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MR-ultrasound imaging registration using 2D spatial phase images

Adrian Basarab¹, Rémi Abbal¹, Marius-Cristian Ureche², Denis Kouamé¹

¹Université de Toulouse, IRIT, UMR CNRS 5505, France

²Technical University of Cluj-Napoca, Romania

Abstract — This paper deals with multimodal magnetic resonance (MR) – ultrasound (US) image registration. One of the major difficulties in such a registration is the lack of correspondence between the gray levels of the pixels in the two modalities. To tackle it, several authors proposed the use of the mutual information as similarity measure in the registration process. Moreover, a few papers proposed recently the use of spatial phase images instead of native intensity images. Phase images have the advantage to contain structural information on the images, free of the energetic information. Although very interesting, to our knowledge only subjective results have been reported concerning the gain of accuracy using phase images. The goal of this paper is to propose a quantitative approach for evaluating the contribution of spatial phase images obtained with monogenic and 2D isotropic analytic signal in MR-US registration.

Index Terms — Affine model, Free-Form Deformation, 2D Isotropic Analytic Signal, Monogenic signal, MR Imaging, Phase-based multimodal registration, Ultrasound Imaging

I. INTRODUCTION

Image registration in medical imaging is a widely explored research field and has various applications in all standard imagery techniques such as magnetic resonance (MR), ultrasound (US) or computed tomography (CT) [1]-[3]. All these techniques make available to physicians different types of information, which could be complementary and thus could help to improve diagnosis, surgery or therapy. For this reason, the comparison and especially the fusion of information from multiple image modalities is of increasing interest in medical applications. However, in almost all the cases, this comparison and fusion can be possible only after registering the images, i.e. after processing multimodal medical image registration. In this paper, the MR-US image registration problem is addressed.

Generally, medical image registration methods can be divided into two categories: geometric feature-based methods and pixel intensity based methods [4]. The first category presents the inconvenient of being application dependent, in the sense that anatomical landmarks have to be detected in both images before processing the registration. The second category is based on the assumption that a correspondence exists between the pixel intensities of the two images to be registered. For multimodal registration, this correspondence is often measured using the mutual information, which was shown to be more robust than classical similarity measures

such as correlation-based techniques [5]. More recently, a few studies showed interesting experimental results when processing multimodal registration using phase images instead of native intensity of the pixels [1], [3], [6]. However, as in experimental cases the ground truth is not available, these papers only presented qualitative results.

In this context, the main purpose of this paper is to propose a quantitative comparison between MR-US registration using both the native intensity of the pixels and the spatial phase images.

The spatial phase images evaluated herein are obtained using two recent 2D generalizations of the classical analytic signal. These spatial phase images have the advantage of providing structural information, free from the energetic information. Unlike the 1D analytic signal which has a complex representation, its generalizations to the two dimensional case are hypercomplex signals, having two (for the monogenic signal [7]) or five (for the 2D isotropic analytic signal [8]) imaginary components. A brief reminder concerning the monogenic and 2D isotropic analytic signal is given in section II.

To perform a quantitative comparison, we propose in section III a realistic simulation method allowing the control of the deformation field. For this, an ultrasound image simulation is proposed, starting from a real MR image.

In order to evaluate the contribution of spatial phase images to MR-US imaging, a state-of-the-art registration algorithm has been used. Based on the mutual information and on a multi-scale approach, it searches for a local affine transformation. The scope of the paper is not to evaluate the performance of this registration method, but to evaluate the results obtained by applying it to the native images or to the corresponding spatial phase images.

II. HYPERCOMPLEX SIGNALS

In 1D signal processing, the complex representation of a real 1D signal, called analytic signal, has been introduced by Gabor in 1964 [9]. Starting from a real value signal $s(t)$, the analytic signal has complex values $s_A(t) = s(t) + is_H(t)$, where the imaginary part $s_H(t)$ corresponds to the Hilbert transform of $s(t)$. The major contribution of the analytic signal is the possibility to define the concepts of instantaneous (or local) amplitude and phase.

The extension of the analytic signal to image processing is not straightforward as it requires the generalization of the Hilbert transform to the 2D case.

Chronologically, the first attempts to generalize the 1D analytic signal to images were based on complex numbers and on the so called total or partial 2D Hilbert transforms, which are direct extensions of the 1D case [10]. Combining in different ways the real image with these 2D Hilbert transforms, several 2D analytic representations of an image have been proposed, such as the total, partial or single orthant analytic signal [11]-[12]. Despite interesting properties and several applications, these 2D analytic signals are not a strict generalization of the 1D analytic signal, especially because of the lack of isotropy. The isotropy is a crucial property in order to obtain a proper representation of the local phase that fulfills the invariance-equivariance. In other words, we can notice that complex numbers are able to represent two degrees of freedom. In the case of 1D signals, they are represented by the local amplitude and phase. However, for images, a third degree of freedom appears, namely the local orientation. For this reason, it has been recently shown that the use of hyper-complex numbers is necessary in order to obtain a strict generalization of the 1D analytic signal [7], [8]. These hyper-complex representations of real images are called monogenic signal [7] and 2D isotropic analytic signal [8]. The main practical aspects of both of them are given below.

1) The Monogenic Signal

The monogenic signal (MS) was introduced by Felsberg and Sommer in 2001 [7]. The main idea behind the MS is to combine the local phase with the local orientation information, or in other words to combine the 1D analytic signal with the local orientation. For this reason, the MS is adapted to locally intrinsically one dimensional images (i1D), i.e. $p(x_1, x_2) = r(x_1 n_1 + x_2 n_2)$, for any 1D function $r(x)$, where the orientation of the vector $\mathbf{n}=[n_1, n_2]$ represents the local orientation of the image structures, denoted by θ in the following. A typical example of an i1D image is shown on Figure 1(b), representing an orientated 2D sinusoid.

The monogenic signal of an image denoted by $p(x_1, x_2)$ is obtained from the responses to three 2D spherical quadrature filters (SQF): one even part consisting in a rotation invariant band-pass filter ($B(\mathbf{u})$) and two odd parts constructed using the Riesz transform [7]. In the literature, authors mainly use Poisson (or Difference of Poisson, DoP) [13], or logGabor [14] as band-pass filter.

$$I_M(\mathbf{x}) = p_b(\mathbf{x}) + iq_x(\mathbf{x}) + jq_y(\mathbf{x}) \quad (1)$$

Where \mathbf{x} is the vector corresponding to the position $[x_1, x_2]$ of the pixel and $p_b(\mathbf{u}) = P(\mathbf{u}) \cdot B(\mathbf{u})$ is the spectrum of the band-pass filtered image. Capital letters represent the 2D Fourier Transform of corresponding images and $\mathbf{u} = [u, v]^T$ is the 2D frequency variable. As explained above, the two imaginary parts are obtained by two quadrature filters $h_x(\mathbf{x})$ and $h_y(\mathbf{x})$, which turn in the Fourier domain in:

$$\begin{aligned} Q_x(\mathbf{u}) &= H_x(\mathbf{u})B(\mathbf{u})P(\mathbf{u}) \\ Q_y(\mathbf{u}) &= H_y(\mathbf{u})B(\mathbf{u})P(\mathbf{u}) \end{aligned} \quad (2)$$

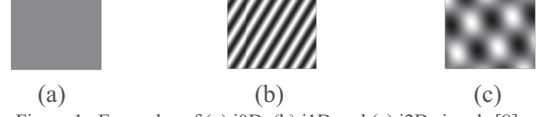


Figure 1. Examples of (a) i0D, (b) i1D and (c) i2D signals [8].

With

$$H_x(\mathbf{u}) = -i \frac{u}{\|\mathbf{u}\|}, \quad H_y(\mathbf{u}) = -i \frac{v}{\|\mathbf{u}\|} \quad (3)$$

From the monogenic signal, local features such as local amplitude, phase and orientation are extracted using the pixel-wise formulas given in [7]. Herein, we remind the one corresponding to the phase.

$$\varphi_{MS}(\mathbf{x}) = \tan^{-1} \left(\frac{p_b(\mathbf{x})}{\sqrt{p_b^2(\mathbf{x}) + q_1^2(\mathbf{x}) + q_2^2(\mathbf{x})}} \right) \quad (4)$$

2) The 2D Isotropic Analytic Signal

In order to overcome the limitation of the MS related to i2D images, the 2D isotropic analytic signal (2D IAS) has been recently introduced by Wietzke et al. [8]. The 2D IAS extends the MS by using the first and second order Riesz transforms. The second order Riesz transforms are expressed in the frequency domain by:

$$H_{xx}(\mathbf{u}) = -\frac{u^2}{\|\mathbf{u}\|^2}, \quad H_{xy}(\mathbf{u}) = -\frac{uv}{\|\mathbf{u}\|^2}, \quad H_{yy}(\mathbf{u}) = -\frac{v^2}{\|\mathbf{u}\|^2} \quad (5)$$

Consequently, in addition to the three components of the MS, we obtain three new second order components denoted by $q_{xx}(\mathbf{x})$, $q_{xy}(\mathbf{x})$ and $q_{yy}(\mathbf{x})$.

Before extracting features such as phase or orientation, it is necessary to compute three intermediate components:

$$q_s(\mathbf{x}) = \frac{1}{2}(q_{xx}(\mathbf{x}) + q_{yy}(\mathbf{x})) = \frac{1}{2}p_b(\mathbf{x}) \quad (6)$$

$$q_+(\mathbf{x}) = q_{xy}(\mathbf{x}) \quad (7)$$

$$q_{+-}(\mathbf{x}) = \frac{1}{2}(q_{xx}(\mathbf{x}) - q_{yy}(\mathbf{x})) \quad (8)$$

Moreover, a so called apex angle $\alpha(\mathbf{x})$, also known as opening angle, can be calculated from the 2D IAS as shown in (9) and quantifies the intrinsic dimension of the image. $\alpha(\mathbf{x}) = 0$ means that the image is locally i1D around the position \mathbf{x} .

$$\alpha(\mathbf{x}) = \tan^{-1} \left(\frac{\sqrt{q_s^2(\mathbf{x}) - (q_+^2(\mathbf{x}) + q_{+-}^2(\mathbf{x}))}}{q_+^2(\mathbf{x}) + q_{+-}^2(\mathbf{x})} \right) \quad (9)$$

The homogeneous signal component $q_h(\mathbf{x})$ is further computed from the apex angle.

$$q_h(\mathbf{x}) = \sqrt{\frac{1 + \cos(\alpha(\mathbf{x}))}{2}} \quad (10)$$

Normalizing the first order signal components, it is possible to extract local main orientation, phase and amplitude, whose interpretation is equivalent to the information obtained with the monogenic signal. Concerning the spatial phase, (4) is replaced, for the 2D IAS, by:

$$\varphi_{2DIAS}(\mathbf{x}) = \tan^{-1} \left(\frac{p_b(\mathbf{x})}{\sqrt{p_b^2(\mathbf{x}) + (q_h^{-1}(\mathbf{x})q_x(\mathbf{x}))^2 + (q_h^{-1}(\mathbf{x})q_y(\mathbf{x}))^2}} \right) \quad (11)$$

It is obvious that for $\alpha(\mathbf{x}) = 0$, $q_h(\mathbf{x}) = 1$ and therefore (11) is simplified to (4). In this case, the image is intrinsically 1D.

III. MRI-US SIMULATION

Quantifying the performance of MRI-US registration techniques is a complicated task when doing it on *in vivo* images. Indeed, in such experimental cases, the ground truth is not available and only subjective measures can be exploited, using for example fiducial markers manually identified and matched on MR and US images.

In this work, we propose to use a realistic simulation in order to quantify the accuracy of MR-US image registration, giving access to the true deformation field. The input of our simulation is an experimental 2D MR image. For illustration purpose, we used herein a gynecological image (a sagittal slice extracted from a MR volume).

1) Scatterer map generation

The property of the tissues exploited in US imaging is their echogenicity, i.e. their ability to reflect ultrasound waves and thus produce echoes. To simulate this process, US simulators generally use scatterer maps. A scatterer is defined by its spatial position and its amplitude. Moreover, the scatterers are positioned following a uniform random distribution. Their number must be sufficiently large in order to insure a density of at least one scatterer per resolution cell. In our simulations, 50,000 scatterers were generated.

An important issue is the way of generating the amplitude of the scatterers. For this task, we propose to link their amplitude to the grey levels of the MR image (denoted by I). By proceeding in this way, we make the assumption that the US echogenicity of a tissue is directly proportional to the MRI T2 relaxation time. For a scatterer i at the position (x_{1i}, x_{2i}) , its amplitude denoted by a_i has been randomly generated using a zero mean Gaussian distribution:

$$a_i < N(0, I^2(\tilde{x}_{1i}, \tilde{x}_{2i})) \quad (12)$$

The variance of the Gaussian law is related to the grey level of the MR image as shown in (12). The coordinates $(\tilde{x}_{1i}, \tilde{x}_{2i})$ stand for the closest pixel position in image I to the position (x_{1i}, x_{2i}) of the current scatterer.

It should be noticed that the assumption of direct proportionality between the echogenicity of a tissue and the T2 relaxation time in MR may not be always valid. In this case, our simulation framework still remains valid, but the way of generating the scatterer amplitudes in (12) should be adapted. In Figure 2, we show an example of a generated scatterer map.

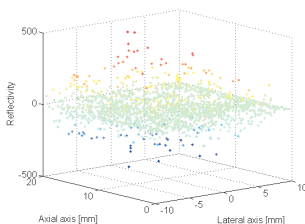


Figure 2. Uniformly random distributed scatterer map.

2) US image simulation

The scatterer map generated as explained above was used to simulate an US images using Field II simulator program [15]. Without loss of generality, US images in linear geometry (corresponding to a 1D linear probe) were simulated.

In our experiments, a 256 elements linear ultrasound probe with 64 active elements was simulated. The width of one element was set at 0.22 mm, the kerf at 0.011 mm (which resulted in a pitch of 0.231 mm) and the height at 5 mm. The central frequency of the probe was fixed at 7MHz, with an axial sampling frequency of 100MHz. The impulse response of the emit aperture was a two-period sinus of the nominal frequency (the excitation) multiplied by a Hanning window. The reception aperture was also a 64-length Hanning window. A multiple point focalization was simulated for the reception.

An example of a simulated US image, as well as the native *in vivo* MR image, is given on Figure 3 (b and c).

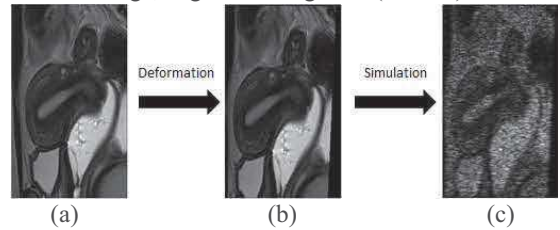


Figure 3 (a) Original MRI slice, (b) deformed MR image with a known deformation field (affine in this example) and (c) simulated ultrasound image after generating a scatterer map starting from the image in (b).

3) Deformation field

A known deformation field was imposed to the MR image before scatterer map generation and US simulation, as shown in Figure 3. In this paper, two different types of deformation fields are considered: an affine transformation and a cubic B-spline free form deformation. The choice was made so that the deformation model fits to the ones considered with the two state-of-the-art registration techniques used herein and introduced in [16], [17]. In this way, the evaluation of the registration results was limited to the images on which the registration was performed, and was not influenced by a deviation between the model and the imposed deformation map.

IV. RESULTS

1) Affine estimation

Imposed deformation field

The displacement imposed corresponds to a rotation $\rho = \pi/80$, to scale factors $sc_x = 5\%$ and $sc_y = -2\%$, to shear factors $sh_x = 1\%$ and $sh_y = 2\%$ and to translations $t_x = 0.5$ pixels (or 0.094 mm) and $t_y = 0.8$ pixels (or 0.079 mm).

Figures of merit

The evaluation is done through the following criteria: absolute error between the imposed and estimated affine parameters, minimum (14) and maximum (15), mean (16) and standard deviation (17) of the absolute error between the imposed and estimated deformation fields. Denoting by $U(x, y)$ and $\hat{U}(x, y)$, respectively $V(x, y)$ and $\hat{V}(x, y)$, the lateral

(true and estimated) and axial (true and estimated) deformation fields, the absolute errors and the associated figures of merit are defined as follows:

$$E_{\Gamma}(x, y) = \left| \Gamma(x, y) - \hat{\Gamma}(x, y) \right| \quad (13)$$

$$m_{\Gamma} = \min_{x,y} (E_{\Gamma}(x, y)) \quad (14)$$

$$M_{\Gamma} = \max_{x,y} (E_{\Gamma}(x, y)) \quad (15)$$

$$\mu_{\Gamma} = \frac{1}{LC} \sum_{x=1}^C \sum_{y=1}^L E_{\Gamma}(x, y) \quad (16)$$

$$\sigma_{\Gamma} = \frac{1}{LC-1} \sqrt{\sum_{x=1}^C \sum_{y=1}^L (E_{\Gamma}(x, y) - \mu_{\Gamma})^2} \quad (17)$$

Where Γ stands for U or V and L and C are the image dimensions.

Table I
Absolute errors of affine parameters simulation

	a_{11}	a_{12}	a_{21}	a_{22}	a_{31}	a_{32}
Intensity	0.76	8.1	1.55	0.16	168.33	83.59
φ_{MS}	0.02	13.79	2.99	0.42	1.5	9.1
φ_{2DIAS}	0.03	13.55	2.99	0.38	4.75	0.09

Relative error of the affine parameter estimation in % obtained using intensity and spatial phase (MS and 2D IAS) images.

Table II
Minimum and maximum absolute errors

	m_U	M_U	m_V	M_V
Intensity	5.9×10^{-6}	1.61	0.67	1.9
φ_{MS}	7.78×10^{-6}	0.81	1.98×10^{-5}	2.66
φ_{2DIAS}	8.1×10^{-5}	0.75	6.9×10^{-3}	2.58

Minimum and maximum absolute errors in pixels of the affine estimation for the entire motion field estimated.

Table III
Mean absolute errors and its standard deviation

	μ_U	σ_U	μ_V	σ_V
Intensity	0.59	0.4	1.29	0.25
φ_{MS}	0.4	0.22	1.2	0.58
φ_{2DIAS}	0.33	0.22	1.29	0.54

Mean and standard deviation of the absolute errors in pixels along the entire estimated affine motion field.

Results

Table I presents the absolute errors of the parameters' estimation for the affine registration with the native images, with the monogenic spatial phase φ_{MS} and with 2D IAS spatial phase φ_{2DIAS} . We observe that for a_{12} , a_{21} and a_{22} the intensity-based approach provides slightly less error than the phase-based estimations. However, a_{11} , a_{31} and a_{32} are much more accurate when using phase images.

The consequence of this difference is illustrated in Table II and Table III. Whereas the lateral maximum absolute error is reduced by roughly 50%, the axial error is increased about 50%. This is due to the higher resolution in the axial direction for intensity images and to the band-pass filter degrading the

axial resolution of the phase images. However, the mean absolute errors stay lower or equal than the intensity-based approach, which highlights the interest of the use of phase images. We can also observe that in this experiment, 2D IAS seems to be slightly more accurate than MS.

V. CONCLUSION

In this paper, we considered the use of local spatial phase for MR-US image registration. We tested spatial phases extracted from two different hyper-complex signals: the monogenic signal and its extension, the 2D isotropic analytic signal. A realistic US simulation based on a real MR image allowed us to control the imposed affine deformation field and thus to have access to the ground truth. The obtained quantitative results showed the contribution of the spatial phase images compared to the use of the native gray level of the pixels.

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