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# Crack damage identification of a thick composite sandwich structure based on Gaussian Processes classification

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#### Abstract

Structural damage of composite materials used in aeronautics and aerospace has attracted increasing attention. Efficient and reliable Structural Health Monitoring (SHM) systems are required to provide a probabilistic interpretation of diagnostics. In this study, crack damage identification of a thick composite sandwich structure based on Gaussian Processes (GP) classification is reported by numerical simulations. The goal of the study is to obtain a data-driven probabilistic interpretation of damage detection. The investigation is carried out based on healthy and damaged status of a sandwich panel with a honeycomb core modelled in ANSYS. Instantaneous signals with different frequencies are applied to the structure and finite element analysis is performed to obtain vibration responses in both statuses. Features extracted by Discrete Wavelet Transform (DWT) are used to train and test the GP model to assess the health status of the structure. Impacts of mother wavelet in DWT, likelihood function and inference method, as well as iteration numbers are investigated on the classification accuracy. The pertinence of sensors located at different positions is also investigated. This proposed method is effective for crack-type damage detection in the studied composite sandwich structure. It is expected to be suitable for damage detection of more complex structures.

*Keywords:* Structural health monitoring, Gaussian Process classification, composite sandwich structure

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#### 1 1. Introduction

Advanced composite materials have been widely used in different areas, in-2 cluding aerospace, medicine, machinery, construction and other industries due 3 to the characteristics of light weight, corrosion resistance, heat insulation, sound 4 insulation, shock absorption and high (low) temperature resistance, etc., which 5 typically meet the functional requirements in specific working environments [1]. 6 The application of composite materials is gradually replacing the role of con-7 ventional metal alloys in many fields. However, due to the synthesis method of 8 composite materials, they are susceptible to several structural damages, such as 9 fiber fracture, matrix crack and delamination. These damages are usually caused 10 by fatigue and impact events. In the early stage of the damages, they are very small 11 and barely visible to visual inspections, but under certain conditions they may 12 affect the performance of structures and further lead to catastrophic consequences, 13 especially for aircrafts, resulting in huge loss of people lives and money. Therefore, 14 the development of *Structural Health Monitoring* (SHM) systems that can detect 15 damages in a structure has been considerable concerns in the last 2 decades [2]. 16

SHM aims to give, at every moment during the life of a structure, a diagnosis of 17 the "state" of the constituent materials, of different parts, and of the full assembly 18 of these parts constituting the structure as a whole [2]. Health monitoring of 19 structures is initially assessed by visual inspection to approximate the damage 20 location, but damages in bonded structures especially in composite materials are 21 often within the structure and barely visible or even invisible. As a result, several 22 non-destructing testing (NDT) methods that are capable of detecting internally 23 hidden damages are employed during the short inspection intervals [3]. 24

Two of NDT methods, vibration-based technique and guided wave-based technique have been developed for the extraction of damage-sensitive information about the health state of structures. They are the most commonly used among others. A general process of the SHM based on these methods involves collecting relevant data, which is the structure response, from an array of sensors attached on the structure. Then necessary signal processing is carried out for the purpose of data reduction and key feature extraction from these measurements. Finally, the

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healthy state of the structure is determined by statistical analysis of these features. 32 Vibration-based damage detection focuses on the detection of the mode shape 33 singularity and natural frequency changes created by local discontinuity due to 34 damages [4-12]. Several researches have successfully implemented this method in 35 SHM of composite materials. Yang et al. [4] proposed a vibration-based damage 36 detection method for composite plates with delaminations using modal frequency 37 surface (MFS). It is found that the effectiveness of the MFS approach depends 38 on the delamination location by analyzing the modal frequencies. Zhu et al. [5] 39 proposed a vibration-based NDT to detect debonding in honeycomb sandwich 40 beams based on the natural frequency changes caused by damages. Honeycomb 41 sandwich beam is considered equivalent to homogeneous materials in low fre-42 quency because the local periodic structure is much smaller than the wavelength. 43 However, the proposed method cannot effectively detect small damages in large 44 structures. A damage indicator based on modal rotational mode shapes obtained 45 with a uniform rate continuously scanning laser Doppler vibrometer (CSLDV) 46 technique was proposed by Huang et al. [6] for crack damage detection. The pro-47 posed method is proved potential for practical applications, such as ultra-light or 48 composite structures. It is worth mentioning that in vibration-based NDT, wavelet 49 analysis has been applied in many studies for the post-processing of vibrational 50 mode shapes to extract features for damage detection. Vibration-based NDT with 51 wavelet analysis was applied to a composite sandwich plate to detect different types 52 of damages by extracting modal shapes of vibration in the research of Katunin 53 [7]. Sandwich plate with damages was scanned by two laser Doppler vibrometers 54 (LDV) by experiment and the amplitudes of wavelet analysis coefficients were 55 used to represent the presence and location of damages. Results show that the 56 proposed method is capable to detect and localize different damages using wavelet 57 analysis. But the proposed method should not be limited to the laboratory scale test. 58 A novel method for identification of multiple damage by combining shearographic 59 NDT and 2D undecimated wavelet transform based on modal data was proposed 60 by Katunin et al. [8]. The proposed method with wavelet analysis shows high 61 sensitivity compared to the analysis of raw shearographic results. Similar result 62 was observed in another research conducted by Zhou et al. [9] based on contin-63 uous wavelet transform, which shows that the sensitivity for damage detection 64 is increased by wavelet analysis. A thorough review of vibration-based damage 65 detection is presented in [13-15]. 66

Guided wave-based damage detection focuses on the detection of discriminative features such as the difference of amplitudes, elastic wave energy variation and changes in wave propagation pattern due to the interaction between propagated

waves and material discontinuity where damage occurs [16-19]. Yu et al. [16] used 70 ultrasonic feature guided waves (FGW) which focused on the wave propagation 71 energy to detect damages on quasi-isotropic composite laminates. The interaction 72 of the identified FGW mode with different types of defects was studied by both 73 simulation and experiment. Close agreement was observed between the numerical 74 measurement and experimental measurement. It is demonstrated that the proposed 75 FGW method has good potential for efficient damage detection in composite bends. 76 Aryan et al. [17] proposed a model-based method for damage detection with 77 guided wave. Normally guided wave-based method is conducted by comparing a 78 baseline signal recorded for a damage-free structure with or subtracted from the 70 signal recorded during the inspection. In the proposed method, the uncontrollable 80 factors that may affect the accuracy such as temperature variation, sensor errors 81 and material property changes due to degradation were compensated. Experimental 82 and numerical approaches were conducted and demonstrated the feasibility of 83 the proposed method. Nevertheless, the utilisation of 3D measurement system 84 together with transient finite element simulations will significantly increase the 85 cost. Theoretical and numerical studies were conducted by Sikdar et al. to identify 86 disbond and high density core region in a honeycomb composite sandwich structure 87 using ultrasonic guided waves [18]. Laboratory experiment was then carried out 88 to validate theoretical and numerical results. Interaction of guided waves with 89 damages was analyzed through the structural response signals. A good agreement 90 91 was observed between analytical, numerical and experimental results. It is found that the presence of high density core region results in a decrease in amplitude 92 of the propagating guided wave modes and the presence of debond results in a 93 significant amplification of the primary anti-symmetric mode. Similar method 94 was also adopted in [20-22]. A thorough review of guided wave-based damage 95 detection methods is presented in [19, 23, 24]. 96

To achieve a better accuracy in damage detection, Radzienski et al. [25] 97 combined vibration-based and guided wave-based approaches without reducing the 98 effectiveness of NDT techniques for detection of debonding in honeycomb core 99 panels, and higher defect detection reliability was achieved by a double verification. 100 Both vibration-based and guided wave-based techniques have been proved capable 101 of detecting damages occurred in composite structures and other materials. They 102 have good performance in some certain conditions and show a good potential in the 103 application in more fields. However, a common process of these two methods is that 104 the vibration responses of a structure should be analysed all by human labor, which 105 leads to two disadvantages: firstly, they are time-consuming and labor-intensive; 106 secondly, there will be high requirements of expertise for practitioners during the 107

analysis of structural vibration responses, especially for complex structures, whichis not always available.

With the development of Artificial Intelligence (AI) in the last two decades, 110 the problems encountered in the traditional approaches have been solved. In this 111 study, a machine learning algorithm Gaussian Process is proposed to predict crack 112 damages of a thick composite sandwich panel by numerical simulations address-113 ing the difficulty in constructing a database for structural health monitoring of 114 real composite structures and the inconvenience in conventional expertise-based 115 SHM approaches. The goal of the study is to obtain a data-driven probabilistic 116 interpretation of damage detection. A squared panel constituted of two composite 117 faces in carbon/epoxy and a honeycomb core is modelled by commercial software. 118 The investigation of this structure is carried out based on two status of the model: 119 healthy model and damaged model. Instantaneous signals with different frequen-120 cies are applied to the structure and finite element analysis is performed to obtain 121 vibration responses in healthy and damaged status, respectively. Features extracted 122 by discrete Wavelet Transform (DWT) from these responses are fused and defined 123 as input to the Gaussian Process. The Gaussian Process model is trained and tested 124 to assess the health status of the structure. The DWT can speed up the computation 125 time with proper selection of mother wavelet without major loss of information. 126 The impact of likelihood function and inference methods employed in Gaussian 127 Process on the classification accuracy is investigated. It is observed that with more 128 129 iterations, the classification is slightly better than with less iterations, which is consistent with common sense. The pertinence of data from sensors located at 130 different positions is also investigated. Finally, an overall classification accuracy of 131 100% is obtained, which proves the proposed method is effective for crack-type 132 damage detection in the studied composite sandwich structure. 133

The rest of this paper is organized as follows: the basic theoretical background including the feature extraction method DWT as well as machine learning approach GP will be introduced in section 2. The proposed damage detection system and data processing technique are explained in section 3. Model description together with simulation approach are described in section 4, followed by results and discussions in section 5. Finally, section 6 concludes the paper and suggests potential future works.

#### 141 2. Theoretical background

The development of data-driven approaches has provided great convenience in scientific research, but the problem of data redundancy has been an obstacle to efficiency. Ideally, data containing key information are used while useless data are
eliminated. For this purpose, a signal processing and feature extraction method,
Discrete wavelet transform (DWT) is firstly introduced in the current research.
Then conventional machine learning method Gaussian Process will be applied.

#### 148 2.1. Feature extraction by Discrete Wavelet Transform

DWT was proposed, on one hand, to extract information in both time and 149 frequency domain through multi-resolution analysis, on the other hand to reduce 150 the dimension of data, which resolves the problem of redundancy. Since the time 151 domain signal is a discrete time sequence, we denote the sequence as x[n] with n 152 an integer. The transform is computed by passing the signal through a half band 153 digital lowpass filter with impulse response h[n] and a half band highpass filter 154 with impulse response q[n] simultaneously. The filtering, from a mathematical 155 point of view, is convolution of the signal with the filter. A half band lowpass 156 filter removes all frequencies above half of the highest frequency in the signal, 157 whereas a half band highpass filter removes all frequencies below half of the highest 158 frequency. After passing the signal through filters, detail coefficients from the 159 output of highpass filter and approximation coefficients from the output of lowpass 160 filter are obtained. Since half the frequencies of the signal have been removed, half 161 the samples can be discarded according to Nyquist's theorem. Thus, the output of 162 lowpass filter is subsampled by 2. This constitutes one decomposition level. This 163 decomposition has halved the time resolution since the number of samples has 164 been halved, but has doubled the frequency resolution since the frequency band 165 has been halved. The subsampled output of lowpass filter is further processed 166 by passing it again through a new lowpass filter h|n| and a highpass filter g|n|167 constituting another decomposition level. It should be noted that the highpass and 168 lowpass filters are known as the Quadrature Mirror Filters (QMF) and are related 169 by: 170

$$g[L - n - 1] = (-1)^n \times h[n]$$
(1)

#### 171 2.2. Gaussian Processes classification

Supervised machine learning has been widely used to learn a function that maps an input to an output based on example input-output pairs [26]. As one sub-field of machine learning, it helps to improve the efficiency and reduce error in problem solving. It can be divided into regression and classification problems. The outputs for regression are continuous values whereas for classification are discrete class labels. The idea of machine learning-based SHM is to learn the relations between input variables and output variables. One machine learning algorithm that is capable of learning features from data and providing a probabilistic interpretation
of predictions is Gaussian Process (GP). A GP can be considered as a Gaussian
distribution over functions rather than over variables, and inference takes place
directly in the space of functions [27]. A machine learning algorithm involving GP
takes a measure of the similarity between points to predict the value for an unseen
point from the training data. There are several GP models for regression problems,
but in this study, a GP model for classification is employed.

An introduction of a GP model for regression problems is firstly carried out because it is a necessary step for understanding GP model for classification problems. Given an input vector variable x with dimension D, the corresponding output target t is related with the input vector by a nonlinear smooth mapping function f with an additional Gaussian noise  $\epsilon$ 

$$t = f(\mathbf{x}) + \epsilon \tag{2}$$

In the same way, for a given input training data set  $\mathbf{D} = {\mathbf{X}, \mathbf{t}}$  containing input training matrix  $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_N]^T$  constituted by vectors  $\mathbf{x}_i$  and corresponding training target vector  $\mathbf{t}$ , in which each element is expressed as  $t_i = f(\mathbf{x}_i) + \epsilon$ , i =1, 2, ..., N, we are interested in making inferences about the relationship between inputs and targets as well as making predictions for a new input. Therefore, GP is involved by modeling the mapping function f with a zero mean and covariance matrix  $\mathbf{K}$ , see Eq. (3):

$$p(\mathbf{f}|\mathbf{D}) \sim \mathcal{N}(\mathbf{f}|\mathbf{0}, \mathbf{K})$$
 (3)

where  $\mathbf{f} = [f(\mathbf{x}_1), f(\mathbf{x}_2), ..., f(\mathbf{x}_N)]^T$ , **K** is the covariance matrix, computed by covariance function  $k(\mathbf{x}_i, \mathbf{x}_j)$ , also called kernel function, expressed by Eq. (4). The covariance function is expected to make similar predictions of target values  $t_i$ and  $t_j$  for similar input points  $\mathbf{x}_i$  and  $\mathbf{x}_j$ . Therefore, the squared exponential with automatic relevance determination distance (SE-ARD) measure expressed by Eq. (4) is adopted in the present study:

$$k(\mathbf{x}_i, \mathbf{x}_j) = cov(f(\mathbf{x}_i), f(\mathbf{x}_j)) = \sigma_f^2 exp(-\frac{1}{2}(\mathbf{x}_i - \mathbf{x}_j)^T \mathbf{M}(\mathbf{x}_i - \mathbf{x}_j))$$
(4)

where  $\mathbf{M} = diag(\lambda_1, \lambda_2, ..., \lambda_N)$ , with each  $\lambda_i$  corresponding to input dimension characteristic length scale.  $\sigma_f^2$  is the signal variance.  $\lambda$  and  $\sigma_f^2$  are hyperparameters. In the training step, the objective is to model an appropriate mapping function f so that the training target  $t_i$  corresponds well to the training input vector  $\mathbf{x}_i$ . The learning task is achieved by tuning the hyperparameters denoted by  $\Theta$  in the covariance function. And the optimization is accomplished by minimizing the negative logarithmic likelihood function with respect to the hyperparameters in Eq. (5), which corresponds to choosing the value of  $\Theta$  for which the probability of the observed data set is maximized.

$$L(\Theta) = -\log\left(p\left(\mathbf{t}|\mathbf{X}\right)\right) = \frac{1}{2}\log|\mathbf{K}| + \frac{1}{2}\mathbf{t}^{\mathrm{T}}\mathbf{K}^{-1}\mathbf{t} + \frac{N}{2}\log\left(2\pi\right)$$
(5)

where  $|\mathbf{K}|$  refers to the determinant of the matrix  $\mathbf{K}$ .

The role of the GP model is to use known data X and  $\mathbf{t} = [t_1, t_2, ..., t_N]$  to predict the output target of a new input vector  $\mathbf{x}_{N+1}$ . As the covariance matrix K is composed of the covariance between each of the first N input vectors, for a new input vector  $\mathbf{x}_{N+1}$ , the joint probability distribution can be expressed as:

$$p(\mathbf{t}_{N+1}) = \mathcal{N}(\mathbf{t}_{N+1}|\mathbf{0}, \mathbf{K}_{N+1})$$
(6)

where  $\mathbf{t}_{N+1} = [t_1, t_2, ..., t_{N+1}]^{\mathrm{T}}$ , and the covariance matrix  $\mathbf{K}_{N+1}$  is expressed as:

$$\mathbf{K}_{N+1} = \begin{bmatrix} \mathbf{K} + \sigma_n^2 \mathbf{I} & \mathbf{k} \\ \mathbf{k}^{\mathrm{T}} & c \end{bmatrix}$$
(7)

with **k** a vector with elements  $k(\mathbf{x}_n, \mathbf{x}_{N+1})$  for n = 1, 2, ..., N, and c a scalar with value  $c = k(\mathbf{x}_{N+1}, \mathbf{x}_{N+1}) + \sigma_n^2$ . It's clear to see that the vector **k** and the scalar care both dependent on the test point input vector  $\mathbf{x}_{N+1}$ . The predictive conditional distribution over  $t_{N+1}$  is a Gaussian distribution with mean and covariance given by [28]:

$$\mu \left( \mathbf{x}_{N+1} \right) = \mathbf{k}^{\mathrm{T}} \mathbf{K} \mathbf{t},$$
  

$$\sigma^{2} \left( \mathbf{x}_{N+1} \right) = c - \mathbf{k}^{\mathrm{T}} \mathbf{K} \mathbf{k}$$
(8)

These two items are the most important for the regression because they provide both prediction mean value and uncertainty information. In a GP regression example, the regression problem is resolved by making a prediction of a new target for a new input with a predictive mean value and uncertainty information indicated by a confidential interval. It shows the more sparse the data, the larger the uncertainty interval of the prediction.

For a classification problem, our goal is to model the posterior probability distribution of the target for a new input vector, given a set of training data. The predictive probabilities should be in the interval [0, 1], but the prediction result of the Gaussian Process is within the entire real range. However, GP model can be adapted to classification problems by transforming the output using an appropriate nonlinear activation function, such as logistic sigmoid:

$$\sigma(f) = \frac{1}{1 + exp(-f)} \tag{9}$$

Consider a binary classification problem with target value  $t \in \{-1, 1\}$ . A Gaussian Process is defined over a function f(x) and then this function is transformed by a logistic sigmoid  $y = \sigma(f)$ , with  $y \in (0, 1)$ . The probability distribution of the target variable is given by the Bernoulli distribution:

$$p(t|f) = \sigma(f)^{t} (1 - \sigma(f))^{1-t}$$
(10)

Similar to the regression, the training input vectors are denoted by  $x_1, x_2, ..., x_N$ , 240 the corresponding observed targets are denoted by  $\mathbf{t}_N = [t_1, t_2, ..., t_N]^{\mathrm{T}}$ . The 241 objective is to determine the predictive distribution of  $p(t_{N+1}|\mathbf{t}_N)$ . In classification 242 problems, the Gaussian noise  $\epsilon$  in covariance matrix no longer exists because 243 it is assumed that every training input vector is correctly labelled. In a two-244 class problem, predicting  $p(t_{N+1} = 1|\mathbf{t})$  is enough because the probability of 245  $p(t_{N+1} = -1|\mathbf{t})$  is obtained by  $1 - p(t_{N+1} = 1|\mathbf{t})$ . The expected predictive 246 distribution is obtained by a marginal distribution expressed as: 247

$$p(t_{N+1} = 1|\mathbf{t}) = \int p(t_{N+1} = 1|f_{N+1})p(f_{N+1}|\mathbf{t})df_{N+1}$$
(11)

where  $f_{N+1} = f(\mathbf{x}_{N+1})$ . However, this integral is analytically intractable. To approximate the integral, several inference methods can be taken into account, such as Laplace approximation, variational inference, expectation propagation, etc.

# 3. Proposed Gaussian Processes classification method for composite sand wich structure

The proposed Gaussian Process includes 2 main steps: training step and testing step for the purpose of classification using the processed signals from sensors. In the first step, training for each case corresponding to healthy and damaged structural status is performed. The training data is correctly labeled. In the second step, the GP model obtained from previous step is used to evaluate unknown features so as to determine if damages appear in the structure or not.

#### 259 3.1. Training step

Damage detection of a structure is achieved by a SHM system consisting of several sensors permanently attached on the structure. Each sensor can be used as an actuator to apply an pulse excitation signal or as a receiver to collect data. In each simulation scenario, a pre-defined pulse signal is applied on the actuator. The signal interacts with elements of the structure during the propagation over

the whole structure. Sensors located at three corners are considered capable of 265 collecting signals that have interacted with potential damages without missing 266 information. These raw time series signals are processed with Discrete Wavelet 267 Transform. This step can be regarded as reduction of data dimension and feature 268 extraction because DWT is used to extract information in both time and frequency 269 domains as well as discarding data that is not dominant without any major loss of 270 information. The Coiflet 5 is chosen as mother wavelet after comparing with other 271 wavelets. This wavelet is the optimal among others in terms of errors. 272

In each simulation case, one file containing signals collected by three sensors 273 is obtained. It should be noted that, the duration of each simulation is 0.01s and 274 the sampling frequency depends on the input signal frequency, thus the number 275 of sampling points for a fixed time duration is different for different signals. Note 276 that in DWT the successive subsampling is by 2, the collected signal length should 277 be a power of 2 or a multiple of power of 2 in order to make the scheme efficient. 278 Thus, the first 512 sampled points for signals whose length is more than 512 are 279 used for DWT, while for collected signals whose length is less than 512, zeros 280 are added after each signal until its length becomes 512. DWT is employed for 281 each collected signal, and the corresponding coefficients are saved as one vector. 282 Since the frequency bands that are not very prominent in the original signal will 283 have very low amplitudes, that part of the DWT signal can be discarded without 284 any major loss of information. For this reason, only the first 256 coefficients are 285 286 used, as shown in figure 1. In each simulation, the three vectors after reduction obtained by DWT are merged into one vector which contains all features from 287 different sensors in the order of the sensors. The same procedure is performed for 288 all simulation cases. All the vectors are organized in one matrix in which each row 289 consists of one transposed vector representing one simulation. This matrix contains 290 all features of the structures and this procedure is considered as data fusion. 291 The matrix after data fusion is in the form of: 292

$$\mathbf{X} = \begin{pmatrix} x_{11}^1 & \dots & x_{1K}^1 & x_{11}^2 & \dots & x_{1K}^2 & x_{11}^J & \dots & x_{1K}^J \\ \vdots & \ddots & \vdots & \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ x_{I1}^1 & \cdots & x_{IK}^1 & x_{I1}^2 & \cdots & x_{IK}^2 & x_{I1}^J & \cdots & x_{IK}^J \end{pmatrix}$$
(12)

where the element is denoted by  $x_{ik}^{j}$  in which *i* indicates the simulation number (*i*<sup>th</sup> simulation), *j* indicates the sensor number (*j*<sup>th</sup> sensor) and *k* indicates the coefficient number (*k*<sup>th</sup> coefficient). Group scaling is performed on this matrix in order to remove the mean trajectories of each sensor and to make sure that data from any sensor have the same variance [29]. The element in the matrix is scaled 298 by:

$$\bar{x}_{ik}^j = \frac{x_{ik}^j - \mu_k^j}{\sigma^j} \tag{13}$$

where  $\mu_k^j = \frac{1}{I} \sum_{i=1}^{I} x_{ik}^j$  is the mean of the *I* measurements of sensor *j* for the

<sup>300</sup> 
$$k^{th}$$
 coefficient,  $\sigma^j = \sqrt{\frac{1}{IK} \sum_{i=1}^{I} \sum_{k=1}^{K} (x_{ik}^j - \mu^j)^2}$  is the standard deviation of all

measurements of sensor j, and  $\mu^{j}$  is the mean of all measurements of sensor j. 301 This scaled matrix  $\mathbf{X}$  is used as input of Gaussian Process for subsequence analysis. 302 In GP training step, input vectors in the matrix X are correctly labelled by the 303 ground truth t with t = 1 indicating *healthy status* and t = -1 indicating *damaged* 304 status. Likelihood function together with inference method are employed. These 305 two functions are specified in the training step. Hyperparameters are predefined 306 randomly for the purpose of initialization. The input is then fed into the GP model 307 and in turn an output predicted by the model is given. During the learning process, 308 negative logarithmic likelihood function is used as loss function to optimize all 309 hyperparameters in kernel function and likelihood function so that the error between 310 the predictive output derived from GP and the corresponding ground truth is 311 minimized. The optimization process is achieved by minimizing the negative 312 logarithmic likelihood function with respect to the hyperparameters  $\Theta$ , which 313 corresponds to choosing the value of  $\Theta$  for which the probability of the observed 314 data set is maximized. This procedure is illustrated in figure 2. 315

#### 316 3.2. Testing step

Once the hyperparameters are optimized for the training data, the validated 317 GP model can be used to make predictions for new inputs. In this study, the GP 318 model is used to predict if damages occur in the structure. The testing procedure 319 is the same as that of training before inserting the transformed input into the GP 320 321 model. In testing step, only the trained GP model is used. Besides, different from the training phase where optimized hyperparameters are as output, the trained GP 322 model will provide a predictive mean value corresponding to the new input and a 323 variance of the predictive distribution based on the training data. The predictive 324 mean value indicates in which label class the input is most likely distributed, that's 325 to say healthy or damaged class, while the variance provides an information of 326 confidence, which indicates the reliability of the classification result. It should be 327 noted that the GP model is used to predict the appearance of damages, but unable 328

to localized the probable region where damages occur. The procedure of the testing
step is presented in figure 3.

#### **4. Numerical approach**

In data driven-based SHM systems, information containing the structure's 332 health status is quite important for the performance of the system. Thus, perti-333 nent structural status should be collected to construct a reliable database because 334 different sets of data correspond to different healthy conditions of a structure. 335 However, it is neither economic nor realistic to build real structures of different 336 health status, especially for huge and expensive structures to construct a database. 337 To understand the behaviour of a structure, numerical simulation of structures in 338 different conditions is a promising idea. Therefore, SHM achieved by simulation 339 becomes a compromise way. This study is conducted by simulation approach. 340 The structure is constructed with software ANSYS<sup>®</sup> and numerical model under 341 external excitation is simulated within the software. 342

#### 343 4.1. Composite sandwich plate model

In the present work, a hexagonal shaped Nomex honeycomb core (3D core) 344 and CFRP-skin made composite sandwich plate is selected for simulation and 345 classification tasks. The plate of spatial dimensions 300 mm  $\times$  294 mm  $\times$  19 346 mm consists of a honeycomb core and two face sheets. The thickness of the 347 honeycomb core is H = 15mm in which the radius and wall thickness of each cell 348 are r = 5mm and t = 0.2mm, respectively. The Nomex core's material properties 349 are: density  $\rho_1 = 1240 kg/m^3$ , Poisson's ratio  $\nu_1 = 0.33$ , Young's modulus 350  $E_1 = 5.5 \times 10^9 Pa$ . The thickness of each face sheet is h = 2mm. The face sheets 351 are laminate panels made of carbon/epoxy materials whose properties are: density 352  $\rho_2 = 1850 kg/m^3$ , Poisson's ratio  $\nu_2 = 0.3$ , Young's modulus  $E_2 = 70 \times 10^9 Pa$ . 353 A simplifies illustration of the sandwich structure is referred to figure 4(a). 354

The honeycomb sandwich plate model consisting of a honeycomb core and two skin plates is shown in figure 4(b). Within our study the dimensions of the face sheets and the core will not change.

The face sheets are modeled by the SOLSH190 solid-shell element which has 8 nodes with 3 degrees of freedom at each node: translation in x, y and z directions. In this manner, face sheet shear phenomena can be taken into account when a signal with high frequency propagates in the structure. 2D shell element SHELL181 is used to model the honeycomb cells. The transition area where the face sheet connect to the honeycomb cell is often the weakest region. In our study, the elements of shell and solid-shell are connected with an automatic constrain equation developed by ANSYS<sup>®</sup>. The total number of meshing elements is about 177000, which guarantees a minimum mesh density of 10 elements per wavelength for the model.

Composite materials exposed to long term loads and critical working environ-368 ment may have damages due to fatigue, impact or material degradation. Cracks and 369 delamination are two most common damages for composites. In the first attempt 370 of this study, crack damage is designed in the sandwich structure by disconnecting 371 local nodes and investigation of the capability of detecting this kind of damage is 372 conducted. Models with cracks in different positions are constructed. Five crack 373 damages in the x direction and one crack damage in y direction are created. Cracks 374 in x direction are located at  $(x = \frac{L}{4}, y = \frac{W}{4})$ ,  $(x = \frac{L}{4}, y = \frac{W}{2})$ ,  $(x = \frac{L}{2}, y = \frac{W}{4})$ ,  $(x = \frac{L}{2}, y = \frac{W}{2})$ ,  $(x = \frac{3L}{4}, y = \frac{3W}{4})$ , respectively. Crack in y direction is located at  $(x = \frac{L}{2}, y = \frac{W}{2})$ . The length of cracks is 30mm which is  $\frac{L}{10}$  in x direction, and 375 376 377 crack length in y direction is 43mm, as illustrated in figure 5. Cracks are designed 378 through the core and the top face sheet so that the interaction of the propagated 379 signal with the damage is detectable. 380

For each model, points located in four corners on the top face sheet are 381 selected. One is used as actuator through which the pulse excitation signal is 382 inserted, while the other three are used to collect propagated signals through the 383 structure, as shown in figure 5(a). In actual cases, the actuator converts the input 384 voltage signal into a displacement signal, whereas the sensor converts the received 385 displacement signal into a voltage signal. Thus in the current study, for the sake of 386 convenience, we directly input the displacement signal on the structure and extract 387 the displacement signal at the corresponding position to represent the work of 388 actuator and sensors. The vertical displacement of nodes are collected for further 389 signal processing. 390

#### 391 *4.2. Simulation*

In the simulation of each model, a pulse excitation signal with 7 cycles is 392 applied on the actuator to stimulate vertical displacement. Transient analysis 393 is performed on the sandwich plate structure. Damping coefficients are set as 394 follows: matrix multiplier is set as  $\alpha = 0$  and stiffness matrix multiplier as 395  $\beta = 6.37 \times 10^{-7}$ . The calculation time is set as 0.01s, which is long enough 396 for the wave to propagate through the whole plate. The sampling frequency  $f_s$ 397 should be no less than 2 times the signal frequency f according to the Nyquist's 398 rule. In the present research the sampling frequency is set as  $f_s = 8f$  in order 399 to make the recorded signal be representative. In each simulation case, vibration 400

responses of one structure are collected at three sensors for further use. They are 401 saved in one file to represent the structural health status in that condition. Same 402 simulations are performed for the same structure with input signals of different 403 frequencies. Then the same simulations are conducted for structures with different 404 health status successively. As mentioned above, we have 7 composite sandwich 405 plate models among which one healthy and six with crack damages at different 406 positions. On each model 3 different input signals with frequency 8kHz, 6kHz and 407 4kHz are applied successively corresponding to 3 simulation cases. So far a total 408 of 21 simulation cases are obtained. The objective is to perform the least cases 409 with which machine learning approaches can detect the structure's health status. 410

A comparison of the vibration responses of a healthy structure and the structure 411 in figure 5(b) to a same input signal of 8kHz with 7 cycles at the same position 412 is firstly conducted, as shown in figure 6. The compared signals are from three 413 sensors on the structure together with the input signal. First of all, in both structures 414 it can be seen that the original input excitation signal waveform has changed after 415 propagating along different directions by comparing the signals in figure 6(b-d) 416 with figure 6(a). This is due to the wave dispersion in the structure. Besides, as the 417 core of the structure is honeycomb that has anisotropic properties, the dispersive 418 behavior of the structure is direction-dependant, which results in the differences 419 in the vibration responses from 3 sensors in figure 6(b) to figure 6(d). Moreover, 420 comparing the vibration responses of healthy and damaged structures from sensor 421 422 3, we can find that in the first wave packet, the amplitude of the signal from damaged structure is slightly higher than that from healthy structure, as shown in 423 6(d). It is due to the fact that the existence of the crack damage in this position 424 reduces the bending stiffness of the structure in y direction from the actuator to 425 sensor 3. Furthermore, comparing the healthy and damaged structures in 6(b)426 and (d), the signal difference occurring between wave packets might be caused by 427 the interaction of input signal with the crack, but as the difference is not evident, 428 machine learning algorithm should be used to learn such kind of features. 429

The DWT coefficients are then compared in figure 7. As mentioned in 2.1, 430 DWT can extract information in both time and frequency domain. The mismatch 431 between the vibration responses of healthy and damaged structures can be extracted, 432 as shown in figure 7(b) and (d). It should be noted that only the first 256 coefficients, 433 which correspond to lower frequencies of the analysis, carry relevant information 434 and the rest of the signal can be discarded without any major loss of information. 435 In addition, discarding half of the signal can speed up the computation in further 436 step. 437

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For the six sandwich models with cracks, simulations are conducted with

excitation signals of three different frequencies successively. 30 data sets for each 439 model are collected. For the damage-free sandwich model, same simulations are 440 conducted with excitation signals of three different frequencies successively as for 441 the damage models. 90 data sets are obtained. Thus a data base is constructed with 442 a total number of 270 data sets, in which 90 data for healthy model which is labeled 443 by '1' and 180 data for damaged models labeled by '-1'. 70% of the data base is 444 used for training the GP model and the rest 30% is used for testing. The testing step 445 is a step for evaluating the GP model for damage predictions in composite sandwich 446 plates. In both training and testing step, several factors will affect the results, such 447 as the type of mother wavelet for the DWT, the amount of data discarded by DWT, 448 the selection of likelihood function and inference method for GP, and the number 449 of function evaluations to optimize hyperparameters during the training step, etc. 450 The influence of these factors will be evaluated successively. It is worth mentioning 451 that although discarding the coefficients that have low amplitude in DWT may not 452 lead to major loss of information, it will slightly reduce the accuracy of the results, 453 but the effect is negligible. 454

#### 455 **5. Results and discussions**

In this section, the influence of previously mentioned factors on the classifica-456 tion results is discussed. In binary classification case, 1 represents healthy status 457 while -1 represents damaged status. It is expected that the predictive mean value 458 is as close to 1 as possible for the case whose ground truth is healthy, while the 459 predictive mean value is as close to -1 as possible for the case whose ground truth 460 is damaged. However, in GP classification model, the predictive mean value is not 461 necessarily 1 or -1. Therefore, it is necessary to define a threshold to determine if 462 the prediction from the GP model is correct or not. In the testing step, an overall 463 predictive mean value for each class can be calculated,  $\mu_d$  for damaged class and 464  $\mu_h$  for healthy class. The threshold to separate two classes is defined as the mean 465 value of  $\mu_d$  and  $\mu_h$ . The distance from overall mean value to the threshold is called 466 class distance, which is considered as a measure of the quality of the classifier. If 467 the predictive mean value for a case whose ground truth is damaged is less than 468 the threshold, the prediction is considered as correct, indicating a damaged status. 469 The same, if the predictive mean value for a case whose ground truth is healthy is 470 greater than the threshold, then it means that the status of the structure is predicted 471 as healthy by GP model, which is correct. Otherwise, it is considered that the GP 472 model misclassifies the case. 473

#### 474 5.1. Classification with three sensors

Firstly, the influence of the selection of mother wavelet is investigated. Control 475 variate method is employed, that's to say in each analysis, only one factor is 476 considered as a variable while others are invariant. Daubechies 8 (D8) wavelet and 477 Coiflet 5 (C5) wavelet are compared with 512 saved coefficients in DWT, logistic 478 function as likelihood function, Variational Bayesian (VB) as inference method. 479 40 iterations are adopted in the optimization step, see figure 8. The abbreviation 480 of mother wavelet, saved amount of data in DWT, likelihood function, inference 481 method and iteration numbers are successively listed in the legend on the up-left of 482 the figure. It should be noted that in all the following figures, the first 54 testing 483 points (denoted by  $\Box$ ) along the x-axis are with ground truth 'Damage' while the 484 last 27 testing points (denoted by \*) are with ground truth 'Health'. The global 485 mean value of predictive mean value for all testing damaged cases and that for 486 healthy cases are -0.885 and 0.775 using Coiflet 5 wavelet, while the results using 487 Daubechies 8 wavelet are -0.858 and 0.697 respectively. In addition, every single 488 case is correctly classified using Coiflet 5 wavelet, which suggests that Coiflet 5 is 489 more powerful in extracting features. It should be noted that some other mother 490 wavelets are also evaluated but have poorer performance and the corresponding 491 results are listed in Table 1. the class distance is larger than others while the mean 492 square error is lower, which indicates that the GP model performs better in the 493 classification for both healthy and damaged structures using Coiflet 5 wavelet.

	Haar	Beylkin	Coiflet5	Coiflet3	Coiflet1
Class distance	0.5261	0.8344	0.8803	0.8161	0.8697
MSE	0.0799	0.0374	0.0087	0.0214	0.0135
	D20	D16	D12	D8	D4
Class distance	0.8397	0.8380	0.8408	0.8363	0.8268
MSE	0.0172	0.0140	0.0133	0.0354	0.0251
	Symlet10	Symlet8	Symlet6	Symlet4	Vaidyanathan
Class distance	0.8738	0.8323	0.8575	0.8578	0.8320
MSE	0.0145	0.0329	0.0121	0.0172	0.0162

Table 1: Performance of different wavelets in GP classification.

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Secondly, the influence of the amount of data discarded by DWT on the
 classification accuracy is discussed. According to the previous study, Coiflet
 5 mother wavelet, Logistic likelihood function, Variational Bayesian inference
 method and 40 iterations are used due to the outstanding performance. An example

of DWT coefficients is illustrated in figure 1. All 512 coefficients and the first 499 256 coefficients are separately used for GP model to study the influence on the 500 classification accuracy. Results without discarding coefficients is slightly better 501 than those discarding the last 256 coefficients that have low amplitude, as shown in 502 figure 9, which is reasonable and easy to understand, because although discarding 503 the coefficients that have low amplitude in DWT may not lead to major loss of 504 information, it will slightly reduce the accuracy of the results, but the effect is 505 negligible. 506

Thirdly, the influence of likelihood function and inference method is investi-507 gated simultaneously because there is an issue of compatibility among different 508 likelihood functions and inference methods. Four combinations of likelihood 509 function and inference method are presented in figure 10, including Logistic-VB, 510 Logistic-Expectation Propagation (EP), Logistic-Laplace and Error function (Erf)-511 EP. It can be seen that the Logistic-Laplace combination performs the worst because 512 the predictive mean value for almost all cases are around 0 and far from 1 or -1, 513 which shows that the class distance is too short. The global predictive mean value 514 for healthy and damaged cases are 0.281 and -0.22 respectively. The Logistic-EP 515 combination and Erf-EP combination perform better than Logistic-Laplace, with 516 a global mean value  $\mu_h = 0.714, \mu_d = -0.546$  and  $\mu_h = 0.745, \mu_d = -0.622$ , 517 respectively. However, 3 cases are misclassified with Logistic-EP combination and 518 3 cases are misclassified with Erf-EP combination. A better result is achieved by 519 Logistic-VB combination with global mean value  $\mu_h = 0.667, \mu_d = -0.891$  where 520 the class distance is larger than others, indicating a better classification quality, and 521 only 1 case is misclassified. 522

Finally, the influence of iteration numbers on the accuracy of the classification 523 results is discussed. The iteration number is in the training step of GP model. 524 Normally, the more iterations there are, the more accurate the result is. The 525 result is presented in figure 11, where the horizontal axis indicates intervals of 526 the predictive mean value  $\mu$  and the vertical axis indicates the number of testing 527 data. A comparison of 20 and 40 iterations is carried out. Here the Coiflet 5 (C5) 528 mother wavelet is chosen in the DWT and the first 512 coefficients are saved to 529 be used as input for GP. Logistic function is chosen as the likelihood function and 530 Variational Bayesian (VB) is selected as the inference method. The global mean 531 value of predictive mean value for all testing damaged cases and that for healthy 532 cases  $\mu_g = \frac{1}{n} \sum_{i=1}^{n} \mu_i$  are -0.891 and 0.667 for 20 iterations, while the results for 533 40 iterations are -0.885 and 0.775 respectively. Besides, 1 case with ground truth 534 (GT) 'healthy' is misclassified in the 'damaged' class for 20 iterations, while every 535

case is correctly classified with 40 iterations. Moreover, the class distance for 40
 iterations is larger than that for 20 iterations. It shows that with more iterations, the
 result is slightly better than with less iterations, which is consistent with common
 sense.

It should be noted that the current research is based on simulation, and in 540 real experimental data the impact of environmental noise should be taken into 541 consideration. Therefore, it is necessary to add noise to the simulation data to 542 simulate the influence of environmental noise, so as to verify the stability of the 543 proposed method. White Gaussian noise is added into the raw vibration data that 544 are collected from sensors. Signal-noise ratio (SNR) is set as 20dB. Then the same 545 procedure of signal processing with DWT and Gaussian Process classification is 546 conducted. A comparison of classification result based on noise-free data and data 547 with noise is illustrated in figure 12. Despite the added noise, the class distance has 548 only slightly decreased, and all data can be correctly classified. This proves that 549 the method proposed in this paper is still practical under simulated environmental 550 noise. 551

#### 552 5.2. Classification with one sensor

Now that an acceptable classification result has been obtained with a certain setup of the GP model using the data from 3 sensors, a discussion concerning the reduction of the number of sensors while ensuring the classification result is conducted.

Based on the results obtained in 5.1, the model configuration with mother 557 wavelet C5, 256 DWT coefficients, Logistic likelihood function, VB inference 558 method and 40 iterations is maintained. The pertinence of data from three sensors 559 at different locations to the classification result is investigated. Data from three 560 sensors are used for training and testing of the GP model independently. Results 561 from the three GP models are compared between each other and also with the 562 results with all data from sensor 1, 2 and 3, as shown in figure 13. It shows that 563 with data from all three sensors the GP model achieves the best result in the current 564 study. However, with data only from sensor 1, the classification accuracy can be 565 100%, but it should be noted that as there exist several testing points so close to 566 the threshold in both classes, they could probably be misclassified. With data only 567 from sensor 3, at least 2 point among 81 are misclassified, but with data only from 568 sensor 2 located at the diagonal of the actuator, the result is much worse where at 569 least 6 testing points are misclassified. 570

In this section, Gaussian Process is evaluated by the data base collected through sensors attached on the sandwich plate. 70% of the database is used

for training and the rest 30% is used for testing. Several factors are evaluated 573 successively and it is found that: to optimize hyperparameters during the training 574 step, the more iterations, the better the results; during the signal processing and 575 feature extraction, the mother wavelet Coiflet 5 in DWT is outperforming other 576 mother wavelets; in the whole GP, the combination of Logistic function and Varia-577 tional Bayesian inference method is outstanding compared to other combinations; 578 Reducing the amount of data by DWT will result in a slight loss of accuracy of 579 the predictive mean value, but it can greatly reduce the computation time while 580 ensuring the accuracy of classification, which is worthwhile for processing big data. 581 Therefore, a GP model with mother wavelet C5, 256 DWT coefficients, Logistic 582 likelihood function, VB inference method and 40 iterations is adopted in this study. 583 The corresponding predictive mean values for healthy and damaged structure are 584 0.800 and -0.870, respectively. As for the impact of the number of sensors, the 585 result shows that data from sensor 1 and sensor 3 are more pertinent than that from 586 sensor 2. It shows also that reducing of the number of sensors in the current study 587 will lead to worse results. 588

#### 589 6. Conclusions

This paper addresses the difficulty in constructing a database for structural 590 health monitoring of real composite structures and the inconvenience in conven-591 tional expertise-based SHM approaches. A data-driven approach GP for damage 592 detection in a composite sandwich plate by simulation approach is presented. Sev-593 eral factors that have impact on classification accuracy are investigated, including 594 the selection of mother wavelet during the signal processing and feature extraction 595 by DWT, the amount of data discarded by DWT, the likelihood function and infer-596 ence method that are used to make predictions, as well as iteration numbers in the 597 training step of GP model. Based on the present results, some conclusions can be 598 drawn as below: 599

- The proposed method is proven effective for crack-type damage detection in the studied composite sandwich plate.
- The selection of mother wavelet in discrete wavelet transform has an important impact on the classification accuracy. Coiflet 5 performs better than others for the classification of both healthy and damaged structure.
- Discarding the coefficients that have low amplitude in DWT can speed up the computation time and may not lead to major loss of information. The resulted reduction of classification accuracy is negligible.

- The likelihood function Logistic function and inference method Variational Bayesian perform better than other combinations in the present study.
- With more iterations, the classification is slightly better than with less iterations, which is consistent with common sense.
- Data from sensor 1 and sensor 3 are more pertinent than that from sensor 2.
   Reducing of the number of sensors in the current study will lead to worse
   results.
- The effectiveness of the proposed method is verified under simulated environmental noise.

Although the proposed approach was achieved based on simulation results, it is applicable for real experimental data. The same procedure of data collection, signal processing and the use of GP model can be conducted as for simulation data for the purpose of damage detection. This proposed method is capable to detect crack-type damages for a composite sandwich panel. It is expected to be suitable for damage detection of other kind of damages and for more complex structures.

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### 625 Data availability

The raw/processed data required to reproduce these findings cannot be shared at this time as the data also forms part of an ongoing study.

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#### 727 Figure Captions

- Figure 1: Example of a DWT for a signal collected at sensor 2 (on the diagonal of the actuator)
- Figure 2: Gaussian Process training step

- Figure 3: Gaussian Process testing step
- <sup>732</sup> Figure 4a: Geometry of the composite sandwich panel
- <sup>733</sup> Figure 4b: Numerical model of the composite sandwich panel

Figure 5: Composite sandwich models with crack damage in different positions: (a) in x direction  $x = \frac{L}{4}$ ,  $y = \frac{W}{4}$  (b) in x direction  $x = \frac{L}{4}$ ,  $y = \frac{W}{2}$  (c) in x direction  $x = \frac{L}{2}$ ,  $y = \frac{W}{4}$  (d) in x direction  $x = \frac{L}{2}$ ,  $y = \frac{W}{2}$  (e) in x direction  $x = \frac{3L}{4}$ ,  $y = \frac{3W}{4}$  (f) in y direction  $x = \frac{L}{2}$ ,  $y = \frac{W}{2}$ . 1 actuator (red) and 3 sensors (yellow) attached on the face-sheet.

Figure 6: Comparison of structural vibration responses of a healthy model
 and a model with crack damage to an excitation signal of frequency 8 kHz.

Figure 7: Comparison of DWT coefficients of the vibration responses in Figure 6

Figure 8: Influence of the selection of mother wavelet on the classificationaccuracy

Figure 9: Influence of the amount of data saved by DWT on the classification accuracy

Figure 10: Influence of likelihood function and inference method on the classification accuracy

Figure 11: Influence of iteration numbers to optimize hyperparameters during
 the training step on the classification accuracy

Figure 12: Comparison of classification result based on (a) noise-free data and (b) data with noise

Figure 13: Investigation of the pertinence of three different sensors to the classification result. Classification using data only from sensor 1 (a), data only from sensor 2 (b), data only from sensor 3 (c) and data from sensor 1-3 (d)





Optimization



Raw data

























