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Electronic and magnetic properties of yttria-stabilized zirconia (6.7 mol% in Y_2O_3) doped with Er^{3+} ions from first-principle computations

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ABSTRACT

Yttria-stabilized zirconia (YSZ) is a widely recognized ceramic of distinct electrical, mechanical and optical properties. Although YSZ is an intrinsically paramagnetic solid, it could potentially transform to a magnetic semiconductor by incorporating in its crystalline structure isolated atoms bearing unpaired valence electrons. Based on this hypothesis and motivated by the latest advances on YSZ doped with rare-earth atoms, in the current article we report on the electronic and magnetic properties of YSZ doped with Er^{3+} ($[Xe]4f^{11}6s^0$) cations that comprise three “unpaired” 4f electrons in their ground state electronic configuration. Our computations, conducted on YSZ 6.7 mol% in Y_2O_3 doped with two different Er^{3+} concentrations (3.2 and 6.7 mol% in Er_2O_3), expose that Er^{3+} :YSZ is a stable antiferromagnetic semiconductor ($S = \frac{3}{2}$ per Er^{3+}) bearing a rather wide band gap of about 5 eV. All results presented and discussed in current report rely on spin-polarized density functional theory (DFT) within the spin resolved generalized gradient approximation (SGGA) for the pure Perdew, Burke and Ernzerhof exchange–correlation functional (PBE) and hybrid version widely referred as PBE0. According to our knowledge, this is the first time that the magnetic properties of Er^{3+} : YSZ materials are reported for any Er^{3+} concentration.

Introduction

It is a common sense that semiconductors stand as the cornerstone of current technologies applied in the realms of telecommunications, light-emitting diodes

(LEDs), lasers, integrated sensors [1–7] and spintronics [8, 9]. In particular, for the latter class of applications that seeks to exploit the spin of charge carriers incorporated in the crystal framework of a given solid [10–13], diluted magnetic semiconductors

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have emerged as very promising candidates attracted considerable attention the past decades [11, 14–18].

Yttria-stabilized zirconia (YSZ) is an extra-stable wide band gap functional oxide of high mechanical, chemical and thermal stability [19–31]. A considerable part of its properties are related to the presence of structural oxygen vacancies, created as yttrium cations are incorporated to zirconia dioxide to stabilize its cubic phase in room temperature [32–34]. In particular, YSZ crystals doped with erbium ions have attracted the interest of many researchers in recent years owed to their promising electro-optical properties [35–43]. For instance, Greenberg et al. [36] and Savoini et al. [41] studied the spectroscopic properties of YSZ crystal doped with Er^{3+} ions via optical absorption and emission spectroscopy including lifetime measurements and pointed out Er-doped YSZ is excellent candidate for advanced applications photonics. The spectral and luminescent characteristics of Er^{3+} YSZ (6 mol % in Y_2O_3 , 2 mol % in Er_2O_3) have been studied by X. Wang et al. [43] while P. Ryabochkina et al. [40] studied Er^{3+} YSZ (6 mol% in Y_2O_3 , 5.85% in Er_2O_3) as potential active media of solid state laser emitters in a wavelength range of 1.5–1.7 μm . Furthermore, Caridad et al. [44] starting from 8 mol% in Y_2O_3 YSZ engineered recently high-purity Er^{3+} :YSZ thin films and characterized their optical properties. As those authors point out, high-purity Er^{3+} :YSZ films could find a proper ground in hybrid photonic platforms involving on-chip optical amplification at telecommunication wavelengths (~ 1500 nm). Finally, there are also several studies reporting the doping of other solids with Er^{3+} , for instance, In_2O_3 [45], SnO_2 [46] and pure ZrO_2 [47].

Motivated by the increasing interest in materials built from Er-doped YSZ, in the current article we report on the electronic structure and magnetic properties of YSZ 6.7 mol % in Y_2O_3 doped with two different concentration Er_2O_3 (3.2 mol% and 6.7 mol %). Our aim is to obtain a reliable description of the electronic properties of this appealing material at the atomic level and determine the influence of Er^{3+} on its magnetic properties.

Theoretical methods and computational details

Crystal atomistic structures construction

Although theoretical simulations [48] suggest that YSZ with 3.2 mol% in Y_2O_3 should be regarded as the minimum concentration of Y_2O_3 required to stabilize the cubic phase of ZrO_2 in room temperature, most of the recent experimental investigations are routinely performed at higher concentration of about 8 mol % in Y_2O_3 [49]. Nevertheless, the construction of an YSZ cell model of precisely 8 mol% in Y_2O_3 would require an extra-large *c*- ZrO_2 supercell of more than 190 atoms. Therefore, for the sake of computational efficiency [24] we conducted our investigation on a periodic model of YSZ with 6.7 mol% yttria (instead of 8 mol%) assuming that 1.3 mol% concentration difference would have a minor impact on the properties of interest. Such a modeling choice, adopted also in earlier computations studies, considerably reduces the size of the required supercell simply because YSZ doped with 6.7 mol% in Y_2O_3 can be easily built by introducing two Y_2O_3 units into a $2 \times 2 \times 2$ supercell of a 96-atom conventional crystallographic *c*- ZrO_2 supercell. Even in that case thought, the determination of the most stable configurations remains a challenging computational task. Specifically, to conclude to the most stable local atomistic crystal structure one should systematically remove two oxygen atoms and replace any four zirconium ions with an equal number of charge-compensating Y ions. If this strategy is applied to a $2 \times 2 \times 2$ supercell, an extremely large set of initial nonequivalent local atomistic crystal structures (> 2500) should be generated [24]. To circumvent this hampering point, we relied on the structural data of YSZ proposed by Parkes et al. [24]. These authors have studied YSZ 6.7% in Y_2O_3 by means of gradient corrected DFT and proposed a data set of stable local atomistic structures. Starting from the most stable structure of YSZ proposed by these authors, we constructed six additional independent configurations of YSZ and we reoptimized their atomistic structures at PBE and PBE0 levels of theory. After the most stable structure of YSZ was determined within this set of trial configurations, we added two and four erbium atoms to the YSZ supercell (see Fig. 1). In such a manner, two Er^{3+} :YSZ models of 3.2 mol%

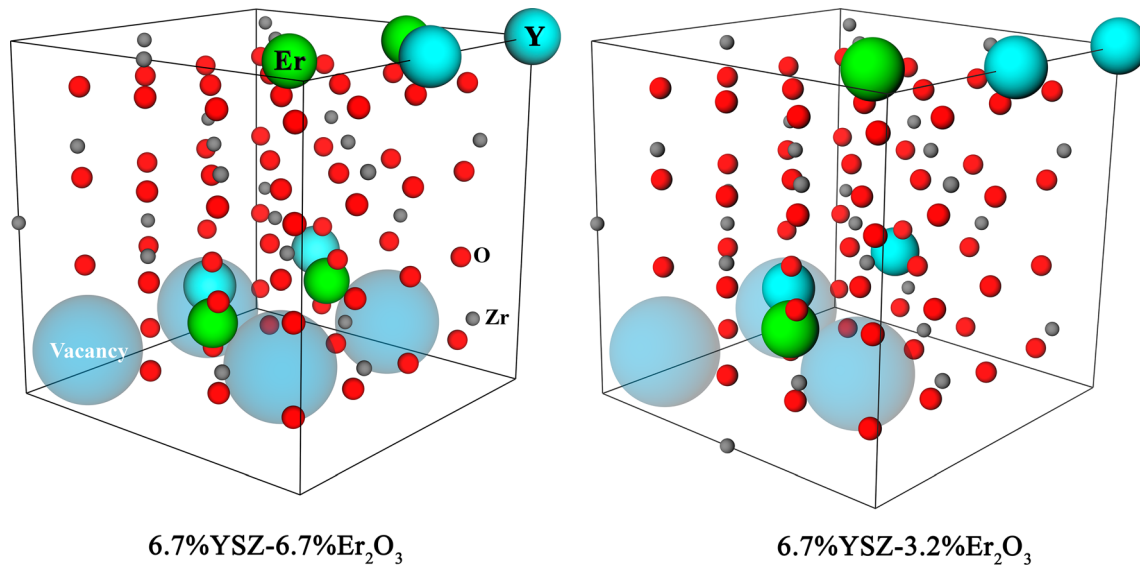


Figure 1 Local atomistic structures of the erbium-doped yttria-stabilized zirconia used in this work built on $2 \times 2 \times 2$ supercell of ZrO_2 . Both supercells have been optimized at the PBE level of

and 6.7 mol% in Er_2O_3 , respectively, have been constructed to study the influence of Er^{+3} concentration.

Computational methods

All theoretical calculations have been performed within the framework of spin-polarized Density Functional Theory (DFT) and the PAW method [50, 51] as implemented in the Vienna ab initio simulation package (VASP) code [52–54]. Brillouin zone sampling has been performed using a $4 \times 4 \times 4$ Monkhorst–Pack (MP) [55] grid in both the $2 \times 2 \times 2$ supercell of $c\text{-ZrO}_2$ and the erbium-doped YSZ. The Gaussian smearing method was used in these calculations, in a width of 0.01 eV. The electronic wave functions were expanded in plane waves with a kinetic energy cutoff of 550 eV. In all cases, the bulk super-cells were relaxed until the residual forces were below 10^{-4} eV/Å and the convergence criteria for the energy deviations were 10^{-5} eV. Bader charge analysis [56–58] was performed on the all-electron charge density (the core density was generated from the pseudo potentials files) in order to evaluate the charge of all atoms of the Er^{+3}YSZ supercells considered.

Being aware of the well-known deficiencies of conventional pure DFT [59] in describing strongly correlated systems, we chose the hybrid PBE0, HSE06 and the pure PBE functionals, respectively. In the

theory without relaxation of the supercell lattice constants. The O vacancy sites are oriented along the (210) direction, with an atomic site separation of is 5.73 Å.

latter approximation, the Hubbard correction term has been also employed [60–64]. In all cases, we applied the spin-polarized generalized gradient approximation (SGGA + U) correction scheme introduced by Liechtenstein et al. [65] where the widely applied correction parameters U and J are implemented as independent corrections. Specifically, the parameter U corresponds to the required energy for the addition of an additional charge to the $4d$ and $4f$ shell in the atomic limit. On the other hand, J parameter describes the intra-atomic screened exchange interaction. Here, we have chosen a value of $U = 7$ eV and $J = 0.9$ eV that have been conventionally added based on the properties of the Er, Y, Zr atoms after extensive benchmark bandgap calculations performed on pure $c\text{-ZrO}_2$.

Results and discussion

Charge distribution, bonding and energy difference between the conduction and valence bands of Er^{+3}YSZ 3.2 mol% and 6.7 mol% in Er_2O_3

To obtain some first insights about the bonding in YSZ 3.2 mol% and 6.7 mol% in Er_2O_3 at the atomic level, we computed and studied the net charges of each atom by applying the Bader partitioning

scheme as implemented in VASP code. Based on carefully chosen topological properties, the latter method partitions the space of a given cell in distinct regions encasing each nucleus and attributes net charges to each of them. The results listed in Table 1 and visualized in Fig. 2 point out that the net atomic charges should be identical for both concentrations of Er_2O_3 in YSZ. Specifically, relying on the computed valence occupation numbers, the atomic charges of Er, Y, Zr and O should lie at +2.0, +2.1, +2.6 and -1.3, electrons, respectively. This result suggests that the net charge of Er ions should be closer to +2 than +3 as chemical intuition would suggest in terms of the expected oxidation degree of Er in isolated Er_2O_3 . The latter result is in line with the computed atomic charge on oxygen atoms which is found around $\text{O} - 1.3e$, (instead of -2.0) if we consider that the embedded Er_2O_3 should remain neutral. To verify this outcome, we recomputed the atomic charges using Mulliken population analysis at the PBE0 level of theory and a pseudopotential basis set of gaussian type functions for all atoms, as implemented in the CRYSTAL 17 suite of programs [66]. In this case, we obtained a charge of +2.6e for Er, +2.1e for Zr, +2.3e for Y and -1.3e in the case of O. As it becomes obvious, neither method attributes an absolute net charge of +3e to the embedded Er atoms. The observed differences might stem either from limitations of the methods used in the description of each atom in the environment of the supercell considered and/or to non-negligible covalent contributions in the intracell bonding. For instance, a careful electron population analysis of each atom in the supercells considered revealed that the reduced positive atomic charge of Er cations in the case of Bader partitioning should stem from additive ρ_α and ρ_β electron densities with $\rho_\alpha + \rho_\beta \sim 1$ and $\rho_\alpha \sim \rho_\beta$ which “appear” in the 5d atomic orbitals of Er.

Table 1 Number of valence electrons (V^0) of the free atoms Er, Y, Zr and O and Bader valence electron (V^B) of each atom in a $2 \times 2 \times 2$ supercell of Er^{+3}YSZ and their differences (ΔV)

	Er	Y	Zr	O
V^0	22	11	12	6
V^B	20.0	8.9	9.4	7.3
ΔV	+2.0	+2.1	+2.6	-1.3

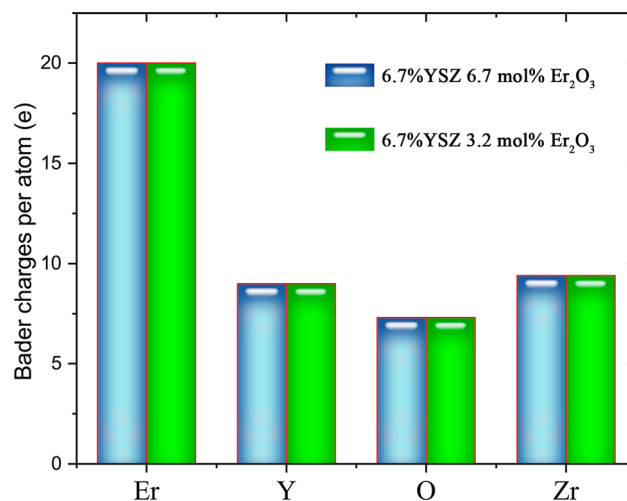


Figure 2 Charge distribution for all atoms in the states of YSZ- Er_2O_3 computed by the Bader charge analysis method.

Let us now turn our attention to the data listed in Table 2, where we compare the computed bandgap of Er^{+3}YSZ with those of $c\text{-ZrO}_2$ and YSZ 6.7 mol% Y_2O_3 , at four levels of theory. As seen, for pure $c\text{-ZrO}_2$ and YSZ, out of the four methods considered here, PBE0 returns the most accurate values with respect to the experiment. Specifically, the PBE0 band gap of pure $c\text{-ZrO}_2$ (YSZ) is found about 6.11 eV (5.65 eV) while the available experimental values vary between 6.10 and 7.08 eV [67, 68] (5.8 eV) [23]. On the other hand, the PBE method undershoots considerably the experimental values. Despite the observed differences between various methods considered, all functionals conclude to the same trend according to which the bandgap of YSZ undergoes a rather weak decrease upon Er doping.

Magnetic properties of Er^{+3}YSZ

In Table 3, we compare the energy differences between various spin states, namely nonmagnetic (NM), ferromagnetic (FM) and antiferromagnetic (AFM), of Er^{3+}YSZ 3.2, 6.7 mol% in Er_2O_3 . A careful study of the computed values suggests that the (A) FM states of Er^{3+}YSZ should lie considerably lower in energy than their nonpolarized counterpart. Depending on the functional used, the exchange energies ($\Delta E_{\text{NM}-\text{FM}}$) vary from a minimum of 1.58 eV (PBE) to a maximum of 5.83 eV (PBE + U). On the other hand, HSE06 and PBE0 approximations return energy differences of 4.85 eV and 4.89 eV, respectively, that lie closer but lower to the PBE + U

Table 2 Computed energy band gaps (Eg, in eV) of 32ZrO₂, YSZ and YSZ-Er₂O₃ where FM (AFM) stands for (anti)ferromagnetic spin distributions

	PBE	PBE + U	HSE06	PBE0	Exp. [23, 67]
ZrO ₂	3.20	4.32	5.42	6.11	6.10–7.08
YSZ ^{6.7% Y₂O₃}	3.10	3.77	4.89	5.65	5.8
Er ⁺³ :YSZ ^{3.2% Er₂O₃} (FM)	–	3.55	4.42	5.19	–
Er ⁺³ :YSZ ^{3.2% Er₂O₃} (AFM)	–	3.57	4.46	5.20	–
Er ⁺³ :YSZ ^{6.7% Er₂O₃} (FM)	–	3.71	4.59	5.31	–
Er ⁺³ :YSZ ^{6.7% Er₂O₃} (AFM)	–	3.75	4.61	5.37	–

Table 3 Exchange energies ($\Delta E_{NM-E_{FM}}$, per Er atom, in eV and $\Delta E_{FM-E_{AFM}}$, per Er atom, in meV), local magnetic moments at the Er atoms (M_{Er} per Er atom, in μ_B) and magnetic anisotropy energy (MAE, in meV) of 32ZrO₂, YSZ and YSZ-Er₂O₃. The notation \uparrow means $S_z = 3/2$ on each Er. In all cases, a complete relaxation of all nuclear positions in the cell has been performed to assure the reliability of the results

	PBE	PBE + U	HSE06	PBE0
	YSZ ^{3.2 mol%Er₂O₃}			
$\Delta E_{NM-E_{FM}}$	1.58	5.83	4.85	4.89
$\Delta E_{AFM-E_{FM}}$	– 0.87	– 0.10	– 0.17	– 0.19
M_{Er}	2.87	2.99	2.96	2.96
	YSZ ^{6.7 mol%Er₂O₃}			
$\Delta E_{AFM(\uparrow\uparrow\downarrow\downarrow)}-E_{FM(\uparrow\uparrow\downarrow\downarrow)}$	1.64	0.16	0.11	0.10
$\Delta E_{AFM(\uparrow\downarrow\uparrow\downarrow)}-E_{FM(\uparrow\downarrow\uparrow\downarrow)}$	– 0.07	– 0.02	– 0.17	– 0.40
$\Delta E_{AFM(\uparrow\uparrow\downarrow\downarrow)}-E_{AFM(\uparrow\downarrow\uparrow\downarrow)}$	– 1.71	– 0.18	– 0.28	– 0.50
M_{Er}	2.86	2.99	2.96	2.96
$M_{Er}(x)$	2.74	2.87	–	–
$M_{Er}(y)$	2.73	2.87	–	–
$M_{Er}(z)$	2.70	2.87	–	–
MAE (ΔE_x-E_y)	5.03	4.97	–	–
MAE (ΔE_x-E_z)	5.04	7.42	–	–

method. Therefore, for the lowest concentration of 3.2 mol% in Er₂O₃ and regardless of the method chosen, the FM state appears to be the most stable one. Turning our attention to the energy differences between the FM and AFM states corresponding to the latter concentration, we see also that all methods predict that the AFM lies lower in energy than FM. In this case, the PBE pure functional returns the largest energy differences (0.87 meV) while the smallest one is returned by PBE + U approximation. Conversely, the two hybrid functionals considered here deliver energy differences of 0.17 and 0.19 meV. Consequently, Er³⁺:YSZ 3.2 mol% in Er₂O₃ at 0 K should be safely considered as a magnetic semiconductor with the corresponding (A)FM states lying very close in energy. Focusing now our attention to

the computed data of Table 3 obtained for Er³⁺:YSZ 6.7 mol% in Er₂O₃, we see that an almost twofold increase in Er³⁺ concentration (from 3.2 to 6.7 mol%) might have a small but worth noticing effect on the energetic ordering between the FM and the two possible AFM states of different spin distributions. Specifically, our outcomes suggest that for the later concentration (comprising four Er³⁺/supercell) the AFM [Er(↑)Er(↓)Er(↑)Er(↓)] state, where each arrow represents a spin of 3/2, is the most stable one. Specifically, at PBE0 level the latter state lies about 0.4 and 0.5 meV lower in energy than the corresponding [Er(↑)Er(↑)Er(↑)Er(↑)] and [Er(↑)Er(↑)Er(↓)Er(↓)] spin-polarized states, respectively.

Let us now proceed with the computed atomic magnetic properties of the systems considered computed at the PBE and PBE + U levels of theory which provide a better ratio between accuracy and efficiency than the two hybrids used in this study. Based on the values summarized in Table 3, we see that the total magnetic moment per cell for both AFM and FM phases and both concentrations is 0 and 6 (12) μ_B , respectively, while the projected spin density on each Er³⁺ yields a magnetic moment (M_{Er}) close to 3 μ_B . This result matches the expectation value for the free Er³⁺ ion in its ground state ([Xe] 4f¹¹6s⁰) and contradicts the Bader partitioning which as we discussed in the previous section suggests that the charge of the Er atoms should be about + 2.0. On the other hand, Mulliken charges seem to provide a better description of the Er net charges in this case. Finally, we computed the local magnetic moment of the erbium atom with the local spin density approximation (LSDA) by Ceperley–Alder (CA) pseudopotential [69]. The obtained result of 2.85 μ_B lies very close to those obtained with the SGGA (2.86 μ_B) approximation.

In a further step, we calculated the magnetic anisotropy energy (MAE) of YSZ 6.7 mol% in Er₂O₃ defined as the difference between the total energies of

a magnetic material for different orientations of the magnetization. For that purpose, we used the SGGA method including spin-orbit coupling (SOC) [62] taking also into account the Hubbard term (U) [63]. Our outcomes returned a slight change on the local magnetic moments by less than $0.12 \mu_B$. Here, it is important to mention that the atomistic local structure and the vacancy/dopant distribution and the gap energies of the systems considered are not influenced by the SO coupling. Finally, the anisotropy energies summarized in Table 3 point out that YSZ 6.7 mol% in Er_2O_3 features a magnetic anisotropy of about 7.42 meV per Er with the magnetic moment lying in the z-direction of the structure. A similar trend should be expected for the other concentration (3.2 mol% in Er_2O_3) considered in this work.

For a deeper understanding of the magnetization distribution, the spin densities, defined as the difference between the spin-up and spin-down electron densities ($\rho_{\text{spin-up}} - \rho_{\text{spin-down}}$), have been also computed and studied for both concentrations in Er_2O_3 (see Fig. 3). To provide an intuitive visualization of the spin densities, we have chosen a spin density cut through the plane of the YSZ- Er_2O_3 . As seen, the spin density contours that vary between -0.02 and 0.02 \AA^{-3} , point out that the rare-earth metal sites are characterized by the highest magnetic moment

values, while their magnetic moments reach a value of about $3.0 \mu_B$ per Er atom. Hence, the main magnetic moment contributions are strongly localized on the Er atom (see Fig. 3) as is also suggested by the local magnetic moments listed in Table 3.

Density of states

We will close this report with a brief discussion about the character of the total and partial densities of states of the ferromagnetic state of Er^{3+} :YSZ starting from three spins up, $S_z = +3/2$, on each Er represented by an upward pointing arrow (\uparrow). The corresponding density-of-states (DOS) plots, computed within the spin-polarized hybrid PBE0 approximation, are illustrated in Fig. 4. As it is readily seen, both Er^{3+} :YSZ 3.2 mol% [$\text{Er}(\uparrow)\text{Er}(\uparrow)$] and 6.7 mol% [$\text{Er}(\uparrow)\text{Er}(\uparrow)\text{Er}(\uparrow)\text{Er}(\uparrow)$] feature a clear semiconductor character with very similar gaps in the “majority” and the “minority” spin-density of states. These gaps refer, of course, to the corresponding spin-up and spin-down electronic configurations, respectively. As we can also see, spin-up and spin-down states are obviously asymmetric, particularly near the Fermi energy level where the DOS is attributed mainly to Er^{+3} . This picture is in accord with our previous outcomes suggesting that the magnetic character of Er^{+3} :YSZ should be solely attributed to the Er^{+3} ions incorporated in the crystal of c- ZrO_2 . Also, it is interesting to

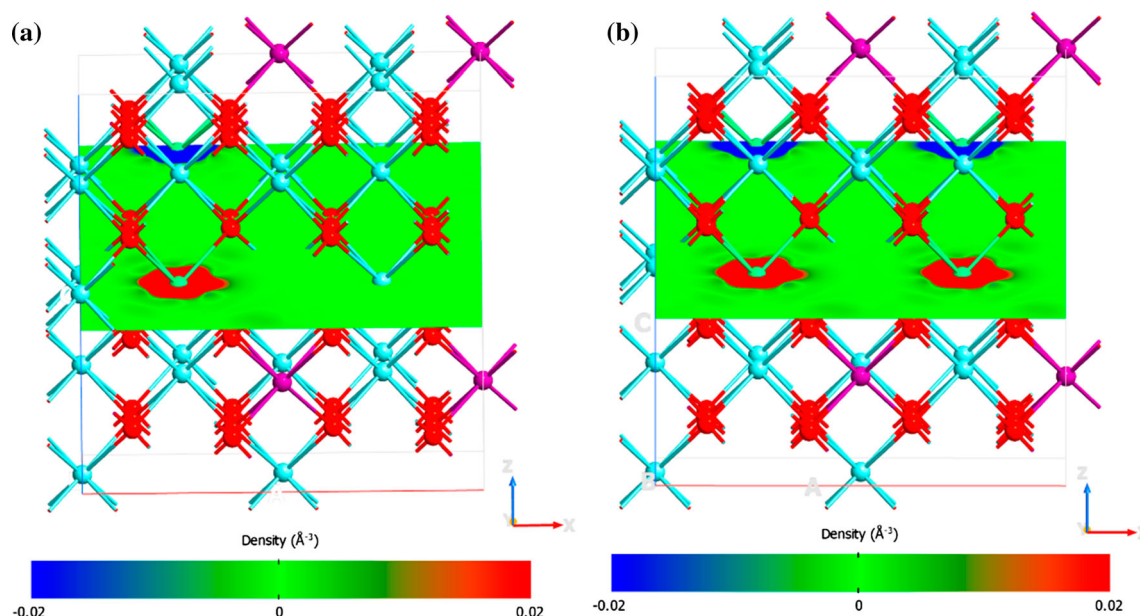


Figure 3 Cut plane of the spin density contribution of the YSZ- Er_2O_3 . The Er positions are in the cut plane of the square, erbium ions in green, yttrium ions in purple, zirconium ions in blue, and oxygen ions in red.

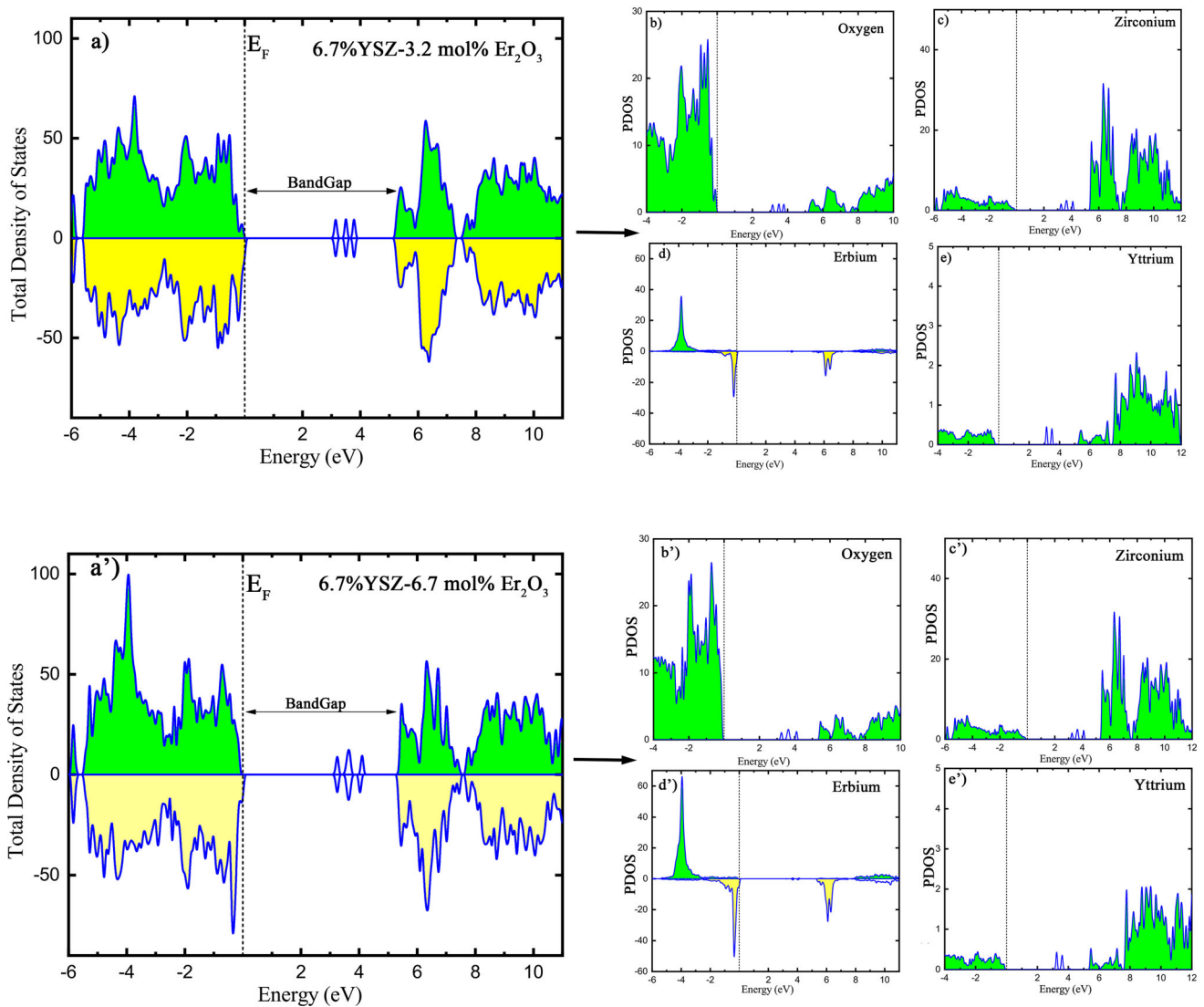


Figure 4 a, a' Total density of states (DOS) and projected density of states (PDOS) of the atoms [(b, b') O, (c, c') Zr, (d, d') Er, (e, e') Y] of YSZ- Er_2O_3 , computed using the PBE0 model. At this point it is important to stress that the reported band gap values do

stress that the top of the valence band (VB) is dominated primarily by the spin-down density, while the conduction band (CB) is mostly populated by states attributed to Zr atoms with a small contribution of spin-down states coming from Er atoms (see Fig. 4c and d). Finally, the antiferromagnetic (AFM) state $\text{Er}(\uparrow)\text{Er}(\downarrow)$ for 3.2% of Er_2O_3 and $\text{Er}(\uparrow)\text{Er}(\downarrow)$ $\text{Er}(\uparrow)\text{Er}(\downarrow)$ for 6.7% has been also studied. In that case, the total DOS (not plotted here) is symmetric but remarkably similar to the ferromagnetic (FM) one. The principal differences come from Er PDOS near the Fermi energy, one half being positive and the other negative without affecting the gap values: 5.19 (5.31) eV for

not take into account the weak peaks appearing around 4 eV of the CB which should be regarded as numerical artifacts due to the non-relaxed lattice constants [70, 71].

FM and 5.20 (5.37) eV for AFM at the PBE0 level of calculation (see Table 2).

Conclusions

We performed an accurate calculation of the electronic, magnetic properties of 3.2 mol% and 6.7 mol% erbium-doped YSZ 6.7 mol% in yttria. In its most stable electronic structure, Er^{3+} :YSZ is an antiferromagnetic semiconductor with a gap of 5.20 eV which is about 0.4 meV per Er atoms more stable with respect to the ferromagnetic spin configuration.

Concerning the energy difference between the conduction and valence bands, a narrowing of the band gap is observed with respect to YSZ and ZrO_2 , upon Er^{+3} doping. Even if there is no experimental confirmation, the fact that the same behavior is observed in other alloyed semiconductors supports our predictions. This could be confirmed by experimental optical transmission measurements via vacuum-ultraviolet (VUV) and valence-band x-ray-photoemission spectroscopies (VB-XPS). Our best estimates for the total magnetic moment of 3.2 mol% and 6.7 mol% in Er_2O_3 YSZ are $M_{\text{tot}} = 6 \mu_B$ and $12 \mu_B$ per cell, respectively, with a local magnetic moment of $2.96 \mu_B$ per Er atom. In addition, we calculated on the magnetic anisotropy energy MAE that controls the observable magnetism in these systems and the magnetic anisotropy energy is found about 7.42 meV per Er atom.

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