

# Modeling (some aspects of ) the female reproductive system

Romain Yvinec

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## Modeling (some aspects of ) the female reproductive system

#### Romain Yvinec

#### Physiologie de la Reproduction et des Comportements INRAe Tours



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### Acknowledgements

- \* INRIA Saclay : Frédérique Clément, Guillaume Ballif, Frédérique Robin
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- CEMRACS 2018 (Céline Bonnet (CMAP, X), Kerloum Chahour (U. Côte d'Azur))

Ínría INRAQ



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The Mammalian female reproductive system : a complex multiscale system

> Encoding and decoding neurohormonal signals

> Population dynamics : gametogenesis

Intra-cellular level : signaling networks



Yvinec et al., Advances in computational modeling approaches of pituitary gonadotropin signaling, Expert Opinion on Drug Discovery, 2018.



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#### Scientific and societal issues in reproductive science

## Understanding of a complex process of developmental biology, occuring during the whole lifespan

Numerous cell types involved, and various interactions Many different spatial and temporal scales Hormonal feedback (endocrine, paracrine, autocrine) Steric and biophysical constraint

#### Preserve the reproductive ability

latrogenic or physiological alterations Sensibility to environmental conditions Biodiversity preservation

#### Control of the reproduction function (in humans and animals)

Biotechnology of reproduction (*in vivo*, *ex vivo*, *in vitro*) Clinical, economical and environmental issues

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Population dynamics : gametogenesis

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#### Neuro-hormonal signals (at the anatomic scale)

Mostly phenomenological equations (DDEs/SDEs) to represent measured levels of circulating hormones, on a daily basis.



Margolskee & Selgrade, JTB 2013



Margolskee & Selgrade, JTB 2013

These models can explain some disorders in hormonal levels and predict the effect of pharmaceutical intervention.

#### Neuro-hormonal signals (at the anatomic scale)

Mostly phenomenological equations (DDEs/SDEs) to represent measured levels of circulating hormones, on a daily basis.



Margolskee & Selgrade, JTB 2013

These models can explain some disorders in hormonal levels and predict the effect of pharmaceutical intervention. **Theoretical analysis gets rapidly challenging**! The Mammalian female reproductive system : a complex multiscale system

> Encoding and decoding neurohormonal signals

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 Morphogenesis and maturation of ovarian follicles somatic and germ (egg) cells
 ⇒ Somatic cell division and germ cell growth up to ovulation



Fig. 1. Illustrations of follicle types: (a) Type B,  $\times$  570; (b) Type B/C,  $\times$  570; (c) Type C,  $\times$  570; (d) Type D,  $\times$  410.

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Gougeon & Chainy, J. Reprod. Fert. 1987

- Morphogenesis and maturation of ovarian follicles somatic and germ (egg) cells
- Pool of Quiescent follicles static reserve (perinatal in most mammals) Slow activation



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Monniaux, Theriogenology 2016

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- Morphogenesis and maturation of ovarian follicles somatic and germ (egg) cells
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- Basal growth
   Dynamic reserve (starting at birth)
   Spanning over several ovarian cycles



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- Morphogenesis and maturation of ovarian follicles somatic and germ (egg) cells
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- Terminal growth After puberty : ovulation within an ovarian cycle



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- Basal growth Dynamic reserve (starting at birth) Spanning over several ovarian cycles
- Terminal growth After puberty : ovulation within an ovarian cycle
- Interactions between all follicles via complex (neuro-) hormonal signals



Ovarian reserves of follicles and their regulations



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Monniaux, Theriogenology 2016

#### Follicle population in women



Scaramuzzi et al., Reprod.Fert. Dev. 2011

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#### Follicle population in women

- Quiescent follicles
  - $\begin{array}{ll} \mbox{peri-natal} & \approx 5 \cdot 10^6 \\ \mbox{At birth} & \approx 1 \cdot 10^6 \\ \mbox{At puberty} & 10^4 10^6 \\ \mbox{At menopause} & < 10^3 \\ \mbox{Activation rate} & "A few per days" \end{array}$
- Growing follicles Maturation time 120 - 180jBasal follicles  $10^3 - 10^4$ Terminal follicles  $10^2$ Pre-Ovulatory follicles a few Atresia Most of them !



Scaramuzzi et al., Reprod.Fert. Dev. 2011

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#### Follicle population in women

- Growing follicles
   Maturation time
   120 180j
   Basal follicles
   10<sup>3</sup> 10<sup>4</sup>
   Terminal follicles
   10<sup>2</sup>
   Pre-Ovulatory follicles
   a few
   Atresia
   Most of them !
   -> Only 400 follicles will ever reach
   the pre-ovulatory stage



Scaramuzzi et al., Reprod.Fert. Dev. 2011

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a single follicle (in women) at different maturation stages somatic cells diam.  $10 \mu m$ ovocyte (egg cell) diam. :  $10 - 100 \mu m$ follicle diam. nb somatic cells

0.03 - 20mm $10^2 - 10^7$ 



Courtesy of Danielle Monniaux.

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## Modeling ovarian folliculogenesis

#### Growth of a single follicle





 Thesis of F. Robin, (co-supervised. F. Clément) 2016-2019





Scaramuzzi et al., Reprod. Fert. Dev. 2011

- CEMRACS 2018 (summer school), C. Bonnet, K. Chahour, (co-supervised by F. Clément, M. Postel)
- Thesis of G. Ballif, (co-supervised. F. Clément) 2019-2022

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- Nonlinear interactions between follicles populations (endocrine and  $\Rightarrow$ paracrine)
- $\Rightarrow$  Slow decay of total follicles number and "stable" repartition in the maturity space



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Faddy et al., J. Exp. Zool. 1976

An Analytical Model for Ovarian Follicle Dynamics

M. J. FADDY.<sup>1</sup> ESTHER C. JONES<sup>2</sup> AND R. G. EDWARDS<sup>3</sup> <sup>1</sup> Department of Mathematical Statistics, University of Birmingham, Birmingham B15 2TT, U.K.<sup>3</sup> Department of Anatomy, University of Birmingham, Birmingham B15 2TJ, U.K., and <sup>2</sup>Physiological Laboratory, University of Cambridge, Cambridge CB2 3EG, U.K.

- "Migration-death" stochastic model
- Linear model with time-dependent coefficient



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Bonnet et al. Multiscale population dynamics in reproductive biology : singular perturbation reduction in deterministic and stochastic models, to appear in ESAIM : PROCEEDINGS AND SURVEYS.





Bonnet et al. Multiscale population dynamics in reproductive biology : singular perturbation reduction in deterministic and stochastic models, to appear in ESAIM : PROCEEDINGS AND SURVEYS.



Theorem (G. Ballif, Averaging slow-fast dynamics) For smooth and lower/upper bounded rates  $\lambda, \mu$ , the CTMC converges as  $\varepsilon \to 0$  (in  $\mathcal{D}_{\mathbb{R}}[0, \infty[\times \mathcal{L}_m(\mathbb{N}^d))$ ) towards the solution of

$$\begin{cases} \frac{dx_0}{dt}(t) &= -\Lambda_0(x_0(t))x_0(t) & x_0(0) = x_0^{in}, \\ \Lambda_0(x_0) &= \sum_{y \in \mathbb{N}^d} \left(\lambda_0(x_0, y) + \mu_0(x_0, y)\right)\pi_{x_0}(y) & \forall x_0 \in \mathbb{R}_+, \\ 0 &= \sum_{y \in \mathbb{N}^d} L_{x_0}f(y)\pi_{x_0}(y) & \forall f \in \mathcal{C}_b^2(\mathbb{N}^d), \\ L_{x_0}f(y) &= \lambda_0(x_0, y)x_0\Big[f(y + e_1) - f(y)\Big] & \forall y \in \mathbb{N}^d, \\ &+ \sum_{i=1}^{d-1} \lambda_i(x_0, y)y_i\Big[f(y + e_{i+1} - e_i) - f(y)\Big] \\ &+ \sum_{i=1}^{d} \mu_i(x_0, y)y_i\Big[f(y - e_i) - f(y)\Big] \end{cases}$$

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• Separation of time scale is coherent with biological knowledge and follicles count data.



- Separation of time scale is coherent with biological knowledge and follicles count data.
- Work in progress...
- Identifiability issues (even with the linear model)
- The limit model allows to test null hypothesis (no regulation)

## Modeling ovarian folliculogenesis

#### Growth of a single follicle



Monniaux et al., M/S. 1999

 Thesis of F. Robin, (co-supervised. F. Clément) 2016-2019



Scaramuzzi et al., Reprod. Fert. Dev. 2011

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#### Follicle initiation



## Key features of follicle initiation

- Leave the quiescent phase (static reserve)
- A single layer of somatic cells
- Two types of cells : Flattened and Cuboid
- Irreversible transition from Flattened to Cuboid cells
- The follicle is "activated" when all cells have transitioned
- "Awakening" signals both from external and internal cues



Fig. 1. Illustrations of follicle types: (a) Type B,  $\times$  570; (b) Type B/C,  $\times$  570; (c) Type C,  $\times$  570; (d) Type D,  $\times$  410.

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Gougeon & Chainy, J. Reprod. Fert. 1987

#### Basal growth



## Key features of follicle basal growth

- Growth of a small follicle after initiation
- Spherical Symmetry
- Spatial structure of somatic cells in concentric layers
- Joint dynamic
  - \* Ovocyte growth
  - \* Somatic cells Proliferation
- Growth signals from the Ovocyte to somatic cells and *vice-versa*.



Courtesy of Danielle Monniaux.

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#### Terminal growth



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### Key features of Follicle terminal growth

- Lost of spherical symmetry
- Joint Dynamic
  - \* Liquid-filled cavity formation and growth
  - Switch from proliferation to differentiation of somatic cells
  - \* Morphogen gradient
- Role of the Liquid-filled cavity?



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Tertiary ( antral) follicle

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#### Simple model : spatial compartment in successive layers

- Spherical ovocyte (d<sub>O</sub>)
- Linear proliferation dynamics of somatics cells
- Layer dependent division rate
- Multi-type Bellman-Harris Branching process

Somatic cells divide and migrate to successive layers.



- The geometrical model allows a simple spatial description
- The model is linear and decomposable : exponential growth, with a stable asymptotic spatial profile : there exists a unique λ > 0 such that the process Z<sub>t</sub> verifies

$$\lim_{t\to\infty} Z_t e^{-\lambda t} = \hat{Z} \quad \text{(in law)}$$





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Clément et al. Analysis and Calibration of a Linear Model for Structured Cell Populations with Unidirectional Motion : Application to the Morphogenesis of Ovarian Follicles, SIAM App. math, 2019

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#### Fitting results

- $\Rightarrow~$  Exponential growth dominated by the first cell layer
- ⇒ Parameter identifiability and doubling time quantification ( $\approx$  16 days) : Cell-cycle time  $\nearrow$  with ovocyte distance



Clément et al. Analysis and Calibration of a Linear Model for Structured Cell Populations with Unidirectional Motion : Application to the Morphogenesis of Ovarian Follicles, SIAM App. math, 2019

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#### More realistic model?



 $\frac{\partial u}{\partial t} + div (\overrightarrow{v} u) = b(x)u(t,x)$ for  $x \in \Omega(t)$  and with  $\overrightarrow{v}$  linked to the negative gradient of the pressure, and the pressure related to the density... Under locally constant density and spherical geometry, one have :

$$\frac{d}{dt}(r_F(t)) = \gamma \int_{\Omega(t)} b(x) dx + \frac{d}{dt}(r_O(t))$$

work in progress...

### Antrum growth model

• Multiphasic advection-diffusion-reaction PDE

$$\begin{array}{rcl} (\partial_t + \operatorname{div}_{\mathbf{x}}(\mathbf{v}_{\mathbf{M}} \cdot )) \, u_{\mathbf{M}} &=& R_{\mathbf{M}} \\ & & & & \\ & & & & \\ & & & p_{\mathbf{M}} &=& C_{\mathbf{M}}(u_{\mathbf{M}} - u_0)^{\gamma_{\mathbf{M}}} \, , \\ (\partial_t + \operatorname{div}_{\mathbf{x}}(\mathbf{v}_a \cdot )) \, \Phi_a &=& D\Delta \Phi_a + R_a \\ & & & \\ &$$

+ Boundary conditions and constitutive laws work in progress...



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### Antrum growth model

• Multiphasic advection-diffusion-reaction PDE

$$\begin{array}{rcl} (\partial_t + \operatorname{div}_{\mathbf{x}}(\mathbf{v}_{\mathbf{M}} \cdot)) \, u_M &=& R_M \\ & v_M &=& -\mu_M \nabla_{\mathbf{x}} p_M \,, \\ & p_M &=& C_M (u_M - u_0)^{\gamma_M} \,, \\ (\partial_t + \operatorname{div}_{\mathbf{x}}(\mathbf{v}_{\mathbf{a}} \cdot)) \, \Phi_a &=& D \Delta \Phi_a + R_a \\ & \operatorname{div}_{\mathbf{x}} \mathbf{v}_{\mathbf{a}} &=& 0 \,, \\ & \nabla \Phi_a \cdot \overrightarrow{n}_a &=& s(t) = \kappa \int_{\Omega_M} u_M(t, \mathbf{x}) d\mathbf{x} \\ & \frac{d}{dt} \left( \frac{4}{3} \pi r_a(t)^3 \right) &=& J_{H_2O} = L_p(t) \left( \Delta \Pi - \Delta p \right) \\ & \Delta \Pi &=& c_a \Phi_a^{\gamma_a} \\ & \Delta p &=& p_M(t, |\mathbf{x}| = r_a^+) - p_e \\ & L_p(t) &=& \frac{\Pi(r_F(t) - r_a(t))^4}{8 \eta e(u_M)} \, n(u_M) \,, \end{array}$$



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#### $+ \mbox{ Boundary conditions and constitutive laws}$

work in progress...

The Mammalian female reproductive system : a complex multiscale system

> Encoding and decoding neurohormonal signals

> Population dynamics : gametogenesis

Intra-cellular level : signaling networks





Yvinec et al., Advances in computational modeling approaches of pituitary gonadotropin signaling, Expert Opinion on Drug Discovery, 2018.

#### cAMP-induced FSH and its regulation at the cellular level

- FSHR signaling network and short-term cAMP induction.
- Long-term regulation of the FSHR network during follicular selection.
- $\Rightarrow$  The Cellular "switch" is a pre-requisite for follicle selection .
- ⇒ This switch is implemented at molecular level by the FSHR network and cAMP output (which is a good marker of follicle maturity).



#### FSHR networks : very complicated dynamics !



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#### FSHR networks : very complicated dynamics !



"Network Biology"-> next week!

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- Circulating hormones dynamical models (Selgrade's model)
  - \* Purely hormonal dynamics
  - $\star\,$  limit cycles in compact delay differential equation models of the ovarian cycle



- Circulating hormones dynamical models (Selgrade's model)
- Follicles dynamics in compartment (Faddy's model)
  - $\star$  Reproductive lifespan timescale
  - Follicle communication and "hormonal control" through population feedback



Clark & Kruger, WIREs Syst Biol Med 2017

- Circulating hormones dynamical models (Selgrade's model)
- Follicles dynamics in compartment (Faddy's model)
- Coupled Hormonal/Follicle dynamical models (Lacker's & Clément's model)
  - $\star\,$  Ovarian cycle / follicle cohort timescale
  - \* Follicle cohort subject to a shared hormonal environment
  - \* The individual follicle maturity rate has local positive feedback and global negative feedback.



- Circulating hormones dynamical models (Selgrade's model)
- Follicles dynamics in compartment (Faddy's model)
- Coupled Hormonal/Follicle dynamical models (Lacker's & Clément's model)
- Cell dynamics in a single follicle (Clément's model)
  - $\star$  Cell cycle time scale
  - $\star\,$  Pool of different cell types within a single follicle
  - \* Complex geometry and moving boundary problems



Clark & Kruger, WIREs Syst Biol Med 2017 🖬 🕨 🖉 🕨 🖉 🖉 🖉

- Circulating hormones dynamical models (Selgrade's model)
- Follicles dynamics in compartment (Faddy's model)
- Coupled Hormonal/Follicle dynamical models (Lacker's & Clément's model)
- Cell dynamics in a single follicle (Clément's model)
- Intra-cellular dynamics (Clément / Quignot & Bois)
  - $\star$  Steroidogenesis, cAMP response



Reinecke & Deuflhard, JTB 2007 🛛 🔾 🖬 🕨 🖉 🕨 🖉 🕨 🖉 👘 🖉

#### Multiscale Models of ovarian follicle selection

#### • Putting "many" pieces together (Reinecke & Deuflhard)



- From (stochastic) GnRH pulse generator to detailed steroid metabolism through (compartment-based) follicle development
- \* Focus in this paper is on the model development
- \* 43 equations (stochastic input and delay differential equations), 191 parameters.

Reinecke & Deuflhard, JTB 2007

## Population dynamics in ovarian folliculogenesis

- Somatic cells proliferation, differentiation, and migration during follicle initiation& growth
- Multiscale nonlinear dynamics shape the follicle population distribution into different maturity stages.



## Population dynamics in ovarian folliculogenesis

- Somatic cells proliferation, differentiation, and migration during follicle initiation& growth
- Multiscale nonlinear dynamics shape the follicle population distribution into different maturity stages.





Image: A mathematical states and a mathem



- Ex vivo data in sheep fetus ( Courtesy of K. McNatty) : WT (++) vs Mutant (BB)
- $\Rightarrow \text{ Proportion of} \\ \text{ cuboid cells} \\ p_C = C/(F+C) \text{ vs} \\ \text{ number of cuboid} \\ \text{ cells } C$

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- Ex vivo data in sheep fetus WT vs BB
- Once activated, follicles have "fast" cell proliferation
- ⇒ Are both differentiation et de proliferation process concomitant or successive ?



- Ex vivo data in sheep fetus WT vs BB
- Proportion of cuboid cells seems higher in mutant than WT, for a given number of cuboid cells.
- ⇒ Is it coming from a kinetic difference?



- Ex vivo data in sheep fetus WT vs BB
- Regulatory mechanism for this process are barely known.
- ⇒ Is the transition of cell differentiation abrupt or more progressive ?

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Events	Reaction	Intensity function	→ Two cell populations : F (flattened and C (cuboid)
differentiation	F  ightarrow C	$\alpha F + \beta \frac{FC}{F+C}$	$\begin{array}{l} \hookrightarrow \\ Small number of cells \\ \hookrightarrow \\ Retro-action of cuboid cells on the \end{array}$
prolifération	$C \rightarrow C + C$	γC	differentiation rate : is it relevant ? $\hookrightarrow$ From $(F_0, 0)$ to $(0, C_{\tau})$

- Theoretical study
  - $\Rightarrow$  Statistics of the "transition" time  $\tau$  to reach F = 0.
  - $\Rightarrow$  Variability of final cuboid cells ( $\mathbb{E}[C_{\tau}] < \infty$  if  $\gamma < \alpha + \beta$ )
  - ⇒ Impact of parameters e.g. on qualitative dynamics (progressive vs abrupt)
- Parameter calibration : lack of identifiability. Either  $\gamma << 1$  and  $\beta$  unconstrained, or  $\gamma > 1$  and  $\beta/\gamma >> 1$



Robin et al. Stochastic nonlinear model for somatic cell population dynamics during ovarian follicle activation, (submitted) arXiv :1903.01316

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#### Agreement to data



- $\Rightarrow$  The model can capture both data sets
- $\Rightarrow$  Lack of identifiability (non-conclusive on retro-action)
- $\Rightarrow$  First differentiation, then proliferation (sligtly more concomitant in mutant case)



Robin et al. Stochastic nonlinear model for somatic cell population dynamics during ovarian follicle activation, (submitted) arXiv:1903.01316 \_\_ > < \_> > < \_> > < \_> > < \_> > < \_> > <

## Dynamical model (Multi-type Bellman-Harris Branching process)

- Age and position dependent division rate (cell cycle regulated by the ovocyte)
- At division, unidirectional motion centrifugal
- Cells are independant between each other (Unlimited layer capacity)



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- Age and position dependent division rate (cell cycle regulated by the ovocyte)
- At division, unidirectional motion centrifugal
- Cells are independant between each other (Unlimited layer capacity)



#### Data

• We have counting data of somatic cells in snapshot data, morphological data (diameter) and *order of magnitude of transit times between follicle "type"* 

	t = 0	t = 20	t = 35
‡Data points	34	10	18
Total cell number	$113.89 \pm  57.76$	$885.75 \pm \scriptscriptstyle 380.89$	$2241.75 \pm {\scriptstyle 786.26}$
Oocyte diameter ( $\mu m$ )	$49.31 \pm 8.15$	$75.94 \pm \scriptscriptstyle 10.89$	$88.08 \pm \textbf{7.43}$
Follicle diameter ( $\mu m$ )	$71.68 \pm \texttt{13.36}$	$141.59\ \pm \ {}^{17.11}$	$195.36 \pm {\scriptstyle 23.95}$

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⇒ Can we explain proliferation in concentric layers by a simple model of "division-migration"? Or do physical constraint play important role?

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- $\Rightarrow$  Can we characterize the growth rate of a follicle and spatial repartition of somatic cells?
- $\Rightarrow$  What is the impact of spatial position of a somatic cell on its division rate ?

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