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# Statistical physics modelling of azo dyes biosorption onto modified powder of *Acorus calamus* in batch reactor

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## Abstract

The methylene blue adsorption was carried out on a natural material powder of *Acorus calamus* treated firstly with H<sub>2</sub>SO<sub>4</sub> and then activated by KMnO<sub>4</sub>. The new material was called PACK. Fourier transform infrared FTIR spectroscopy, pH<sub>zpc</sub> analysis and SEM micrograph were carried out to characterize the material. Pseudo-first-order, pseudo-second-order and pseudo-n<sup>th</sup> order constant rates were calculated for analysis of the dynamics of the sorption process, showing that sorption kinetics followed a pseudo-n<sup>th</sup> order model. Among the tested isotherm models, the R-P isotherm was considered to be the most relevant to describe MB sorption onto PACK. Advanced statistical physic models, Monolayer single-energy, monolayer two-energy, and double-layer two-energy were used to analyze the adsorption mechanism of methylene blue (MB) and to understand the PACK adsorbent performance. Based on the R<sup>2</sup> values obtained, the monolayer two-energy

model was found to be the most suitable to describe the MB adsorption onto the PACK material. From this, the adsorption of MB was assumed on two different sites of PACK with two different energies, E1 for the first site and E2 for the second site. These two different receptor sites can interact with a variable number of MB molecules (n), n1 with the first type of sites and n2 with the second type of sites. The sorption capacity of this material was about 1500 mg/g at 30°C. The potential of PACK, a readily available material to use as an alternative biosorbent material to eliminate the MB color from aqueous solutions was therefore confirmed.

**Keywords:** Adsorption; Isotherms; Kinetics; Methylene Blue; Physical models; Wastewater.

## 1. Introduction

Water is the main raw material in our planet, vital for humans, animals, plants and microorganisms; all the vital phenomena of the biosphere are related to the availability of water. Water pollution affecting rivers, seas, groundwater and lakes is the result of the wastewater arising from many industrial discharges, repeatedly contaminated with diverse organic, inorganic and volatile compounds, such as benzene, toluene, phenol, heavy metals, suspended solids, etc[1]. This causes a degradation of the ecosystem. Among the industries that use water in large quantities are the tanning and textile industry, where it is used primarily for dyeing and finishing. These industries are one of the main sources of huge pollution problems in the world due to their water polluted with toxic dyes, even in small amounts. In fact, 100,000 varieties of textile dyes with an annual production estimated at 7.105 metric tons are available on the world market; 30% of these dyes are used at more than 1000 tons per year, and 90% of textile products are used at 100 tons per year or less [2, 3]. 2 to 20% of textile dyes are diversified in liquid effluents during the dyeing process and can cause serious problems because their presence in water, even in very small amounts, is very visible and indisputable [4, 5]. The treatment of industrial waste containing this type of dye has a great interest. Vast variety of biological, chemical and physical techniques has been developed and tested in the treatment of effluents filled with dyes, such as flocculation, precipitation, ion exchange, membrane filtration, irradiation and ozonation. However, the use of these processes is very costly and contributes to the creation of vast volumes of sludge [2, 6]. Adsorption remains one of the most favorable methods for removing dyes, due to its simplicity of use [7, 8].

The principle of the adsorption treatment is to trap the dyes with a solid material, the adsorbent. There are several solid materials in the literature (biosorbents, clays, zeolites, activated carbons ...) that can be used in water bleaching processes. In recent years, research focuses on the use of cost-effective adsorbents, available locally, biodegradable adsorbents made from natural sources [9]. In this regard, biosorbents synthesized from lignocellulosic residues have been widely used as adsorbents to treat colored effluents, because of their very large porous structure, large surface area and high adsorption capacity. Among these adsorbents, we can mention among others: date stones [10], apple skin [11], olive stones [10], peach stones [13], corn cobs [14], coffee beans [15], and coffee grounds [16, 17], Tea waste [18], bagasse [19], coconut shell [20], apricot stones [21], fungi [22], algae [23], chitosan [24], bacteria [25]. Also, in recent times, Ash of *Cassia fistula* seeds [26], rice husk [27], coconut shell and coal ash [28], *Stipa tenassicima* fibers [29], cones of *Pinus brutia* [30], wild carob [31], LDHs [32] and acid treated *Cupressus sempervirens* cones pomegranate peel [33], as well as pectin from orange industry residues [34], polyacrylamide-diatomite (PAA-D) [35], Fe<sub>3</sub>O<sub>4</sub> [36], chitosan vermiculite beads [37], *Pseudoevernia furfuracea* [8], Orange Peel treated with H<sub>3</sub>PO<sub>4</sub> [38] and particles of *Ziziphus jujuba* stones (BZJS1) [39].

Methylene blue is the most frequently used dye in cotton dyeing, wool, and silk. It causes breathing difficulties when there is an inhalation, a burning sensation if swallowed by mouth, causes nausea [5].

In the present study, we were interested in the removal of methylene blue (BM) dye using a new inexpensive and naturally abundant material *Acorus calamus* collected from the Sahara of Algeria, which is considered to be a potential material for adsorption of cationic dyes. Moreover and to our knowledge, no work has been reported in the literature on the use of this material for the elimination of dyes. In the present study, it was first treated with H<sub>2</sub>SO<sub>4</sub> and then activated with

KMnO<sub>4</sub>. The new material was called PACK. Various experimental parameters were analyzed, such as pH, contact time, effect of the mass of adsorbent and effect of initial dye concentration. The effect of temperature on the adsorption of the dye was also studied and the thermodynamic parameters were determined.

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## 2. Materials and methods

### 2.1. Materials

The *Acorus calamus* collected from the Sahara of Algeria was used as biosorbent in this work. The following chemicals products were used, Methylene Blue (MB), H<sub>2</sub>SO<sub>4</sub> (65%), KMnO<sub>4</sub>, and humic acid. All the chemicals mentioned were purchased from Sigma-Aldrich

### 2.2. Preparation of dye solutions and concentration determination

Methylene Blue (MB), a typical cationic dye was selected as an adsorbate. Its chemical structure and some of its properties are presented in Figure 1 and Table 1. It was obtained from ACROS with 99.99% purity.

Working solutions were prepared by dilution of the stock solution with distilled water to yield the appropriate concentrations. The pH of the solutions was adjusted by adding either 0.1 M HCl or 0.1 M NaOH solutions. Before use, all bottles and glassware were beforehand cleaned and then rinsed with distilled water and oven-dried at 60°C. There residual dye concentrations were assessed by An SP-8001 UV/vis Spectrophotometer of Axiom (Germany, Shimadzu).

**Table 1:** Chemical properties of Methylene Blue.

Dye	Classification	$\lambda_{\max}$ (nm)	Empirical formula	Formula weight (g. mol <sup>-1</sup> )	Solubility in water
Methylene Blue	Cationic dye	664	C <sub>16</sub> H <sub>18</sub> N <sub>3</sub> ClS	320	>50g. L <sup>-1</sup>

### 2.3. Preparation of the adsorbent

Aquatic reeds of Sahara (Algeria) were firstly washed with distilled water, then dried at a temperature of about 40°C. This quantity was sieved and crushed to obtain small grains, generally

less than 2 mm. A first treatment was carried out with a mixture of sulfuric acid (65%) and the aquatic reeds powder at a ratio of (1g (powder) / 20ml (H<sub>2</sub>SO<sub>4</sub>)); the reaction mixture was stirred at a temperature of 70 °C for 5 hours. The powder was filtered and washed several times with distilled water until purification and then dried in an oven overnight at 80 °C. The resulting product was treated again with KMnO<sub>4</sub> (1 M) at a ratio of (1g (powder) / 10ml (KMnO<sub>4</sub>)) at room temperature for 24 hours. The powder obtained was washed until purification and then dried in an oven overnight at 80 °C. It was then stored in desiccator for future use. The obtained product, namely powder of *Acorus Calamus* KMnO<sub>4</sub>-activated, was abbreviated as PACK.

## **2.4. Characterization of the adsorbent**

### **2.4.1. Infrared spectroscopy (IRTF)**

FTIR analysis enables to determine the functional surface groups of materials. This analysis was conducted on a Spectrum Two-type infrared spectroscopy apparatus using the technique of high-pressure KBr granules; the analysis was done over a wavelength range of 400-4000 cm<sup>-1</sup>.

### **2.4.2. The Point of Zero Charge of PACK**

The pH<sub>pzc</sub> (pH of the zero or no charge point) refers to the pH value at which the net charge on the adsorbent surface is null. This parameter is very important in adsorption phenomena, especially when electrostatic forces are involved in the mechanism. A quick and simple protocol to determine the pH<sub>pzc</sub> consists in placing 50 ml of the distilled water in closed vials and then adjusting the pH of each (values between 2 and 12) by addition of NaOH (0.1M) or HCl (0.1M) solution. 25 mg of PACK material was added to each vial. The suspension was agitated at room temperature around 24 hours, and then the final pH was determined.



### 2.4.3. Scanning electron microscopy (SEM)

Scanning electron microscopy (SEM) of PACK biosorbent before biosorption was visualized using Hitachi S-3000 N SEM at 10 kV and various magnifications, 500 and 20,000. From the SEM, it is possible to see the topography surface of the material.

## 2.5. Adsorption studies

### 2.5.1. Adsorption kinetics

The effect of the contact time on the adsorption of methylene blue (MB) on the PACK material was considered in this study at the natural pH, 6.5. Experiments were performed, adding a given amount of biosorbent (50 mg) in 200 ml of dye solutions of known concentrations (100 and 150 mg/L) in two conical flasks (500 ml) with continuous stirring (250 rpm) at  $25 \pm 2^\circ\text{C}$ . After withdrawing samples at fixed time intervals and centrifugation, the supernatants were analyzed for residual MB. The amount of dye adsorbed  $Q_t$  (mg/g) at time  $t$ , was calculated according to Eq. 1.

$$Q_t = \frac{(C_0 - C_t)V}{m} \quad (1)$$

Where  $C_0$  and  $C_t$  (mg/L) are the dye concentrations in the solution at the beginning and after time  $t$ ,  $V$  (L) and  $m$  (g) are respectively the volume of the solution and the mass of dry biosorbent.

### 2.5.2. Kinetics modeling

Kinetics provide information on the adsorption process and the type of solute migration from the liquid phase to the solid phase. For this purpose, some models were considered to fit experimental data, the pseudo-first-order, pseudo-second-order (PSO) (PFO) [40, 41] and pseudo- $n^{\text{th}}$  order (PNO) [42, 43]. The models formulas and their parameters are gathered in Table 2.

**Table 2:** Adsorption kinetics models used in this work and their parameters.

Kinetics models	Equation	Parameters
Pseudo-first order	$Q_t = Q_e(1 - e^{-k_1 t})$	$Q_e$ (mg g <sup>-1</sup> ) and $Q_t$ (mg g <sup>-1</sup> ) refer to the amount of dye adsorbed at equilibrium and at time $t$ (min) respectively. $k_1$ (L min <sup>-1</sup> ) is the equilibrium rate constant of the pseudo-first-order equation
Pseudo-second order	$Q_t = \frac{k_2 Q_e^2 t}{1 + k_2 Q_e t}$	$k_2$ (L min <sup>-1</sup> ) is the equilibrium rate constant of the pseudo-second-order equation
Pseudo-n <sup>th</sup> order	$Q_t = Q_e - [(n-1)k_n t + Q_e^{(n-1)}]^{1/n}$	$k_n$ is a constant and $n$ is the biosorption reaction order

### 2.5.3. Adsorption isotherms

The adsorption isotherm is a representative characteristic of the thermodynamic equilibrium between the adsorbent and the adsorbate [29]. It is very useful for understanding the adsorption mechanism; it gives information about the affinity, the binding energy between the adsorbate and the adsorbent, and about the adsorption capacity. Experiments were carried out in a series of Erlenmeyer flasks (50 ml) placed on a multi-station magnetic stirrer shaken at 250 rpm and loaded with 50 ml of MB at different concentrations (in the range 50 to 1100 mg L<sup>-1</sup>). 25 mg of the PACK material was added to each Erlenmeyer; the mixture was stirred for 24 hours, and the process was

repeated for two temperatures 20 and 30 °C. Adsorption capacity  $Q_e$  ( $\text{mg}\cdot\text{g}^{-1}$ ) was calculated based on Eq. (2).

$$Q_e = \frac{(C_0 - C_e)V}{m} \quad (2)$$

Where  $C_0$  and  $C_t$  ( $\text{mg}/\text{L}$ ) are the dye concentrations in the solution at the beginning and after time  $t$  respectively,  $V$  (L) is the solution volume and  $m$  (g) is the dry adsorbent mass.

#### 2.5.4. Isotherm modeling

Mathematical modeling of isotherms provides a relationship between solute concentration in solution and adsorbed quantity per unit mass of adsorbent [44]. The two most commonly used two-parameter models are the Langmuir and Freundlich models; the Dubinin Radushkevich (D-R) model was also considered. However, to go a little further in the understanding of adsorption mechanisms, three-parameter models like the sips model and the Redlich-Peterson model were also considered. Table 3 describes these isotherm models and their parameters.

**Table 3:** Adsorption isotherm models adopted in this work and their parameters.

Isotherm	Equation	Parameters
Langmuir	$\frac{Q_e}{Q_m} = \frac{K_L C_e}{1 + K_L C_e}$	<p><math>Q_e</math> (<math>\text{mg g}^{-1}</math>) is the amount of MB adsorbed per unit mass of adsorbent</p> <p><math>C_e</math>. (<math>\text{mg L}^{-1}</math>)the equilibrium dye concentration in solution</p> <p><math>Q_m</math>(<math>\text{mg g}^{-1}</math>) the monolayer capacity of the adsorbent</p> <p><math>K_L</math> the Langmuir constant</p>

Freundlich	$Q_e = K_F C_e^{1/n}$	$K_F$ and $n^{-1}$ are empirical constants indicative of sorption capacity and sorption intensity, respectively
Sips	$\frac{Q_e}{Q_m} = \frac{(K_S C_e)^m}{1 + (K_S C_e)^m}$	$K_S$ is (L mg <sup>-1</sup> ) the Sips constant m the exponent of the Sips model
Redlich-Peterson	$Q_e = \frac{k_R C_e}{1 + \alpha_R C_e^{\beta_R}}$	$k_R$ (L g <sup>-1</sup> ) is the Redlich–Peterson (R-P) isotherm constant $\alpha_R$ (L mg <sup>-1</sup> ) is also having a constant unit of $\beta_R$ is an exponent
Dubinin-Radushkevich	$Q_e = Q_{DR} \exp(-k_{DR} \varepsilon^2)$	$Q_{DR}$ is capacity of the adsorbent (mg/g) $K_{DR}$ is the activity coefficient (mol <sup>2</sup> KJ <sup>2</sup> ) $E_{DR}$ The biosorption energy (kJ mol <sup>-1</sup> ), ( $E_{DR} = (2K_{DR})^{-0.5}$ ) $\varepsilon$ stands for constant related to the biosorption energy ( $\varepsilon = RT \ln(1 + 1/C_e)$ )

## 2.6. Statistical physics

In an attempt to understand the adsorption phenomenon by means of statistical physics processing, the following hypotheses were assumed: (i) it was considered that a variable amount of solute molecules were adsorbed on interstitial  $N_m$  sites of the adsorbent (unit mass); (ii) adsorption reaction of solute molecule (A) at an interstitial site (S) must include a stoichiometric coefficient  $n$  according to the following reaction[45]:



Depending on the value of  $n$ , two different ways of adsorption of the solute on the adsorbent can be distinguished. If  $n$  is less than 1, only a fraction of solute molecules are adsorbed; it consists in multi-anchorage adsorption. In the second case, if  $n$  is greater than 1, it is an interstitial site filled with more than one molecule; this case corresponds to multi-molecular adsorption [46].

Statistical physical simulation is used in this study to explain the adsorption of MB in the PACK material. For a system in specific physical conditions, we used the large canonical partition function  $Z_{gc}$  which describes the microscopic state:

$$Z_{gc} = \sum_{N_i} e^{-\beta(-\varepsilon - \mu)N_i} \quad (4)$$

Where  $N_i$  is the receptor site occupation state,  $\mu$  is the chemical potential,  $\varepsilon_i$  is the receptor site adsorption energy, and  $\beta$  is defined as  $1/k_B T$  (where  $T$  is the absolute temperature and  $k_B$  is the Boltzmann constant).

The MB adsorption isotherms are simulated by three different models of statistical physics, monolayer single-energy, monolayer two-energy, and double-layer two-energy models [45].

The three models are summarized in the following table (Table 4).

**Table 4:** Grand canonical partition function and equation of the three models of statistical physics

Model	Grand canonical partition function	Equation
1	$z_{gc} = \sum_{N_i=0.1} 1 + e^{\beta(\varepsilon+\mu)N_i}$	$Q = \frac{n \cdot Nm}{1 + \left(\frac{C_{1/2}}{C_e}\right)^n}$
2	$z_{gc} = (1 + e^{\beta(\varepsilon_1+\mu)})^{N_{1m}} + (1 + e^{\beta(\varepsilon_2+\mu)})^{N_{2m}}$	$Q = \frac{n1 \cdot Nm1}{1 + \left(\frac{C1}{C_e}\right)^{n1}} + \frac{n2 \cdot Nm2}{1 + \left(\frac{C2}{C_e}\right)^{n2}}$
3	$z_{gc} = \sum_1 1 + e^{\beta(\varepsilon+\mu)} + e^{2\beta(\varepsilon+\mu)N_m}$	$Q = n \cdot N_M \cdot \frac{\left(\frac{C}{C1}\right)^n + 2 \cdot \left(\frac{C}{C2}\right)^{2n}}{1 + \left(\frac{C}{C1}\right)^n + 2 \cdot \left(\frac{C}{C2}\right)^{2n}}$

In model 1, it is assumed that the adsorption of the dye takes place by a monolayer single-energy model [47]. The receptor sites can interact with several dye molecules. The quantity adsorbed  $Q_e$  as a function of  $C_e$  is given by Eq.1 in the Table 4 [48].

Where the parameter  $n$  represents the number of MB molecules captured per active site of PACK, the density of the adsorbent receptor sites is  $N_m$  and the concentration at half-saturation is  $C_{1/2}$ .

In model 2, monolayer two-energy, the adsorption of MB is assumed on two different sites of PACK with two different energy,  $E_1$  for the first site and  $E_2$  for the second site. The receptor sites can interact with a variable number of MB molecules,  $n_1$  with the first site (type one) and  $n_2$  with the second site (type two). The evolution of  $Q_e$  as a function of  $C_e$  is given by the Eq. 2 in Table 4. In the equation 4,  $N_{m1}$  and  $N_{m2}$  are the first and the second type densities of adsorbent receptor sites respectively,  $C_1$  and  $C_2$  are the concentration at half-saturation of the first and of the second receptor site.

For model 3, namely double-layer two-energy model,  $E_1$  and  $E_2$  are related to the first and the second layer, with the second layer having less energy than the first [49]. From this, the quantity  $Q_e$  adsorbed as a function of  $C_e$  is given by Eq.3 in Table 4 [50].

Where  $C_1$  and  $C_2$  are the concentrations of the first and second layers at half-saturation, respectively.

## 2.7. Statistical assessment of equilibrium parameters

Evaluation of nonlinear adsorption isotherms by the error function ( $F_{\text{error}}$ ) represented by Eq.5 was conducted. This function allows to compare the experimental data point by point with those obtained by the adjusted model. Models with a low  $F_{\text{error}}$  value are the most appropriate for describing the experimental behavior:

$$F_{\text{error}} = \sqrt{\sum_1^P \left( \frac{1}{P-1} \right) \left( \frac{Q_{i,\text{mod}} - Q_{i,\text{exp}}}{Q_{i,\text{exp}}} \right)^2} \quad (5)$$

Where  $Q_{i,\text{mod}}$  is the adsorption capacity of the adsorbent given by the model;  $Q_{i,\text{exp}}$  is the experimental adsorption capacity, and  $P$  is the number of experimental points [51].

## 2.8. Parameters governing adsorption phenomena

### 2.8.1. The effect of the initial pH on adsorption

The pH is a very important factor in the adsorption phenomenon. The surface charge and the distribution of ions of the material may change significantly with pH. The effect of pH on the adsorption of MB on PACK has been studied at different initial pH (in the range 3 to 12). The pH adjusted to the desired values with HCl (1 M) and NaOH (1 M). The initial concentration of MB

was 160 mg/l (stock solution). The other parameters, such as the tank volume, temperature, stirring speed, and adsorbate mass were  $V = 50\text{ml}$ ,  $T = 25 \pm 2^\circ\text{C}$ , stirring speed = 250 rpm,  $m_{\text{PACK}} = 25\text{mg}$ .

### **2.8.2. The effect of humic acid on the adsorption**

Textile wastewater, as it is known contains variable concentrations of organic and inorganic ions, mainly cations and anions such as nitrates, chlorides, sulfates, carbonates and hydrogenocarbonates. In this part, the effect of humic acids on adsorption was examined to better understand their effect on the adsorption of MB on the adsorbent. Indeed, humic acids can be found in nature in significant quantities. Therefore, different humic acid quantities (5, 20, 30, and 50 mg) were added in 50 ml of a solution of MB at 800 mg/L in the presence of 25 mg of adsorbent. After stirring until the equilibrium time the results obtained were compared to the result of adsorption without humic acid.

### **2.8.3. Effect of the biosorbent dose on biosorption**

The ratio of biosorbent-solution is an important factor in assessing the biosorption capacity of the material biosorbent. In order to examine the impact of the initial dose of PACK biosorbent on the MB dye, a range of doses between 10 to 100 mg of adsorbent was examined in the presence of 400 mg/L initial dye concentration.



### 3. Result and discussions

#### 3.1. Characterization of the adsorbent

##### 3.1.1. Infrared spectroscopy (FT-IR) interpretation of PACK material

The FT-IR spectrum of the PACK material before adsorption (Figure 2) gives certain absorption bands that can be defined by the following functional groups. A broad absorption band of about 3600–3000  $\text{cm}^{-1}$  which characterizes the vibration of elongation of hydrogen from hydroxyl groups  $\text{OH}^-$  (phenol, alcohols, or carbonyls). It can also correspond to the vibration of elongation of the  $\text{OH}^-$  groups of cellulose (lignin and pectin). Another band at 2360  $\text{cm}^{-1}$  may correspond to the presence of a = N-H bond. The characteristic band between 1640  $\text{cm}^{-1}$  and 1530  $\text{cm}^{-1}$  can be identified as the carboxylic group bonding ionic ( $\text{COO}^-$ ) elongation vibrations and can be assigned to the C=C aromatic stretching. The characteristic band at 1380  $\text{cm}^{-1}$  can be related to the C-H and O-H deformation vibration in hydroxyls, phenols, methyl and olefins. For the comparison between the two FT-IR spectra before and after adsorption, similar peaks of different intensity were observed with the appearance of new peaks such as: at 1321  $\text{cm}^{-1}$ , a characteristic band attributed to the valence vibrations of the aliphatic C-H groups existing in the structure of the MB. The peak at 1120  $\text{cm}^{-1}$  corresponds to the mode of vibration and elongation of the aromatic groups C-H existing in the structure of the MB; another band at 665  $\text{cm}^{-1}$  may correspond to the presence of a C-S bond existing in the structure of the MB. These peaks confirmed the adsorption of MB onto the PACK material.

### **3.1.2. The Point of Zero Charge**

From the graph presented in Figure 3, the  $pH_{pzc}$  of adsorbate was equal to 8.3, which means that the surface of PACK was positively charged when the pH of the solution was lower than 8.3 and negatively charged when the pH of the solution was higher than 8.3.

### **2.1.3 Scanning electron microscopy (SEM)**

It can be seen the SEM surface images of PACK in Figure 4. The images obtained at a one and ten micron-meter scale showed a heterogeneous surface morphology composed of many cavities (micro-pores) of different sizes. This irregular morphology of the material can facilitate the sorption of MB, and we can consequently assume that the PACK material represented an appropriate morphological profile for the adsorption of dyes [52].

### **3.2. Kinetics analysis**

Two initial concentrations, 100 and 150 mg/L were considered. As expected, the adsorption capacity of PACK increased with the increase of the initial dye concentrations. As shown in Figure 5, biosorption increased rapidly during the first 90 minutes, before reaching equilibrium, for both considered concentrations. According to adsorption kinetics, more information on the adsorption mechanism (adsorbent/adsorbate) or in another way the transfer of a solute from the liquid phase to the solid phase can be provided. For this purpose, several kinetic models, namely the pseudo-first kinetic model (PFO), pseudo-second-order model (PSO) and pseudo- $n^{\text{th}}$  order model (PNO) were applied to explain the adsorption mechanism. Figure 5 and Table 5 shows the parameters obtained with the different kinetic models for the adsorption of MB onto the PACK material. It can be seen from this table, that all models accurately fitted experimental data, leading to

coefficients of correlation between 0.95 and 0.997; however, the values of the coefficients of correlation given by the PSO model were slightly lower than those given by PFO and PNO (Table 5). In addition, theoretically calculated  $Q_t$  (373.87mg/g and 604.37mg/g) values from the PNO model agreed very well with the experimental  $Q_t$  (374mg/g and 547 mg/g) values, for both 100 and 150 mg/L dye respectively, if compared to those obtained by the PFO and PSO models. Moreover, the rates constants ( $K_1$ ,  $K_2$ , and  $K_n$ ) for all models, declined in a significant way when the initial MB concentration increased from 100 to 150 mg/L. Furthermore, the coefficient  $n$  of the PNO increased from 1.31 to 2.5 for 100 and 150 mg/L initial dye amount, respectively. From this, it can be inferred that the order of the reaction was greater than 2 for 150 mg/L dye. In summary, according to the modeling results, it can be considered that experimental data were most accurately fitted in this order PNO > PFO > PSO models.

**Tableau 5:** Kinetic parameters and correlation coefficients for nonlinear regression of PFO, PSO and PNO models for the adsorption of MB onto PACK at room temperature.

Material	Model	Parameters	100	150
PACK	PFO	$Q_{exp}$	<b>374</b>	<b>547</b>
		$Q_e$	368.88	528.05
		$K_1$	0.153	0.093
		<b><math>R^2</math></b>	<b>0.994</b>	<b>0.9494</b>
	PSO	$Q_e$	391.46	572.70
		$K_2 \cdot 10^{+4}$	6.94	2.60
		<b><math>R^2</math></b>	<b>0.989</b>	<b>0.986</b>
	PNO	$Q_e$	373.87	604.37
		$k_n$	0.029	1.16E-05
		$n$	1.31	2.50
<b><math>R^2</math></b>		<b>0.997</b>	<b>0.986</b>	

### 3.3. Isotherm analysis

Adsorption isotherm is very important both theoretically and practically to optimize an adsorption system; the corresponding results are shown in Figure 6. The two isotherms showed an L-type appearance (Langmuir type). The L shape of an adsorption isotherm means that there is no strong competition between the solvent and the adsorbent to occupy the adsorption sites; consequently, the affinity between the adsorbate and the adsorbent is relatively high. This was confirmed by the modeling of the adsorption isotherms (the affinity between the adsorbent and the adsorbate increased when the value of the  $K_L$  constant decreased). The maximum values of the adsorption capacity at equilibrium were 1285.34 mg/g and 1528.02 mg/g for the two temperatures, 20 and 30 °C respectively. According to the results obtained, there was a positive temperature effect on the adsorption of MB-PACK. To properly define the sorption process for the elimination of dyes from the effluent, the most appropriate correlation for the equilibrium data should be determined. Isotherm models cited in Table 3 were used and the fitting was carried out using the Marquard-Levenberg program. It is clear that the adsorption capacity increased with increasing equilibrium concentration of MB and reached saturation progressively for all tested models. In the case of the two-parameter models, both Langmuir and Dubinin-Radushkevich isotherm models were the most appropriate to describe experimental data. The calculated parameters are provided in Table 6 and the corresponding graphs are shown in Figure 6. It can be seen from Table 6, that the values of the coefficient of determination,  $R^2$ , obtained for Langmuir and Dubinin-Radushkevich (D-R) were closer to 1.00, if compared to those given by the Freundlich model. From this, the biosorption of the MB molecules was localized without adsorbate-adsorbent interactions [53]. The adsorption capacity for Langmuir and Dubinin-Radushkevich (D-R) (Table 6) using nonlinear regression was found to increase from 1219.83 mg/g to 1522.34 mg/g and from 1096.76 mg/g to 1419.95 mg/g

for Langmuir and Dubinin-Radushkevich (D-R) respectively, namely close to those found experimentally for an increase in temperatures from 20 to 30 °C. The biosorption constant,  $K_L$ , decreased from 256 L/mg to 219 L/mg for the Langmuir model as temperatures varied from 20 to 30 °C. Besides, from Table 6, it can be evaluated that the adsorption behavior of MB onto PACK fitted very well with the Langmuir isotherm model, better than the Freundlich model as reflected by the correlation coefficients and the  $F_{\text{error}}$  of the experimental data.

On the other hand, the three-parameter models, R-P, and Sips Eqs. were also applied to examine the adsorption of MB. The calculated isotherm parameters and their corresponding coefficient of determination  $R^2$  values are also given in Table 6. The high values of  $R^2$  and the low values of  $F_{\text{error}}$  for the the R-P model suggest the applicability of this model to represent the equilibrium sorption of MB on PACK in comparison to the sips model. Several studies showed that the R-P isotherm was more accurate than the Langmuir and Freundlich isotherms as it contains three unknown parameters. Indeed, the Langmuir and Freundlich isotherms can result from the R-P isotherm. Indeed, for  $\beta_R = 1$ , the R-P Eq. becomes the Langmuir isotherm and for  $\beta_R = 0$ , it is closer to the Freundlich Eq. Otherwise, the Sips model is the combination of Langmuir and Freundlich models. From this and Table 6, it is not surprising that the adsorption capacity obtained from the Langmuir, Sips and R-P models could be more realistic than that from the Freundlich Eq. Moreover, the Redlich–Peterson (R–P) model was close to the Sips and Langmuir isotherms in the range of studied temperatures (when  $m$  and  $\beta$  value approach to 1). The isotherm constant  $\alpha_R$  decreased with temperature; while inversely, the  $\beta_R$  exponent increased with temperature. From Table 6, we can note that the  $\beta_R$  values were close to unity (i.e. the Langmuir model was appropriate to describe experimental data). Finally and regarding the statistical parameters given by  $F_{\text{error}}$  and  $R^2$ , it can be noted that the R-P model was the most suitable to describe experimental

data owing to its low  $F_{\text{error}}$  and the high  $R^2$ , compared to the other models in the range of temperatures considered.

In addition, The Dubinin-Radushkevich (D-R) isotherm model provides information about whether the adsorption process is physical or chemical depending on its measured  $E_{\text{DR}}$  parameter; if the  $E_{\text{DR}}$  value is between 8-16  $\text{KJmol}^{-1}$  the adsorption process is a chemisorption process and if  $E_{\text{DR}} < 8 \text{ KJ mol}^{-1}$  it is a physisorption process) [54]. It is worth noting that  $E_{\text{DR}}$  is independent of the temperature; it depends on the nature of the adsorbate-adsorbent couple [55]. From the D-R model, the sorption energy  $E_{\text{DR}}$  was  $0.65 \text{ KJ mol}^{-1}$ , namely within the range of values for physical adsorption reactions. This result suggested that the biosorption process of the MB dye onto PACK biosorbent was physical in nature because the biosorption energy was less than  $8 \text{ KJ mol}^{-1}$ .

**Tableau 6.** Langmuir. Freundlich. Sips, Redlich-Peterson (R-P) and Dubinin-Radushkevich (D-R) constants for the adsorption of MB onto PACK

		20°C	30°C
Langmuir	<b><math>Q_{\text{exp}}(\text{mg/g})</math></b>	<b>1285.34</b>	<b>1528.02</b>
	$Q_{\text{m}}(\text{mg/g})$	1219.23	1522.34
	$K_{\text{L}}(\text{L/mg}) \times 10^3$	0.256	0.219
	<b><math>F_{\text{error}}</math></b>	<b>0.365</b>	<b>0.926</b>
	<b><math>R^2</math></b>	<b>0.949</b>	<b>0.992</b>
Freundlich	1/n	0.22	0.24
	$K_{\text{F}}(\text{mg/g})(\text{L/mg})^{1/n}$	381.59	414.21
	<b><math>F_{\text{error}}</math></b>	<b>0.857</b>	<b>0.950</b>
Sips	<b><math>R^2</math></b>	<b>0.843</b>	<b>0.877</b>
	$Q_{\text{m}}(\text{mg/g})$	1176.18	1502.57
	$K_{\text{S}}(\text{L/mg})$	0.299	0.235
	m	1.26	1.08
	<b><math>F_{\text{error}}</math></b>	<b>0.471</b>	<b>0.329</b>
	<b><math>R^2</math></b>	<b>0.948</b>	<b>0.992</b>

Redlich-Peterson	$k_R(L/g)$	341.261	343.545
	$\alpha_R(L/mg)$	0.325	0.238
	$\beta_R$	0.969	0.989
	$F_{error}$	<b>0.386</b>	<b>0.322</b>
	$R^2$	<b>0.9477</b>	<b>0.991</b>
Dubinin-Radushkevich	$Q_{DR}(mg/g)$	1096.76	1419.95
	$K_{DR} \cdot 10^6$	<b>0.77</b>	1.20
	$R^2$	<b>0.983</b>	<b>0.988</b>

### 3.4. Statistical physics

According to the results obtained by the three statistical models used in this study (Figure 7), it seems that the two-energy monolayer model led to the most accurate modeling results according to the  $R^2$  values obtained (Table 7) for the two temperatures tested (20 and 30 °C). The two other models were therefore not further considered in the interpretations of the different parameters since they gave lower  $R^2$  values.

**Table 7:** Results of calculations of the various anchoring parameters

	Model 1		Model 2		Model 3			
	20°C	30°C	20°C	30°C	20°C	30°C		
<b>n</b>	1.262	1.079	<b>n<sub>1</sub></b>	1.775	3.553	<b>n</b>	1.26	1.078
<b>Nm</b>	931.99	1392.80	<b>Nm<sub>1</sub></b>	548.26	101.82	<b>Nm</b>	932.48	1392.73
<b>C<sub>1/2</sub></b>	3.3464	4.259	<b>C<sub>1</sub></b>	2.433	1.289	<b>C<sub>1</sub></b>	3.347	4.259
<b>R<sup>2</sup></b>	0.9778	0.9966	<b>n<sub>2</sub></b>	1.957	1.025	<b>C<sub>2</sub></b>	732.22	753.18
			<b>Nm<sub>2</sub></b>	173.94	1146.87	<b>R<sup>2</sup></b>	0.9778	0.9966
			<b>C<sub>2</sub></b>	113.86	8.326			
			<b>R<sup>2</sup></b>	0.9873	0.9996			

### 3.4.1 Steric parameters $n_1$ and $n_2$

The steric parameters  $n_1$  and  $n_2$  of the two-energy monolayer model are very useful to propose an adsorption mechanism. Three cases are possible concerning the value of  $n$ ; It can be less than 0.5,  $0.5 < n < 1$ , and the last case  $n > 1$ . In the case where  $0.5 < n < 1$ , the molecules of the solute can orient themselves on the surface of the adsorbate in two different ways, parallel and non-parallel with a certain centering for each type of orientation. The case where  $n < 0.5$  corresponds to an adsorption where the molecules of the solute are oriented in a parallel way on the surface of the adsorbent.  $n > 1$  indicates that the molecules are anchored vertically on a site, leading to an aggregation. It is noted that the anchoring of the molecule on the adsorbent depends on its size, its structure and also on its charge. The results of calculations of the various anchoring parameters are summarized in the Table 7. It should be observed from the Table 7 that at a temperature equal to 20 °C the value of  $n$  was = 1.775, namely between  $n = 1$  (only one molecule is anchored at one site) and  $n=2$  (two molecules are anchored at one site). The following Eq. (6) was considered to measure the percentage of MB molecules with a mono anchorage (noted with  $X$ ), and with two anchorage (noted with  $(1-X)$ ).

$$n = X \times 1 + (1 - X) \times 2 \quad (8)$$

For the first  $n$  ( $n_1=1.775$ ), it was found that 22.5% of the sites (type one) were occupied by one molecule, and the rest of the sites were occupied by two molecules (77.5%) [56]. Regarding the second  $n$  ( $n_2=1.957$ ) at 293 K, it was found that 4.3% of the sites (type two) were occupied by one molecule, while the majority of the sites were occupied by two molecules (95.7%).

The values of  $n_1$  increased from 1.775 for 20 °C to  $n_1 = 3.553$  °C for 30 °C, showing that the arrangement of the MB molecules on the surface of the adsorbent was affected by the temperature.

It can easily be concluded that when the temperature increases, the number of molecules adsorbed



per site decreases. On the contrary, the  $n_2$  values decreased from 1.956 for 20 °C to  $n_2 = 1.025$  for 30 °C. This shows that the percentage of sites (type two) that anchor two molecules decreased from 95.7% to 2.5%. This can possibly be due to the increase in temperature that eliminated the bindings between the MB dye molecules. It should be noted that this observation deserves further study concerning the different functions existing on the surface of the adsorbent material capable of creating an interaction or anchoring, since the sites  $n_1$  and  $n_2$  are not physically defined, which complicates the conclusion. It can be noticed that  $n_1$  increases and  $n_2$  decreases when the temperature increases, showing an exchange or a compromise between the sites  $n_1$  and  $n_2$  concerning the adsorbed molecules when the temperature varied.

Concerning the  $N_{mi}$  parameter, it is defined as the number of receptor sites occupied at saturation, with  $N_{m1}$  the number of receptor of the type one of occupied sites and  $N_{m2}$  is the number of receptor of the type two of occupied sites. From Table 7, it can be noted that the increase in temperature caused a decrease for the first type of density  $N_{m1}$  and an increase for the second type  $N_{m2}$ . Note that each density for each different site varied with an inverse trend compared to the number of MB products captured. In fact, the reduction in the number of MB molecules captured per site created free space for the PACK biosorbent that contribute to the adsorption producing an increase in the number of anchorages ( $n' = 1 / n$ ), followed by an increase in density  $N_{mi}$ .

### **3.5. Study of the effect of the parameters governing adsorption**

#### **3.5.1. The effect of pH**

In Figure 8, the influence of the initial pH is shown. It can be observed a very low adsorbed quantity for a very low pH range compared to the  $pH_{pzc}$  and this may be due to the repulsion force between the positively charged material and the MB cationic dye. The adsorbed quantity increased as the

pH increased towards the  $pH_{pzc}$  until the maximum adsorbed quantity was obtained at the natural pH, 6.5. This increase can be explained by the increase in the negative charges on the PACK surface due to the increase in pH. The availability of negative charges on the PACK biosorbent surface favors the adsorption of the cationic dye MB [38]. Above the natural pH, there was a color change of the solution from blue to green color, associated with a maximum wavelength change from 664 nm to 570 nm with emergence continues of the wavelength of the MB color. This color alteration can be attributed to secondary chemical reactions between the MB dye and the PACK modifying material in a range of pH above the natural pH, which caused the changes in the MB dye's ionic character.

### **3.5.2. The effect of the temperature**

25 mg of PACK adsorbent was added to 50 ml of a MB solution at a concentration of 800 mg/L at the natural pH. The suspension was stirred for the equilibrium time. The protocol was repeated at 20, 30 and 40 °C. Figure 6 showed that the adsorption capacity increased with increasing temperature. As the temperature increases, it is usual for the viscosity of a solution to decrease, thus increased the mobility of the adsorbate as well, and thus an increase in the penetration of the MB molecules through the pores of the PACK is expected. At the same time, there could be more chemical interaction between the adsorbate and the surface of the biosorbent [57, 58]. Tan et al [59] reported a similar pattern in the adsorption of MB on activated oil palm fiber carbon.

### **3.5.3. The humic acid effect**

According to the results obtained (Figure not shown) and compared to the maximum quantity adsorbed for a concentration of 400 mg/L of MB in the absence of humic acid (total elimination), there was a stable negative effect for each addition of different amounts of humic acid. This result

can be explained by the adsorption competition between the cations of the humic acid in the solution and the MB dye on the PACK material. However, Figure 9 demonstrates the ability of the PACK to maintain high MB removal at high ionic strength. Therefore, Textile wastewater treatment, which may contains such components, may be effective by this material.

#### **3.5.4. The Effect of the biosorbent dose on biosorption**

The effect of the adsorbent dosage on the adsorption capacity of BM dye is displayed in **Figure 9**. It showed a reduction in the adsorption capacity per unit mass of the adsorbent for a rise in the mass of the adsorbent, which was however accompanied by an increase in the rate of biosorption, leading to a greater removal of the pollutant. This can be due to an increase in the available surface area and an increase in the number of active sites on the surface of the PACK material [8].

#### **3.6. Desorption study**

In order to determine the recovery rate of the PACK product, the desorption of the adsorbed MB dye after adsorption was carried out in three different solutions, 0.1 M HCl, 0.1 M NaOH, and 0.1 M ethanol; the corresponding results are shown in the **Figure 10**. For this purpose, after MB adsorption experiments at an initial concentration of 400 mg/L, the solid phase (PACK) was separated from the solution and placed in HCl, NaOH, or ethanol and stirred until reached the equilibrium time for the desorption. At equilibrium the quantities of MB desorbed in the three solutions were determined. Using HCl, the amount of desorbed dye was recovered at the highest rate (52.88%), if compared to the two other solutions, NaOH and ethanol; it is probably related to the breakage of the physical bonds (van der Waals) between the MB dye and the PACK product at acidic pH. However, nearly half of the adsorbed dye was not retrieved. This may be due to the loss of adsorbent material during the transition from the absorption process to the desorption

process and also to the possibility that the dye which diffused into the particle or chemically bound was not fully recovered [37].

### **3.7. Proposed mechanism of adsorption of MB onto the PACK material**

Based on the findings of the isoelectric point, the pH effect, the FT-IR analysis and the results of the D.K isotherm model the following assumptions can be drawn. The adsorption mechanism of MB onto the PACK can be supposed to be globally guided by electrostatic interactions (physical adsorption) between the adsorbent which becomes negatively charged, each time the pH is switched from acidic to its  $pH_{pzc}$ , and the positively charged dye; also due to weak hydrogen bonds between the nitrogen atoms present in the molecules of MB and the hydrogen atoms in the functional groups available on the surface of the adsorbent, as well as due to cations exchange.

In addition and according to the analysis result of the FTIR, a  $\pi$ - $\pi$  interaction can also occur in the process of biosorption MB\_PACK. The MB dye is a polycyclic aromatic compound containing therefore several benzene rings; benzene rings were also confirmed in the biosorbent through FT-IR analysis which revealed the presence of a C = C aromatic stretch. In addition, since these benzene rings are electron-rich areas, they can produce a donor-acceptor stacking interactions between MB and PACK. The description of the MB biosorption process is shown in the **Figure 11**.

### **3.8. Comparison of the MB adsorption capacity on some adsorbents**

The comparison of the maximum adsorption capacity of some adsorbents on methylene blue is displayed in Table 7. It should be noted that the adsorption capacity of modified powder of *Acorus calamus* on MB appeared to be greater than that of other adsorbents, including activated carbon. The potential of PACK, an easily available and low-cost material, to be used as an alternative biosorbent material for the removal of a dye, MB, from aqueous solutions was therefore confirmed.

**Table 8.** Comparison of maximum monolayer adsorption of MB on some adsorbents in the literature

Adsorbent	Adsorption Capacity (mg/g)	References
Bentonite (alginate beads)	2024	[60]
PACK	1500	This study
<i>Ziziphus jujuba</i> stones (BZJS1) (alginate beads)	737.13	[39]
pectin from orange industry residues (alginate beads)	398.40	[34]
graphene oxide	357.14	[61]
OP-H <sub>3</sub> PO <sub>4</sub>	307.63	[38]
Palm fiber- activated carbon	278	[59]
Activated carbon from Mangosteen fruit peel	230	[62]
Wild carob-activated carbon	218	[63]
Chitosan flakes-activated carbon	144	[64]
Fe <sub>3</sub> O <sub>4</sub> particle	20.40	[65]

#### 3.5.4. Thermodynamic analysis

Thermodynamic parameters reflect the possibility and the spontaneity of a biosorption process. Parameters such as the free energy change ( $\Delta G$ ), the enthalpy change ( $\Delta H$ ) and the entropy change ( $\Delta S$ ) can be estimated from the variations of the equilibrium constants with the temperature.

The free enthalpy change of a biosorption reaction is given using Eq.9 as reported by Milonjic [66]:

$$\Delta G^{\circ} = -RT\ln(\rho Kc) \quad (9)$$

Where  $\Delta G^{\circ}$  is the free energy change ( $\text{kJ}\cdot\text{mol}^{-1}$ ), R the universal gas constant ( $8.31\text{J}\cdot\text{mol}^{-1}\text{K}^{-1}$ ), T is the absolute temperature (K), Kc the thermodynamic equilibrium constant ( $\text{L}\cdot\text{g}^{-1}$ ) and  $\rho$  the water density ( $\text{g}\cdot\text{L}^{-1}$ ).

$\Delta H^\circ$  and  $\Delta S^\circ$  values of the biosorption mechanism were calculated from Van't Hoff Eqs.10 and 11:

$$\ln(\rho K_c) = -\frac{\Delta H^\circ}{RT} + \frac{\Delta S^\circ}{R} \quad (10)$$

$$K_c = \frac{Q_e}{C_e} \quad (11)$$

$\Delta H$  and  $\Delta S$  can be then deduced from the slope ( $\Delta H/R$ ) and the intercept ( $\Delta S/R$ ) of the plot of  $\ln(\rho K_c)$  versus  $1/T$ .

In general, change in free energy values between  $-20$  and  $0 \text{ kJ mol}^{-1}$  is reported for physisorption, while these values are in a range of  $-400$  to  $-80 \text{ kJ mol}^{-1}$  for chemisorption processes [63, 66].

Table 9 gives the calculation of the thermodynamic parameters. The value obtained for the free energy was about  $-20 \text{ KJ/mol}$  for our material in the range of temperature from  $20$  to  $40^\circ\text{C}$  indicating that adsorption took place physically [63]. This result confirms that found with the Dubinin-Radushkevich (D-R) model. Increased randomness at the interface of the solid solution during MB biosorption on the biosorbent was demonstrated by the positive value of the entropy change.

**Table 9:** Calculation of the thermodynamic parameters

Température (K)	Kc (L/g)	$\Delta H^0(\text{KJ/mol.})$	$\Delta S^0(\text{J/mol.K})$	$\Delta G^0(\text{KJ/mol.})$
293	6.36	54.703	259.72	-21.32
303	14.60			-24.14
313	26.65			-26.65

#### 4. Conclusion

New material was obtained by physical treatment of a low cost and abundant biosorbent, powder of *Acorus calamus*, with  $H_2SO_4$  and  $KMnO_4$ , denoted by PACK material. This material had a high maximum experimental capacity, 1285.34 and 1528.02 mg/g at 20 °C and 30 °C, respectively. Isotherm models with two and three parameters, namely Langmuir, Freundlich, Dubinin-Radushkevich (D-R), Redlich-Peterson and Sips were applied to fit experimental data. Redlich-Peterson isotherm indicated better fit compared to the Langmuir, the Freundlich and the Sips isotherm models. According to the results of the kinetic modeling of MB adsorption onto the PACK material, the pseudo- $n^{th}$  order model led to a better adjustment of the experimental results, if compared to both the pseudo-first and pseudo-second-order kinetics models. As per the  $R^2$  values obtained from the simulation of the results with the three advanced models, monolayer single-energy, monolayer two-energy and double-layer two-energy models as statistical physics models, the two-energy monolayer model led to the best result of the processes of MB adsorption onto the PACK material. From this, it can be assumed that the adsorption of MB onto PACK occurred on two different sites of energy (type one and two); each site can interact with a variable number of MB molecules ( $n$ ),  $n_1$  interact with type one and  $n_2$  with type two.

Regarding desorption, the PACK product gives a slightly low recovery rate with a percentage of around 53% and this can be marked as a point of disadvantage for the material. But according to this study, the promising potential of the PACK material, as very abundant material, easily obtainable and renewable, for removing basic dyes from aqueous solutions was demonstrated.

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**Table 1:** Chemical properties of Methylene Blue.

Dye	Classification	$\lambda_{\max}$ (nm)	Empirical formula	Formula weight (g. mol <sup>-1</sup> )	Solubility in water
Methylene Blue	Cationic dye	664	C <sub>16</sub> H <sub>18</sub> N <sub>3</sub> ClS	320	>50g. L <sup>-1</sup>

**Table 2:** Adsorption kinetics models used in this work and their parameters.

Kinetics model	Equation	Parameters
Pseudo-first order	$Q_t = Q_e (1 - e^{-k_1 t})$	<p><math>Q_e</math> (mg g<sup>-1</sup>) and <math>Q_t</math> (mg g<sup>-1</sup>) refer to the amount of dye adsorbed at equilibrium and at time <math>t</math> (min), respectively.</p> <p><math>k_1</math> (L min<sup>-1</sup>) is the equilibrium rate constant of the pseudo-first-order equation</p>
Pseudo-second order	$Q_t = \frac{k_2 Q_e^2 t}{1 + k_2 Q_e t}$	<p><math>k_2</math> (L min<sup>-1</sup>) is the equilibrium rate constant of the pseudo-second-order equation</p>
Pseudo-n <sup>th</sup> order	$Q_t = Q_e - [(n-1)k_n t + Q_e^{(n-1)}]^{-\frac{1}{n}}$	<p><math>k_n</math> is a constant and <math>n</math> is the biosorption reaction order</p>

**Table 3:** Adsorption isotherm models adopted in this work and their parameters.

Isotherme	Equation	Parameters
Langmuir	$\frac{Q_e}{Q_m} = \frac{K_L C_e}{1 + K_L C_e}$	<p><math>Q_e</math> (mg g<sup>-1</sup>) is the amount of MB adsorbed per unit mass of adsorbent</p> <p><math>C_e</math>. (mg L<sup>-1</sup>)the equilibrium dye concentration in solution</p> <p><math>Q_m</math>(mg g<sup>-1</sup>) the monolayer capacity of the adsorbent</p> <p><math>K_L</math> the Langmuir constant</p>
Freundlich	$Q_e = K_F C_e^{1/n}$	<p><math>K_F</math> and <math>n^{-1}</math> are empirical constants indicative of sorption capacity and sorption intensity, respectively</p>
Sips	$\frac{Q_e}{Q_m} = \frac{(K_S C_e)^m}{1 + (K_S C_e)^m}$	<p><math>K_S</math> i (L mg<sup>-1</sup>) the Sips constant</p> <p><math>m</math> the exponent of the Sips model</p>
Redlich-Peterson	$Q_e = \frac{k_R C_e}{1 + \alpha_R C_e^{\beta_R}}$	<p><math>k_R</math>(L g<sup>-1</sup>) is the Redlich–Peterson (R-P) isotherm constant</p> <p><math>\alpha_R</math> (L mg<sup>-1</sup>) is also having a constant unit of</p> <p><math>\beta_R</math> is an exponent</p>
Dubinin-Radushkevich	$Q_e = Q_{DR} \exp(-k_{DR} \epsilon^2)$	<p><math>Q_{DR}</math> is capacity of the adsorbent (mg/g)</p>
		<p><math>k_{DR}</math> is the activity coefficient (mol<sup>2</sup> KJ<sup>2</sup>)</p>
		<p><math>\epsilon</math> stands for constant related to the biosorption energy</p>

**Table 4:** Grand canonical partition function and equation of the three models of statistical physics

Model	Grand canonical partition function	Equation
1	$z_{gc} = \sum_{N_i=0.1} 1 + e^{\beta(\varepsilon+\mu)N_i}$	$Q = \frac{n \cdot Nm}{1 + \left(\frac{C_{1/2}}{Ce}\right)^n}$
2	$z_{gc} = (1 + e^{\beta(\varepsilon_1+\mu)})^{N_{1m}} + (1 + e^{\beta(\varepsilon_2+\mu)})^{N_{2m}}$	$Q = \frac{n1 \cdot Nm1}{1 + \left(\frac{C1}{Ce}\right)^{n1}} + \frac{n2 \cdot Nm2}{1 + \left(\frac{C2}{Ce}\right)^{n2}}$
3	$z_{gc} = \sum_1 1 + e^{\beta(\varepsilon+\mu)} + e^{2\beta(\varepsilon+\mu)N_m}$	$Q = n \cdot N_M \cdot \frac{\left(\frac{C}{C1}\right)^n + 2 \cdot \left(\frac{C}{C2}\right)^{2n}}{1 + \left(\frac{C}{C1}\right)^n + 2 \cdot \left(\frac{C}{C2}\right)^{2n}}$

**Tableau 5:** Kinetic parameters and correlation coefficients for nonlinear regression of PFO PSO and PNO models for the adsorption of MB onto PACK at room temperature.

Material	Model	Parameters	100	150
PACK	PFO	Qexp	<b>374</b>	<b>547</b>
		Qe	368.88	528.05
		K <sub>1</sub>	0.153	0.093
		<b>R<sup>2</sup></b>	<b>0.994</b>	<b>0.9494</b>
	PSO	Qe	391.46	572.70
		K <sub>2</sub> *10 <sup>+4</sup>	6.94	2.60
		<b>R<sup>2</sup></b>	<b>0.989</b>	<b>0.986</b>
PNO	Qe	373.87	604.37	
	k <sub>n</sub>	0.029	1.16E-05	
	n	1.31	2.50	
	<b>R<sup>2</sup></b>	<b>0.997</b>	<b>0.986</b>	

**Tableau 6.** Langmuir. Freundlich. Sips and Redlich-Peterson (R-P) constants for the adsorption of MB onto PACK

		20°C	30°C		
PACK	Langmuir	<b>Q<sub>exp</sub>(mg/g)</b>	<b>1285.34</b>	<b>1528.02</b>	
		Q <sub>m</sub> (mg/g)	1219.23	1522.34	
		K <sub>L</sub> (L/mg)x 10 <sup>3</sup>	0.256	0.219	
		<b>F<sub>error</sub></b>	<b>0.365</b>	<b>0.926</b>	
		<b>R<sup>2</sup></b>	<b>0.949</b>	<b>0.992</b>	
	Freundlich	1/n	0.22	0.24	
		K <sub>F</sub> (mg/g)(L/mg) <sup>1/n</sup>	381.59	414.21	
		<b>F<sub>error</sub></b>	<b>0.857</b>	<b>0.950</b>	
		<b>R<sup>2</sup></b>	<b>0.843</b>	<b>0.877</b>	
	Sips	Q <sub>m</sub> (mg/g)	1176.18	1502.57	
		K <sub>S</sub> (L/mg)	0.299	0.235	
		m	1.26	1.08	
		<b>F<sub>error</sub></b>	<b>0.471</b>	<b>0.329</b>	
		<b>R<sup>2</sup></b>	<b>0.948</b>	<b>0.992</b>	
		Redlich-Peterson	k <sub>R</sub> (L/g)	341.261	343.545
			α <sub>R</sub> (L/ mg)	0.325	0.238
			β <sub>R</sub>	0.969	0.989
			<b>F<sub>error</sub></b>	<b>0.386</b>	<b>0.322</b>
			<b>R<sup>2</sup></b>	<b>0.9477</b>	<b>0.991</b>
Dubinin-Radushkevich	Q <sub>DR</sub>	--	<b>1419.95</b>		
	k <sub>DR</sub> x 10 <sup>+6</sup> (mol <sup>2</sup> KJ <sup>-2</sup> )	--	<b>1.2</b>		
	E (KJ/mol)	--			
	<b>R<sup>2</sup></b>	--	<b>0.988</b>		

**Table 7:** Results of calculations of the various anchoring parameters

	Model 1		Model 2			Model 3		
	20°C	30°C		20°C	30°C		20°C	30°C
<b>n</b>	1.262	1.079	<b>n<sub>1</sub></b>	1.775	3.553	<b>n</b>	1.26	1.078
<b>Nm</b>	931.99	1392.80	<b>Nm<sub>1</sub></b>	548.26	101.82	<b>Nm</b>	932.48	1392.73
<b>C<sub>1/2</sub></b>	3.3464	4.259	<b>C<sub>1</sub></b>	2.433	1.289	<b>C<sub>1</sub></b>	3.347	4.259
<b>R<sup>2</sup></b>	<b>0.9778</b>	<b>0.9966</b>	<b>n<sub>2</sub></b>	1.957	1.025	<b>C<sub>2</sub></b>	732.22	753.18
			<b>Nm<sub>2</sub></b>	173.94	1146.87	<b>R<sup>2</sup></b>	<b>0.9778</b>	<b>0.9966</b>
			<b>C<sub>2</sub></b>	113.86	8.326			
			<b>R<sup>2</sup></b>	<b>0.9873</b>	<b>0.9996</b>			

**Table 8:** the calculation of the thermodynamic parameters

Température (K)	Kc (L/g)	$\Delta H^0$ (kJ/mol.)	$\Delta S^0$ (J/mol.K)	$\Delta G^0$ (kJ/mol.)
293	6.36	54.703	259.72	-21.32
303	14.60			-24.14
313	26.65			-26.65



## Figures Captions

**Figure 1.** Chemical structure of the methylene blue.

**Figure 2.** FT-IR spectrum of the PACK before and after adsorption of BM.

**Figure 3.** Isoelectric points of PACK ( $V = 50$  ml,  $T = 25 \pm 2$  °C, stirring speed = 250 rpm,  $m_{\text{PACK}} = 25$  mg).

**Figure 4.** SEM captures of PACK

**Figure 5.** Kinetics data (symbol) of MB adsorption onto PACK and modeling data (lines) by PFO, PSO, and  $P^{\text{nth}}\text{O}$  with different initial concentrations. ( $V = 200$  ml,  $T = 25 \pm 2$  °C, stirring speed = 250 rpm,  $m_{\text{PACK}} = 50$  mg).

**Figure 6.** Experimental data (points) of MB adsorption onto PACK. Modeling Data (lines) by Langmuir, Freundlich, Sips, and Redlich-Peterson models at different temperatures. (Stirring speed= 250 rpm, pH=6.5)

**Figure 7.** Simulation of statistical physics models, monolayer single-energy (Model 1), monolayer two-energy (Model 2), and Double-layer two-energy (Model 3).

**Figure 8.** pH effect of MB adsorption onto PACK ( $V = 50$  ml,  $T = 25 \pm 2$  °C, stirring speed = 250 rpm,  $m_{\text{PACK}} = 25$  mg).

**Figure 9.** The effect of biosorbent dosage on the biosorption of MB onto PACK.

**Figure 10 :** Recovery percent of various solvent for desorption of MB dye onto PACK. ( $C_0 = 400$  mg /L,  $m = 0.05$  g, contact time: 24 h, temperature: 25 °C).

**Figure 11:** Mechanism of interaction MB dye with PACK in aqueous solution

Figure. 1



Figure 2

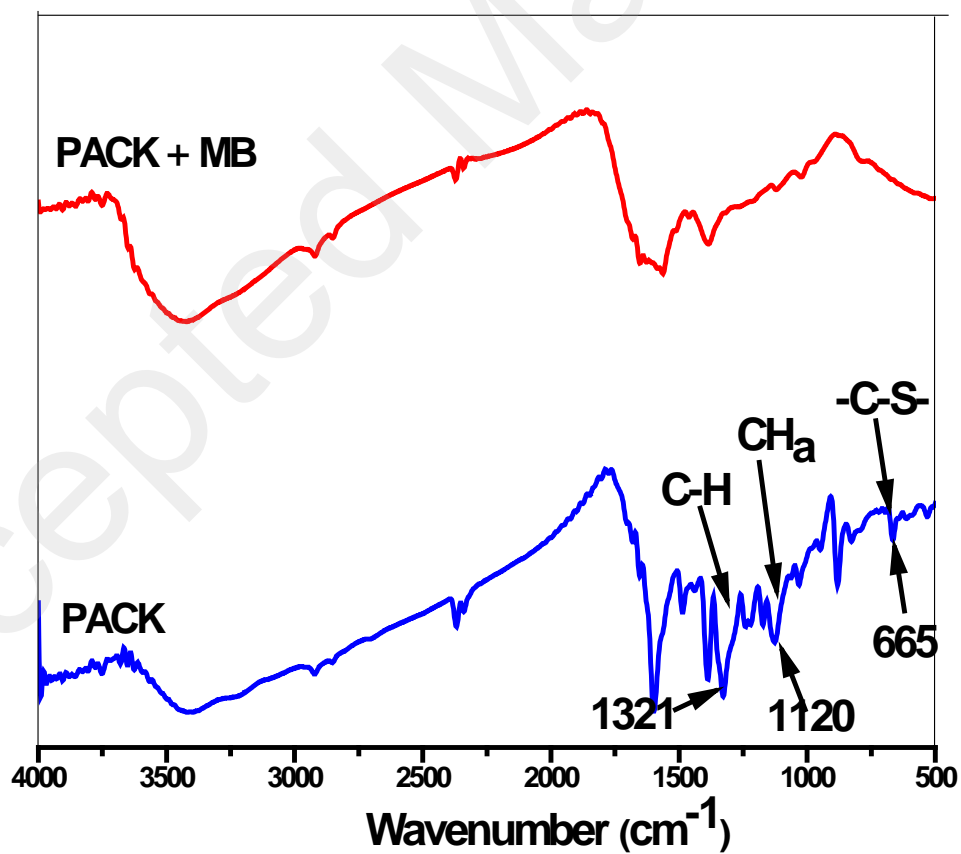


Figure 3

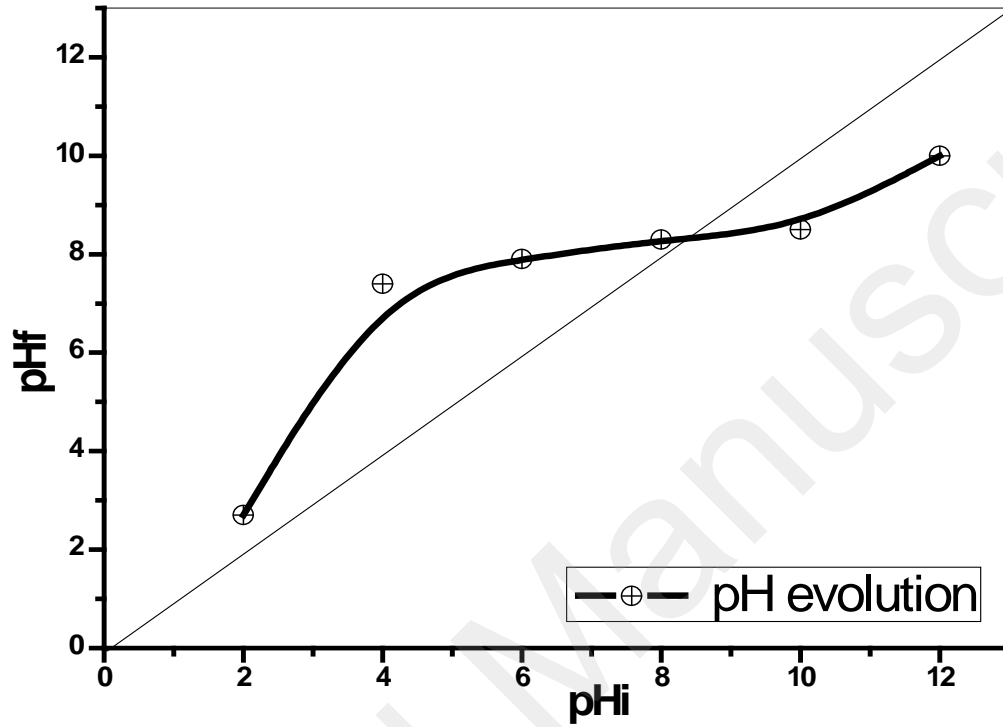


Figure 4

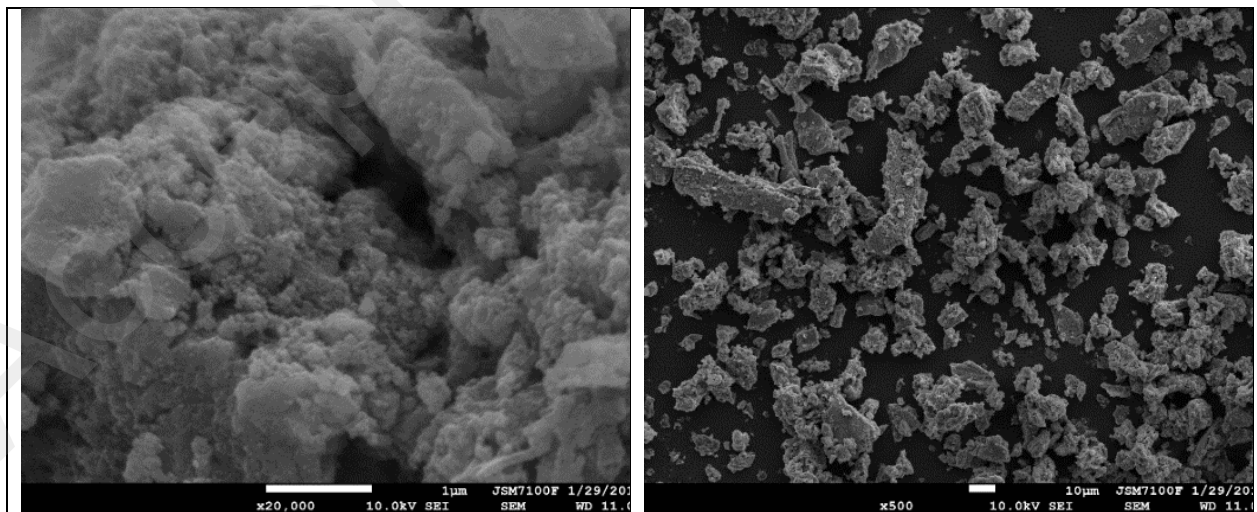
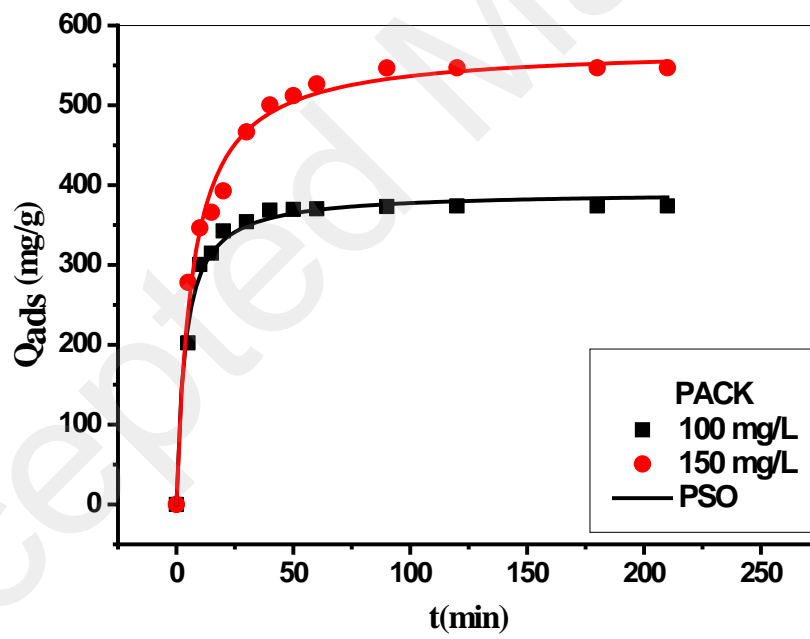
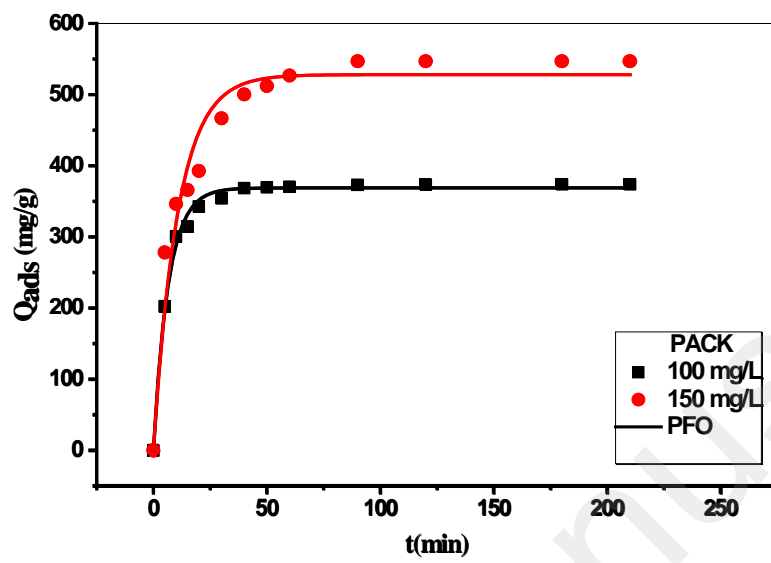


Figure. 5



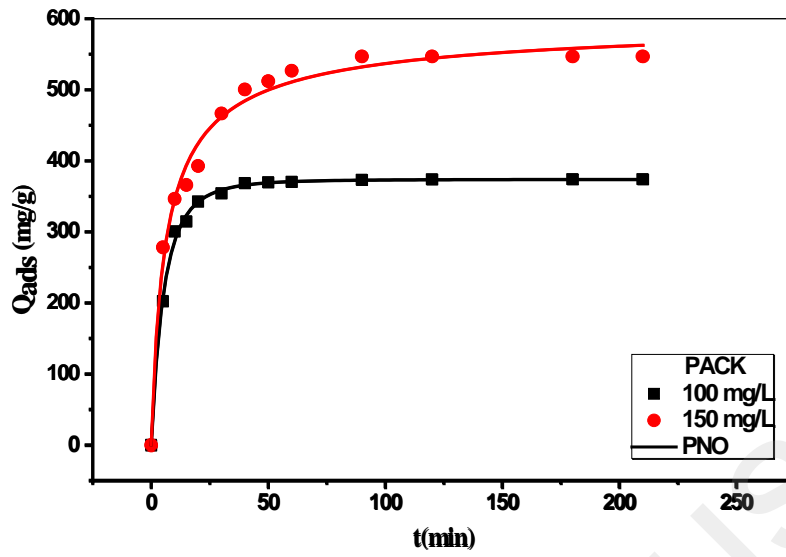
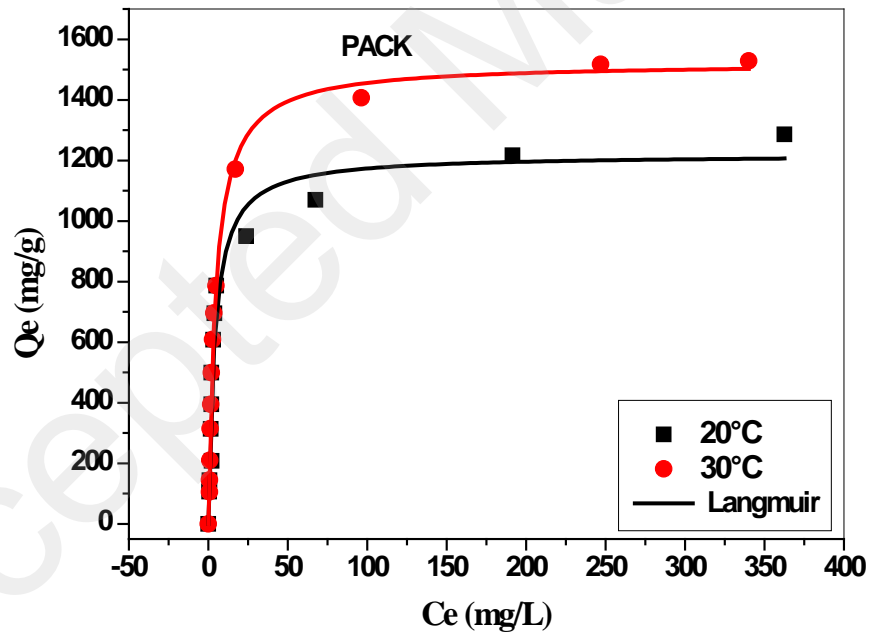
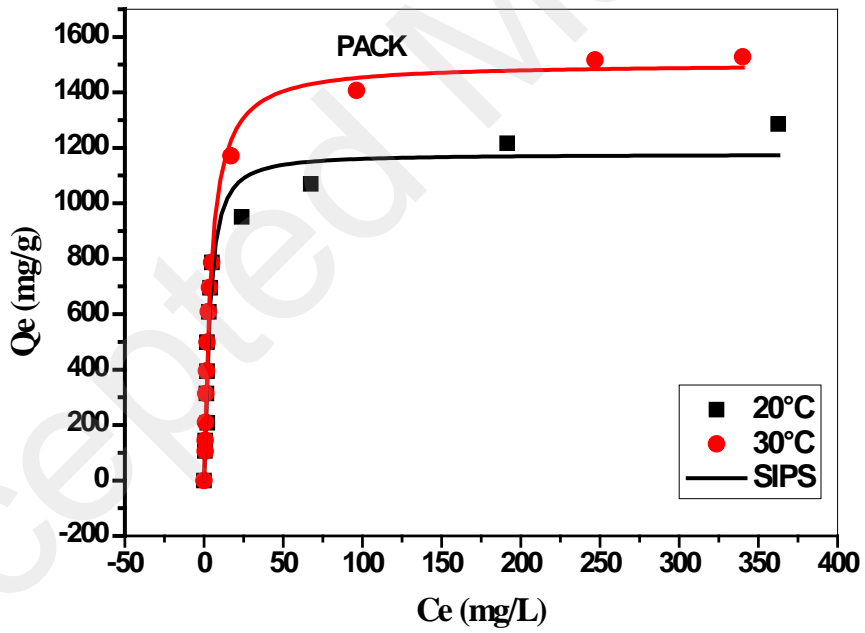
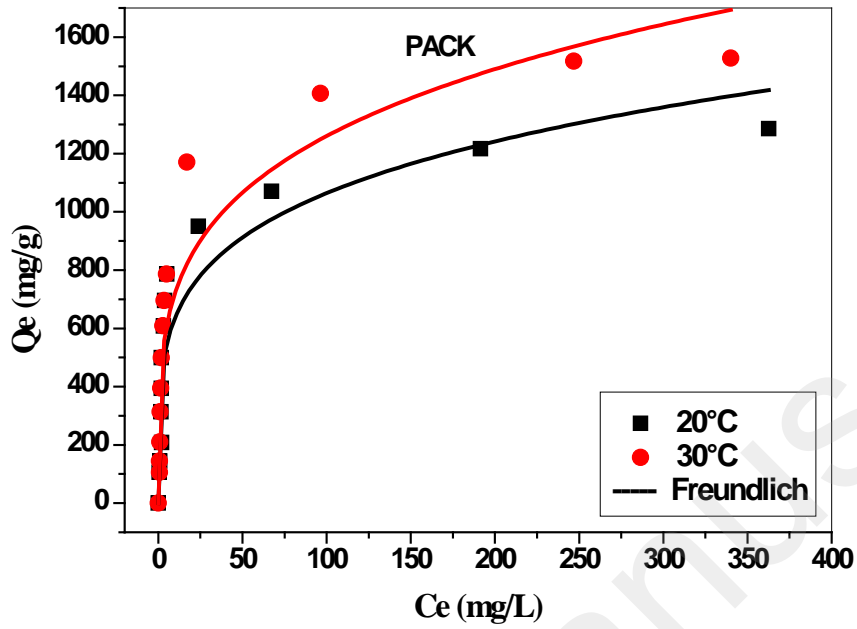


Figure. 6





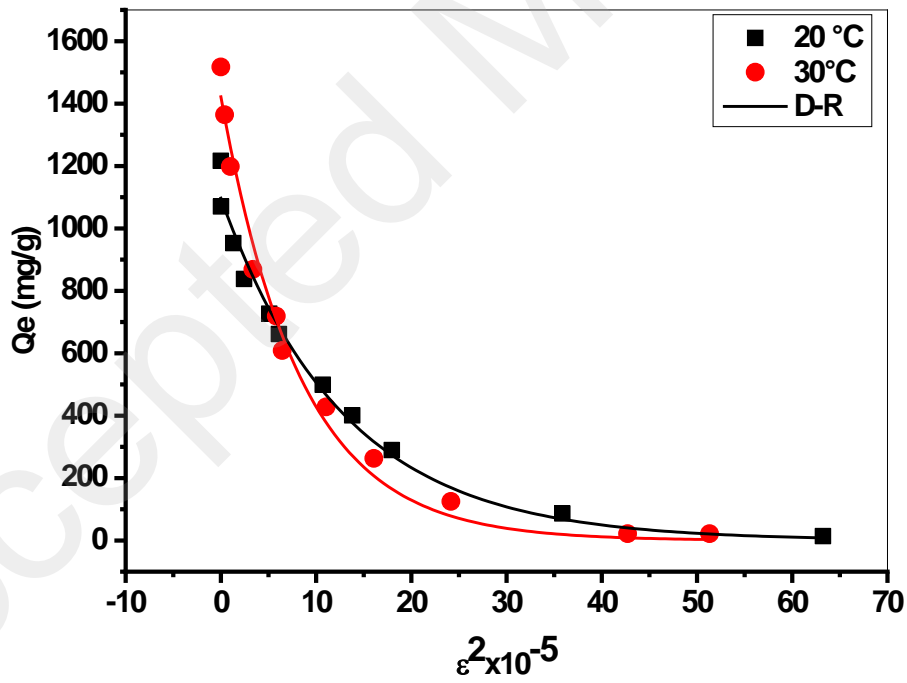
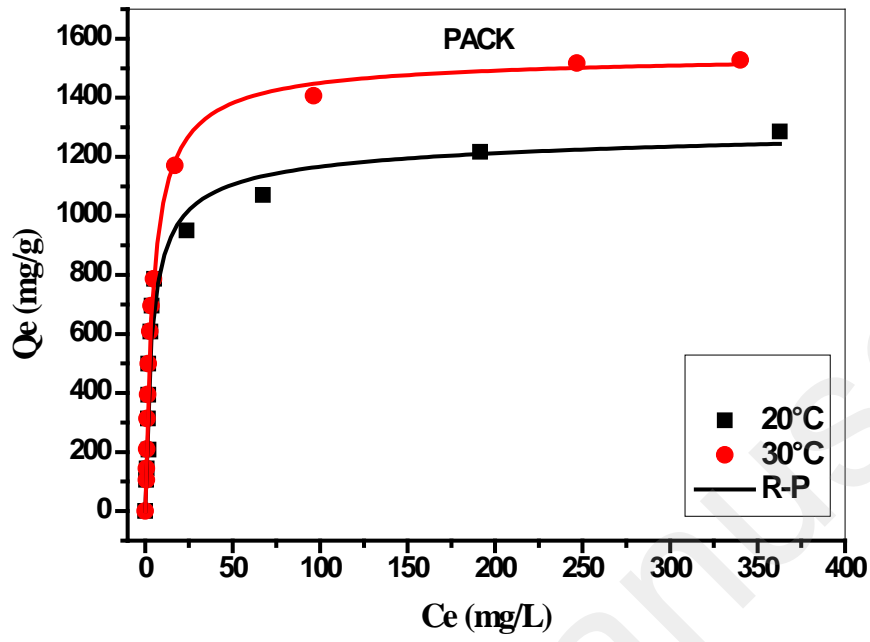


Figure. 7

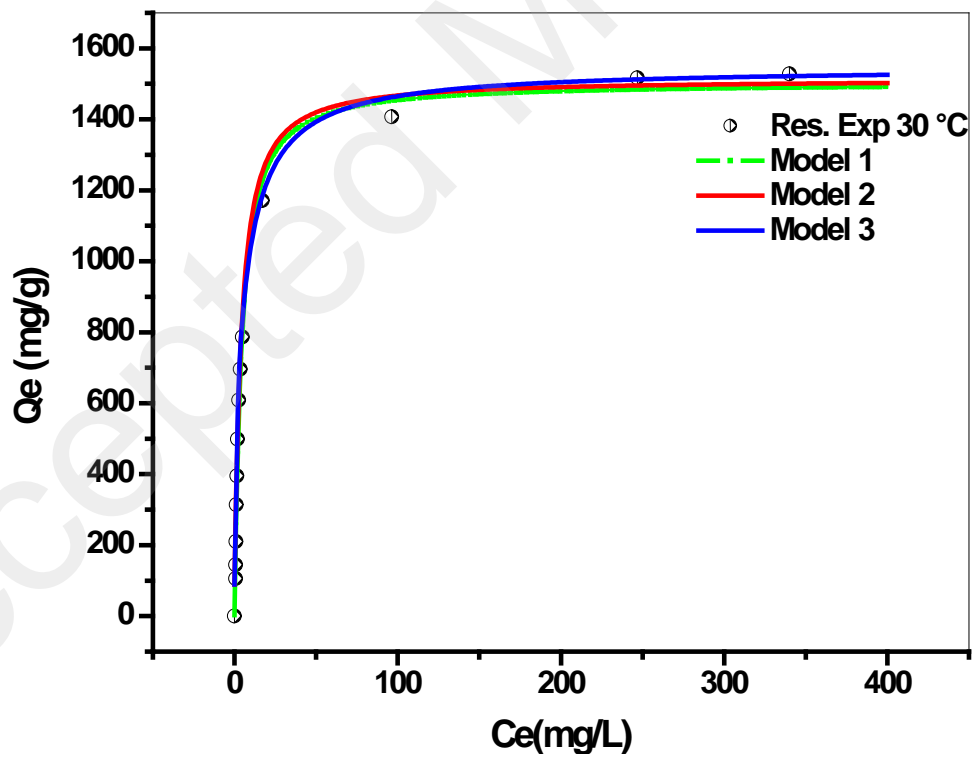
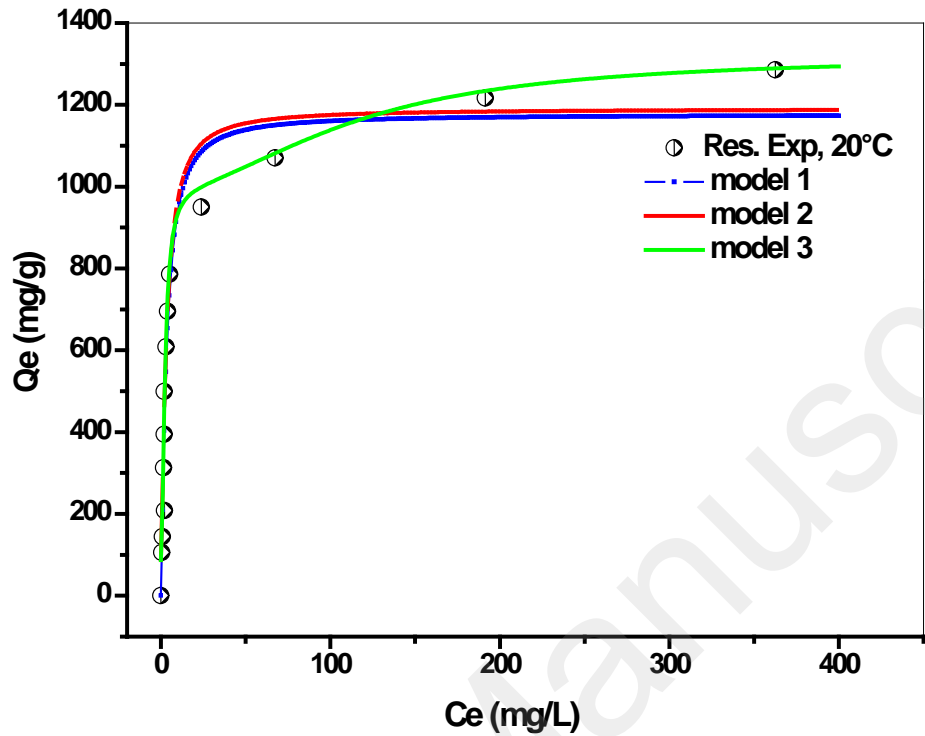




Figure 8

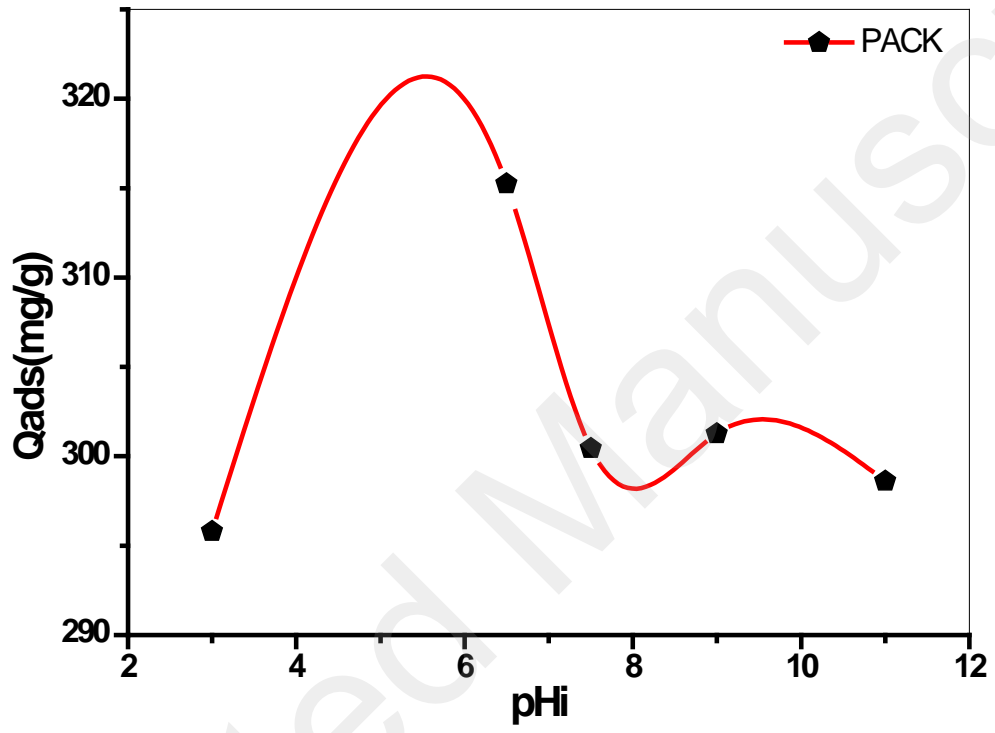


Figure 9

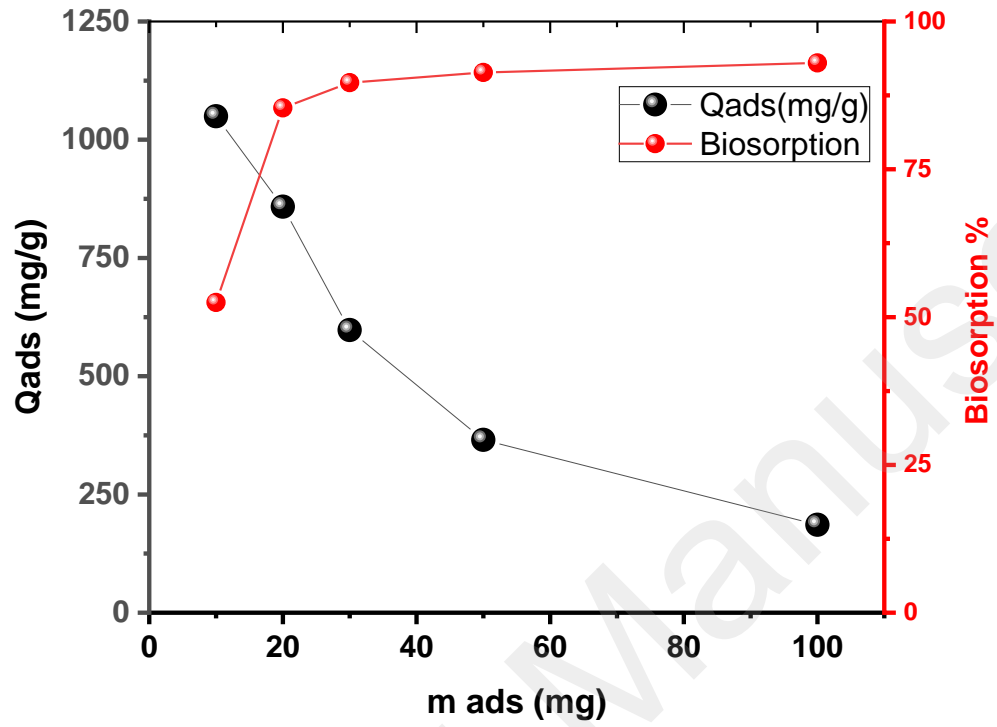


Figure 10

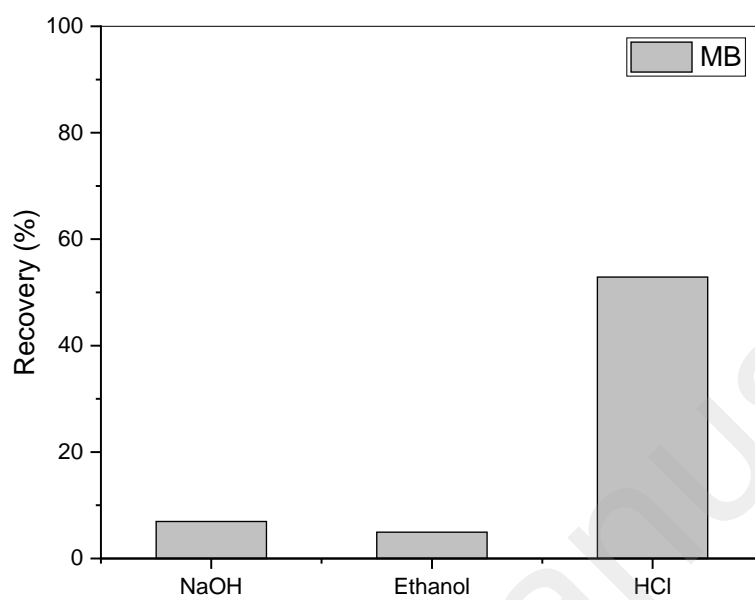


Figure 11

