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Ultrafast Thermal Melting in Nonequilibrium Warm Dense Copper

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The ultrafast dynamics of the loss of crystalline periodicity is investigated in femtosecond laser heated warm dense copper, by the original use of x-ray absorption near-edge specific structures just above the L3 edge. The characteristic time is observed near 1 ps, for specific energy density ranging from 1 to 5 MJ/kg, using ps-resolution x-ray absorption spectroscopy. The overall experimental data are well reproduced with two-temperature hydrodynamic simulations, supporting a thermal phase transition.

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Since the advent of intense and femtosecond laser pulses [1], the study of their interaction with matter has raised a strong enthusiasm. Among other uses, it is a privileged way to bring matter in extreme states of temperature and pressure, with fundamental implications in various fields of physics including laser micromachining, planetology, and inertial confinement fusion [2–5]. Despite these major scientific motivations, the description of this so-called warm dense matter (WDM) is still highly challenging, due to partial disorder, correlated ions, electron degeneracy, and strong coupling between electron structure and ion bonding [6]. As femtosecond laser pulses lead to conditions far from equilibrium (hot electrons and still cold lattice), they offer a unique opportunity to get deeper understanding of the electron-ion dynamic interplay [7,8].

There has been considerable theoretical interest in the dynamics of phase transitions in these nonequilibrium situations [9–11]. In covalent materials, electronically driven phase transitions were reported, also referred to as nonthermal melting. They are attributed to changes in the potential-energy landscape of the lattice by the excited electrons [12–15]. In metals, a thermal process is generally considered driven by the progressive energy transfer from the electrons to the lattice [4,16–18]. Theoretical calculations predict different behaviors depending on the nature of the electronic density of state [10,19]. But even for a given element (e.g., gold as a full *d*-band metal prototype) the question is still debated whether the strongly excited electron system can cause lattice strengthening [10], or weakening [20], also referred to as bond hardening or softening, respectively. There is therefore a critical need for reliable experimental data to constrain the different theoretical approaches, especially for such full *d*-band metals.

Understanding of the electron-ion dynamic interplay requires addressing two major questions. The first difficulty consists of controlling the energy exchange between electrons and ions. The two-temperature model (TTM) has been proposed to provide a simple view of the dynamical process, assuming that both subsystems can be described by respective temperatures T_e and T_i [21]. Their evolution depends on physical parameters (heat capacities C_e and C_i , and electron-ion coupling factor G) that have a strong impact on the structural dynamics of the system and lead whether any phase transition occurs at higher or lower ion temperature rather than the one expected at thermal equilibrium [22]. This is the reason why C_e , C_i and G must be accurately calculated as a function of the temperature.

The second challenge is to get time-resolved data measurements directly related to the phase transition dynamics. That requires appropriate diagnostics whose implementation is complicated by the fact that the sample is generally destroyed after each laser shot. The first studies were carried out with femtosecond all-optical pump-probe experiments [23-25]. They have provided significant advances to the field, including the observation of a quasisteady state lasting about 10 ps in warm dense gold [18,26–28]. However, the link between the phase transitions and the associated changes in the amplitude and phase of an optical probe remains indirect. Time-resolved diffraction experiments of x rays [13,14] and electrons [4,16,17] have also been reported. These constitute real technological prowess and give access to the temporal evolution of the atomic structure. In the regime of high specific energy density (≥ 1 MJ/kg), homogeneous melting transition has been observed to be complete within a relatively long time of ~ 10 ps in warm dense gold [4,17], supporting the theoretical predictions of an increased and T_{e} -dependent melting temperature [10,29].

X-ray absorption near-edge spectroscopy (XANES) has been recently proposed to probe nonequilibrium warm dense matter [7], demonstrating time resolution down to the femtosecond [30–32]. This alternative diagnostic has great potential because it can provide simultaneous information at the atomic scale on the structures of electrons and nuclei. The electron temperature evolution has been retrieved in warm dense copper and supports the TTM predictions with T_e dependent C_e and G [30,33,34]. The short-range picosecond disordering has been resolved in warm dense aluminum [35]. This last provided data on the ion temperature dynamics, but not on the phase transition from solid to liquid in which the short-range order is not significantly changed [36].

In this Letter, we demonstrate that time-resolved XANES can be exploited to resolve the ultrafast dynamics of the phase transition from fcc solid to aperiodic warm dense copper. In addition to the original method presented to track the loss of the crystal periodicity, the diagnostic has already been proven to provide simultaneous control of the T_e dynamics. This results in invaluable data on the solid-to-liquid transition. Such transition is considered from the point of view of the electronic structure that drives most of the macroscopic physical properties. In the range from 1 to 5 MJ/kg, this melting time is observed near one picosecond. It compares quite well with simple TTM predictions using T_e -dependent C_e and G, and considering the melting temperature at thermal equilibrium.

In a crystalline solid, the electronic structure is intimately related to the periodicity of the atomic lattice. Figure 1(a) shows such electronic band structure in the reciprocal space for fcc-Cu. Extrema in the dispersion relation (dE/dk = 0)lead to band edges in the density of state [Fig. 1(b)], which are referred to as van Hove singularities [37]. These result in corresponding peaks in the x-ray absorption spectrum [in the 10 eV above the Cu L edge as reported in Fig. 1(c)]. They are characteristic of the crystalline phase. For example, a peak located at another energy is observed in bcc-Cu [38]. Note that this signature of the crystalline phase is different from the features that result from the photoelectron wave function scattering on the nearestneighboring atoms and that are related to the short-range atomic order, such as sharp resonant lines or EXAFS oscillations [39].

When the solid copper turns to liquid, the lattice periodicity is lost and the consequent peaks above the x-ray absorption L3 edge are expected to vanish. Ab initio molecular dynamic simulations (AIMD) have been performed in order to confirm this intuitive view in warm dense copper. The assumptions and methodology are fully detailed in Ref. [40]. Some calculations are reported for illustration in Figs. 2(b) and 2(c). As it was discussed and exploited in previous papers, a pre-edge is observed as the electron temperature T_e increases [30,33,34]. It is partially compensated by the reduction of the absorption just at the L3 edge (peak labeled "1"). They both result from the promotion of some electrons from the 3d band up to higher energy states when T_e increases. When T_i increases, the postedge peaks (labeled "2" and "3") disappear, as a direct consequence of the van Hove singularities vanishing.

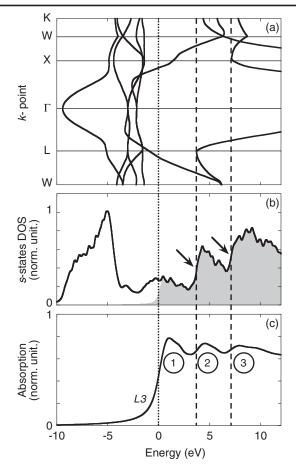


FIG. 1. Principle of the van Hove singularities in fcc-Cu and their signature on the L3-edge XANES spectrum. (a) Electronic band structure. (b) Corresponding projected DOS on *s* states. The shaded area (gray) represents the unoccupied states. The *k* points (L and X) where the energy reaches extrema (vertical dashed lines) lead to singularities in the DOS (edges marked by arrows). (c) They result in peaks labeled 2 and 3 in the XANES spectrum. The peak labelled 1 is the consequence of the Fermi energy E_F that separates occupied and unoccupied states. The *x*-axis origin (dotted vertical line) is set to E_F in (a) and (b), and to the associated L3-edge energy (932.5 eV) in (c).

Time-resolved XANES spectra near the Cu L3 edge have been recorded on a dedicated tabletop setup developed at CELIA laboratory, and fully described in Ref. [41]. The laser-based x-ray source is generated by the interaction of a probe beam (600 fs FWHM, ~80 mJ) with xenon clusters, providing about 35 000 x-ray photons per eV per pulse with 1.2 ± 0.2 ps rms duration at the sample plane [42]. Samples are made of 80 ± 5 nm of Cu deposited on $0.9 \ \mu$ m of Mylar. The copper thickness was chosen to expect a homogeneous energy deposition limited to copper (optical penetration depth of 12.7 nm, and ballistic electron mean free path of 70 nm [30]). Sample are heated by *p*-polarized optical pulses of 300 fs duration, at 30° incidence. The spatial profile is flat top on the sample, with a diameter (~1 mm) larger than the x-ray spot

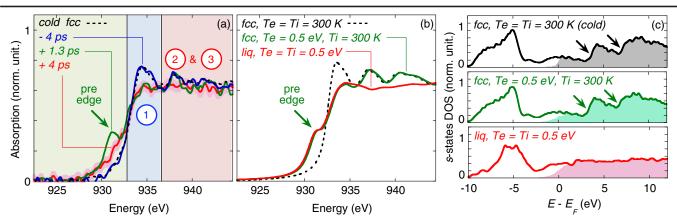


FIG. 2. (a) Some time-resolved XANES spectra measured at $F_{abs} = 0.065 \pm 0.015 \text{ J/cm}^2$. For clarity reason, the error bar is only indicated for the delay +4 ps. The energy intervals for spectral integration of the pre-edge and the postedge peaks labeled 1, then 2 and 3 are indicated with shaded color areas (respectively, in green, blue, and red). (b) Some calculated XANES spectra. (c) Corresponding computed projected DOS on *s* states. The van Hove singularities characteristic of the fcc crystalline phase are indicated with arrows.

(gaussian profile with 300 μ m FWHM diameter). The laser energy reaches ~10 mJ, corresponding to incident fluence up to ~1 J/cm². As the heated area is usually destroyed after a single shot, the sample is replaced by the use of a motorized translation. The effective repetition rate is 2 Hz.

Some registered spectra are presented in Fig. 2(a) for an absorbed laser fluence $F_{abs} = 0.065 \pm 0.015 \text{ J/cm}^2$ (~1 MJ/kg). Each results from the accumulation of more than 2000 laser shots, in order to obtain a signal-to-noise ratio sufficient to resolve the tenuous postedge peaks. Just after the laser heating (delay 1.3 ps), a pre-edge is observed, testifying to the T_e increase. The peaks 2 and 3 are still clearly observed, demonstrating a strong nonequilibrium situation with hot electrons and still fcc-Cu lattice. These peaks then disappear at 4 ps, which reveals an ultrafast phase transition from fcc-solid to liquid. The evolutions of the peak 1, and of the peaks 2 and 3 are plotted in Fig. 3 as a

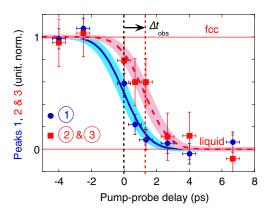


FIG. 3. Time evolution of the peak 1 (blue circles), and the peaks 2 and 3 (red squares) that sign the transition of the electron structure from fcc solid (value set to 1) to liquid (value set to 0). The laser fluence is the same as in Fig. 2(a). The instrumental response is reported (full line in blue). The data of the peaks 2 and 3 are fitted with the same function, but shifted by a delay Δt_{obs} (dashed line in red).

function of the pump-probe delay. They are evaluated by spectral integration [intervals indicated in Fig. 2(a)]. Normalized units, resulting from comparison with cold fcc and liquid spectra are chosen to compare them more easily (see the Supplemental Material [43] for details on the normalization procedure). As expected, the evolution of the peak 1 is simultaneous with the laser heating (zero delay). The decreasing time is limited by the convolution by the 1.2 ± 0.2 ps rms Gaussian x-ray pulse duration. The corresponding instrumental response is plotted in Fig. 3 (full line). The evolution of the peaks 2 and 3 presents the same decreasing time limited by the instrumental response. But the whole set of data is time shifted by Δt_{obs} . This observation suggests a sudden phase transition, that starts at $\Delta t_{\rm obs}$ after the electrons heating. At the relatively low fluence considered here, this measured melting time is estimated at $\Delta t_{obs} = 1.25 \pm 0.5$ ps (the fitting procedure is detailed in the Supplemental Material [43]).

As previously published, the evolution of T_e can be retrieved from the spectral integration of the pre-edge [30,33,34]. Results are plotted in the Fig. 4. They are compared with the T_e and T_i dynamics calculated with the one-dimensional Lagrangian hydrodynamic code ESTHER in which the TTM is consistently integrated [44]. The laser absorbed fluence measured in the experiment is used. T_e dependent coefficients are considered for the electron heat capacity C_e and the electron-ion coupling factor G [22]. The ion heat capacity is derived from the Bushman Lomonosov Fortov (BLF) equations of state that are used in ESTHER [45]. A satisfactory agreement is observed for T_e time evolution, giving a high degree of confidence in the control of the temperatures dynamics. Under these rather simple considerations, we sought to compare the Δt_{obs} measurement with the time Δt_m needed for T_i to pass over the melting temperature.

The delay Δt_{obs} for the loss of lattice periodicity has been measured at different absorbed laser fluences, by using the

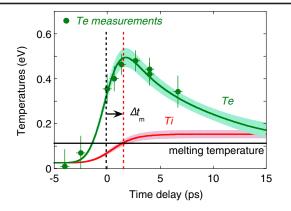


FIG. 4. Time evolution of both electron (T_e) and ion (T_i) temperatures estimated with the two-temperature code at $F_{abs} = 0.065 \pm 0.015 \text{ J/cm}^2$ (see details in the text), and convoluted with the time instrumental response. The shaded areas come from the fluence uncertainty. Values of T_e deduced from the pre-edge measurements are reported (circles).

same procedure detailed above. Results are reported in the Fig. 5 with the corresponding error bars issued from the analysis. The specific energy density deposited in the 80 nm Cu layer ranges from ~ 1 to 5 MJ/kg (corresponding to absorbed fluence from 0.065 to 0.4 J/cm^2), i.e., large enough to guarantee a homogeneous melting transition [17]. The melting times Δt_m issued from ESTHER calculations are plotted for comparison. A strong mismatch is observed when considering the low temperature electronion coupling ($G_0 = 10^{17} \text{ W/m}^3/\text{K}$) and free electron gas electron heat capacity (C_e FEG). That illustrates the importance of properly defining these coefficients. On the other hand, the agreement is rather satisfactory when considering the coefficients $C_e(T_e)$ and $G(T_e)$, which have been independently constrained by the time evolution of T_e (cf. Fig. 4 and Ref. [22]).

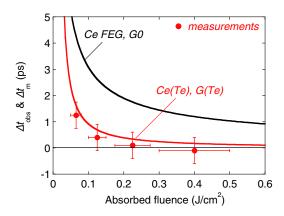


FIG. 5. Time delay Δt_{obs} for the electron structure transition from fcc to liquid, measured as a function of the absorbed laser fluence. Data are compared with two-temperature calculations performed with two sets of physical parameters (Δt_m , see details in the text).

The melting temperature that is taken into account to estimate Δt_m is the tabulated value at ambient conditions $T_{\text{melt}} = 1358 \text{ K}$ (0.117 eV). This has been generally considered by previously reported experimental studies [4,17]. Theoretical work shows that T_{melt} is likely to depend on several factors, that could affect the melting time. It should increase with electronic temperature and pressure, and decrease with density during hydrodynamic expansion (see, e.g., the Refs. [46,47]). A theoretical study integrating all these mechanisms in a self-consistent way goes beyond the scope of the present experimental study, but observations seem to indicate that these effects might compensate each other.

Data indicate a melting time near 1 ps at 1 MJ/kg, and even subpicosecond up to 5 MJ/kg. These values are significantly shorter than previous time-resolved electron diffraction data, measured in a similar regime in warm dense gold [4,17]. This contradiction, assuming that the melting is driven by the same mechanisms in full *d*-band Cu and Au, is probably only apparent, since the observables are not the same. Indeed, AIMD calculations of the ion pair correlation function (see the Supplemental Material [43]) suggest that the transition of the electronic structure (probed by XANES) is more pronounced during the melting than that of the ion structure (probed by diffraction), i.e., is more sensitive to a sudden change of temperature. A last consideration concerns the time needed to reach a complete phase transition, i.e., to achieve the diffraction patterns of the liquid at equilibrium. This requires additional time needed for the solid density to relax down to the liquid one. ESTHER calculations show that following the formation of a liquid layer at the surface, the liquid-solid interface propagates inside the sample at the sound velocity (~ 5 km/s from BLF). This gives a time of ~ 8 ps to put the entire layer in the liquid state, a value consistent with the electron diffraction observations [4,17].

In summary, we have performed a time-resolved XANES experiment to study the phase transition dynamics in femtosecond laser heated warm dense copper. Exploiting some features associated with van Hove singularities in the electron structure, the loss of the lattice periodicity is observed in the picosecond or even subpicosecond timescale, in the range of specific energy density from 1 to 5 MJ/kg. A simultaneous control of the electron temperature dynamics is provided by another feature in the x-ray absorption spectra. The overall observations are fairly well reproduced by a simple two-temperature model, provided that T_e -dependent coefficients are considered [22] and assuming that the melting occurs when the ion temperature exceeds the melting temperature. Data do not indicate any bond hardening effect, which is not surprising since this effect has been predicted for $T_e \ge 3$ eV [10], while T_e does not exceed 2 eV in the present work. In order to investigate such effect, one needs to achieve higher energy deposition and to get XANES data with a femtosecond time resolution, which should be possible now with XFEL [48] or even with laser-based betatron x-ray source [32,49]. The van Hove singularities being expected in a large number of crystalline solids, the technique reported in this paper is *a priori* generalizable to materials other than copper.

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