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Ionization Mechanism in a Thermal Spark Discharge

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The formation of thermal sparks generated by nanosecond pulses is studied experimentally and numerically. The increase of the electron number density, up to 10^{19} cm^{-3} , is measured with sub-nanosecond resolution using Stark broadening of N^+ , Stark broadening of H_α , continuum emission of the electron, and the intensity of N^+ lines. Our experimental results are then compared to 0-D kinetic simulations including the electron-impact ionization of excited electronic states of N and O. The electron temperature, in equilibrium with the gas temperature, reaches 42,000K, which agrees with our experimental findings and the literature on the thermal spark.

I. Introduction

Nanosecond Repetitively Pulsed (NRP) discharges are known for being out of equilibrium in preheated air at atmospheric pressure [1]. At ambient pressure, Pai *et al.* identified three regimes of NRP discharges: the corona, the glow, and the spark. The simulations of these three regimes have already been performed [2–6] based on the kinetic mechanisms of Kossyi *et al.* [7] or Capitelli *et al.* [8] which are well-suited for simulations of non-equilibrium plasmas.

However, another regime does not fall in the classification of Pai *et al.*: the thermal spark. At near atmospheric pressures, the thermal spark has been the subject of several studies in recent years. For instance, Lo *et al.* applied a 35-kV single nanosecond discharge in a 3-mm gap (450 Td) and measured a sudden increase of gas temperature from 1200 to 35,000 K in less than 5 ns [9]. This heating was associated with the emission of N^+ lines. The electron number density, measured by Stark broadening of N^+ , reached $n_e = 9 \times 10^{18} \text{ cm}^{-3}$, representing an ionization of 36%. Such high electron number densities and temperatures were also measured by other teams in pin-to-pin configurations [10–14] and nanosecond Dielectric Barrier Discharges [15,16].

In a previous work [13], we compared our results to the literature and demonstrated that, in pin-to-pin configurations, thermal sparks are generated in five stages:

1. Formation of a partially ionized plasma across the inter-electrodes gap.
2. Formation of a fully ionized filament at the cathode in less than 0.5 ns.
3. Formation of a similar filament at the anode, delayed compared to the cathode filament.
4. Propagation of these two fully ionized filaments toward each other's.
5. Merging of these filaments. The thermal spark is formed.

The fully ionized filaments were found to be at thermal and chemical equilibrium. Although the thermal spark formation was characterized, the reasons behind the abrupt formation of the filaments remained unclear.

In this paper, we investigate the formation of a thermal spark generated in a pin-to-pin configuration. First, in Section II, we describe our experimental setup and, in Section III, we measure the increase of the electron number

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density of the thermal spark. Then, in Section IV, we briefly describe a kinetic mechanism developed in this work and, in Section V, we compare the results of simulations and measurements.

II. Experimental setup

The experimental setup, presented in Figure 1, is extensively described in our previous study [13]. Briefly, a nanosecond discharge is generated (FID FPG 30-100MC4K) at 1 kHz between two pin electrodes separated by 1.2 mm. The experiments are performed in ambient air at 1 bar. In specific experiments, we monitor the H_α Stark broadening in a mixture composed of ambient air and H_2 (3.7%). An Optical Emission Spectroscopy (OES) setup is used to measure the electron number densities and the electron temperatures. The discharge is placed at the focal point of an off-axis parabolic mirror ($f = 10$ cm), as shown in Figure 1. The collimated light from the plasma is then refocused by a second parabolic mirror ($f = 20$ cm) onto the monochromator (Acton 500i) entrance slit. The monochromator is equipped with two gratings of 300 and 1800 $\text{gr}\cdot\text{mm}^{-1}$, both blazed at 500 nm. An ICCD camera (Pi-MAX4) coupled to the monochromator is used to record the spectra with a minimum gate of 450 ps. The pitch of the pixels on the ICCD is 13 μm . A HeNe laser (Thorlabs) is used to determine the instrumental broadening of the OES system.

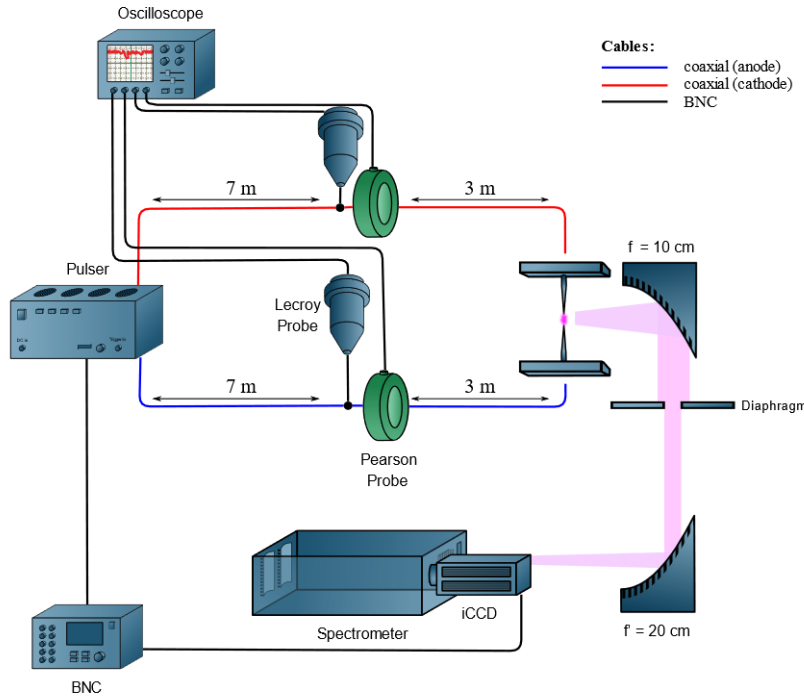


Figure 1 Experimental setup. The length of the coaxial cables is different from previous work [13].

The discharge is generated by a positive 10-ns pulse (sent to the anode) and a negative 10-ns pulse (sent to the cathode). Hence, the energy deposition is monitored by two high voltage probes (LeCroy PPE20kV) and two current transformers (Pearson 6585) connected to an oscilloscope (LeCroy HDO 6104). The measured voltage and current are represented in Figure 2. Note the difference in amplitude between the incident pulses at the anode and at the cathode is only due to a technical peculiarity of the pulser.

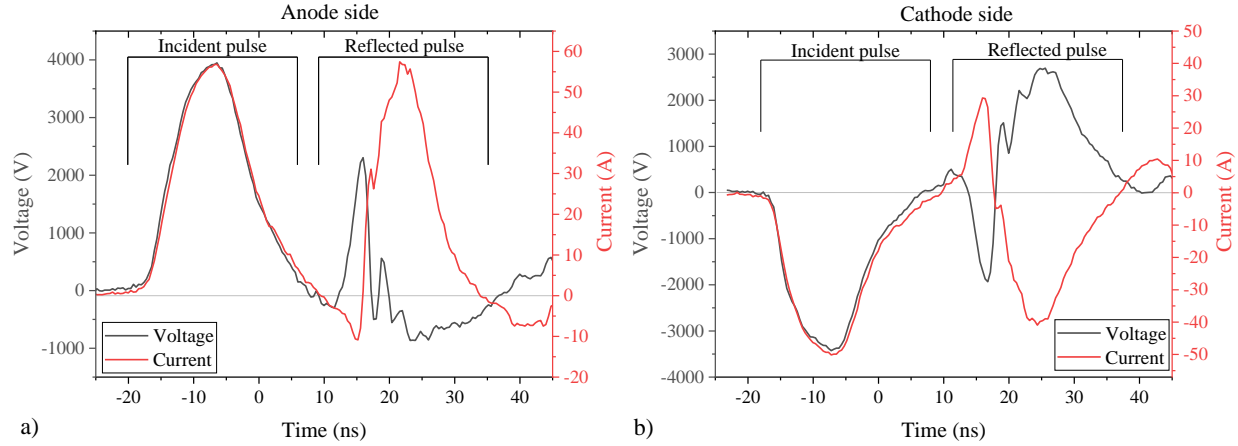


Figure 2 Measured voltage and current on a) the anode and b) the cathode sides.

The instantaneous power is the product of the voltage, U , and current, I . The total energy, E , is the time integration of the power in Eq. 1, where the indices 'an' and 'cat' denote the anode and the cathode, respectively.

$$E(t) = E_{cat}(t) + E_{an}(t) = \int_0^t I_{cat}(t)U_{cat}(t)dt + \int_0^t I_{an}(t)U_{an}(t)dt \quad \text{Eq. 1}$$

The instant $t = 0$ ns is defined as the moment the nanosecond pulse reaches the electrode, after consideration of the propagation time in the coaxial cable. As shown in Figure 3, the incident anode and cathode pulses carry 3.9 mJ to the interelectrode gap. Due to impedance mismatch between the coaxial cable and the plasma, a part of the energy (1.5 mJ) is reflected to the generator, defined as the upstream direction. Another impedance mismatch on the generator (on OFF position at $t > 10$ ns) leads to a new reflection. Thus, a 2nd pulse is sent in the downstream direction and is detected at $t = 75$ ns. The second pulse carries ~ 0.8 mJ and deposits ~ 0.25 mJ in the interelectrode gap. For the same reasons, a 3rd pulse is detected at $t = 150$ ns and deposits another 0.25 mJ. This sequential energy deposition was already observed in previous work [13,17,18] and could explain the "ringing" observed in Ref. [19]. In the following, we study the electron number density increase for $t < 20$ ns.

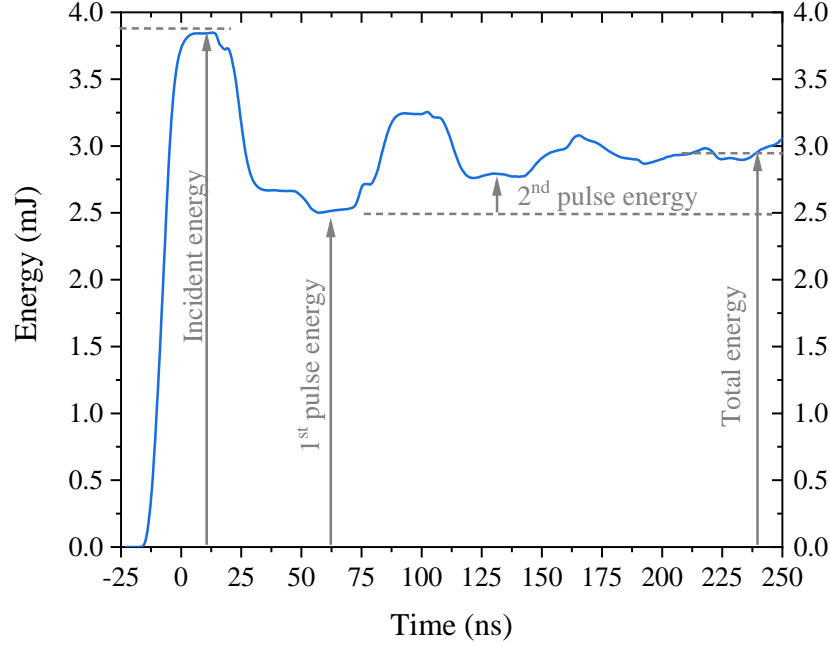


Figure 3 Total transmitted energy according to Eq. 1. Approximately 2.5, 0.25, and 0.25 mJ are deposited in the 1st, 2nd, and 3rd pulses, respectively.

Table 1 Summary of the experimental parameters of this work, compared to those of a previous study [13].

	Setup #1 in [13]	Setup #2 in [13]	This work
Electrode polarities	Cathode-Anode	Cathode-Ground	Cathode-Anode
Interelectrode gap	0.9 mm	2 mm	1.2 mm
Repetition frequency	10 Hz (single pulse)	10 Hz (single pulse)	1 kHz
Deposited energy	2.5 - 3.5 mJ per pulse	2.5 mJ per pulse	2.5 mJ (0 – 20 ns) 3.0 mJ (0 – 100 ns)
Maximal ΔV	8.5 kV	5.5 kV	8 kV
Pressure	58 mbar – 1 bar	1 bar	1 bar
Gas	Ambient air	Ambient air + 1.6% of H ₂	Ambient air (+ 3.7% of H ₂)

We summarized in Table 1 the experimental parameters used in the present study. For comparison, the experimental parameters of our previous work, performed in a single pulse regime, are also shown.

III. Measurement of the electron number density

In this section, we measure the ion and electron number density using four methods:

1. Stark broadening of H _{α} , in Section III.A
2. Stark broadening of N⁺, in Section III.B
3. Calibrated line intensity of N⁺ and O⁺, in Section III.B
4. Continuum emission of electrons, in Section III.C

The measurements are spatially resolved, but only the results obtained near the cathode are presented in this paper.

A. Stark broadening of H α

The electron number density can be accurately measured using the Stark broadening of the H α line at 656 nm. The Half-Width at Half Maximum (HWHM) of H α is the sum of several broadening mechanisms: Doppler, resonant, natural, Van der Waals, Stark, and instrumental. In the following, we estimate the non-Stark contributions to the HWHM of the H α line, and show they are negligible. The broadening formulas used in the present work were initially developed by Griem [20] and simplified for H β in Ref. [21]. The work of Ref. [21] was recently improved and extended to H α , H β , O, N, O $^+$, N $^+$ in Ref. [13].

In the following, we assume that the gas transformation is isochoric up to $t = 20$ ns and take the ambient number density, $2.7 \times 10^{19} \text{ cm}^{-3}$, for initial conditions. The gas temperature varies from 300 K (initial condition) to $\sim 30,000$ K (fully ionized plasma). Based on the gas temperature and number density, we estimate the Doppler, resonant, and Van der Waals HWHM in Table 2 [13]. They are negligible compared to the Stark broadening measurements.

Table 2 Estimation of the H α line HWHM (in pm) for the present conditions based on the formula given in Ref. [13]. See also Table 3 for the estimation of the Van der Waals HWHM.

Time (ns)	T_{gas} (K)	Doppler (pm)	Resonant (pm)	Van der Waals (pm)	Instrumental broadening (pm)	Stark (pm)
0 – 4	300 – 3000	4 - 12	<1	< 34	48 (1800 gr·mm $^{-1}$)	100 – 600
3 – 20	3000 – 30,000	12 - 38	<1	< 267	342 (300 gr·mm $^{-1}$)	600 – 23,000

The Doppler HWHM increases with the square root of the gas temperature. Thus, the Doppler width will be considered constant. The number density of atomic hydrogen is estimated to be below 10^{15} cm^{-3} , resulting in a negligible resonant broadening (HWHM < 1 pm). The natural broadening is also negligible.

The Van der Waals HWHM results from the perturbation of the H α transition by non-hydrogenic particles (N $_2$, O $_2$, O, N, O $^+$, and N $^+$). The sum over all the contributions is given in Eq. 2, where N is the total gas density, T_{gas} the gas temperature, and x_{pert} the perturber mole fraction. The coefficients γ_{pert} are specific to each couple transition – perturber and are calculated in Ref. [13].

$$\Delta\lambda_{\text{Van der Waals}}[nm] = \frac{N}{2.7 \times 10^{19} \text{ cm}^{-3}} \left(\frac{T_{\text{gas}}}{273 \text{ K}} \right)^{0.3} \sum_{\text{pert}} \left(\frac{\gamma_{\text{pert}}}{100} x_{\text{pert}} \right) \quad \text{Eq. 2}$$

We simplify the sum in Eq. 2 using γ_{mean} defined in Eq. 3.

$$\gamma_{\text{mean}} = \sum_{\text{pert}} (x_{\text{pert}} \gamma_{\text{pert}}) \quad \text{Eq. 3}$$

In Table 3, the value of γ_{mean} is calculated in air. During the thermal spark formation, the gas composition varies from N $_2$ / O $_2$ at 300 K, to N / O at 20,000 K and finally N $^+$ / O $^+$ at 40,000 K. For these compositions, the Van der Waals HWHM varies from 34 to 267 pm. For comparison, when the plasma is partially ionized, a Stark HWHM of 34 pm corresponds to $n_e \sim 10^{14} \text{ cm}^{-3}$, which is well below our sensitivity limit. When the gas is fully ionized and $T = 40,000$ K, a Stark HWHM of 267 pm corresponds to $3 \times 10^{16} \text{ cm}^{-3}$, which is three orders of magnitude lower than the measured electron number density.

Table 3 Estimated γ_{mean} coefficient and Van der Waals broadening HWHM of the H α line in ambient air at 300 K, dissociated air at 20,000 K, and fully ionized air at 40,000 K.

Composition	γ_{mean}	T (K)	N (cm $^{-3}$)	$\Delta\lambda_{\text{vdW}}$ (HWHM – pm)
N $_2$ / O $_2$	3.36	300	2.7×10^{19}	34
N / O	3.64	20,000	5.4×10^{19}	150
N $^+$ / O $^+$	3.26	40,000	5.4×10^{19}	267

The Stark HWHM can be calculated** with Eq. 4 [22,23].

$$\frac{n_e}{10^{17} \text{ cm}^{-3}} = \left(\frac{\Delta\lambda_{\text{Stark}, \text{H}\alpha}}{0.549 \text{ nm}} \right)^{1.47134} \quad \text{Eq. 4}$$

The instrumental broadening mainly depends on the spectrometer slit opening and the grating. We used two gratings in this study to follow the variations of the H α HWHM from 0.1 nm to 20 nm. The corresponding instrumental HWHM is given in Table 2. A typical example of the H α line fitting is shown in Figure 4. The H α width uncertainty is about $\pm 20\%$, which leads to a 30% uncertainty on the n_e measurement with this technique.

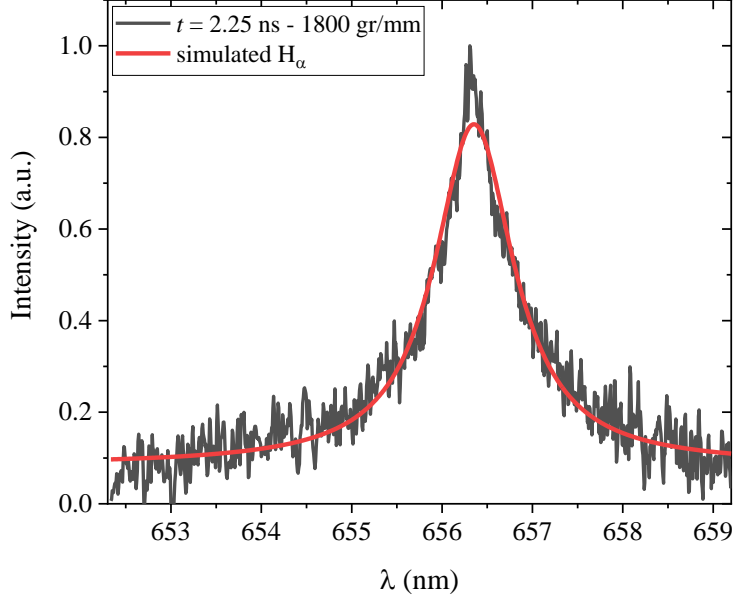


Figure 4 Fitting of the H α line at $t = 2.25$ ns (1800-gr/mm grating).

In this work, some of the Stark broadening measurements are performed during the high-voltage pulse. In Ref. [24], it was shown that the applied electric field can have an impact on the Stark broadening. In that case, the width of the spectral line would be related to the current density instead of the electron number density. In Ref. [24], expressions are derived for the Stark broadening of H α and H β generated by the sum of two fields:

- A microscopic field, arising from the presence of ions and electrons in the plasma. *This is the typical Stark broadening effect.*
- A macroscopic field applied in one direction during the experiment. *This field can interfere with the Stark broadening.*

According to Bastien & Marode, the H β Stark broadening is mainly due to the shifting of intense external lines caused by the static ions' microfield [24]. The addition of an external field has, therefore, an impact on the H β Stark broadening. On the other hand, Bastien & Marode showed that the addition of an external field has a weak impact on the H α lineshape. For instance, at $n_e = 10^{17} \text{ cm}^{-3}$ and $T_e = 10,000 \text{ K}$, the Stark HWHM of H α remains independent of the applied field up to at least^{††} $12 \text{ kV}\cdot\text{mm}^{-1}$, see Table 1 of [24]. In our experiments, the maximum applied field is $6.7 \text{ kV}\cdot\text{mm}^{-1}$

** The relation given initially by Gigosos *et al.* [22] must be corrected by a factor 2 as noted by Konjević *et al.* [23].

†† Bastien & Marode calculated the effect of the external field up to four times the Holtzmark field, where the Holtzmark field is, in SI unit:

$$E_{\text{Holtzmark}} = \frac{e}{4\pi\epsilon_0 n_e^{2/3}}$$

where e is the elementary charge, ϵ_0 the dielectric constant, and n_e the electron number density.

when $n_e \sim 10^{17} \text{ cm}^{-3}$. Therefore, the applied field does not influence our Stark broadening measurements of H_α during the pulse.

B. Stark broadening and intensity of the N^+ lines

We expect that the plasma will reach full ionization and hence thermal and chemical equilibrium at $T = 30,000 \text{ K} - 50,000 \text{ K}$ [13]. At these temperatures, after an isochoric transformation, the plasma is mainly composed of electrons (50%), N^+ (40%) and O^+ (10%) [25]. Thus, the number density of the ions (N^+ and O^+) is expected to follow n_e . We measure the densities of several excited states of the ions by calibrated OES and infer the total ion density assuming a Boltzmann distribution of the electronic states at the measured electron temperature. The OES calibration is performed using an integration lamp (OL455, Gooch and Housego).

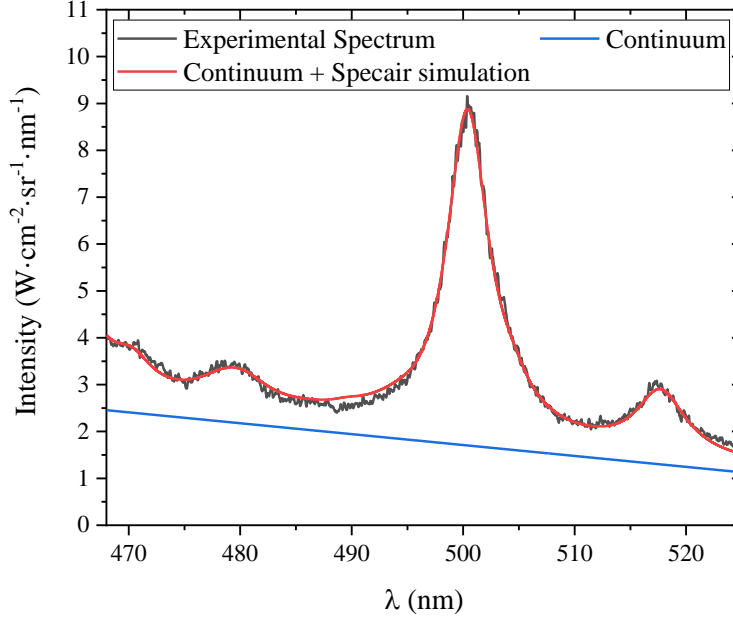


Figure 5 Fit of the N^+ and O^+ emission near the cathode at $t = 9.75 \text{ ns}$. The continuum emission is approximated by a linear function (in blue) and the N^+ and O^+ emission is calculated by Specair (in red). The N^+ and O^+ lines are calculated accounting for self-absorption ($\Delta l = 15 \mu\text{m}$). The fit gives $n_e = 2.0 \times 10^{19} \text{ cm}^{-3}$, $n_{N^+} = 3.6 \times 10^{18} \text{ cm}^{-3}$, $n_{O^+} = 1.2 \times 10^{17} \text{ cm}^{-3}$, and $T_e = 35,000 \text{ K}$ (accuracy discussed in the text).

A typical spectrum, shown in Figure 5, is fitted with a Specair calculation [21,26]. For N^+ lines, the Stark line broadening dominates the others and the lineshape fit provides another measurement of n_e . The uncertainty on the Stark broadening fitting (and n_e determination) remains below 20%. The continuum radiation (assumed to be linear) is subtracted and studied in Section III.C. All electronic states of the ions are assumed to follow a Boltzmann distribution at T_e . The measured electronic temperature ($T_e = 35,000 \text{ K}$) corresponds to values usually reported in thermal spark literature [9,12,13]. In the following, we discuss the determination of N^+ and O^+ number density.

In the work of Shcherbanev *et al.* [16], it was reported that the emission of filamentary SDBD was indeed the sum of two concentric channels. In their case, the intense N^+ and continuum emissions were emitted from the central core, whereas a weaker N_2 emission originated from the outer shell. Shcherbanev *et al.* reported a filament Full Width at Half Maximum (FWHM) of $18 \pm 2 \mu\text{m}$. In a configuration similar to ours, Orriere measured the FWHM of a thermal spark [27]. He found an FWHM of $50 \mu\text{m}$ for a 6-kV discharge of 20 ns applied across a 1-mm gap between the electrodes^{‡‡}. However, no filter was used and the measurement of Orriere *et al.* is an upper bound of their thermal

^{‡‡} For a 2-kV pulse across 200- μm gap, Orriere measured a FWHM of $40 \mu\text{m}$.

spark diameter. Finally, in a 25-kV discharge of 40 ns at ambient conditions, Parkevich *et al.* measured the n_e distribution of a thermal spark by interferometry [14]. Their discharge looked homogeneous with conventional lenses but was indeed composed of several fully ionized filaments, 10 – 50 μm in diameter. Finally, Lo *et al.* clearly observed a constriction of the discharge channel during the transition to the thermal spark in a microsecond pulsed discharge in air [9].

In the present study, the plasma column diameter is estimated with a 10-nm bandpass filter centered at 480 nm (Hard Coated OD 4.0 10-nm Bandpass Filter, Edmund Optics). An accurate measurement is challenging with our present setup because of shot-to-shot fluctuations (of the order of a few 10s of microns) and because the column width is comparable with the pixel width, which could result in pixel bleeding. Based on these measurements, we assume in the following that the plasma diameter is constant in time and of the order or less than the pixel resolution, *i.e.* $\Delta l = 15 \mu\text{m}$. We note that this value is comparable with the measurements of Shcherbanev *et al.*, Orriere, and Parkevich *et al.*

The accuracy of the T_e measurements is $\pm 10\%$. This uncertainty has strong consequences on the number density of the ions. For instance, in Figure 6, we show three N^+ spectra calculated at $35,000 \text{ K} \pm 10\%$. The N^+ number density of each spectrum in Figure 6 is adjusted to conserve the peak intensity at $\lambda = 500 \text{ nm}$. This example shows that a 10% variation on T_e results in a factor-two increase/decrease in the N^+ number density.

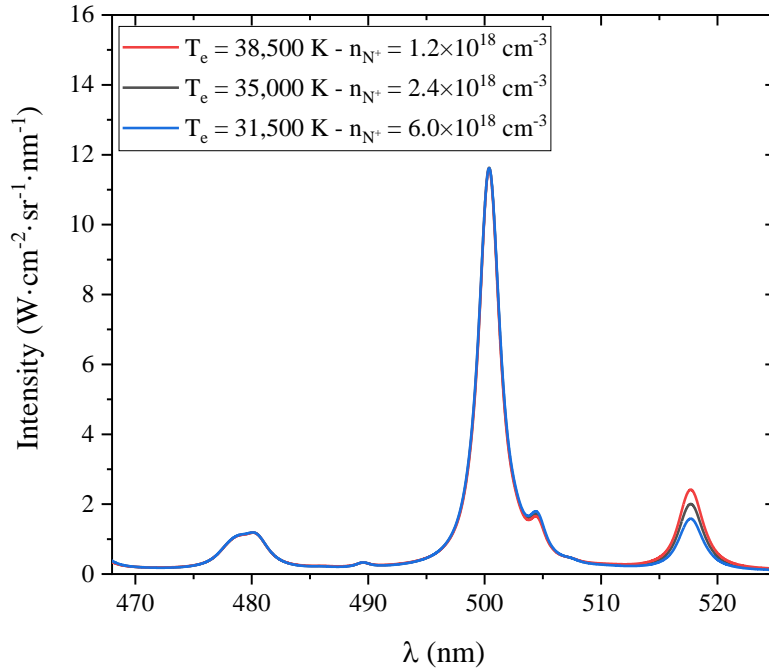


Figure 6 Influence of the temperature on the N^+ number density. Three spectra are calculated using Specair [21,26] at $35,000 \text{ K} \pm 10\%$, accounting for the slight self-absorption in a $40\text{-}\mu\text{m}$ plasma column.

Note that the Stark broadening constants of the lines at 518 nm are not available in the literature above 28,000 K. Their values were adjusted in previous work, see the appendix in Ref. [13], and are consistent with the values found at lower temperatures in the literature, but could add uncertainty to the measurement. Thus, we estimate that the statistical error on the measurements of N^+ and O^+ number densities is about a factor of two. The impact of the plasma diameter estimation is discussed in Section III.D. Nevertheless, we conclude that the positive ion (N^+ and O^+) number density is in the range $10^{18} - 10^{19} \text{ cm}^{-3}$, which is consistent with the maximal electron number density measured by Stark broadening ($\sim 10^{19} \text{ cm}^{-3}$).

C. Continuum radiation of electrons

As shown in several works, continuum radiation can be significant in laser-induced plasmas [28], DBD discharges [16], or pin-to-pin nanosecond discharges [10]. We decompose the plasma volumetric emission coefficient, ε , in two terms: the bound-bound emission coefficient, ε_{bb} , and the continuum emission coefficient, ε_c .

$$\varepsilon = \varepsilon_{bb} + \varepsilon_c \quad \text{Eq. 5}$$

The bound-bound contribution was discussed in the previous section. The continuum emission is the sum of the free-free radiation (also called Bremsstrahlung) and the free-bound radiation (also called recombination continuum). The continuum emission coefficient is given in Eq. 6, where n_e and n_i are the electron and ion number densities, Z_i the ion charge, T_e the electron temperature, ξ the free-bound Gaunt factor, and G the free-free Gaunt factor [29].

$$\varepsilon_c(\lambda, T_e, n_e) = C_8 Z_i \frac{n_e n_i}{\lambda^2 \sqrt{T_e}} [\xi(1 - e^{-u}) + G e^{-u}] \quad \text{Eq. 6}$$

If more than one ion is present in the mixture, the total continuum radiation will be a sum over Z_i , i being the ion species. In the present case, we consider that N^+ is the dominant ion and $Z_i = 1$. If the plasma is mainly composed of neutral atoms, another formulation must be used, see Refs. [30,31]. The C_8 constant can be determined with Eq. 7, where e is the electron charge, k_b the Boltzmann constant, c the speed of light, and m_e the electron mass.

$$C_8 = \frac{16\pi e^6}{3c^2 \sqrt{6\pi m_e^3 k_b}} = 1.63 \times 10^{-34} [\text{W} \cdot \text{m}^3 \cdot \text{nm} \cdot \text{K}^{0.5} \cdot \text{sr}^{-1}] \quad \text{Eq. 7}$$

The dimensionless variable u is defined in Eq. 8, where h is the Planck constant, k_b the Boltzmann constant, c the speed of light and λ the wavelength.

$$u = \frac{hc}{\lambda k_b T_e} \quad \text{Eq. 8}$$

The free-free Gaunt factor of N^+ (and O^+) at $\lambda = 500$ nm varies from $G = 1.08$ to $G = 1.1$ for T in the range 32,000 – 42,000 K, interpolating^{§§} the results of Ref. [32]. The free-bound Gaunt factor should be averaged on the atom's final states (*i.e.* after the electron has recombined with the ion). The free-bound gaunt factor at $\lambda = 500$ nm = 0.18 Ry ranges between $\xi = 0.8$ and $\xi = 1.2$ depending on the final bound state, see the values calculated for any ions in Table 1 of Ref. [33]. Therefore, we assume $\xi = 1$ and $G = 1.09$ in the present application. These coefficients are assumed to be accurate^{***} within 10%.

Assuming $n_e = n_i$, we obtain n_e [m^{-3}] as a function of λ [nm], the volumetric emission coefficient ε_c [$\text{W} \cdot \text{m}^{-3} \cdot \text{sr}^{-1} \cdot \text{nm}^{-1}$], and T_e [K], see Ref. [29]:

$$n_e^2 = \frac{\lambda^2 \sqrt{T_e}}{C_8} \frac{1}{\xi(1 - e^{-u}) + G e^{-u}} \varepsilon_c \quad \text{Eq. 9}$$

We can relate ε_c with the continuum intensity I_c [$\text{W} \cdot \text{m}^{-2} \cdot \text{sr}^{-1} \cdot \text{nm}^{-1}$], the absorption coefficient k [m^{-1}], and the plasma width Δl [m].

^{§§} We used the ChiantiPy Python package [48,49] at <https://github.com/chianti-atomic/ChiantiPy>.

^{***} If needed, a more precise value could be obtained using the summation performed by the ChiantiPy Python Package with the values of Ref. [50]. As described later, the dominant uncertainty is on the plasma thickness.

$$I_c = \varepsilon_c \frac{1 - \exp(-k\Delta l)}{k} \quad \text{Eq. 10}$$

As in Eq. 5, the absorption coefficient, k , is the sum of the continuum and bound-bound absorption, k_{bb} and k_c , respectively. We assume that the absorption coefficient is dominated by the bound-bound contribution, *i.e.* $k \sim k_{bb}$. For a plasma diameter of 15 μm and $n_e = n_{N^+} = 10^{19} \text{ cm}^{-3}$, we calculated with Specair that $k_{bb}\Delta l < 0.5$ between 460 and 530 nm. Based on this estimation, the plasma is optically thin, *i.e.* $I_c \approx \varepsilon_c \Delta l$. This approximation leads to, at most, an overestimation of ε_c by 40%. *We will see in the next paragraph that this uncertainty is acceptable.* Finally, Eq. 9 can be further simplified as Eq. 11 where n_e [m^{-3}] is given as a function of Δl [m] the plasma width, I_c [$\text{W}\cdot\text{m}^{-2}\cdot\text{sr}^{-1}\cdot\text{nm}^{-1}$] the continuum intensity, T_e [K] the electron temperature, and λ [nm] the wavelength of observation.

$$n_e = \left(\frac{\lambda^2 \sqrt{T_e}}{C_8} \frac{1}{\xi(1 - e^{-u}) + Ge^{-u}} \frac{I_c}{\Delta l} \right)^{\frac{1}{2}} \quad \text{Eq. 11}$$

The uncertainty of this measurement is now discussed. Thanks to the power 1/2 on the right-hand side of Eq. 11, the large uncertainties mentioned earlier will be halved in the final result. The uncertainty on T_e is about 10%. The free-free and free-bound coefficients vary slowly with T_e and, in this case, are known within $\pm 10\%$. The intensity calibration of the absolute spectrum was performed with other sources and are found to be accurate within about $\pm 20\%$. Thus, considering the thin plasma maximal uncertainty, the maximal uncertainty on ε_c is +20% and -60%. The plasma thickness, Δl , is assumed to be exact and discussed later. We find that the n_e measurement by continuum emission is accurate by -50% and +30% after propagation of uncertainty.

D. Comparison of the four measurements

In Figure 7, we compare electron number densities measured with the four different techniques applied in this section. The H_α line measurements are performed using two gratings, with overlap between the acquisitions to ensure reproducibility. From $t = 1.25 \text{ ns}$ to $t = 8 \text{ ns}$, n_e increases from 10^{16} to $3 \times 10^{19} \text{ cm}^{-3}$. Note that the steep increase of the electron number density (more than one decade) at $t = 4 \text{ ns}$ corresponds to the filament formation. For $t > 10 \text{ ns}$, the electron density slowly decays to $5 \times 10^{18} \text{ cm}^{-3}$ at 25 ns.

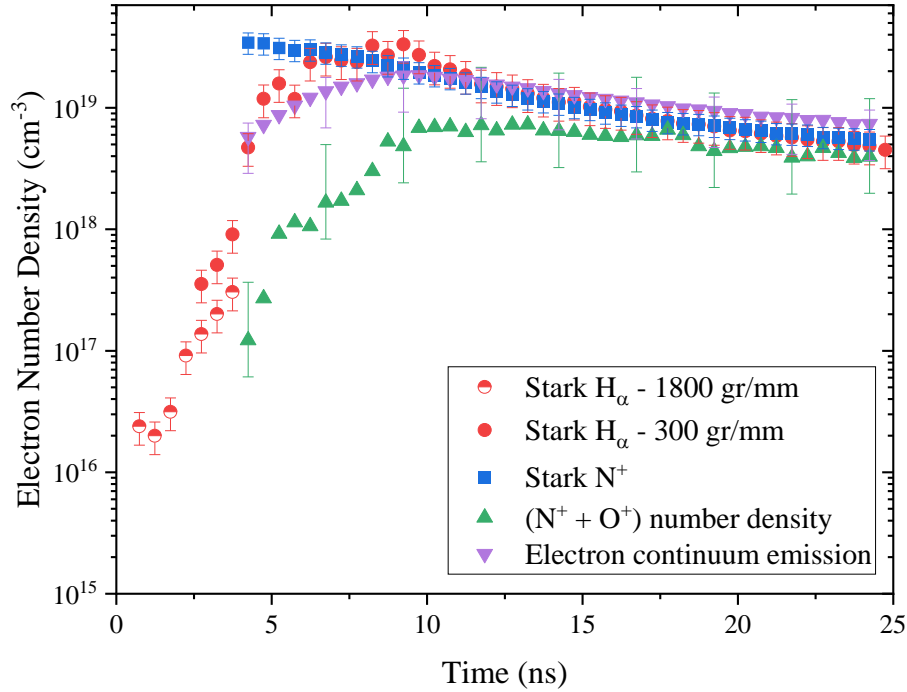


Figure 7 Evolution of the electron number density near the cathode measured with Stark broadening of H_α (red circles), Stark broadening of N^+ (blue squares), intensity of N^+ lines (green triangles), and continuum radiation (purple triangles). We assumed an optically thin plasma for continuum radiation only (uncertainty propagated in the error bars). The plasma width is taken to be constant and equal to $15 \mu\text{m}$.

We note that the measurements from the Stark broadening of H_α and N^+ are in excellent agreement. The electron number densities measured with the continuum emission and the intensity of N^+ and O^+ lines agree within the uncertainties of each technique for $t > 12 \text{ ns}$. However, at earlier times, the electron densities measured from the absolute OES measurements underestimate the electron number density. This could be because the diameter of the plasma column was overestimated. Since the plasma is neutral, we can use the absolute OES measurements to infer the diameter of the plasma column. To do so, we assume that the ion number density is equal to the electron number density measured by Stark broadening of N^+ , and we adjust the plasma diameter so that the OES measurements yield the same number density as the Stark broadening measurements. This method enables us to determine the evolution of the plasma diameter as a function of time. The inferred plasma diameter evolution is shown in Figure 8. The same procedure is applied for the continuum radiation measurements, using the electron number density determined from the Stark broadening of N^+ as a reference. As shown in Figure 8, the two methods provide a plasma diameter evolution that agrees within a factor of about 2 at times greater than 10 ns. This agreement level is actually quite good, considering the uncertainties on each of these two independent, absolute emission-based techniques. These discharge diameters also correspond to those reported by Shcherbanev *et al.* [16].

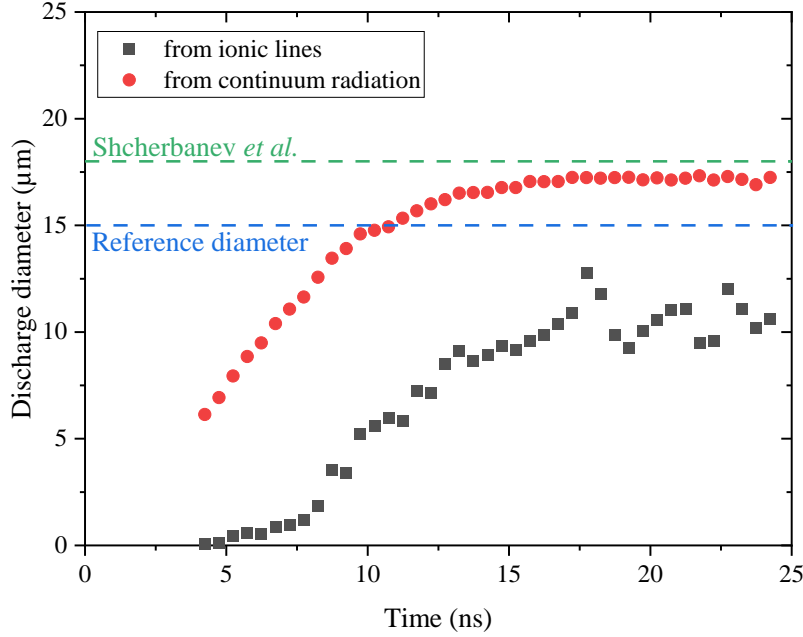


Figure 8 Discharge diameter estimation from the continuum and atomic line radiations. These evolutions are compared to the diameter estimation performed earlier in our conditions (dashed blue line) and the diameter measured in Ref. [16] (dashed green line).

According to the measurement of ionic lines, the measurements obtained with the filtered images overestimated the plasma diameter at all times. According to the continuum radiation, the 15- μm diameter was overestimated for $t < 10$ ns and underestimated at later times. From the graphical comparison, we conclude that a 15- μm diameter is ultimately a reasonable approximation.

IV. Kinetic model description

It has been shown numerically in Ref. [16] that the ionization rate in nanosecond DBD can be increased by the electron impact ionization of $\text{N}_2(\text{B})$ and $\text{N}_2(\text{C})$. We demonstrated in Ref. [34,35] that this process has indeed a significant impact, but that the formation of a fully-ionized plasma by a single nanosecond discharge is rather due to the electron-impact ionization of electronically excited states of N and O. We therefore developed a model of ionization adapted for air discharges, including the ionization of N_2 , N, and O excited states. The complete reaction set is given in Ref. [36, Chap. 5] and only its major features are described here. The mechanism includes N_2 , O_2 , NO, N, O, N_2^+ , O_2^+ , NO^+ , N^+ , O^+ , N^{++} , and O^{++} . The chemistry of ground states species is based on the reaction set of Laux *et al.* [37,38]. We added the excitation, ionization, and dissociation by electron impact of four excited states of N_2 : $\text{N}_2(\text{A})$, $\text{N}_2(\text{B})$, $\text{N}_2(\text{a}')$, and $\text{N}_2(\text{C})$ [39].



We also included the dissociation of O_2 by N_2 excited states quenching [40]. The electron impact ionization of the first three electronic states of O are also included: $\text{O}(^3\text{P})$, $\text{O}(^1\text{D})$, and $\text{O}(^1\text{S})$ [41].



Concerning N electronic states, we included the ionization of eight electronic states of N: $\text{N}(^4\text{S}^0)$, $\text{N}(^2\text{D}^0)$, $\text{N}(^2\text{P}^0)$, $\text{N}(^4\text{P})$, $\text{N}(^2\text{P})$, $\text{N}(^4\text{P}, 2s^22p^4)$, $\text{N}(^2\text{S}^0)$, and $\text{N}(^4\text{D}^0)$ [42,43].



For a field of up to 240 Td at ambient conditions, we demonstrated that the discharge ionization is essentially due to the ionization of the first six electronic states of N [34–36]. The 0-D plasma kinetics and the gas energy equation are solved using ZDPlasKin [44]. The Electron Energy Distribution Function (EEDF) is computed using BOLSIG+ [45,46]. A simplified representation of the kinetic mechanism is given in Figure 9.

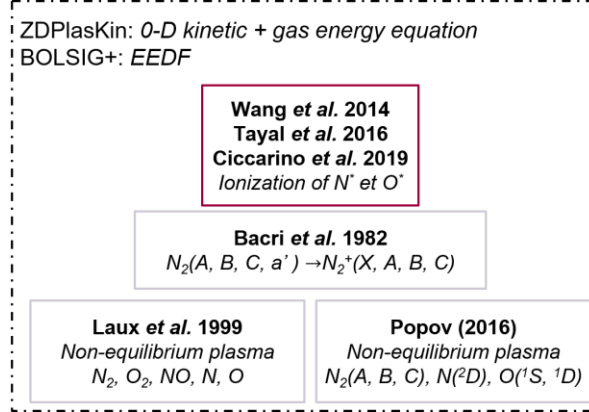


Figure 9 Schematic representation of the reactions included in our mechanism [36] based on the work of Refs. [38–43].

V. Comparison of the numerical kinetics with the experimental findings

We now compare the measurements near the cathode and the simulation. Initial conditions and numerical parameters are listed in Table 4.

Table 4 Initial conditions and numerical parameters. The initial N₂ and O₂ number densities correspond to air at 1 atm and 300 K, and the initial electron and N₂⁺ number densities to typical ionization in streamer discharges.

Initial gas state						Numerical parameters
N ₂ (cm ⁻³)	O ₂ (cm ⁻³)	N ₂ ⁺ (cm ⁻³)	e- (cm ⁻³)	T _{gas} (K)	T _e (K)	Time step (ps)
1.90×10 ¹⁹	5.06×10 ¹⁸	1.00×10 ¹⁴	1.00×10 ¹⁴	300	1000	1.0

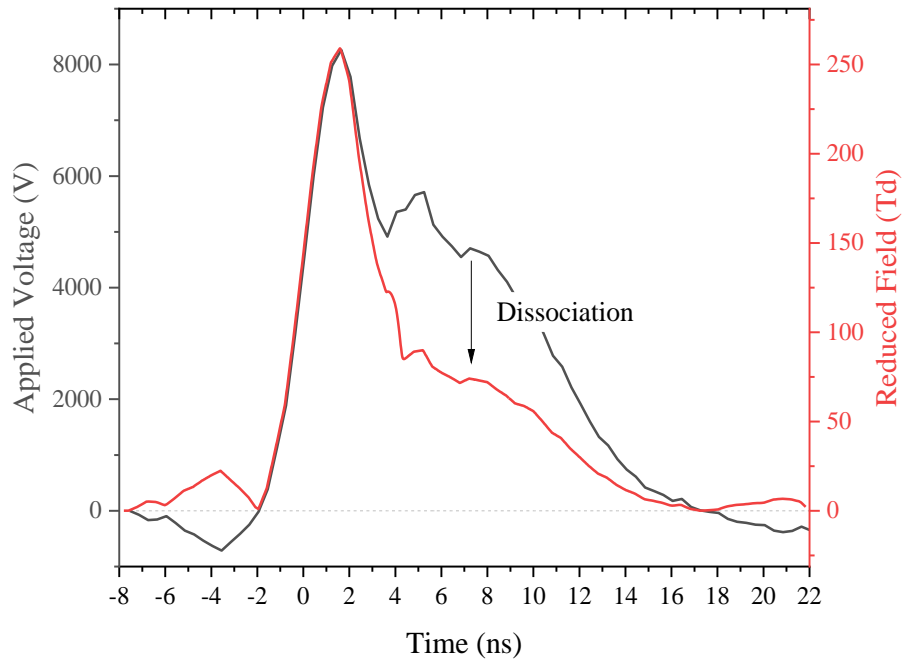


Figure 10 Applied voltage (across the 1.2-mm gap) reconstructed from the difference of incident and reflected voltage (grey line) and reduced field in the simulation (red line).

The applied voltage on the 1.2-mm gap is represented in Figure 10 and was reconstructed from the anode and cathode pulse shapes. The reduced field, E/N , is calculated assuming a Laplacian field between the electrodes. We arbitrarily reduced the reduced field by 6% to account for the cathode fall (500 V at maximal applied voltage). The reduced field is not strictly proportional to the applied voltage because dissociation of N_2 and O_2 increases the gas number density. In BOLSIG+, the reduced field E/N is defined as the ratio of the electric field to the neutral particle density, N_{neutral} . However, the neutral particle number density can drop to negligible values. Thus, the reduced field tends toward infinity and the electron temperature increases above reasonable values. Therefore, we define N as the heavy particle density, *i.e.* $N = N_{\text{ion}} + N_{\text{neutral}}$ [34,35].

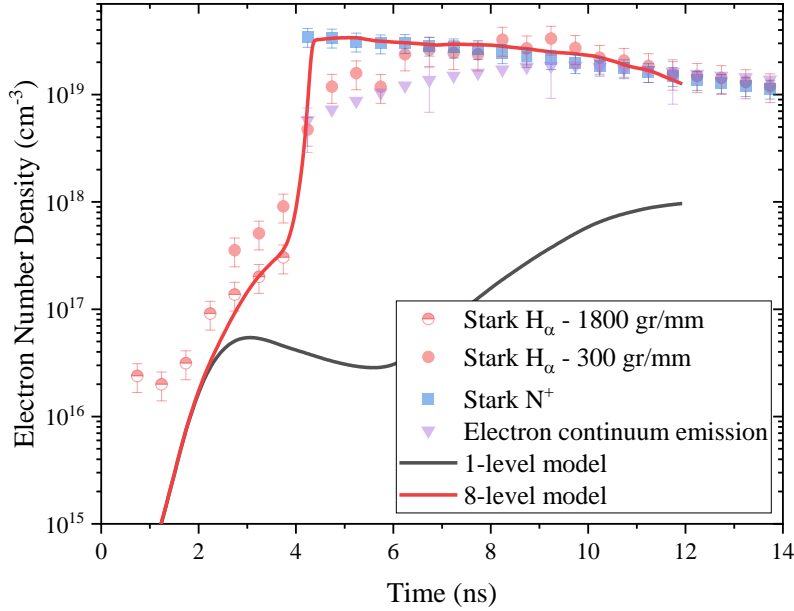


Figure 11 Comparison of the electron number density obtained by simulation (red solid line) with that measured by Stark broadening and continuum emission. If the simulation is run without the ionization of O and N excited states (grey solid line), full ionization is not reached.

Figure 11 compares the evolution of the electron number density measured with Stark broadening of N^+ , Stark broadening of H_α , and the free-free/free-bound continuum, with the electron number density calculated with our kinetic mechanism. The "1-level model" includes only the ionization of N_2 excited states, Reac. 1, and the electron-impact ionization of N and O *ground* states. In this case, n_e reaches at most 10^{18} cm^{-3} at the end of the 10-ns pulse.

With the "8-level model" the electron-impact ionization of the first eight electronic states of N and three electronic states of O are added (*i.e.* including Reac. 1, Reac. 2, and Reac. 3). For $t < 4$ ns, in the "8-level model", the production of electrons is primarily due to the ionization of N_2 excited states. Then, at $t \approx 4$ ns, enough N_2 molecules are dissociated, N^+ ions are produced through stepwise ionization of N, and full ionization is reached. This ionization phase is very abrupt, as reported in the experiments, even though the applied field is decreasing at this instant. The simulation is stopped at $t = 12$ ns.

The decay of n_e at later times is due to an isentropic expansion during at least 100 ns [9,13]. In these simulations, it was assumed that the process is isochoric, which is usually correct in non-thermal nanosecond discharge. We believe the agreement would be improved if the model would include the plasma channel expansion, which could begin as early as $t = 5$ ns, see also Figure 8. The inclusion of the radiative loss, which could be non-negligible, would also represent an improvement. The radiative loss by continuum radiation of the electrons and black body emission is, for instance, included in arc discharge models [47].

VI. Conclusions and future work

In this work, we study the formation of thermal sparks generated at ambient conditions by an 8-kV pulse of 10 ns across a 1.2-mm gap. Near the cathode, we measure the increase of the electron number density using several methods relying on optical emission spectroscopy. First, the Stark broadening of H_α , at 656 nm, and N^+ , at 500 nm, are used. Then, after calibration of the emission spectrum near $\lambda = 500$ nm, we use the continuum radiation of the electron to infer their number density. Assuming the electronic states of N^+ and O^+ are in a Boltzmann equilibrium, we get the ion number density, equal to the electron number density. These four measurements of n_e are in agreement and confirm that the thermal spark's full ionization occurs on a timescale of 0.5 ns. In a second part, we demonstrate using a 0-D

kinetic mechanism that this abrupt ionization can be reproduced if the electron impact ionization of O and N excited states are included.

The agreement between simulations and experiments strongly supports the role of the atomic excited states in the ionization of the thermal spark filaments (steps 2 and 3 of the thermal spark formation). However, other questions remain. As future work, we aim to determine which process triggers the cathode filament generation before the anode one. Also, electron-impact ionization of N and O excited states should be incorporated in a 1-D or 2-D simulation for a description of the filament propagation.

VII. References

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