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## Cross-relaxation and ion clustering in Tm<sup>3+</sup>:CaF<sub>2</sub> crystals

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### ABSTRACT

We systematically study cross-relaxation (CR) and ion clustering in  $Tm^{3+}$ :CaF<sub>2</sub> crystals using a spectroscopic approach. For this, the luminescence from the <sup>3</sup>H<sub>4</sub> and <sup>3</sup>F<sub>4</sub> states was monitored for a broad range of  $Tm^{3+}$  doping concentrations, from 0.01 at.% to 7 at.%. The decay curves were fitted using a model of two ions classes, namely isolated ions showing no energy-transfer processes and ions with neighbors exhibiting both CR and energy-transfer upconversion (ETU), and accounting for energy-migration. The fraction of ions with neighbors and the microscopic concentration-independent CR and ETU parameters are deduced. The critical  $Tm^{3+}$  doping level for which at least half of the active ions are clustered is only 0.7 at.%. The obtained results are relevant for achieving efficient laser operation of  $Tm^{3+}$ :CaF<sub>2</sub> crystals at the <sup>3</sup>F<sub>4</sub>  $\rightarrow$  <sup>3</sup>H<sub>6</sub> (at ~1.9 µm) and the <sup>3</sup>H<sub>4</sub>  $\rightarrow$  <sup>3</sup>H<sub>5</sub> (at ~2.3 µm) transitions.

Keywords: calcium fluoride, thulium ions, cross-relaxation, ion clustering, luminescence.

## 1. INTRODUCTION

Cubic (fluorite-type) calcium fluoride (CaF<sub>2</sub>) crystals are well-known for fabrication of optical elements because of their good thermo-mechanical properties (thermal conductivity:  $\kappa \sim 9.7$  W/(mK) for an undoped crystal), broad transparency range (0.13–10 µm) and low refractive index (n = 1.424 at  $\sim 2$  µm). CaF<sub>2</sub> crystals are also suitable for doping with trivalent rare-earth ions (RE<sup>3+</sup>) for laser applications [1-3]. They feature a strong RE<sup>3+</sup> ion clustering even at low doping concentrations about 0.1–1 at.% [4,5] resulting in broad and smooth spectral bands both in absorption and emission (the so-called glassy-like spectroscopic behavior). It is of interest for broadly tunable [6] and mode-locked [7,8] lasers. The good thermal properties of the host matrix allow for power scaling.

Thulium (Tm<sup>3+</sup>) doped CaF<sub>2</sub> crystals exhibit a broadband emission at ~1.9 µm due to the  ${}^{3}F_{4} \rightarrow {}^{3}H_{6}$  electronic transition. Efficient Tm<sup>3+</sup>:CaF<sub>2</sub> lasers were reported [2,9]. Camy *et al.* reported on a laser-pumped Tm:CaF<sub>2</sub> laser delivering ~135 mW at 1887 nm with a slope efficiency of 41% and a laser threshold of only 68 mW [2]. Liu *et al.* reported on power scaling of a Tm:CaF<sub>2</sub> laser under diode-pumping yielding 2.71 W with a higher slope efficiency of 70.1% [9]. The same group of authors demonstrated continuous wavelength tunability for this laser between 1.85 and 2.04 µm (189 nm broad) and mode-locked operation employing a SESAM. In the latter case, 15 ps-long pulses were obtained at a central wavelength of 1886.8 nm with a repetition rate of 96.35 MHz [9]. Thin films of Tm:CaF2 were grown [10].

It was proven that the ion clustering determines the emission properties of  $Tm^{3+}$  ions in CaF<sub>2</sub> [5]. For low doping levels (0.01-0.1 at.%), the  $Tm^{3+}$  ions are mostly isolated and they accommodate in sites with different symmetry depending on the charge compensation mechanism involving interstitial F<sup>-</sup> anions. For higher doping levels, ion clusters are formed. To prevent the clustering of active ions, the CaF<sub>2</sub> crystals were codoped by  $Tm^{3+}$  ions and optically passive "buffer" ions  $Ln^{3+}$  such as Gd<sup>3+</sup>, Lu<sup>3+</sup>, La<sup>3+</sup> or Y<sup>3+</sup> [11,12]. Laser operation with such codoped crystals was also demonstrated. Zhang *et al.* reported on a Tm,La:CaF<sub>2</sub> laser delivering 4.27 W at 1921 nm with a slope efficiency of 67.8% [12].

A key spectroscopic process which determines the laser efficiency of ~1.9 µm Tm lasers is the cross-relaxation (CR) for adjacent Tm<sup>3+</sup> ions,  ${}^{3}H_{4}(Tm_{1}) + {}^{3}H_{6}(Tm_{2}) \rightarrow {}^{3}F_{4}(Tm_{1}) + {}^{3}F_{4}(Tm_{2})$ , potentially leading to a pump quantum efficiency of 2 [13]. This means that after an excitation at ~0.8 µm (to the  ${}^{3}H_{4}$  pump level), there can be up to 2 excited ions in the upper laser level ( ${}^{3}F_{4}$ ). CR in Tm<sup>3+</sup>-doped laser materials increases the laser slope efficiency and reduces the heat dissipation. Up to now, no detailed study of CR for Tm:CaF<sub>2</sub> crystals was performed.

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The aim of the present work is to study the cross-relaxation (and other energy-transfer processes, such as energy-transfer upconversion (ETU)) in  $\text{Tm:CaF}_2$  crystals accounting for the ion clustering. For this, we involve the spectroscopic model of distinct ion classes which was recently developed [14].

### 2. EXPERIMENTAL RESULTS

For the spectroscopic studies, we grew a series of  $Tm^{3+}$ :CaF<sub>2</sub> crystals with the doping level ranging from 0.01 at.% to 7 at.%. The Tm:CaF<sub>2</sub> crystals were grown using a conventional Bridgman technique with a homemade furnace. A mixture of high purity (4N) CaF<sub>2</sub> and TmF<sub>3</sub> powders was introduced in a graphite crucible. A good vacuum (<10<sup>-5</sup> mbar) was realized before introducing Ar and CF<sub>4</sub> gases to avoid oxygen pollution. The furnace temperature was set to about 50 K higher than the melting point of CaF<sub>2</sub>. After soaking, the charge was thoroughly melted and the crystal growth was carried out with a rate of 2-4 mm/h. When the growth was finished, the crystal was cooled down to room temperature (RT, 293 K) within 48 hours.

#### 2.1 Absorption and luminescence

The RT absorption spectra of  $Tm^{3+}$ :CaF<sub>2</sub> crystals containing predominantly isolated ions (0.05 at.% Tm) and ion clusters (1.5 at.% and 4.5 at.% Tm) are shown in Fig. 1. It is known that in  $Tm^{3+}$ -doped CaF<sub>2</sub> crystals with very low doping levels, the active ions are distributed over three types of sites with the symmetry C<sub>3v</sub> (trigonal), C<sub>4v</sub> (tetragonal) or O<sub>h</sub> (cubic). The particular symmetry depends on the charge compensation mechanism (as trivalent  $Tm^{3+}$  ions are replacing the divalent Ca<sup>2+</sup> ones). The latter is provided by an interstitial fluorine anion (F<sub>i</sub><sup>-</sup>). Here, we do not consider the possible charge compensation by oxygen (O<sup>2-</sup>) or univalent alkali metal cations (Na<sup>+</sup>, K<sup>+</sup>) leading to other types of sites. As a result, the absorption spectra of the 0.05 at.%  $Tm^{3+}$ :CaF<sub>2</sub> crystal represent a superposition of sharp absorption lines of  $Tm^{3+}$  ions in all three sites. For high doping levels, the  $Tm^{3+}$  ions are mostly arranged in clusters leading to smooth and broad spectral bands. There is no significant change in the absorption spectra of 1.5 at.% Tm and 4.5 at.% Tm-doped crystals, except of the <sup>3</sup>H<sub>6</sub>  $\rightarrow$  <sup>3</sup>H<sub>5</sub> transition. The small changes may reflect the transition from simple clusters (dimers, trimers) to large agglomerates of active ions.



Figure 1. RT absorption cross-section,  $\sigma_{abs}$ , spectra of Tm<sup>3+</sup>:CaF<sub>2</sub> crystals with different Tm doping concentrations (0.05 at.%, 1.5 at.% and 4.5 at.%): transitions from the ground-state (<sup>3</sup>H<sub>6</sub>) to the excited-states: (a) <sup>3</sup>F<sub>4</sub>, (b) <sup>3</sup>H<sub>5</sub>, (c) <sup>3</sup>H<sub>4</sub> and <sup>3</sup>F<sub>2,3</sub>, and (d) <sup>1</sup>G<sub>4</sub> and <sup>1</sup>D<sub>2</sub>.

For the  ${}^{3}\text{H}_{6} \rightarrow {}^{3}\text{H}_{4}$  pump transition, the maximum absorption cross-section  $\sigma_{abs}$  is  $0.46 \times 10^{-20}$  cm<sup>2</sup> at 766.2 nm and the full width at half maximum (FWHM) of the absorption band is 13.2 nm (for the 4.5 at.% Tm doping). For the 0.05 at.% Tm doping, the peak  $\sigma_{abs}$  value is much lower,  $0.17 \times 10^{-20}$  cm<sup>2</sup> at ~768 nm.

The evolution of RT luminescence spectra for the  ${}^{3}H_{4} \rightarrow {}^{3}H_{6}$  (at ~0.8 µm) and  ${}^{3}F_{4} \rightarrow {}^{3}H_{6}$  (at ~1.9 µm) transitions in emission was studied for a broad range of Tm doping concentrations (0.01–7 at.%). This comparative study revealed a critical Tm concentration (0.5–0.7 at.%) for which a significant change in the shape of the emission bands is observed: the spectra become smooth and broad and they resemble to a great extent those for Tm<sup>3+</sup>-doped fluoride glasses. This is an indication of a change in the predominant ion coordination (a transition from isolated ions to clusters). Figure 2 shows such a comparison for the emission from the pump level ( ${}^{3}H_{4}$ ) at ~0.8 µm.



Figure 2. Normalized RT luminescence spectra of Tm<sup>3+</sup>:CaF<sub>2</sub> crystals with different doping concentrations (the  ${}^{3}\text{H}_{4} \rightarrow {}^{3}\text{H}_{6}$  transition),  $\lambda_{exc} = 769$  nm (non-selective excitation).

#### 2.2 Luminescence decay

We monitored the decay of  $Tm^{3+}$  luminescence from the  ${}^{3}H_{4}$  and  ${}^{3}F_{4}$  multiplets for a broad range of Tm doping levels (0.01–7 at.%) in CaF<sub>2</sub>. Figure 3 shows the measured luminescence decay curves for the  ${}^{3}H_{4} \rightarrow {}^{3}H_{6}$  transition in emission (at ~0.8 µm). For very low doping level (0.01 at.% Tm), the luminescence decay curve is close to a single-exponential one with a characteristic lifetime  $\tau_{lum}$  of 3.55 ms. Despite the existence of several species contributing to this emission (namely, isolated  $Tm^{3+}$  ions in various sites), the intrinsic lifetimes of the  ${}^{3}H_{4}$  state for the  $C_{3v}$  and  $C_{4v}$  coordinated  $Tm^{3+}$  ions in CaF<sub>2</sub> are rather close: 3.03 ms and 3.59 ms, respectively (as determined in site-selective excitation experiments). With increasing Tm doping, the decay from the  ${}^{3}H_{4}$  state becomes faster and the luminescence decay curves notably deviate from the single-exponential law.



Figure 3. Luminescence decay curves from the  ${}^{3}H_{4}$  Tm<sup>3+</sup> state in Tm<sup>3+</sup>:CaF<sub>2</sub>: *black* – experimental data, *red* – their fitting with the rate-equation model of distinct ion classes,  $\lambda_{exc} = 765$  nm,  $\lambda_{lum} = 820$  nm. Measured under ns pulse excitation.

To explain this behavior, we used the model of spectroscopically distinct ion classes [14]. A simplified scheme of  $Tm^{3+}$  energy-levels was considered, Fig. 4. The populations of the  $Tm^{3+}$  ground-state ( ${}^{3}H_{6}$ ) and two relevant excited-states ( ${}^{3}F_{4}$  and  ${}^{3}H_{4}$ ) were monitored; the population of the intermediate  ${}^{3}H_{5}$  excited-state was assumed to be almost zero as this state is depopulated by very efficient multi-phonon non-radiative (NR) relaxation. The states above  ${}^{3}H_{4}$  were not taken into account. The following spectroscopic processes were considered: (i) radiative (R) decay from the  ${}^{3}F_{4}$  and  ${}^{3}H_{4}$  states, (ii) cross-relaxation (CR)  ${}^{3}H_{4}(Tm_{1}) + {}^{3}H_{6}(Tm_{2}) \rightarrow {}^{3}F_{4}(Tm_{1}) + {}^{3}F_{4}(Tm_{2})$ , (iii) energy-transfer upconversion,  ${}^{3}F_{4}(Tm_{1}) +$ 

 ${}^{3}F_{4}(Tm_{2}) \rightarrow {}^{3}H_{6}(Tm_{1}) + {}^{3}H_{4}(Tm_{2}) (ETU_{1}) and {}^{3}F_{4}(Tm_{1}) + {}^{3}F_{4}(Tm_{2}) \rightarrow {}^{3}H_{6}(Tm_{1}) + {}^{3}H_{5}(Tm_{2}) (ETU_{2})$ , and (iv) energymigration (EM) to impurities leading to de-excitations from the  ${}^{3}F_{4}$  and  ${}^{3}H_{4}$  multiplets. We assumed the existence of two distinct ion classes: (a) isolated ions showing no energy-transfer processes (CR and ETU) and (b) ions with neighbors exhibiting both CR and ETU. The fraction of ions with neighbors *f*, the macroscopic rates of CR ( $W_{CR}$ ) and ETU ( $W_{ETU1}$ and  $W_{ETU2}$ ) and the  ${}^{3}H_{4}$  level lifetime  $\tau_{3}$  accounting for EM were used as free parameters of the fitting (for luminescence decay curves shown in Fig. 3). The model gives a satisfactory agreement with the experiment.



Figure 4. The scheme of energy-levels of  $Tm^{3+}$  ions (for a free-ion) showing relevant spectroscopic processes associated with the conventional pumping scheme (to the <sup>3</sup>H<sub>4</sub> state): R – radiative relaxation, NR – multiphonon non-radiative relaxation, CR – cross-relaxation, ETU – energy-transfer upconversion, EM – energy-migration.

#### 3. DISCUSSION

The results on the fraction of  $\text{Tm}^{3+}$  ions with neighbors *f* are shown in Fig. 5. With increasing the Tm doping level, the fraction of isolated ions (1 - f) gradually decreases. The critical Tm doping level for which at least half of the active ions are clustered is only  $0.7\pm0.1$  at.%. This agrees well with our conclusion drawn from the measured luminescence spectra at ~0.8 µm. The dependence of *f* on the doping concentration was fitted using a statistical approach [14,15]:



Figure 5. Ion clustering in  $Tm^{3+}$ :CaF<sub>2</sub>: fraction of ions with neighbors *f*, *symbols* – data extracted from the modeling of the experimental luminescence decay curves using the rate-equation model of distinct ion classes, *curve* – their fit using a statistical approach.

Here,  $P_{m,n}$  is the probability for occurrence of neighbor Tm<sup>3+</sup> ions in the first coordination sphere of the considered Tm<sup>3+</sup> ion, *n* is the coordination number (C.N.) by nearest-neighbor rare-earth sites, *m* is the actual number of Tm<sup>3+</sup> ions in the first coordination sphere (m = 0 corresponds to a single ion and  $m \ge 1$  - to an ion pair or cluster), and  $p = N_{Tm}/N_{max}$  represents the relative doping concentration ( $N_{max}$  is the maximum possible concentration). The expression for the fraction of ions with neighbors ( $m \ge 1$ , not specifying the exact *m* number) is:

$$f = 1 - \left[1 - \left(N_{\rm Tm} / N_{\rm max}\right)\right]^{\rm C.N.}.$$
(2)

For calculation, we assume  $N_{\text{max}} = 10$  at.% and C.N. = 10 which gives a good agreement with the data obtained from the measured luminescence curves.

The model also yields the macroscopic rates  $W_{CR}$ ,  $W_{ETU1}$  and  $W_{ETU2}$  [in s<sup>-1</sup>], as shown in Fig. 6. The CR is Tm:CaF<sub>2</sub> is much stronger than the ETU.  $W_{CR}$  and  $W_{ETU1(2)}$  show a quadratic dependence on the Tm doping concentration ( $N_{Tm}$ ):

$$W_{\rm CR} = C_{\rm CR} N_{\rm Tm}^{2},\tag{3a}$$

$$W_{\text{ETU1(2)}} = C_{\text{ETU1(2)}} N_{\text{Tm}}^{2},$$
 (3b)

where  $C_{CR}$  and  $C_{ETU1(2)}$  are the concentration-independent microscopic energy-transfer parameters. CR in Tm<sup>3+</sup>:CaF<sub>2</sub> is about one order of magnitude stronger than that in other well-known fluoride crystal, Tm<sup>3+</sup>:LiYF<sub>4</sub> [16].



Figure 6. Energy-transfer processes in  $Tm^{3+}$ :CaF<sub>2</sub>: macroscopic rates of cross-relaxation (CR)  $W_{CR}$  and energy-transfer upconverison (ETU)  $W_{ETU1(2)}$ , *symbols* – data extracted from the modeling of the experimental luminescence decay curves using the rate-equation model of distinct ion classes, *lines* – their quadratic fits.

### 4. CONCLUSIONS

To conclude, we have quantified ion clustering (in terms of fraction of ions with neighbors) and CR and ETU energytransfer processes (in terms of macroscopic rates and microscopic concentration-independent parameters) in Tm<sup>3+</sup>-doped CaF<sub>2</sub> crystals, for the first time, to the best of our knowledge. This information is of key importance for the design of Tm:CaF<sub>2</sub> lasers operating on the  ${}^{3}F_{4} \rightarrow {}^{3}H_{6}$  (~1.9 µm) and  ${}^{3}H_{4} \rightarrow {}^{3}H_{5}$  (~2.3 µm [17]) transitions. Indeed, for the ~1.9 µm lasers, quantification of CR is important to determine the possibility to reach high pump quantum efficiency of 2 for the upper laser level ( ${}^{3}F_{4}$ ) [13]. For the ~2.3 µm lasers which have not been demonstrated yet in Tm:CaF<sub>2</sub>, in contrast, CR is a detrimental effect as it quenches the lifetime of the upper laser level ( ${}^{3}H_{4}$ ). However, ETU1 in such lasers can play a key role in refilling the  ${}^{3}H_{4}$  state leading to increased laser slope efficiency [16,18]. The proposed spectroscopic model can be extended to describe the ion clustering in Tm<sup>3+</sup>,Ln<sup>3+</sup>:CaF<sub>2</sub> crystals codoped with "buffer" ions.

## 5. ACKNOWLEDGEMENTS

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