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Hyperspectral remote sensing of shallow waters: considering environmental noise and bottom intra-class spectral variability for modeling and inversion of water reflectance

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Abstract

Hyperspectral remote sensing is now an established tool to determine shallow water properties over large areas, usually by inverting a semi-analytical model of water reflectance. However, various sources of error may make the observed subsurface remote-sensing reflectance deviate from the model, resulting in an increased retrieval error when inverting the model based on classical least-squares fitting. In this paper, we propose a probabilistic forward model of shallow water reflectance variability that describes two of the main sources of error, namely, (1) the environmental noise that includes every source of above-water variability (e.g., sensor noise and rough water surface), and (2) the potentially complex inherent spectral variability of each benthic class through their associated spectral covariance matrix. Based on this probabilistic model, we derive two inversion approaches, namely, MILE (Maximum Likelihood estimation including Environmental noise) and MILEBI (Maximum Likelihood estimation including Environmental noise and Bottom Intra-class variability) that utilize the information contained in the proposed covariance matrices to further constrain the inversion while allowing the observation to differ from the model in the less reliable wavebands. In this paper, MILE and MILEBI are compared with the widely used least-squares (LS) criterion in terms of depth, water clarity and benthic cover retrievals. For these three approaches, we also assess the influence of constraining bottom mixture coefficients to sum to one on

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estimation results.

The results show that the proposed probabilistic model is a valuable tool to investigate the influence of bottom intra-class variability on subsurface reflectance, e.g., as a function of optical depth or sensor noise. As expected, this influence is critical in very optically shallow waters, and decreases with increasing optical depth. The inversion results obtained from synthetic and airborne data of Quiberon Peninsula, France, show that MILE and MILEBI generally provide better performances than LS. For example, in the case of airborne data with depth ranging from 0.44 to 12.00 m, the bathymetry estimation error decreases by about 32% when using MILE and MILEBI instead of LS. Estimated maps of bottom cover are also more consistent when derived using sum-to-one constrained versions of MILE and MILEBI. MILE is shown to be a simple but powerful method to map simple benthic habitats with negligible influence of intra-class variability. Alternatively, MILEBI is to be preferred if this variability cannot be neglected, since taking bottom covariance matrices into account concurrently with mean reflectance spectra may help the bottom discrimination, e.g., in the presence of overlapping classes. This study thus shows that taking potential sources of error into account through appropriate parameterizations of spectral covariance may be critical to improve the remote sensing of shallow waters, hence making MILE and MILEBI interesting alternatives to LS.

Keywords: Bottom intra-class variability, Environmental noise, Maximum likelihood estimation, Radiative transfer model inversion, Shallow water hyperspectral remote sensing, Spectral covariance

1. Introduction

Optical remote sensing provides an outstanding opportunity to monitor aquatic environments from local to global scales, potentially offering high temporal and spatial resolutions, e.g., as allowed by recent advances in unmanned aerial vehicles or by the Sentinel-2 mission developed by the European Space Agency within the “Copernicus” program (Aschbacher & Milagro-Pérez, 2012; Drusch et al., 2012). The use of such high spatial resolution data (i.e., less than a few dozen meters) is particularly critical for coastal and inland waters, e.g., to map heterogeneous benthic habitats (Mishra et al., 2006; Hedley et al., 2012b), to detect coral bleaching (Andréfouët et al., 2002; Hedley et al., 2012a) or to monitor small lakes and rivers (Joshi & D’Sa, 2015). As compared with the open ocean, coastal and inland waters

11 are generally more complex environments, whose remotely-sensed reflectance may be highly
12 variable due to simultaneous changes in bathymetry, water quality, bottom type, water sur-
13 face and atmospheric conditions. In shallow waters, the decoupling of these effects has been
14 shown to be more accurate when using hyperspectral data instead of multispectral data (Lee
15 & Carder, 2002; Lee et al., 2013). Indeed, a higher number of spectral bands as well as
16 an increased spectral resolution allow reducing confounding effects between optically-active
17 parameters, e.g., by detecting the subtle changes in reflectance that originate from narrow
18 absorption regions potentially present in bottom albedo (Kutser et al., 2003; Hochberg &
19 Atkinson, 2003; Hedley et al., 2012a; Botha et al., 2013).

20

21 In coastal environments, hyperspectral remote sensing methods that allow the simultane-
22 ous retrieval of bathymetry, water quality and benthic cover are usually based on a radiative
23 transfer model that describes how light propagates in water (Mobley, 1994). This inverse
24 problem is generally solved using either look-up tables (LUTs) or iterative optimization
25 (Dekker et al., 2011). In the first case, a spectral library corresponding to different combi-
26 nations of depth, water quality and benthic cover is pre-computed using an exact (Mobley,
27 1994) or approximated (Lee et al., 1998) radiative transfer model. For each image pixel,
28 the measured reflectance is then matched with the closest simulated spectrum in the LUT.
29 CRISTAL (Comprehensive Reflectance Inversion based on Spectrum matching and TABLE
30 Lookup) (Mobley et al., 2005) and ALLUT (Adaptive Linearized Look-Up Trees) (Hedley
31 et al., 2009) as denoted by Dekker et al. (2011) are examples of such approaches. The inverse
32 problem can also be solved by numerically optimizing a cost function that relates measured
33 and simulated reflectance spectra. In this case, the forward model used for simulation has
34 to be sufficiently fast to permit multiple runs for each image pixel. To this end, a number of
35 analytical and semi-analytical models have been developed under various assumptions and
36 water types (Maritorena et al., 1994; Lee et al., 1998; Albert & Mobley, 2003). These models
37 approximate the radiative transfer equation and generally simulate the reflectance of shal-
38 low waters as a function of sun-sensor geometry, depth, bottom albedo and water-column
39 inherent optical properties (i.e., absorption and scattering properties of the water column).
40 Note that, whenever possible, the latter can further be related to specific inherent optical

41 properties and concentrations of optically-active water constituents (Brando et al., 2009).

42

43 Due to its accurate performance and simplicity, the Euclidean distance has generally been
44 used to assess the goodness-of-fit between the observation and the model, either when using
45 LUTs (Mobley et al., 2005; Hedley et al., 2009, 2012a) or iterative optimization (Lee et al.,
46 1999, 2001; Lee & Carder, 2002; Albert & Gege, 2006; Klonowski et al., 2007; Dekker et al.,
47 2011; Jay et al., 2012; Giardino et al., 2012; Garcia et al., 2014a; McKinna et al., 2015; Jay
48 & Guillaume, 2016). Note that in the case of iterative optimization, the use of Euclidean dis-
49 tance for model inversion corresponds to nonlinear unweighted least-squares fitting. However,
50 this cost function does not fully consider the information contained in the reflectance data.
51 In particular, it does not utilize spectral covariance (i.e., covariance between wavebands), yet
52 such knowledge of the data structure may be useful to improve the retrieval accuracy due to
53 the non-negligible correlation between hyperspectral bands (Gillis et al., 2013).

54

55 Importantly, as the least-squares method tries to find the best possible fit between the
56 observation and the model, it is not designed to handle possible deviations between them.
57 For example, the “environmental noise equivalent reflectance difference” (Brando & Dekker,
58 2003) (hereafter called environmental noise and denoted $NE\Delta r_E$) may lead the measured
59 subsurface reflectance to strongly differ from the modeled one. For a given spectral band,
60 $NE\Delta r_E$ corresponds to the reflectance standard deviation as estimated over an “as homoge-
61 neous as possible” water area. As a result, it not only takes into account the sensor noise, but
62 also scene-specific above-water variability, including atmospheric variability, effects related
63 to the rough water surface, refractions of diffuse and direct sunlight, and residuals from im-
64 perfect atmospheric, air-water interface and sun glint corrections (Brando & Dekker, 2003;
65 Brando et al., 2009; Botha et al., 2013). To consider such errors within model inversion,
66 Brando et al. (2009) and Botha et al. (2013) have weighted the contribution of each wave-
67 band according to the inverse of $NE\Delta r_E$. In doing so, the influence of the noisiest and least
68 accurate spectral bands is reduced, which lowers the estimation variance.

69

70 Another important source of error between the measured and simulated spectra is the

71 inherent spectral variability of each considered benthic class. Based on PlanarRad simu-
72 lations and a comprehensive bottom spectral library, Hedley et al. (2012b) have actually
73 demonstrated that this is one of the primary limiting factors for benthic mapping purposes
74 (whereas sensor noise is only a minor factor). Indeed, while a single mean reflectance spec-
75 trum is generally used to characterize the spectral response of each benthic class, many
76 authors show that such intrinsic variability may sometimes be greater than the mean re-
77 flectance itself, either at the local or global scales (Hochberg et al., 2003; Mobley et al., 2005;
78 Hedley et al., 2012b; Petit et al., 2017). Therefore, this variability may strongly affect the re-
79 trieval accuracy if it is not (or not properly) taken into account during the inversion process.
80 To this end, assuming that the bottom reflectance spectrum only varies according to a single
81 multiplicative factor across all the wavebands, several authors have proposed to estimate this
82 factor for each possible substrate (Lee et al., 1999; Fearn et al., 2011; Garcia et al., 2014b;
83 Petit et al., 2017). Under the same assumption, using the Spectral Angle Mapper (SAM) as
84 a cost function may also decrease the detrimental influence of bottom intra-class variability,
85 since the SAM is insensitive to variations in the global reflectance magnitude (Brando et al.,
86 2009; Botha et al., 2013; Petit et al., 2017). However, this spectral variability cannot always
87 be reliably represented using a single multiplicative factor (Hochberg et al., 2003; Hedley
88 et al., 2012b), thus making the development of alternative inversion methods highly desirable.

89

90 In this study, we first propose a realistic probabilistic model of shallow water reflectance
91 variability based on the semi-analytical model of Lee et al. (1998) and that fully describes
92 the influences of environmental noise and bottom intra-class variability. Both sources of
93 error are considered to be Gaussian and characterized by a mean vector and a spectral
94 covariance matrix. Then, using this modeling, we develop two new inversion approaches
95 based on maximum likelihood estimation that enable a pixelwise retrieval of all optically-
96 active parameters, i.e., bathymetry, water clarity parameters and benthic cover. These two
97 approaches are compared with the classical least-squares method using both simulated and
98 airborne data.

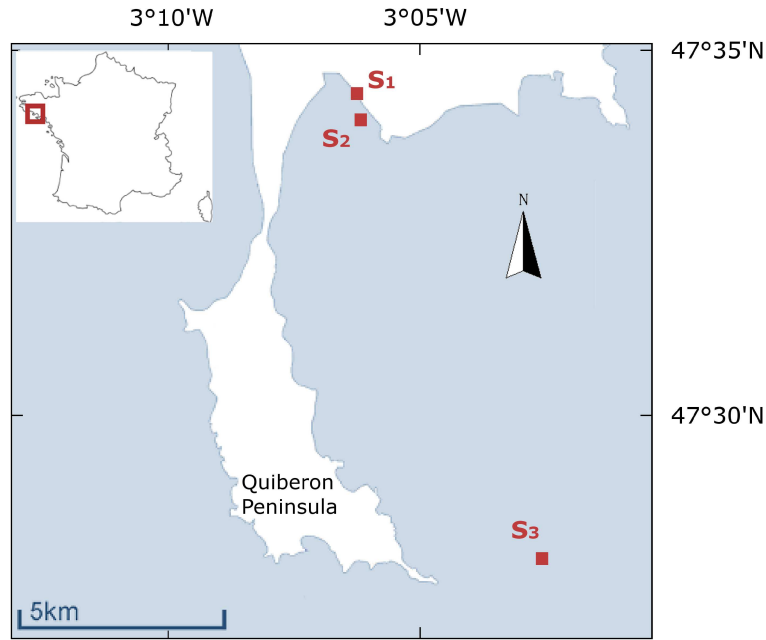


Figure 1: Location of the three study sites S_1 , S_2 and S_3 .

99 **2. Data**

100 *2.1. Study area*

101 As shown in Fig. 1, the overall study area is located in the Quiberon Bay on the French
 102 west coast (around $47^{\circ}31'N$, $3^{\circ}05'W$). Three sites (hereafter denoted S_1 , S_2 and S_3) were
 103 chosen in order to include a large bathymetric range and various bottom covers. Site S_1
 104 and Site S_2 are located near the shore in the Bay of Plouharnel ($47^{\circ}34'46''N$, $3^{\circ}06'24''W$),
 105 and are characterized by relatively shallow waters (less than 5 m at the time of acquisitions)
 106 and heterogeneous bottom covers including sand, brown algae, seagrasses and oyster farming
 107 structures. Site S_3 is located a few kilometers away from the Quiberon peninsula ($47^{\circ}28'11''N$,
 108 $3^{\circ}02'18''W$) and is characterized by a large bathymetric range (from 4 to 12 m at the time
 109 of acquisitions) and a nearly uniform sandy bottom.

110 *2.2. Image acquisition and preprocessing*

111 Eight hyperspectral images were acquired on September 14-18, 2010 around solar noon
 112 (the solar zenith angle being close to 50°) using an airborne Hypspec VNIR-1600 push-broom
 113 camera (Norsk Elektro Optikk, Norway). The flight altitude was 650 m, resulting in a 0.5 m
 114 spatial resolution. The camera acquired successive lines of 1600 pixels and 160 spectral bands

115 ranging from 410 to 987 nm. The spectral sampling interval and full width at half maxi-
116 mum were 3.7 nm and 4.5 nm respectively. Only 105 bands in the 410-800 nm domain were
117 kept when removing the strong water and oxygen absorption regions. Further, a three-band
118 aggregate was performed similarly to the PRISM instrument developed by the Jet Propul-
119 sion Laboratory (Mouroulis et al., 2014), therefore leading to a 11 nm sampling interval (35
120 bands). This allows us to enhance the signal-to-noise ratio while keeping similar estimation
121 results (Hochberg & Atkinson, 2003; Garcia et al., 2015).

122

123 After conversion to spectral radiance, images were geometrically corrected using ground-
124 based targets whose positions had been measured using a real-time kinematic GPS. Images
125 were then geolocated, the estimated georeferencing accuracy not exceeding one pixel at the
126 sea level. Atmospheric correction was performed using the ATCOR model (Richter, 2012).
127 A set of multiplicative factors (one for each spectral band) were derived comparing ATCOR
128 apparent reflectance spectra and ground-based spectro-radiometric measurements of above-
129 water reference targets (colored tarpaulins) placed on the nearby beach (Clark et al., 2002).
130 These factors were finally applied to the entire images in order to correct residuals from the
131 radiative transfer algorithm and to obtain the reflectance images. Note that some results of
132 atmospheric correction have already been presented by Jay & Guillaume (2016). Sun glint
133 (Hedley et al., 2005) and the air/water interface (Lee et al., 1999) were corrected in order
134 to finally obtain the subsurface remote-sensing reflectance $r(\lambda)$ (in sr^{-1}). For each day of
135 acquisition, the environmental noise $\text{NE}\Delta r_E$ (in sr^{-1}) (Brando & Dekker, 2003) was estimated
136 over optically deep waters according to the methodology proposed by Wettle et al. (2004).
137 As shown in Fig. 2, its spectral shape is similar to those obtained in previous studies (Brando
138 et al., 2009; Wettle et al., 2004), i.e., $\text{NE}\Delta r_E$ is nearly constant across all wavebands and
139 mainly increases in the blue domain, where the sensitivity of the CCD sensor is the lowest
140 and spectral variations in incident light are the strongest.

141 2.3. Data used for depth and phytoplankton concentration estimations

142 The eight hyperspectral images were used to evaluate the accuracy of bathymetry re-
143 trieval. For each image, the depth was only known in a few $6 \times 6 \text{ m}^2$ flat sandy-bottom areas

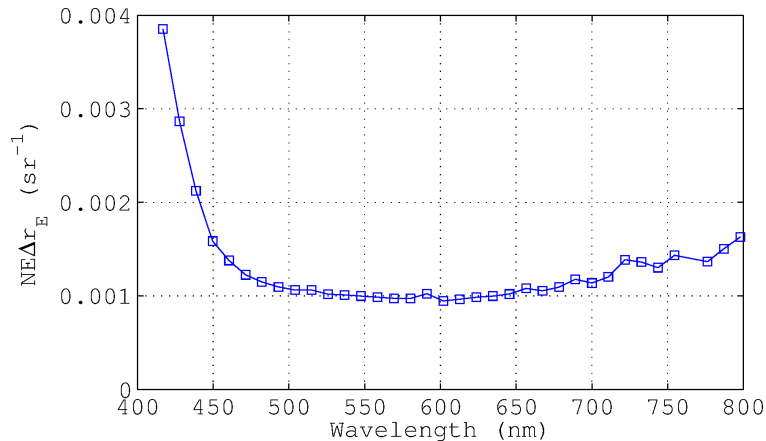


Figure 2: Environmental noise as measured on September 18, 2010.

144 thanks to sonar measurements and a tide model. A total of 14 validation points (depth
 145 ranging from 0.44 to 12 m) were therefore available to assess the accuracy of bathymetry
 146 estimation.

147 In addition, phytoplankton concentration was also measured concurrently with most airborne
 148 acquisitions in Site S₃. To do so, water samples were collected at the surface and bottom
 149 (whose depth ranged from 4.70 to 12 m) levels to better account for a possible vertical gra-
 150 dient in phytoplankton concentration. Chlorophyll-a and pheopigment concentrations were
 151 measured according to the French standard NF T 90117 (AFNOR, December 1999). Surface
 152 and bottom phytoplankton concentrations were then given by the sum of chlorophyll-a and
 153 pheopigment concentrations, and averaged so as to obtain a single measurement for each
 154 sampled area. These mean values were finally used to derive the absorption coefficient of
 155 phytoplankton at 440 nm (denoted P , in m^{-1}) similarly to Lee et al. (1999). In total, 8 vali-
 156 dation points (phytoplankton concentration ranging from 1.25 to 1.95 $\mu\text{g.L}^{-1}$, corresponding
 157 to P ranging from 0.069 to 0.093 m^{-1}) were available (still over $6 \times 6 \text{ m}^2$ flat sandy-bottom
 158 areas within which P was assumed to be homogeneous).

159 Note that no data were available to assess the retrievals of the other optically-active wa-
 160 ter constituents, namely, colored dissolved organic and detrital matter as well as suspended
 161 matter (see Section 3.1.1).

162 2.4. Data used for bottom cover estimation

163 The above eight images were also used to assess bottom cover estimation over the 14
 164 $6 \times 6 \text{ m}^2$ flat sandy-bottom areas of known depth. In addition, one of these images was

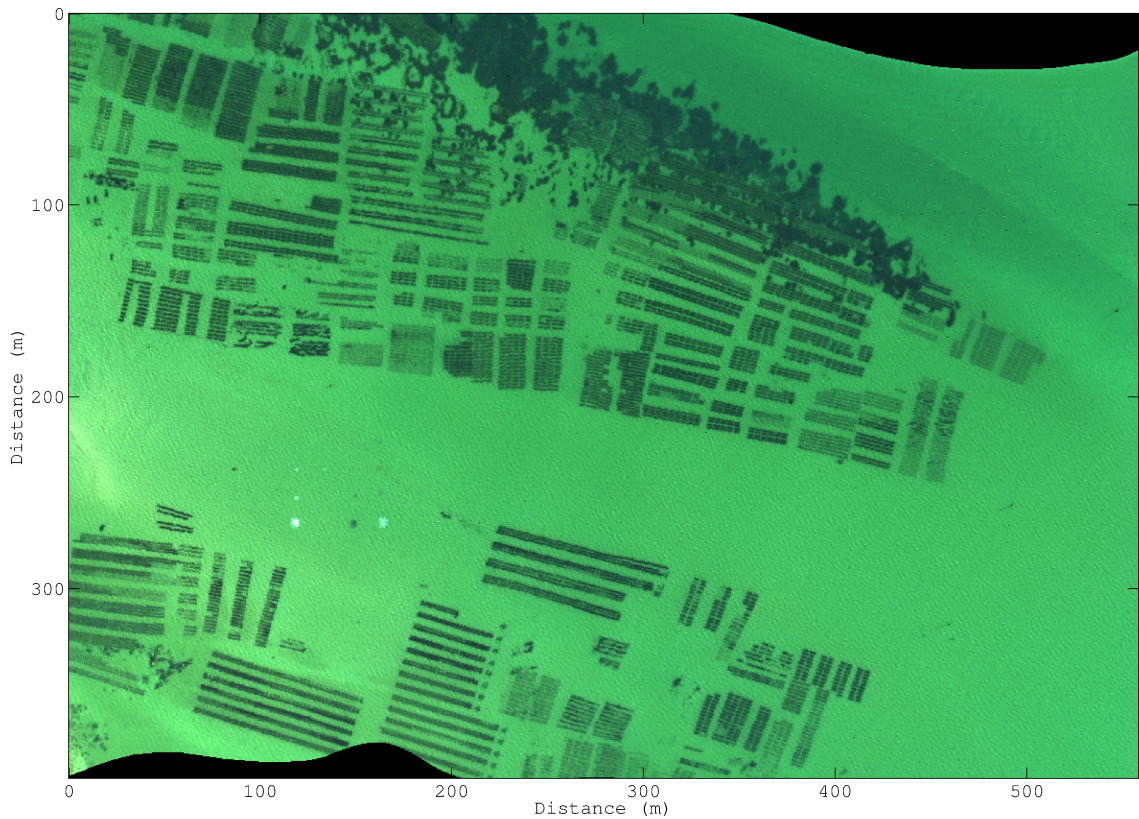


Figure 3: True color composite image derived from the deglinted subsurface hyperspectral image that was used to assess bottom cover estimation.

165 used to assess the tested methods over more complex bottom covers (Fig. 3). This image
 166 was acquired over a 0.22 km² area located in site S₂. This shallow area was part of a large
 167 oyster farming area and was thus relatively heterogeneous, both in terms of bottom cover and
 168 bathymetry (the depth ranged from about 1 m in the left-hand part to 5 m in the top-right
 169 part, with locally sharp changes in bathymetry due to the presence of oyster racks). Various
 170 bottom types were identified in this area. Numerous oyster racks were present on a mostly
 171 sandy bottom. Some of these wooden structures were empty (e.g., in the upper left part of
 172 the image), but most of them were full of oyster bags at the time of acquisition. Depending
 173 on when these bags had been put on racks, they could partly or completely be covered with
 174 green algae and/or brown algae. Lastly, there was a large seagrass meadow in the upper right
 175 part of the image, as well as small patches of brown algae irregularly distributed within the
 176 image (e.g., between oyster racks in the lower left part). Note that the colored tarpaulins
 177 present on the left-hand side (in the middle of which depth was 2.83 m) were ignored in this
 178 study.

179 For each bottom class and based on expert knowledge, numerous endmember spectra were

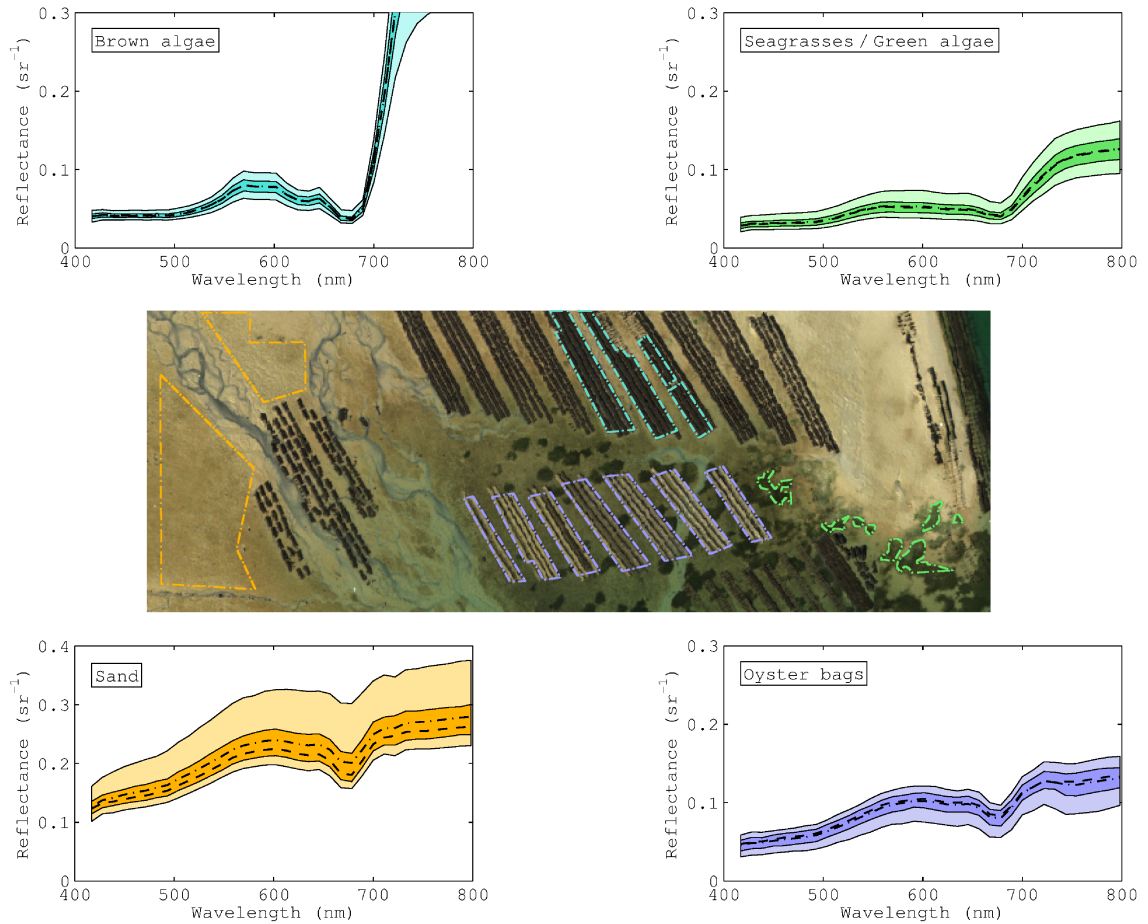


Figure 4: Reflectance distributions of sand, oyster bag, seagrass/green algae and brown algae classes as estimated from the areas emphasized in the airborne hyperspectral image shown in the middle. For each plot, the darkest and brightest shades correspond to the 25-75% and 5-95% quantiles resp., whereas the median and mean spectra are indicated by dashed and dash-dot lines resp..

180 extracted from supplementary hyperspectral images acquired over the neighboring zones in
 181 Site S₂ during low tide (Fig. 4). It is worth mentioning that, due to intra-class variability
 182 and because these zones are a few hundred meters to a dozen kilometers from the zones used
 183 to assess the inversion methods (Fig. 1), the extracted endmember spectra may not perfectly
 184 match those encountered in the whole study area. Selecting reflectance spectra of emerged
 185 substrates directly from the remote-sensing images allowed us to avoid potential issues of
 186 intercalibration between airborne and ground-based sensors. However, note that, since empty
 187 wooden structures were too thin to fill entirely the $0.5 \times 0.5 \text{ m}^2$ pixels of hyperspectral images,
 188 they were not included as a possible endmember. Further, green algae and seagrasses were
 189 grouped into a single class corresponding to green vegetation elements. Four bottom classes
 190 were thus used, namely sand, oyster bags, brown algae and seagrasses/green algae (note that
 191 these surfaces were assumed to be Lambertian). The corresponding reflectance distributions

192 were estimated based on 150 to 3,000 image spectra, and all show some intra-class variability
 193 around the mean reflectance spectra (Fig. 4). Such variability may be due, e.g., to the bottom
 194 chemistry itself (e.g., variations in chlorophyll content in seagrasses/green algae) or to the
 195 bottom 3-D arrangement that may make the illumination conditions within the surface highly
 196 variable (Manolakis et al., 2003). Given the similar magnitudes of brown alga, seagrass/green
 197 alga and, to a lesser extent, oyster bag mean reflectance spectra, such variability potentially
 198 makes the identification of these three partially overlapping classes quite difficult.

199 3. Methodology

200 3.1. Forward modeling of subsurface remote-sensing reflectance

201 3.1.1. Bio-optical modeling

In this study, we use the semi-analytical model $\tilde{r}(\lambda)$ developed by Lee et al. (1998, 1999) to express the subsurface remote-sensing reflectance as measured from nadir as a function of depth H (in m), bottom albedo $\rho_b(\lambda)$ (unitless), total absorption and backscattering properties of the water column $a(\lambda)$ and $b_b(\lambda)$ resp. (in m^{-1}), and subsurface solar zenith angle θ_s (in $^\circ$):

$$\tilde{r}(\lambda) = r_\infty(\lambda) \left(1 - e^{-(k_d(\lambda) + k_u^c(\lambda))H}\right) + \frac{\rho_b(\lambda)}{\pi} e^{-(k_d(\lambda) + k_u^b(\lambda))H} \quad (1)$$

202 where the subsurface remote-sensing reflectance of optically-deep water $r_\infty(\lambda)$ (in sr^{-1}) and
 203 attenuation coefficients $k_d(\lambda)$, $k_u^c(\lambda)$ and $k_u^b(\lambda)$ (in m^{-1}) are related to $a(\lambda)$, $b_b(\lambda)$ and θ_s by:

$$r_\infty(\lambda) = \left(0.084 + 0.17 \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)}\right) \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)} \quad (2)$$

$$k_d(\lambda) = \frac{a(\lambda) + b_b(\lambda)}{\cos \theta_s} \quad (3)$$

$$k_u^b(\lambda) = 1.04(a(\lambda) + b_b(\lambda)) \left(1 + 5.4 \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)}\right)^{0.5} \quad (4)$$

$$k_u^c(\lambda) = 1.03(a(\lambda) + b_b(\lambda)) \left(1 + 2.4 \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)}\right)^{0.5}. \quad (5)$$

204 Eq. (1) to Eq. (5) have been used and validated in numerous studies dealing with shallow
 205 water remote sensing over a wide range of coastal waters (Lee et al., 1999, 2001; Klonowski

206 et al., 2007; Goodman et al., 2008; Brando et al., 2009; Hedley et al., 2009; Dekker et al.,
 207 2011; Fearnings et al., 2011; Garcia et al., 2014a; Jay & Guillaume, 2014; McKinna et al.,
 208 2015; Jay & Guillaume, 2016; Petit et al., 2017). In the absence of *in-situ* measurements of
 209 inherent optical properties to develop a site-specific bio-optical model, the total absorption
 210 and backscattering coefficients are given by the sum of the contributions of optically-active
 211 water constituents and parameterized according to the generic expressions of Lee et al. (1998)
 212 and Dekker et al. (2011):

$$a(\lambda) = a_w(\lambda) + [a_0(\lambda) + a_1(\lambda) \ln P] P + Ge^{-0.015(\lambda-440)} \quad (6)$$

$$b_b(\lambda) = b_{b,w}(\lambda) + X \left(\frac{550}{\lambda} \right)^{0.5} \quad (7)$$

where $a_w(\lambda)$ and $b_{b,w}(\lambda)$ (in m^{-1}) are the pure water absorption and backscattering coefficients (Buiteveld et al., 1994; Morel, 1974), $a_0(\lambda)$ and $a_1(\lambda)$ (unitless) are empirical spectra tabulated by Lee et al. (1998), P (in m^{-1}) is the absorption coefficient of phytoplankton at 440 nm, G (in m^{-1}) is the absorption coefficient of colored dissolved organic and detrital matter at 440 nm, and X (in m^{-1}) is the particle backscattering coefficient at 550 nm. The above parameterizations of absorption coefficients of phytoplankton and colored dissolved organic and detrital matter have been shown to be sufficiently accurate over a wide range of coastal waters (Lee et al., 1999, 2001; Lee & Carder, 2002; Goodman et al., 2008; Hedley et al., 2009; Dekker et al., 2011; Hedley et al., 2012a; Jay & Guillaume, 2014, 2016). Note also that the power law exponent used to model particle backscattering was set to -0.5, which is adequate for normal to more turbid coastal waters (Lee et al., 2001).

In this study, given the high spatial resolution of considered images (0.5 m), the bottom albedo is parameterized using a linear combination of only two pure substrates similarly to Brando et al. (2009) and Hedley et al. (2009):

$$\rho_b(\lambda) = B_1\rho_{b,1}(\lambda) + B_2\rho_{b,2}(\lambda) \quad (8)$$

213 where $\rho_{b,1}(\lambda)$ and $\rho_{b,2}(\lambda)$ are two known substrate albedos (e.g., obtained from ground-based
 214 measurements or a generic spectral library). The scalars B_1 and B_2 (unitless) may represent

215 the fractional covers of both substrates within the considered pixel, so in this case, only one
 216 bottom coefficient B is required, i.e., $B_1 = B$, $B_2 = 1 - B$ and $0 \leq B \leq 1$ (Klonowski et al.,
 217 2007; Goodman & Ustin, 2007; Brando et al., 2009; Hedley et al., 2009, 2012a). Alterna-
 218 tively, Fearn et al. (2011) and Garcia et al. (2014b) used a mixture of benthic reflectances
 219 normalized at 550 nm, and they estimated the relative brightness of each substrate without
 220 imposing any constraint on the mixture coefficients to be retrieved. In this case, a single
 221 multiplicative factor is used to model both the fractional cover and the brightness (or magni-
 222 tude) of each substrate. Although the sum-to-one constraint applies for the fractional cover,
 223 the brightness of substrate $\rho_{b,1}$ is independent from that of substrate $\rho_{b,2}$. As a result, the
 224 mixture coefficients B_1 and B_2 are independent and do not necessarily sum to one. It is worth
 225 noting that, even though such a modeling enables the magnitudes of $\rho_{b,1}$ and $\rho_{b,2}$ to vary,
 226 it also adds an extra degree of freedom during the inversion process. This may increase the
 227 estimation noise and require post-processing steps in order to smooth estimated maps, e.g.,
 228 using median filtering (Fearn et al., 2011). In the following, we test these two approaches
 229 in order to assess the impact of the sum-to-one constraint on estimation performance.

230 3.1.2. Probabilistic modeling

As widely accepted in the community (Jay & Guillaume, 2011; Hedley et al., 2012a;
 Jay et al., 2012; Gillis et al., 2013; Garcia et al., 2014b; Jay & Guillaume, 2014; Knudby
 et al., 2016), the measured subsurface remote-sensing reflectance, denoted in vector form
 $\mathbf{r} = [r(\lambda_1), \dots, r(\lambda_L)]^t$ (where L is the number of wavebands), is assumed to follow a mul-
 tivariate Gaussian distribution with mean $\boldsymbol{\mu} = \mathbb{E}[\mathbf{r}]$ and spectral covariance matrix $\boldsymbol{\Gamma} =$
 $\mathbb{E}[(\mathbf{r} - \mathbb{E}(\mathbf{r}))(\mathbf{r} - \mathbb{E}(\mathbf{r}))^t]$. The mean vector is parameterized using the bio-optical model
 presented in Section 3.1.1, which may be written in matrix notation as

$$\boldsymbol{\mu}(\boldsymbol{\Delta}) = (\mathbb{I} - \mathbf{K}_c)\mathbf{r}_\infty + \mathbf{K}_b \left(B_1 \frac{\boldsymbol{\rho}_{b,1}}{\pi} + B_2 \frac{\boldsymbol{\rho}_{b,2}}{\pi} \right) \quad (9)$$

231 where $\boldsymbol{\Delta} = [H, P, G, X, B_1, B_2]^t$, $\mathbf{r}_\infty = [r_\infty(\lambda_1), \dots, r_\infty(\lambda_L)]^t$, \mathbb{I} is the $L \times L$ identity matrix,
 232 $\mathbf{K}_c = \text{diag} \left[e^{-(k_d(\lambda_i) + k_u^c(\lambda_i))H} \right]_{i \in \llbracket 1; L \rrbracket}$, $\mathbf{K}_b = \text{diag} \left[e^{-(k_d(\lambda_i) + k_u^b(\lambda_i))H} \right]_{i \in \llbracket 1; L \rrbracket}$, and $\boldsymbol{\rho}_{b,i} = [\rho_{b,i}(\lambda_1), \dots, \rho_{b,i}(\lambda_L)]^t$.

233

The different sources of deviations between the measured and simulated spectra can be modeled via an appropriate parameterization of \mathbf{I} . In the probabilistic modeling subsequently used within the proposed MILE (MaxImum Likelihood estimation including Environmental noise) inversion method (Section 3.2), we assume that the random variability around mean $\boldsymbol{\mu}(\Delta)$ can be described using the full spectral covariance matrix of the environmental noise, \mathbf{I}_{surf} , similarly to Hedley et al. (2012a), Garcia et al. (2014b) and Knudby et al. (2016). The subsurface remote-sensing reflectance is then modeled as

$$\mathbf{r} = \left[(\mathbb{I} - \mathbf{K}_c) \mathbf{r}_\infty + \mathbf{K}_b \left(B_1 \frac{\boldsymbol{\rho}_{b,1}}{\pi} + B_2 \frac{\boldsymbol{\rho}_{b,2}}{\pi} \right) \right] + \mathbf{n}_{surf} \quad (10)$$

234 where the random vector \mathbf{n}_{surf} follows a multivariate Gaussian distribution with zero mean
 235 and covariance matrix \mathbf{I}_{surf} . Note that, in real scenarios, \mathbf{I}_{surf} can be estimated over opti-
 236 cally deep waters similarly to $\text{NE}\Delta r_E$.

237

However, Eq. (10) only allows the bottom remote-sensing reflectances $(\boldsymbol{\rho}_{b,1}/\pi)$ and $(\boldsymbol{\rho}_{b,2}/\pi)$ to vary according to the multiplicative factors B_1 and B_2 . As an alternative to this usual bottom modeling, the proposed MILEBI (MaxImum Likelihood estimation including Environmental noise and Bottom Intra-class variability) probabilistic modeling uses a multivariate Gaussian distribution to describe the reflectance inherent variability of each benthic class. Due to the compromise offered between accuracy and mathematical tractability, the Gaussian modeling has been widely used to develop hyperspectral remote-sensing algorithms that must take into account the spread of each class of materials (and therefore potential overlaps between these classes) to obtain good performances, e.g., classification and target detection algorithms (Manolakis et al., 2003; Melgani & Bruzzone, 2004; Palmason et al., 2005). Preliminary tests (not shown here for the sake of brevity) demonstrated that, except for a small minority of samples corresponding to extreme data points, the bottom intra-class variabilities presented in Fig. 4 could indeed be reliably represented using multivariate Gaussian distributions. In this case, the subsurface remote-sensing reflectance can be modeled as

$$\mathbf{r} = \left\{ (\mathbb{I} - \mathbf{K}_c) \mathbf{r}_\infty + \mathbf{K}_b \left[B_1 (\boldsymbol{\mu}_{b,1} + \mathbf{n}_{b,1}) + B_2 (\boldsymbol{\mu}_{b,2} + \mathbf{n}_{b,2}) \right] \right\} + \mathbf{n}_{surf} \quad (11)$$

where $\boldsymbol{\mu}_{b,i}$ is the mean remote-sensing reflectance spectrum of bottom class i and $\mathbf{n}_{b,i}$ follows a multivariate Gaussian distribution with zero mean and covariance matrix $\boldsymbol{\Gamma}_{b,i}$. Separating deterministic terms from random terms in Eq. (11) leads to

$$\mathbf{r} = [(\mathbf{I} - \mathbf{K}_c)\mathbf{r}_\infty + \mathbf{K}_b (B_1\boldsymbol{\mu}_{b,1} + B_2\boldsymbol{\mu}_{b,2})] + [\mathbf{n}_{surf} + \mathbf{K}_b(B_1\mathbf{n}_{b,1} + B_2\mathbf{n}_{b,2})]. \quad (12)$$

The corresponding total covariance matrix is obtained by applying $\boldsymbol{\Gamma} = \mathbb{E}[(\mathbf{r} - \mathbb{E}(\mathbf{r}))(\mathbf{r} - \mathbb{E}(\mathbf{r}))^t]$ to Eq. (12) and by assuming that $\mathbf{n}_{b,1}$, $\mathbf{n}_{b,2}$ and \mathbf{n}_{surf} are independent:

$$\boldsymbol{\Gamma}(\boldsymbol{\Delta}) = \mathbf{K}_b [B_1^2\boldsymbol{\Gamma}_{b,1} + B_2^2\boldsymbol{\Gamma}_{b,2}] \mathbf{K}_b + \boldsymbol{\Gamma}_{surf}. \quad (13)$$

238 In Eq. (12), possible deviations between the observed subsurface remote-sensing reflectance
 239 \mathbf{r} and the model (left-hand term of the sum) are not only due to the environmental noise,
 240 but also to the intrinsic spectral variability of each benthic class. As expected, for the i^{th}
 241 class, the influence of this variability is proportional to B_i , and becomes negligible when
 242 depth and/or turbidity increase(s) (because of progressive attenuation by \mathbf{K}_b). Also, if $\boldsymbol{\Gamma}_{b,1}$
 243 and $\boldsymbol{\Gamma}_{b,2}$ perfectly describe the bottom intrinsic variabilities, the parameters B_1 and B_2 only
 244 represent fractional covers, so the sum-to-one constraint applies. In this case, the MILEBI
 245 probabilistic modeling disentangles the fractional cover (which is taken into account by a
 246 single multiplicative factor $B = B_1 = 1 - B_2$) from intra-class variabilities (which are taken
 247 into account through the bottom covariance matrices $\boldsymbol{\Gamma}_{b,1}$ and $\boldsymbol{\Gamma}_{b,2}$), which is not possible
 248 when using Eq. (10). Alternatively, relaxing the sum-to-one constraint may allow potential
 249 deviations from the assumed Gaussian modeling.

250 3.2. Inversion methods

In this study, various inversion methods are derived based on the above two probabilistic models of shallow water reflectance variability. All these inversion methods consist in maximizing the likelihood of observing \mathbf{r} given the set $\boldsymbol{\Delta}$ of water column parameters to be estimated. Under the Gaussian assumption, the likelihood is defined as

$$P(\mathbf{r}|\boldsymbol{\Delta}) = [(2\pi)^L |\boldsymbol{\Gamma}(\boldsymbol{\Delta})|]^{-1/2} e^{-\frac{1}{2}(\mathbf{r} - \boldsymbol{\mu}(\boldsymbol{\Delta}))^t \boldsymbol{\Gamma}(\boldsymbol{\Delta})^{-1} (\mathbf{r} - \boldsymbol{\mu}(\boldsymbol{\Delta}))}. \quad (14)$$

The maximum likelihood estimate $\widehat{\Delta}_{ML}(\mathbf{r})$ is the value of Δ that maximizes the likelihood:

$$\widehat{\Delta}_{ML}(\mathbf{r}) = \underset{\Delta}{\operatorname{argmax}} P(\mathbf{r}|\Delta). \quad (15)$$

In Eq. (14), the mean vector $\boldsymbol{\mu}(\Delta)$ is given by Eq. (9) for every tested inversion method.

The main difference between the methods actually lies in the parameterization of $\boldsymbol{\Gamma}(\Delta)$.

In MILE, $\boldsymbol{\Gamma}(\Delta) = \boldsymbol{\Gamma}_{surf}$ does not depend on Δ since it only characterizes the above-water variability. Eq. (14) can thus be simplified, and the MILE estimate $\widehat{\Delta}_{MILE}(\mathbf{r})$ is given by the minimum Mahalanobis distance between the measured and simulated spectra:

$$\widehat{\Delta}_{MILE}(\mathbf{r}) = \underset{\Delta}{\operatorname{argmin}} (\mathbf{r} - \boldsymbol{\mu}(\Delta))^t \boldsymbol{\Gamma}_{surf}^{-1} (\mathbf{r} - \boldsymbol{\mu}(\Delta)). \quad (16)$$

In MILEBI, $\boldsymbol{\Gamma}(\Delta)$ depends on Δ , so Eq. (14) cannot be further simplified:

$$\widehat{\Delta}_{MILEBI}(\mathbf{r}) = \underset{\Delta}{\operatorname{argmax}} \left\{ [(2\pi)^L |\boldsymbol{\Gamma}(\Delta)|]^{-1/2} e^{-\frac{1}{2}(\mathbf{r} - \boldsymbol{\mu}(\Delta))^t \boldsymbol{\Gamma}(\Delta)^{-1} (\mathbf{r} - \boldsymbol{\mu}(\Delta))} \right\} \quad (17)$$

where $\boldsymbol{\Gamma}(\Delta)$ is given by Eq. (13).

In this paper, MILE and MILEBI are compared to the widely used least-squares (LS) method. Note that the LS estimate can also be obtained by maximizing the likelihood in Eq. (14), taking $\boldsymbol{\Gamma} = \sigma^2 \boldsymbol{I}$ where σ is a positive real number and \boldsymbol{I} is the $L \times L$ identity matrix (i.e., uncertainties of all spectral bands are assumed to be uncorrelated and of equal variances). The LS estimate $\widehat{\Delta}_{LS}(\mathbf{r})$ is given by the minimum Euclidean distance between the measured and simulated spectra:

$$\widehat{\Delta}_{LS}(\mathbf{r}) = \underset{\Delta}{\operatorname{argmin}} (\mathbf{r} - \boldsymbol{\mu}(\Delta))^t (\mathbf{r} - \boldsymbol{\mu}(\Delta)). \quad (18)$$

251 Comparing Eq. (16), Eq. (17) and Eq. (18) shows that, unlike LS, MILE and MILEBI utilize
 252 the information contained in the spectral covariance matrix to further constrain the inversion.
 253 In addition, both methods allow some deviations between the measured and simulated spectra
 254 by giving the less reliable wavebands little weights in the cost function. For MILE, these are
 255 located in the domains of strong environmental noise. For MILEBI, these wavebands not

Table 1: Methods compared in this study and derived from the likelihood function presented in Eq. (14). Subscript “S21” indicates the use of the sum-to-one constraint.

Method	Δ	$\mu(\Delta)$	$\Gamma(\Delta)$
LS _{S21}	$[H, P, G, X, B]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B \frac{\rho_{b,1}}{\pi} + (1 - B) \frac{\rho_{b,2}}{\pi} \right)$	$\sigma^2 \mathbb{I}$
MILE _{S21}	$[H, P, G, X, B]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B \frac{\rho_{b,1}}{\pi} + (1 - B) \frac{\rho_{b,2}}{\pi} \right)$	Γ_{surf}
MILEBI _{S21}	$[H, P, G, X, B]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B \frac{\rho_{b,1}}{\pi} + (1 - B) \frac{\rho_{b,2}}{\pi} \right)$	$\mathbf{K}_b [B^2 \Gamma_{b,1} + (1 - B)^2 \Gamma_{b,2}] \mathbf{K}_b + \Gamma_{surf}$
LS	$[H, P, G, X, B_1, B_2]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B_1 \frac{\rho_{b,1}}{\pi} + B_2 \frac{\rho_{b,2}}{\pi} \right)$	$\sigma^2 \mathbb{I}$
MILE	$[H, P, G, X, B_1, B_2]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B_1 \frac{\rho_{b,1}}{\pi} + B_2 \frac{\rho_{b,2}}{\pi} \right)$	Γ_{surf}
MILEBI	$[H, P, G, X, B_1, B_2]$	$(\mathbb{I} - \mathbf{K}_c)r_\infty + \mathbf{K}_b \left(B_1 \frac{\rho_{b,1}}{\pi} + B_2 \frac{\rho_{b,2}}{\pi} \right)$	$\mathbf{K}_b [B_1^2 \Gamma_{b,1} + B_2^2 \Gamma_{b,2}] \mathbf{K}_b + \Gamma_{surf}$

only correspond to the domains of strong environmental noise, but also to the domains of strong bottom intrinsic variabilities.

Implementing MILE, MILEBI and LS with or without the sum-to-one constraint on bottom mixture coefficients results in the six methods summarized in Table 1. Note that other cost functions, such as SAM or least-squares on spectral derivative (Brando et al., 2009; Botha et al., 2013; Petit et al., 2017), could also be tested, since, for example, SAM may provide more accurate bathymetry retrieval than LS (Petit et al., 2017). We, however, only compared MILE, MILEBI and LS (1) in order to focus primarily on the influence of $\Gamma(\Delta)$ parameterization on the inversion, and (2) because LS generally offers a better tradeoff than SAM and least-squares on spectral derivative for accurately retrieving all the parameters at the same time (Petit et al., 2017).

3.3. Implementation of inversion methods

For the six methods presented in Table 1, the cost function was iteratively optimized using the trust-region reflective algorithm implemented in MATLAB[®] (version 8.0.0, The MathWorks Inc., Natick, MA, 2012) within the “lsqcurvefit” function. Lower and upper optimization bounds were similar to those found in the literature for turbid waters (Hedley et al., 2009; Garcia et al., 2014b, 2015), i.e., $0 \leq H \leq 30$ m, $0 \leq P \leq 0.5$ m⁻¹, $0 \leq G \leq 0.5$ m⁻¹, $0 \leq X \leq 0.08$ m⁻¹, $0 \leq B_1, B_2 \leq 1.5$ and $0 \leq B \leq 1$.

A special attention was given to the initialization step. While default parameter values (Lee et al., 2001; Klonowski et al., 2007; McKinna et al., 2015) or reflectance-derived values (Lee et al., 1999; Dekker et al., 2011; Jay & Guillaume, 2016) may be used as initial guesses, Garcia et al. (2014a,b) have shown that different initial guesses could lead to different local

279 minima and therefore different parameter estimates. This step may be more critical in the
 280 case of maximum likelihood estimation because considering spectrally-correlated noise may
 281 introduce more local minima in the parameter solution space (Garcia et al., 2014b). In this
 282 paper, we thus implemented a Latin Hypercube Sampling scheme as proposed by Garcia et al.
 283 (2014b) to generate preliminary LUTs containing 100,000 initial guesses and corresponding
 284 simulated reflectance spectra. Normal distributions were used for H , P , G and X , and uni-
 285 form distributions bounded by the above lower and upper bounds were used for B , B_1 and
 286 B_2 . Empirical values were used for means and standard deviations of normal distributions:
 287 means were set to 0, while standard deviations were set such that the value of the probability
 288 density function at half maximum corresponded to one-third of the upper bound (e.g., we
 289 used a standard deviation of 8.5 m for H). Only positive sets of parameters were then kept
 290 to build the LUTs. The use of such normal distributions allowed us to sample more finely the
 291 regions of the parameter space where the reflectance strongly varies with depth and water
 292 clarity parameters, namely, shallow waters and high water clarity (Hedley et al., 2009; Jay
 293 & Guillaume, 2016). For each measured spectrum to be inverted, the 100 sets of parameters
 294 corresponding to the 100 closest spectra in the LUT were averaged to provide a single initial
 295 guess for the iterative optimization process. In vegetation remote sensing, averaging multiple
 296 best solutions instead of retaining only the best one is known to increase the estimation
 297 accuracy when the inversion problem is ill-posed and/or the reflectance model is not fully
 298 accurate (Darvishzadeh et al., 2011; Verrelst et al., 2015; Jay et al., 2017).

299
 300 In this study, four substrates were identified as possible endmembers (Fig. 4). As only
 301 two of them could be used in the bottom reflectance model (Eq. (8)), we implemented the
 302 same type of approach as Brando et al. (2009), i.e., (1) each measured reflectance spectrum
 303 was inverted using each of the six possible pairs of substrates (note that this requires gener-
 304 ating six preliminary LUTs for initialization), and (2) these six pairs were sorted according to
 305 their $P(\mathbf{r}|\Delta)$ value. For similar reasons as for initialization and unlike Brando et al. (2009)
 306 who only retained the best pair (i.e., corresponding to the highest $P(\mathbf{r}|\Delta)$ value, P_{\max}), the
 307 solution was here obtained by averaging all pairs whose $P(\mathbf{r}|\Delta)$ values were sufficiently close
 308 to P_{\max} , i.e., within $n\%$ of P_{\max} . In the following, the value of n was investigated based on

309 simulated data (Section 4.2), testing $n = 0$ (i.e., only the best pair is retained), 1 and 2%.
310 The optimum value was then used for processing the airborne data (Section 4.3).

311

312 The four bottom intra-class covariance matrices used in MILEBI and MILEBI_{S21} were
313 estimated from hyperspectral images acquired at low tide, similarly to the mean reflectance
314 spectra (see Section 2.4). It is worth noting that inverting the covariance matrices detailed in
315 Table 1 requires (at least) as many samples (i.e., spectra) as spectral bands for $\mathbf{\Gamma}_{surf}$ and $\mathbf{\Gamma}_{b,i}$
316 estimations. The more samples we have, the more accurate the estimations. In this paper,
317 a minimum of 150 spectra (for oyster bag class) were used, this number being substantially
318 higher than the number of spectral bands (35).

319 3.4. Performance assessment

320 3.4.1. Simulated data

321 We conducted two series of simulations, each of which corresponded to a different model
322 to generate the synthetic data set. For the first data set, we used the probabilistic modeling
323 of Eq. (10), therefore assuming that the random variability is only described by $\mathbf{\Gamma}_{surf}$. The
324 influence of water column properties was studied at four depths, i.e., 1, 5, 10 and 20 m, and
325 intermediate water clarity as given by Garcia et al. (2015), i.e., $P = 0.1 \text{ m}^{-1}$, $G = 0.1 \text{ m}^{-1}$,
326 and $X = 0.01 \text{ m}^{-1}$. The bottom was given either as one of the four substrates shown in
327 Fig. 4, or as a 50%/50% mixture of two substrates, thus resulting in ten tested bottom spec-
328 tra. Note that intra-class variability was not simulated for this data set. We used the $\mathbf{\Gamma}_{surf}$
329 matrix that was estimated over optically deep waters from the airborne data set presented
330 in Section 2, the diagonal of $\mathbf{\Gamma}_{surf}$ being given as the square of $\text{NE}\Delta r_E$ shown in Fig. 2. The
331 sun-sensor geometry was identical to that used for airborne acquisitions, i.e., nadir viewing
332 and a solar zenith angle of 50° .

333 The second synthetic data set was generated using the probabilistic modeling of Eq. (12).
334 As compared with the first data set, the only difference related to the simulation of bottom
335 reflectance, which was here not only modeled using multiplicative factors, but also using ran-
336 dom vectors $\mathbf{n}_{b,1}$ and $\mathbf{n}_{b,2}$. These vectors were generated based on the intra-class covariance
337 matrices estimated from airborne data (see Section 3.3).

338 For each data set, the “mvnrnd” MATLAB function allowed us to generate 100 noise-
339 perturbed spectra for every depth and bottom reflectance, hence providing 4,000 simulated
340 spectra in total. These spectra were then inverted using the six methods and according to
341 the procedure described in Section 3.3. The estimation performances were evaluated in terms
342 of mean absolute error (MAE), which has proven to be a more reliable measure of error than
343 the classical root mean square error (Willmott & Matsuura, 2005).

344 *3.4.2. Airborne data*

345 The retrievals of bathymetry, absorption of phytoplankton at 440 nm and bottom cover
346 were also assessed using the airborne data set (Section 2). For each 6×6 m² flat sandy-bottom
347 area (thus containing 12×12 pixels), the semi-analytical model was inverted for each pixel
348 using the six methods, and estimated values of H , P and bottom coefficients were compared to
349 their actual values whenever possible. The six methods were also used to retrieve the bottom
350 cover for the image presented in Fig. 3, the estimated benthic habitats being qualitatively
351 evaluated by visual inspection.

352 **4. Results and discussion**

353 *4.1. Influences of environmental noise and bottom intra-class variability on subsurface re-* 354 *flectance*

355 A preliminary study was conducted to quantify the influences of environmental noise
356 and bottom intra-class variability on the measured subsurface reflectance, based on the total
357 covariance matrix presented in Eq. (13). Representing this matrix for the four depths in-
358 vestigated in the simulations (same water quality) and the four pure substrates presented in
359 Fig. 4 allows us to see how these two sources of error make the observation deviate from the
360 model (note that, if the bio-optical model in Eq. (9) would be perfect, the total covariance
361 matrix would be the zero matrix).

362 In the absence of water, the four bottom intra-class covariance matrices show quite different
363 patterns and magnitudes (Fig. 5). While, overall, sand and oyster bag variabilities steadily
364 increase with wavelength, brown algae and, to a lesser extent, seagrasses/green algae, show
365 lower variability in the blue and red domains due to the strong chlorophyll absorption leading

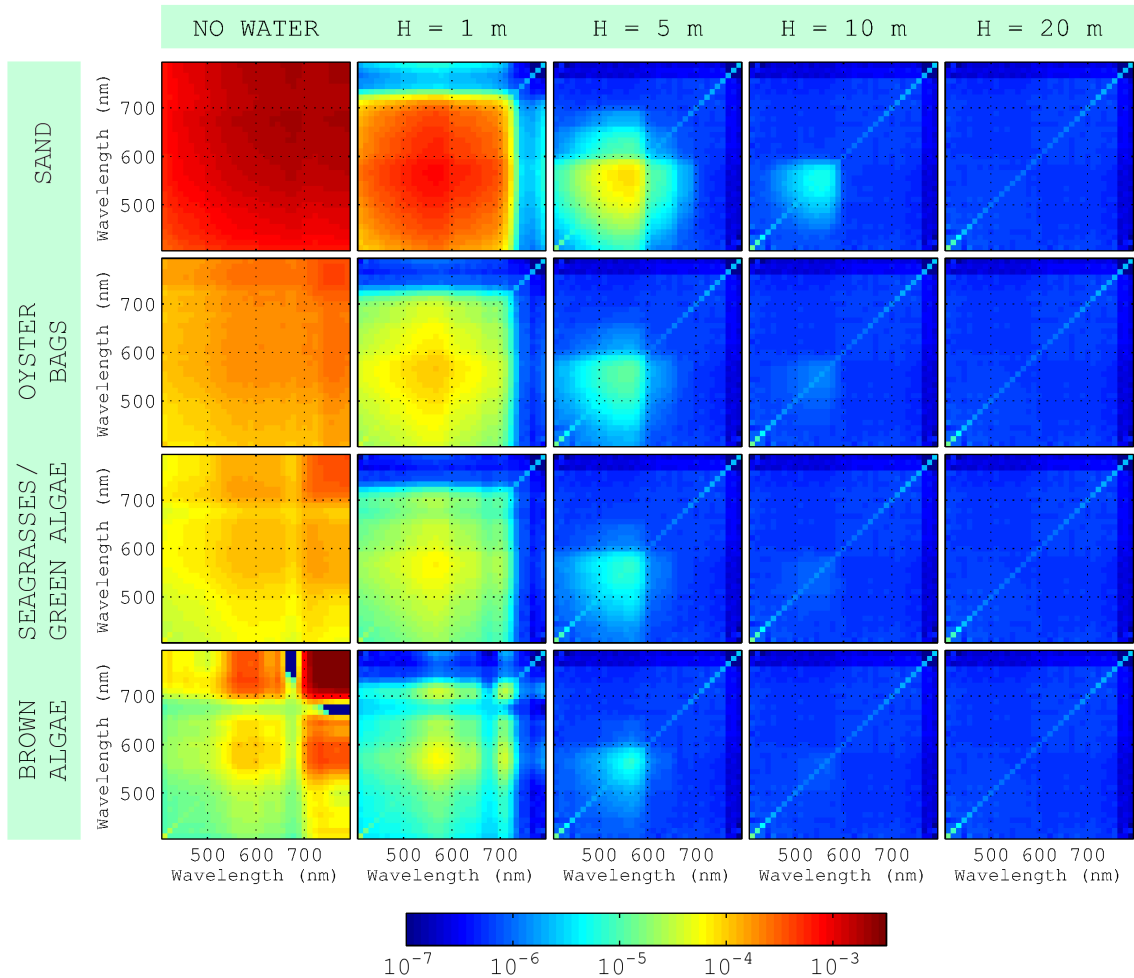


Figure 5: Total covariance matrix (as defined by Eq. (13)) as a function of depth for the four pure substrates investigated ($P = 0.1 \text{ m}^{-1}$, $G = 0.1 \text{ m}^{-1}$ and $X = 0.01 \text{ m}^{-1}$). The color scale is the same for every matrix.

366 to reflectance saturation. For the four substrates, the influence of bottom intra-class variabil-
 367 ity (resp., environmental noise) decreases (resp., increases) with increasing optical depth. At
 368 1 m and, to a lesser extent, 5 m, the subsurface reflectance variability in the visible domain is
 369 primarily driven by the bottom intra-class variability, showing that the latter should not be
 370 neglected for such optically shallow waters as also observed by Hedley et al. (2012b). Note
 371 that, at 1 m and for most wavebands larger than 700 nm, the water attenuation is already
 372 such that the total covariance matrix is mainly dominated by the environmental noise for the
 373 four substrates. At 10 m, the influence of environmental noise tends to overshadow that of
 374 bottom intra-class variability; only the variability of the brightest benthic class, namely sand,
 375 affects the subsurface reflectance in the domain of lower absorption (i.e., in the green region
 376 for this water type). In quasi-optically deep waters (20 m), the bottom is nearly not visible so
 377 only the environmental noise contributes to the total covariance matrix. Of course, note that

378 the relative influences of environmental noise and bottom intra-class variability as functions
379 of optical depth depend on their magnitude, meaning that they should be re-evaluated for
380 every sensor, study area, etc.

381 To our knowledge, only a few authors (e.g., Hedley et al. (2012b)) have thoroughly analyzed
382 the influence of bottom intra-class spectral variability on subsurface reflectance. Using the
383 analytical expression in Eq. (13) appears as a simple but convenient way to undertake such an
384 analysis and to investigate how accurate Eq. (8) is in modeling the total bottom reflectance.

385 4.2. Estimation results obtained with the simulated data

386 In Fig. 6 and Fig. 7, we show the inversion results obtained from the two synthetic data
387 sets presented in Section 3.4.1. Importantly, as the bottom reflectance variability was simu-
388 lated differently in these two data sets, we only present LS_{S21} , $MILE_{S21}$, LS and $MILE$ (resp.
389 $MILEBI_{S21}$ and $MILEBI$) bottom estimation results when using the first (resp. the second)
390 data set. For both data sets, we, however, show the H , P , G and X estimation results for
391 the six methods in order to study the influence of bottom mismodeling.

392
393 For each method, the H estimation error is similar for both data sets and increases with
394 depth (Fig. 6). It could be shown that this increase is caused both by a progressive H un-
395 derestimation and by an increasing estimation variance. Overall, $MILE_{S21}$ and $MILEBI_{S21}$
396 (resp., $MILE$ and $MILEBI$) provide lower errors than LS_{S21} (resp., LS). For example, at 10 m
397 (first data set, $n = 0\%$), the MAEs are 1.52, 1.63 and 2.32 m for $MILEBI_{S21}$, $MILE_{S21}$ and
398 LS_{S21} resp.. Using the sum-to-one constraint generally improves the performances, especially
399 for $H \geq 5$ m, $MILEBI$, $MILE$ and LS respectively obtaining MAEs of 2.48, 2.46 and 3.14 m
400 at 10 m.

401 On the one hand, the P and G errors tend to show a bowl-shaped pattern with respect to
402 depth (the minimum being located at 5 m in most cases), especially when considering the
403 second data set. On the other hand, the X error steadily declines with increasing depth
404 (Fig. 6). Similarly to H , $MILE$ - and $MILEBI$ -based methods generally better estimate these
405 water clarity parameters than LS -based methods. This is more visible for $H \geq 5$ m, for
406 which similar errors are generally obtained with $MILE_{S21}$, $MILEBI_{S21}$, $MILE$ and $MILEBI$.

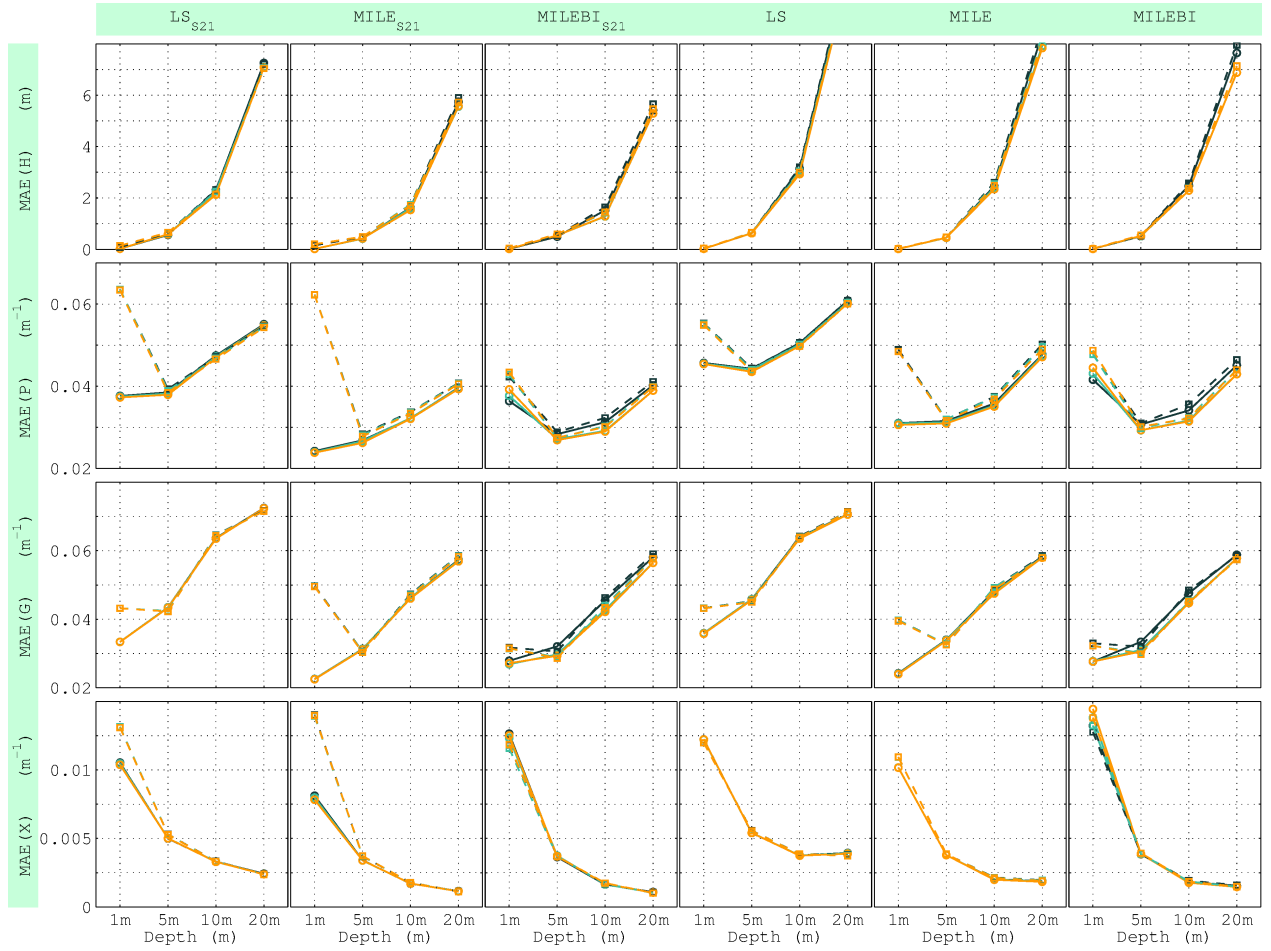


Figure 6: H , P , G and X (rows 1-4, resp.) estimation results obtained by applying the six methods (columns 1-6, resp.) presented in Table 1 to the synthetic data simulated using either Eq. (10) (solid lines) or Eq. (12) (dashed lines). Black, turquoise and orange lines respectively correspond to the use of $n = 0, 1$ and 2% for averaging the best bottom pairs.

407 For example, at 10 m (first data set, $n = 0\%$), the P (resp., X) retrieval error decreases by
 408 about 30% (resp., 48%) when using one of these four methods instead of LS_{S21} or LS .
 409 While both data sets lead to similar results for $H \geq 5$ m, strong differences appear for
 410 $H = 1$ m. When using the first data set, MILE-based methods offer the best performances
 411 for P and G , followed by MILEBI- and LS -based methods. In the case of X , $MILE_{S21}$ and
 412 $MILE$ still perform better, followed by LS - and MILEBI-based methods. However, the errors
 413 obtained with MILE- and LS -based methods increase when using the second data set. This
 414 increase is stronger (1) when the bottom mixture coefficients are constrained to sum to one
 415 (e.g., for P estimation, the MAEs obtained with LS_{S21} and LS increase by 70 and 21% resp.),
 416 and (2) in the cases of MILE-based methods as compared to LS -based methods (e.g., for
 417 X estimation, the MAEs obtained with LS_{S21} and $MILE_{S21}$ increase by 26 and 78% resp.).

418 On the other hand, MILEBI-based methods offer more similar results over both data sets,
419 MILEBI_{S21} generally performing better than the other methods for these three parameters
420 when using the second data set.

421 Using $n = 0, 1$ or 2% for averaging the best bottom pairs does not significantly change the
422 H, P, G and X inversion results for LS- and MILE-based methods. For MILEBI_{S21} and
423 MILEBI, increasing the value of n generally slightly degrades the estimation accuracy at 1 m
424 (e.g., for P estimation, the MAE obtained with MILEBI_{S21} increases by 7% when taking
425 $n = 2\%$ as compared to $n = 0\%$). However, the performances generally improve for $H \geq 5$ m
426 when taking either $n = 1$ or 2% . For example, at 10 m (first data set) and for both n values,
427 the MAE obtained with MILEBI_{S21} decreases by 15% for H and 7% for P .

428

429 The bottom estimation results show similar trends for every benthic class, method, data
430 set and n value, i.e., the error increases with depth (Fig. 7). For $H \leq 5$ m, the easiest
431 class to be retrieved is generally sand, followed by brown algae, seagrasses/green algae and
432 oyster bags. For deeper waters, it is more difficult to note any clear trend among methods
433 and benthic classes. Similarly to depth and water clarity parameters, MILE-based methods
434 provide equal or better performances than LS-based methods for $H \leq 5$ m (e.g., for the sand
435 coefficient, the MAEs obtained with LS_{S21} and MILE_{S21} at 5 m are 0.13 and 0.09 resp.).
436 It is worth noting that, despite the additional bottom intra-class variability present in the
437 second data set, the performances of MILEBI-based methods generally remain comparable to
438 those of MILE-based methods. Also, it can be seen that applying the sum-to-one constraint
439 significantly improves the retrieval for every method, especially for $H \geq 5$ m. For example,
440 for the oyster bag coefficient, the MAE obtained with MILEBI_{S21} at 5 m ($n = 0\%$) increases
441 by 38% when relaxing the sum-to-one constraint.

442 Averaging over several bottom pairs instead of retaining only the best one generally has a
443 positive effect for every method and $H \geq 10$ m (or even for $H \geq 5$ m in the cases of LS
444 and MILE). For such optically deep waters, taking $n = 2\%$ and, to a lesser extent, $n = 1\%$,
445 provides equal or better performances than taking $n = 0\%$ in most cases. For example, for
446 the sand coefficient, the MAE obtained with LS_{S21} at 10 m decreases by 13% when taking
447 $n = 2\%$ as compared to $n = 0\%$. For shallower waters, this averaging does not significantly

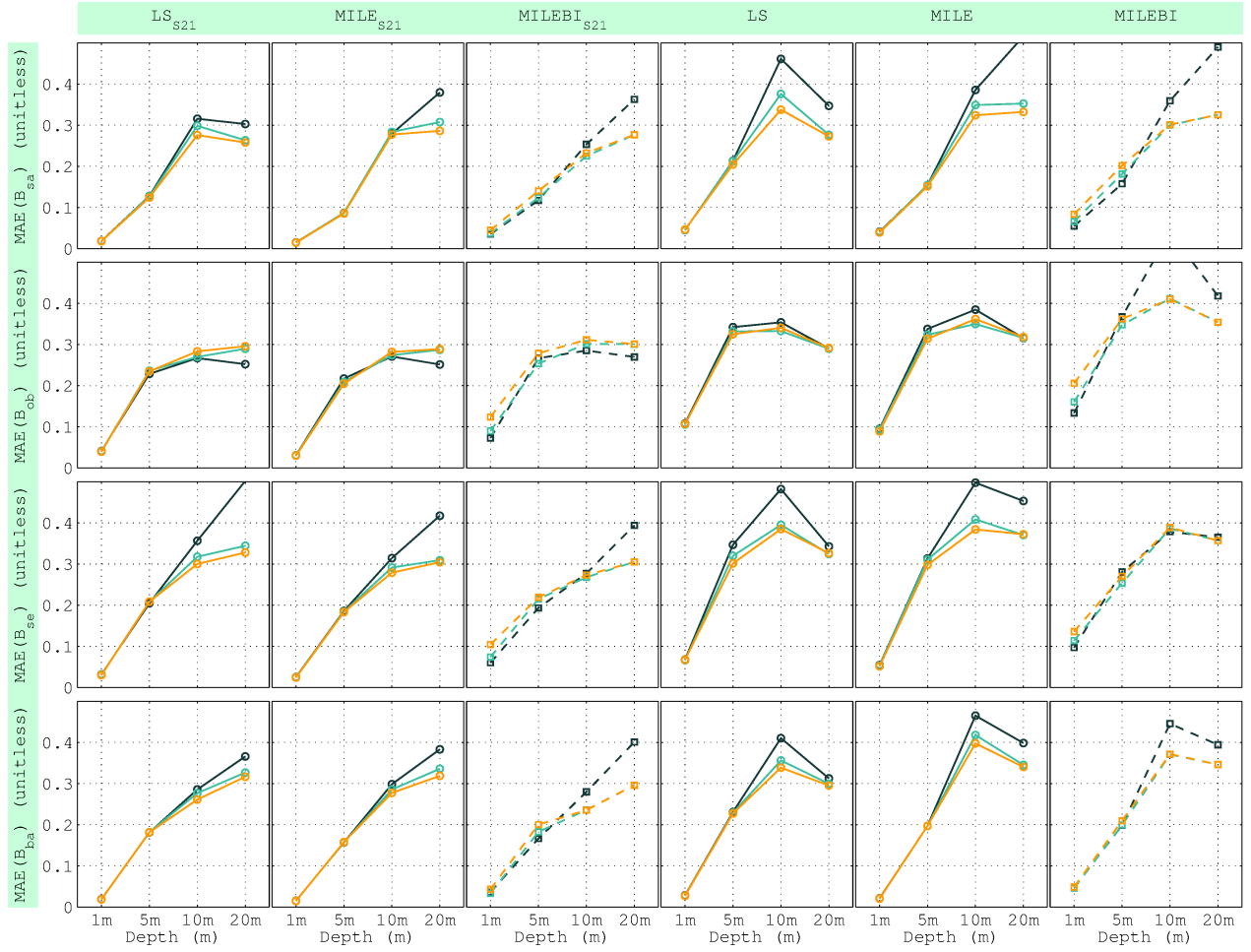


Figure 7: Bottom estimation results obtained by applying the six methods (columns 1-6, resp.) presented in Table 1 to the synthetic data simulated using either Eq. (10) (solid lines) or Eq. (12) (dashed lines). Black, turquoise and orange lines respectively correspond to the use of $n = 0, 1$ and 2% for averaging the best bottom pairs. B_{sa} , B_{ob} , B_{se} and B_{ba} (rows 1-4, resp.) refer to the coefficients of sand, oyster bag, seagrass/green alga and brown alga spectra, resp..

448 change the retrieval accuracy for LS- and MILE-based methods. However, taking $n = 2\%$,
 449 and, to a lesser extent, $n = 1\%$, slightly degrades the $MILEBI_{S21}$ and $MILEBI$ bottom
 450 estimation results. In the following results, n is therefore set to 1% as this value offers a good
 451 compromise between optically shallow and deep waters for the six methods.

452 4.3. Estimation results obtained with the airborne data

453 Similarly to simulations, for every method, the H estimation error increases with depth
 454 as a result of a progressive H underestimation and an increasing estimation variance (Fig. 8).
 455 This underestimation occurs for shallower waters in the cases of LS-based methods as com-
 456 pared to MILE- and MILEBI-based methods. Unlike for simulations, the sum-to-one con-
 457 straint leads to poorer performances for every method. MILEBI provides the highest overall

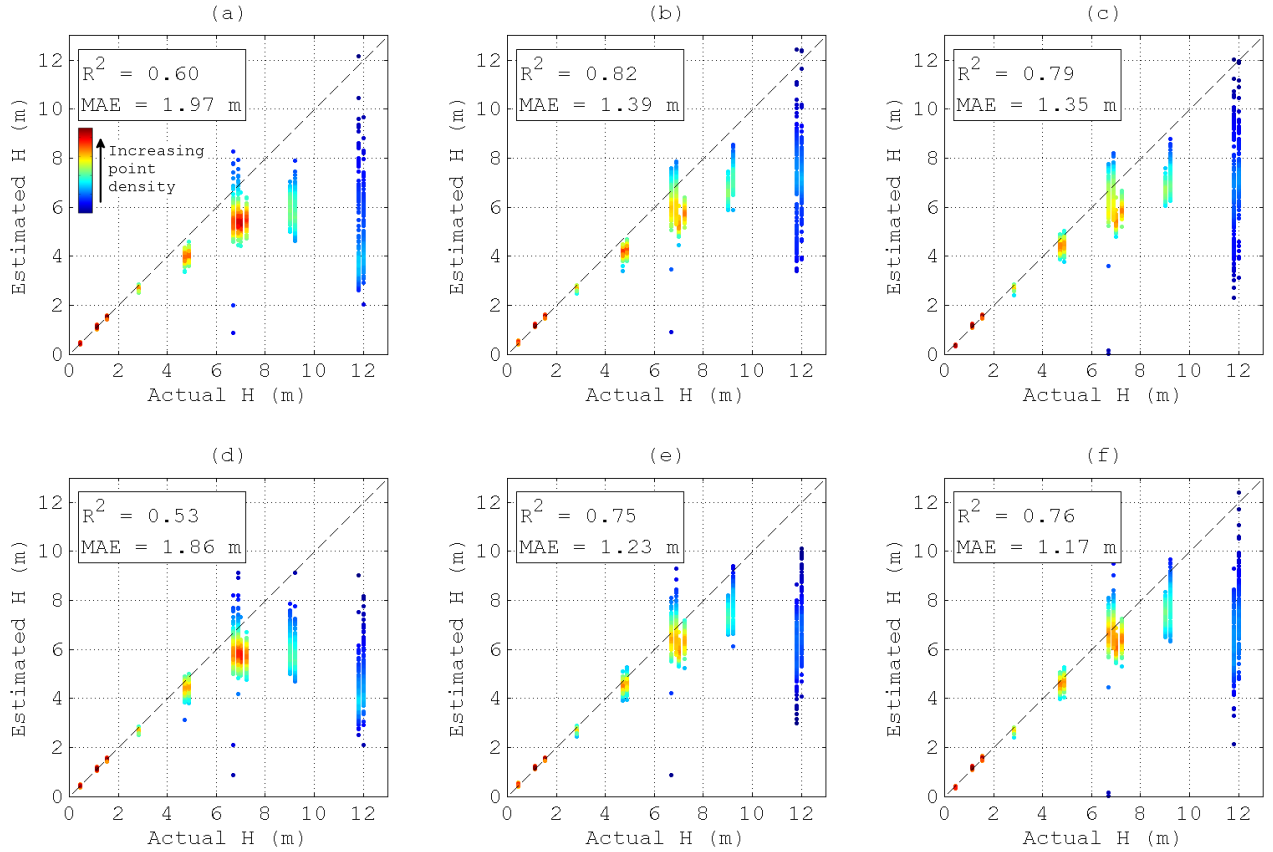


Figure 8: Depth estimation results obtained from airborne data ($n = 1\%$): (a) LS_{S21} , (b) $MILE_{S21}$, (c) $MILEBI_{S21}$, (d) LS , (e) $MILE$ and (f) $MILEBI$.

458 accuracy (MAE = 1.17 m), followed by $MILE$ (MAE = 1.23 m), $MILEBI_{S21}$ (MAE = 1.35 m)
 459 and $MILE_{S21}$ (MAE = 1.39 m). On the other hand, LS_{S21} and LS obtain significantly higher
 460 errors, with MAEs of 1.97 and 1.86 m respectively.

461

462 Similar observations are made from the P inversion results (Fig. 9), i.e., (1) $MILE$ - and
 463 $MILEBI$ -based methods perform better than LS -methods, and (2) relaxing the sum-to-one
 464 constraint improves the estimation accuracy. $MILEBI$ and $MILE$ still provide the best per-
 465 formances with $MAE \approx 0.016 \text{ m}^{-1}$, while LS_{S21} and LS lead to $MAE \approx 0.027 \text{ m}^{-1}$.

466

467 The bottom estimation results obtained from the 14 areas of known depth (Fig. 10) show
 468 the same pattern for every method, i.e., (1) the sandy-bottom cover is accurately retrieved
 469 in shallow waters, and (2) the estimated sand coefficient decreases as depth increases, which
 470 is compensated for by increasing coefficients of darker substrates. This decrease occurs for
 471 shallower waters (i.e., for $H \geq 4.70 \text{ m}$) for the three methods that do not constrain the sum

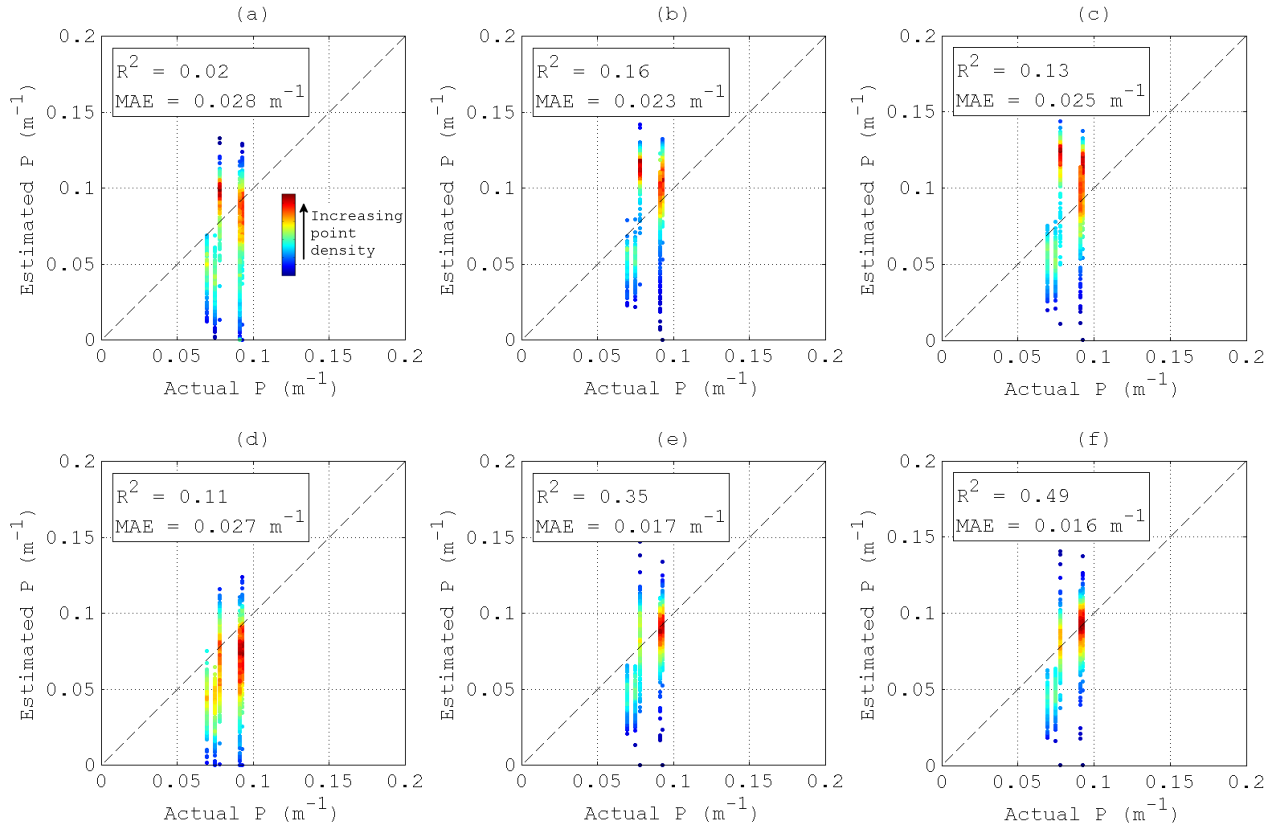


Figure 9: P estimation results obtained from airborne data ($n = 1\%$): (a) LS_{S21} , (b) $MILE_{S21}$, (c) $MILEBI_{S21}$, (d) LS , (e) $MILE$ and (f) $MILEBI$.

472 to one, i.e., LS , $MILE$ and $MILEBI$. For example, for these methods and $H \geq 4.70$ m, the
 473 estimated sand coefficient generally does not exceed 0.5, while the estimated brown alga co-
 474 efficient is mostly close to 1.5. On the other hand, LS_{S21} , $MILE_{S21}$ and $MILEBI_{S21}$ generally
 475 lead to reasonable estimates of bottom cover until around 9.00 m, the best performances
 476 being obtained using $MILE_{S21}$ with a minimum estimated sand coefficient of 0.6.

477

478 In Fig. 11, the same concise and qualitative RGB representation as Petit et al. (2017) is
 479 adopted to show the estimated spatial distributions of the four investigated substrates based
 480 on the image presented in Fig. 3. Beforehand, for each pixel, the four estimated bottom
 481 coefficients were normalized by their sum (that obviously equals one for LS_{S21} , $MILE_{S21}$ and
 482 $MILEBI_{S21}$) so that the obtained normalized coefficients were closer to the actual fractional
 483 covers (if we assume that the effect of intra-class variability is lower than that of fractional
 484 cover), which facilitates the comparison of the six methods. This allows representing (1) the
 485 distributions of oyster bags, seagrasses/green algae and brown algae through the blue, green

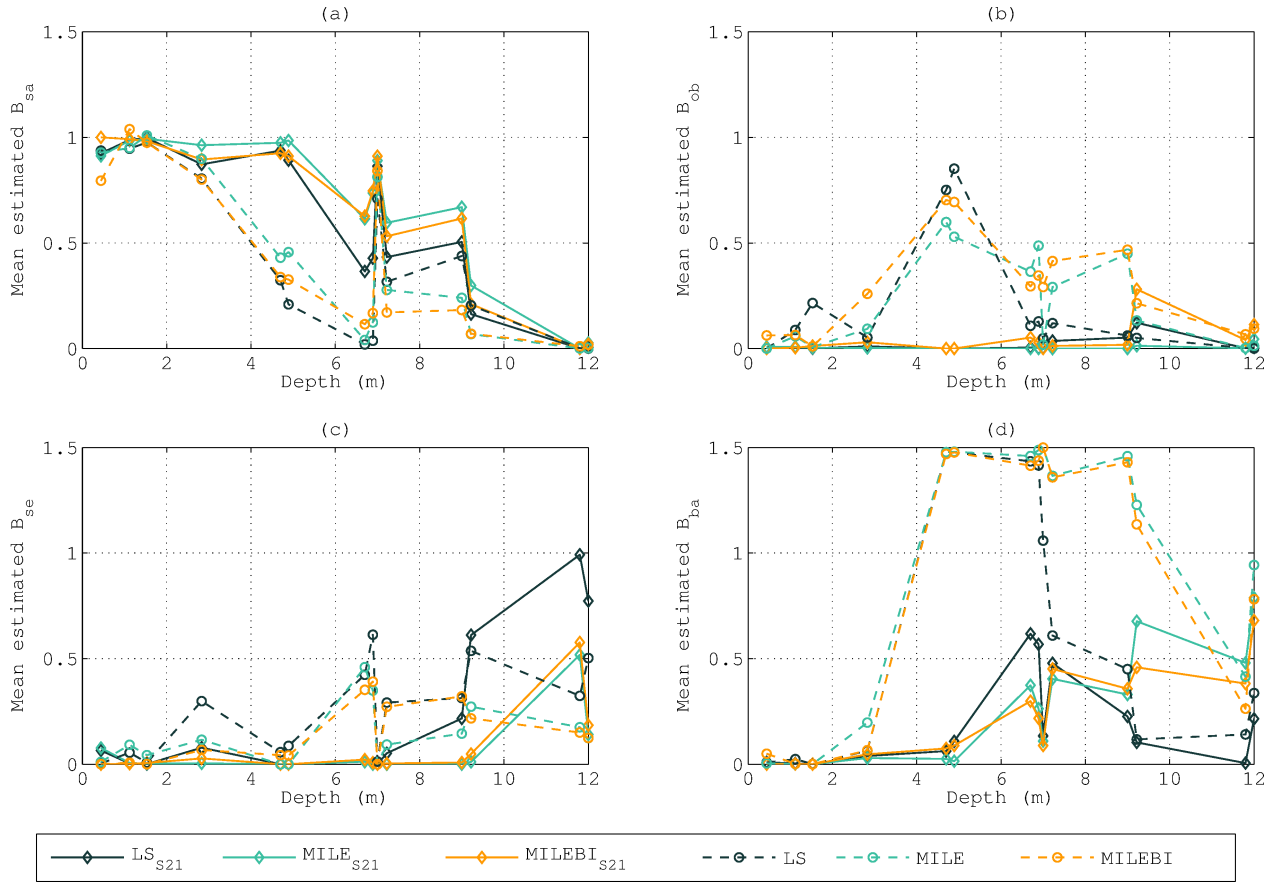


Figure 10: Mean estimated coefficients for (a) sand (B_{sa}), (b) oyster bags (B_{ob}), (c) seagrasses/green algae (B_{se}) and (d) brown algae (B_{ba}) for the 14 sandy-bottom areas ($n = 1\%$).

486 and red channels of the color composite image, resp., and (2) the distribution of sand through
 487 the absence of blue, green and red, i.e., through the pixel darkness.

488 The large sandy-bottom area is accurately retrieved by LS_{S21} , $MILE_{S21}$ and $MILEBI_{S21}$, the
 489 LS_{S21} map being slightly noisier than the other two, e.g., in the deeper (upper right) part
 490 of the image. Except in the shallower (left-hand) part of the image for MILEBI, relaxing
 491 the sum-to-one constraint leads to poorer results in the main sandy area. Indeed, even
 492 if LS, MILE and MILEBI retrieve some sand, they greatly overestimate the presence of
 493 seagrasses/green algae, brown algae and oyster bags respectively.

494 Overall, the six methods accurately retrieve the seagrass meadow. Some confusions with
 495 brown algae however occur in the lower and shallower part of the meadow when using MILE,
 496 MILEBI, and to a lesser extent, $MILEBI_{S21}$, $MILE_{S21}$ and LS_{S21} .

497 Similarly to what is observed with simulations, the retrieval of oyster bag distribution is
 498 generally less accurate. The results are seemingly more consistent with $MILEBI_{S21}$ and

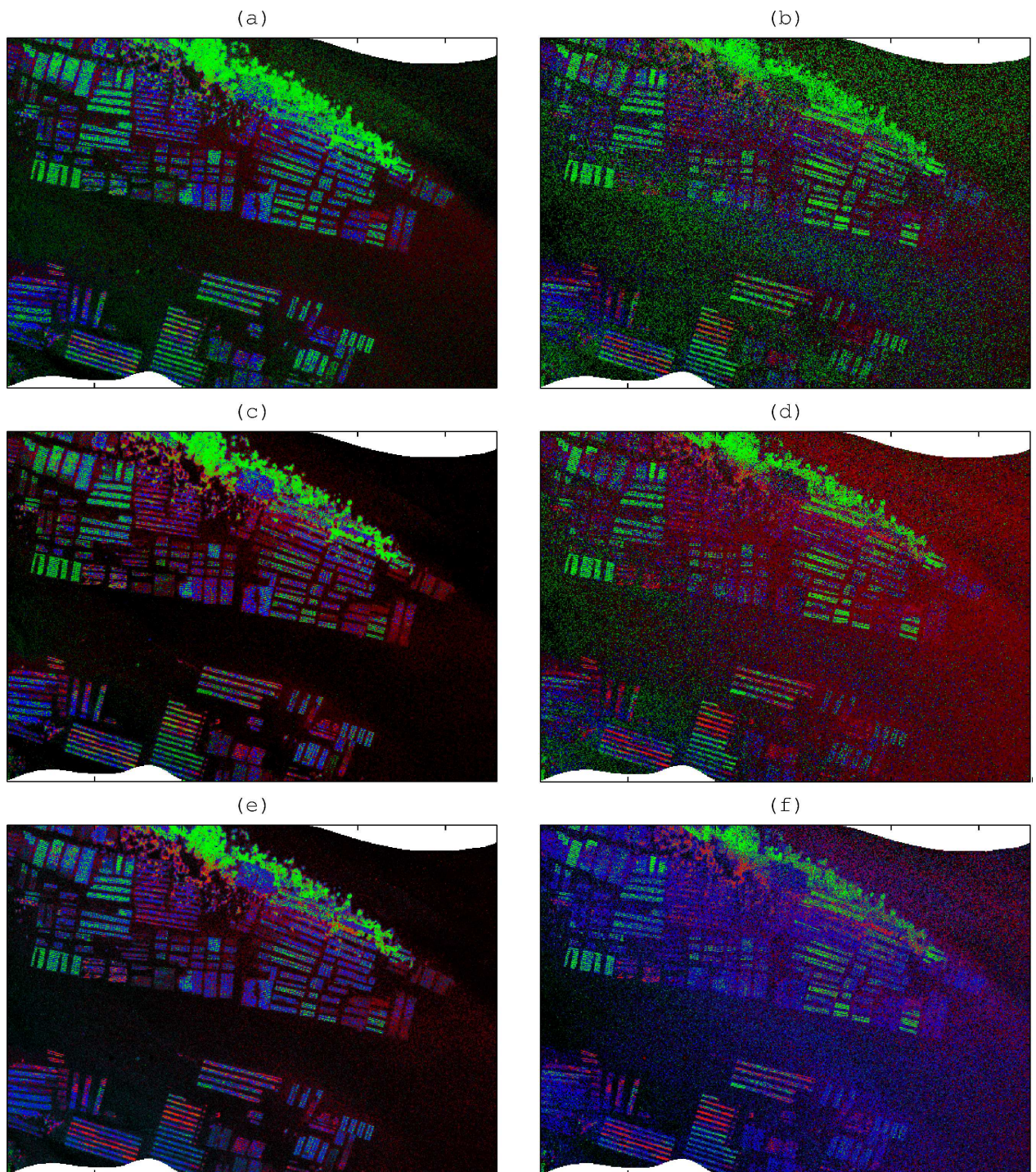


Figure 11: Color composite images showing the estimated spatial distributions of the four investigated substrates based on the image presented in Fig. 3: (a) LS_{S21} , (b) LS , (c) $MILE_{S21}$, (d) $MILE$, (e) $MILEBI_{S21}$, and (f) $MILEBI$ ($n = 1\%$). The normalized estimated coefficients of oyster bags, seagrasses/green algae and brown algae are respectively coded by the blue, green and red channels. The normalized estimated sand coefficient is coded by the pixel darkness (i.e., the absence of red, green and blue).

509 MILEBI, as both methods obtain higher and more homogeneously-distributed oyster bag
500 coefficients over oyster racks as compared to the other methods. Note that only the MILE_{S21}
501 and MILEBI-based methods can reliably detect the deepest oyster racks located within the
502 seagrass meadow. On the other hand, LS_{S21} obtains a spatially-inconsistent mixture of oyster
503 bags and seagrasses, while LS and MILE retrieve a sand-dominated bottom.
504 It is worth noting that the brown algae retrieved by MILEBI_{S21} over some oyster racks in the
505 lower left part of the image are more sparsely detected by MILE_{S21} and almost not detected
506 by LS_{S21}. These brown algae are, however, consistently retrieved by the three methods with
507 relaxed sum-to-one constraint.

508 *4.4. Discussion of estimation performances*

509 *4.4.1. General considerations*

510 By definition, a bio-optical model is only a model, which means that various sources of
511 error may make it deviate from the observation. Given the number of potential sources (e.g.,
512 environmental noise or bottom intra-class variability), the difficulty to properly take them
513 into account (e.g., skyglint) and the low water-leaving radiance, it seems quite challenging
514 to include them explicitly within the modeling and to estimate the corresponding additional
515 parameters during the inversion process. Yet, the results presented in Fig. 5 show that
516 such variability may make the shallow water reflectance strongly differ from the bio-optical
517 model. As a result, it may significantly decrease the estimation accuracy as obtained using the
518 classical LS method, since the latter tries to perfectly match the model with the observation.
519 Alternatively, we propose to include these deviations within a probabilistic forward model of
520 shallow water reflectance variability, thus assuming that they all can be described through
521 an additive zero-mean multivariate Gaussian noise that is fully determined by its spectral
522 covariance matrix. The MILE- and MILEBI-based inversion methods are derived from such
523 probabilistic modeling, and the results derived from simulated and airborne data show that
524 they all succeed in decreasing the detrimental influence of environmental noise as compared to
525 LS-based methods, especially in optically deep waters. In addition, MILEBI-based methods
526 decrease the influence of bottom intra-class variability, especially in very optically shallow
527 waters.

528 4.4.2. Common trends in method performances

529 Overall, the results obtained with simulated and airborne data show similar trends and
530 are consistent with expectations for every method. For example, depth and benthic cover
531 estimations become less accurate as depth increases due to the decreasing bottom influence
532 on subsurface reflectance (Fig. 6, Fig. 7, Fig. 8 and Fig. 10). The retrievals of water clarity
533 parameters differ between absorbing (P and G) and scattering (X) components that respec-
534 tively decrease and increase the subsurface reflectance (Fig. 6). For P and G , the depth
535 of minimum error is the one that offers the best compromise between (1) maximizing the
536 subsurface reflectance so that there is more contrast between absorbing and non-absorbing
537 regions (which facilitates the retrieval), and (2) minimizing the influence of bottom variabil-
538 ity on subsurface reflectance. For X , the error is minimum in optically deep waters, where
539 the bottom does not affect the subsurface reflectance.

540 4.4.3. Influence of averaging the best bottom pairs

541 Due to the ill-posedness of the inversion problem (resulting in compensations between
542 model parameters) or to potential deviations between the measured reflectance and the
543 model, the actual bottom pair may not be the one that leads to the lowest cost function
544 value. In simulations, the inversion is particularly ill-posed for quasi-optically deep waters,
545 where (1) H and coefficients of dark bottoms often tend to compensate, and (2) all the dark
546 benthic classes (e.g., seagrasses/green algae and brown algae) nearly have the same effect on
547 subsurface reflectance (Fig. 6 and Fig. 7). In this case, selecting a particular dark substrate
548 in the bottom spectral library instead of another dark substrate is not strongly justified,
549 given the different sources of error between the observed and modeled reflectances that ac-
550 tually make both substrates equally likely. The results (Fig. 6 and Fig. 7) demonstrate that,
551 alternatively, taking the average of multiple best bottom pairs (if sufficiently close to the
552 best pair) can decrease the ill-posedness influence and increase the overall retrieval accuracy,
553 acting as a regularization step. Testing the effect of the n value (that directly controls the
554 number of best pairs to be averaged), we show that a high n value (even greater than 2%) can
555 be chosen for optically deep waters, where a reasonable aim is only to discriminate among
556 bright and dark substrates. In very shallow waters, a too large n value may, however, increase

557 the confusion between classes, therefore making the value of 1% a good compromise for our
558 data. Of course, this value should be reassessed for each data set, as it is expected to depend
559 on, e.g., the environmental noise and/or the benthic classes encountered on the study site.

560 4.4.4. Influence of sum-to-one constraint

561 The results show that the sum-to-one constraint always leads to better inversion results
562 if the shallow water reflectance model is perfect (e.g., when applying LS- and MILE-based
563 methods to the first data set, or MILEBI-based methods to the second data set), because
564 reducing the number of parameters to be retrieved reduces the estimation uncertainty. In
565 practice, the observation may, however, deviate from the model. These deviations may be
566 caused either by the observation, e.g., in the case of imperfect preprocessing of at-sensor
567 radiance (e.g., atmospheric and sea surface corrections), or by the model, e.g., in the case of
568 imperfect bio-optical modeling. In this study, such deviations are present when considering
569 airborne remote-sensing data or when applying LS- and MILE-based (resp., MILEBI-based)
570 methods to the second (resp., first) synthetic data set. In these cases, relaxing the sum-to-one
571 constraint adds a degree of freedom, which enables unmodeled (or mismodeled) variability
572 to be compensated for by misestimation of bottom cover rather than by misestimation of
573 depth and/or water clarity parameters. This is demonstrated by the results obtained with
574 airborne data, since (1) Fig. 8 and Fig. 9 show that LS, MILE and MILEBI better retrieve
575 H and P as compared to LS_{S21} , $MILE_{S21}$ and $MILEBI_{S21}$ resp. (note that this is consistent
576 with the results of Petit et al. (2017) in the case of LS), and (2) Fig. 10 shows that LS_{S21} ,
577 $MILE_{S21}$ and $MILEBI_{S21}$ provide better bottom retrievals than LS, MILE and MILEBI resp..
578 However, relaxing the sum-to-one constraint does not always degrade the bottom retrieval:
579 indeed, if the bottom intra-class variabilities affect the subsurface reflectance (i.e., mostly
580 for low optical depths, see Fig. 5), allowing both benthic reflectances in Eq. (8) to vary in
581 a multiplicative way enables LS and MILE to better capture this intra-class variability and
582 improve the overall performances.

583 $MILEBI_{S21}$ thus appears as an interesting alternative to LS- and MILE-based methods, be-
584 cause (1) it takes into account potentially complex (i.e., not only multiplicative) bottom
585 intra-class variabilities through their associated covariance matrix, and (2) it limits the prob-

586 lem ill-posedness as it does not require any additional parameter to be estimated. The benthic
587 covers derived from airborne data (Fig. 11) illustrate this dual improvement, as MILEBI_{S21}
588 not only provides accurate performances in the deepest sandy-bottom areas similarly to LS_{S21}
589 and MILE_{S21}, but also retrieves the presence of brown algae over oyster racks in shallower
590 waters, similarly to LS, MILE and MILEBI.

591 4.4.5. Robustness of inversion methods

592 All LS-, MILE- and MILEBI-based methods require some prior knowledge on the con-
593 sidered scene, this knowledge concerning either the mean endmember reflectances or the
594 covariance matrices. However, obtaining an accurate prior knowledge may be difficult, which
595 requires investigating how such errors can affect the method performances.

596 It should first be noted that obtaining an accurate estimate of the environmental noise ma-
597 trix (as necessary for MILE- and MILEBI-based methods) is usually not problematic, since
598 it only necessitates finding a homogeneous area in the image. This may easily be done using
599 the methodology proposed by Wettle et al. (2004), and areas of optically deep water are ideal
600 to perform this estimation. Using this matrix for inversion allows MILE-based methods to
601 greatly improve the retrieval of depth and water clarity parameters in sufficiently deep waters
602 as compared to LS-based methods (Fig. 6, Fig. 8 and Fig. 9). It also improves the remote
603 sensing of shallow waters if Eq. (8) accurately models the actual bottom reflectance. How-
604 ever, if the latter cannot accurately be modeled by Eq. (8) (e.g., due to complex intra-class
605 variabilities or poorly-known mean endmember reflectances) while having a strong effect on
606 subsurface reflectance (i.e., in very optically shallow waters), the performances of MILE-
607 based methods may decrease more strongly than those of LS-based methods (Fig. 6). In
608 such cases, MILE is shown to better estimate depth and water clarity parameters than LS,
609 LS_{S21} and MILE_{S21} (Fig. 6, Fig. 8 and Fig. 9), especially because relaxing the sum-to-one
610 constraint reduces the detrimental influence of bottom intra-class variability.

611 Alternatively, MILEBI and MILEBI_{S21} allow the modeled endmember spectra to vary around
612 their mean through the use of bottom intra-class covariance matrices. Both methods are thus
613 less affected by an imperfect knowledge of endmember reflectances. This aspect is one of the
614 primary advantages of these methods as compared to LS- and MILE-based methods, and

615 may be of tremendous importance when mapping poorly-known shallow water environments,
616 for which the use of a single mean reflectance spectrum for each benthic class may seem
617 unrealistic.

618 However, obtaining accurate estimates of bottom covariance matrices may sometimes be diffi-
619 cult since, similarly to the mean endmember reflectances used by the six tested methods, and
620 as emphasized in Section 2.4, these matrices are estimated from a limited number of spectra
621 that may not be fully representative of the variability encountered in the whole study area.
622 That said, the results obtained with simulated data (Fig. 6) suggest that accurate knowl-
623 edge of these matrices may only be necessary for very optically shallow waters, as MILE- and
624 MILEBI-based obtain nearly the same results over both data sets beyond 5 m. As the optical
625 depth increases, the water attenuation and environmental noise smooths the spectral details
626 present in bottom covariance matrices (Fig. 5), so rough estimates become sufficient to take
627 this variability into account. For very optically shallow waters, unlike LS- and MILE-based
628 methods, MILEBI-based methods show similar performances for both synthetic data sets
629 (Fig. 6), although the first data set is generated using zero covariance matrices that strongly
630 differ from those used in MILEBI_{S21} and MILEBI. This important result demonstrates the
631 robustness of these two methods against imperfect knowledge of bottom covariance matrices,
632 which may have important implications for their implementation at larger scales (e.g., global
633 scale).

634 5. Conclusions and perspectives

635 In this study, we propose a realistic probabilistic model of shallow water reflectance vari-
636 ability as well as two associated inversion methods, denoted MILE and MILEBI. As compared
637 to classical least-squares fitting, these methods improve the remote sensing of shallow waters
638 by utilizing specific parameterizations of the spectral covariance matrix. MILE and MILEBI
639 not only constrain model inversion based on the off-diagonal terms of covariance matrices, but
640 also allow the measured data to differ from the model by giving the less reliable wavebands
641 lower weights in the cost function. For MILE, these wavebands correspond to the domains
642 where the environmental noise is the strongest. For MILEBI, the less reliable wavebands
643 not only correspond to the domains of strong environmental noise, but also to the domains

644 where the bottom intra-class variability is the highest. To our knowledge, MILEBI is one of
645 the first shallow water remote-sensing methods that explicitly take into account the inherent
646 variability of each benthic class without adding any multiplicative parameter to be estimated
647 during the inversion process (the bottom covariance matrices, however, need to be estimated
648 beforehand, similarly to the mean endmember reflectances).

649 Based on simulated and airborne data, we show that these specific covariance parameteriza-
650 tions enable MILE and MILEBI to generally perform better than LS. Further, studying the
651 influence of constraining bottom mixture coefficients to sum to one shows that this constraint
652 provides better inversion results if the reflectance model reliably describes the observation. In
653 the presence of unmodeled (or mismodeled) variability in the remote-sensing data (e.g., due to
654 bottom intra-class variability, imperfect atmospheric correction or bio-optical modeling, etc),
655 relaxing this constraint may decrease the detrimental influences of these deviations, however
656 at the cost of an increasingly noisy bottom retrieval as the optical depth increases. In prac-
657 tice, as there are always some slight deviations between measured and simulated data, these
658 results thus suggest that most inversion methods cannot accurately retrieve all the targeted
659 parameters at the same time, and that applying different constraints during the inversion
660 will lead these deviations to affect the estimation of other unconstrained parameters. That
661 said, the sum-to-one constrained version of MILEBI combines the advantage of limiting the
662 number of parameters to be estimated (thus reducing the problem ill-posedness) with that
663 of allowing the observation to differ from the model. This dual aspect makes this method
664 promising to remotely sense complex shallow water environments.

665
666 Future studies would certainly benefit from the probabilistic forward model of shallow
667 water reflectance variability presented in Eq. (12) so as to generate more realistic data sets
668 than those usually generated using Eq. (10). This model could also be combined with other
669 mixing models (e.g., linear models including more than two substrates or non-linear mixing
670 models) in order to further refine the modeling of bottom reflectance. This may be important
671 for more accurately simulating the response of very shallow waters, for which an increase in
672 bottom modeling complexity significantly affects the measured subsurface reflectance.

673 As far as the inversion is concerned, perspectives include refining the initialization part, that

674 may be critical for MILE methods in very shallow waters (results not shown). Optimizing the
675 construction of the LUT used for initialization (size, parameter distributions, etc) is likely
676 to speed up the inversion while keeping similar estimation performances. Alternatively, the
677 Mahalanobis distance used in MILE could easily be used as a metric within a LUT-based
678 inversion approach such as ALLUT (Hedley et al., 2009) in order to further speed up the
679 inversion process or to avoid local minima. Note that the approach recently proposed by Jay
680 & Guillaume (2016) could also be implemented to regularize the inversion by introducing
681 prior knowledge on targeted parameters.

682 Ultimately, an important perspective is the assessment of MILE and MILEBI performances
683 for shallow water remote sensing at the global scale, e.g., in the context of the forthcoming
684 “Environmental Mapping and Analysis Program” mission (Guanter et al., 2015). For this
685 purpose, besides properly estimating the environmental noise on the image itself, a generic
686 library of bottom mean reflectance spectra will be necessary to parameterize the total benthic
687 reflectance. This library may be built from a comprehensive spectral database gathering all
688 the expected bottom classes in the considered study site. For example, the 12-class database
689 presented by Hochberg et al. (2003) could be of great help for coral reef remote sensing. This
690 database could also be used to build an associated generic library of intra-class covariance
691 matrices to implement MILEBI. As shown by Hochberg et al. (2003) in Fig. 3, the intra-
692 class variability at the global scale is such that using a single mean reflectance spectrum
693 for each bottom class to map this class across different areas worldwide seems to be highly
694 unrealistic. MILEBI thus offers an interesting alternative to LS and MILE to take such
695 variability into account in a more accurate manner. In particular, given the high intra-class
696 variabilities presented by Hochberg et al. (2003) and the significant overlaps between these
697 classes, MILEBI may greatly improve the remote sensing of coral reefs.

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