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## Modeling the demography of species providing extended parental care: <br> A capture-recapture approach with a case study on Polar Bears (Ursus maritimus)

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| Abstract: | In species providing extended parental care, one or both parents care for altricial young over a period including more than one breeding season. We expect large parental investment and long-term dependency within family units to cause high variability in life trajectories among individuals with complex consequences at the population level. So far, models for estimating demographic parameters in free-ranging animal populations mostly ignore extended parental care, thereby limiting our understanding of its consequences on parents and offspring life histories. We designed a capture-recapture multi-event model for studying the demography of species providing extended parental care. It handles statistical multiple-year dependency among individual demographic parameters grouped within family units, variable litter size, and uncertainty on the timing at offspring independence. It allows for the evaluation of trade-offs among demographic parameters, the influence of past reproductive history on the caring parent's survival status, breeding probability and litter size probability, while accounting for imperfect detection of family units. We assess the model performance using simulated data, and illustrate its use with a long-term dataset collected on the Svalbard polar bears (Ursus maritimus). <br> Our model performed well, both when offspring departure probability from the family unit occurred at a constant rate or varied during the field season depending on the date of capture. For the polar bear case study, |

# Modeling the demography of species providing extended parental care: <br> A capture-recapture multievent model with a case study on Polar Bears (Ursus 

 maritimus)Sarah Cubaynes ${ }^{1}$, Jon Aars ${ }^{2}$, Nigel G. Yoccoz ${ }^{3}$, Roger Pradel ${ }^{1}$, Øystein Wiig ${ }^{4}$, Rolf A Ims ${ }^{3}$ and Olivier Gimenez ${ }^{1}$<br>${ }^{1}$ CEFE, Univ Montpellier, CNRS, EPHE-PSL University, IRD, Univ Paul Valéry<br>Montpellier 3, Montpellier, France<br>${ }^{2}$ Norwegian Polar Institute, FRAM Centre, Tromsø, Norway<br>${ }^{3}$ UiT The Arctic University of Norway, Department of Arctic and Marine Biology, Tromsø, Norway<br>${ }^{4}$ Natural History Museum, University of Oslo, Norway


#### Abstract

1. In species providing extended parental care, one or both parents care for altricial young over a period including more than one breeding season. We expect large parental investment and long-term dependency within family units to cause high variability in life trajectories among individuals with complex consequences at the population level. So far, models for estimating demographic parameters in free-ranging animal populations mostly ignore extended parental care, thereby limiting our understanding of its consequences on parents and offspring life histories. 2. We designed a capture-recapture multi-event model for studying the demography of species providing extended parental care. It handles statistical multiple-year dependency among individual demographic parameters grouped within family units, variable litter size, and uncertainty on the timing at offspring independence. It allows for the evaluation of trade-offs


among demographic parameters, the influence of past reproductive history on the caring parent's survival status, breeding probability and litter size probability, while accounting for imperfect detection of family units. We assess the model performance using simulated data, and illustrate its use with a long-term dataset collected on the Svalbard polar bears (Ursus maritimus).
3. Our model performed well in terms of bias and mean square error and in estimating demographic parameters in all simulated scenarios, both when offspring departure probability from the family unit occurred at a constant rate or varied during the field season depending on the date of capture. For the polar bear case study, we provide estimates of adult and dependent offspring survival rates, breeding probability and litter size probability. Results showed that the outcome of the previous reproduction influenced breeding probability.
4. Overall, our results show the importance of accounting for i) the multiple-year statistical dependency within family units, ii) uncertainty on the timing at offspring independence, and iii) past reproductive history of the caring parent. If ignored, estimates obtained for breeding probability, litter size, and survival can be biased. This is of interest in terms of conservation because species providing extended parental care are often long-living mammals vulnerable or threatened with extinction.

Key-words: apex predator, arctic ecosystem, Bayesian modeling, capture-recapture, dependency among individuals, family structure, parental care, state uncertainty, timing at independence.

## INTRODUCTION

Parental care includes any pre-natal and post-natal allocation, such as feeding and protecting the young, which benefits the offspring development and survival chances, thereby enhancing
the parent's reproductive success (Trivers 1972). Altricial mammals having offspring that need to learn complex skills to ensure survival beyond independence, such as hunting, orientation, or nest building, show extended parental care (hereafter EPC; Clutton-Brock 1991). It is defined as a prolonged period, i.e. lasting more than one breeding season, over which one or both parents care for one or several dependent young. This period typically lasts for several years and can extend until lifelong maternal care in primates (Van Noordwijk 2012). For the offspring, the quality and quantity of care received can have long-lasting effects on future survival (e.g. Pavard and Branger 2012), social status (e.g. Shenk and Scelza 2012) and reproduction (Royle et al. 2012). For the parent, investment in one offspring can compromise its own condition or survival and/or its ability to invest in other offspring (siblings or future offspring) (Williams 1966, Stearns 1992). It can indeed take several years during which a parent caring for its offspring will not be available to reproduce, sometimes not until the offspring have reached independence, e.g. on average 2.5 years for female polar bears (Ramsay and Stirling 1988), 3.5 to 6 years for female African elephants (Lee and Moss 1986), and 9.3 years for female Sumatran orangutans (Wich et al. 2004). The fitness costs of losing one offspring, in terms of lost investment and skipped breeding opportunities, are particularly high if death occurs near independence. We therefore expect EPC, through large parental investment and multiple-year dependency among individuals within family units, to cause high variability in life trajectories among individuals and family groups, in interbirth intervals depending on offspring's fate, and consequently on lifetime reproductive success for the caring parent (Clutton-Brock 1991).

Capture-recapture (CR) models allow studying species with complex demography in the wild, e.g. by considering 'breeder' and 'non-breeder' reproductive states to estimate breeding probabilities and status-specific demographic parameters while accounting for imperfect detectability (e.g., Lebreton et al. 2009). One can distinguish between successful and
failed breeding events (e.g., Lagrange et al. 2017) and include varying litter or clutch size (e.g., Doligez et al. 2002) and memory effects (Cole et al. 2014), to investigate the costs of reproduction on survival and future reproduction for species providing short-term parental care, i.e. when offspring reach independence before the next breeding season (e.g., Yoccoz et al. 2002). Indeed, most CR models rely on the assumption of independence among individual CR histories (Lebreton et al. 2009).

In the case of species providing EPC, one challenge stems from the multiple-year dependency among individual's life histories within parent-offspring units. Only few attempts have been made to tackle this issue when estimating demographic parameters, despite the fact that species providing EPC are often among long-living mammals vulnerable or threatened with extinction (e.g. polar bears, orangutans, elephants). Lunn et al. (2016) proposed to model CR histories of mother-offspring units (instead of individuals) to consider the multiple-year dependency of female breeding probability upon offspring survival status for polar bears in Hudson Bay. However, in this model, offspring survival after 9 months is assumed independent of mother survival. Lunn et al. (2016)'s model does therefore not handle multiple-year dependency of offspring survival upon mother survival status, typical of species providing EPC. In addition, because litter size is modeled separately, Lunn et al. (2016)'s model (also used in Regehr et al. (2018)) does not permit to explore potential trade-offs among offspring traits and parental phenotypic or demographic traits.

Another challenge involves dealing with uncertain timing at offspring independence, when the offspring departs the caring parent(s) and becomes independent. When studying freeranging populations, this key life history event is rarely directly observed. When a mature individual is observed without dependent offspring, it is often impossible to know if its offspring have died or already departed its natal group. As a result, estimates of demographic rates and trade-offs can be underestimated. Based on the analysis of mother-offspring units CR
histories, Couet et al. (2019) provided estimates of dolphin reproductive parameters corrected for state uncertainty, but their model assumed a fixed age and timing at offspring independence. Lunn et al. (2016)'s model included variable age at independence, but variability in the timing at offspring independence was not fully dealt with. Demographic rates were corrected by the average annual probability that independence occurred prior to sampling for all offspring, and offspring survival was assumed independent of litter size (Regehr et al. 2018). In most species, timing at offspring independence is variable and could depend on the offspring phenotypic traits (e.g. body size in brown bears, Dahle and Swenson 2003), on parental traits (e.g. parentoffspring conflict in kestrels, Vergara et al. 2010), social and mating system (e.g. helping behavior in humans, Kramer 2005), or other environmental determinants (e.g. food supply, Eldegard and Sonerud 2010). To our knowledge, no model is available to tackle both the issues of multiple-year dependency among individuals and variable timing at offspring independence. Because of these methodological challenges, the population-level consequences of EPC remain to be understood, especially in free-ranging animal populations.

Here, we develop a CR model specifically for species providing EPC. It is designed to handle multiple-years statistical dependency (until offspring independence) among individual demographic parameters by modeling CR histories grouped within family units. The model accounts for uncertain timing at offspring independence. In addition, our model allows for variability in the number of offspring born and recruited at each breeding event, variable offspring survival depending on number of siblings, and includes the influence of past reproductive history on the caring parent's current status. Finally, estimates of survival rates, breeding probability and litter size probability are corrected for imperfect detection possibly depending upon family unit composition.

In what follows, we present the model, assess its performance using simulated data, and illustrate its use with a long-term dataset collected on the Svalbard polar bears. Female polar
bears rely solely on stored fat reserves during pregnancy and the first three months of lactation, before feeding and protecting litters of one to three young, usually during two more years (Ramsay and Stirling 1988). They can lose more than $40 \%$ of body mass while fasting (Atkinson and Ramsay 1995). In many areas, climate change and related sea ice decline impact female bear condition and capacity to provide care for their young, with an associated decline in reproductive output (Derocher et al. 2004; Stirling and Derocher, 2012, Laidre et al. 2020). More insights into the species demography, such as the consequences of long-duration parental care on mother and offspring life histories, could help our understanding of polar bear population responses to environmental perturbations and extinction risks in future decades (Hunter et al., 2010; Regehr et al., 2016).

## METHODS

## 1. Capture-recapture model for species providing EPC

### 1.1 Principle

We develop a CR model in the multievent framework (Pradel 2005) that is also known as a hidden Markov modeling framework (Gimenez et al. 2012). The principle is to relate the field observations, called events, to the underlying demographic states of interest through the observation process. Uncertainty on state assignment due to variable timing at offspring independence is included in the observation process. In parallel, the state process describes the transition rates between states from one year to the next. The transition rates correspond here to the demographic parameters corrected for imperfect detection and state uncertainty. Below we describe the general procedure to specify the model by defining the states and state-to-state transition process, then the events and observation process. However, for simplicity, the events and states are chosen to match the polar bear life cycle (i.e. females are captured in spring, alone
or together with a litter of one or two dependent offspring; offspring gain independence in the year following their second birthday, and offspring cannot survive the loss of their mother before gaining independence). The resulting model assumptions and its applicability to other species are discussed below.

### 1.2 Specification of states and state process

One specificity of our model lies in the use of CR histories based on family groups instead of individuals, which permits to include the multiple-year dependency among the caring parent and dependent offspring's demographic rates and life history traits. Below, we describe the specification of 24 unique states and 6 matrices needed to construct the model.

States correspond to the 'real' demographic states of the individuals composing the family. We consider 12 states $\mathrm{S}, S=\{J 2, J 3, S A 4, S A 5, A 01, A 02, A 11, A 12, A S 1, A S 2, A, D\}$, to represent the polar bear life cycle (defined in Table 1). In addition, we specify 13 intermediary states $\mathrm{S}^{\prime}, \mathrm{S}^{\prime}=\{\mathrm{J} 3, \mathrm{SA} 4, \mathrm{SA} 5, \mathrm{~A} 11, \mathrm{~A} 12, \mathrm{AS} 1, \mathrm{AS} 2, \mathrm{~A} 0-, \mathrm{A} 1-, \mathrm{I} / \mathrm{AS} 1, \mathrm{I} / \mathrm{AS} 2, \mathrm{~A}, \mathrm{D}\}$, and 16 intermediary states $S^{\prime}$, $\mathrm{S}^{\prime} ’=\{\mathrm{J} 3, \mathrm{SA} 4, \mathrm{SA} 5, \mathrm{~A} 11, \mathrm{~A} 12, \mathrm{AS} 1, \mathrm{AS} 2, \mathrm{~B} / \mathrm{A} 0-, \mathrm{NB} / \mathrm{A} 0-, \mathrm{B} / \mathrm{A} 1-, \mathrm{NB} / \mathrm{A} 1-$ , $\mathrm{B} / \mathrm{AS}, \mathrm{NB} / \mathrm{AS}, \mathrm{B} / \mathrm{A}, \mathrm{NB} / \mathrm{A}, \mathrm{D}\}$, leading to a total of 24 unique states (defined in Table 1). The specification of intermediary states is what permits to distinguish between failed and successful breeders in the transition matrix to consider the influence of past reproductive history on parameters (see below).

Table 1. Definition of the states and events used in the model to describe the polar bear life cycle.

## TYPE CODE DEFINITION

| STATES | J2 | 2 y.o. independent juvenile female |
| :---: | :---: | :---: |
|  | J3 | 3 y.o. independent juvenile female |


|  | SA4 | 4 y.o. independent subadult female |
| :---: | :---: | :---: |
|  | SA5 | 5 y.o. independent subadult female |
|  | A01 | mother with one dependent cub of the year |
|  | A02 | mother with two dependent cubs of the year |
|  | A11 | mother with one dependent yearling |
|  | A12 | mother with two dependent yearlings |
|  | AS1 | successful female breeder with one two-year old offspring reaching independence |
|  | AS2 | successful female breeder with two two-year old offspring reaching independence |
|  | A | adult female without dependent offspring |
|  | D | dead state |
|  | A0- | failed breeder, death of all offspring cubs of the year |
|  | A1- | failed breeder, death of all offspring yearlings |
|  | I/AS1 | successful female breeder alone after departure of one independent offspring |
|  | I/AS2 | successful female breeder alone after departure of two independent offspring |
|  | B/A0- | breeder following loss of a cub of the year litter |
|  | NB/A0- | non breeder following loss of a cub of the year litter |
|  | B/A1- | breeder following loss of a yearling litter |
|  | NB/A1- | non breeder following loss of a yearling litter |
|  | B/AS | breeder following successful reproduction |
|  | NB/AS | non breeder following successful reproduction |
|  | B/A | breeder given that previously without dependent offspring |
|  | NB/A | non breeder given that previously without dependent offspring |
| EVENTS | '1' | capture of a 2 yo independent female juvenile |
|  | '2' | capture of a 3yo independent female juvenile |
|  | '3' | capture of a 4yo independent subadult female |


| '4' | capture of a 5 yo independent subadult female |
| :---: | :---: |
| '5' | capture of a mother with one dependent cub of the year |
| '6' | capture of a mother with two dependent cub of the year |
| '7' | capture of a mother with one dependent yearling |
| '8' | capture of a mother with two dependent yearlings |
| '9' | capture of a mother with one dependent two-year old offspring |
| '10' | capture of a mother with two dependent two-year old offspring |
| '11' | capture of an adult female without dependent offspring |
| ${ }^{\prime} 0$ | non observation |

The model is conditioned upon first capture. The initial state vector, $\mathrm{s}_{0}$, gathers the proportions of family units in each state $S$ at first capture, $s_{0}=\left(\pi_{1}, \ldots, \pi_{11}, 0\right)^{\prime}$ (with $\pi_{12}=0$ for state D, because an individual must be alive at first capture).

The transition matrix, $\Psi$, describing all possible state-to-state transitions from spring one year $(\mathrm{t})$ to spring the next year $(\mathrm{t}+1)$, is obtained as the matrix product of four matrices $\Psi=\Phi \cdot \Psi_{1} \cdot \Psi_{2} \cdot \Psi_{3}$. This decomposition is another particularity of our model which permits to estimate the relevant set of demographic parameters: independent juvenile, subadult and adult survival (matrix $\Phi$ ), dependent offspring survival (matrix $\Psi_{1}$ ), breeding probabilities (matrix $\Psi_{2}$ ) and litter size probabilities (matrix $\Psi_{3}$ ), and potential trade-offs among them. This formulation of the transition matrix implies that litter size is conditioned upon breeding decision, itself conditioned upon offspring survival, itself conditioned upon survival of the caring parent to deal with the statistical dependency existing among individuals within family units.

The $\Phi$ matrix (eq. 1) describes transitions from each state $S$ at time $t$ (rows) to each state S after the occurrence of the survival process for independent individuals (columns):

|  | J2 | J3 | SA4 | SA5 | A01 | A02 | A11 | A12 | AS1 | AS2 | A | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | $\varphi_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi_{1}$ |
| J3 | 0 | $\varphi_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi_{2}$ |
| SA4 | 0 | 0 | $\varphi_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi_{3}$ |
| SA5 | 0 | 0 | 0 | $\varphi_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi_{4}$ |
| A01 | 0 | 0 | 0 | 0 | $\varphi_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi$ |
| A02 | 0 | 0 | 0 | 0 | 0 | $\varphi_{6}$ | 0 | 0 | 0 | 0 | 0 | $1-\varphi_{6}$ |
| A11 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi_{7}$ | 0 | 0 | 0 | 0 | $1-\varphi_{7}$ |
| A12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi_{8}$ | 0 | 0 | 0 | $1-\varphi_{8}$ |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi_{9}$ | 0 | 0 | $1-\varphi_{9}$ |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi_{10}$ | 0 | $1-\varphi_{10}$ |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi_{11}$ | $1-\varphi_{11}$ |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

The $\Psi_{1}$ matrix (eq.2) describes transitions from states S after the occurrence of the survival process for independent individuals (rows) to states S' after the occurrence of the offspring survival process (columns):

|  | J3 | SA4 | SA5 | A11 | A12 | AS1 | AS2 | AO- | A1- | I/AS1 | 1/AS2 | A | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA4 | 0 | 0 | 1- $\kappa$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\kappa$ | 0 |
| SA5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| A01 | 0 | 0 | 0 | $s_{1}$ | 0 | 0 | 0 | $1-s_{1}$ | 0 | 0 | 0 | 0 | 0 |
| A02 | 0 | 0 | 0 | $2 \cdot s_{2} \cdot\left(1-s_{2}\right)$ | $s_{2}{ }^{2}$ | 0 | 0 | $1-s_{2}{ }^{2}-2 \cdot s_{2} \cdot\left(1-s_{2}\right)$ | 0 | 0 | 0 | 0 | 0 |
| A11 | 0 | 0 | 0 | 0 | 0 | $s_{3}$ | 0 | 0 | $1-s_{3}$ | 0 | 0 | 0 | 0 |
| A12 | 0 | 0 | 0 | 0 | 0 | $2 \cdot s_{4} \cdot\left(1-s_{4}\right)$ | $s_{4}{ }^{2}$ | 0 | $1-s_{4}{ }^{2}-2 \cdot s_{4} \cdot\left(1-s_{4}\right)$ | 0 | 0 | 0 | 0 |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

In the $\Psi_{1}$ matrix, $\kappa$ is the probability of first reproduction at age $5, s$ is dependent offspring survival conditioned upon mother survival ( $s_{1}$ for singleton cub, $s_{2}$ for singleton yearling; $s_{3}$ for twin litter's individual cub, and $s_{4}$ for twin litter's individual yearling). Litter survival rates can be obtained from individual offspring survival rates (for singleton litters $l_{01}=s_{1}$ and $l_{11}=$
$s_{3}$ for cub and yearling respectively, and for twin litters $l_{02}=1-\left(1-s_{2}{ }^{2}-2 \cdot s_{2} \cdot\left(1-s_{2}\right)\right)$ and $l_{12}=1-\left(1-s_{4}{ }^{2}-2 \cdot s_{4} \cdot\left(1-s_{4}\right)\right)$ for cubs and yearlings respectively $)$.

The $\Psi_{2}$ matrix (eq.3) describes transitions from states $S^{\prime}$ after occurrence of the survival processes (rows) to states $S$ ' ' depending on breeding decision (columns):

|  | J3 | SA4 | SA5 | A11 | A12 | AS1 | AS2 | B/AO- | NB/AO- | B/A1- | NB/A1- | B/AS1 | B/AS2 | B/A | NB/A | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J3 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA4 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA5 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A11 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A12 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A21 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A22 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A0- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{1}$ | $1-\beta_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A1- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{2}$ | $1-\beta_{2}$ | 0 | 0 | 0 | 0 | 0 |
| 1/AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{3}$ | $1-\beta_{3}$ | 0 | 0 | 0 |
| 1/AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{3}$ | $1-\beta_{3}$ | 0 | 0 | 0 |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{4}$ | $1-\beta_{4}$ | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Parameter $\beta$ is breeding probability conditioned upon mother and offspring's survival status ( $\beta_{1}$ following loss of a cub litter, $\beta_{2}$ loss of a yearling litter, $\beta_{3}$ for successful breeder, $\beta_{4}$ for female without dependent offspring at the beginning of the year).

The $\Psi_{3}$ matrix (eq. 4) describes transitions from states $S$ " after occurrence of the survival processes and breeding decision (rows) to states S at $\mathrm{t}+1$ after determination of litter size for breeders (columns):

|  | J2 | J3 | SA4 | SA5 | A01 | A02 | A11 | A12 | AS1 | AS2 | A | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA4 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA5 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| A11 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| A12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |


| B/AO- | 0 | 0 | 0 | 0 | $\gamma_{1}$ | $1-\gamma_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NB/AO- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| B/A1- | 0 | 0 | 0 | 0 | $\gamma_{2}$ | $1-\gamma_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| NB/A1- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| B/AS1 | 0 | 0 | 0 | 0 | $\gamma_{3}$ | $1-\gamma_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| B/AS2 | 0 | 0 | 0 | 0 | $\gamma_{3}$ | $1-\gamma_{3}$ | 0 | 0 | 0 | 0 | 1 | 0 |
| B/A | 0 | 0 | 0 | 0 | $\gamma_{4}$ | $1-\gamma_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| NB/A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Parameter $\gamma$ is the probability of producing a singleton litter conditioned upon mother's and offspring's survival status and upon breeding decision ( $\gamma_{1}$ following the loss a cub litter, $\gamma_{2}$ loss of a yearling litter, $\gamma_{3}$ for successful breeder, $\gamma_{4}$ for female without dependent offspring at the beginning of the year).

By modifying the constraints on parameters (i.e. setting them equal or different among states), the model can be used to investigate: i) the cost of reproduction on parent's survival (by comparing the $\varphi$ s in matrix $\Phi$ ), ii) the influence of litter size on individual offspring survival (by comparing $s_{1}$ to $s_{2}$, and $s_{3}$ to $s_{4}$ in matrix $\Psi_{1}$ ) and on litter survival (by comparing $1_{01}$ to $1_{02}$ and $1_{11}$ to $1_{12}$ ), iv) the influence of past reproductive history on breeding probability (by comparing the $\beta$ s in matrix $\Psi_{2}$ ), and on litter size probability (by comparing the $\gamma \mathrm{s}$ in matrix $\Psi_{3}$ ).

### 1.3 Specification of events and observation process

The events correspond to the observation or non-observation of family units in the field at each sampling occasion. Each event is coded depending on the number and age of the individuals composing the family. Here, we consider 12 possible events, $\Omega=\{1,2,3,4,5,6,7,8,9,10,11,12\}$ to describe field observations for polar bears family groups (defined in Table 1).

In a multievent model, one specific event may relate to several possible states. Due to variable timing at offspring independence, a female successful breeder (state 'AS1' or 'AS2') departure probability, denoted $\alpha$.

|  | '1' | '2' | '3' | '4' | '5' | '6' | '7' | '8' | '9' |  |  | '10' |  | '11' | '12' |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| J3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| SA4 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| SA5 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| A01 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| A02 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| A11 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |  |  | 0 |  | 0 | 0 |
| A12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |  |  | 0 |  | 0 | 0 |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1- $\alpha_{i, d}$ |  |  | 0 |  | $\alpha_{i, d}$ | 0 |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $2 \cdot \alpha_{i, d} \cdot\left(1-\alpha_{i, d}\right)$ | $1-$ | $2 \cdot \alpha_{i, d}$ | $\cdot(1-$ | $\left.-\alpha_{i, d}\right)-\alpha_{i, d}{ }^{2}$ | $\alpha_{i, d}{ }^{2}$ | 0 |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 1 | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | 1 |

Here, $\alpha_{i, d}$ is the departure probability of a two-year old individual offspring belonging to family unit ion its date of capture d . The relationship between date of capture and departure probability is species-specific and either assessed from prior knowledge on the species' biology or field data (see Appendix 2). Here we assume that siblings' timing at independence can, but does not have to, occur independently (if both offspring can only depart the family on the same date, the transition from state 'AS2' to event ' 9 ' should be set to 0 ).

The second event matrix, $E_{2}$, (eq. 6) relates all possible observations at the time of capture O to the events, $\Omega$, actually observed in the field through the state-dependent capture probability, denoted $\mathrm{p}_{\mathrm{s}}$.

|  | $1^{\prime}$ | $2^{\prime}$ | $3^{\prime}$ | $4^{\prime}$ | $5^{\prime}$ | $6^{\prime}$ | $7{ }^{7}$ | $8^{\prime}$ |  | $9^{\prime}$ |  | $10^{\prime}$ |  |  | $11^{\prime}$ | $12^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1^{1}$ | $p_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{1}$ |
| $2^{\prime}$ | 0 | $p_{2}$ | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{2}$ |
| $3^{\prime}$ | 0 | 0 | $p_{3}$ | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{3}$ |
| $4^{\prime}$ | 0 | 0 | 0 | $p_{4}$ | 0 | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{4}$ |
| $5^{\prime}$ | 0 | 0 | 0 | 0 | $p_{5}$ | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{5}$ |
| $6^{\prime}$ | 0 | 0 | 0 | 0 | 0 | $p_{6}$ | 0 |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{6}$ |
| 71 | 0 | 0 | 0 | 0 | 0 | 0 | $p_{7}$ |  |  | 0 |  | 0 |  | 0 | 0 | $1-p_{7}$ |
| 8' | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | $p_{8}$ |  |  | 0 |  | 0 | 0 | $1-p_{8}$ |
| $9^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 | $p_{9}$ |  |  | 0 | 0 | $1-p_{9}$ |
| 10' | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 | $p_{10}$ |  | 0 | $1-p_{10}$ |
| $11^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |  |  | 0 |  | 0 |  | 0 | $p_{11}$ | $1-p_{11}$ |
| $12^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 |  | 0 |  | 0 | 0 | 1 |

The composite event matrix, E, which relates the events to the states, is obtained as the matrix product of these two matrices $E=E_{1} \cdot E_{2}$. Because the model is conditioned upon first capture, the initial event vector, $e_{0}$, takes the value of 1 for all events (except of 0 for the event ' 12 ' corresponding to a non-observation).

### 1.4 Applicability to other species

The model described above matches the Svalbard polar bear life cycle. The model therefore assumes that care is provided by the mother only, to one or two offspring (we modelled triplets as twins because there were just 8 litters of triplets in the data), for a duration of two years maximum. Offspring under age 2 cannot survive if the mother dies. A mother caring for offspring cannot mate and produce a second litter. Independent males (that have already departed from the family unit) are not included in the model.

To apply the model to other species, one should modify the number of events and states to match the species life cycle (depending on age at sexual maturity, number of care providers, maximum litter size, duration of parental care) but the number of matrices should remain the same. For example, modeling a hypothetical species similar to polar bears but in which both males and females care for offspring would increase the number of unique states from 24 to 42 (8 states for immature females and males, 21 states for dependent offspring cared for by both parents, just the mother in case of father loss, or just the father in case of mother loss). Such a model could be used to assess the influence of father versus mother loss on litter size, offspring survival and father and/or mother breeding probabilities. After defining the states and events, one should modify the shape of the relationship between departure probability and date of capture to match the species life cycle. In species like primates or wolves, departure from the family unit can occur throughout the year, at a more or less constant rate depending on the season, while it occurs only between February and May in polar bears due to environmental constraints. In addition, the influence of individual traits such as age or body weight, or environmental variables such as temperature, can be included in the model under the form of individual or temporal covariates (Pollock 2002). Other specificities related to data collection can be included in a similar way, such as trap effects (Pradel and Sanz-Aguilar 2012) or latent individual heterogeneity by using mixture of distributions or random effects (Gimenez et al. 2018). Guidance to fit the model in a Bayesian framework in program Jags for real and simulated data are provided in Appendices 1 and 2.

## Simulation study

The simulation study was aimed at evaluating the performance of our model to estimate demographic parameters under various assumptions about the timing at offspring independence (constant versus seasonal departure rate) and various degrees of capture probability (low $\mathrm{p}=$
0.25 , high $\mathrm{p}=0.7$ ), for a medium-size data set ( $\mathrm{T}=15$ sampling occasions, with $\mathrm{R}=80$ newly marked at each occasion in equal proportion among the 11 alive states).

We simulated data for a virtual long-lived mammal species mimicking the polar bear using the model described in box 1 . We used $\varphi=0.9$ for independent female bear survival (aged $2+$ y.o.), $s_{1}=l_{01}=0.6$ for singleton cub survival, $s_{2}=0.55$ for twin litter' s cub survival (corresponding to twin litter survival $l_{02}=0.7975$ ), $s_{3}=0.8$ for singleton yearling survival and $s_{4}=0.75$ for twin litter's yearling survival (corresponding to litter survival $l_{12}$ $=0.94)$. Offspring survival rates were conditioned upon mother survival. If a mother dies, its dependent offspring had no chances of surviving. For breeding probabilities, we used $\beta_{1}=0.5$ , $\beta_{2}=0.7, \beta_{3}=0.9$ and $\beta_{4}=0.8$. For litter size probabilities, we used $\gamma_{1}=0.4, \gamma_{2}=0.5, \gamma_{3}$ $=0.6$ and $\gamma_{4}=0.7$. We set $\kappa=0$ and assumed that females had their first litter at age 6 or older.

We assumed that captures occurred each year between mid-March to end of May (day of the year $\mathrm{d}=80$ to $\mathrm{d}=130$ ). For each capture event, date of capture was randomly sampled from the distribution of the polar bear data dates of capture (see Appendix 1). In the constant scenario, we assumed that two-year old bears reached independence at a constant departure rate $(\alpha)$ during the field season, independently of the date of capture. We chose an intermediate value of $\alpha=0.5$ (if independence occurred always after the field season, $\alpha=0$, versus always before the field season, $\alpha=1$ ). In the seasonal scenario, we assumed that departure rate varied with date of capture (d) following a logistic relationship (regression coefficients were estimated from the polar bear data, see Appendix 2). Most of the two-year old offspring were captured with their mother at the beginning of the field season, while departure probability increased logistically up to $80 \%$ at the end of the field season.

We simulated 100 CR datasets for each of the 4 scenarios (S1: low detection with constant departure, S2: low detection with seasonal departure, S3: high detection with constant departure, S4: high detection with seasonal departure). We simulated the data using program R. We fitted the model using program jags called from R (Plummer 2016). For each parameter and each dataset, we calculated absolute bias as $\hat{B}=\hat{\theta}-\theta$, and root mean squared error as $R \widehat{M S} E=\sqrt{(\hat{\theta}-\theta)^{2}}$, with $\theta$ the parameter used to simulate the data and $\hat{\theta}$ the mean value of the estimated parameter. Appendix 1 containing guidance, R code and files to simulate data and fit the model is available on GitHub at

## https://github.com/SCubaynes/Appendix1 extendedparentalcare.

## Case study: Polar bears in Svalbard

In polar bears, care of offspring is provided by the mother only (Amstrup, 2003). Males were therefore discarded from our analysis. Adult female polar bears mate in spring (February to May, Amstrup 2003), and in Svalbard usually have their first litter at the age of six years, but some females can have their first litter at five years (Derocher 2013). They have delayed implantation where the egg attaches to the uterus in autumn (Ramsay and Stirling 1988). A litter with small cubs (ca 600 grams) is born around November to January, in a snow den that the mothers dig out in autumn, and where the family stay $4-5$ months. The family usually emerges from the den in March-April, and stay close to the den while the cubs get accustomed to the new environment outside their home, for a few days up to 2-3 weeks (Hansson and Thomassen 1983). Litter size in early spring vary from one to three, with two cubs being most common, three cubs in most areas being rare, and commonly around one out of three litters having one cub only (Amstrup 2003). In Svalbard, polar bears become independent from their mother shortly after their second birthday (average age at independence is 2.3 ). Two-year old bears typically depart from the mother in spring (between mid-March to end of May), when the
mother can mate again. There is only one anecdotal record of a yearling alive without his mother. Because the field season can last for several weeks, some two-year-old bears were captured together with their mother and others were already independent at the time of capture. The minimum reproductive interval for successful Barents Sea polar bears is 3 years. On the contrary, loss of a cub litter shortly after den emergence may mean the mother can produce new cubs in winter the same year (Ramsay and Stirling 1988).

Bears captured in Svalbard are shown to be a mixture of resident and pelagic bears (Mauritzen et al. 2002). To focus on the resident population, independent bears captured only once were not included in our analysis. We therefore analyzed $\mathrm{N}=158$ encounter histories of resident polar bear family units captured each spring after den emergence between doy 80 to 130 (mid-March to mid-May), from 1992 to 2019, in Svalbard. It corresponds to 81 capture events of juvenile and subadults, 231 cubs, 96 yearling, 23 dependent two-year old, and 444 captures of adult females. Polar bears were caught and individually marked as part of a longterm monitoring program on the ecology of polar bears in the Barents Sea region (Derocher 2005). All bears one year or older were immobilized by remote injection of a dart (Palmer CapChur Equipment, Douglasville, GA, USA) with the drug Zoletil® (Virbac, Carros, France) (Stirling et al. 1989). The dart was fired from a small helicopter (Eurocopter 350 B2 or B3), usually from a distance of about 4 to 10 meters. Cubs of the year were immobilized by injection with a syringe. Cubs and yearlings were highly dependent on their mother; therefore, they remained in her vicinity and were captured together with their mother. A female captured alone was considered to have no dependent offspring alive. Death of the cubs could have occurred in the den or shortly after den emergence but before capture. Hereafter, estimated cub survival thus refers to survival after capture. Infant mortality occurring before capture will be assigned to a reduced litter size. Because only $3 \%$ of females were observed with 3 offspring, we analyzed jointly litters of twins with triplets.

We built the model described above with 12 states and 12 events to describe the life cycle (Table 1). Preliminary analyses suggested that mother survival did not vary according to state, we therefore constrained parameter $\varphi$ to be equal among all states in matrix $\Phi$. To avoid identifiability issues due to a relatively small sample size, we assumed breeding probability and litter size probability did not vary between successful breeders (states AS1 and AS2) and female without dependent offspring (state A) by setting $\beta_{3}=\beta_{4}$ and $\gamma_{3}=\gamma_{4}$. We also assumed that litter size probability did not vary among failed breeders (loss of a cub versus a yearling litter), by setting $\gamma_{1}=\gamma_{2}$. We could not assess formally the fit of our model because no test is yet available for multievent models. However, the multi-state version of our model (without uncertainty on timing at independence) fitted the data adequately. Adding a level of complexity should make the model even more adequate.

Using the conditional probabilities estimated in the model, we calculated the net probability for a female to raise none, $\operatorname{Pr}(\mathrm{X}=0)$, one, $\operatorname{Pr}(\mathrm{X}=1)$, or two offspring, $\operatorname{Pr}(\mathrm{X}=2)$ to independence over a 3-year period (details are provided in Appendix 2).


Figure 1: Life history events with associated probabilities of raising one ( $\mathrm{X}=1$ ) or two ( $\mathrm{X}=2$ ) offspring to independence over a 3 years period for a female polar bear alive and without dependent offspring at the beginning of the period (state A). State A01 represents a female with one dependent cub of the year, A02 with two dependent cubs of the year, A11 with one dependent yearling, A12 with two dependent yearlings, AS1 a successful female breeder with one two-year old offspring reaching independence and AS2 a successful female breeder with two two-year old offspring reaching independence. Parameter $\varphi$ is adult survival, $\beta_{3}$ is breeding probability of a female without dependent offspring, $\gamma_{3}$ is the probability of a singleton litter, $s_{1}$ is cub and $s_{2}$ is yearling survival in a singleton litter, $s_{3}$ is cub and $s_{4}$ yearling survival in a twin litter.

We considered adult females without dependent offspring at the beginning of the time period, so that we have:
$\operatorname{Pr}(\mathrm{X}=1)=\varphi^{3} \cdot \beta_{3} \cdot\left[\gamma_{3} \cdot s_{1} \cdot s_{3}+\left(1-\gamma_{3}\right) \cdot\left(2 s_{2}\left(1-s_{2}\right) \cdot s_{3}+s_{2}{ }^{2} \cdot 2 s_{4}\left(1-s_{4}\right)\right)\right]$,
$\operatorname{Pr}(\mathrm{X}=2)=\varphi^{3} \cdot \beta_{3} \cdot\left(1-\gamma_{3}\right) \cdot s_{2}{ }^{2} \cdot s_{4}{ }^{2}$,
$\operatorname{Pr}(\mathrm{X}=0)=1-\operatorname{Pr}(X=1)-\operatorname{Pr}(X=2)$.

Appendix 2 containing guidance, R code, data files to fit the model to the polar bear data, and additional results is available on GitHub at

## https://github.com/SCubaynes/Appendix2 extendedparentalcare.

## RESULTS

## Model performance evaluated on simulated datasets

Model performance was satisfying and comparable in all 4 simulated scenarios (S1 with low detection and constant departure, S2 with low detection and seasonal departure, S3 with high detection and constant departure and S 4 with high detection and seasonal departure), with low average bias $\left(B_{S 1}=-0.000, B_{S 2}=-0.004, B_{S 3}=-0.004, B_{S 4}=-0.003\right)$ and root-meansquare error $\left(r m s e_{S 1}=0.042, r m s e_{S 2}=0.041, r m s e_{S 3}=0.031\right.$ and $\left.r m s e_{S 4}=0.031\right)($ see Appendix 1 for details).

For most parameters, bias was very low, $\mathrm{B}<0.02$, except for parameters $\beta_{2}$ in scenarios S2, S3 and S4 $(-0.04<\mathrm{B}<-0.03)$ and $s_{3}$ in scenario $\mathrm{S} 2(\mathrm{~B}=-0.03)$, rmse $<0.05$, except for parameters $\beta_{2}, \gamma_{1}$ and $\gamma_{2}(0.05<\mathrm{rmse}<0.07)$. For these three parameters, precision was lower in the two scenarios with low detection (see Appendix 1). Estimates obtained for the scenario mimicking the polar bear study case (S2: low detection and seasonal departure) are provided in Figure 2.


Figure 2. Performance of the model on simulated data with low detection with seasonal departure (scenario $S 2$ ). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X -axis for each parameter. Regarding notations, $\phi$ stands for juvenile, subadult and adult survival, $\kappa$ is the probability of first reproduction at age $5, s$ is dependent offspring survival conditioned upon mother survival ( $s_{1}$ and $s_{2}$ for singleton cub resp. yearling; $s_{3}$ and $s_{4}$ for twin litter's cub resp. yearling), $\beta$ is breeding probability conditioned upon mother and offspring survival status ( $\beta_{1}$ following loss of a cub litter, $\beta_{2}$ loss of a yearling litter, $\beta_{3}$ for successful breeder, $\beta_{4}$ for female without dependent offspring), $\gamma$ is the probability of producing a singleton litter conditioned upon mother's and offspring's survival status and upon breeding decision ( $\gamma_{1}$ following loss of a cub litter, $\gamma_{2}$ loss of a yearling litter, $\gamma_{3}$ for successful breeder, $\gamma_{4}$ for female without dependent offspring), $p$ is detection probability.

Departure probability was about $40 \%$ at the end of March and reached $80 \%$ at mid-May (Appendix 2). About half of the two-year old bears had departed their mother at the time of capture. Estimates of demographic parameters are provided in Table 2 (more results are provided in Appendix 2). Independent female (aged $2+$ ) survival was high (0.93). Individual offspring survival rates, conditioned upon mother survival, did not vary significantly with litter size for cubs or yearlings. Average yearling survival was lower for singleton (0.67) than for litters of twin (0.80), although the $95 \%$ credible intervals did overlap. Concerning litter survival conditioned upon mother survival, it was higher for twin compared to singleton, for both cubs, and yearlings' litters. A small proportion of females, about $12 \%$, started to reproduce (i.e. produced a litter that survived at least until the first spring) at 5 y.o. Outcome of the previous reproduction influenced breeding probability. Breeding probability following the loss of a cub litter during the year (after capture) was low, about $10 \%$, while it was about $50-60 \%$ for female' successful breeders or without dependent offspring at the beginning of the year or after the loss of a yearling litter. Detection probability was relatively low, about 0.25 (0.22-0.27). At first capture, $37 \%$ were independent juvenile or subadult females, $18 \%$ were adult females alone, $28 \%$ were adult females with one or two cubs, $12 \%$ with one or two yearlings and $5 \%$ with twoyear old bears.

Table 2: Parameter estimates. Means are given with $95 \%$ credible intervals (CI). Dependent offspring (cub age $<1$ y.o., yearling 1 y.o.) survival and breeding probabilities are conditioned upon mother survival, litter size probability of producing a singleton is as well conditioned upon breeding decision.

| Parameter | Notation | Mean | Standard <br> error | $\mathbf{9 5 \%}$ CI |
| :--- | :---: | :--- | :--- | :--- |
| Survival of female juveniles <br> (2yo,3yo) subadults (4yo, 5yo) <br> and adults (5+ yo) | $\varphi$ | 0.93 | 0.01 | $0.92-0.95$ |
| Cub survival (<1yo) |  |  |  |  |


| - singleton (=litter survival) <br> litter of 2 (averaged individual survival) | $\begin{gathered} s_{1}=l_{01} \\ s_{2} \end{gathered}$ | $\begin{aligned} & 0.54 \\ & 0.51 \end{aligned}$ | 0.10 0.05 | $\begin{aligned} & 0.34-0.72 \\ & 0.41-0.62 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| Yearling survival (1yo) <br> - Singleton (=litter survival) <br> - litter of 2 (averaged individual survival) | $\begin{gathered} s_{3}=l_{11} \\ s_{4} \end{gathered}$ | 0.67 0.80 | 0.11 0.09 | $\begin{aligned} & 0.46-0.87 \\ & 0.59-0.93 \end{aligned}$ |
| Litter survival for twin litters <br> - cubs <br> - yearlings | $\begin{aligned} & l_{02} \\ & l_{12} \end{aligned}$ | $\begin{aligned} & 0.76 \\ & 0.95 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0.05 \\ & 0.04 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0.65-0.85 \\ & 0.83-0.99 \\ & \hline \end{aligned}$ |
| Probability of first reproduction at 5 yo (mate at 4yo) | $\kappa$ | 0.12 | 0.08 | 0.02-0.30 |
| Breeding probability <br> - following loss of a cub litter <br> - following loss of a yearling litter <br> - of successful female breeders or previously without dependent offspring | $\beta_{1}$ $\beta_{2}$ $\beta_{3}=\beta_{4}$ | $\begin{aligned} & 0.09 \\ & 0.58 \\ & 0.52 \end{aligned}$ | $\begin{aligned} & 0.06 \\ & 0.21 \\ & 0.04 \end{aligned}$ | $\begin{aligned} & 0.01-0.23 \\ & 0.19-0.96 \\ & 0.43-0.61 \end{aligned}$ |
| Probability of singleton litter following loss of a cub or yearling litter of successful females breeders or previously without dependent offspring | $\gamma_{1}=\gamma_{2}$ $\gamma_{3}=\gamma_{4}$ | $\begin{aligned} & 0.35 \\ & 0.40 \end{aligned}$ | 0.17 0.05 | $0.07-0.71$ $0.30-0.44$ |
| Capture probability | p | 0.25 | 0.01 | 0.22-0.27 |

Over a 3 years period, the probability to successfully raise one offspring to independence for a female polar bear, alive and without dependent offspring at the beginning of the period, was on average $0.29(0.20-0.38)$ and $0.04(0.02-0.07)$ to raise two offspring to independence. The probability of failed breeding (no offspring successfully reached independence) over this period was high, about 0.67 ( $0.57-0.76$ ). Note that this calculation includes breeding probability, and therefore does not reflect offspring survival until independence (see Method section).

## DISCUSSION

Overall, our model performed well in estimating all demographic parameters in all the simulated scenarios. A multievent approach is a promising tool to deal with uncertainty on the timing at offspring independence both when departure probability was constant or varied within the field season. Estimates obtained for adult and offspring survival, probability of sexual maturation, breeding probability (except after the loss of a yearling litter), litter size probabilities and detection probability were unbiased in most simulated scenarios. Precision was satisfying in most cases, but it was lower for breeding probability after the loss of a yearling litter and for litter size probabilities of failed breeders, especially in scenarios with low detection (Appendix 1). These specific parameters should therefore be interpreted with caution for the study case. In our simulations, $\mathrm{T}=15$ sampling occasions appeared sufficient to obtain satisfying estimates for most parameters. In the polar bear data, there were few recaptures of females on subsequent years due to relatively low detection rate. As a result, preliminary analyses suggested a potential confusion between these parameters. We dealt with this issue by including a biologically realistic constraint on prior distributions, stating that cub survival was lower than that of yearling survival (Amstrup and Durner, 1995) which was enough to ensure parameter estimability. Inference in a Bayesian framework is useful in this regard, because it allows for the inclusion of prior information when available (McCarthy and Masters 2005) to improve the estimation of model parameters.

For polar bears, we showed that outcome of the previous breeding event influenced breeding probability. Reduced offspring survival one year, for example due to poor environmental conditions (Derocher et al. 2004), might therefore increase intervals between successful reproduction through reduced breeding probability the next year (Wiig 1998). This means that by ignoring multiple-year dependency among mother and offspring, classical models can underestimate reproductive intervals, therefore risking to overestimate the
population growth rate. However, the biological relevance of our model is currently limited, because we ignored temporal and individual heterogeneity among females in the model. Survival rates for independent female bears (0.93) were close to an earlier study for the same population (0.96), based on telemetry data (Wiig 1998). Our results may overestimate dependent offspring survival because we focused on resident bears captured more than once. Wiig (1998) results indicated that females in Svalbard went into den on average every second year (while successful breeding means denning on a three-year interval), which seems coherent with our results (about $33 \%$ chances of successful reproduction over a three-year period).

Here, we proposed a general model structure that can be applied to other species providing EPC. The originalities of our approach lie in using family structure to define statistical units in our model, and the inclusion of variable timing at offspring independence. Using families instead of individuals allows for the inclusion of dependency among individuals over multiple-years and therefore the evaluation of trade-offs and correlations between offspring's and parents' life history parameters. Our model could be used, for example, to evaluate the population-level consequences of positive or negative correlation between parents' and offspring's traits (e.g. food sharing among group members Lee 2008; or parent-offspring conflict Kölliker et al. 2013). In the case of social species (e.g. primates, elephants, orcas, wolves), several adults often play a role in caring for offspring. In addition, females often give birth to new offspring while still caring for older offspring and, above a certain age, adolescent dependent offspring can survive despite the loss of their mother and gain independence at various ages. In such cases, the number of states to represent all possible family units' composition can rapidly increase, leading to potential computational challenges to deal with huge matrices. One solution is to use sparse matrices to store the data efficiently and optimize matrix calculations. Above this level of complexity, an alternative solution is to limit the number of states by simplifying the life cycle depending on the question of interest (e.g.
focusing on mother and maternal grand-mother considering only one litter, or focusing on mother caring alone for one or more litters). For polar bears specifically, future analyses will integrate in the model the effect of female age on survival and reproductive success (Atkinson and Ramsay 1995; Folio et al. 2019) and influence of climatic variables on body weight and demography (Derocher et al. 2004; Stirling and Derocher 2012) as individual and environmental covariates in a regression-like framework. Our model could then be used to provide population predictions of the demographic response of the Barents Sea polar bear population under climate change (Hunter et al., 2010; Regehr et al., 2016, 2018, Laidre et al. 2020).

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Data Accessibility Statement : Authors agree to archive the data used in this manuscript in a publicly accessible repository such as Dryad and Github upon acceptance of the manuscript (together with R scripts to run the model and the simulation study).

Authors' contributions: SC, OG, NY and RP conceived the ideas and designed methodology; JA, RAI and ØW collected the data; SC analysed the data; SC led the writing of the manuscript. All authors contributed critically to the drafts and gave final approval for publication.

## Bibliography

Amstrup, S. C., \& DeMaster, D. P. (2003). Polar bear, Ursus maritimus. Wild mammals of North America: biology, management, and conservation, 2, 587-610.

Amstrup, S. C., \& Durner, G. M. (1995). Survival rates of radio-collared female polar bears and their dependent young. Canadian Journal of Zoology, 73, 1312-1322. doi:10.1139/z95-155

Atkinson, S. N., \& Ramsay, M. A. (1995). The Effects of Prolonged Fasting of the Body Composition and Reproductive Success of Female Polar Bears (Ursus maritimus). Functional Ecology, 9(4), 559. doi:10.2307/2390145

Clutton-Brock, T. H. (1991). The evolution of parental care. Princeton: Princeton University Press.

Cole, D. J., Morgan, B. J. T., McCrea, R. S., Pradel, R., Gimenez, O., \& Choquet, R. (2014). Does your species have memory? Analyzing capture-recapture data with memory models. Ecology and Evolution, 4(11), 2124-2133.

Couet, P., Gally, F., Canonne, C., \& Besnard, A. (2019). Joint estimation of survival and breeding probability in female dolphins and calves with uncertainty in state assignment. Ecology and evolution, 9(23), 13043-13055.

Dahle, B., \& Swenson, J. E. (2003). Factors influencing length of maternal care in brown bears (Ursus arctos) and its effect on offspring. Behavioral Ecology and Sociobiology, 54(4), 352-358.

Derocher A., \& Stirling, I. (1994). Age-specific reproductive performance of female polar bears (Ursus maritimus). Journal of Zoology, 234(4), 527-536.

Derocher, A. ., Lunn, N. ., \& Stirling, I. (2004). Polar bears in a warming climate. (Ursus maritimus). Integrative and Comparative Biology, 44(2), 163-176.

Derocher, A.E., 2005. Population ecology of polar bears at Svalbard, Norway. Population Ecology, 47(3), pp.267-275.

Derocher, A. (2013). Polar bears: a complete guide to their biology and behavior. Choice Reviews Online, 49(12), 49-6887-49-6887. doi:10.5860/choice.49-6887

Doligez, B., Clobert, J., Pettifor, R. A., Rowcliffe, M., Gustafsson, L., Perrins, C. M., \& McCleery, R. H. (2002). Costs of reproduction: Assessing responses to brood size manipulation on life-history and behavioural traits using multi-state capture-recapture models. Journal of Applied Statistics, 29(1-4), 407-423.

Eldegard, K., \& Sonerud, G. A. (2010). Experimental increase in food supply influences the outcome of within-family conflicts in Tengmalm's owl. Behavioral Ecology and Sociobiology, 64(5), 815-826.

Folio, D.M., Aars, J., Gimenez, O., Derocher, A.E., Wiig, Ø. and Cubaynes, S., (2019). How many cubs can a mum nurse? Maternal age and size influence litter size in polar bears. Biology letters, 15(5), p. 20190070.

Gimenez, O., Lebreton, J.-D., Gaillard, J.-M., Choquet, R. and R. Pradel (2012). Estimating demographic parameters using hidden process dynamic models. Theoretical Population Biology 82, 307-316.

Gimenez, O., Cam, E., \& Gaillard, J.-M. (2018). Individual heterogeneity and capture-recapture models: what, why and how? Oikos, 127(5), 664-686.

Hansson, R., \& Thomassen, J. (1983). Behavior of polar bears with cubs in the denning area. Bears: Their Biology and Management, 246-254.

Hunter, C. M., Caswell, H., Runge, M. C., Regehr, E. V., Amstrup, S. C., \& Stirling, I. (2010). Climate change threatens polar bear populations: a stochastic demographic analysis.

Ecology, 91(10), 2883-2897.

Kölliker, M., Kilner, R. M., \& Hinde, C. A. (2013). Parent-offspring conflict. In The Evolution of Parental Care.

Kramer, K. L. (2005). Children's help and the pace of reproduction: cooperative breeding in humans. Evolutionary Anthropology: Issues, News, and Reviews: Issues, News, and Reviews, 14(6), 224-237.

Lagrange, P., Gimenez, O., Doligez, B., Pradel, R., Garant, D., Pelletier, F., \& Bélisle, M. (2017). Assessment of individual and conspecific reproductive success as determinants of breeding dispersal of female tree swallows: A capture-recapture approach. Ecology and Evolution, 7(18), 7334-7346.

Laidre, K. L., Atkinson, S., Regehr, E. V., Stern, H. L., Born, E. W., Wiig, Ø., ... \& Dyck, M. (2020). Interrelated ecological impacts of climate change on an apex predator. Ecological Applications, e02071.

Lebreton, J. D., Nichols, J. D., Barker, R. J., Pradel, R., \& Spendelow, J. A. (2009). Chapter 3 Modeling Individual Animal Histories with Multistate Capture-Recapture Models. Advances in Ecological Research.

Lee, P. C., \& Moss, C. J. (1986). Early maternal investment in male and female African elephant calves. Behavioral Ecology and Sociobiology, 18(5), 353-361.

Lee, R. (2008). Sociality, selection, and survival: Simulated evolution of mortality with intergenerational transfers and food sharing. Proceedings of the National Academy of Sciences.

Lunn, N.J., Servanty, S., Regehr, E.V., Converse, S.J., Richardson, E. and Stirling, I.( 2016). Demography of an apex predator at the edge of its range: impacts of changing sea ice on polar bears in Hudson Bay. Ecological Applications, 26(5), pp.1302-1320.Mauritzen, M.,

Derocher, A. E., \& Wiig, Ø. (2011). Space-use strategies of female polar bears in a dynamic sea ice habitat. Canadian Journal of Zoology, 79(9), 1704-1713.

Mauritzen, M., Derocher, A.E., Wiig, Ø., Belikov, S.E., Boltunov, A.N., Hansen, E. and Garner, G.W., (2002). Using satellite telemetry to define spatial population structure in polar bears in the Norwegian and western Russian Arctic. Journal of Applied Ecology, 39(1), pp.7990.

McCarthy, M. A., \& Masters, P. (2005). Profiting from prior information in Bayesian analyses of ecological data. Journal of Applied Ecology, 42(6), 1012-1019.

Pavard, S., \& Branger, F. (2012). Effect of maternal and grandmaternal care on population dynamics and human life-history evolution: A matrix projection model. Theoretical Population Biology.

Plummer, M., Stukalov, A., Denwood, M. and Plummer, M.M., (2016). Package 'rjags'. Vienna, Austria.

Pollock, K. H. (2002). The use of auxiliary variables in capture-recapture modelling: An overview. Journal of Applied Statistics, 29(1-4), 85-102.

Pradel, R. (2005) Multievent: An extension of multistate capture-recapture models to uncertain states ». Biometrics 61: 442-447

Pradel, R., \& Sanz-Aguilar, A. (2012). Modeling Trap-Awareness and Related Phenomena in Capture-Recapture Studies. PLoS ONE, 7(3), e32666.

Ramsay, M. A., \& Stirling, I. (1988). Reproductive biology and ecology of female polar bears in western Hudson Bay. Naturaliste Canadien, 109(4), 941-946.

Regehr, E. V., Laidre, K. L., Resit Akcakaya, H., Amstrup, S. C., Atwood, T. C., Lunn, N. J., ... Wiig, Ø. (2016). Conservation status of polar bears (Ursus maritimus) in relation to projected sea-ice declines. Biology Letters, 12(12).

Regehr, E.V., Hostetter, N.J., Wilson, R.R., Rode, K.D., Martin, M.S. and Converse, S.J., (2018). Integrated population modeling provides the first empirical estimates of vital rates and abundance for polar bears in the Chukchi Sea. Scientific reports, 8(1), pp.1-12.

Royle, N., Smiseth, P., \& Kölliker, M. (2012). The evolution of parental care.
Shenk, M. K., \& Scelza, B. A. (2012). Paternal investment and status-related child outcomes: Timing of father's death affects offspring success. Journal of Biosocial Science.

Stearns, S.C. 1992. The Evolution of Life Histories. Oxford University Press.
Stirling, I., \& Derocher, A. E. (2012). Effects of climate warming on polar bears: a review of the evidence. Global Change Biology, 18(9), 2694-2706.

Stirling, I., Spencer, C., \& Andriashek, D. (1989). Immobilization of polar bears (Ursus maritimes) with Telazol in the Canadian Arctic. Journal of Wildlife Diseases, 25(2), 159168.

Trivers, R. L. 1972. Parental investment and sexual selection. Pages 136-179 in B. G. Campbell, editor. Sexual selection and the descent of man,1871-1971. Aldine, Chicago

Van Noordwijk, M. A. (2012). From Maternal Investment to Lifetime Maternal Care. In Evolution of Primate Societies (pp. 321-342).

Vergara, P., Fargallo, J. A., \& Martínez-Padilla, J. (2010). Reaching independence: food supply, parent quality, and offspring phenotypic characters in kestrels. Behavioral ecology, 21(3), 507-512.

Wich, S., Utami-Atmoko, S., Setia, T. M., Rijksen, H. D., Schürmann, C., Van Hooff, J. A. R. A. ., \& van Schaik, C. P. (2004). Life history of wild Sumatran orangutans (Pongo abelii). Journal of Human Evolution, 47(6), 385-398.

Wiig, Ø. (1998). Survival and Reproductive Rates for Polar Bears at Svalbard. Ursus, 10, 2532.

Williams, G.C. (1966) Natural selection, the costs of reproduction, and a refinement of Lack's principle. American Naturalist. 100, 687-690

Yoccoz, N. G., Erikstad, K. E., Bustnes, J. O., Hanssen, S. A., \& Tveraa, T. (2002). Costs of reproduction in common eiders ( Somateria mollissima ): An assessment of relationships between reproductive effort and future survival and reproduction based on observational and experimental studies. Journal of Applied Statistics, 29(1-4), 57-64.

# Appendix 1: Guidance and code to simulate multi-event data based on family units CR histories, with variable litter size and variable timing at offspring independence, and fit the model to the simulated data 

Sarah Cubaynes

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All files associated with Appendix 1 are available on GitHub here.

## Simulate multi-event data based on family units CR histories

We assume a post-breeding census, with captures occuring in spring (after den exit, cubs are about 4 months old). The year goes from 1st of April year $t$ to 1st of April $t+1$.

Load useful package :
library(jtools)
First, set the general parameters used to simulate the data:

```
n.occasions <- 15 # duration of the study
R <- 50 # number of newly family units captured per occasion
nrepet = 100 # number of simulated data set (repetitions)
```

Second, define scenario: S1 (low detection, apha constant=0.5), S2 (low detection alpha varies with date of capture), S3 (high detection, apha constant=0.5) or S4 (low detection alpha varies with date of capture):

```
S <- 2 # set to 1 for S1, 2 for S2, 3 for S3 or 4 for S4
```

capture <- c(0.25,0.25,0.5,0.5) \# capture probability
p <- capture[S]

Load the model to infer departure status of two-year old bears at the time of capture (still with family unit or already departed from family unit). For scenarios S1 and S3, departure probability is constant throughout the field season. For scenarios S2 and S4, we used the regression coefficients estimated from the polar bear data, see Appendix 2.

```
filename <- c("glmdeparture_alphaconstant05.Rdata","glm_departure_date.Rdata",
    "glmdeparture_alphaconstant05.Rdata","glm_departure_date.Rdata")
fileS <- filename[S]
load(file=paste(fileS))
# plot departure rate with date of capture
doypred<-80:130 # day of the year, match the timing of the polar bear field season (spring)
effect_plot(modeld, pred = doy, pred.values=doypred,interval = TRUE,
    plot.points = FALSE,y.label = "departure probability")
```



Figure S1. Departure probability of two-year old bears as a fuction of date of capture within the field season in day of the year (doy).

Dates of capture used in the simulations below are randomly sampled from the distribution of capture dates (in day of the year) from the polar bear data:

```
load(file="dateofcapturePB.Rdata") # load data on winter date of capture
hist(wcapt,main="",xlab="Date of capture (doy)") # plot dates of capture
```



S2. Histogram of te dates of capture of polar bears in Svalbard in day of the year (doy).
Define the demographic parameters used to simulate the data. Here we simulate a virtual long-lived species mimicking the polar bear:

```
phi <- 0.9 # survival of independent juvenile, subadult and adult (phi6+) females.
s <- c(0.6,0.55,0.8,0.75) # dependent offspring survival (conditional upon mother
#survival) by increasing age and litter size (in this order: s1,s2,s3,s4)
# we can calculate litter survival rates from individual offspring survival :
    #Litter survival (lxy, x offspring age, y litter size):
101 = s[1]
102 = 1 - (1-s[2]~ 2-2*s[2]*(1-s[2])) #0.7975for twin litter of cubs
111= s[3]
l12= 1 - (1-s[4] 2-2*s[4]*(1-s[4]))#0.94 for twin litter of yearlings
        # Probability that :
        #- only one aO offspring in a litter of 2 survives= 2*s[2]*(1-s[2]),
        #- both survive :s[2]`2
        # Probability that
        #-only one a1 offspring in a litter of 2 survives= 2*s[2]*(1-s[2]),
        #- both offspring survive:s[2] ~2
    # Which gives us the transition probabilities for litter size of 1 and 2 offspring,
#that one, both, or any offspring survive:
psi <- c(s[1],2*s[2]*(1-s[2]),s[2]^2,
    (1- s[2]~2 -2*s[2]*(1-s[2])), s[3],2*s[4]*(1-s[4]),s[4]~2,
    1- 2*s[4]*(1-s[4]) - s[4] 2)
# 0.6, 0.495,0.3025, 0.2025, 0.8, 0.375, 0.5625, 0.0625
beta <- c(0.5,0.7,0.9,0.8) # breeding probabilities
#(in the following order beta1,beta2,beta3,beta4)
gamma <- c(0.4,0.5,0.6,0.7) # probability of litter size of 2
#(in the following order gamma1,gamma2,gamma3,gamma4)
```

Define the states and the events used in the model:

```
## Define the states (12 states = 11 alive+ 1dead) describe family unit composition
# as decribed in the methods section
```

```
    # J2 independent 2yo juvenile female
    # J3 independent 3yo juvenile female
    #SA4 independent 4yo subadult female
    #SA5 independent 5yo subadult female
    #A01 adult female caring for 1 dependent offspring of the year (age <1)
    #A02 adult female caring for 2 dependent offspring of the year (age <1)
    #A11 adult female caring for 1 dependent yearling (age 1)
    #A12 adult female caring for 2 dependent yearlings (age 1)
    #AS1 adult female successful breeder raising 1 offspring reaching independence
    #AS2 adult female successful breeder raising 2 offspring reaching independence
    #A adult female without dependent offspring
    # D dead state
n.states <- 11
all.states <- n.states + 1 # with dead state
## Define the events
# as defined in the methods section
    # non-observation code "O"
    # capture of a 2y female code "1"
    # capture of a 3y female code "2"
    # capture of a 4y female code "3"
    # capture of a 5y female code "4"
    # capture of an adult female with 1 offspring of the year (age <1) code "5"
    # capture of an adult female with 2 offspring of the year (age <1) code "6"
    # capture of an adult female with 1 yearling code "\eta"
    # capture of an adult female with 2 yearlings code "8"
    # capture of an adult female with 1 two-year old offspring code "9"
    # capture of an adult female with 2 two-year old offspring code "10"
    # capture of an adult female alone code "11"
n.events <- 11
all.events <- n.events + 1 #with not seen
```

Define the initial state vector, gathering the proportion of individual in each state at first capture:

```
SO <- c(rep(1/n.states,n.states),0)#initial state vector SO
```

Here we considered equal proportions in the eleven alive states.
Now construct the transition matrices PHI, PS11, PSI2, PSI3 involved in the state process:

```
### State transitions
# define PHI matrix gathering survival of independent juveniles, subadults and adults
temp1 <- diag(c(phi,phi,phi,phi,rep(phi,7)),nrow=all.states,ncol=n.states)
PHI <- cbind(temp1,c(1-phi,1-phi,1-phi,1-phi,rep(1-phi,7),1))
# Define PSI matrices gathering state-to-state transition probabilities, it includes:
# PSI1: litter survival, individual dependent offspring suvival and growth to next age:
PSI1 <- matrix(0,nrow=all.states,ncol=all.states + 1)
for(i in 1:3){PSI1[i,i] <- 1} # juvenile and subadults grow to next age
PSI1[4,12] <- 1 # 5a grow to sexually mature female without dependent offspring
PSI1[5,4] <- psi[1] ; PSI1[5,8] <- (1-psi[1]) #a0 offspring survives or dies
PSI1[6,4] <- psi[2] ; PSI1[6,5] <- psi[3] ; PSI1[6,8] <- psi[4]#1,both
#or any aO offspring in a litter of 2 survive
PSI1[7,6] <- psi[5] ; PSI1[7,9] <- (1-psi[5])#a1 offspring in a litter
#of 1 survives or die
```

```
PSI1[8,6] <- psi[6] ; PSI1[8,7] <- psi[7] ;PSI1[8,9] <- psi[8]#1,both or any
#a1 offspring in a litter of 2 survive or die
for(i in 9:12){PSI1[i,i+1] <- 1} # for offspring reaching independence and females
#without dependent offspring
# PSI2: breeding probabilities:
PSI2 <- matrix(0,nrow=all.states+1,ncol=all.states+4)
for(i in 1:7){PSI2[i,i] <- 1} # here we assume that juveniles, subaduts and adults
#caring for dependent offspring are not available to breed
PSI2[8,8] <- beta[1];PSI2[8,9] <- 1-beta[1]
PSI2[9,10] <- beta[2];PSI2[9,11] <- 1-beta[2]
PSI2[10,12] <- beta[3];PSI2[10,13] <- 1-beta[3]
PSI2[11,12] <- beta[3];PSI2[11,13] <- 1-beta[3]
PSI2[12,14] <- beta[4];PSI2[12,15] <- 1-beta[4]
PSI2[13,16] <- 1 # dead state
# PSI3:litter size probabilities
#(Pr(singleton litter) = gamma, Pr(twin litter)= 1-gamma)
PSI3 <- matrix(0,nrow=all.states+4,ncol=all.states)
for(i in 1:3){PSI3[i,i+1] <- 1}
for(i in 4:7){PSI3[i,i+3] <- 1}
PSI3[8,5] <- gamma[1];PSI3[8,6] <- 1-gamma[1]
PSI3[9,11] <-1
PSI3[10,5] <- gamma[2];PSI3[10,6] <- 1-gamma[2]
PSI3[11,11] <-1
PSI3[12,5] <- gamma[3];PSI3[12,6] <- 1-gamma[3]
PSI3[13,11] <-1
PSI3[14,5] <- gamma[4];PSI3[14,6] <- 1-gamma[4]
PSI3[15,11] <-1
PSI3[16,12] <-1
```

We can now define the part of the observation process (matrix $E 2$ modeling capture probability, matrix $E 1$ will be defined later) which does not depend on capture date:

```
# Define observation process
# step 1 : matrix E1
# it involves departure probability which is function of day of capture,
#it will be define below within the loop
# step 2 : matrix E2, involves capture probability
E2 <- matrix(0,nrow=all.states, ncol=all.events)
for(i in 1:all.states){E2[i,i] <- p} #detection probability
E2[,all.events] <- c(rep(1-p,4), rep(1-p,7),1)
```

Below, we generate the data using multinomial trials for each sampling occasion, for each family unit. This script is based on the script from Chapter 7 in Kery and Schaub (2011) to simulate multistate CMR data. To deal with variable timing at offspring independence, the probabilities within matrix $E 1$ used in the observation process depend on date of capture. Matrix $E 1$ is therefore defined within the loop for each individual at each sampling occasion depending on its date of capture.

```
## Generate data
for(r in 1:nrepet){ # number of dataset generated
    marked <- matrix(0, ncol = all.states, nrow = n.occasions) # empty object to store
    #marked family units
```

```
for(t in 1:n.occasions){
    marked[t,] <- rmultinom(1,R,prob=S0) # define states at first capture
}
    # Below we use transition and event matrices wwtih 4-dimensions:
    # Dimension 1: state of departure
    # Dimension 2: state of arrival
    # Dimension 3: family unit
    # Dimension 4: time
    # 1. State process matrix
    totrel <- sum(marked)*(n.occasions-1)
    PSI.STATE <- array(NA, dim=c(all.states, all.states, totrel, n.occasions-1))
    for (i in 1:totrel){
        for (t in 1:(n.occasions-1)){
            PSI.STATE[,,i,t] <- PHI %*% PSI1 %*% PSI2 %*% PSI3 # transition matrix
            #is the matrix product of PHI PSI1 PSI2 and PSI3 defiend above
        } #t
    } #i
    # 2.Observation process matrix
    E <- array(NA, dim=c(all.states, all.events, totrel, n.occasions-1))
    # day of capture, sampled from polar bears capture dates
    daycapt <- matrix(sample(wcapt,size=(totrel*(n.occasions-1)),
                                    replace=TRUE), nrow=totrel, ncol=n.occasions-1)
        for (i in 1:totrel){
        for (t in 1:(n.occasions-1)){
    # predict departure probability function of date of capture
    alpha <- predict(modeld,newdata=list(doy=daycapt[i,t]),type="response")
    # now define event matrix E1 using departure probability alpha
    E1 <- diag(1,nrow=all.states,ncol=all.events)
    E1[9,9 ]<- 1-alpha
    E1[9,10]<- 0
    E1[9,11]<- alpha
    E1[10,9]<- 2*(1-alpha)*alpha
    E1[10,10]<- 1 - (2*(1-alpha)*alpha) - (alpha)^2
    E1[10,11]<- (alpha)^2
            E[,,i,t] <- E1 %*% E2 # define E which is the matrix product of E1 and E2
        } #t
    } #i
}#r
```

Make a function to simulate the data using the state and event matrices we just defined:

```
# Define function to simulate multistate capture-recapture data
simul.ms <- function(PSI.STATE, E, marked, unobservable = NA){
    # Unobservable: number of state that is unobservable
    n.occasions <- dim(PSI.STATE)[4] + 1
    CH <- CH.TRUE <- dayC <- matrix(NA, ncol = n.occasions, nrow = sum(marked))
```

```
    # Define a vector with the occasion of marking
    mark.occ <- matrix(0, ncol = dim(PSI.STATE)[1], nrow = sum(marked))
    g <- colSums(marked)
    for (s in 1:dim(PSI.STATE)[1]){
        if (g[s]==0) next # To avoid error message if nothing to replace
        mark.occ[(cumsum(g[1:s])-g[s]+1)[s]:cumsum(g[1:s])[s],s] <-
            rep(1:n.occasions, marked[1:n.occasions,s])
    } #s
    for (i in 1:sum(marked)){
        for (s in 1:dim(PSI.STATE)[1]){
            if (mark.occ[i,s]==0) next
            first <- mark.occ[i,s]
            CH[i,first] <- s
            CH.TRUE[i,first] <- s
        } #s
        for (t in (first+1):n.occasions){
            # Multinomial trials for state transitions
            if (first==n.occasions) next
            state <- which(rmultinom(1, 1, PSI.STATE[CH.TRUE[i,t-1],,i,t-1])==1)
            CH.TRUE[i,t] <- state
            # Multinomial trials for observation process
            event <- which(rmultinom(1, 1, E[CH.TRUE[i,t],,i,t-1])==1)
            CH[i,t] <- event
            dayC[i,t] <- daycapt[i,t-1]
        } #t
    } #i
    # Replace the NA and the highest state number (dead) in the file by 0
    CH[is.na(CH)] <- 0
    CH[CH==dim(PSI.STATE) [1]] <- 0
    CH[CH==unobservable] <- 0
    id <- numeric(0)
    for (i in 1:dim(CH)[1]){
        z <- min(which(CH[i,]!=0))
        ifelse(z==dim(CH)[2], id <- c(id,i), id <- c(id))
    }
    return(list(CH=CH[-id,], CH.TRUE=CH.TRUE[-id,],dayC=dayC[-id,]))
    # CH: capture histories to be used
    # CH.TRUE: capture histories with perfect observation
    # dayC: date of capture
}
```

Generate the data using the function above, and save the family units CR histories, underlying states and dates of captures:

```
# Execute function
sim <- simul.ms(PSI.STATE, E, marked)
CH <- sim$CH # family units CR histories
init <- sim$CH.TRUE # real state matrix used as initial values for jags model
daycapt <- sim$dayC # info on date of capture
# save files
write.table(CH,paste("simCH",r,"_p",p,"_T",n.occasions,".txt",
    sep=""),row.names=F, col.names=F, sep =" ")
write.table(init,paste("siminit",r,"_p",p,"_T",n.occasions,".txt",
    sep=""),row.names=F, col.names=F, sep =" ")
```

```
    write.table(daycapt,paste("simdaycapt",r,"_p",p,"_T",n.occasions,".txt",sep=""),
    row.names=F, col.names=F, sep =" ")
}
```


## Fit the model to simulated data

First, load the required package:

```
# Load packages
library(jagsUI)
## Loading required package: lattice
##
## Attaching package: 'jagsUI'
## The following object is masked from 'package:utils':
##
## View
```

Choose working directory name corresponding to scenario S1, S2, S3 or S4 (to read the corresponding data):

```
rep <- c("S1_p025alphaconstant","S2p025alphadate","S3p05alphaconstant","S4p05alphadate")
```

repname <- rep[1] \#\# 1 for S1, 2 for S2, 3 for S3, 4 for S4

Define capture probability and model to infer departure probability used to simulate the data in the corresponding scenario: S1 (low detection, apha constant=0.5), S2 (low detection alpha varies with date of capture), S3 (high detection, apha constant $=0.5$ ) or S 4 (low detection alpha varies with date of capture):

```
S <- 2 # set to 1 for S1, 2 for S2, 3 for S3 or 4 for S4
capture <- c(0.25,0.25,0.5,0.5) # capture probability
p <- capture[S]
filename <- c("glmdeparture_alphaconstant05.Rdata","glm_departure_date.Rdata",
    "glmdeparture_alphaconstant05.Rdata","glm_departure_date.Rdata")
fileS <- filename[S]
load(file=paste(fileS))
n.occasions =15 # number of sampling occasions
nrepet = 100 # number of simulated dataset (repetitions)
```

Sink the jags model :

```
# JAGS MODEL
sink("Multieventmodel_Fit_simul.txt")
cat("
model {
    # Probabilities of events given states and states given states
    # vector of initial states
    SO[1] <- prop[1] / (1 + sum(prop[1:10])) # prob. of being in initial state J2
    SO[2] <- prop[2] / (1 + sum(prop[1:10])) # prob. of being in initial state J3
    SO[3] <- prop[3] / (1 + sum(prop[1:10])) # prob. of being in initial state SA4
    SO[4] <- prop[4] / (1 + sum(prop[1:10])) # prob. of being in initial state SA5
    S0[5] <- prop[5] / (1 + sum(prop[1:10])) # prob. of being in initial state A01
```

```
SO[6] <- prop[6] / (1 + sum(prop[1:10])) # prob. of being in initial state A02
SO[7] <- prop[7] / (1 + sum(prop[1:10])) # prob. of being in initial state A11
S0[8] <- prop[8] / (1 + sum(prop[1:10])) # prob. of being in initial state A12
SO[9] <- prop[9] / (1 + sum(prop[1:10])) # prob. of being in initial state AS1
SO[10] <- prop[10] / (1 + sum(prop[1:10])) # prob. of being in initial state AS2
SO[11] <- 1 / (1 + sum(prop[1:10])) # prob. of being in initial state A-
SO[12] <- O # prob. of being in initial state dead
# State process: define probabilities of S(t+1) given S(t)
# define PHI matrix gathering survival of independent juveniles, subadults and adults
PHI [ 1 , 1 ]<- phi
PHI [ 1 , 2 ]<- 0
PHI [ 1 , 3 ]<- 0
PHI [ 1 , 4 ]<- 0
PHI [ 1 , 5 ]<- 0
PHI [ 1 , 6 ]<- 0
PHI [ 1 , 7 ]<- 0
PHI [ 1 , 8 ]<- 0
PHI [ 1 , 9 ]<- 0
PHI [ 1 , 10 ]<- 0
PHI [ 1 , 11 ]<- 0
PHI [ 1 , 12 ]<- 1-phi
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline PHI & [ & 2 & & 1 & ]<- & 0 \\
\hline PHI & [ & 2 & & 2 & ]<- & \\
\hline PHI & [ & 2 & & 3 & ]<- & 0 \\
\hline PHI & [ & 2 & , & 4 & ]<- & 0 \\
\hline PHI & [ & 2 & & 5 & ]<- & 0 \\
\hline PHI & [ & 2 & & 6 & ]<- & 0 \\
\hline PHI & [ & 2 & & 7 & ]<- & 0 \\
\hline PHI & [ & 2 & & 8 & ]<- & 0 \\
\hline PHI & [ & 2 & , & 9 & ]<- & 0 \\
\hline PHI & [ & 2 & & 10 & ]<- & 0 \\
\hline PHI & [ & 2 & & 11 & ]<- & 0 \\
\hline PHI & [ & 2 & & 12 & ]<- & 1-phi \\
\hline
\end{tabular}
PHI [ 3 , 1 ]<- 0
PHI [ 3 , 2 ]<- 0
PHI [ 3 , 3 ]<- phi
PHI [ 3 , 4 ]<- 0
PHI [ 3 , 5 ]<- 0
PHI [ 3 , 6 ]<- 0
PHI [ 3 , 7 ]<- 0
PHI [ 3 , 8 ]<- 0
PHI [ 3 , 9 ]<- 0
PHI [ 3 , 10 ]<- 0
PHI [ 3 , 11 ]<- 0
PHI [ 3 , 12 ]<- 1-phi
PHI [ 4 , 1 ]<- 0
PHI [ 4 , 2 ]<- 0
PHI [ 4 , 3 ]<- 0
PHI [ 4 , 4 ]<- phi
```

| PHI | [ | 4 | , | 5 | ]<-0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 4 | , | 6 | ]<-0 |
| PHI | [ | 4 | , | 7 | ]<-0 |
| PHI | [ | 4 | , | 8 | ]<-0 |
| PHI | [ | 4 | , | 9 | ]<-0 |
| PHI | [ | 4 | , | 10 | ]<-0 |
| PHI | [ | 4 | , | 11 | ]<-0 |
| PHI | [ | 4 | , | 12 | ]<- 1 - phi |
| PHI | [ | 5 | , | 1 | ]<-0 |
| PHI | [ | 5 | , | 2 | ]<-0 |
| PHI | [ | 5 | , | 3 | ]<-0 |
| PHI | [ | 5 | , | 4 | ]<-0 |
| PHI | [ | 5 | , | 5 | ]<- phi |
| PHI | [ | 5 | , | 6 | ]<-0 |
| PHI | [ | 5 | , | 7 | ]<-0 |
| PHI | [ | 5 | , | 8 | ]<-0 |
| PHI | [ | 5 | , | 9 | ]<-0 |
| PHI | [ | 5 | , | 10 | ]<-0 |
| PHI | [ | 5 | , | 11 | ]<-0 |
| PHI | [ | 5 | , | 12 | ]<- 1 - phi |
| PHI | [ | 6 | , | 1 | ]<-0 |
| PHI | [ | 6 | , | 2 | ]<-0 |
| PHI | [ | 6 | , | 3 | ]<-0 |
| PHI | [ | 6 | , | 4 | ]<-0 |
| PHI | [ | 6 | , | 5 | ]<-0 |
| PHI | [ | 6 | , | 6 | ]<- phi |
| PHI | [ | 6 | , | 7 | ]<-0 |
| PHI | [ | 6 | , | 8 | ]<-0 |
| PHI | [ | 6 | , | 9 | ]<-0 |
| PHI | [ | 6 | , | 10 | ]<-0 |
| PHI | [ | 6 | , | 11 | ]<-0 |
| PHI | [ | 6 | , | 12 | ]<- 1 - phi |
| PHI | [ | 7 | , | 1 | ]<-0 |
| PHI | [ | 7 | , | 2 | ]<-0 |
| PHI | [ | 7 | , | 3 | ]<-0 |
| PHI | [ | 7 | , | 4 | ]<-0 |
| PHI | [ | 7 | , | 5 | ]<-0 |
| PHI | [ | 7 | , | 6 | ]<-0 |
| PHI | [ | 7 | , | 7 | ]<- phi |
| PHI | [ | 7 | , | 8 | ]<-0 |
| PHI | [ | 7 | , | 9 | ]<-0 |
| PHI | [ | 7 | , | 10 | ]<-0 |
| PHI | [ | 7 | , | 11 | ]<- 0 |
| PHI | [ | 7 | , | 12 | ]<- 1-phi |
| PHI | [ | 8 | , | 1 | ]<-0 |
| PHI | [ | 8 | , | 2 | ]<-0 |
| PHI | [ | 8 | , | 3 | ]<-0 |
| PHI | [ | 8 | , | 4 | ]<-0 |
| PHI | [ | 8 |  | 5 | ]<-0 |


| PHI | [ | 8 | 6 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 8 | 7 | ]<- 0 |
| PHI | [ | 8 | 8 | ]<- phi |
| PHI | [ | 8 | 9 | ]<-0 |
| PHI | [ | 8 | 10 | ]<- 0 |
| PHI | [ | 8 | 11 | ]<- 0 |
| PHI | [ | 8 | 12 | ]<- 1-phi |
| PHI | [ | 9 | 1 | ]<- 0 |
| PHI | [ | 9 | 2 | ]<-0 |
| PHI | [ | 9 | 3 | ]<-0 |
| PHI | [ | 9 | 4 | ]<- 0 |
| PHI | [ | 9 | 5 | ]<- 0 |
| PHI | [ | 9 | 6 | ]<-0 |
| PHI | [ | 9 | 7 | ]<- 0 |
| PHI | [ | 9 | 8 | ]<- 0 |
| PHI | [ | 9 | 9 | ]<- phi |
| PHI | [ | 9 | 10 | ]<- 0 |
| PHI | [ | 9 | 11 | ]<- 0 |
| PHI | [ | 9 | 12 | ]<- 1-phi |
| PHI | [ | 10 | 1 | ]<- 0 |
| PHI | [ | 10 | 2 | ]<- 0 |
| PHI | [ | 10 | 3 | ]<- 0 |
| PHI | [ | 10 | 4 | ]<-0 |
| PHI | [ | 10 | 5 | ]<- 0 |
| PHI | [ | 10 | 6 | ]<-0 |
| PHI | [ | 10 | 7 | ]<-0 |
| PHI | [ | 10 | 8 | ]<-0 |
| PHI | [ | 10 | 9 | ]<- 0 |
| PHI | [ | 10 | 10 | ]<- phi |
| PHI | [ | 10 | 11 | ]<- 0 |
| PHI | [ | 10 | 12 | ]<- 1-phi |
| PHI | [ | 11 | 1 | ]<- 0 |
| PHI | [ | 11 | 2 | ]<- 0 |
| PHI | [ | 11 | 3 | ]<- 0 |
| PHI | [ | 11 | 4 | ]<- 0 |
| PHI | [ | 11 | 5 | ]<- 0 |
| PHI | [ | 11 | 6 | ]<- 0 |
| PHI | [ | 11 | 7 | ]<- 0 |
| PHI | [ | 11 | 8 | ]<- 0 |
| PHI | [ | 11 | 9 | ]<- 0 |
| PHI | [ | 11 | 10 | ]<-0 |
| PHI | [ | 11 | 11 | ]<- phi |
| PHI | [ | 11 | 12 | ]<- 1-phi |
| PHI | [ | 12 | 1 | ]<- 0 |
| PHI | [ | 12 | 2 | ]<-0 |
| PHI | [ | 12 | 3 | ]<-0 |
| PHI | [ | 12 | 4 | ]<-0 |
| PHI | [ | 12 | 5 | ]<-0 |
| PHI | [ | 12 | 6 | ]<- 0 |


| PHI | $[$ | 12 | , | 7 | $]<-$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 12 | 0 |  |  |
| PHI | $[$ | 8 | $]<-$ | 0 |  |
| PHI | $[$ | 12 | 9 | $]<-$ | 0 |
| PHI | $[$ | 12 | 10 | $]<-$ | 0 |
| PHI | $[$ | 12 | 11 | $]<-$ | 0 |
|  | 12 | $]<-$ | 1 |  |  |

\# Define PSI matrices gathering state-to-state transition probabilities, it includes:
\# PSI1: offspring survival and growth to next age, proba of sexual maturation:
PSI1 $[1 \quad, \quad 1 \quad]<-1$
PSI1 $[1,30$
PSI1 $[1,4]<-0$
PSI1 [ 1 , 5 ]<- 0
PSI1 $[1 \quad, \quad 6 \quad]<-0$
PSI1 $[1 \quad, \quad 7 \quad]<-0$
PSI1 $[1$, 8 ]<- 0
PSI1 [ 1 , 9 ]<- 0
PSI1 [ 1 , 10 ]<- 0
PSI1 [ 1 , 11 ]<- 0
PSI1 $[1, \quad 12]<-0$
PSI1 $[1, \quad 13]<-0$
PSI1 $[2,01]<-0$
PSI1 $[2,2]<-1$
PSI1 $[2,03<-0$
PSI1 $[2,4]<-0$
PSI1 $[2,05]<-0$
PSI1 $[2,6]<-0$
PSI1 $[2,7]<-0$
PSI1 $[2,8]<-0$
PSI1 $[2,0$
PSI1 $[2,010]<-0$
PSI1 $[2,011]<-0$
PSI1 $[2, \quad 12]<-0$
PSI1 $[2, \quad 13]<-0$
PSI1 $[3,01]<-0$
PSI1 $[3,2]<-0$
PSI1 [ 3 , 3 ]<- 1-kappa \# first repro at age 6
PSI1 $[3,4]<-0$
PSI1 $[3,5]<-0$
PSI1 $[3,6]<-0$
PSI1 $[3,7]<-0$
PSI1 $[3,0]<-0$
PSI1 $[3,0]<-0$
PSI1 $[3,0$
PSI1 $[3,011]<-0$
PSI1 [ 3 , 12 ]<- kappa \# first repro at age 5
PSI1 $[3,13]<-0$
PSI1 $[4,1 \quad]<-0$
PSI1 $[4,2]<-0$

```
PSI1 [ 4 , 3 ]<- 0
PSI1 [ 4 , 4 ]<- 0
PSI1 [ 4 , 5 ]<- 0
PSI1 [ 4 , 6 ]<- 0
PSI1 [ 4 , 7 ]<- 0
PSI1 [ 4 , 8 ]<- 0
PSI1 [ 4 , 9 ]<- 0
PSI1 [ 4 , 10 ]<- 0
PSI1 [ 4 , 11 ]<- 0
PSI1 [ 4 , 12 ]<- 1
PSI1 [ 4 , 13 ]<- 0
PSI1 [ 5 , 1 ]<- 0
PSI1 [ 5 , 2 ]<- 0
PSI1 [ 5 , 3 ]<- 0
PSI1 [ 5 , 4 ]<- s[1] # litter of 1, cub's survival
PSI1 [ 5 , 5 ]<- 0
PSI1 [ 5 , 6 ]<- 0
PSI1 [ 5 , 7 ]<- 0
PSI1 [ 5 , 8 ]<- 1-s[1] #litter of 1, cub's death
PSI1 [ 5 , 9 ]<- 0
PSI1 [ 5 , 10 ]<- 0
PSI1 [ 5 , 11 ]<- 0
PSI1 [ 5 , 12 ]<- 0
PSI1 [ 5 , 13 ]<- 0
PSI1 [ 6 , 1 ]<- 0
PSI1 [ 6 , 2 ]<- 0
PSI1 [ 6 , 3 ]<- 0
PSI1 [ 6 , 4 ]<- 2*s[2]*(1-s[2]) # litter of 2, 1 cub survives
PSI1 [ 6 , 5 ]<- s[2]^2 # litter of 2, both cubs survive
PSI1 [ 6 , 6 ]<- 0
PSI1 [ 6 , 7 ]<- 0
PSI1 [ 6 , 8 ]<- (1- s[2]~2 -2*s[2]*(1-s[2])) #litter of 2, both cubs die
PSI1 [ 6 , 9 ]<- 0
PSI1 [ 6 , 10 ]<- 0
PSI1 [ 6 , 11 ]<- 0
PSI1 [ 6 , 12 ]<- 0
PSI1 [ 6 , 13 ]<- 0
PSI1 [ 7 , 1 ]<- 0
PSI1 [ 7 , 2 ]<- 0
PSI1 [ 7 , 3 ]<- 0
PSI1 [ 7 , 4 ]<- 0
PSI1 [ 7 , 5 ]<- 0
PSI1 [ 7 , 6 ]<- s[3] # litter of 1, yearling's survival
PSI1 [ 7 , 7 ]<- 0
PSI1 [ 7 , 8 ]<- 0
PSI1 [ 7 , 9 ]<- (1-s[3] ) # litter of 1, yearling's death
PSI1 [ 7 , 10 ]<- 0
PSI1 [ 7 , 11 ]<- 0
PSI1 [ 7 , 12 ]<- 0
PSI1 [ 7 , 13 ]<- 0
```

```
PSI1 [ 8 , 1 ]<- 0
PSI1 [ 8 , 2 ]<- 0
PSI1 [ 8 , 3 ]<- 0
PSI1 [ 8 , 4 ]<- 0
PSI1 [ 8 , 5 ]<- 0
PSI1 [ 8 , 6 ]<- 2*s[4]*(1-s[4]) # litter of 2, 1 yearling survives
PSI1 [ 8 , 7 ]<- s[4]^2 # litter of 2, both yearlings survive
PSI1 [ 8 , 8 ]<- 0
PSI1 [ 8 , 9 ]<- (1- s[4] 2 -2*s[4]*(1-s[4])) #litter of 2, both yearlings die
PSI1 [ 8 , 10 ]<- 0
PSI1 [ 8 , 11 ]<- 0
PSI1 [ 8 , 12 ]<- 0
PSI1 [ 8 , 13 ]<- 0
PSI1 [ 9 , 1 ]<- 0
PSI1 [ 9 , 2 ]<- 0
PSI1 [ 9 , 3 ]<- 0
PSI1 [ 9 , 4 ]<- 0
PSI1 [ 9 , 5 ]<- 0
PSI1 [ 9 , 6 ]<- 0
PSI1 [ 9 , 7 ]<- 0
PSI1 [ 9 , 8 ]<- 0
PSI1 [ 9 , 9 ]<- 0
PSI1 [ 9 , 10 ]<- 1
PSI1 [ 9 , 11 ]<- 0
PSI1 [ 9 , 12 ]<- 0
PSI1 [ 9 , 13 ]<- 0
PSI1 [ 10 , 1 ]<- 0
PSI1 [ 10 , 2 ]<- 0
PSI1 [ 10, 3 ]<- 0
PSI1 [ 10, 4 ]<- 0
PSI1 [ 10, 5 ]<- 0
PSI1 [ 10 , 6 ]<- 0
PSI1 [ 10, 7 ]<- 0
PSI1 [ 10 , 8 ]<- 0
PSI1 [ 10 , 9 ]<- 0
PSI1 [ 10 , 10 ]<- 0
PSI1 [ 10 , 11 ]<- 1
PSI1 [ 10 , 12 ]<- 0
PSI1 [ 10 , 13 ]<- 0
PSI1 [ 11 , 1 ]<- 0
PSI1 [ 11 , 2 ]<- 0
PSI1 [ 11 , 3 ]<- 0
PSI1 [ 11 , 4 ]<- 0
PSI1 [ 11 , 5 ]<- 0
PSI1 [ 11 , 6 ]<- 0
PSI1 [ 11 , 7 ]<- 0
PSI1 [ 11 , 8 ]<- 0
PSI1 [ 11 , 9 ]<- 0
PSI1 [ 11 , 10 ]<- 0
PSI1 [ 11 , 11 ]<- 0
```


\# PSI2: breeding probabilities:
PSI2 [ 1 , 1 ]<- 1
PSI2 $[1,2]<-0$
PSI2 $[1,3]<-0$
PSI2 $[1], 4]<-0$
PSI2 [ 1 , 5 ]<- 0
PSI2 $[1,6]<-0$
PSI2 [ 1 , 7 ]<- 0
PSI2 [ 1 , 8 ]<- 0
PSI2 [ 1 , 9 ]<- 0
PSI2 [ 1 , 10 ]<- 0
PSI2 [ 1 , 11 ]<- 0
PSI2 [ 1 , 12 ]<- 0
PSI2 [ 1 , 13 ]<- 0
PSI2 [ 1 , 14 ]<- 0
PSI2 [ 1 , 15 ]<- 0
PSI2 $[1,16]<-0$
PSI2 [ 2,1 ]<- 0
PSI2 $[2,2]<-1$
PSI2 [ 2,3 ]<- 0
PSI2 [ 2,4 ]<- 0
PSI2 [ 2 , 5 ]<- 0
PSI2 [ 2,6 ]<- 0
PSI2 [ 2,7 ]<- 0
PSI2 [ 2,8 ]<- 0
PSI2 $[2,0]<-0$
PSI2 [ 2,10 ]<- 0
PSI2 $[2,11]<-0$
PSI2 $[2,12]<-0$
PSI2 $[2,13]<-0$
PSI2 [ 2,14 ]<- 0
PSI2 $[2,15]<-0$
PSI2 [ 2,16 ]<- 0
PSI2 [ 3 , 1 ]<- 0

| PSI2 | [ | 3 | , 2 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 3 | 3 | ]<- 1 |
| PSI2 | [ | 3 | 4 | ]<- 0 |
| PSI2 | [ | 3 | 5 | ]<- 0 |
| PSI2 | [ | 3 | 6 | ]<- 0 |
| PSI2 | [ | 3 | 7 | ]<- 0 |
| PSI2 | [ | 3 | 8 | ]<- 0 |
| PSI2 | [ | 3 | 9 | ]<- 0 |
| PSI2 | [ | 3 | 10 | ]<- 0 |
| PSI2 | [ | 3 | 11 | ]<- 0 |
| PSI2 | [ | 3 | 12 | ]<- 0 |
| PSI2 | [ | 3 | 13 | ]<- 0 |
| PSI2 | [ | 3 | 14 | ]<- 0 |
| PSI2 | [ | 3 | 15 | ]<- 0 |
| PSI2 | [ | 3 | 16 | ]<- 0 |
| PSI2 | [ | 4 | 1 | ]<- 0 |
| PSI2 | [ | 4 | 2 | ]<- 0 |
| PSI2 | [ | 4 | 3 | ]<- 0 |
| PSI2 | [ | 4 | 4 | ]<-1 |
| PSI2 | [ | 4 | 5 | ]<- 0 |
| PSI2 | [ | 4 | 6 | ]<- 0 |
| PSI2 | [ | 4 | 7 | ]<- 0 |
| PSI2 | [ | 4 | 8 | ]<- 0 |
| PSI2 | [ | 4 | 9 | ]<- 0 |
| PSI2 | [ | 4 | 10 | ]<- 0 |
| PSI2 | [ | 4 | 11 | ]<- 0 |
| PSI2 | [ | 4 | 12 | ]<- 0 |
| PSI2 | [ | 4 | 13 | ]<- 0 |
| PSI2 | [ | 4 | 14 | ]<-0 |
| PSI2 | [ | 4 | 15 | ]<- 0 |
| PSI2 | [ | 4 | 16 | ]<- 0 |
| PSI2 | [ | 5 | 1 | ]<- 0 |
| PSI2 | [ | 5 | 2 | ]<- 0 |
| PSI2 | [ | 5 | 3 | ]<- 0 |
| PSI2 | [ | 5 | 4 | ]<- 0 |
| PSI2 | [ | 5 | 5 | ]<-1 |
| PSI2 | [ | 5 | 6 | ]<- 0 |
| PSI2 | [ | 5 | 7 | ]<-0 |
| PSI2 | [ | 5 | 8 | ]<-0 |
| PSI2 | [ | 5 | 9 | ]<- 0 |
| PSI2 | [ | 5 | 10 | ]<- 0 |
| PSI2 | [ | 5 | 11 | ]<- 0 |
| PSI2 | [ | 5 | 12 | ]<- 0 |
| PSI2 | [ | 5 | 13 | ]<- 0 |
| PSI2 | [ | 5 | 14 | ]<- 0 |
| PSI2 | [ | 5 | 15 | ]<- 0 |
| PSI2 | [ | 5 | 16 | ]<- 0 |
| PSI2 | [ | 6 | 1 | ]<- 0 |
| PSI2 | [ | 6 | 2 | ]<- 0 |
| PSI2 | [ | 6 | 3 | ]<- 0 |


| PSI2 | [ | 6 | , | 4 | ]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 6 | , | 5 | ]<- |  |
| PSI2 | [ | 6 | , | 6 | ]<- |  |
| PSI2 | [ | 6 | , | 7 | ]<- |  |
| PSI2 | [ | 6 | , | 8 | ]<- |  |
| PSI2 | [ | 6 | , | 9 | ]<- | 0 |
| PSI2 | [ | 6 | , | 10 | ]<- | 0 |
| PSI2 | [ | 6 | , | 11 | ]<- | 0 |
| PSI2 | [ | 6 | , | 12 | ]<- | 0 |
| PSI2 | [ | 6 | , | 13 |  | 0 |
| PSI2 | [ | 6 | , | 14 |  | 0 |
| PSI2 | [ | 6 | , | 15 |  | 0 |
| PSI2 | [ | 6 |  | 16 | ]<- | 0 |
| PSI2 | [ | 7 | , | 1 | ]<- |  |
| PSI2 | [ | 7 | , | 2 | ]<- | 0 |
| PSI2 | [ | 7 |  | 3 | ]<- | 0 |
| PSI2 | [ | 7 | , | 4 | ]<- | 0 |
| PSI2 | [ | 7 | , | 5 | ]<- | 0 |
| PSI2 | [ | 7 | , | 6 | ]<- | 0 |
| PSI2 | [ | 7 | , | 7 | ]<- | 1 |
| PSI2 | [ | 7 | , | 8 | ]<- | 0 |
| PSI2 | [ | 7 | , | 9 | ]<- | 0 |
| PSI2 | [ | 7 | , | 10 | ]<- | 0 |
| PSI2 | [ | 7 | , | 11 | ]<- | 0 |
| PSI2 | [ | 7 | , | 12 | ]<- | 0 |
| PSI2 | [ | 7 | , | 13 | ]<- | 0 |
| PSI2 | [ | 7 | , | 14 | ]<- | 0 |
| PSI2 | [ | 7 | , | 15 | ]<- | 0 |
| PSI2 | [ | 7 | , | 16 | ]<- |  |
| PSI2 | [ | 8 | , | 1 | ]<- |  |
| PSI2 | [ | 8 | , | 2 | ]<- | 0 |
| PSI2 | [ | 8 | , | 3 | ]<- | 0 |
| PSI2 | [ | 8 | , | 4 | ]<- | 0 |
| PSI2 | [ | 8 | , | 5 | ]<- | 0 |
| PSI2 | [ | 8 |  | 6 | ]<- | 0 |
| PSI2 | [ | 8 |  | 7 | ]<- | 0 |
| PSI2 | [ | 8 |  | 8 | ]<- | beta[1] |
| PSI2 | [ | 8 |  | 9 | ]<- | 1-beta[1] |
| PSI2 | [ | 8 |  | 10 | ]<- | 0 |
| PSI2 | [ | 8 |  | 11 | ]<- | 0 |
| PSI2 | [ | 8 |  | 12 | ]<- | 0 |
| PSI2 | [ | 8 |  | 13 | ]<- | 0 |
| PSI2 | [ | 8 | , | 14 | ]<- | 0 |
| PSI2 | [ | 8 | , | 15 | ]<- |  |
| PSI2 | [ | 8 | , | 16 | ]<- |  |
| PSI2 | [ | 9 | , | 1 | ]<- |  |
| PSI2 | [ | 9 |  | 2 | ]<- |  |
| PSI2 | [ | 9 |  | 3 | ]<- | 0 |
| PSI2 | [ | 9 |  | 4 | ]<- | 0 |
| PSI2 | [ | 9 |  | 5 | ]<- | 0 |


| PSI2 | [ | 9 | 6 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 9 | 7 | ]<- 0 |
| PSI2 | [ | 9 | 8 | ]<- 0 |
| PSI2 | [ | 9 | 9 | ]<- 0 |
| PSI2 | [ | 9 | 10 | ]<- beta[2] |
| PSI2 | [ | 9 | 11 | ]<- 1-beta[2] |
| PSI2 | [ | 9 | 12 | ]<- 0 |
| PSI2 | [ | 9 | 13 | ]<- 0 |
| PSI2 | [ | 9 | 14 | ]<- 0 |
| PSI2 | [ | 9 | 15 | ]<- 0 |
| PSI2 | [ | 9 | 16 | ]<- 0 |
| PSI2 | [ | 10 | 1 | ]<- 0 |
| PSI2 | [ | 10 | 2 | ]<-0 |
| PSI2 | [ | 10 | 3 | ]<-0 |
| PSI2 | [ | 10 | 4 | ]<- 0 |
| PSI2 | [ | 10 | 5 | ]<- 0 |
| PSI2 | [ | 10 | 6 | ]<- 0 |
| PSI2 | [ | 10 | 7 | ]<-0 |
| PSI2 | [ | 10 | 8 | ]<- 0 |
| PSI2 | [ | 10 | 9 | ]<-0 |
| PSI2 | [ | 10 | 10 | ]<- 0 |
| PSI2 | [ | 10 | 11 | ]<- 0 |
| PSI2 | [ | 10 | 12 | ]<- beta[3] |
| PSI2 | [ | 10 | 13 | ]<- 1-beta[3] |
| PSI2 | [ | 10 | 14 | ]<- 0 |
| PSI2 | [ | 10 | 15 | ]<- 0 |
| PSI2 | [ | 10 | 16 | ]<- 0 |
| PSI2 | [ | 11 | 1 | ]<- 0 |
| PSI2 | [ | 11 | 2 | ]<- 0 |
| PSI2 | [ | 11 | 3 | ]<- 0 |
| PSI2 | [ | 11 | 4 | ]<- 0 |
| PSI2 | [ | 11 | 5 | ]<-0 |
| PSI2 | [ | 11 | 6 | ]<-0 |
| PSI2 | [ | 11 | 7 | ]<- 0 |
| PSI2 | [ | 11 | 8 | ]<-0 |
| PSI2 | [ | 11 | 9 | ]<-0 |
| PSI2 | [ | 11 | 10 | ]<- 0 |
| PSI2 | [ | 11 | 11 | ]<- 0 |
| PSI2 | [ | 11 | 12 | ]<- beta[3] |
| PSI2 | [ | 11 | 13 | ]<- 1-beta[3] |
| PSI2 | [ | 11 | 14 | ]<- 0 |
| PSI2 | [ | 11 | 15 | ]<- 0 |
| PSI2 | [ | 11 | 16 | ]<- 0 |
| PSI2 | [ | 12 | 1 | ]<- 0 |
| PSI2 | [ | 12 | 2 | ]<-0 |
| PSI2 | [ | 12 | 3 | ]<- 0 |
| PSI2 | [ | 12 | 4 | ]<-0 |
| PSI2 | [ | 12 | 5 | ]<- 0 |
| PSI2 | [ | 12 | 6 | ]<- 0 |
| PSI2 | [ | 12 | 7 | ]<- 0 |


| PSI2 | [ | 12 | 8 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 12 | 9 | ]<- 0 |
| PSI2 | [ | 12 | 10 | ]<-0 |
| PSI2 | [ | 12 | 11 | ]<-0 |
| PSI2 | [ | 12 | 12 | ]<-0 |
| PSI2 | [ | 12 | 13 | ]<- 0 |
| PSI2 | [ | 12 | 14 | ]<- beta[4] |
| PSI2 | [ | 12 | 15 | ]<- 1-beta[4] |
| PSI2 | [ | 12 | 16 | ]<- 0 |
| PSI2 | [ | 13 | 1 | ]<- 0 |
| PSI2 | [ | 13 | 2 | ]<-0 |
| PSI2 | [ | 13 | 3 | ]<-0 |
| PSI2 | [ | 13 | 4 | ]<-0 |
| PSI2 | [ | 13 | 5 | ]<-0 |
| PSI2 | [ | 13 | 6 | ]<- 0 |
| PSI2 | [ | 13 | 7 | ]<-0 |
| PSI2 | [ | 13 | 8 | ]<-0 |
| PSI2 | [ | 13 | 9 | ]<-0 |
| PSI2 | [ | 13 | 10 | ]<- 0 |
| PSI2 | [ | 13 | 11 | ]<- 0 |
| PSI2 | [ | 13 | 12 | ]<- 0 |
| PSI2 | [ | 13 | 13 | ]<- 0 |
| PSI2 | [ | 13 | 14 | ]<- 0 |
| PSI2 | [ | 13 | 15 | ]<- 0 |
| PSI2 | [ | 13 | 16 | ]<-1 |
| \# PSI3:litter size probabilities |  |  |  |  |
| PSI3 | [ | 1 | 1 | ]<- 0 |
| PSI3 | [ | 1 | 2 | ]<-1 |
| PSI3 | [ | 1 | 3 | ]<- 0 |
| PSI3 | [ | 1 | 4 | ]<-0 |
| PSI3 | [ | 1 | 5 | ]<-0 |
| PSI3 | [ | 1 | 6 | ]<-0 |
| PSI3 | [ | 1 | 7 | ]<-0 |
| PSI3 | [ | 1 | 8 | ]<-0 |
| PSI3 | [ | 1 | 9 | ]<- 0 |
| PSI3 | [ | 1 | 10 | ]<-0 |
| PSI3 | [ | 1 | 11 | ]<- 0 |
| PSI3 | [ | 1 | 12 | ]<- 0 |
| PSI3 | [ | 2 | 1 | ]<- 0 |
| PSI3 | [ | 2 | 2 | ]<-0 |
| PSI3 | [ | 2 | 3 | ]<-1 |
| PSI3 | [ | 2 | 4 | ]<- 0 |
| PSI3 | [ | 2 | 5 | ]<- 0 |
| PSI3 | [ | 2 | 6 | ]<- 0 |
| PSI3 | [ | 2 | 7 | ]<- 0 |
| PSI3 | [ | 2 | 8 | ]<- 0 |
| PSI3 | [ | 2 | 9 | ]<- 0 |
| PSI3 | [ | 2 | 10 | ]<-0 |
| PSI3 | [ | 2 | 11 | ]<-0 |
| PSI3 | [ | 2 | 12 | ]<-0 |


| PSI3 | [ | 7 | 2 | ]<-0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 7 | 3 | ]<-0 |
| PSI3 | [ | 7 | 4 | ]<-0 |
| PSI3 | [ | 7 | 5 | ]<-0 |
| PSI3 | [ | 7 | 6 | ]<-0 |
| PSI3 | [ | 7 | 7 | ]<-0 |
| PSI3 | [ | 7 | 8 | ]<-0 |
| PSI3 | [ | 7 | 9 | ]<-0 |
| PSI3 | [ | 7 | 10 | ]<-1 |
| PSI3 | [ | 7 | 11 | ]<-0 |
| PSI3 | [ | 7 | 12 | ]<-0 |
| PSI3 | [ | 8 | 1 | ]<-0 |
| PSI3 | [ | 8 | 2 | ]<-0 |
| PSI3 | [ | 8 | 3 | ]<-0 |
| PSI3 | [ | 8 | 4 | ]<-0 |
| PSI3 | [ | 8 | 5 | ]<- gamma[1] |
| PSI3 | [ | 8 | 6 | ]<- 1-gamma[1] |
| PSI3 | [ | 8 | 7 | ]<-0 |
| PSI3 | [ | 8 | 8 | ]<-0 |
| PSI3 | [ | 8 | 9 | ]<-0 |
| PSI3 | [ | 8 | 10 | ]<-0 |
| PSI3 | [ | 8 | 11 | ]<-0 |
| PSI3 | [ | 8 | 12 | ]<-0 |
| PSI3 | [ | 9 | 1 | ]<-0 |
| PSI3 | [ | 9 | 2 | ]<-0 |
| PSI3 | [ | 9 | 3 | ]<-0 |
| PSI3 | [ | 9 | 4 | ]<-0 |
| PSI3 | [ | 9 | 5 | ]<-0 |
| PSI3 | [ | 9 | 6 | ]<-0 |
| PSI3 | [ | 9 | 7 | ]<-0 |
| PSI3 | [ | 9 | 8 | ]<-0 |
| PSI3 | [ | 9 | 9 | ]<-0 |
| PSI3 | [ | 9 | 10 | ]<-0 |
| PSI3 | [ | 9 | 11 | ]<-1 |
| PSI3 | [ | 9 | 12 | ]<-0 |
| PSI3 | [ | 10 | 1 | ]<-0 |
| PSI3 | [ | 10 | 2 | ]<-0 |
| PSI3 | [ | 10 | 3 | ]<-0 |
| PSI3 | [ | 10 | 4 | ]<-0 |
| PSI3 | [ | 10 | 5 | ]<- gamma[2] |
| PSI3 | [ | 10 | 6 | ]<- 1-gamma[2] |
| PSI3 | [ | 10 | 7 | ]<-0 |
| PSI3 | [ | 10 | 8 | ]<-0 |
| PSI3 | [ | 10 | 9 | ]<-0 |
| PSI3 | [ | 10 | 10 | ]<-0 |
| PSI3 | [ | 10 | 11 | ]<-0 |
| PSI3 | [ | 10 | 12 | ]<-0 |
| PSI3 | [ | 11 | 1 | ]<-0 |
| PSI3 | [ | 11 | 2 | ]<-0 |


| PSI3 | [ | 11 | , | 3 | ]<- | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 11 | , | 4 | ]<- | 0 |
| PSI3 | [ | 11 | , | 5 | ]<- | 0 |
| PSI3 | [ | 11 | , | 6 | ]<- | 0 |
| PSI3 | [ | 11 | , | 7 | ]<- | 0 |
| PSI3 | [ | 11 | , | 8 | ]<- | 0 |
| PSI3 | [ | 11 | , | 9 | ]<- | 0 |
| PSI3 | [ | 11 | , | 10 | ]<- | 0 |
| PSI3 | [ | 11 | , | 11 | ]<- | 1 |
| PSI3 | [ | 11 | , | 12 | ]<- |  |
| PSI3 | [ | 12 | , | 1 | ]<- | 0 |
| PSI3 | [ | 12 | , | 2 | ]<- | 0 |
| PSI3 | [ | 12 | , | 3 | ]<- | 0 |
| PSI3 | [ | 12 | , | 4 | ]<- | 0 |
| PSI3 | [ | 12 | , | 5 | ]<- | gamma [3] |
| PSI3 | [ | 12 | , | 6 | ]<- | 1-gamma [3] |
| PSI3 | [ | 12 | , | 7 | ]<- | 0 |
| PSI3 | [ | 12 | , | 8 | ]<- | 0 |
| PSI3 | [ | 12 | , | 9 | ]<- | 0 |
| PSI3 | [ | 12 | , | 10 | ]<- | 0 |
| PSI3 | [ | 12 | , | 11 | ]<- | 0 |
| PSI3 | [ | 12 | , | 12 | ]<- |  |
| PSI3 | [ | 13 | , | 1 | ]<- | 0 |
| PSI3 | [ | 13 | , | 2 | ]<- |  |
| PSI3 | [ | 13 | , | 3 | ]<- |  |
| PSI3 | [ | 13 | , | 4 | ]<- |  |
| PSI3 | [ | 13 | , | 5 | ]<- |  |
| PSI3 | [ | 13 | , | 6 | ]<- |  |
| PSI3 | [ | 13 | , | 7 | ]<- |  |
| PSI3 | [ | 13 | , | 8 | ]<- |  |
| PSI3 | [ | 13 | , | 9 | ]<- |  |
| PSI3 | [ | 13 | , | 10 |  |  |
| PSI3 | [ | 13 | , | 11 |  | 1 |
| PSI3 | [ | 13 | , | 12 | ]<- |  |
| PSI3 | [ | 14 | , | 1 | ]<- | 0 |
| PSI3 | [ | 14 | , | 2 | ]<- | 0 |
| PSI3 | [ | 14 | , | 3 | ]<- | 0 |
| PSI3 | [ | 14 | , | 4 | ]<- | 0 |
| PSI3 | [ | 14 | , | 5 | ]<- | gamma [4] |
| PSI3 | [ | 14 | , | 6 | ]<- | 1-gamma [4] |
| PSI3 | [ | 14 | , | 7 | ]<- | 0 |
| PSI3 | [ | 14 | , | 8 | ]<- | 0 |
| PSI3 | [ | 14 | , | 9 | ]<- | 0 |
| PSI3 | [ | 14 | , | 10 | ]<- | 0 |
| PSI3 | [ | 14 | , | 11 | ]<- | 0 |
| PSI3 | [ | 14 | , | 12 | ]<- |  |
| PSI3 | [ | 15 | , | 1 | ]<- |  |
| PSI3 | [ | 15 | , | 2 | ]<- |  |
| PSI3 | [ | 15 | , | 3 | ]<- |  |


| PSI3 | [ | 15 |  | 4 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 15 |  | 5 | ]<- 0 |
| PSI3 | [ | 15 |  | 6 | ]<- 0 |
| PSI3 | [ | 15 |  | 7 | ]<- 0 |
| PSI3 | [ | 15 |  | 8 | ]<- 0 |
| PSI3 | [ | 15 |  | 9 | ]<- 0 |
| PSI3 | [ | 15 |  | 10 | ]<- 0 |
| PSI3 | [ | 15 | , | 11 | ]<- 1 |
| PSI3 | [ | 15 | , | 12 | ]<- 0 |
| PSI3 | [ | 16 | , | 1 | ]<- 0 |
| PSI3 | [ | 16 |  | 2 | ]<- 0 |
| PSI3 | [ | 16 |  | 3 | ]<- 0 |
| PSI3 | [ | 16 |  | 4 | ]<- 0 |
| PSI3 | [ | 16 |  | 5 | ]<- 0 |
| PSI3 | [ | 16 |  | 6 | ]<- 0 |
| PSI3 | [ | 16 |  | 7 | ]<- 0 |
| PSI3 | [ | 16 |  | 8 | ]<- 0 |
| PSI3 | [ | 16 |  | 9 | ]<- 0 |
| PSI3 | [ | 16 |  | 10 | ]<- 0 |
| PSI3 | [ | 16 |  | 11 | ]<- 0 |
| PSI3 | [ | 16 |  | 12 | ]<- 1 |

\# Matrix product for state-to-state transitions S
S[1:12,1:12] <- PHI[1:12,1:12] \%*\% PSI1[1:12,1:13] \%*\% PSI2[1:13,1:16] \%*\% PSI3[1:16,1:12]
\#\# Observation process: Define probabilities of E(t) given $S(t)$.
\#for initial capture, conditional on first capture

| E0 | [ | 1 | , | 1 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| E0 | [ | 1 | , | 2 | ]<-1 |
| E0 | [ | 1 | , | 3 | ]<- 0 |
| E0 | [ | 1 | , | 4 | ]<- 0 |
| E0 | [ | 1 | , | 5 | ]<- 0 |
| E0 | [ | 1 | , | 6 | ]<- 0 |
| E0 | [ | 1 | , | 7 | ]<- 0 |
| E0 | [ | 1 | , | 8 | ]<- 0 |
| E0 | [ | 1 | , | 9 | ]<- 0 |
| E0 | [ | 1 | , | 10 | ]<- 0 |
| E0 | [ | 1 |  | 11 | ]<- 0 |
| E0 | [ | 1 |  | 12 | ]<- 0 |


| EO | $[$ | 2 | , | 1 | $]<-$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| EO | $[$ | 2 | , | 2 | $]<-$ |
| EO | $[$ | 2 | , | 3 | $]<-$ |
| EO | $[$ | 2 | , | 4 | $]<-$ |
| EO | $[$ | 2 | , | 5 | $]<-$ |
| EO | $[$ | 2 | , | 6 | $]<-$ |
| EO | $[$ | 2 | , | 7 | $]<-$ |
| EO | $[$ | 2 | , | 8 | $]<-$ |
| EO | $[$ | 2 | , | 9 | $]<-$ |
| EO | $[$ | 2 | , | 10 | $]<-$ |
| EO |  |  |  |  |  |

```
\begin{tabular}{|c|c|c|c|c|c|}
\hline E0 & [ & 11 & , & 1 & ]<- 0 \\
\hline E0 & [ & 11 & , & 2 & ]<- 0 \\
\hline E0 & [ & 11 & , & 3 & ]<- \\
\hline E0 & [ & 11 & , & 4 & ]<- \\
\hline E0 & [ & 11 & , & 5 & ]<- \\
\hline E0 & [ & 11 & , & 6 & ]<- \\
\hline EO & [ & 11 & , & 7 & ]<- \\
\hline E0 & [ & 11 & , & 8 & ]<- \\
\hline EO & [ & 11 & , & 9 & ]<- \\
\hline EO & [ & 11 & , & 10 & ]<- \\
\hline EO & [ & 11 & & 11 & ]<- \\
\hline EO & [ & 11 & & 12 & ]< \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|}
\hline E0 & [ & 12 & & 1 & ]<- 1 \\
\hline E0 & [ & 12 & & 2 & ]<- 0 \\
\hline E0 & [ & 12 & & 3 & ]<- 0 \\
\hline E0 & [ & 12 & & 4 & ]<- 0 \\
\hline E0 & [ & 12 & & 5 & ]<- 0 \\
\hline E0 & [ & 12 & & 6 & ]<- 0 \\
\hline E0 & [ & 12 & & 7 & ]<- 0 \\
\hline E0 & [ & 12 & , & 8 & ]<- 0 \\
\hline E0 & [ & 12 & & 9 & ]<- 0 \\
\hline E0 & [ & 12 & & 10 & ]<- 0 \\
\hline E0 & [ & 12 & & 11 & ]<- 0 \\
\hline E0 & [ & 12 & & 12 & ]<- 0 \\
\hline
\end{tabular}
# departure probability of a2 offspring
for(i in 1:N){
        for(t in 1:(Years-1)){
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline E1 & [ & 1 & , & 1 & ,i,t]< & \\
\hline E1 & [ & 1 & , & 2 & ,i,t]< & \\
\hline E1 & [ & 1 & , & 3 & , i, t] & \\
\hline E1 & [ & 1 & , & 4 & ,i,t]< & 0 \\
\hline E1 & [ & 1 & , & 5 & ,i,t]< & 0 \\
\hline E1 & [ & 1 & , & 6 & ,i,t]< & \\
\hline E1 & [ & 1 & , & 7 & ,i,t]< & \\
\hline E1 & [ & 1 & , & 8 & ,i,t]< & \\
\hline E1 & [ & 1 & , & 9 & ,i,t]< & 0 \\
\hline E1 & [ & 1 & , & & i, t]<- & 0 \\
\hline E1 & [ & 1 & & & i, t]<- & 0 \\
\hline E1 & [ & 1 & & & i,t]<- & 0 \\
\hline
\end{tabular}
E1 [ 2 , 1 ,i,t]<- 0
        E1 [ 2 , 2 ,i,t]<- 1
        E1 [ 2 , 3 ,i,t]<- 0
        E1 [ 2 , 4 ,i,t]<- 0
        E1 [ 2 , 5 ,i,t]<- 0
        E1 [ 2 , 6 ,i,t]<- 0
        E1 [ 2 , 7 ,i,t]<- 0
        E1 [ 2 , 8 ,i,t]<- 0
        E1 [ 2 , 9 ,i,t]<- 0
        E1 [ 2 [ l 10,i,t]<- 0
```

| E1 | [ | 2 | , | 12,i,t]<- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 3 | , | 1 | ,i,t] |  |
| E1 | [ | 3 | , | 2 | ,i,t] |  |
| E1 | [ | 3 |  | 3 | ,i,t] |  |
| E1 | [ | 3 | , | 4 | , i, t] |  |
| E1 | [ | 3 |  | 5 | , i, t] |  |
| E1 | [ | 3 |  | 6 | , i, t] |  |
| E1 | [ | 3 |  | 7 | ,i,t] |  |
| E1 | [ | 3 |  | 8 | , i, t] |  |
| E1 | [ | 3 |  | 9 | , i, t] |  |
| E1 | [ | 3 |  |  | , t] <- | 0 |
| E1 | [ | 3 |  |  | , t]<- | 0 |
| E1 | [ | 3 |  |  | , t] <- | 0 |


| E1 | [ | 4 | , | 1 | ,i,t] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 4 | , | 2 | ,i,t] |  |
| E1 | [ | 4 | , | 3 | ,i,t]< | 0 |
| E1 | [ | 4 |  | 4 | ,i,t]< | 1 |
| E1 | [ | 4 |  | 5 | ,i,t]< | 0 |
| E1 | [ | 4 |  | 6 | ,i,t]< | 0 |
| E1 | [ | 4 | , | 7 | ,i,t]< | 0 |
| E1 | [ | 4 |  | 8 | ,i,t]< | 0 |
| E1 | [ | 4 |  | 9 | ,i,t]< | 0 |
| E1 | [ | 4 |  |  | , t]<- | 0 |
| E1 | [ | 4 |  |  | , t]<- | 0 |
| E1 | [ | 4 |  |  | , t]<- | 0 |


| E1 | [ | 5 | , | 1,i,t]<- | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 5 | , | 2,i,t]<- | 0 |
| E1 | [ | 5 | , | 3,i,t]<- | 0 |
| E1 | [ | 5 | , | 4,i,t]<- | 0 |
| E1 | [ | 5 | , | 5,i,t]<- | 1 |
| E1 | [ | 5 | , | 6,i,t]<- | 0 |
| E1 | [ | 5 | , | 7,i,t]<- | 0 |
| E1 | [ | 5 | , | 8,i,t]<- | 0 |
| E1 | [ | 5 | , | 9,i,t]<- | 0 |
| E1 | [ | 5 | , | 10, i, t]<- | 0 |
| E1 | [ | 5 |  | 11,i,t]<- | 0 |
| E1 | [ | 5 |  | 12,i,t]<- | 0 |


| E1 | [ | 6 | , | 1 | ,i,t]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 6 | , | 2 | ,i,t]<- |  |
| E1 | [ | 6 |  | 3 | ,i,t]<- |  |
| E1 | [ | 6 |  | 4 | , i, t]<- |  |
| E1 | [ | 6 |  | 5 | , i, t]<- |  |
| E1 | [ | 6 | , | 6 | , i, t]<- |  |
| E1 | [ | 6 |  | 7 | , i, t]<- |  |
| E1 | [ | 6 |  | 8 | , i, t]<- |  |
| E1 | [ | 6 |  | 9 | ,i,t]<- | 0 |
| E1 | [ | 6 |  |  | i, t]<- | 0 |
| E1 | [ | 6 |  |  | i, t]<- | 0 |
| E1 | [ | 6 |  |  | i, t]<- | 0 |

```
E1 
\begin{tabular}{lllllll} 
E1 & {\([\)} & 8 &, & 1 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 2 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 3 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 4 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 5 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 6 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 7 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & 8 & \(, \mathrm{i}, \mathrm{t}]<-\) & 1 \\
E1 & {\([\)} & 8 &, & 9 & \(, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & \(10, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & \(11, \mathrm{i}, \mathrm{t}]<-\) & 0 \\
E1 & {\([\)} & 8 &, & \(12, \mathrm{i}, \mathrm{t}]<-\) & 0
\end{tabular}
\begin{tabular}{llllll} 
E1 & {\([\)} & 9 &, & 1 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 2 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 3 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 4 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 5 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 6 & \(, i, t]<-\) \\
E1 & {\([9\)} &, & 7 & \(, i, t]<-\) \\
E1 & {\([\)} & 9 &, & 8 & \(, i, t]<-\)
\end{tabular}
E1 [ 9 , 9 ,i,t]<- 1-alpha[i,t+1]
E1 [ 9 , 10,i,t]<- 0
E1 [ 9 , 11,i,t]<- alpha[i,t+1]
    , 12,i,t]<- 0
\begin{tabular}{|c|c|c|c|c|c|}
\hline E1 & [ & 10 & , & 1,i,t]<- & 0 \\
\hline E1 & [ & 10 & , & 2,i,t]<- & 0 \\
\hline E1 & [ & 10 & , & 3,i,t]<- & 0 \\
\hline E1 & [ & 10 & , & 4,i,t]<- & 0 \\
\hline E1 & [ & 10 & , & 5,i,t]<- & 0 \\
\hline E1 & [ & 10 & , & 6,i,t]<- & 0 \\
\hline E1 & [ & 10 & & 7,i,t]<- & 0 \\
\hline E1 & & 10 & & 8,i,t]<- & 0 \\
\hline
\end{tabular}
E1 [ 10 , 9,i,t]<- 2*(1-alpha[i,t+1])*alpha[i,t+1]
E1 [ 10 , 10,i,t]<- 1 - (2*(1-alpha[i,t+1])*alpha[i,t+1]) - (alpha[i,t+1]) ^2
E1 [ 10 , 11,i,t]<- (alpha[i,t+1])^2
E1 [ 10 , 12,i,t]<- 0
E1 [ 11 , 1 ,i,t]<- 0
```

| E1 | [ | 11 | , | 2 | ,i,t]< |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 11 | , | 3 | ,i,t]< |  |
| E1 | [ | 11 | , | 4 | ,i,t]< |  |
| E1 | [ | 11 | , | 5 | ,i,t]< |  |
| E1 | [ | 11 | , | 6 | ,i,t]< |  |
| E1 | [ | 11 | , | 7 | ,i,t]< |  |
| E1 | [ | 11 | , | 8 | ,i,t]< | 0 |
| E1 | [ | 11 | , | 9 | ,i,t]< | 0 |
| E1 | [ | 11 | , |  | i, t]<- | 0 |
| E1 | [ | 11 | , | 11 | , t]<- | 1 |
| E1 | [ | 11 | , | 12 | , t]<- | 0 |
| E1 | [ | 12 | , | 1 | ,i,t]< | 0 |
| E1 | [ | 12 | , | 2 | ,i,t]< |  |
| E1 | [ | 12 | , | 3 | ,i,t]< |  |
| E1 | [ | 12 | , | 4 | ,i,t]< |  |
| E1 | [ | 12 | , | 5 | ,i,t]< |  |
| E1 | [ | 12 | , | 6 | ,i,t]< |  |
| E1 | [ | 12 | , | 7 | ,i,t]< |  |
| E1 | [ | 12 |  | 8 | ,i,t]< |  |
| E1 | [ | 12 |  | 9 | ,i,t]< |  |
| E1 | [ | 12 |  |  | i, t]<- | 0 |
| E1 | [ | 12 |  |  | , t]<- | 0 |
| E1 | [ | 12 |  |  | , t]<- | 1 |

\# for recapture probability


| E2 | [ | 2 |  |  |  | , i, t] |  | -p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E2 | [ | 2 |  | 2 |  | , i, t] |  |  |
| E2 | [ | 2 |  | 3 |  | ,i,t] |  |  |
| E2 | [ | 2 | , | 4 |  | , i, t] |  |  |
| E2 | [ | 2 |  | 5 |  | ,i,t] |  |  |
| E2 | [ | 2 | , | 6 |  | , i, t] |  |  |
| E2 | [ | 2 | , | 7 |  | , i, t] |  |  |
| E2 | [ | 2 | , | 8 |  | ,i,t] |  |  |
| E2 | [ | 2 | , | 9 |  | , i, t] |  |  |
| E2 | [ | 2 | , |  |  | i, t]<- |  |  |
| E2 | [ | 2 | , |  |  | i, t]<- |  |  |
| E2 | [ | 2 | , |  |  | i, t]<- |  |  |
| E2 | [ | 3 |  |  |  | , i, t] |  | -p |



1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19

$$
\begin{aligned}
& \begin{array}{llllll}
\text { E2 } & {[7} & 7 & 3 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 4 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 5 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 6 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 7 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 8 & , \mathrm{i}, \mathrm{t}]<- & \mathrm{p} \\
\text { E2 } & {[77} & , & 9 & , \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 10, \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 11, \mathrm{i}, \mathrm{t}]<- & 0 \\
\text { E2 } & {[77} & , & 12, \mathrm{i}, \mathrm{t}]<- & 0
\end{array} \\
& \text { E2 }[8 \quad, \quad 1 \quad, i, t]<-1-p \\
& \text { E2 }[8,2, i, t]<-0 \\
& \text { E2 [ } 8,3, i, t]<-0 \\
& \text { E2 [ } 8 \quad, 4 \mathrm{i}, \mathrm{t}]<-0 \\
& \text { E2 } \quad[\quad 8 \quad, \quad 5 \quad, i, t]<-0
\end{aligned}
$$

$$
\begin{aligned}
& \text {, } \begin{array}{ll}
8 & , i, t]<-0 \\
, & , i, t]<-p
\end{array} \\
& \text {, } 10, i, t]<-\quad 0 \\
& \text {, } 11, \mathrm{i}, \mathrm{t}]<-\quad 0 \\
& \text {, } 1 \text {,i,t]<- 1-p } \\
& \text {, } 2 \text {,i,t]<- } 0 \\
& \text {, } 3 \text {,i,t]<- } 0 \\
& \text {, } 4, i, t]<-0 \\
& \text {, } 5 \text {, } 6, t]<-0 \\
& \text {, } 7 \begin{array}{ll}
\text {, } & , i, t]<-0 \\
8 & i, t]<-0
\end{array} \\
& \text {, } 9 \text {,i,t]<- } 0 \\
& \text {, } 10, i, t]<-\quad \text { p } \\
& \text {, } 12, i, t]<-\quad 0 \\
& \text {, 1,i,t]<- } 1-\mathrm{p} \\
& \text {, 2,i,t]<- } 0 \\
& \text {, 3,i,t]<- } 0 \\
& \text {, 4,i,t]<- } 0 \\
& \text { 5,i,t]<- } \quad 0 \\
& \text {, 6,i,t]<- } 0 \\
& 7, i, t]<-\quad 0 \\
& \text {, 8,i,t]<- } 0 \\
& \text {, } 9, i, t]<-\quad 0 \\
& \text {, 10,i,t]<- } 0 \\
& \begin{array}{ll}
11, i, t]<- & p \\
12, i, t]<- & 0
\end{array} \\
& \text {, } 1 \text {,i,t]<- } 1 \text { - p }
\end{aligned}
$$

```
        E2 [ 11 , 4 ,i,t]<- 0
        E2 [ 11 , 5 ,i,t]<- 0
        E2 [ 11 , 6 ,i,t]<- 0
        E2 [ 11 , 7 ,i,t]<- 0
        E2 [ 11 , 8 ,i,t]<- 0
        E2 [ 11 , 9 ,i,t]<- 0
        E2 [ 11 , 10,i,t]<- 0
        E2 [ 11 , 11,i,t]<- 0
        E2 [ 12 , 1 ,i,t]<- 1
        E2 [ 12, 2 ,i,t]<- 0
        E2 [ 12, 3 ,i,t]<- 0
        E2 [ 12 , 4 ,i,t]<- 0
        E2 [ 12 , 5 ,i,t]<- 0
        E2 [ 12 , 6 ,i,t]<- 0
        E2 [ 12 , 7 ,i,t]<- 0
        E2 [ 12 , 8 ,i,t]<- 0
        E2 [ 12 , 9 ,i,t]<- 0
        E2 [ 12 , 10,i,t]<- 0
        E2 [ 12 , 11,i,t]<- 0
        E2 [ 12 , 12,i,t]<- 0
        # Matrix product for offspring independence and recapture
        E[1:12,1:12,i,t] <- E1[1:12,1:12,i,t] %*% E2[1:12,1:12,i,t]
    }
}
## LIKELIHOOD
for (i in 1:N) # for each individual
{
    # The estimated probabilities of initial states SO are the proportions in each state
    #at first capture occasion
    alive[i,First[i]] ~ dcat(S0[1:12])
    mydata[i,First[i]] ~ dcat(EO[alive[i,First[i]],1:12])
    for (j in (First[i]+1):Years)
    {
        ## STATE EQUATIONS ##
        # draw S(t) given S(t-1)
        alive[i,j] ~ dcat(S[alive[i,j-1],1:12])
        ## OBSERVATION EQUATIONS ##
        # draw events E(t) given states S(t)
        mydata[i,j] ~ dcat(E[alive[i,j],1:12,i,j-1])
    }
}
```

```
    ## PRIORS
    # capture probability
    p ~ dunif(0,1)
    # juveniles, subadults and adult survival
    phi ~ dunif(0,1)
    # initial states
    for (i in 1:10){ log(prop[i]) <- theta[i]
    theta[i] ~ dnorm(0,1)}
    # offspring survival
    # litter survival n=2 offspring
    102 <- 1 -(1- s[2]~2 -2*s[2]*(1-s[2]))
    l12 <- 1- (1- s[4]~2 -2*s[4]*(1-s[4]))
    # indiviual offspring survival
    for(i in 1:2){s[i]~ dunif(0,1)}
    # Set constraints
    for(u in 1:2){ X[u] ~ dunif(0,1)} # with X ~ U[0,1] then (a + ( b - a ) * X)
    #so that s[1] < s[3] <phi[1] for litter of 1
    s[3] <- s[1] + (phi[1] - s[1]) * X[1]
    # and s[2] < s[4] < phi[1] for litters of 2
    s[4] <- s[2] + (phi[1] - s[2]) * X[2]
    # Breeding probability
    kappa ~ dunif(0,1)
    for(i in 1:4){beta[i] ~ dunif(0,1)}
    # Litter size probability
    for(i in 1:4){gamma[i]~ dunif(0,1)}
} # end model
    ",fill=TRUE)
sink()
#######
#######
```

We used non-informative priors on the model parameters, with uniform distribution between 0 and 1 for probabilities, and normal distribution with mean 0 and variance of 1 for regression coefficients. To help estimation of the parameters in the model, we introduced the constraint that survival of cubs (age $<1$ ) was lower than that of yearling survival (aged 1). We used one chain with 10000 iterations and 4000 burnin.

Load the data (family unit CR histories, initial state matrix, date of captures) and fit the model :

```
RES <- list()
for(r in 1:100){
nameCH <- paste(repname,"/simCH",r,"_p",p,"_T",n.occasions,".txt",sep="")
# load capture histories
data <- read.table(paste(nameCH),sep=" ",header=FALSE)
# initial values for state matrix
nameINIT <- paste(repname,"/siminit",r,"_p",p,"_T",n.occasions,".txt",sep="")
initmat <- read.table(paste(nameINIT),sep="")
```

```
# date of capture
nameDAY <- paste(repname,"/simdaycapt",r,"_p",p,"_T",n.occasions,".txt",sep="")
daycapt <- read.table(paste(nameDAY),sep="")
data <- data.matrix(data)
alive1 <- data.matrix(initmat)
head(data)
N <- dim(data)[1]
Years <- dim(data) [2]
# Compute vector with occasion of first capture
get.first <- function(x) min(which(x!=0))
First <- apply(data, 1, get.first)
# Predict departure probability function of date of capture
alpha = matrix(0,nrow=N,ncol=Years)
    for(i in 1:N){
        for(j in (First[i]+1):Years){
        alpha[i,j] <- predict(modeld,newdata=list(doy=daycapt[i,j]),type="response")
    }
}
# Bundle data for jags
mydatax <- list(N=N,First=First,Years=Years,mydata=data.matrix(data+1)
                        ,alpha=data.matrix(alpha))
# Initial values
init1 <- list(theta=rnorm(10, mean = 0, sd = 1), alive=alive1) #
inits <- list(init1)
# Parameters monitored
params <- c("phi","kappa","s","l02","l12","beta","gamma","p","S0")
# Call JAGS from R to fit the model
out <- jags(data=mydatax,inits=inits, parameters.to.save=params,
    model.file = 'Multieventmodel_Fit_simul.txt',n.chains=1,
    n.iter=10000,n.burnin=4000)
RES[[r]] <- out # store results
print(paste(r))
}
save(RES,file=paste('RES',n.occasions,'p',p,'.RData',sep="")) # save results
```


## Post process simulation results

Load and plot the results:

```
# load results of the simulations
capture <- c(0.25,0.25,0.5,0.5)
filenames <- c("S1RESp0.25alpha05.RData","S2RESp0.25alphaDate.RData",
    "S3RESp0.5alpha05.RData", "S4RESp0.5alphaDate.RData")
EST <- CI1 <- CI2 <- simres <- biasall <- rMSEall <- list()
```

```
for(S in 1:4){
    p = capture[S]
load(paste(filenames[S]))
# parameters used to simulate the data in same order
# phi, kappa, s1,s2,s3,s4,beta1,beta2,beta3,beta4,gamma1,gamma2,gamma3,gamma4,p
theta <- c(0.9,0,0.6,0.55,0.8,0.75,0.5,0.7,0.9,0.8,0.4,0.5,0.6,0.7,as.numeric(paste(p)))
nparam <- length(theta)
nrepet <- length(RES)
# Calculate summary of posterior distribution estimated for all parameters
#(mean, and 95% credible interval) and calculate bias and root mean-square-errors :
    est <- ci1 <- ci2 <- BIAS <- pBIAS <- rMSE <- matrix(NA,nrow=length(RES),ncol=nparam)
    for(i in 1:nrepet){
        #get estimates
        est[i,] <- unlist(RES[[i]]$mean[c(1,2,3,6,7,8)])
        ci1[i,] <- unlist(RES[[i]]$q2.5[c(1,2,3,6,7,8)])
        ci2[i,] <- unlist(RES[[i]]$q97.5[c(1,2,3,6,7,8)])
        # absolute bias, and root mean square error
        BIAS[i,] <- (est[i,] - theta)
        rMSE[i,] <- sqrt( (est[i,] - theta)~2 )
    }#nrepet
# Plot the results
# pdf(width=9,height=6,pointsize=4,file="test.pdf",paper="a4r")
        par(mfrow=c(3,5))
        xlabs <- c(expression(phi), expression(kappa), expression(S[1]), expression(S[2]),
                                    expression(S[3]), expression(S[4]),
                                    expression(beta[1]), expression(beta[2]),
                    expression(beta[3]), expression(beta[4]),
                    expression(gamma[1]), expression(gamma[2]),
                    expression(gamma[3]), expression(gamma[4]),
                    expression(p))
        for(j in 1:nparam){
            plot(est[,j], 1:nrepet, ylab='',xlim=c(0,1),las=TRUE,cex=1,type="n",
                    main=xlabs[j],xlab=paste("bias = ",round(mean(BIAS[,j]),3),
                                    "; rmse =",round(mean(rMSE[,j]),2), sep=""))
            segments(ci1[,j], 1:100,ci2[,j], 1:nrepet,col="grey70",lwd=0.5)
        points(est[,j], 1:nrepet,col="black",cex=0.4,pch=16,)
        abline(v=theta[j], lty=2, col='red')
        }
# dev.off()
    #store results
    EST[[S]] <- est
    CI1[[S]] <- ci1
    CI2[[S]] <- ci2
    simres[[S]] <- RES
    biasall[[S]] <- BIAS
    rMSEall[[S]] <- rMSE
```



Figure S3. Performance of the model on simulated data with low detection with constant departure (scenario S1). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X-axis for each parameter.


Figure S4. Performance of the model on simulated data with low detection with departure varying with date of capture (scenario S2). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X-axis for each parameter.


Figure S5. Performance of the model on simulated data with high detection with constant departure (scenario S3). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X-axis for each parameter.


Figure S6. Performance of the model on simulated data with high detection with departure varying with date of capture (scenario S4). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X-axis for each parameter.
Make tables with values of bias and rsme for each parameter for all scenarios:

```
# average bias
```

mean(c(biasall[[1]], biasall[[2]], biasall[[3]], biasall[[4]]))
\#\# [1] -0.002881172
\# average rmse
mean(c(rMSEall[[1]], rMSEall[[2]], rMSEall[[3]],rMSEall[[4]]))
\#\# [1] 0.03638131
tabB <- rbind ( round(apply(biasall[[1]],2,mean),2), round(apply(biasall[[2]],2,mean),2),
round(apply(biasall[[3]],2,mean),2), round(apply(biasall[[4]],2,mean),2) )
tabR <- rbind ( round(apply(rMSEall[[1] ],2,mean),2), round(apply(rMSEall[[2]],2,mean), 2),
round (apply (rMSEall[[3]],2,mean),2), round(apply(rMSEall[[4]],2,mean),2) )
parnames <- c(expression(phi), expression(kappa), expression(S[1]), expression(S[2]),
expression(S[3]), expression(S[4]),
expression(beta[1]), expression(beta[2]), expression(beta[3]),
expression(beta[4]), expression(gamma[1]), expression(gamma[2]), expression(gamma [3]),
expression(gamma[4]), expression(p))
colnames (tabB) <- colnames (tabR) <- parnames
rownames (tabB) <- rownames (tabR) <- c("S1","S2","S3","S4")
tabB
\#\# phi kappa S[1] S[2] S[3] S[4] beta[1] beta[2] beta[3] beta[4] gamma[1]

$\begin{array}{llllllllll}\text { \#\# S2 } & 0 & 0.02 & 0.01 & 0 & -0.03 & -0.02 & 0.01 & -0.04 & 0.00\end{array} 0.00 \quad 0.00$

```
\begin{tabular}{lrrrrrrrrrr} 
\#\# S3 & 0 & 0.01 & 0.00 & 0 & -0.01 & 0.00 & 0.00 & -0.03 & 0.00 & 0.00 \\
\#\# S4 & 0 & 0.01 & 0.00 & 0 & -0.02 & 0.00 & 0.00 & -0.03 & 0.00 & -0.01
\end{tabular}
## gamma[2] gamma[3] gamma[4] p
## S1 -0.01 -0.01 -0.01 0
## S2 0.00 0.00 0.00 0
## S3 -0.01 0.00 0.00 0
## S4 0.0.01 0.00 0.00 0
tabR
## phi kappa S[1] S[2] S[3] S[4] beta[1] beta[2] beta[3] beta[4] gamma[1]
## S1 0.01 0.02 0.04 0.03 0.04 0.04 0.0.05 0.0.09 0.0.02 
## S2 0.01 0.02 0.03 0.03 0.04 0.04 0.0.04 0.0.09 0.0.02 0.0.03 0.03 0.07
## S3 0.00 0.01 0.02 0.02 0.03 0.04 0.0.03 0.0.08
## S4 0.00 0.01 0.03 0.02 0.04 0.05 0.03 0.0.08 0.0.01 0.0.02 0.05
## gamma[2] gamma[3] gamma[4] p
## S1 0.09 0.04 0.04 0.01
## S2 0.11 0.04 0.04 0.01
## S3 0.07 0.02 0.02 0.01
## S4 0.06 0.03 0.03 0.01
#write.csv(tabB,file = "RES_biasperparam.csv")
#write.csv(tabR,file = "RES_rmseperparam.csv")
```


## Bibliogrpahy

Kéry, M., \& Schaub, M. (2011). Bayesian population analysis using WinBUGS: a hierarchical perspective. Academic Press.

# Guidance to fit the model to the polar bear data, R code, and additional results. 

Sarah Cubaynes

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We fitted our model to the Polar bear data in a Bayesian framework using Markov Chain Monte Carlo (MCMC) simulation implemented in program JAGS (Hornik et al. 2003) called from R using package jagsUI (Kellner 2015). We ran two MCMC in parallel with different initial values, we used 20.000 iterations with an initial burn-in of 9.000 iterations, thinning every 5 iterations, to reach convergence to a stationary distribution, assessed by visual inspection of trace plots for each model parameter to ensure adequate mixing and by using the Gelman and Rubin diagnostic (R-hat $<1.02$ ). We used non-informative priors on the model parameters, with uniform distribution between 0 and 1 for probabilities, and normal distribution with mean 0 and variance of 1 for regression coefficients. To help estimation of the parameters in the model, we introduced the constraint that survival of cubs was lower than that of yearling survival (Amstrup and Durner, 1995). The constraint was enough to reach convergence with satisfactory posterior distribution for each of the estimated parameters (see Figure below).

Below we provide the code to prepare the data, run the model and analyse the results. All files associated with Appendix 2, including the polar bear data files, are available on GitHub here.

## Prepare data and run jags model

Load data and useful packages :

```
load(file = "CRlocalbears_revision2MEE.Rdata") # family units CR histories
data <- data.matrix(CRlb)
load(file = "daylocalbears_revision2MEE.Rdata") # capture date in day of the yaer
daycapt <- daylb
load(file="initstatelocalbears_revision2MEE.Rdata")#matrix of initial states
alive1 <- data.matrix(initmatlb)
load(file = "dataweaning_revision2MEE.Rdata") # all two-year old bear captures
library(jagsUI) # to run jags model
## Loading required package: lattice
##
## Attaching package: 'jagsUI'
## The following object is masked from 'package:utils':
##
## View
```

```
library(jtools) # to make predict plot from glm
```

Define useful quantities:

```
N <- dim(data)[1] # number of family units
Years <- dim(data)[2] #number of sampling occasions
# Compute vector with occasion of first capture
get.first <- function(x) min(which(x!=0))
First <- apply(data, 1, get.first)
```

We use the ratio of two-year old bears captured alone versus still together with their mother (include all bears, not only resident females) to estimate the shape of the relationship between offspring departure probability and date within the field season:

```
nty <- dim(dataweaning) [[1]] # number of two-year old bears captured
status <- dataweaning$status #status of two-year old bears at the time of capture :
#1 alone (already departed from family unit),
#O still together with mother (not yet departed from family unit)
doy <- dataweaning$daysinseason # date of capture
# glm of departure probability as a function of date of capture
modeld<-glm(status~doy,family="binomial")
summary(modeld)
##
## Call:
## glm(formula = status ~ doy, family = "binomial")
##
## Deviance Residuals:
## rrrrer
##
## Coefficients:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.56486 1.75383 -2.033 0.0421 *
## doy 0.03803 0.01646 2.310 0.0209 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 154.11 on 119 degrees of freedom
## Residual deviance: 137.99 on 118 degrees of freedom
## AIC: 141.99
##
## Number of Fisher Scoring iterations: 6
```

Plot predicted departure probability of two-year old bears as a function of date in day of the year (doy):

```
effect_plot(modeld, pred = doy, pred.values=80:130,interval = TRUE,
    plot.points = FALSE,y.label = "departure probability")
```



Departure probability increased throughout the field season. It was about $40 \%$ at the end of March and reached $80 \%$ at mid-May.

Predict departure probability from date of capture for resident family units (departure probability will be used in matrix E2 of the observation process to relate state to events for family units in states AS1 or AS2 ):

```
# Predict departure probability function of date of capture
daycapt <- daylb # dates of capture
# if not captured, replace with 80 (in date of capture) to avoid NAs
daycapt <- replace(daycapt,is.na(daycapt),80)
# create empty object to store predicted departure probability
alpha = matrix(0,nrow=N,ncol=Years)
# predict departure probability based on date of capture using modeld
for(i in 1:N){
    for(j in (First[i]):Years){
        alpha[i,j] <- predict(modeld,newdata=list(doy=daycapt[i,j]),type="response")
    }
}
```

Create a list containing the data to run the jags model:

```
# Bundle data for jags
mydatax <- list(N=N,First=First,Years=Years,mydata=data.matrix(data+1),alpha=data.matrix(alpha))
```

Generate initial values for each of the two chains:

```
set.seed(42)
# Initial values
```

```
init1 <- list(theta=rnorm(10, mean = 0, sd = 1),alive=alive1)
init2 <- list(theta=rnorm(10, mean = 0, sd = 1),alive=alive1)
inits <- list(init1,init2)
```

Create a list with names of the parameters to monitor:

```
# Parameters monitored
params <- c("phi","s","l02","l12","kappa","beta","gamma","p","prop")
```

Load the script of the jags model :

```
# JAGS MODEL
sink("Multieventmodel_FitresidentBeardata.txt")
cat("
model {
    # Probabilities of events given states and states given states
    # vector of initial states
    S0[1] <- prop[1] / (1 + sum(prop[1:10])) # prob. of being in initial state J2
    SO[2] <- prop[2] / (1 + sum(prop[1:10])) # prob. of being in initial state J3
    SO[3] <- prop[3] / (1 + sum(prop[1:10])) # prob. of being in initial state SA4
    SO[4] <- prop[4] / (1 + sum(prop[1:10])) # prob. of being in initial state SA5
    SO[5] <- prop[5] / (1 + sum(prop[1:10])) # prob. of being in initial state A01
    S0[6] <- prop[6] / (1 + sum(prop[1:10])) # prob. of being in initial state A02
    S0[7] <- prop[7] / (1 + sum(prop[1:10])) # prob. of being in initial state A11
    S0[8] <- prop[8] / (1 + sum(prop[1:10])) # prob. of being in initial state A12
    S0[9] <- prop[9] / (1 + sum(prop[1:10])) # prob. of being in initial state AS1
    S0[10] <- prop[10] / (1 + sum(prop[1:10])) # prob. of being in initial state AS2
    SO[11] <- 1 / (1 + sum(prop[1:10])) # prob. of being in initial state A-
    SO[12] <- O # prob. of being in initial state dead
    # State process: define probabilities of S(t+1) given S(t)
    # define PHI matrix gathering survival of independent juveniles, subadults and adults
    PHI [ 1 , 1 ]<- phi[1]
    PHI [ 1 , 2 ]<- 0
    PHI [ 1 , 3 ]<- 0
    PHI [ 1 , 4 ]<- 0
    PHI [ 1 , 5 ]<- 0
    PHI [ 1 , 6 ]<- 0
    PHI [ 1 , 7 ]<- 0
    PHI [ 1 , 8 ]<- 0
    PHI [ 1 , 9 ]<- 0
    PHI [ 1 , 10 ]<- 0
    PHI [ 1 , 11 ]<- 0
    PHI [ 1 , 12 ]<- 1-phi[1]
    PHI [ 2 , 1 ]<- 0
    PHI [ 2 , 2 ]<- phi[1]
    PHI [ 2 , 3 ]<- 0
    PHI [ 2 , 4 ]<- 0
    PHI [ 2 , 5 ]<- 0
    PHI [ 2 , 6 ]<- 0
    PHI [ 2 , 7 ]<- 0
    PHI [ 2 , 8 ]<- 0
```

| PHI | $[$ | 2 | , | 9 | $]<-$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 2 | , | 10 | $]<-$ |
| PHI | $[$ | 2 | , | 11 | $]<-$ |
| PHI | $[$ | 2 | , | 12 | $]<-$ |
| 1-phi [1] |  |  |  |  |  |



| PHI | $[$ | 4 | , | 1 | $]<-0$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 4 | , | 2 | $]<-$ |
| PHI | $[$ | 4 | , | 3 | $]<-0$ |
| PHI | $[$ | 4 | , | 4 | $]<-$ phi $[1]$ |
| PHI | $[$ | 4 | , | 5 | $]<-0$ |
| PHI | $[$ | 4 | , | 6 | $]<-0$ |
| PHI | $[$ | 4 | , | 7 | $]<-0$ |
| PHI | $[$ | 4 | , | 8 | $]<-0$ |
| PHI | $[$ | 4 | , | 9 | $]<-0$ |
| PHI | $[$ | 4 | , | 10 | $]<-0$ |
| PHI | $[$ | 4 | , | 11 | $]<-0$ |
| PHI | $[$ | 4 | , | 12 | $]<-1-\operatorname{phi}[1]$ |


| PHI | $[$ | 5 | , | 1 | $]<-$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 5 | , | 2 | $]<-0$ |
| PHI | $[$ | 5 | , | 3 | $]<-0$ |
| PHI | $[$ | 5 | , | 4 | $]<-0$ |
| PHI | $[$ | 5 | , | 5 | $]<-$ phi $[1]$ |
| PHI | $[$ | 5 | , | 6 | $]<-0$ |
| PHI | $[$ | 5 | , | 7 | $]<-0$ |
| PHI | $[$ | 5 | , | 8 | $]<-0$ |
| PHI | $[$ | 5 | , | 9 | $]<-0$ |
| PHI | $[$ | 5 | , | 10 | $]<-0$ |
| PHI | $[$ | 5 | , | 11 | $]<-0$ |
| PHI | $[$ | 5 | , | 12 | $]<-1-\operatorname{phi[1]}$ |


| PHI | $[$ | 6 | , | 1 | $]<-$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 6 | , | 2 | $]<-$ |
| PHI | $[$ | 6 | , | 3 | $]<-$ |
| PHI | $[$ | 6 | , | 4 | $]<-$ |
| PHI | $[$ | 6 | , | 5 | $]<-$ |
| PHI | $[$ | 6 | , | 6 | $]<-$ phi $[1]$ |
| PHI | $[$ | 6 | , | 7 | $]<-0$ |
| PHI | $[$ | 6 | , | 8 | $]<-$ |
| PHI | $[$ | 6 | , | 9 | $]<-$ |


| PHI | $[$ | 6 | , | 10 | $]<-$ | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PHI | $[$ | 6 | , | 11 | $]<-$ | 0 |
| PHI | $[$ | 6 | , | 12 | $]<-$ | $1-\operatorname{phi}[1]$ |


| PHI | [ | 7 | , | 1 | ]<- | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 7 | , | 2 | ]<- | 0 |
| PHI | [ | 7 |  | 3 | ]<- | 0 |
| PHI | [ | 7 | , | 4 | ]<- | 0 |
| PHI | [ | 7 | , | 5 | ]<- | 0 |
| PHI | [ | 7 | , | 6 | ]<- | 0 |
| PHI | [ | 7 | , | 7 | ]<- | phi [1] |
| PHI | [ | 7 | , | 8 | ]<- | 0 |
| PHI | [ | 7 | , | 9 | ]<- | 0 |
| PHI | [ | 7 | , | 10 | ]<- | 0 |
| PHI | [ | 7 |  | 11 | ]<- | 0 |
| PHI | [ | 7 |  | 12 | ]<- | 1-phi [1] |


| PHI | [ | 8 | , | 1 | ]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 8 | , | 2 | ]<- | 0 |
| PHI | [ | 8 | , | 3 | ]<- | 0 |
| PHI | [ | 8 | , | 4 | ]<- | 0 |
| PHI | [ | 8 | , | 5 | ]<- | 0 |
| PHI | [ | 8 | , | 6 | ]<- | 0 |
| PHI | [ | 8 | , | 7 | ]<- | 0 |
| PHI | [ | 8 | , | 8 | ]<- | phi [1] |
| PHI | [ | 8 | , | 9 | ]<- | 0 |
| PHI | [ | 8 | , | 10 | ]<- | 0 |
| PHI | [ | 8 | , | 11 | ]<- | 0 |
| PHI | [ | 8 | , | 12 | ]<- | 1-phi [1] |


| PHI | [ | 9 | , | 1 | ]<- |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 9 | , | 2 | ]<- | 0 |  |
| PHI | [ | 9 | , | 3 | ]<- | 0 |  |
| PHI | [ | 9 | , | 4 | ]<- | 0 |  |
| PHI | [ | 9 | , | 5 | ]<- | 0 |  |
| PHI | [ | 9 | , | 6 | ]<- | 0 |  |
| PHI | [ | 9 | , | 7 | ]<- | 0 |  |
| PHI | [ | 9 | , | 8 | ]<- | 0 |  |
| PHI | [ | 9 | , | 9 | ]<- | ph | [ [1] |
| PHI | [ | 9 | , | 10 | ]<- | 0 |  |
| PHI | [ | 9 |  | 11 | ]<- | 0 |  |
| PHI | [ | 9 |  | 12 | ]<- | 1 | -phi [1] |


| PHI | [ | 10 | , | 1 | ]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PHI | [ | 10 | , | 2 | ]<- |  |
| PHI | [ | 10 | , | 3 | ]<- | 0 |
| PHI | [ | 10 | , | 4 | ]<- | 0 |
| PHI | [ | 10 | , | 5 | ]<- | 0 |
| PHI | [ | 10 | , | 6 | ]<- | 0 |
| PHI | [ | 10 | , | 7 | ]<- | 0 |
| PHI | [ | 10 | , | 8 | ]<- | 0 |
| PHI | [ | 10 | , | 9 | ]<- | 0 |
| PHI | [ | 10 | , | 10 | ]<- | phi [1] |

$\left.\begin{array}{lllll}\text { PHI } & {[ } & 10 & , & 11 \\ \text { PHI } & {[ } & 10 & , & 12 \\ ]<- & 0 \\ \text { PHI } & {[ } & 11 & , & 1 \\ \hline\end{array}\right]<-0-$ phi $[1]$

```
# Define PSI matrices gathering state-to-state transition probabilities, it includes:
```

\# PSI1: offspring survival and growth to next age, proba of sexual maturation:
PSI1 [ 1 , 1 $\ll-1$
PSI1 [ 1 , 2 ]<- 0
PSI1 $[1,3]<-0$
PSI1 $[1,4]<-0$
PSI1 $[1,05]<-0$
PSI1 $\left[\begin{array}{llll}1 & , & 0\end{array}<-0\right.$
PSI1 $[1 \quad, \quad 7 \quad]<-0$
PSI1 $[1$, 8 ]<- 0
PSI1 $[1 \quad, \quad 9 \quad]<-0$
PSI1 [ 1 , 10 ]<- 0
PSI1 [ 1 , 11 ]<- 0
PSI1 $[12,12]<-0$
PSI1 [ 1 , 13 ]<- 0
PSI1 $[2,01]<-0$
PSI1 $[2,2]<-1$
PSI1 $[2,3]<-0$
PSI1 $[2,4]<-0$
PSI1 $[2,05<-0$
PSI1 $[2,6]<-0$
PSI1 $[2,7]<-0$
PSI1 $[2,0$ ] 0

```
PSI1 [ 2 , 9 ]<- 0
PSI1 [ 2 , 10 ]<- 0
PSI1 [ 2 , 11 ]<- 0
PSI1 [ 2 , 12 ]<- 0
PSI1 [ 2 , 13 ]<- 0
PSI1 [ 3 , 1 ]<- 0
PSI1 [ 3 , 2 ]<- 0
PSI1 [ 3 , 3 ]<- 1-kappa#1 #
PSI1 [ 3 , 4 ]<- 0
PSI1 [ 3 , 5 ]<- 0
PSI1 [ 3 , 6 ]<- 0
PSI1 [ 3 , 7 ]<- 0
PSI1 [ 3 , 8 ]<- 0
PSI1 [ 3 , 9 ]<- 0
PSI1 [ 3 , 10 ]<- 0
PSI1 [ 3 , 11 ]<- 0
PSI1 [ 3 , 12 ]<- kappa #0
PSI1 [ 3 , 13 ]<- 0
PSI1 [ 4 , 1 ]<- 0
PSI1 [ 4 , 2 ]<- 0
PSI1 [ 4 , 3 ]<- 0
PSI1 [ 4 , 4 ]<- 0
PSI1 [ 4 , 5 ]<- 0
PSI1 [ 4 , 6 ]<- 0
PSI1 [ 4 , 7 ]<- 0
PSI1 [ 4 , 8 ]<- 0
PSI1 [ 4 , 9 ]<- 0
PSI1 [ 4 , 10 ]<- 0
PSI1 [ 4 , 11 ]<- 0
PSI1 [ 4 , 12 ]<- 1
PSI1 [ 4 , 13 ]<- 0
PSI1 [ 5 , 1 ]<- 0
PSI1 [ 5 , 2 ]<- 0
PSI1 [ 5 , 3 ]<- 0
PSI1 [ 5 , 4 ]<- s[1] # litter of 1, cub survives
PSI1 [ 5 , 5 ]<- 0
PSI1 [ 5 , 6 ]<- 0
PSI1 [ 5 , 7 ]<- 0
PSI1 [ 5 , 8 ]<- 1-s[1] #litter of 1, cub dies
PSI1 [ 5 , 9 ]<- 0
PSI1 [ 5 , 10 ]<- 0
PSI1 [ 5 , 11 ]<- 0
PSI1 [ 5 , 12 ]<- 0
PSI1 [ 5 , 13 ]<- 0
PSI1 [ 6 , 1 ]<- 0
PSI1 [ 6 , 2 ]<- 0
PSI1 [ 6 , 3 ]<- 0
PSI1 [ 6 , 4 ]<- 2*s[2]*(1-s[2]) # litter of 2, 1 cub survives
PSI1 [ 6 , 5 ]<- s[2]^2 # litter of 2, both cubs survive
```

```
PSI1 [ [ 6 , 6 % ]<- 0
PSI1 [ 6 , 8 ]<- (1- s[2] 2 - 2*s[2]*(1-s[2])) #litter of 2, both cubs die
PSI1 [ 6 , 9 ]<- 0
PSI1 [ 6 , 10 ]<- 0
PSI1 [ 6 , 11 ]<- 0
PSI1 [ 6 , 12 ]<- 0
PSI1 [ 6 , 13 ]<- 0
PSI1 [ 7 , 1 ]<- 0
PSI1 [ 7 , 2 ]<- 0
PSI1 [ 7 , 3 ]<- 0
PSI1 [ 7 , 4 ]<- 0
PSI1 [ 7 , 5 ]<- 0
PSI1 [ 7 , 6 ]<- s[3] # litter of 1, yearling survives
PSI1 [ 7 , 7 ]<- 0
PSI1 [ 7 , 8 ]<- 0
PSI1 [ 7 , 9 ]<- (1-s[3] ) # litter of 1, yearling dies
PSI1 [ 7 , 10 ]<- 0
PSI1 [ 7 , 11 ]<- 0
PSI1 [ 7 , 12 ]<- 0
PSI1 [ 7 , 13 ]<- 0
PSI1 [ 8 , 1 ]<- 0
PSI1 [ 8 , 2 ]<- 0
PSI1 [ 8 , 3 ]<- 0
PSI1 [ 8 , 4 ]<- 0
PSI1 [ 8 , 5 ]<- 0
PSI1 [ 8 , 6 ]<- 2*s[4]*(1-s[4]) # litter of 2, 1 yearling survives
PSI1 [ 8 , 7 ]<- s[4] 2 # litter of 2, both yearlings survive
PSI1 [ 8 , 8 ]<- 0
PSI1 [ 8 , 9 ]<- (1- s[4] 2 -2*s[4]*(1-s[4])) #litter of 2, both yearlings die
PSI1 [ 8 , 10 ]<- 0
PSI1 [ 8 , 11 ]<- 0
PSI1 [ 8 , 12 ]<- 0
PSI1 [ 8 , 13 ]<- 0
PSI1 [ 9 , 1 ]<- 0
PSI1 [ 9 , 2 ]<- 0
PSI1 [ 9 , 3 ]<- 0
PSI1 [ 9 , 4 ]<- 0
PSI1 [ 9 , 5 ]<- 0
PSI1 [ 9 , 6 ]<- 0
PSI1 [ 9 , 7 ]<- 0
PSI1 [ 9 , 8 ]<- 0
PSI1 [ 9 , 9 ]<- 0
PSI1 [ 9 , 10 ]<- 1
PSI1 [ 9 , 11 ]<- 0
PSI1 [ 9 , 12 ]<- 0
PSI1 [ 9 , 13 ]<- 0
PSI1 [ 10 , 1 ]<- 0
```

| PSI1 | [ | 10 | 2 | ]<- |
| :---: | :---: | :---: | :---: | :---: |
| I1 | [ | 10 | 3 | ]<- |
| I1 | [ | 10 | 4 | ]<- |
| SI1 | [ | 10 | 5 | ]< |
| I1 | [ | 10 | 6 | ]<- |
| PSI1 | [ | 10 | 7 | ]<- |
| I1 | [ | 10 | 8 | ]< |
| I1 | [ | 10 | 9 | ]< |
| I1 | [ | 10 | 10 | ]<- |
| I1 | [ | 10 | 11 | ]<- |
| SI1 | [ | 10 | 12 | ]<- |
| PSI1 | [ | 10 | 13 | ]< |
| PSI1 |  | 11 | , 1 | ]<- 0 |
| PSI1 | [ | 11 | , 2 | ]<- |
| I1 | [ | 11 | , 3 | ]<- |
| PSI1 | [ | 11 | 4 | ] |
| PSI1 | [ | 11 | 5 | ]< |
| PSI1 | [ | 11 | - 6 | ]<- |
| SI1 | [ | 11 | 7 | ]<- |
| I1 | [ | 11 | - 8 | ]< |
| I1 | [ | 11 | 9 | ] |
| I1 | [ | 11 | 10 | ]<- |
| I1 | [ | 11 | 11 | ]<- |
| PSI1 | [ | 11 | 12 | ]<- |
| PSI1 | [ | 11 | 13 | ]< |
| I1 | [ | 12 | 1 | ]<- 0 |
| PSI1 | [ | 12 | 2 | ]<- 0 |
| I1 | [ | 12 | 3 | ]< |
| SI1 | [ | 12 | - 4 | ]<- |
| PSI1 | [ | 12 | - 5 | ]<- |
| PSI1 | [ | 12 | , 6 | ]<- 0 |
| PSI1 | [ | 12 | 7 | ]<- 0 |
| PSI1 | [ | 12 | 8 | ]<- |
| SI1 | [ | 12 | - 9 | ]<- |
| PSI1 | [ | 12 | 10 | ]<- |
| PSI1 | [ | 12 | 11 | ]<- 0 |
| PSI1 | [ | 12 | 12 | ]<- 0 |
| SI1 | [ | 12 | 1 | ]<- |

\# PSI2: breeding probabilities:
PSI2 [ 1 , 1 ]<- 1
PSI2 [ 1 , 2 ]<- 0
PSI2 [ 1 , 3 ]<- 0
PSI2 $[1,4]<-0$
PSI2 $[1,0] \quad 0<-0$
PSI2 $[1$, 6 ]<- 0
PSI2 [ 1 , 7 ]<- 0
PSI2 [ 1 , 8 ]<- 0
PSI2 [ 1 , 9 ]<- 0
PSI2 $[11, \quad 10]<-0$

| PSI2 | $[$ | 1 | , | 12 | $]<-$ | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PSI2 | $[$ | 1 | , | 13 | $]<-$ | 0 |
| PSI2 | $[$ | 1 | , | 14 | $]<-$ | 0 |
| PSI2 | $[$ | 1 | , | 15 | $]<-$ | 0 |
| PSI2 | $[$ | 1 | , | 16 | $]<-$ | 0 |


| PSI2 | [ | 2 |  | 1 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 2 |  | 2 | ]<-1 |
| PSI2 | [ | 2 |  | 3 | ]<- 0 |
| PSI2 | [ | 2 |  | 4 | ]<- 0 |
| PSI2 | [ | 2 |  | 5 | ]<- 0 |
| PSI2 | [ | 2 |  | 6 | ]<- 0 |
| PSI2 | [ | 2 |  | 7 | ]<- 0 |
| PSI2 | [ | 2 | , | 8 | ]<- 0 |
| PSI2 | [ | 2 | , | 9 | ]<-0 |
| PSI2 | [ | 2 |  | 10 | ]<- 0 |
| PSI2 | [ | 2 |  | 11 | ]<- 0 |
| PSI2 | [ | 2 |  | 12 | ]<- 0 |
| PSI2 | [ | 2 |  | 13 | ]<-0 |
| PSI2 | [ | 2 |  | 14 | ]<-0 |
| PSI2 | [ | 2 |  | 15 | ]<- 0 |
| PSI2 | [ | 2 |  | 16 | ]<- |


| PSI2 | [ | 3 |  | 1 | ]<-0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 3 |  | 2 | ]<-0 |
| PSI2 | [ | 3 |  | 3 | ]<-1 |
| PSI2 | [ | 3 |  | 4 | ]<-0 |
| PSI2 | [ | 3 |  | 5 | ]<-0 |
| PSI2 | [ | 3 |  | 6 | ]<-0 |
| PSI2 | [ | 3 |  | 7 | ]<-0 |
| PSI2 | [ | 3 |  | 8 | ]<-0 |
| PSI2 | [ | 3 |  | 9 | ]<-0 |
| PSI2 | [ | 3 |  | 10 | ]<-0 |
| PSI2 | [ | 3 |  | 11 | ]<-0 |
| PSI2 | [ | 3 |  | 12 | ]<-0 |
| PSI2 | [ | 3 |  | 13 | ]<-0 |
| PSI2 | [ | 3 |  | 14 | ]<-0 |
| PSI2 | [ | 3 |  | 15 | ]<-0 |
| PSI2 | [ | 3 |  | 16 | ]<-0 |

PSI2 $[4$, 1 ]<- 0
PSI2 $[4,2]<-0$
PSI2 [ 4 , 3 ]<- 0
PSI2 $[4,4]<-1$
PSI2 [ 4 , 5 ]<- 0
PSI2 $[4,6]<-0$
PSI2 $[4,7]<-0$
PSI2 $[4,0]<-0$
PSI2 $[4,0] \quad 0<-0$
PSI2 $[4,010]<-0$
PSI2 $[4,11]<-0$
PSI2 $[4,12]<-0$
PSI2 $[4,13]<-0$

| PSI2 | [ | 4 | 14 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 4 | 15 | ]<- 0 |
| PSI2 | [ | 4 | 16 | ]<- 0 |
| PSI2 | [ | 5 | , 1 | ]<- 0 |
| PSI2 | [ | 5 | 2 | ]<- 0 |
| PSI2 | [ | 5 | 3 | ]<- 0 |
| PSI2 | [ | 5 | 4 | ]<- 0 |
| PSI2 | [ | 5 | , 5 | ]<-1 |
| PSI2 | [ | 5 | 6 | ]<- 0 |
| PSI2 | [ | 5 | , 7 | ]<-0 |
| PSI2 | [ | 5 | 8 | ]<-0 |
| PSI2 | [ | 5 | 9 | ]<- 0 |
| PSI2 | [ | 5 | 10 | ]<-0 |
| PSI2 | [ | 5 | 11 | ]<-0 |
| PSI2 | [ | 5 | 12 | ]<- 0 |
| PSI2 | [ | 5 | 13 | ]<-0 |
| PSI2 | [ | 5 | 14 | ]<- 0 |
| PSI2 | [ | 5 | 15 | ]<-0 |
| PSI2 | [ | 5 | 16 | ]<- 0 |
| PSI2 | [ | 6 | , 1 | ]<- 0 |
| PSI2 | [ | 6 | 2 | ]<- 0 |
| PSI2 | [ | 6 | 3 | ]<-0 |
| PSI2 | [ | 6 | 4 | ]<-0 |
| PSI2 | [ | 6 | 5 | ]<- 0 |
| PSI2 | [ | 6 | 6 | ]<-1 |
| PSI2 | [ | 6 | 7 | ]<- 0 |
| PSI2 | [ | 6 | 8 | ]<- 0 |
| PSI2 | [ | 6 | 9 | ]<- 0 |
| PSI2 | [ | 6 | 10 | ]<- 0 |
| PSI2 | [ | 6 | 11 | ]<-0 |
| PSI2 | [ | 6 | 12 | ]<- 0 |
| PSI2 | [ | 6 | 13 | ]<- 0 |
| PSI2 | [ | 6 | 14 | ]<-0 |
| PSI2 | [ | 6 | 15 | ]<-0 |
| PSI2 | [ | 6 | 16 | ]<- 0 |
| PSI2 | [ | 7 | , 1 | ]<- 0 |
| PSI2 | [ | 7 | 2 | ]<-0 |
| PSI2 | [ | 7 | 3 | ]<- 0 |
| PSI2 | [ | 7 | 4 | ]<-0 |
| PSI2 | [ | 7 | 5 | ]<-0 |
| PSI2 | [ | 7 | 6 | ]<- 0 |
| PSI2 | [ | 7 | 7 | ]<-1 |
| PSI2 | [ | 7 | 8 | ]<-0 |
| PSI2 | [ | 7 | 9 | ]<- 0 |
| PSI2 | [ | 7 | 10 | ]<- 0 |
| PSI2 | [ | 7 | 11 | ]<- 0 |
| PSI2 | [ | 7 | 12 | ]<- 0 |
| PSI2 | [ | 7 | 13 | ]<- 0 |
| PSI2 | [ | 7 | 14 | ]<- |
| PSI2 | [ | 7 | 15 | ]<- |


| PSI2 | [ | 7 |  | 16 | ]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PSI2 | [ | 8 | , | 1 | ]<- | 0 |
| PSI2 | [ | 8 | , | 2 | ]<- | 0 |
| PSI2 | [ | 8 |  | 3 | ]<- | 0 |
| PSI2 | [ | 8 | , | 4 | ]<- | 0 |
| PSI2 | [ | 8 | , | 5 | ]<- | 0 |
| PSI2 | [ | 8 | , | 6 | ]<- | 0 |
| PSI2 | [ | 8 | , | 7 | ]<- | 0 |
| PSI2 | [ | 8 | , | 8 | ]<- | beta[1] |
| PSI2 | [ | 8 | , | 9 | ]<- | 1-beta[1] |
| PSI2 | [ | 8 | , | 10 |  | 0 |
| PSI2 | [ | 8 | , | 11 | ]<- | 0 |
| PSI2 | [ | 8 | , | 12 | ]<- | 0 |
| PSI2 | [ | 8 | , | 13 | ]<- | 0 |
| PSI2 | [ | 8 | , | 14 | ]<- | 0 |
| PSI2 | [ | 8 | , | 15 | ]<- | 0 |
| PSI2 | [ | 8 | , | 16 | ]<- | 0 |
| PSI2 | [ | 9 | , | 1 | ]<- | 0 |
| PSI2 | [ | 9 | , | 2 | ]<- | 0 |
| PSI2 | [ | 9 | , | 3 | ]<- | 0 |
| PSI2 | [ | 9 | , | 4 | ]<- | 0 |
| PSI2 | [ | 9 | , | 5 | ]<- | 0 |
| PSI2 | [ | 9 | , | 6 | ]<- | 0 |
| PSI2 | [ | 9 | , | 7 | ]<- | 0 |
| PSI2 | [ | 9 | , | 8 | ]<- | 0 |
| PSI2 | [ | 9 | , | 9 | ]<- | 0 |
| PSI2 | [ | 9 |  | 10 | ]<- | beta[2] |
| PSI2 | [ | 9 |  | 11 | ]<- | 1-beta[2] |
| PSI2 | [ | 9 |  | 12 | ]<- | 0 |
| PSI2 | [ | 9 |  | 13 | ]<- | 0 |
| PSI2 | [ | 9 |  | 14 | ]<- | 0 |
| PSI2 | [ | 9 |  | 15 | ]<- | 0 |
| PSI2 | [ | 9 | , | 16 | ]<- | 0 |
| PSI2 | [ | 10 | , | 1 | ]<- | 0 |
| PSI2 | [ | 10 |  | 2 | ]<- | 0 |
| PSI2 | [ | 10 |  | 3 | ]<- | 0 |
| PSI2 | [ | 10 |  | 4 | ]<- | 0 |
| PSI2 | [ | 10 | , | 5 | ]<- | 0 |
| PSI2 | [ | 10 |  | 6 | ]<- | 0 |
| PSI2 | [ | 10 |  | 7 | ]<- | 0 |
| PSI2 | [ | 10 |  | 8 | ]<- | 0 |
| PSI2 | [ | 10 | , | 9 | ]<- | 0 |
| PSI2 | [ | 10 |  | 10 | ]<- | 0 |
| PSI2 | [ | 10 |  | 11 | ]<- | 0 |
| PSI2 | [ | 10 |  | 12 | ]<- | beta [3] |
| PSI2 | [ | 10 |  | 13 | ]<- | 1-beta [3] |
| PSI2 | [ | 10 |  | 14 | ]<- | 0 |
| PSI2 | [ | 10 |  | 15 | ]<- | 0 |
| PSI2 | [ | 10 |  | 16 | ]<- | 0 |

```
PSI2 [ 11 , 1 ]<- 0
PSI2 [ 11 , 2 ]<- 0
PSI2 [ 11 , 3 ]<- 0
PSI2 [ 11 , 4 ]<- 0
PSI2 [ 11 , 5 ]<- 0
PSI2 [ 11 , 6 ]<- 0
PSI2 [ 11 , 7 ]<- 0
PSI2 [ 11 , 8 ]<- 0
PSI2 [ 11 , 9 ]<- 0
PSI2 [ 11 , 10 ]<- 0
PSI2 [ 11 , 11 ]<- 0
PSI2 [ 11 , 12 ]<- beta[3]
PSI2 [ 11 , 13 ]<- 1-beta[3]
PSI2 [ 11 , 14 ]<- 0
PSI2 [ 11 , 15 ]<- 0
PSI2 [ 11 , 16 ]<- 0
PSI2 [ 12 , 1 ]<- 0
PSI2 [ 12 , 2 ]<- 0
PSI2 [ 12 , 3 ]<- 0
PSI2 [ 12 , 4 ]<- 0
PSI2 [ 12 , 5 ]<- 0
PSI2 [ 12 , 6 ]<- 0
PSI2 [ 12 , 7 ]<- 0
PSI2 [ 12 , 8 ]<- 0
PSI2 [ 12 , 9 ]<- 0
PSI2 [ 12 , 10 ]<- 0
PSI2 [ 12 , 11 ]<- 0
PSI2 [ 12 , 12 ]<- 0
PSI2 [ 12 , 13 ]<- 0
PSI2 [ 12 , 14 ]<- beta[3]
PSI2 [ 12 , 15 ]<- 1-beta[3]
PSI2 [ 12 , 16 ]<- 0
PSI2 [ 13 , 1 ]<- 0
PSI2 [ 13 , 2 ]<- 0
PSI2 [ 13 , 3 ]<- 0
PSI2 [ 13 , 4 ]<- 0
PSI2 [ 13 , 5 ]<- 0
PSI2 [ 13 , 6 ]<- 0
PSI2 [ 13 , 7 ]<- 0
PSI2 [ 13 , 8 ]<- 0
PSI2 [ 13 , 9 ]<- 0
PSI2 [ 13 , 10 ]<- 0
PSI2 [ 13 , 11 ]<- 0
PSI2 [ 13 , 12 ]<- 0
PSI2 [ 13 , 13 ]<- 0
PSI2 [ 13 , 14 ]<- 0
PSI2 [ 13 , 15 ]<- 0
PSI2 [ 13 , 16 ]<- 1
# PSI3:litter size probabilities
PSI3 [ 1 , 1 ]<- 0
```

| PSI3 | [ | 1 | 2 | ]<- 1 |
| :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 1 | 3 | ]<- 0 |
| PSI3 | [ | 1 | 4 | ]<- 0 |
| PSI3 | [ | 1 | 5 | ]<- 0 |
| PSI3 | [ | 1 | 6 | ]<-0 |
| PSI3 | [ | 1 | 7 | ]<-0 |
| PSI3 | [ | 1 | 8 | ]<- 0 |
| PSI3 | [ | 1 | 9 | ]<- 0 |
| PSI3 | [ | 1 | 10 | ]<- 0 |
| PSI3 | [ | 1 | 11 | ]<-0 |
| PSI3 | [ | 1 | 12 | ]<- 0 |
| PSI3 | [ | 2 | 1 | ]<- 0 |
| PSI3 | [ | 2 | 2 | ]<- 0 |
| PSI3 | [ | 2 | 3 | ]<-1 |
| PSI3 | [ | 2 | 4 | ]<- 0 |
| PSI3 | [ | 2 | 5 | ]<- 0 |
| PSI3 | [ | 2 | 6 | ]<-0 |
| PSI3 | [ | 2 | 7 | ]<- 0 |
| PSI3 | [ | 2 | 8 | ]<- 0 |
| PSI3 | [ | 2 | 9 | ]<-0 |
| PSI3 | [ | 2 | 10 | ]<- 0 |
| PSI3 | [ | 2 | 11 | ]<- 0 |
| PSI3 | [ | 2 | 12 | ]<- 0 |
| PSI3 | [ | 3 | 1 | ]<- 0 |
| PSI3 | [ | 3 | 2 | ]<-0 |
| PSI3 | [ | 3 | 3 | ]<- 0 |
| PSI3 | [ | 3 | 4 | ]<-1 |
| PSI3 | [ | 3 | 5 | ]<- 0 |
| PSI3 | [ | 3 | 6 | ]<-0 |
| PSI3 | [ | 3 | 7 | ]<-0 |
| PSI3 | [ | 3 | 8 | ]<- 0 |
| PSI3 | [ | 3 | 9 | ]<- 0 |
| PSI3 | [ | 3 | 10 | ]<- 0 |
| PSI3 | [ | 3 | 11 | ]<- 0 |
| PSI3 | [ | 3 | , 12 | ]<- 0 |
| PSI3 | [ | 4 | 1 | ]<- 0 |
| PSI3 | [ | 4 | 2 | ]<-0 |
| PSI3 | [ | 4 | 3 | ]<-0 |
| PSI3 | [ | 4 | 4 | ]<-0 |
| PSI3 | [ | 4 | 5 | ]<- 0 |
| PSI3 | [ | 4 | 6 | ]<- 0 |
| PSI3 | [ | 4 | 7 | ]<-1 |
| PSI3 | [ | 4 | 8 | ]<- 0 |
| PSI3 | [ | 4 | 9 | ]<-0 |
| PSI3 | [ | 4 | 10 | ]<- 0 |
| PSI3 | [ | 4 | 11 | ]<- 0 |
| PSI3 | [ | 4 | , 12 | ]<-0 |
| PSI3 | [ | 5 | 1 | ]<- 0 |
| PSI3 | [ | 5 | 2 | ]<- 0 |


| PSI3 | [ | 5 | , | 3 | ]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 5 | , | 4 | ]<- | 0 |
| PSI3 | [ | 5 | , | 5 | ]<- | 0 |
| PSI3 | [ | 5 | , | 6 | ]<- | 0 |
| PSI3 | [ | 5 | , | 7 | ]<- | 0 |
| PSI3 | [ | 5 | , | 8 | ]<- | 1 |
| PSI3 | [ | 5 | , | 9 | ]<- | 0 |
| PSI3 | [ | 5 | , | 10 | ]<- | 0 |
| PSI3 | [ | 5 | , | 11 | ]<- | 0 |
| PSI3 | [ | 5 | , | 12 | ]<- | 0 |
| PSI3 | [ | 6 | , | 1 | ]<- | 0 |
| PSI3 | [ | 6 | , | 2 | ]<- | 0 |
| PSI3 | [ | 6 | , | 3 | ]<- | 0 |
| PSI3 | [ | 6 | , | 4 | ]<- | 0 |
| PSI3 | [ | 6 | , | 5 | ]<- | 0 |
| PSI3 | [ | 6 | , | 6 | ]<- | 0 |
| PSI3 | [ | 6 | , | 7 | ]<- | 0 |
| PSI3 | [ | 6 | , | 8 | ]<- | 0 |
| PSI3 | [ | 6 | , | 9 | ]<- | 1 |
| PSI3 | [ | 6 | , | 10 | ]<- | 0 |
| PSI3 | [ | 6 | , | 11 | ]<- | 0 |
| PSI3 | [ | 6 | , | 12 | ]<- | 0 |
| PSI3 | [ | 7 | , | 1 | ]<- | 0 |
| PSI3 | [ | 7 | , | 2 | ]<- | 0 |
| PSI3 | [ | 7 | , | 3 | ]<- | 0 |
| PSI3 | [ | 7 | , | 4 | ]<- | 0 |
| PSI3 | [ | 7 | , | 5 | ]<- | 0 |
| PSI3 | [ | 7 | , | 6 | ]<- | 0 |
| PSI3 | [ | 7 | , | 7 | ]<- | 0 |
| PSI3 | [ | 7 | , | 8 | ]<- | 0 |
| PSI3 | [ | 7 | , | 9 | ]<- | 0 |
| PSI3 | [ | 7 | , | 10 | ]<- | 1 |
| PSI3 | [ | 7 | , | 11 | ]<- | 0 |
| PSI3 | [ | 7 | , | 12 | ]<- | 0 |
| PSI3 | [ | 8 | , | 1 | ]<- | 0 |
| PSI3 | [ | 8 | , | 2 | ]<- | 0 |
| PSI3 | [ | 8 | , | 3 | ]<- | 0 |
| PSI3 | [ | 8 | , | 4 | ]<- | 0 |
| PSI3 | [ | 8 | , | 5 | ]<- | gamma [1] |
| PSI3 | [ | 8 | , | 6 | ]<- | 1-gamma [1] |
| PSI3 | [ | 8 | , | 7 | ]<- | 0 |
| PSI3 | [ | 8 | , | 8 | ]<- | 0 |
| PSI3 | [ | 8 | , | 9 | ]<- | 0 |
| PSI3 | [ | 8 | , | 10 | ]<- | 0 |
| PSI3 | [ | 8 | , | 11 | ]<- |  |
| PSI3 | [ | 8 | , | 12 | ]<- |  |
| PSI3 | [ | 9 | , | 1 | ]<- |  |
| PSI3 | [ | 9 |  | 2 | ]<- |  |
| PSI3 | [ | 9 |  | 3 | ]<- |  |


| PSI3 | [ | 9 | 4 | ]<- 0 |
| :---: | :---: | :---: | :---: | :---: |
| PSI3 | [ | 9 | 5 | ]<- 0 |
| PSI3 | [ | 9 | 6 | ]<- 0 |
| PSI3 | [ | 9 | 7 | ]<- 0 |
| PSI3 | [ | 9 | 8 | ]<- 0 |
| PSI3 | [ | 9 | 9 | ]<- 0 |
| PSI3 | [ | 9 | 10 | ]<- 0 |
| PSI3 | [ | 9 | 11 | ]<-1 |
| PSI3 | [ | 9 | , 12 | ]<- 0 |
| PSI3 | [ | 10 | 1 | ]<- 0 |
| PSI3 | [ | 10 | 2 | ]<- 0 |
| PSI3 | [ | 10 | 3 | ]<- 0 |
| PSI3 | [ | 10 | 4 | ]<- 0 |
| PSI3 | [ | 10 | 5 | ]<- gamma[1] |
| PSI3 | [ | 10 | 6 | ]<- 1-gamma[1] |
| PSI3 | [ | 10 | 7 | ]<- 0 |
| PSI3 | [ | 10 | 8 | ]<- 0 |
| PSI3 | [ | 10 | 9 | ]<-0 |
| PSI3 | [ | 10 | 10 | ]<- 0 |
| PSI3 | [ | 10 | 11 | ]<- 0 |
| PSI3 | [ | 10 | 12 | ]<- 0 |
| PSI3 | [ | 11 | 1 | ]<- 0 |
| PSI3 | [ | 11 | 2 | ]<- 0 |
| PSI3 | [ | 11 | 3 | ]<- 0 |
| PSI3 | [ | 11 | 4 | ]<- 0 |
| PSI3 | [ | 11 | 5 | ]<- 0 |
| PSI3 | [ | 11 | , 6 | ]<- 0 |
| PSI3 | [ | 11 | , 7 | ]<- 0 |
| PSI3 | [ | 11 | , 8 | ]<- 0 |
| PSI3 | [ | 11 | , 9 | ]<- 0 |
| PSI3 | [ | 11 | 10 | ]<- 0 |
| PSI3 | [ | 11 | , 11 | ]<- 1 |
| PSI3 | [ | 11 | , 12 | ]<- 0 |
| PSI3 | [ | 12 | 1 | ]<- 0 |
| PSI3 | [ | 12 | 2 | ]<- 0 |
| PSI3 | [ | 12 | 3 | ]<- 0 |
| PSI3 | [ | 12 | 4 | ]<- 0 |
| PSI3 | [ | 12 | 5 | ]<- gamma[2] |
| PSI3 | [ | 12 | 6 | ]<- 1-gamma[2] |
| PSI3 | [ | 12 | 7 | ]<- 0 |
| PSI3 | [ | 12 | 8 | ]<- 0 |
| PSI3 | [ | 12 | 9 | ]<- 0 |
| PSI3 | [ | 12 | 10 | ]<- 0 |
| PSI3 | [ | 12 | , 11 | ]<- 0 |
| PSI3 | [ | 12 | , 12 | ]<- 0 |
| PSI3 | [ | 13 | 1 | ]<- 0 |
| PSI3 | [ | 13 | 2 | ]<- 0 |
| PSI3 | [ | 13 | 3 | ]<- 0 |
| PSI3 | [ | 13 | 4 | ]<- 0 |



```
PSI3 [ 14 , 1 ]<- 0
PSI3 [ 14 , 2 ]<- 0
PSI3 [ 14 , 3 ]<- 0
PSI3 [ 14 , 4 ]<- 0
PSI3 [ 14 , 5 ]<- gamma [2]
PSI3 [ 14 , 6 ]<- 1-gamma [2]
PSI3 [ 14 , 7 ]<- 0
PSI3 [ 14 , 8 ]<- 0
PSI3 [ 14 , 9 ]<- 0
PSI3 [ 14 , 10 ]<- 0
PSI3 [ 14 , 11 ]<- 0
PSI3 [ 14 , 12 ]<- 0
PSI3 [ 15 , 1 ]<- 0
PSI3 [ 15 , 2 ]<- 0
PSI3 [ 15 , 3 ]<- 0
PSI3 [ 15 , 4 ]<- 0
PSI3 [ 15 , 5 ]<- 0
PSI3 [ 15 , 6 ]<- 0
PSI3 [ 15 , 7 ]<- 0
PSI3 [ 15 , 8 ]<- 0
PSI3 [ 15 , 9 ]<- 0
PSI3 [ 15 , 10 ]<- 0
PSI3 [ 15 , 11 ]<- 1
PSI3 [ 15 , 12 ]<- 0
PSI3 [ 16 , 1 ]<- 0
PSI3 [ 16 , 2 ]<- 0
PSI3 [ 16 , 3 ]<- 0
PSI3 [ 16 , 4 ]<- 0
PSI3 [ 16 , 5 ]<- 0
PSI3 [ 16 , 6 ]<- 0
PSI3 [ 16 , 7 ]<- 0
PSI3 [ 16 , 8 ]<- 0
PSI3 [ 16 , 9 ]<- 0
PSI3 [ 16 , 10 ]<- 0
PSI3 [ 16 , 11 ]<- 0
PSI3 [ 16 , 12 ]<- 1
# Matrix product for state-to-state transitions S
S[1:12,1:12] <- PHI[1:12,1:12] %*% PSI1[1:12,1:13] %*% PSI2[1:13,1:16] %*% PSI3[1:16,1:12]
## Observation process: Define probabilities of E(t) given S(t).
```



| EO | [ | 9 | 2 | ]<-0 |
| :---: | :---: | :---: | :---: | :---: |
| E0 | [ | 9 | 3 | ]<-0 |
| E0 | [ | 9 | 4 | ]<-0 |
| E0 | [ | 9 | 5 | ]<-0 |
| E0 | [ | 9 | 6 | ]<-0 |
| EO | [ | 9 | 7 | ]<-0 |
| EO | [ | 9 | 8 | ]<-0 |
| E0 | [ | 9 | 9 | ]<-0 |
| E0 | [ | 9 | 10 | ]<-1 |
| E0 | [ | 9 | 11 | ]<-0 |
| E0 | [ | 9 | 12 | ]<- 0 |
| E0 | [ | 10 | 1 | ]<-0 |
| E0 | [ | 10 | 2 | ]<-0 |
| E0 | [ | 10 | 3 | ]<-0 |
| E0 | [ | 10 | 4 | ]<-0 |
| E0 | [ | 10 | 5 | ]<-0 |
| E0 | [ | 10 | 6 | ]<-0 |
| E0 | [ | 10 | 7 | ]<-0 |
| E0 | [ | 10 | 8 | ]<-0 |
| E0 | [ | 10 | 9 | ]<-0 |
| E0 | [ | 10 | 10 | ]<-0 |
| E0 | [ | 10 | 11 | ]<-1 |
| E0 | [ | 10 | 12 | ]<-0 |
| EO | [ | 11 | 1 | ]<-0 |
| EO | [ | 11 | 2 | ]<-0 |
| EO | [ | 11 | 3 | ]<-0 |
| E0 | [ | 11 | 4 | ]<-0 |
| EO | [ | 11 | 5 | ]<-0 |
| E0 | [ | 11 | 6 | ]<-0 |
| E0 | [ | 11 | 7 | ]<-0 |
| E0 | [ | 11 | 8 | ]<-0 |
| E0 | [ | 11 | , 9 | ]<-0 |
| E0 | [ | 11 | 10 | ]<-0 |
| E0 | [ | 11 | 11 | ]<-0 |
| E0 | [ | 11 | 12 | ]<-1 |
| E0 | [ | 12 | 1 | ]<-1 |
| E0 | [ | 12 | 2 | ]<-0 |
| E0 | [ | 12 | 3 | ]<-0 |
| E0 | [ | 12 | 4 | ]<-0 |
| E0 | [ | 12 | 5 | ]<-0 |
| E0 | [ | 12 | 6 | ]<-0 |
| E0 | [ | 12 | 7 | ]<-0 |
| E0 | [ | 12 | 8 | ]<-0 |
| E0 | [ | 12 | 9 | ]<-0 |
| E0 | [ | 12 | 10 | ]<- 0 |
| E0 | [ | 12 | 11 | ]<-0 |
| EO | [ | 12 | , 12 | ]<-0 |

1
2

| for(t in 1:(Years-1))\{ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E1 | [ | 1 | , | 1 | ,i,t]< |  |
| E1 | [ | 1 | , | 2 | ,i,t] |  |
| E1 | [ | 1 | , | 3 | ,i,t] |  |
| E1 | [ | 1 | , | 4 | ,i,t] |  |
| E1 | [ | 1 | , | 5 | ,i,t] |  |
| E1 | [ | 1 | , | 6 | ,i,t] |  |
| E1 | [ | 1 | , | 7 | ,i,t] |  |
| E1 | [ | 1 | , | 8 | ,i,t] |  |
| E1 | [ | 1 | , | 9 | ,i,t] |  |
| E1 | [ | 1 | , |  | i,t]<- | 0 |
| E1 | [ | 1 | , |  | i, t]<- | 0 |
| E1 | [ | 1 | , |  | i, t]<- | 0 |
| E1 | [ | 2 | , | 1 | ,i,t] |  |
| E1 | [ | 2 | , | 2 | ,i,t]< | 1 |
| E1 | [ | 2 | , | 3 | ,i,t]< | 0 |
| E1 | [ | 2 | , | 4 | ,i,t] | 0 |
| E1 | [ | 2 | , | 5 | ,i,t] | 0 |
| E1 | [ | 2 | , | 6 | ,i,t] | - 0 |
| E1 | [ | 2 | , | 7 | ,i,t]< | - 0 |
| E1 | [ | 2 | , | 8 | ,i,t]< | - 0 |
| E1 | [ | 2 | , | 9 | ,i,t]< |  |
| E1 | [ | 2 | , |  | i, t]<- | 0 |
| E1 | [ | 2 | , |  | i, t]<- | 0 |
| E1 | [ | 2 | , |  | i, t]<- | 0 |
| E1 | [ | 3 | , | 1 | ,i,t]< |  |
| E1 | [ | 3 | , | 2 | ,i,t]< | - 0 |
| E1 | [ | 3 | , | 3 | ,i,t]< | - 1 |
| E1 | [ | 3 | , | 4 | ,i,t]< |  |
| E1 | [ | 3 | , | 5 | ,i,t]< | - 0 |
| E1 | [ | 3 | , | 6 | ,i,t]< | - 0 |
| E1 | [ | 3 | , | 7 | ,i,t]< | - 0 |
| E1 | [ | 3 | , | 8 | ,i,t]< | - 0 |
| E1 | [ | 3 | , | 9 | ,i,t]< |  |
| E1 | [ | 3 | , |  | i, t]<- | 0 |
| E1 | [ | 3 | , |  | i, t]<- | 0 |
| E1 | [ | 3 | , |  | i, t]<- | 0 |
| E1 | [ | 4 | , | 1 | ,i,t]< | 0 |
| E1 | [ | 4 | , | 2 | ,i,t]< | - 0 |
| E1 | [ | 4 | , | 3 | ,i,t]< | 0 |
| E1 | [ | 4 | , | 4 | ,i,t]< | 1 |
| E1 | [ | 4 | , | 5 | ,i,t]< | - 0 |
| E1 | [ | 4 | , | 6 | ,i,t]< | 0 |
| E1 | [ | 4 | , | 7 | ,i,t]< | - 0 |
| E1 | [ | 4 | , | 8 | ,i,t]< | 0 |
| E1 | [ | 4 | , | 9 | ,i,t]< |  |
| E1 | [ | 4 | , |  | i, t]<- | 0 |
| E1 | [ | 4 |  |  | i, t]<- | 0 |
| E1 | [ | 4 |  |  | i, t]<- |  |

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$$
\begin{aligned}
& \begin{array}{lllll}
\text { E1 } \\
\text { E1 }
\end{array} \quad\left[\begin{array}{llll}
{[ } & , & 2 & , i, t]<- \\
0 & , & 3 & , i, t]<- \\
0
\end{array}\right. \\
& \text { E1 }[9,4, i, t]<-0 \\
& \text { E1 [ } 9 \text {, } 5 \text {,i,t]<- } 0 \\
& \text { E1 [ } 9 \quad, \quad 6 \quad, i, t]<-\quad 0 \\
& \text { E1 [ } \quad[\quad, \quad 7 \quad, i, t]<-0 \\
& \begin{array}{lllll}
\text { E1 } & {\left[\begin{array}{lll}
9 & 8 & , i, t]<- \\
\text { E1 } & {[ } & 9
\end{array}, \quad 9\right.} & , i, t]<-1-a l p h a[i, t+1]
\end{array} \\
& \text { E1 }[9 \quad, \quad 10, i, t]<-\quad 0 \\
& \text { E1 [ } 9 \text {, 11,i,t]<- alpha[i,t+1] } \\
& \text { E1 [ } 9 \quad, \quad 12, i, t]<-\quad 0 \\
& \text { E1 }[10, \quad 1, i, t]<-\quad 0 \\
& \text { E1 }[10,2, i, t]<-\quad 0 \\
& \text { E1 }[10,3, i, t]<-\quad 0 \\
& \text { E1 }[10,4, \mathrm{i}, \mathrm{t}]<-\quad 0 \\
& \text { E1 [ } 10,5, i, t]<-\quad 0 \\
& \text { E1 [ } \quad 10,6, \mathrm{i}, \mathrm{t}]<-\quad 0 \\
& \begin{array}{llll}
\text { E1 } & {\left[\begin{array}{lll}
10 & 7, i, t
\end{array}\right]<-} & 0 \\
\text { E1 } & {[0} & 8, i, t]<- & 0
\end{array} \\
& \text { E1 [ } 10, \quad 9, i, t]<-\quad 2 *(1-a l p h a[i, t+1]) * a l p h a[i, t+1] \\
& \text { E1 [ } 10,10, i, t]<-\quad 1-(2 *(1-a l p h a[i, t+1]) * a l p h a[i, t+1])-(a l p h a[i, t+1]) \sim 2 \\
& \text { E1 [ } 10 \text {, 11,i,t]<- (alpha[i,t+1])~2 } \\
& \text { E1 }[10,12, i, t]<-\quad 0
\end{aligned}
$$

> \# for recapture probability
> E2 [ 1 , 1 ,i,t]<- $1-p$

| E2 | [ | 1 | , | 2 | ,i,t]<- |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| E2 | [ | 1 | , | 3 | ,i,t]<- |  |
| E2 | [ | 1 | , | 4 | ,i,t]<- |  |
| E2 | [ | 1 | , | 5 | ,i,t]<- |  |
| E2 | [ | 1 | , | 6 | ,i,t]<- |  |
| E2 | [ | 1 | , | 7 | ,i,t]<- |  |
| E2 | [ | 1 | , | 8 | ,i,t]<- |  |
| E2 | [ | 1 | , | 9 | ,i,t]<- | 0 |
| E2 | [ | 1 | , |  | i, t]<- | 0 |
| E2 | [ | 1 | , |  | i, t]<- | 0 |
| E2 | [ | 1 | , |  | i, t]<- | 0 |
| E2 | [ | 2 | , | 1 | , i, t]<- | 1 |
| E2 | [ | 2 | , | 2 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 3 | ,i,t]<- | p |
| E2 | [ | 2 | , | 4 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 5 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 6 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 7 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 8 | ,i,t]<- | 0 |
| E2 | [ | 2 | , | 9 | ,i,t]<- | 0 |
| E2 | [ | 2 | , |  | i,t]<- | 0 |
| E2 | [ | 2 | , |  | i, t]<- | 0 |
| E2 | [ | 2 | , |  | i, t]<- | 0 |
| E2 | [ | 3 | , | 1 | ,i,t]<- | 1 |
| E2 | [ | 3 | , | 2 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 3 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 4 | ,i,t]<- | p |
| E2 | [ | 3 | , | 5 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 6 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 7 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 8 | ,i,t]<- | 0 |
| E2 | [ | 3 | , | 9 | ,i,t]<- | 0 |
| E2 | [ | 3 | , |  | i, t]<- | 0 |
| E2 | [ | 3 | , |  | i, t]<- | 0 |
| E2 | [ | 3 | , |  | i, t]<- | 0 |
| E2 | [ | 4 | , | 1 | ,i,t]<- | 1 |
| E2 | [ | 4 | , | 2 | ,i,t]<- | 0 |
| E2 | [ | 4 | , | 3 | ,i,t]<- | 0 |
| E2 | [ | 4 | , | 4 | ,i,t]<- | 0 |
| E2 | [ | 4 | , | 5 | ,i,t]<- |  |
| E2 | [ | 4 | , | 6 | ,i,t]<- |  |
| E2 | [ | 4 | , | 7 | ,i,t]<- |  |
| E2 | [ | 4 | , | 8 | ,i,t]<- |  |
| E2 | [ | 4 | , | 9 | ,i,t]<- |  |
| E2 | [ | 4 | , |  | i, t]<- | 0 |
| E2 | [ | 4 | , |  | i,t]<- | 0 |
| E2 | [ | 4 | , |  | i,t]<- | 0 |
| E2 | [ | 5 | , |  | , t]<- | 1 |
| E2 | [ | 5 |  |  | , t]<- | 0 |

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| E2 | [ | 5 | , | 3,i,t]<- | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| E2 | [ | 5 | , | 4,i,t]<- | 0 |
| E2 | [ | 5 |  | 5,i,t]<- | 0 |
| E2 | [ | 5 | , | 6,i,t]<- | p |
| E2 | [ | 5 | , | 7,i,t]<- | 0 |
| E2 | [ | 5 | , | 8,i,t]<- | 0 |
| E2 | [ | 5 | , | 9,i,t]<- | 0 |
| E2 | [ | 5 | , | 10,i, t]<- | 0 |
| E2 | [ | 5 | , | 11,i,t]<- | 0 |
| E2 | [ | 5 | , | 12,i,t]<- | 0 |
| E2 | [ | 6 | , | 1 , i, t] | $1-p$ |
| E2 | [ | 6 | , | 2 ,i,t] | 0 |
| E2 | [ | 6 | , | 3 , i, t] | 0 |
| E2 | [ | 6 | , | 4 , i, t] | 0 |
| E2 | [ | 6 | , | 5 , i, t] | 0 |
| E2 | [ | 6 | , | 6 ,i,t] | 0 |
| E2 | [ | 6 | , | 7 ,i,t] | p |
| E2 | [ | 6 | , | 8 ,i,t] | 0 |
| E2 | [ | 6 | , | 9 , i, t] | 0 |
| E2 | [ | 6 | , | 10,i,t]<- | 0 |
| E2 | [ | 6 | , | 11,i,t]<- | 0 |
| E2 | [ | 6 | , | 12,i,t]<- | 0 |
| E2 | [ | 7 | , | 1 , i, t] | $1-\mathrm{p}$ |
| E2 | [ | 7 | , | 2 , i, t] | 0 |
| E2 | [ | 7 | , | 3 , i, t] | 0 |
| E2 | [ | 7 | , | 4 , i, t] | 0 |
| E2 | [ | 7 | , | 5 , i, t] | 0 |
| E2 | [ | 7 | , | 6 , i, t] | 0 |
| E2 | [ | 7 |  | 7 , i, t] | 0 |
| E2 | [ | 7 | , | 8 , i, t] | p |
| E2 | [ | 7 |  | 9 , i, t] | 0 |
| E2 | [ | 7 | , | 10,i,t]<- | 0 |
| E2 | [ | 7 | , | 11,i,t]<- | 0 |
| E2 | [ | 7 | , | 12,i,t]<- | 0 |
| E2 | [ | 8 | , | 1 , i, t] | $1-\mathrm{p}$ |
| E2 | [ | 8 |  | 2 ,i,t] | 0 |
| E2 | [ | 8 |  | 3 , i, t] |  |
| E2 | [ | 8 |  | 4 , i, t] |  |
| E2 | [ | 8 |  | 5 , i, t] |  |
| E2 | [ | 8 |  | 6 , i, t] |  |
| E2 | [ | 8 |  | 7 , i, t] |  |
| E2 | [ | 8 |  | 8 , i, t] | 0 |
| E2 | [ | 8 | , | 9 , i, t] |  |
| E2 | [ | 8 | , | 10,i,t]<- | 0 |
| E2 | [ | 8 | , | 11,i,t]<- | 0 |
| E2 | [ | 8 | , | 12,i,t]<- | 0 |
| E2 | [ | 9 |  | 1 , i, t] | 1-p |
| E2 | [ | 9 |  | 2 ,i,t] | 0 |
| E2 | [ | 9 |  | 3 , i, t] | 0 |

$$
\begin{aligned}
& \text { E2 }[10,1, i, t]<-\quad 1-p \\
& \text { E2 [ } 10,2, i, t]<-\quad 0 \\
& \text { E2 }[10,3, i, t]<-\quad 0 \\
& \text { E2 }[10,4, i, t]<-\quad 0 \\
& \text { E2 }[10, \quad 5, i, t]<-\quad 0 \\
& \text { E2 [ } 10,6, i, t]<-\quad 0
\end{aligned}
$$

$$
\begin{aligned}
& \text { E2 } \quad[\quad 10, \quad 9, i, t]<-\quad 0 \\
& \text { E2 [ } 10, \quad 10, \mathrm{i}, \mathrm{t}]<-\quad 0 \\
& \begin{array}{llll}
\text { E2 } & {\left[\begin{array}{ll}
{[10,} & 11, i, t]<- \\
\text { E2 } & {\left[\begin{array}{l}
10
\end{array} \quad 12, i, t\right]<-} \\
10
\end{array}\right.}
\end{array} \\
& \text { E2 } \quad[\quad 11,1 \quad, i, t]<-1-p \\
& \text { E2 }[11,2, i, t]<-0 \\
& \text { E2 }[11,3, i, t]<-0 \\
& \text { E2 }[11,4, i, t]<-0 \\
& \begin{array}{lllll}
\text { E2 } \\
\text { E2 } & {\left[\begin{array}{llll}
{[11} & , & 5 & , i, t]<- \\
{[11} & , & 6 & , i, t]<- \\
0
\end{array}\right.}
\end{array} \\
& \text { E2 [ } 11,7, i, t]<-0 \\
& \text { E2 } \quad\left[\begin{array}{llll}
11 & 8 & , i, t]<-0 \\
\text { E2 }
\end{array}\right. \\
& \text { E2 } \quad[\quad 11, \quad 10, \mathrm{i}, \mathrm{t}]<-\quad 0 \\
& \begin{array}{llll}
\text { E2 } \\
\text { E2 }
\end{array} \quad\left[\begin{array}{llll}
{[ } & 11 & , & 11, i, t]<- \\
11 & , & 12, i, t]<- & p
\end{array}\right.
\end{aligned}
$$

        \# Matrix product for offspring independence and recapture
        \(E[1: 12,1: 12, i, t]<-E 1[1: 12,1: 12, i, t] \% * \%\) E2[1:12,1:12,i,t]
    \}
    \}

```
## LIKELIHOOD
for (i in 1:N) # for each individual
{
    # The estimated probabilities of initial states S0 are the proportions in each state at first captu
    alive[i,First[i]] ~ dcat(S0[1:12])
    mydata[i,First[i]] ~ dcat(E0[alive[i,First[i]],1:12])
    for (j in (First[i]+1):Years)
    {
            ## STATE EQUATIONS ##
        # draw S(t) given S(t-1)
        alive[i,j] ~ dcat(S[alive[i,j-1],1:12])
        ## OBSERVATION EQUATIONS ##
        # draw events E(t) given states S(t)
        mydata[i,j] ~ dcat(E[alive[i,j],1:12,i,j-1])
    }
}
## PRIORS
# capture probability
p ~ dunif (0,1)
# juveniles, subadults and adult survival
#for(i in 1:2){phi[i] ~ dunif(0,1)}
phi[1] ~ dunif(0,1)
# initial states
for (i in 1:10){ log(prop[i]) <- theta[i]
theta[i] ~ dnorm(0,1)}
# offspring survival
# litter survival n=2 offspring
102 <- 1 -(1- s[2]~2 -2*s[2]*(1-s[2]))
112 <- 1- (1- s[4]^2 -2*s[4]*(1-s[4]))
# indiviual offspring survival
#for(i in 1:4){s[i] ~ dunif(0,1)}
for(i in 1:2){s[i]~ dunif(0,1)}
    # Set constraints
    for(u in 1:2){ X[u] ~ dunif(0,1)} # with X ~ U[0,1] then (a + ( b - a ) * X)
    #so that s[1] < s[3] <phi[1] for litter of 1
    s[3] <- s[1] + (phi[1] - s[1]) * X[1]
    # and s[2] < s[4] < phi[1] for litters of 2
    s[4] <- s[2] + (phi[1] - s[2]) * X[2]
# Breeding probability
kappa ~ dunif(0,1)
```

```
    for(i in 1:3){beta[i]~ dunif(0,1)}
    # Litter size probability
    for(i in 1:2){gamma[i] ~ dunif(0,1)}
} # end model
    ")
```

This model differs from the model used for the simulations in just a few points. It assumes breeding probability and litter size probability does not vary between successful breeders (states AS1 and AS2) and female without dependent offspring (state A) by setting beta ${ }_{3}=$ beta $_{4}$ (in the code beta[3]) and $g a m m a_{3}=g a m m a_{4}$ (in the code gamma[2]) . It also assumes that litter size probability is the same among failed breeders (loss of cub versus yearling litter), by setting gamma $_{1}=$ gamma $_{2}$ (in the code gamma[1]).

Run the jags model and save the results:

```
# Call JAGS from R
out <- jags(data=mydatax,inits=inits, parameters.to.save=params,
    model.file = 'Multieventmodel_FitresidentBeardata.txt',n.chains=2,n.iter=20000,n.burnin=900
save(out,file='noage_lb_phip.RData')
```


## Analyse the results

Load useful packages:
library (jagsUI)
library(MCMCvis)
Load model results and print a summary :
load (file='Fit_beardata.RData')
MCMCsummary (out, round=2)

| \#\# | mean | sd | $2.5 \%$ | $50 \%$ | $97.5 \%$ | Rhat | n.eff |
| :--- | ---: | ---: | :--- | :--- | :--- | :--- | ---: |
| \#\# phi | 0.93 | 0.01 | 0.92 | 0.93 | 0.95 | 1.00 | 2027 |
| \#\# s [1] | 0.54 | 0.10 | 0.34 | 0.54 | 0.72 | 1.00 | 4400 |
| \#\# s [2] | 0.51 | 0.05 | 0.41 | 0.51 | 0.62 | 1.00 | 4400 |
| \#\# s [3] | 0.67 | 0.11 | 0.46 | 0.68 | 0.87 | 1.00 | 1458 |
| \#\# s [4] | 0.80 | 0.09 | 0.59 | 0.82 | 0.93 | 1.01 | 422 |
| \#\# l02 | 0.76 | 0.05 | 0.65 | 0.76 | 0.85 | 1.00 | 4400 |
| \#\# l12 | 0.95 | 0.04 | 0.83 | 0.97 | 0.99 | 1.01 | 331 |
| \#\# kappa | 0.12 | 0.08 | 0.02 | 0.11 | 0.30 | 1.00 | 4400 |
| \#\# beta [1] | 0.09 | 0.06 | 0.01 | 0.07 | 0.23 | 1.00 | 2978 |
| \#\# beta[2] | 0.58 | 0.21 | 0.19 | 0.57 | 0.96 | 1.00 | 4400 |
| \#\# beta[3] | 0.52 | 0.04 | 0.43 | 0.52 | 0.61 | 1.00 | 1763 |
| \#\# gamma [1] | 0.35 | 0.17 | 0.07 | 0.34 | 0.71 | 1.00 | 2652 |
| \#\# gamma [2] | 0.40 | 0.05 | 0.30 | 0.40 | 0.51 | 1.00 | 4400 |
| \#\# p | 0.25 | 0.01 | 0.22 | 0.25 | 0.27 | 1.01 | 182 |
| \#\# prop [1] | 0.56 | 0.16 | 0.30 | 0.54 | 0.92 | 1.00 | 4400 |
| \#\# prop[2] | 0.46 | 0.14 | 0.24 | 0.44 | 0.79 | 1.00 | 4400 |
| \#\# prop [3] | 0.66 | 0.18 | 0.37 | 0.63 | 1.08 | 1.00 | 4400 |
| \#\# prop[4] | 0.42 | 0.14 | 0.21 | 0.40 | 0.74 | 1.00 | 4400 |
| \#\# prop[5] | 0.80 | 0.21 | 0.45 | 0.77 | 1.28 | 1.00 | 4400 |


| \#\# prop [6] | 0.76 | 0.20 | 0.43 | 0.74 | 1.22 | 1.00 | 4400 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| \#\# prop [7] | 0.46 | 0.15 | 0.24 | 0.44 | 0.80 | 1.00 | 4400 |
| \#\# prop [8] | 0.20 | 0.08 | 0.08 | 0.19 | 0.40 | 1.00 | 4400 |
| \#\# prop[9] | 0.20 | 0.08 | 0.08 | 0.19 | 0.40 | 1.00 | 4400 |
| \#\# prop[10] | 0.09 | 0.05 | 0.02 | 0.08 | 0.22 | 1.00 | 4400 |
| \#\# deviance | 1611.02 | 25.81 | 1563.30 | 1609.45 | 1664.85 | 1.02 | 133 |

Check mixing of the chains and posterior distributions:
MCMCtrace(out,params = c('phi','s','l02','l12','kappa','beta','gamma','p'),pdf=FALSE)



Trace - s[1]






Trace - s[4]


Trace - 102


Trace - I12







Density - s[4]



Parameter estimate
Density - 112



Plot a summary of the posterior distribution for each model parameter: MCMCplot (out ,

```
params = c('phi','s','l02','l12','kappa','beta','gamma','p'),
    xlim = c(0, 1),
    xlab = 'Value',
    main = 'Estimates',
    labels = c(expression(phi),expression(s[1]),expression(s[2]),expression(s[3]),
        expression(s[4]), expression(l[02]),expression(l[12]),expression(kappa),
            expression(beta[1]), expression(beta[2]), expression(beta[3]),
```

expression(gamma[1]), expression(gamma[3]), expression(p)),
col = 'black',
sz_labels = 1.5,
sz_med = 1.5,
sz_thick = 4,
sz_thin = 2,
sz_ax = 4,
sz_main_txt = 2)

Estimates


Dots represent posterior medians, thick lines represent 50 percent credible intervals while thin lines represent 95 percent credible intervals.

Calculate the probabilities of successfully raising 1 or 2 or 0 offspring to independence over a three-year period for an adult female without dependent offspring at the start of the period:

```
prx1 <- (out$sims.list$phi)^3 * out$sims.list$beta[,3] *
    (
        out$sims.list$gamma[,2] * out$sims.list$s[,1] * out$sims.list$s[,3]
        +
(1- out$sims.list$gamma[,2]) *
    (2 * out$sims.list$s[,2] * (1-out$sims.list$s[,2]) * out$sims.list$s[,3]
+ (out$sims.list$s[,2])^2 + 2 * out$sims.list$s[,4] * (1 -out$sims.list$s[,4])
)
)
prx2 <- (out$sims.list$phi)^3 * out$sims.list$beta[,3] *
    (1- out$sims.list$gamma[,2]) * (out$sims.list$s[,2])^2 * (out$sims.list$s[,4])^2
```

```
prx0 <- 1 -prx1 -prx2
```

Make a table with the median value and $95 \%$ credible interval for the probabilities of successfully raising 1 or 2 or 0 offspring to independence over a three-year period for an adult female without dependent offspring at the start of the period:

```
# Summary of results
tabres <- matrix(NA,3,3)
tabres[1,]<-quantile(prx0,probs=c(0.025,0.5,0.975))
tabres[2,]<-quantile(prx1,probs=c(0.025,0.5,0.975))
tabres[3,]<-quantile(prx2,probs=c(0.025,0.5,0.975))
rownames(tabres)=c("Pr (X=0)", "Pr (X=1)", "Pr(X=2)")
colnames(tabres)=c("Q 2.5%","Median","Q 97.5%")
round(tabres,2)
## Q 2.5% Median Q 97.5%
## Pr(X=0) 0.57 0.67 0.76
## Pr(X=1) 0.20 0.29 0.38
## Pr(X=2) 0.02 0.04 0.07
```


## References

Amstrup, S. C., \& Durner, G. M. (1995). Survival rates of radio-collared female polar bears and their dependent young. Canadian Journal of Zoology, 73, 1312-1322. doi:10.1139/z95-155

Hornik, K., Leisch, F., \& Zeileis, A. (2003). JAGS: A program for analysis of Bayesian graphical models using Gibbs sampling. In Proceedings of DSC (Vol. 2, No. 1).

Kellner, K. (2015). jagsUI: a wrapper around rjags to streamline JAGS analyses. R package version, 1(1).

Modeling the demography of species providing extended parental care:<br>A capture-recapture multievent model with a case study on Polar Bears (Ursus maritimus)<br>Sarah Cubaynes ${ }^{1}$, Jon Aars ${ }^{2}$, Nigel G. Yoccoz ${ }^{3}$, Roger Pradel ${ }^{1}$, Øystein Wiig ${ }^{4}$, Rolf A Ims $^{3}$ and Olivier Gimenez ${ }^{1}$<br>${ }^{1}$ CEFE, Univ Montpellier, CNRS, EPHE-PSL University, IRD, Univ Paul Valéry<br>Montpellier 3, Montpellier, France<br>${ }^{2}$ Norwegian Polar Institute, FRAM Centre, Tromsø, Norway<br>${ }^{3}$ UiT The Arctic University of Norway, Department of Arctic and Marine Biology, Tromsø, Norway<br>${ }^{4}$ Natural History Museum, University of Oslo, Norway


#### Abstract

1. In species providing extended parental care, one or both parents care for altricial young over a period including more than one breeding season. We expect large parental investment and long-term dependency within family units to cause high variability in life trajectories among individuals with complex consequences at the population level. So far, models for estimating demographic parameters in free-ranging animal populations mostly ignore extended parental care, thereby limiting our understanding of its consequences on parents and offspring life histories. 2. We designed a capture-recapture multi-event model for studying the demography of species providing extended parental care. It handles statistical multiple-year dependency among individual demographic parameters grouped within family units, variable litter size, and uncertainty on the timing at offspring independence. It allows for thete evaluate-evaluation of


trade-offs among demographic parameters, the influence of past reproductive history on the caring parent's survival status, breeding probability and litter size probability, while accounting for imperfect detection of family units. We assess the model performances using simulated data, and illustrate its use with a long-term dataset collected on the Svalbard polar bears (Ursus maritimus).
3. Our model performed well in terms of bias and mean square error and in estimating demographic parameters in all simulated scenarios, both when offspring departure probability from the family unit occurred at a constant rate or varied during the field season depending on the date of capture. For the polar bear case study, we provide estimates of adult and dependent offspring survival rates, breeding probability and litter size probability. Results showed that the outcome of the previous reproduction influenced breeding probability.
4. Overall, our results show the importance of accounting for i) the multiple-year statistical dependency within family units, ii) uncertainty on the timing at offspring independence, and iii) past reproductive history of the caring parent. If ignored, estimates obtained for breeding probability, litter size, and survival can be biased. This is of interest in terms of conservation because species providing extended parental care are often long-living mammals vulnerable or threatened with extinction.

Key-words: apex predator, arctic ecosystem, Bayesian modeling, capture-recapture, dependency among individuals, family structure, parental care, state uncertainty, timing at independence.

## INTRODUCTION

Parental care includes any pre-natal and post-natal allocation, such as feeding and protecting the young, which benefits the offspring development and survival chances, thereby enhancing
the parent's reproductive success (Trivers 1972). Altricial mammals having offspring that need to learn complex skills to ensure survival beyond independence, such as hunting, orientation, or nest building, show extended parental care (hereafter EPC; Clutton-Brock 1991). It is defined as a prolonged period, i.e. lasting more than one breeding season, over which one or both parents care for one or several dependent young. This period typically lasts for several years and can extend until lifelong maternal care in primates (Van Noordwijk 2012). For the offspring, the quality and quantity of care received can have long-lasting effects on future survival (e.g. Pavard and Branger 2012), social status (e.g. Shenk and Scelza 2012) and reproduction (Royle et al. 2012). For the parent, investment in one offspring can compromise its own condition or survival and/or its ability to invest in other offspring (siblings or future offspring) (Williams 1966, Stearns 1992). It can indeed take several years during which a parent caring for its offspring will not be available to reproduce, sometimes not until the offspring have reached independence, e.g. on average 2.5 years for female polar bears (Ramsay and Stirling 1988), 3.5 to 6 years for female African elephants (Lee and Moss 1986), and 9.3 years for female Sumatran orangutans (Wich et al. 2004). The fitness costs of losing one offspring, in terms of lost investment and skipped breeding opportunities, are particularly high if death occurs near independence. We therefore expect EPC, through large parental investment and multiple-year dependency among individuals within family units, to cause high variability in life trajectories among individuals and family groups, in interbirth intervals depending on offspring's fate, and consequently on lifetime reproductive success for the caring parent (Clutton-Brock 1991).

Capture-recapture (CR) models allow studying species with complex demography in the wild, e.g. by considering 'breeder' and 'non-breeder' reproductive states to estimate breeding probabilities and status-specific demographic parameters while accounting for imperfect detectability (e.g., Lebreton et al. 2009). One can distinguish between successful and
failed breeding events (e.g., Lagrange et al. 2017) and include varying litter or clutch size (e.g., Doligez et al. 2002) and memory effects (Cole et al. 2014), to investigate the costs of reproduction on survival and future reproduction for species providing short-term parental care, i.e. when offspring reach independence before the next breeding season (e.g., Yoccoz et al. 2002). Indeed, most CR models rely on the assumption of independence among individual CR histories (Lebreton et al. 2009).

In the case of species providing EPC, one challenge stems from the multiple-year dependency among individual's life histories within parent-offspring units. Only few attempts have been made to tackle this issue when estimating demographic parameters, despite the fact that species providing EPC are often among long-living mammals vulnerable or threatened with extinction (e.g. polar bears, orangutans, elephants). Lunn et al. (2016) and Couet et al. (2019) proposed to model CR histories of family mother-offspring units (instead of individuals) which permits-to consider the multiple-year dependency of offspring survival upon mother survival status and-of female breeding probability upon offspring survival status for polar bears in Hudson Bay.--However, in this model, offspring survival after 9 months is assumed independent of mother survival. Lunn et al. (2016)'s model does therefore not handle multipleyear dependency of offspring survival upon mother survival status, typical ofin species providing EPC. In addition, because litter size is modeled separately, Lunn et al. (2016)'s model (also used in Regehr et al. (2018)) does not permit to explore potential trade-offs among offspring traits and parental phenotypic or demographic traits. Genet al. (2019) provided estimates of dolphin reproductive parameters corrected for state uncertainty but their model assumed a fixed age and timing at offspring independence.

Another challenge involves dealing with uncertain timing at offspring independence, when the offspring departs the caring parent(s) and becomes independent. When studying freeranging populations, this key life history event is rarely directly observed. When a mature
individual is observed without dependent offspring, it is often impossible to know if its offspring have died or already departed its natal group. As a result, estimates of demographic rates and trade-offs can be underestimated. Based on the analysis of mother-offspring units CR histories, Couet et al. (2019) provided estimates of dolphin reproductive parameters corrected for state uncertainty, but their model assumed a fixed age and timing at offspring independence. Lunn et al. (2016)'s model for polar bears in Hudson Bay (later used in Regehr et al. (2018)) included variable age at independence, but variability in the timing at offspring independence was not fully dealt with. Demographic rates were corrected by the average annual probability that independence occurred prior to sampling for all offspring, and offspring survival was assumed independent of litter size (Regehr et al. 2018). In most species, timing at offspring independence is variable and could depend on the offspring phenotypic traits (e.g. body size in brown bears, Dahle and Swenson 2003), on parental traits (e.g. parent-offspring conflict in kestrels, Vergara et al. 2010), social and mating system (e.g. helping behavior in humans, Kramer 2005), or other environmental determinants (e.g. food supply, Eldegard and Sonerud 2010). To our knowledge, no model is available to tackle both the issues of multiple-year dependency among individuals and variable timing at offspring independence. Because of these methodological challenges, the population-level consequences of EPC remain to be understood, especially in free-ranging animal populations.

Here, we develop a CR model specifically for species providing EPC. It is designed to handle multiple-years statistical dependency (until offspring independence) among individual demographic parameters by modeling CR histories grouped within family units. The model accounts for uncertain timing at offspring independence. In addition, our model allows for variability in the number of offspring born and recruited at each breeding event, variable offspring survival depending on number of siblings, and includes the influence of past reproductive history on the caring parent's current status. Finally, estimates of survival rates,
breeding probability and litter size probability are corrected for imperfect detection possibly depending upon family unit composition.

In what follows, we present the model, assess its performances using simulated data, and illustrate its use with a long-term dataset collected on the Svalbard polar bears. Female polar bears rely solely on stored fat reserves during pregnancy and the first three months of lactation, before feeding and protecting litters of one to three young, usually during two more years (Ramsay and Stirling 1988). They can lose more than $40 \%$ of body mass while fasting (Atkinson and Ramsay 1995). In many areas, climate change and related sea ice decline impact female bear condition and capacity to provide care for their young, with an associated decline in reproductive output (Derocher et al. 2004; Stirling and Derocher, 2012, Laidre et al. 2020). More insights into the species demography, such as the consequences of long-duration parental care on mother and offspring life histories, could help our understanding of polar bear population responses to environmental perturbations and extinction risks in future decades (Hunter et al., 2010; Regehr et al., 2016).

## METHODS

## 1. Capture-recapture model for species providing EPC

### 1.1 Principle

We develop a CR model in the multievent framework (Pradel 2005) that is also known as a hidden Markov modeling framework (Gimenez et al. 2012). The principle is to relate the field observations, called events, to the underlying demographic states of interest through the observation process. Uncertainty on state assignment due to variable timing at offspring independence is included in the observation process. In parallel, the state process describes the transition rates between states from one year to the next. The transition rates correspond here
to the demographic parameters corrected for imperfect detection and state uncertainty. Below we describe the general procedure to specify the model by defining the states and state-to-state transition process, then the events and observation process. However, for simplicity, the events and states are chosen to match the polar bear life cycle (i.e. females are captured in sSpring, alone or together with a litter of one or two dependent offspring; offspring gain independence in the year following their second birthday, and offspring cannot survive the loss of their mother before gaining independence). The resulting model assumptions and its applicability to other species are discussed below.

### 1.2 Specification of states and state process

One specificity of our model lies in the use of CR histories based on family groups instead of individuals, which permits to include the multiple-year dependency among the caring parent and dependent offspring' $\underline{s}$ demographic rates and life history traits. Below, we describe the specification of 24 unique states and 6 matrices needed to construct the model.

States correspond to the 'real' demographic states of the individuals composing the family. We consider 12 states $\mathrm{S}, S=\{J 2, J 3, S A 4, S A 5, A 01, A 02, A 11, A 12, A S 1, A S 2, A, D\}$, to represent the polar bear life cycle (defined in Table 1). In addition, we specify 13 intermediary states $\mathrm{S}^{\prime}, \mathrm{S}^{\prime}=\{\mathrm{J} 3, \mathrm{SA} 4, \mathrm{SA} 5, \mathrm{~A} 11, \mathrm{~A} 12, \mathrm{AS} 1, \mathrm{AS} 2, \mathrm{~A} 0-, \mathrm{A} 1-\mathrm{I} / \mathrm{AS} 1, \mathrm{I} / \mathrm{AS} 2, \mathrm{~A}, \mathrm{D}\}$, and 16 intermediary states $S^{\prime \prime}$, $S^{\prime \prime}=\{J 3, S A 4, S A 5, A 11, A 12, A S 1, A S 2, B / A 0-, N B / A 0-, B / A 1-, N B / A 1-$ , $\mathrm{B} / \mathrm{AS}, \mathrm{NB} / \mathrm{AS}, \mathrm{B} / \mathrm{A}, \mathrm{NB} / \mathrm{A}, \mathrm{D}\}$, leading to a total of 24 unique states (defined in Table 1). The specification of intermediary states is what permits to distinguish between failed and successful breeders in the transition matrix to consider the influence of past reproductive history on parameters (see below).

175 Table 1. Definition of the states and events used in the model to describe the polar bear life 176 cycle.

## TYPE CODE DEFINITION

STATES | J2 | 2 y.o. independent juvenile female |
| :---: | :--- |
| J3 | 3 y.o. independent juvenile female |
| SA4 | 4 y.o. independent subadult female |
| SA5 | 5 y.o. independent subadult female |
| A01 | mother with two-one dependent effspring cub of the year $\leq 1 y \theta$ |
| A02 | mother with ene-two dependent effspring cubs of the year $\leq 1 y e$ |

A11 mother with one dependent effspring-yearling tye
A12 mother with two dependent effspring-yearlings 1 yo
AS1 successful female breeder with one two-year old offspring reaching independence
AS2 successful female breeder with two two-year old offspring reaching independence
A adult female without dependent offspring
D dead state
A0- failed breeder, death of all offspring cubs of the year aged $<1$ yo
A1- failed breeder, death of all offspring yearlingsaged 1 yo
I/AS1 successful female breeder alone after departure of one independent offspring
I/AS2 successful female breeder alone after departure of two independent offspring
B/A0- breeder following loss of a cub of the year litter of $<1$ yo offspring
NB/A0- non breeder following loss of a cub of the year litter of $<1$ yo offspring
B/A1- breeder following loss of a yearling litter of 1 yo offspring
NB/A1- non breeder following loss of a yearling litter-of 1 yo offspring
B/AS breeder following successful reproduction
NB/AS non breeder following successful reproduction

decision, itself conditioned upon offspring survival, itself conditioned upon survival of the caring parent to deal with the statistical dependency existing among individuals within family units.

The $\Phi$ matrix (eq. 1) describes transitions from each state $S$ at time $t$ (rows) to each state S after the occurrence of the survival process for independent individuals (columns):

|  | J2 | J3 | SA4 | SA5 | A01 | A02 | A11 | A12 | AS1 | AS2 | A | D |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | $\varphi \phi_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi \phi_{1}$ |  |
| J3 | 0 | $\varphi \phi_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\varphi \phi_{2}$ |  |
| SA4 | 0 | 0 | $\varphi \phi_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\underline{\varphi} \phi_{3}$ |  |
| SA5 | 0 | 0 | 0 | $\varphi \phi_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $1-\underline{\varphi} \phi_{4}$ |  |
| A01 | 0 | 0 | 0 | 0 | $\varphi \phi_{5}$ | 0 | 0 | 0 | 0 | 0 | 0 | 1- $\varphi \phi_{5}$ |  |
| A02 | 0 | 0 | 0 | 0 | 0 | $\varphi \phi_{6}$ | 0 | 0 | 0 | 0 | 0 | $1-\varphi \phi_{6}$ | (eq. 1) |
| A11 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi \phi_{7}$ | 0 | 0 | 0 | 0 | $1-\varphi \phi_{7}$ |  |
| A12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi \phi_{8}$ | 0 | 0 | 0 | $1-\varphi \phi_{8}$ |  |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\underline{\varphi}_{9}$ ¢ $_{9}$ | 0 | 0 | 1- $\varphi \phi_{9}$ |  |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\phi \varphi_{10}$ | 0 | 1- $\varphi \phi_{10}$ |  |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\varphi \phi_{11}$ | 1- $\varphi \phi_{11}$ |  |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |  |

In the $\Phi$ matrix, $\varphi \phi_{1}, \ldots, \varphi \phi_{11}$ correspond to survival of immature independent (juveniles and subadults) and adult female bears.

The $\Psi_{1}$ matrix (eq.2) describes transitions from states S after the occurrence of the survival process for independent individuals (rows) to states S' after the occurrence of the offspring survival process (columns):

|  | J3 | SA4 | SA5 | A11 | A12 | AS1 | AS2 | AO- | A1- | I/AS1 | I/AS2 | A | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| J3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA4 | 0 | 0 | $\begin{aligned} & \text { 1- } \\ & \underline{\kappa} \kappa \end{aligned}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\kappa$ | 0 |
| SA5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| A01 | 0 | 0 | 0 | $s_{1}$ | 0 | 0 | 0 | $1-s_{1}$ | 0 | 0 | 0 | 0 | 0 (eq.2) |
| (eA02 | 0 | 0 | 0 | $2 \cdot s_{2} \cdot\left(1-s_{2}\right)$ | $s_{2}{ }^{2}$ | 0 | 0 | $1-s_{2}{ }^{2}-2 \cdot s_{2} \cdot\left(1-s_{2}\right)$ | 0 | 0 | 0 | 0 | 0 |
| A11 | 0 | 0 | 0 | 0 | 0 | $s_{3}$ | 0 | 0 | $1-s_{3}$ | 0 | 0 | 0 | 0 |
| A12 | 0 | 0 | 0 | 0 | 0 | $2 \cdot s_{4} \cdot\left(1-s_{4}\right)$ | $s_{4}{ }^{2}$ | 0 | $1-s_{4}{ }^{2}-2 \cdot s_{4} \cdot\left(1-s_{4}\right)$ | 0 | 0 | 0 | 0 |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |

In the $\Psi_{1}$ matrix, $\kappa$ is the probability of first reproduction at age $5, s$ is dependent offspring survival conditioned upon mother survival ( $s_{1}$ for singleton cub, and $s_{2}$ for singleton cub resp. for singleton yearling; $s_{3}$ for twin litter's individual cub, and $s_{4}$ for twin litter's or twin litter's eub individual resp-yearling). Litter survival rates can be obtained from individual offspring survival rates (for singleton litters $l_{01}=s_{1}$ and $l_{11}=s_{3}$ for cub resp-and yearling respectively, and for twin litters $l_{02}=1-\left(1-s_{2}{ }^{2}-2 \cdot s_{2} \cdot\left(1-s_{2}\right)\right)$ and $l_{12}=1-\left(1-s_{4}{ }^{2}-2 \cdot s_{4}\right.$. $\left.\left(1-s_{4}\right)\right)$ for cubs resp-and yearlings respectively).

The $\Psi_{2}$ matrix (eq.3) describes transitions from states $S^{\prime}$ after occurrence of the survival processes (rows) to states $S$ ' ' depending on breeding decision (columns):

|  | J3 | SA4 | SA5 | A11 | A12 | AS1 | AS2 | $\mathrm{B} / \mathrm{AO}-$ | $\mathrm{NB} / \mathrm{AO}-$ | $\mathrm{B} / \mathrm{A} 1-$ | $\mathrm{NB} / \mathrm{A} 1-$ | $\mathrm{B} / \mathrm{AS} 1$ | $\mathrm{~B} / \mathrm{AS} 2$ | $\mathrm{~B} / \mathrm{A}$ | $\mathrm{NB} / \mathrm{A}$ | D |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J3 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| SA4 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| SA5 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A11 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A12 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A21 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A22 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (eq.3) |
| A0- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{1}$ | $1-\beta_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A1- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{2}$ | $1-\beta_{2}$ | 0 | 0 | 0 | 0 | 0 |  |
| I/AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{3}$ | $1-\beta_{3}$ | 0 | 0 | 0 |  |
| I/AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{3}$ | $1-\beta_{3}$ | 0 | 0 | 0 |  |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $\beta_{4}$ | $1-\beta_{4}$ | 0 |  |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |  |

Parameter $\beta$ is breeding probability conditioned upon mother and offspring's survival status ( $\beta_{1}$ following loss of a cub litter, and $\beta_{2}$ following the loss a cub litter resp-loss of a yearling litter-for failed female breeders, $\beta_{3}$ for successful breeder, $\beta_{4}$ for female without dependent offspring at the beginning of the year).

The $\Psi_{3}$ matrix (eq. 4) describes transitions from states $S^{\prime \prime}$ after occurrence of the survival processes and breeding decision (rows) to states S at $\mathrm{t}+1$ after determination of litter size for breeders (columns):

|  | J2 | 13 | SA4 | SA5 | A01 | A02 | A11 | A12 | AS1 | AS2 | A | D |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| SA4 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| SA5 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| A11 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |  |
| A12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |  |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |  |
| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | (eq.4) |
| B/AO- | 0 | 0 | 0 | 0 | $\gamma_{1}$ | $1-\gamma_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |
| NB/AO- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |  |
| B/A1- | 0 | 0 | 0 | 0 | $\gamma_{2}$ | $1-\gamma_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |
| NB/A1- | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |  |
| B/AS1 | 0 | 0 | 0 | 0 | $\gamma_{3}$ | $1-\gamma_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |
| B/AS2 | 0 | 0 | 0 | 0 | $\gamma_{3}$ | $1-\gamma_{3}$ | 0 | 0 | 0 | 0 | 1 | 0 |  |
| B/A | 0 | 0 | 0 | 0 | $\gamma_{4}$ | $1-\gamma_{4}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |
| NB/A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |  |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |  |

Parameter $\gamma$ is the probability of producing a singleton litter conditioned upon mother's and offspring's survival status and upon breeding decision ( $\gamma_{1}$ following the loss a cub litter, and $\gamma_{2}$ following the loss a cub litter resp-loss of a yearling litter, $\gamma_{3}$ for successful breeder, $\gamma_{4}$ for female without dependent offspring at the beginning of the year).

By modifying the constraints on parameters (i.e. setting them equal or different among states), the model can be used to investigate: i) the cost of reproduction on parent's survival (by comparing the $\varphi \phi-$ s in matrix $\Phi)$, ii) the influence of litter size on individual offspring survival (by comparing $s_{1}$ to $s_{2}$, and $s_{3}$ to $s_{4}$ in matrix $\Psi_{1}$ ) and on litter survival (by comparing $1_{01}$ to $1_{02}$ and $l_{11}$ to $l_{12}$ ), iv) the influence of past reproductive history on breeding probability (by comparing the $\beta \smile$ s among them-in matrix $\Psi_{2}$ ), and on litter size probability (by comparing the $\gamma-$ s among them-in matrix $\Psi_{3}$ ).

### 1.3 Specification of events and observation process

The events correspond to the observation or non-observation of family units in the field at each sampling occasion. Each event is coded depending on the number and age of the individuals composing the family. Here, we consider 12 possible events, $\Omega=\{1,2,3,4,5,6,7,8,9,10,11,12\}$ to describe field observations for polar bears family groups (defined in Table 1).

In a multievent model, one specific event may relate to several possible states. Due to variable timing at offspring independence, a female successful breeder (state 'AS1' or 'AS2') can be captured together with 1 or 2 two-year old dependent offspring (event ' 9 ' or ' 10 ') or without (event ' 11 ') its two-year old offspring or not captured (event ' 12 ') depending on i) whether the offspring has already departed from its mother at the time of capture and ii) on capture probability. To include uncertainty on state assignment due to variable timing at offspring independence, we decompose the observation process into two event matrices, $E_{1}$ and $E_{2}$, modeling respectively departure probability $(\alpha)$ and capture probability $(p)$.

The $E_{1}$ matrix (eq. 5), relates the states $S$ to the possible observations at the time of capture, $O=\{1,2,3,4,5,6,7,8,9,10,11,12\}$ (same code as the events, see Table 1), through the departure probability, denoted $\alpha$.

|  | '1 | '2 | '3 | '4 | '5 | '6 | '7 | '8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| J3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| SA4 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| SA5 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| $\begin{gathered} \text { AO } \\ 1 \end{gathered}$ | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| $\begin{gathered} \text { AO } \\ 2 \end{gathered}$ | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| A1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| $\begin{gathered} \text { A1 } \\ 2 \end{gathered}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| AS1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |


| $\prime 9 '$ | $' 10 '$ |
| :---: | :---: |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| $1-\underline{\alpha}_{i, d} a$ | 0 |


| '11' | '0'12 |
| :---: | :---: |
|  | 1 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| 0 | 0 |
| $\underline{\alpha}_{i, d}{ }^{\text {a }}$ | 0 |


| AS2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $2 \cdot \alpha_{i, d} \cdot\left(1-\alpha_{i, d}\right)$ | $1-2 \cdot \alpha_{i, d} \cdot\left(1-\alpha_{i, d}\right)-\alpha_{i, d}{ }^{2}$ | $\alpha_{i, d}{ }^{2}$ | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Here, $\alpha_{i, j \underline{d}}$ is the departure probability of a two-year old individual offspring belonging to family unit i on its date of capture d . The relationship between date of capture and departure probability is species-specific and either be-assessed from prior knowledge on the species' biology or field data (see Appendix 2). Here we assume that siblings' timing at independence can, but does not have to, occur independently (if both offspring can only depart the family on the same date, the transition from state 'AS2' to event ' 9 ' should be set to 0 ).

The second event matrix, $E_{2}$, (eq. 6) relates all possible observations at the time of capture O to the events, $\Omega$, actually observed in the field through the state-dependent capture probability, denoted $\mathrm{p}_{\mathrm{s}}$.

|  | $1^{\prime}$ | $2^{\prime}$ | $3^{\prime}$ | $4^{\prime}$ | $5^{\prime}$ | $6^{\prime}$ | $7^{\prime}$ | $8^{\prime}$ | $9^{\prime}$ |  | $1^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- | :--- |
| $1^{\prime}$ | $p_{1}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| $2^{\prime}$ | 0 | $p_{2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| $3^{\prime}$ | 0 | 0 | $p_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| $4^{\prime}$ | 0 | 0 | 0 | $p_{4}$ | 0 | 0 | 0 | 0 | 0 |  |  |
| $5^{\prime}$ | 0 | 0 | 0 | 0 | $p_{5}$ | 0 | 0 | 0 | 0 |  |  |
| $6^{\prime}$ | 0 | 0 | 0 | 0 | 0 | $p_{6}$ | 0 | 0 | 0 |  |  |
| $7^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | $p_{7}$ | 0 | 0 |  |  |
| $8^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $p_{8}$ |  | 0 |  |
| $9^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $p_{9}$ |  |  |
| $1^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $p_{10}$ |  |
| $10^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |
| $0^{\prime}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  |


|  | 1' | $\theta^{\prime} \underline{\underline{12}}$ |
| :---: | :---: | :---: |
| 0 | 0 | $1-p_{1}$ |
| 0 | 0 | $1-p_{2}$ |
| 0 | 0 | $1-p_{3}$ |
| 0 | 0 | $1-p_{4}$ |
| 0 | 0 | $1-p_{5}$ |
| 0 | 0 | $1-p_{6}$ |
| 0 | 0 | $1-p_{7}$ |
| 0 | 0 | $1-p_{8}$ |
| 0 | 0 | $1-p_{9}$ |
|  | 0 | $1-p_{10}$ |
| 0 | $p_{11}$ | $1-p_{11}$ |
| 0 | 0 | 1 |

The composite event matrix, E, which relates the events to the states, is obtained as the matrix product of these two matrices $E=E_{1} \cdot E_{2}$. Because the model is conditioned upon first capture, the initial event vector, $e_{0}$, takes the value of 1 for all events (except of 0 for the event

### 1.4 Applicability to other species

The model described above matches the Svalbard polar bear life cycle. The model therefore assumes that care is provided by the mother only, to one or two offspring (we modelled triplets as twins because there were just 8 litters of triplets in the dataignored triplets present at a low probability in polar bears), for a duration of two years maximum. Offspring under age 2 cannot survive if the mother dies. A mother caring for offspring cannot mate and produce a second litter. Independent males (that have already departed from the family unit) are not included in the model.

To apply the model to other species, one should modify the number of events and states to match the species life cycle (depending on age at sexual maturity, number of care providers, maximum litter size, duration of parental care) but the number of matrices should remain the same-and the shape of the relationship between departure probability and date of capture to match the species life cycle. For example, modeling a hypothetical species similar to polar bears but in which both males and females care for offspring would increase the number of unique states from 24 to 42 ( 8 states for immature females and males, 21 states for dependent offspring cared for by both parents, just the mother in case of father loss, or just the father in case of mother loss). Such a model could be used to assess the influence of father versus mother loss on litter size, offspring survival and father and/or mother breeding probabilities. In-After defining the states and events, one should modify the shape of the relationship between departure probability and date of capture to match the species life cycle. In species-species like primates or wolves, departure from the family unit can occur throughout the year, at a more or less constant rate depending on the season, while it occurs only between February and May in polar bears due to environmental constraints. In addition, The general model structure, types of parameters involved and-steps of model definition should remain similar. Tthe influence of
individual traits such as age or body weight, or environmental variables such as temperature, can be included in the model under the form of individual or temporal covariates (Pollock 2002). In addition, $O$ Other specificities related to data collection can also-be included in a similar way, such as trap effects (Pradel and Sanz-Aguilar 2012) or latent individual heterogeneity by using mixture of distributions or random effects (Gimenez et al. 2018). Guidance to fit the model in a Bayesian framework in program Jags for real and simulated data are provided in Appendices 1 and 2.

## Simulation study

The simulation study was aimed at evaluating the performance of our model to estimate demographic parameters under various assumptions about the timing at offspring independence (constant versus seasonal departure rate) and various degrees of capture probability (low $\mathrm{p}=$ 0.25 , high $\mathrm{p}=0.7$ ), for a medium-size data set ( $\mathrm{T}=15$ sampling occasions, with $\mathrm{R}=80$ newly marked at each occasion in equal proportion among the 11 alive states).

We simulated data for a virtual long-lived mammal species mimicking the polar bear using the model described in box 1 . We used $\varphi=0.9$ for independent female bear survival (aged $2+$ y.o.), $s_{1}=l_{01}=0.6$ for singleton cub survival, $s_{2}=0.55$ for twin litter's cub survival (corresponding to twin litter survival $l_{02}=0.7975$ ), $s_{3}=0.8$ for singleton yearling survival and $s_{4}=0.75$ for twin litter's yearling survival (corresponding to litter survival $l_{12}$ $=0.94)$. Offspring survival rates were conditioned upon mother survival. If a mother dies, its dependent offspring had no chances of surviving. For breeding probabilities, we used $\beta_{1}=0.5$ , $\beta_{2}=0.7, \beta_{3}=0.9$ and $\beta_{4}=0.8$. For litter size probabilities, we used $\gamma_{1}=0.4, \gamma_{2}=0.5$, $\not \forall \gamma_{3}=0.6$ and $\gamma_{4}=0.7$. We set $\kappa=0$ and assumed that females had their first litter at age 6 or older.

We assumed that captures occurred each year between mid-March to end of May (day of the year $d=80$ to $d=130$ ). For each capture event, date of capture was randomly sampled from the distribution of the polar bear data dates of capture (see Appendix 1). In the constant scenario, we assumed that two-year old bears reached independence at a constant departure rate $(\alpha)$ during the field season, independently of the date of capture. We chose an intermediate value of $\alpha=0.5$ (if independence occurred always after the field season, $\alpha=0$, versus always before the field season, $\alpha=1$ ). In the seasonal scenario, we assumed that departure rate varied with date of capture (d) following a logistic relationship (regression coefficients were estimated from the polar bear data, see Appendix 2). Most of the two-year old offspring were captured with their mother at the beginning of the field season, while departure probability increased logistically up to $80 \%$ at the end of the field season.

We simulated 100 CR datasets for each of the 4 scenarios (S1: low detection with constant departure, S2: low detection with seasonal departure, S3: high detection with constant departure, S 4 : high detection with seasonal departure). We simulated the data using program R. We fitted the model using program jags called from R (Plummer 2016). For each parameter and each dataset, we calculated absolute bias as $\underline{\hat{B}} \equiv \underline{\hat{\theta}}=\underline{\theta}$, and root mean squared $\underline{\text { error as }} \underline{R \widehat{M S} E}=\sqrt{\left(\underline{\theta}=\underline{\theta}^{2}\right.} \underline{\underline{2}}$, with $\underline{\theta}$ the parameter used to simulate the data and $\hat{\theta}$ the mean value of the estimated parameter. Appendix 1 containing guidance, R code and files to simulate data and fit the model is available on GitHub at https://github.com/SCubaynes/Appendix1_extendedparentalcare.

## Case study: Polar bears in Svalbard

In polar bears, care of offspring is provided by the mother only (Amstrup, 2003). Males were therefore discarded from our analysis. Adult female polar bears mate in spring (February
to May, Amstrup 2003), and in Svalbard usually have their first litter at the age of six years, but some females can have their first litter at five years (Derocher 2013). They have delayed implantation where the egg attaches to the uterus in autumn (Ramsay and Stirling 1988). A litter with small cubs (ca 600 grams) is born around November to January, in a snow den that the mothers dig out in autumn, and where the family stay $4-5$ months. The family usually emerges from the den in March-April, and stay close to the den while the cubs get accustomed to the new environment outside their home, for a few days up to 2-3 weeks (Hansson and Thomassen 1983). Litter size in early spring vary from one to three, with two cubs being most common, three cubs in most areas being rare, and commonly around one out of three litters having one cub only (Amstrup 2003). In Svalbard, polar bears become independent from their mother shortly after their second birthday (average age at independence is 2.3 ). Two-year old bears typically depart from the mother in spring (between mid-March to end of May), when the mother can mate again. There is only one anecdotalie record of a yearling alive without his mother. Because the field season can last for several weeks, some two-year-old bears were captured together with their mother and others were already independent at the time of capture. The minimum reproductive interval for successful Barents Sea polar bears is 3 years. On the contrary, loss of a cub litter shortly after den emergence may mean the mother can produce new cubs in winter the same year (Ramsay and Stirling 1988).

Bears captured in Svalbard are shown to be a mixture of resident and pelagic bears (Mauritzen et al. 2002). To focus on the resident population, independent bears captured only once were not included in our analysis. We therefore analyzed $\mathrm{N}=158$ encounter histories of resident polar bear family units captured each spring after den emergence between doy 80 to 130 (mid-March to mid-May), from 1992 to 2019, in Svalbard. It corresponds to 81 capture events of juvenile and subadults, 231 cubs, 96 yearling, 23 dependent two-year old, and 444 captures of adult females. Polar bears were caught and individually marked as part of a long-
term monitoring program on the ecology of polar bears in the Barents Sea region (Derocher 2005). All bears one year or older were immobilized by remote injection of a dart (Palmer CapChur Equipment, Douglasville, GA, USA) with the drug Zoletil® (Virbac, Carros, France) (Stirling et al. 1989). The dart was fired from a small helicopter (Eurocopter 350 B2 or B3), usually from a distance of about 4 to 10 meters. Cubs of the year were immobilized by injection with a syringe. Cubs and yearlings were highly dependent on their mother; therefore, they remained in her vicinity and were captured together with their mother. A female captured alone was considered to have no dependent offspring alive. Death of the cubs could have occurred in the den or shortly after den emergence but before capture. Hereafter, estimated cub survival thus refers to survival after capture. Infant mortality occurring before capture will be assigned to a reduced litter size. Because only $3 \%$ of females were observed with 3 offspring, we analyzed jointly litters of twins with triplets.

We built the model described above with 12 states and 12 events to describe the life cycle (Table 1). Preliminary analyses suggested that mother survival did not vary according to state, we therefore constrained parameter $\varphi \phi$ to be equal among all states in matrix $\Phi$. To avoid identifiability issues due to a relatively small sample size, we assumed breeding probability and litter size probability did not vary between successful breeders (states AS1 and AS2) and female without dependent offspring (state A) by setting $\beta_{3}=\beta_{4}$ and $\gamma_{3}=\gamma_{4}$. We also assumed that litter size probability did not vary among failed breeders (loss of a cub versus a yearling litter), by setting $\gamma_{1}=\gamma_{2}$. We could not assess formally the fit of our model because no test is yet available for multievent models. However, the multi-state version of our model (without uncertainty on timing at independence) fitted the data adequately. Adding a level of complexity should make the model even more adequate.

Using the conditional probabilities estimated in the model, we calculated the net probability for a female to raise none, $\operatorname{Pr}(\mathrm{X}=0)$, one, $\operatorname{Pr}(\mathrm{X}=1)$, or two offspring, $\operatorname{Pr}(\mathrm{X}=2)$ to independence over a 3-year period (details are provided in Appendix 2).


Figure 1: Life history events with associated probabilities of raising one ( $\mathrm{X}=1$ ) or two ( $\mathrm{X}=2$ ) offspring to independence over a 3 years period for a female polar bear alive and without dependent offspring at the beginning of the period (state A). State A01 represents a female with one dependent cub of the year, A02 with two dependent cubs of the year, A11 with one dependent yearling, A12 with two dependent yearlings, AS1 a successful female breeder with one two-year old offspring reaching independence and AS2 a successful female breeder with two two-year old offspring reaching independence. Parameter $\left(\underline{\varphi} \phi\right.$ is adult survival, $\beta_{3}$ is breeding probability of a female without dependent offspring, $\gamma_{3}$ is the probability of a singleton litter, $s_{1}$ is cub andand $s_{2}$ is resp.cub and yearling survival in a singleton litter, $s_{3}$ is cub and $s_{4}$ resp.cub and yearling survival in a twin litterf.

We considered adult females without dependent offspring at the beginning of the time period, so that we have:
$\operatorname{Pr}(\mathrm{X}=1)=\varphi^{3} \cdot \beta_{3} \cdot\left[\gamma_{3} \cdot s_{1} \cdot s_{3}+\left(1-\gamma_{3}\right) \cdot\left(2 s_{2}\left(1-s_{2}\right) \cdot s_{3}+s_{2}{ }^{2} \cdot 2 s_{4}\left(1-s_{4}\right)\right)\right]$, $\operatorname{Pr}(\mathrm{X}=2)=\varphi^{3} \cdot \beta_{3} \cdot\left(1-\gamma_{3}\right) \cdot s_{2}{ }^{2} \cdot s_{4}{ }^{2}$, $\operatorname{Pr}(\mathrm{X}=0)=1-\operatorname{Pr}(X=1)-\operatorname{Pr}(X=2)$.

Appendix 2 containing guidance, R code, data files to fit the model to the polar bear data, and additional results is available on GitHub at https://github.com/SCubaynes/Appendix2 extendedparentalcare.

## RESULTS

## Model performance evaluated on simulated datasets

Model performance was satisfying and comparable in all 4 simulated scenarios (S1 with low detection and constant departure, S2 with low detection and seasonal departure, S3 with high detection and constant departure and S4 with high detection and seasonal departure), with low average bias $\left(B_{S 1}=-0.000, B_{S 2}=-0.004, B_{S 3}=-0.004, B_{S 4}=-0.003\right)$ and root-mean-
 . .


















square error $\left(r m s e_{S 1}=0.042, r m s e_{S 2}=0.041, r m s e_{S 3}=0.031\right.$ and $\left.r m s e_{S 4}=0.031\right)(\mathrm{see}$ Appendix 1 for details).

For most parameters, bias was very low, $\mathrm{B}<0.02$, except for parameters $\beta_{2}$ in scenarios S2, S3 and S4 $(-0.04<\mathrm{B}<-0.03)$ and $s_{3}$ in scenario $\mathrm{S} 2(\mathrm{~B}=-0.03)$, rmse $<0.05$, except for parameters $\beta_{2}, \gamma_{1}$ and $\gamma_{2}(0.05<\mathrm{rmse}<0.07)$. For these three parameters, precision was lower in the two scenarios with low detection (see Appendix 1). Estimates obtained for the scenario mimicking the polar bear study case (S2: low detection and seasonal departure) are provided in Figure 2.


Figure 2. Performance of the model on simulated data with low detection with seasonal departure (scenario S2). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X -axis for each parameter. Regarding notations, $\phi$ stands for juvenile, subadult and adult survival, $\kappa$ is the probability of first
reproduction at age $5, s$ is dependent offspring survival conditioned upon mother survival ( $s_{1}$ and $s_{2}$ for singleton cub resp. yearling; $s_{3}$ and $s_{4}$ for twin litter's cub resp. yearling), $\beta$ is breeding probability conditioned upon mother and offspring survival status ( $\beta_{1}$ following loss of a cub litter, and $\beta_{2}$ after loss acub litter resp. loss of a yearling litter, $\beta_{3}$ for successful breeder, $\beta_{4}$ for female without dependent offspring), $\gamma$ is the probability of producing a singleton litter conditioned upon mother's and offspring's survival status and upon breeding decision ( $\gamma_{1}$ following loss of a cub litter, and $\gamma_{2}$ after loss a cub litter resp. loss of a yearling litter, $\gamma_{3}$ for successful breeder, $\gamma_{4}$ for female without dependent offspring), $p$ is detection probability.

## Case study: Polar bear demography

Departure probability was about $40 \%$ at the end of March and reached $80 \%$ at mid-May (Appendix 2). About half of the two-year old bears had departed their mother at the time of capture. Estimates of demographic parameters are provided in Table 2 (more results are provided in Appendix 2). Independent female (aged 2+) survival was high (0.93). Individual offspring survival rates, conditioned upon mother survival, did not vary significantly with litter size for cubs or yearlings. Average yearling survival was lower for singleton (0.67) than for litters of twin (0.80), although the $95 \%$ credible intervals did overlap. Concerning litter survival conditioned upon mother survival, it was higher for twin compared to singleton, for both cubs’ and yearlings' litters. A small proportion of females, about $12 \%$, started to reproduce (i.e. produced a litter that survived at least until the first spring) at 5 y.o. Outcome of the previous reproduction influenced breeding probability. Breeding probability following the loss of a cub litter during the year (after capture) was low, about $10 \%$, while it was about $50-60 \%$ for female' successful breeders or without dependent offspring at the beginning of the year or after the loss of a yearling litter. Detection probability was relatively low, about 0.25 (0.22-0.27). At first capture, $37 \%$ were independent juvenile or subadult females, $18 \%$ were adult females alone, $28 \%$ were adult females with one or two cubs, $12 \%$ with one or two yearlings and $5 \%$ with twoyear old bears.

| Parameter | Notation | Mean | Standard error | 95\% CI |
| :---: | :---: | :---: | :---: | :---: |
| Survival of female juveniles (2yo,3yo) subadults (4yo, 5yo) and adults (5+ yo) | $\varphi$ | 0.93 | 0.01 | 0.92-0.95 |
| $\begin{aligned} & \hline \text { Cub survival (<1yo) } \\ &- \text { singleton (=litter } \\ & \text { survival) } \\ &- \text { litter of } 2 \text { (averaged } \\ & \text { individual survival) } \\ & \hline \end{aligned}$ | $\begin{gathered} s_{1}=l_{01} \\ s_{2} \end{gathered}$ | $\begin{aligned} & 0.54 \\ & 0.51 \end{aligned}$ | $\begin{aligned} & 0.10 \\ & 0.05 \end{aligned}$ | $\begin{aligned} & 0.34-0.72 \\ & 0.41-0.62 \end{aligned}$ |
| Yearling survival (1yo) <br> - Singleton (=litter survival) <br> - litter of 2 (averaged individual survival) | $s_{3}=l_{11}$ $S_{4}$ | $\begin{aligned} & 0.67 \\ & 0.80 \end{aligned}$ | $\begin{aligned} & 0.11 \\ & 0.09 \end{aligned}$ | $\begin{aligned} & 0.46-0.87 \\ & 0.59-0.93 \end{aligned}$ |
| Litter survival for twin litters <br> - cubs <br> - yearlings | $\begin{aligned} & l_{02} \\ & l_{12} \end{aligned}$ | $\begin{aligned} & 0.76 \\ & 0.95 \end{aligned}$ | $\begin{aligned} & 0.05 \\ & 0.04 \end{aligned}$ | $\begin{aligned} & 0.65-0.85 \\ & 0.83-0.99 \end{aligned}$ |
| Probability of first reproduction at 5 yo (mate at 4yo) | $\kappa$ | 0.12 | 0.08 | 0.02-0.30 |
| Breeding probability <br> - following loss of a cub litter <br> - following loss of a yearling litter <br> - of successful female breeders or previously without dependent offspring | $\begin{gathered} \beta_{1} \\ \beta_{2} \\ \beta_{3}=\beta_{4} \end{gathered}$ | $\begin{aligned} & 0.09 \\ & 0.58 \\ & 0.52 \end{aligned}$ | $\begin{aligned} & 0.06 \\ & 0.21 \\ & 0.04 \end{aligned}$ | $\begin{aligned} & 0.01-0.23 \\ & 0.19-0.96 \\ & 0.43-0.61 \end{aligned}$ |
| Probability of singleton litter <br> - following loss of a cub or yearling litter <br> - of successful females breeders or previously without dependent offspring | $\begin{gathered} \gamma_{1}=\gamma_{2} \\ \gamma_{3}=\gamma_{4} \end{gathered}$ | 0.35 0.40 | 0.17 0.05 | $\begin{aligned} & 0.07-0.71 \\ & 0.30-0.44 \end{aligned}$ |
| Capture probability | p | 0.25 | 0.01 | 0.22-0.27 |

Over a 3 years period, the probability to successfully raise one offspring to independence for a female polar bear, alive and without dependent offspring at the beginning of the period, was on average $0.29(0.20-0.38)$ and $0.04(0.02-0.07)$ to raise two offspring to independence. The probability of failed breeding (no offspring successfully reached independence) over this period was high, about 0.67 ( $0.57-0.76$ ). Note that this calculation includes breeding probability, and therefore does not reflect offspring survival until independence (see Method section).

## DISCUSSION

Overall, our model performed well in estimating all demographic parameters in all the simulated scenarios. A multievent approach is a promising tool to deal with uncertainty on the timing at offspring independence both when departure probability was constant or varied within the field season. Estimates obtained for adult and offspring survival, probability of sexual maturation, breeding probability (except after the loss of a yearling litter), litter size probabilities and detection probability were unbiased in most simulated scenarios. Precision was satisfying in most cases, but it was lower for breeding probability after the loss of a yearling litter and for litter size probabilities of failed breeders, especially in scenarios with low detection (Appendix 1). These specific parameters should therefore be interpreted with caution for the study case. In our simulations, $\mathrm{T}=15$ sampling occasions appeared sufficient to obtain satisfying estimates for most parameters. In the polar bear data, there were few recaptures of females on subsequent years due to relatively low detection rate. As a result, preliminary analyses suggested a potential confusion between these parameters. We dealt with this issue by including a biologically realistic constraint on prior distributions, stating that cub survival was lower than that of yearling survival (Amstrup and Durner, 1995) which was enough to ensure parameter estimability. Inference in a Bayesian framework is useful in this regard, because it allows to-for
the include-inclusion of prior information when available (McCarthy and Masters 2005) to improve the estimation of model parameters.

For polar bears, we showed that outcome of the previous breeding event influenced breeding probability. Reduced offspring survival one year, for example due to poor environmental conditions (Derocher et al. 2004), might therefore increase intervals between successful reproduction through reduced breeding probability the next year (Wiig 1998). This means that by ignoring multiple-year dependency among mother and offspring, classical models can underestimate reproductive intervals, therefore risking to overestimate the population growth rate. However, the biological relevance of our model is currently limited, because we ignored temporal and individual heterogeneity among females in the model. Survival rates for independent female bears ( 0.93 ) were close to an earlier study for the same population (0.96), based on telemetry data (Wiig 1998). Our results may overestimate dependent offspring survival because we focused on resident bears captured more than once. Wiig (1998) results indicated that females in Svalbard went into den on average every second year (while successful breeding means denning on a three-year interval), which seems coherent with our results (about $33 \%$ chances of successful reproduction over a three-year period).

Here, we proposed a general model structure that can be applied to other species providing EPC. The originalities of our approach lie in using family structure to define statistical units in our model, and the inclusion of variable timing at offspring independence. It allowsUsing families instead of individuals allows for the inclusion of to include dependency among individuals over multiple-years and therefore the evaluation of trade-offs and correlations correlations-between offspring's and parents' life history parameters. Our model could be applied to other species providing EPC, such as wolves, showing variable litter size and age at offspring independence. However, applying our model to species like elephants, killer whales or humans would require including an additional 'post-reproductive' stage and
estimate the age at menopause. Such extensions of our model could be-used, for example, to evaluate the population-level consequences of positive or negative correlation between parents' and offspring's traits (e.g. food sharing among group members Lee 2008; or parent-offspring conflict Kölliker et al. 2013). In the case of social species (e.g. primates, elephants, orcas, wolves), several adults often play a role in caring for offspring. In addition, females often give birth to new offspring while still caring for older offspring and, above a certain age, adolescent dependent offspring can survive despite the loss of their mother and gain independence at various ages. In such cases, the number of states to represent all possible family units' composition can rapidly increase, leading to potential computational challenges to deal with huge matrices. One solution is to use sparse matrices tools in matlab which seem to work well up to XX states to store the data efficiently and optimize matrix calculations. Above this level of complexity, an alternative solution is to limit the number of states by simplifying the life cycle depending on the question of interest (e.g. focusing on mother and maternal grand-mother considering only one litter, or focusing on mother caring alone for one or more litters). For polar bears specifically, future analyses will integrate in the model the effect of female age on survival and reproductive success (Atkinson and Ramsay 1995; Folio et al. 2019) and influence of climatic variables on body weight and demography (Derocher et al. 2004; Stirling and Derocher 2012) as individual and environmental covariates in a regression-like framework. Our model could then be used to provide population predictions of the demographic response of the Barents Sea polar bear population under climate change (Hunter et al., 2010; Regehr et al., 2016, 2018, Laidre et al. 2020).

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Data Accessibility Statement : Authors agree to archive the data used in this manuscript in a publicly accessible repository such as Dryad and Github upon acceptance of the manuscript (together with R scripts to run the model and the simulation study).

Authors' contributions: SC, OG, NY and RP conceived the ideas and designed methodology; JA, RAI and ØW collected the data; SC analysed the data; SC led the writing of the manuscript. All authors contributed critically to the drafts and gave final approval for publication.

## Bibliography

Amstrup, S. C., \& DeMaster, D. P. (2003). Polar bear, Ursus maritimus. Wild mammals of North America: biology, management, and conservation, 2, 587-610.

Amstrup, S. C., \& Durner, G. M. (1995). Survival rates of radio-collared female polar bears and their dependent young. Canadian Journal of Zoology, 73, 1312-1322. doi:10.1139/z95-155

Atkinson, S. N., \& Ramsay, M. A. (1995). The Effects of Prolonged Fasting of the Body Composition and Reproductive Success of Female Polar Bears (Ursus maritimus). Functional Ecology, 9(4), 559. doi:10.2307/2390145

Clutton-Brock, T. H. (1991). The evolution of parental care. Princeton: Princeton University Press.

Cole, D. J., Morgan, B. J. T., McCrea, R. S., Pradel, R., Gimenez, O., \& Choquet, R. (2014). Does your species have memory? Analyzing capture-recapture data with memory models. Ecology and Evolution, 4(11), 2124-2133.

Couet, P., Gally, F., Canonne, C., \& Besnard, A. (2019). Joint estimation of survival and breeding probability in female dolphins and calves with uncertainty in state assignment. Ecology and evolution, 9(23), 13043-13055.

Dahle, B., \& Swenson, J. E. (2003). Factors influencing length of maternal care in brown bears (Ursus arctos) and its effect on offspring. Behavioral Ecology and Sociobiology, 54(4), 352-358.

Derocher A., \& Stirling, I. (1994). Age-specific reproductive performance of female polar bears (Ursus maritimus). Journal of Zoology, 234(4), 527-536.

Derocher, A. ., Lunn, N. ., \& Stirling, I. (2004). Polar bears in a warming climate. (Ursus maritimus). Integrative and Comparative Biology, 44(2), 163-176.

Derocher, A.E., 2005. Population ecology of polar bears at Svalbard, Norway. Population Ecology, 47(3), pp.267-275.

Derocher, A. (2013). Polar bears: a complete guide to their biology and behavior. Choice Reviews Online, 49(12), 49-6887-49-6887. doi:10.5860/choice.49-6887

Doligez, B., Clobert, J., Pettifor, R. A., Rowcliffe, M., Gustafsson, L., Perrins, C. M., \& McCleery, R. H. (2002). Costs of reproduction: Assessing responses to brood size manipulation on life-history and behavioural traits using multi-state capture-recapture models. Journal of Applied Statistics, 29(1-4), 407-423.

Eldegard, K., \& Sonerud, G. A. (2010). Experimental increase in food supply influences the outcome of within-family conflicts in Tengmalm's owl. Behavioral Ecology and Sociobiology, 64(5), 815-826.

Folio, D.M., Aars, J., Gimenez, O., Derocher, A.E., Wiig, Ø. and Cubaynes, S., (2019). How many cubs can a mum nurse? Maternal age and size influence litter size in polar bears. Biology letters, 15(5), p. 20190070.

Gimenez, O., Lebreton, J.-D., Gaillard, J.-M., Choquet, R. and R. Pradel (2012). Estimating demographic parameters using hidden process dynamic models. Theoretical Population Biology 82, 307-316.

Gimenez, O., Cam, E., \& Gaillard, J.-M. (2018). Individual heterogeneity and capture-recapture models: what, why and how? Oikos, 127(5), 664-686.

Hansson, R., \& Thomassen, J. (1983). Behavior of polar bears with cubs in the denning area. Bears: Their Biology and Management, 246-254.

Hunter, C. M., Caswell, H., Runge, M. C., Regehr, E. V., Amstrup, S. C., \& Stirling, I. (2010). Climate change threatens polar bear populations: a stochastic demographic analysis.

Ecology, 91(10), 2883-2897.

Kölliker, M., Kilner, R. M., \& Hinde, C. A. (2013). Parent-offspring conflict. In The Evolution of Parental Care.

Kramer, K. L. (2005). Children's help and the pace of reproduction: cooperative breeding in humans. Evolutionary Anthropology: Issues, News, and Reviews: Issues, News, and Reviews, 14(6), 224-237.

Lagrange, P., Gimenez, O., Doligez, B., Pradel, R., Garant, D., Pelletier, F., \& Bélisle, M. (2017). Assessment of individual and conspecific reproductive success as determinants of breeding dispersal of female tree swallows: A capture-recapture approach. Ecology and Evolution, 7(18), 7334-7346.

Laidre, K. L., Atkinson, S., Regehr, E. V., Stern, H. L., Born, E. W., Wiig, Ø., ... \& Dyck, M. (2020). Interrelated ecological impacts of climate change on an apex predator. Ecological Applications, e02071.

Lebreton, J. D., Nichols, J. D., Barker, R. J., Pradel, R., \& Spendelow, J. A. (2009). Chapter 3 Modeling Individual Animal Histories with Multistate Capture-Recapture Models. Advances in Ecological Research.

Lee, P. C., \& Moss, C. J. (1986). Early maternal investment in male and female African elephant calves. Behavioral Ecology and Sociobiology, 18(5), 353-361.

Lee, R. (2008). Sociality, selection, and survival: Simulated evolution of mortality with intergenerational transfers and food sharing. Proceedings of the National Academy of Sciences.

Lunn, N.J., Servanty, S., Regehr, E.V., Converse, S.J., Richardson, E. and Stirling, I.( 2016). Demography of an apex predator at the edge of its range: impacts of changing sea ice on polar bears in Hudson Bay. Ecological Applications, 26(5), pp.1302-1320.Mauritzen, M.,

Derocher, A. E., \& Wiig, Ø. (2011). Space-use strategies of female polar bears in a dynamic sea ice habitat. Canadian Journal of Zoology, 79(9), 1704-1713.

Mauritzen, M., Derocher, A.E., Wiig, Ø., Belikov, S.E., Boltunov, A.N., Hansen, E. and Garner, G.W., (2002). Using satellite telemetry to define spatial population structure in polar bears in the Norwegian and western Russian Arctic. Journal of Applied Ecology, 39(1), pp.7990.

McCarthy, M. A., \& Masters, P. (2005). Profiting from prior information in Bayesian analyses of ecological data. Journal of Applied Ecology, 42(6), 1012-1019.

Pavard, S., \& Branger, F. (2012). Effect of maternal and grandmaternal care on population dynamics and human life-history evolution: A matrix projection model. Theoretical Population Biology.

Plummer, M., Stukalov, A., Denwood, M. and Plummer, M.M., (2016). Package 'rjags'. Vienna, Austria.

Pollock, K. H. (2002). The use of auxiliary variables in capture-recapture modelling: An overview. Journal of Applied Statistics, 29(1-4), 85-102.

Pradel, R. (2005) Multievent: An extension of multistate capture-recapture models to uncertain states». Biometrics 61: 442-447

Pradel, R., \& Sanz-Aguilar, A. (2012). Modeling Trap-Awareness and Related Phenomena in Capture-Recapture Studies. PLoS ONE, 7(3), e32666.

Ramsay, M. A., \& Stirling, I. (1988). Reproductive biology and ecology of female polar bears in western Hudson Bay. Naturaliste Canadien, 109(4), 941-946.

Regehr, E. V., Laidre, K. L., Resit Akcakaya, H., Amstrup, S. C., Atwood, T. C., Lunn, N. J., ... Wiig, Ø. (2016). Conservation status of polar bears (Ursus maritimus) in relation to projected sea-ice declines. Biology Letters, 12(12).

Regehr, E.V., Hostetter, N.J., Wilson, R.R., Rode, K.D., Martin, M.S. and Converse, S.J., (2018). Integrated population modeling provides the first empirical estimates of vital rates and abundance for polar bears in the Chukchi Sea. Scientific reports, 8(1), pp.1-12.

Royle, N., Smiseth, P., \& Kölliker, M. (2012). The evolution of parental care.
Shenk, M. K., \& Scelza, B. A. (2012). Paternal investment and status-related child outcomes: Timing of father's death affects offspring success. Journal of Biosocial Science.

Stearns, S.C. 1992. The Evolution of Life Histories. Oxford University Press.

Stirling, I., \& Derocher, A. E. (2012). Effects of climate warming on polar bears: a review of the evidence. Global Change Biology, 18(9), 2694-2706.

Stirling, I., Spencer, C., \& Andriashek, D. (1989). Immobilization of polar bears (Ursus maritimes) with Telazol in the Canadian Arctic. Journal of Wildlife Diseases, 25(2), 159168.

Trivers, R. L. 1972. Parental investment and sexual selection. Pages 136-179 in B. G. Campbell, editor. Sexual selection and the descent of man,1871-1971. Aldine, Chicago

Van Noordwijk, M. A. (2012). From Maternal Investment to Lifetime Maternal Care. In Evolution of Primate Societies (pp. 321-342).

Vergara, P., Fargallo, J. A., \& Martínez-Padilla, J. (2010). Reaching independence: food supply, parent quality, and offspring phenotypic characters in kestrels. Behavioral ecology, 21(3), 507-512.

Wich, S., Utami-Atmoko, S., Setia, T. M., Rijksen, H. D., Schürmann, C., Van Hooff, J. A. R. A. ., \& van Schaik, C. P. (2004). Life history of wild Sumatran orangutans (Pongo abelii). Journal of Human Evolution, 47(6), 385-398.

Wiig, Ø. (1998). Survival and Reproductive Rates for Polar Bears at Svalbard. Ursus, 10, 2532.

Williams, G.C. (1966) Natural selection, the costs of reproduction, and a refinement of Lack's principle. American Naturalist. 100, 687-690

Yoccoz, N. G., Erikstad, K. E., Bustnes, J. O., Hanssen, S. A., \& Tveraa, T. (2002). Costs of reproduction in common eiders ( Somateria mollissima ): An assessment of relationships between reproductive effort and future survival and reproduction based on observational and experimental studies. Journal of Applied Statistics, 29(1-4), 57-64.


Figure 1: Life history events with associated probabilities of raising one ( $X=1$ ) or two ( $X=2$ ) offspring to independence over a 3 years period for a female polar bear alive and without dependent offspring at the beginning of the period (state A). State A01 represents a female with one dependent cub of the year, A02 with two dependent cubs of the year, A11 with one dependent yearling, A12 with two dependent yearlings,

AS1 a successful female breeder with one two-year old offspring reaching independence and AS2 a successful female breeder with two two-year old offspring reaching independence. Parameter $\varphi$ is adult survival, $\beta_{2} 3$ is breeding probability of a female without dependent offspring, $Y \_3$ is the probability of a singleton litter, s_1 is cub and s_2 is yearling survival in a singleton litter, s_3 is cub and s_4 yearling survival in a twin litter.


Figure 2. Performance of the model on simulated data with low detection with seasonal departure (scenario S2). For each of the 100 simulated data sets, we displayed the mean (circle) and the $95 \%$ confidence interval (horizontal solid line) of the parameter. The actual value of the parameter is given by the vertical dashed red line. The estimated absolute bias and root-mean-square error are provided in the legend of the X -axis for each parameter. Regarding notations, $\phi$ stands for juvenile, subadult and adult survival, k is the probability of first reproduction at age $5, \mathrm{~s}$ is dependent offspring survival conditioned upon mother survival (s_1 and s_2 for singleton cub resp. yearling; s_3 and s_4 for twin litter's cub resp. yearling), $\beta$ is breeding probability conditioned upon mother and offspring survival status $\mathbb{(}) \beta \rrbracket 1$ following loss of a cub litter, $\beta \_2$ loss of a yearling litter, $\beta \_3$ for successful breeder, $\beta \_4$ for female without dependent offspring), $\gamma$ is the probability of producing a singleton litter conditioned upon mother's and offspring's survival status and upon breeding decision ( $Y \_1$ following loss of a cub litter, $Y \_2$ loss of a yearling litter, $Y$ _ 3 for successful breeder, $\mathrm{Y} \_4$ for female without dependent offspring), p is detection probability.


Bear picture for graphical abstract or cover

