 1 eV, it increases slightly with photon energy before a we found that it was necessary to include excitation of 552 old, followed by a steep increase due to the opening of

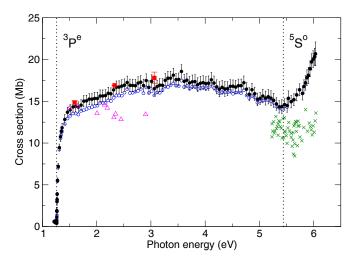


FIG. 3. Experimental cross sections for photodetachment of  $C^{-}(^{4}S^{o})$  as a function of the photon energy. Full circle: present work with a pulsed laser and correction for saturation; open circles: present work with a pulsed laser without correction for saturation; full square: present work with a continuous laser. Error bars for the pulsed laser correspond to one standard deviation as estimated by expression (8). Open triangles: Seman and Branscomb [4]; crosses: Haeffler et al. [31]. Vertical dotted lines: positions of the  $C(^3P)$  and  $C(^5S^o)$ 

In the wake of their pioneering work on the photodeexcited state. Several control measurements from thresh- 555 tachment of O<sup>-</sup> [35, 36], Seman and Branscomb [4] invesold to a photon energy of  $2.7\,\mathrm{eV}$  were conducted using 556 tigated C<sup>-</sup> in the spectral region between 0.4 and  $2.6\,\mu\mathrm{m}$ the VMI spectrometer to determine the branching ra- 557 (0.478 eV - 3.1 eV). Their relative cross sections were nortio between each channel. We found that the branching 558 malized using the absolute values for O<sup>-</sup> [36] in the phoratio is almost constant at 2% throughout the controlled 559 ton energy region between 2 and 3 eV where the values it reaches at most 4%. As this quantity depends on both 551 O<sup>-</sup> cross sections were recently found to have been unthe population and the cross section of each state entering 562 derestimated by about 20% and to be in fact slightly inthe beam composition, the problem is not experimentally 563 creasing with photon energy [3]. Renormalizing the data constrained. We will address this in future work, but 564 from [4] using the revised photodetachment cross section some insight can be gained from the theoretical study 565 of O brings them into better agreement with our cur-

the <sup>4</sup>S<sup>o</sup> photodetachment threshold. This in turn sug- <sub>570</sub> constant behaviour observed in this region by Haeffler

We also note the very good agreement between our measurements using a continuous laser and using a pulsed laser taking into account the saturation effect, validating the developments leading to the correction coefficients of Fig. 2.

In Fig. 4, the current absolute cross sections for photodetachment of  $C^-({}^4S^o)$  are compared with the results of our R-matrix calculation and those by Zhou et~al.~[7]. Other theoretical studies undertaken before 2004 [37–39] have been thoroughly discussed in [2, 7], and since the agreement with experiment tends to be less good, they are not reproduced here.

Both calculations are completely ab initio, all coupled angular momenta are included and no energy shift was  $_{590}$  introduced. The radius a of the inner region is defined by the most diffuse atomic orbital, but as mentioned earlier, we have verified the stability of our results by performing calculations with different values of a from  $25 a_0$  to  $35 a_0$ , varying the number of continuum orbitals between 25 and 50, obtaining electron affinities between 1.2575 eV and 1.2613 eV. The cross sections resulting from these parametric tests are summarized in Fig. 4 by the thick-598 ness of the lines corresponding to the current R-matrix calculations. More precisely, two curves following the largest and smallest values of the calculated cross sections are plotted, and the area between them is shaded. The differences between the cross sections obtained using the length and velocity representations of the dipole matrix are very small, less than 2% over the energy range considered, which is generally a good, but not sufficient, indication of the accuracy of a calculation.

The agreement between calculation and experiment is excellent over the whole range of energy covered by the experiment. The overall agreement with the results by Zhou et al. [7] is also very good. The main difference is in the region just above the first photodetachment threshold where our values for the total cross section, experimental and theoretical, increase monotonically, without the narow peak due to a slightly larger contribution from the  $C(1s^22s^22p^2^3P) + e^-(\ell=0)$  channel in the calculations of [7].

Since the objective of [7] was to study photode-618 tachment from threshold up to 13 eV, only one orbital 619 (3d) was optimized on the polarizability of the carbon ground state, while the 3s and 3p orbitals correspond to spectroscopic orbitals for the  $C(1s^22s^22p3s^3P^o)$ and  $C(1s^22s^22p3p^3D)$  states. In our work, the n=3 $_{623}$  and the 4f orbitals are used to improve the energy of  $C(1s^22s^22p^2 ^3P)$ , while the 4s, 4p and 4d orbitals are op- $_{625}$  timized on its polarizability. The size of our R-matrix 626 inner region  $(a=25-35a_0)$  is hence substantially larger than in the calculations by Zhou et al.  $(a=23.4 a_0)$ , but 628 our computed cross sections remain stable with varying 629 a. As a result, our calculations yield better values for the 630 polarizability of the carbon ground state and for the elec- $^{631}$  tron affinity, as well as for the  $^5S^o$  threshold. Part of the 632 difference might also be due to the treatment of the outer 633 region. However, in previous work on photodetachement

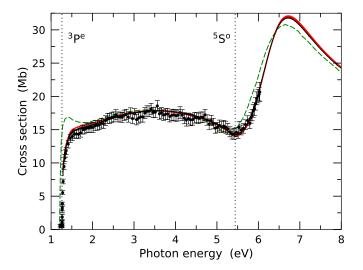


FIG. 4. Experimental and theoretical photodetachment cross sections of  $C^-(^4S^o)$  as a function of the photon energy. Full circles: present work with a pulsed laser and correction for saturation. Black full line: R-matrix method, length form; red full line: R-matrix method, velocity form; the thickness of the lines corresponds to the variation of results for different values of the calculation parameters, see text for details. Dashed line: Zhou et al. [7], length form. Vertical dotted lines: positions of the  $C(^3P)$  and  $C(^5S^o)$  thresholds.

 $^{634}$  of H<sup>-</sup> [40] and O<sup>-</sup> [11], for example, it was shown that  $^{635}$  for weak laser intensities, the perturbative approach of  $^{636}$  the UK APAP code gives results indistinguishable from  $^{637}$  those of the full R-matrix Floquet code [41, 42] that in- $^{638}$  cludes a numerically very robust treatment of the outer  $^{639}$  region.

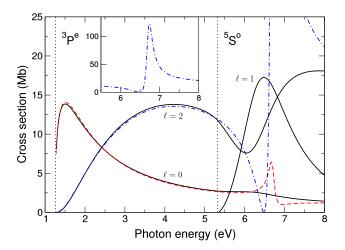


FIG. 5. Theoretical partial photodetachment cross sections as a function of the photon energy, length form. Full lines: full calculation, final channels  $C(^3P) + e^-(\ell = 0, 2)$  and  $C(^5S^o) + e^-(\ell = 1)$ ; dashed line: without  $C(^5S^o)$ , final channel  $C(^3P) + e^-(\ell = 0)$ ; dashed-dot line: without  $C(^5S^o)$ , final channel  $C(^3P) + e^-(\ell = 2)$ . Vertical dotted lines: positions of the  $C(^3P)$  and  $C(^5S^o)$  thresholds in the R-matrix calculations.

641 plays a broad plateau between 2.5 and 4.5 eV, then a 699 eigenvalue of the lifetime matrix. Using this, we find that minimum in the vicinity of the  ${}^5S^o$  threshold followed 700 the probability of the resonance to decay into the  $C({}^3P)$ close balance between the  $\ell=0,2$  partial wave contribution of decaying into the  $C(^3P)$  +  $e^-(\ell=2)$  or  $C(^5S^o)$  + 645 tions, which are shown in Fig. 5. The structure above the  $_{703}$  e<sup>-</sup>( $\ell=1$ ) channels are 0.16 and 0.84 respectively.  ${}^{5}S^{o}$  threshold is often referred to in the litterature as a  $_{647}$   $1s^22s2p^{4}$   $^4P$  shape resonance (see for example [7, 39, 43– 648 45). The dichotomic classification into shape resonances 649 (open channel resonances occuring above a threshold) 650 and Feshbach resonances (closed-channel resonances oc-651 curing below a threshold) is however not appropriate if 652 electron correlations are strong and one-electron potential interaction models break down [43]. As shown in Fig. 5, the peak above the  $C(^5S^o)$  threshold is in fact 655 present even if this state is not included at all in the cal-656 culation. Fig. 6 gives a schematic depiction of the different photodetachment pathways: direct photodetachment or excitation into a multiply excited  $C^{-}(^{4}P)$  state em-659 bedded in the continuum, followed by autodetachment. 660 The resonant state is represented by a shaded rectangular area centered on the resonance position, whose vertical 662 extent indicates its width. When the  $C(^5S^o)$  state is not  $_{663}$  included in the R-matrix basis expansion, the resonance 664 is found at a higher energy with a greatly reduced width; including it shifts down and broadens the resonance. The 666 strong interaction in the <sup>4</sup>P configuration space is thus 667 responsible for the very broad resonance profile in the to-668 tal cross section. This is reflected in the eigenvectors of 669 the hamiltonian of the R-matrix inner region: in the absence of the  $C(^5S^o)$  state, there is an eigenvalue very close 671 to the position of the resonance, characterized by weights of 46%, 14% and 17% for the  $1s^22s2p^4$ ,  $1s^22s2p^3(^5S^o)3p$ and  $1s^2 2s 2p^3 (^5S^o) 4p$  bound configurations respectively; 674 the remaining 23% is distributed into more excited con-675 figurations. When the  $C(^5S^o)$  state is included in the 676 calculation, the eigenvector of the R-matrix inner re-677 gion hamiltonian associated with the resonance has a weight of only 18% in the  $1s^22s2p^4$  configuration, 16% in  $5^{679}$   $1s^2 2s 2p^3 (^5S^o) 4p$  and 7% in  $1s^2 2s 2p^3 (^5S^o) 3p$ . The other components are mainly those formed by  $C(^5S^o)$  coupled 681 to an R-matrix continuum p orbital.

An efficient way of analyzing resonances is to use 709 683 the time-delay or lifetime matrix of the corresponding 710 nel corresponds to a photoelectron in the spherically 685 nances relatively close to threshold with a strong energy- 712 the smallest possible value, -1, at about 2 eV before in-686 dependent background and overlapping resonances can 713 creasing again to  $\beta \approx 0$ . This general trend is similar 687 be fitted to Lorentzian functions whose position and 714 to that for the photodetachment of O<sup>-</sup> and reflects the 688 height correspond respectively to the energy and lifetime 715 interference between the  $\ell=0$  and  $\ell=2$  outgoing waves. of the resonances [46, 47]. When the  ${}^5S^o$  threshold is 716 The agreement with the few existing experimental data 690 omitted from the calculation, the resonance occurs at 717 by Hall et al. [32], Calabrese et al. [48] and Brandon et al.  $_{691}$   $E_{res} = 5.457 \,\mathrm{eV}$  above the  $\mathrm{C}(^3P)$  threshold, with a width  $_{718}$  [33] is very good. The agreement with the R-matrix cal- $_{692}$   $\Gamma=0.177\,\mathrm{eV}$ . In our full calculations, the resonance posi-  $_{79}$  culations is also excellent over the whole range of photon  $E_{res} = 4.99 \, eV$  above the  $C(^3P)$  threshold, corre-  $^{720}$  energies considered. The small difference in the region <sub>694</sub> sponding to a photon energy of  $6.25\,\mathrm{eV}$ , with a width of <sub>721</sub> of the minimum at  $2\,\mathrm{eV}$  with the calculation by Zhou et  $_{695}$   $\Gamma = 1.56$  eV. Furthermore, the probability of decay into  $_{722}$  al. [7] reflects the differences at low energies in the  $\ell = 0$ <sub>696</sub> a particular open channel (autodetachment, see Fig. 6) <sub>723</sub> and  $\ell = 2$  partial cross sections shown in Fig. 5. Above 697 is given by the square of the modulus of the correspond- 724 the  $C(1s^22s2p^3 \, {}^5S^o)$  threshold, the  $\ell=1$  channel gives

The total photodetachment cross section in Fig. 4 dis- 698 ing element in the eigenvector associated with the largest by a broad maximum. The plateau is the result of a  $701 + e^-(\ell = 0)$  channel is negligible, while the probability

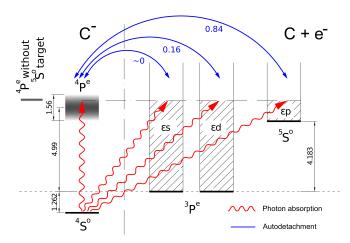


FIG. 6. Schematic representation of the photodetachment process involving an excited state of C<sup>-</sup> embedded in three continua leading to the structure around 5.5 eV in the total cross section. The strong interaction between the  $C^{-}(^4P)$ and  $C(^5S^o)$  excited states greatly broadens and pushes down the  $C^{-}(^{4}P)$  level, smoothing the resonance profile in the total cross section. The energy differences indicated are in eV. The shaded areas represent the positions and widths of the  ${}^{4}P$  resonance in the calculations with and without the  $C({}^{5}S^{o})$ state. The numbers below the arrows indicating the different autodetachment channels are the corresponding branching ra-

#### Asymmetry parameter

In Fig. 7, we present the values of the asymmetry pa-706 rameter  $\beta$  from our experiment and our R-matrix calcu-707 lations, and compare them with those from earlier work 708 [7, 32, 33, 48].

Close to threshold, the dominant detachment chanelectron-carbon scattering problem: even broad reso- 711 isotropic  $\ell = 0$  wave, so that  $\beta \approx 0$ . It decreases to nearly <sub>725</sub> a constant contribution of  $\beta = 2$ , and is therefore not <sub>752</sub> from threshold up to 4 eV. The results are in excellent 726 shown in Fig. 7. As in the calculations by Zhou et al. 753 agreement with the few data available from previous mea-[7], the asymmetry parameter displays a dip above the 754 surements [32, 33, 48].  ${}^5{
m S}^o$  threshold; in our work, this dip is slightly deeper and  ${}^{755}$ 729 occurs at a slightly higher energy than in [7].

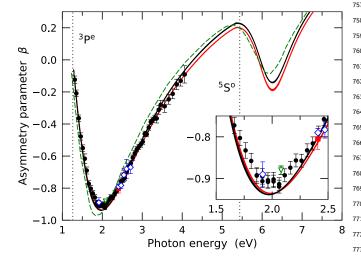


FIG. 7. Asymmetry parameter  $\beta$  for the photodetachment of  $C(^4S^o)$ . Experiment: circles, present measurements; full square, Hall et al. [32]; open lozenge, Calabrese et al. [48]; open triangle down, Brandon et al. [33]. Theory: black full line: current R-matrix results, length form; red full line: current R-matrix results, velocity form; the thickness of the lines corresponds to the variation of results for different values of of the  $C(^3P)$  and  $C(^5S^o)$  thresholds.

#### CONCLUSION

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measured absolute cross sections for the photodetach- 790 reminder of the importance of correlation effects in open 733 ment of the ground state of carbon anion in the ground 791 shell systems which break the convenient system of clas-734 state, C<sup>-</sup>(<sup>4</sup>S<sup>o</sup>), for photon energies ranging from thresh- 792 sification of resonances based on electron in a potential old up to  $6\,\mathrm{eV}$ . As the peak intensity of the laser is high  $^{793}$  approximations. enough to provoke saturation in neutral production, a  $^{794}$ that the relative cross sections by Seman and Branscomb 801 Si<sup>-</sup>, but this requires the use of different light sources. [4], renormalized using the absolute cross sections for O by Génévriez et al. [3], tend to be in much better agreement with our measurements and the best available theoretical predictions.

By analyzing the images formed by the photoelectrons 803 749 extracted from the interaction chamber through a Ve- 804 Scientifique-FNRS through IISN Contract No. 4.4504.10. 750 locity Map Imaging spectrometer, we have also deter- 805 Calculations were performed on the computational clus-751 mined the asymmetry parameters for photon energies 806 ter of the Institut de Physique de Rennes.

The experimental study has been completed by a set 756 of R-matrix calculations including orbitals and pseudo-757 orbitals optimized using the CIVPOL computer code to reproduce accurate values of electron affinity and polarizability of the carbon ground state in an ab initio way. The photodetachment cross sections in length and velocity representations are very similar, satisfying a necessary criterion of convergence of the calculations. Our results are in excellent agreement with the measured absolute cross sections up to 6 eV, and are also very close to the values determined by Zhou et al. [7] who used the Rmatrix method with the Variable Phase Method to treat the outer region. Our experiment and calculations however do not reproduce the peak just above threshold obtained by Zhou et al. The photon energy range covered 770 by our calculations extends up to 8 eV, which might be 771 somewhat high considering the absence of excited states 772 in our basis beyond  $C(1s^22s2p^3 {\,}^5S^o)$ . Our results are 773 however in excellent agreement with the values by Zhou 774 et al. who included seven more threshold states [7] up 775 to nearly 11 eV, which indicates that our calculations are 776 converged over the whole range considered. The theoretical asymmetry parameters are also in excellent agreement 778 with the experimental data.

Between the  $C(^5S^o)$  threshold and 8 eV, the photode-780 tachment cross section presents a broad peak which has the calculation parameters, see text for details; dashed line: 781 often been qualified as a <sup>4</sup>P shape resonance with a con-Zhou et al. [7], length form. Vertical dotted lines: positions  $_{782}$  figuration  $1s^22s2p^4$  or  $1s^22s2p^3\bar{n}p$ . We have shown that this resonance appears even in the absence of the  $C(^5S^o)$ 784 threshold, albeit with a much narrower width, provided 785 excitations of at least two electrons from the ground con-786 figuration are taken into account. When the  $C(^5S^o)$ 787 threshold is included, continuum orbital configurations 788 of the form  $1s^2 2s 2p^3(^5S^o) \epsilon p$  contribute to nearly 60% of Using the Animated Crossed Beam technique, we have 789 the resonance wave function. These characteristics are a

A more detailed study of the photodetachment of the correction factor has been estimated at the cost of intro-  $^{795}$  excited  $C^-(^2D)$  anion should also be performed in order ducing further assumptions about the laser beam profile. 796 to verify that its contribution to the measured signal in We have verified that the corrected cross sections are in 797 the current experiment is indeed neglible. It would be inexcellent agreement with the uncorrected absolute cross 798 teresting to extend the range of photon energies in order sections obtained using the ACB technique with continu- 799 to investigate experimentally resonances at higher enerous lasers, for which saturation does not occur. We note 800 gies, not just for C<sup>-</sup> but also in heavier systems such as

#### ACKNOWLEDGMENTS

This work was supported by the Fonds de la Recherche

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