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Fragmentation dynamics of $\text{Ar}_4\text{He}_{1000}$ upon electron impact ionization: competition between ion ejection and trapping

Nadine Halberstadt¹ and David A. Bonhommeau^{a)2}

¹⁾ *Université Paul Sabatier, CNRS, LCAR UMR 5589, 31062 Toulouse, France.*

²⁾ *Université de Reims Champagne Ardenne, CNRS, GSMA UMR 7331, 51097 Reims, France.*

The fragmentation upon electron impact ionization of $\text{Ar}_4\text{He}_{1000}$ is investigated by means of mixed quantum-classical dynamics simulations. The Ar_4^+ dopant dynamics is described by a surface hopping method coupled with a diatomics-in-molecules model to properly take into account the multiple Ar_4^+ electronic surfaces and possible transitions between them. Helium atoms are treated individually using the zero-point averaged dynamics (ZPAD), a method based on the building of an effective He-He potential. Fast electronic relaxation is observed, from less than 2 ps to ~ 30 ps depending on initial conditions. The main fragments observed are Ar_2^+He_q and Ar_3^+He_q ($q \leq 1000$), with a strong contribution of the bare Ar_2^+ ion, and neither Ar^+ nor Ar^+He_q fragments are found. The smaller fragments ($q \leq 50$) are found to mostly come from ion ejection whereas larger fragments ($q > 500$) originate from long-term ion trapping. Although the structure of the trapped Ar_2^+ ions is the same as in the gas phase, trapped Ar_3^+ and Ar_4^+ are rather slightly bound $\text{Ar}_2^+ \cdots \text{Ar}$ and $\text{Ar}_2^+ \cdots \text{Ar} \cdots \text{Ar}$ structures (*i.e.*, an Ar_2^+ core with one or two argon atoms roaming within the droplet). These loose structures can undergo geminate recombination and release Ar_3^+He_q or Ar_4^+He_q ($q \leq 50$) in the gas phase and/or induce strong helium droplet evaporation. Finally, the translational energy of the fragment center of mass was found suitable to provide a clear signature of the broad variety of processes at play in our simulations.

Keywords: mixed quantum-classical dynamics, superfluid helium nanodroplets, ionic-rare-gas clusters, ionization induced fragmentation, zero-point energy, ejection, trapping.

^{a)} Author to whom correspondence should be addressed. Electronic mail: david.bonhommeau@univ-reims.fr

I. INTRODUCTION

At the very low temperature of their formation, $T \approx 0.37\text{ K}$,¹ superfluid helium nanodroplets have revealed to be an ideal environment to perform high resolution spectroscopy,^{2,3} to form molecular assemblies that would be unstable in the gas phase,⁴ or to grow metallic nanocluster wires which can be deposited on surfaces for applications in optics or catalysis.⁵ These applications are based on the helium superfluid properties at low temperature (no viscosity, no entropy). However, the property of frictionless motion is only valid at low energy excitations. Upon ionization of a doped droplet, the electronic hole initially created on a helium atom is prone to migrate to the neutral dopant, the efficiency of this charge transfer depending on the droplet size and dopant nature.⁶⁻¹¹ The ensuing dopant ionization is likely to make it dissociate, a process which is well known for rare-gas clusters where the large equilibrium structure difference between the neutral cluster and the parent ion, as well as the availability of multiple excited electronic states of the latter, can bring a lot of internal energy into the process.¹²⁻²⁰ In this case, the speed of the fragmenting dopant atoms usually exceeds the Landau critical velocity, $v_L \approx 55 - 60\text{ m s}^{-1}$ at $T = 1\text{ K}$ and $p = 1\text{ atm}$.²¹ These atoms thus undergo a friction force due to the helium environment. If their velocity is not too large they are trapped inside the droplet which can lead to geminate recombination²² or “caging”.

The study of the cage effect exerted by helium atoms on ionized dopants has attracted a lot of interest during the past decades. For instance, electron impact ionization of SF_6 in a helium droplet only yields SF_6^+ and SF_5^+ whereas F^+ and all the SF_n^+ ($n=0-5$) fragments are produced upon gas phase ionization at $T = 300\text{ K}$.^{7,23} This result evidenced a significant hindering of the fragmentation by the surrounding helium atoms. This caging is even more efficient for NO_2^+ whose fragments remain in the droplet and are therefore prone to recombine before detection.²⁴ Assuming thermal evaporation, the ejection of a single helium atom from large nanodroplets is expected to dissipate about 5 cm^{-1} of energy, which should provide an easy way of assessing the cooling power of a helium droplet.^{6,25,26} However, Lewis et al.²⁷ found that the first 5000 helium atoms removed about $22\text{ cm}^{-1}/\text{atom}$ in the case of triphenylmethanol (TPM) electron impact ionization, although the cooling from 10 000 to 40 000 helium atoms only removed $0.16\text{ cm}^{-1}/\text{atom}$. A similar nonthermal evaporation has been observed for HCN molecules whose fragmentation could be accurately measured by coupling

helium droplet mass spectrometry and infrared laser spectroscopy.²⁸ More recently, Braun et al. investigated the translational dynamics of alkyl iodides photodissociated in helium nanodroplets.^{29,30} Besides the expected influence of droplet size on caging, they noticed that CF_3 and C_2H_5 photofragments escaped the helium droplets by nonthermal direct processes with speed distributions properly modeled by assuming independent binary hard-sphere collisions between the fragments and the surrounding helium atoms. On the contrary, CH_3^+ fragments were only detected for small photoexcited droplets in velocity map images, which lead them to conclude that the CH_3 and I photofragments were subject to recombinations.³¹

The significant caging by helium atoms observed experimentally is in stark contrast with the theoretical results obtained by Takayanagi et al. for the photodissociation of Cl_2 in He_{200} .³² These authors took into account quantum effects in their model by combining quantum wavepacket dynamics for Cl_2 and path integral centroid molecular dynamics for helium atoms. Dissociation of Cl_2 occurred in almost 100% of the trajectories. In a more recent study combining He-TDDFT for the helium density and a wave packet description of the Cl-Cl coordinate, Vilá *et al.*³³ also observed complete dissociation of Cl_2 and escape of Cl fragments from a droplet of up to 500 ^4He atoms, together with the ejection of only up to 10 ^4He atoms within the first 3 ps (about 50 atoms after 150 ps)³⁴, even though 91% of the diatomic energy was released in the droplet. Interesting quantum interferences in the velocity distributions were assigned to the effect of the surrounding helium environment.³⁵

We have previously studied the fragmentation dynamics upon electron impact ionization of small neon-doped helium clusters, $\text{Ne}_n^+\text{He}_{100}$ ($n = 4 - 6$), using a mixed quantum-classical method³⁶ where the nonadiabatic dynamics of the central neon cluster was modeled by surface hopping techniques while helium atoms moved classically on an effective potential-energy surface (PES) including average zero-point effects (ZPAD method).^{37,38} The results showed that Ne_n^+ fragmentation was mostly completed within the first 30 ps. By comparing with gas phase ionization, the fragment distributions revealed some caging (Table IX in Ref. 38) although in a minor proportion. For instance, fewer fragments contained Ne^+ (2.6% instead of 11.2%, for Ne_4 ionization in He_{100} and in gas phase, respectively), and some Ne_3^+ -containing fragments were observed (10.5%) subsequent to Ne_6 ionization in He_{100} rather than traces (0.1%) in gas phase. In addition, this study evidenced a dopant ejection mechanism as well as nonthermal evaporation of helium atoms, with $28 - 45 \text{ cm}^{-1}/\text{atom}$ lost on average depending on the cluster size. Finally, Ne_p^+ ($2 \leq p \leq n$) and Ne_p^+He_q

($1 \leq p \leq n$, $q \leq 100$) fragment abundances provided valuable data sets to be compared with experiments.^{39–42}

In both the study by Takayanagi et al.³² and ours,^{37,38} the modest size of the droplet compared to typical experimental sizes could explain the absence or near absence of caging. Even the 500-atom droplet seemed too small to observe any caging in the study by Vilá *et al.*³³ In the present work, we extend our former study of neon-doped helium clusters to larger argon-doped helium clusters, considering more specifically $\text{Ar}_4^+\text{He}_{1000}$ as a prototype system for large helium droplets. Argon clusters are preferred to neon or heavier rare gases (*i.e.*, krypton or xenon) clusters due to a number of properties: a more classical character compared to neon, that is a low zero-point energy and delocalization; moderate spin-orbit coupling;⁴³ the high natural abundance of isotope ^{40}Ar ($\sim 99.6\%$) which makes it easier to compare with experimental mass spectra;⁴⁴ and the availability of both theoretical and experimental benchmark data on the fragmentation of argon clusters ionized by electron impact in the gas phase.^{15,19,20,45,46}

On the experimental side, Callicoatt et al.⁹ have investigated the fragmentation of argon-doped helium nanodroplets upon electron impact ionization. They mostly detected fragments composed of up to four argon atoms after ionizing their smaller helium nanodroplets (droplet size $\sim 600 - 8000$) with 60 eV electrons. They concluded that singly-doped droplets yielded Ar^+He_q but no Ar^+ , Ar_2 doped droplets mainly yielded Ar_2^+ , and Ar_3 and Ar_4 -doped droplets mostly gave Ar_2^+ . Upon photoionization of argon-doped helium droplets, Kim et al.¹¹ have observed Ar^+He_q , Ar_2^+ and Ar_2^+He_q , but no Ar^+ .

More recently, Bartl et al. investigated the fragmentation of argon-doped helium nanodroplets (droplet size $\sim 10^4 - 10^6$) ionized by electrons with energies ranging from 70 to 140 eV.⁴² Thanks to the high resolving power of their mass spectrometer ($m/\Delta m = 7000$), they could easily discriminate between Ar_n^+He_q fragments with nominally identical masses (the mass of an argon atom is close to that of ten helium atoms). They reported progressions of Ar_n^+He_q fragments for $n \leq 7$ and $q \leq 50$. They observed that bare cluster ions Ar_n^+ and mixed complexes Ar_n^+He_q had about the same yield ($n > 1$). They also discussed the origin of about twenty magic numbers from the smaller $\text{Ar}^+\text{He}_{12}$ to the larger $\text{Ar}_7^+\text{He}_{12}$, and noted an enhanced stability for all the clusters with $n + q = 19$ ($2 \leq n \leq 7$). Although the theoretical check of magic numbers would be a significant challenge for dynamics simulations, owing to the experimental width of droplet and dopant size distributions as well

as the great number of lengthy trajectories required to converge theoretical mass spectra intensities, some of the observables, *e.g.* the proportion of bare cluster ions, might be related to the electronic relaxation of the excited dopant, the subsequent energy distribution within the droplet, and possible recombinations, three aspects of the fragmentation mechanisms of argon-doped helium droplets that can be investigated with our mixed quantum-classical method.

We will first recall in the Method section some essential features of the mixed quantum-classical method and detail the improvements brought to model the dynamics of $\text{Ar}_4^+\text{He}_{1000}$. A brief discussion of the influence of the model parameters (effective He-He interaction potentials and velocity adjustment techniques) is reported in the Supplementary Material. The Results section focuses on the fast character of electronic relaxation, ionic fragment abundances, characteristic times of the dynamics, and proposes two extreme mechanisms, fast ejections and long-term trappings, before studying the possibility to use fragment kinetic energy distributions to characterize them. The final section discusses the results and concludes in the perspective of a more extensive study.

II. METHOD

Ionization-induced fragmentation of Ar_4 clusters embedded in a helium nanodroplet of 1000 atoms has been simulated using a method similar to that employed in our previous work on the fragmentation of Ne_n ($n=4-6$) clusters upon electron impact ionization in a $^4\text{He}_{100}$ droplet.^{37,38} We recall here the essential features of the original method and stress the modifications brought in the current work.

This study faces the double challenge of modelling the multisurface dynamics of the ionized argon cluster and the significant quantum effects due to a large number of helium atoms. So far, only the time-dependent ^4He density functional method (^4He -TDDFT) has been able to accurately describe excited state dynamics for a realistic droplet size.^{47,48} However, the electronic state of the dopants is described in a mean-field approach, which does not identify electronic transitions. Ring polymer molecular dynamics (RPMD) has been tested, initially on potassium⁴⁹ or silver⁵⁰ atom excitation and Cl_2 photodissociation³² in small helium droplets, and more recently to investigate size-dependent submersion of sodium clusters into helium and para-hydrogen droplets.⁵¹ These studies involved only one electronic

state and did not take into account ^4He atom exchange. We have preferred to use a more approximate method, in order to explicitly track electronic state transitions and identify individual helium atoms, at the expense of a more approximate description of quantum effects: zero-point delocalization is treated phenomenologically using the ZPAD method, while exchange-correlation effects are neglected. At the high energy of the dynamics induced by argon clusters ionization, it is expected to be a reasonable approximation.

A. Essential features of the ZPAD method

In order to take into account, at least approximately, the quantum delocalization of the helium atoms, the ZPAD method is based on the idea of “dressing” each helium atom with a wave function that will be kept frozen during the dynamics. This is the same idea as the frozen-Gaussian approach⁵² adapted by Sterling *et al.*⁵³ to study the dynamics of dopants in quantum crystals. The version used here is based on the method described by Slavíček *et al.*⁵⁴ to describe the photodissociation of HBr and HCl in floppy neon clusters. It has the advantage that the wave function dressing each helium atom is not restricted to be a Gaussian, and that the method is iterative and self-consistent. It has been adapted for helium atoms in Refs. 37 and 38.

As in the frozen-Gaussian approach, using a frozen wave function during the dynamics is equivalent to running classical dynamics on an effective potential, which is the original potential convolved with the squared wave function. Hence, the method is able to treat a large number of helium atoms. Both the wave function and the effective potential are determined at the same time by an iterative procedure. In the preliminary step, a classical dynamics is run for the neutral $\text{Ar}_4\text{He}_{1000}$ cluster at the droplet temperature (0.38 K).⁵⁵ The potential-energy surface is built from the HFDID1 Ar-Ar interaction potential,⁵⁶ the HFD-B He-Ar interaction potential,^{57,58} and the SAPT2 He-He potential proposed by Janzen and Aziz,⁵⁹ namely

$$V_{\text{neut}}(\mathbf{R}) = \sum_{i=1}^4 \sum_{\substack{j=1 \\ j>i}}^4 V_{\text{Ar-Ar}}(R_{ij}) + \sum_{i=1}^4 \sum_{a=1}^{1000} V_{\text{He-Ar}}(R_{ia}) + \sum_{a=1}^{1000} \sum_{\substack{b=1 \\ b>a}}^{1000} V_{\text{He-He}}(R_{ab}) \quad (1)$$

where \mathbf{R} stands for all the internuclear distances. The corresponding Ar-Ar, He-Ar, and He-He interaction potentials are depicted in Figure 1.

Then, the following procedure is applied:

1. The classical radial distribution function (rdf) of helium atoms, normalized by assuming that the cluster is spherical, is built on the fly during the dynamical run of step i , using the effective He-He potential of step $i-1$. For $i > 1$, it is subsequently convolved with helium wavefunction of step $i-1$ to produce a semiclassical rdf.
2. The semiclassical rdf is convolved with the SAPT2 He-He potential to provide the average radial potential felt by one helium atom in the mean field due to the others.
3. This average radial potential is included in a Schrödinger equation, the solution of which gives the helium wave function for step i .
4. The original He-He interaction potential is convolved with the newly calculated helium wavefunction to build the effective He-He potential for step i .

This procedure is initiated with the original SAPT2 He-He potential.⁵⁹ Steps (1) to (4) are repeated until convergence of the effective potential. In previous works^{37,38} we found it practical to remove the tail of the helium wave function beyond a cutoff radius $R_{\text{cut}} \approx 1.5 - 1.6 \text{ \AA}$ in order to reach convergence more efficiently. This was not necessary in the original study of Slavíček et al.⁵⁴ for neon clusters since the effective Ne-Ne potential curves converged after as few as 4 iterations, to be compared with the 27 iterations needed to converge the effective He-He potential curve for $R_{\text{cut}} = 1.6 \text{ \AA}$ in the present work. For this reason, we expect our converged effective He-He potential to be slightly too deep to represent liquid helium droplets since the well depth of the effective potential decreases with larger cutoff radii. However, the helium radial probability density functions deduced from such potentials in the case of neon-doped helium clusters were found to compare very well with diffusion Monte Carlo (DMC) simulations,³⁷ which makes us believe that most of the quantum effects are indeed taken into account. In the following, the ZPAD method will refer to both the iterative process that aims to incorporate zero-point energy effects in the He-He interaction potential (potential part of the ZPAD method) and the subsequent dynamics of helium atoms performed using this effective potential (dynamical part of the ZPAD method).

B. Effective potential, structure and energy of Ar₄He₁₀₀₀

The final effective He-He potential is reported in Figure 1, together with the ones obtained for several iterations, to highlight the convergence of the aforementioned iterative procedure for the potential part of the ZPAD method. In order to validate it, the surface tension of Ar₄He₁₀₀₀ clusters was calculated and compared with the experimental data from Iino et al.²⁶ ($\gamma_{exp} = 3.536 \times 10^{-4}$ N/m) using the approximate formula for homogeneous clusters of radius R and size N

$$\gamma_{th} = \frac{E_s}{4\pi R^2} = \frac{(A + BN^{-1/3})V_{LJ}}{(36\pi)^{1/3}\sigma_{LJ}^2} \quad (2)$$

where the expression of surface energy $E_s = (AN^{2/3} + BN^{1/3})V_{LJ}$ ($A = 10.3$ and $B = -2.7$ are two dimensionless constants and V_{LJ} is the corresponding Lennard-Jones (LJ) pair well depth) has been devised by Echt et al.⁶⁰ on the basis of the work by Briant and Burton on argon microclusters,⁶¹ and the approximate radius of the cluster is given by $R = (3N/4\pi)^{1/3}\sigma_{LJ}$, with σ_{LJ} the pair diameter of LJ particles (helium atoms here). For the effective He-He potential with $R_{cut} = 1.6 \text{ \AA}$, $V_{LJ} = 1.254 \text{ cm}^{-1}$ (2.491×10^{-23} J) and $\sigma_{LJ} = R_{eq}/2^{1/6} = 3.92 \text{ \AA}$ ($R_{eq} = 4.40 \text{ \AA}$ is the equilibrium He-He distance), and we get $\gamma_{th} = 3.362 \times 10^{-4}$ N/m which is 5% below the bulk surface tension at $T = 0.4$ K. This is a reasonable agreement although the stabilization of the droplet by the dopant makes He-He bonds somewhat shorter and the He-He potential somewhat deeper than those expected for pure helium nanodroplets.

In order to reach a better accuracy in the classical dynamics, the resulting ZPAD effective potential points were fitted to an analytical form

$$V_{\text{He-He}}^{\text{eff}}(R) = V_{\text{short}}(R) + T(R)[V_{\text{long}}(R) - V_{\text{short}}(R)], \quad (3)$$

where

$$V_{\text{short}} = A \exp[-\alpha_1 R/R_e - \alpha_2 (R/R_e)^2] \quad (4a)$$

$$V_{\text{long}} = \sum_{i=3}^6 c_{2i} (R/R_e)^{-2i} \quad (4b)$$

$$T(R) = 0.5 (1 + \tanh[a(R - b)]). \quad (4c)$$

This expression slightly improves the fit in the short-range region of the potential curve of previous studies by adding a quadratic term $\alpha^2(R/R_e)^2$ in the exponential argument,^{37,38,62}

at the expense of additional computational cost. The fit parameters obtained for $R_{\text{cut}} = 1.6 \text{ \AA}$ are collected in Table I. Note that parameter $R_e \approx 4.43 \text{ \AA}$, obtained by fitting the bottom of the effective He-He potential well on a harmonic oscillator and subsequently used to initiate the overall fitting process of the effective potential, slightly differs from the true equilibrium distance of the analytical effective He-He potential ($R_{eq} \approx 4.40 \text{ \AA}$) considered to evaluate the droplet surface tension.

After converging the effective He-He potential, a last dynamical run is carried out to get an $\text{Ar}_4\text{He}_{1000}$ structure equilibrated at $T = 0.38 \text{ K}$. This structure is used as input configuration in our mixed quantum-classical method devised to model the fragmentation of $\text{Ar}_4^+\text{He}_{1000}$.

C. Mixed quantum-classical dynamics of $\text{Ar}_4^+\text{He}_{1000}$

The dynamical simulations are divided into three successive steps: an equilibration of the neutral cluster prior to its ionization by electron impact, a nonadiabatic dynamics of the ionized cluster during which electronic transitions can take place, and a long-term adiabatic fragmentation dynamics once electronic relaxation to the ground electronic state is completed.

The first step consists in running a ZPAD trajectory for the sake of equilibrating the neutral $\text{Ar}_4\text{He}_{1000}$ cluster. As explained above, ZPAD is equivalent to classical dynamics using the effective He-He interaction obtained as described in the preceding section. Hence, the potential-energy surface is that reported in Eq.(1), except that the SAPT2 He-He interaction potential $V_{\text{He-He}}(R)$ is replaced by the converged effective He-He potential $V_{\text{He-He}}^{\text{eff}}(R)$ from Eq.(3). This equilibration dynamics starts from the $\text{Ar}_4\text{He}_{1000}$ positions and velocities obtained upon convergence of the He-He effective potential, namely one particular phase-space configuration corresponding to a kinetic temperature of 0.38 K . Although this initial configuration is the same for all the trajectories, the random duration of the ZPAD trajectory ensures a reasonable exploration of $\text{Ar}_4\text{He}_{1000}$ phase space and therefore the production of distinct configurations used as input for the dynamics of the ion.

The second step is the simulation of the dynamics following dopant ionization. The most likely first event in electron impact ionization of a doped helium cluster is the creation of a positive He^+ hole within the droplet (see for instance Ref. 9). It is then followed

by charge migration inside the droplet, until either Ar_4 is ionized by charge transfer from He^+ or the charge is localized to form He_2^+ . In order to specify accurate initial conditions for the electronic wave packet and to select the initial potential-energy surface on which the dynamics starts, the whole process would have to be simulated, which is beyond the scope of this work. Hence, in the absence of any other indications, we have assumed “instantaneous” Ar_4 ionization. In other words, at the end of each equilibrated trajectory described above, the whole system is switched to the ionic state by randomly selecting one of the adiabatic surfaces of Ar_4^+ converging to $\text{Ar}^+(^2\text{P}) + 3 \text{Ar}$, denoted V_j for $j \in [1, 12]$. The random selection of the initial electronic state is reflected in the electronic wave packet by taking identical initial weights for all electronic states. Note that all the (spin-free) electronic states correlating with ground state $\text{Ar}^+(^2\text{P}) + 3 \text{Ar}$ are considered in this study. Electronic states of Ar_4^+ correlating to electronically excited Ar^+ are not included since they cannot be reached by charge transfer.

From there on, the second step in our simulations is mixed quantum-classical nonadiabatic dynamics of the ionized cluster, in which the argon and helium nuclei are treated classically but the electronic hole, only delocalized on argon atoms, is treated quantum mechanically. We use the molecular dynamics with quantum transitions (MDQT) method.^{63,64} The classical dynamics of the nuclei is run on one adiabatic surface, and the multisurface character of the simulation is taken into account by allowing for hops between Ar_4^+ adiabatic surfaces. The adiabatic energies are obtained by diagonalizing the diatomics-in-molecules (DIM) model hamiltonian^{65–67} for Ar_4^+ in the basis set of the twelve argon effective p orbitals. The matrix elements are constructed from the analytical expressions of the Ar-Ar and Ar_2^+ diatomic potentials,^{19,56} supplemented by the addition of the induced dipole-induced dipole interaction, with electric dipole polarizability $\alpha = 1.664 \text{ \AA}^3$.⁶⁸ The total potential-energy surface is then built from the relevant Ar_4^+ adiabatic electronic state V_j , an average He- Ar^+ interaction potential, denoted $\bar{V}_{\text{He}-\text{Ar}^+}$, and the same He-Ar and effective He-He interaction potentials as used for the dynamics of the neutral cluster,

$$V_{\text{ion}}^j(\mathbf{R}) = V_j + V_{\text{He-dopant}}^j + \sum_{a=1}^{1000} \sum_{\substack{b=1 \\ b>a}}^{1000} V_{\text{He-He}}^{\text{eff}}(R_{ab}) \quad (5)$$

$$V_{\text{He-dopant}}^j = \sum_{i=1}^4 \sum_{a=1}^{1000} \left[q_i^{(j)} \bar{V}_{\text{He}-\text{Ar}^+}(R_{ia}) + (1 - q_i^{(j)}) V_{\text{He}-\text{Ar}}(R_{ia}) \right] \quad (6)$$

where \mathbf{R} stands for all the internuclear distances, V_j is the j^{th} adiabatic energy of Ar_4^+ , $q_i^{(j)}$ is

the fractional charge carried by the argon atom i (see Appendix) for that adiabatic energy, and the average He-Ar⁺ potential is built as a weighted sum of the analytical forms proposed by Carrington et al.⁶⁹ for the X²Σ⁺ and A²Π electronic states of He-Ar⁺ (see Figure 1),

$$\bar{V}_{\text{He-Ar}^+}(R_{ia}) = \frac{1}{3}V_{\text{He-Ar}^+}^{\text{X}^2\Sigma^+}(R_{ia}) + \frac{2}{3}V_{\text{He-Ar}^+}^{\text{A}^2\Pi}(R_{ia}). \quad (7)$$

Note that the spin-orbit interaction is not taken into account in order to keep the simulations within reasonable computational cost. As commented in our previous work on gas phase ionization of Ar_{*n*} clusters,^{19,20} the influence of spin-orbit coupling on ionization induced fragmentation was negligible for cluster sizes greater than $n = 6$, and it was already very small for $n = 4$ and 5.

In our implementation of the DIM+MDQT method⁷⁰ the probability for the system to hop from an adiabatic surface j to an adiabatic surface k is given by

$$P_{j \rightarrow k} = -2\Delta t \frac{\xi_k}{\xi_j} \dot{\mathbf{R}} \cdot \mathbf{d}_{kj} \cos(\varphi_k - \varphi_j) \quad (8)$$

where Δt is the current time step of the dynamics, ξ_j and φ_j are the modulus and the phase of the j^{th} time-dependent wave packet coefficient (corresponding to the time-evolution of the positive charge), and d_{kj} is the nonadiabatic coupling vector between surfaces k and j calculated from the Hellmann-Feynman formula. If a hop from surface j to surface k is accepted, the total kinetic energy has to be adjusted in order to ensure total energy conservation. In the original MDQT method this is done by adjusting atomic momenta along the nonadiabatic coupling vector \mathbf{d}_{kj} .^{63,64} However, this choice does not conserve the total angular momentum when applied to model the fragmentation dynamics of ionized neon clusters in the gas phase.¹⁷ We had chosen instead the direction of the gradient of the energy difference between adiabatic states k and j , $g_{kj} = \nabla(V_k - V_j)$.⁷¹⁻⁷³ In the present work, where helium atoms are explicitly taken into account in the dynamics, the partial charge $q_i^{(j)}$ on argon atom i depends on the electronic state j . Hence, upon a hop, the potential is also suddenly modified for the helium atoms dynamics, as seen in the second term of the right-hand side of Eq.(5). We have therefore chosen the gradient $g_{\text{He}} = \nabla(V_{\text{He-dopant}}^k - V_{\text{He-dopant}}^j)$, where $V_{\text{He-dopant}}^j$ is the He-dopant interaction calculated for charges representative of adiabatic state j and defined in Eq.(6), to adjust the argon and the helium momenta. Very similar results are obtained when using g_{kj} as discussed in the Supplementary Material.

The third step of the mixed quantum-classical simulation is an adiabatic classical run

performed for trajectories that reached the ground electronic state ($> 95\%$ of the trajectories) at the end of the 100 ps of the second step (*i.e.*, the nonadiabatic step). Nuclei evolve adiabatically on the ground ionic electronic surface, *i.e.* the ionic surface of Eq.(5) where V_j is the ground electronic state of Ar_4^+ . This adiabatic simulation is devoted to the study of possible fragmentation and recombination mechanisms that might occur on longer time scales, up to 0.5 ns in this work.

D. Computational details

A typical dynamical simulation is a set of 160 trajectories where the classical positions and momenta and the wave packet coefficients (modulus and phase) are propagated using the Hamming's predictor corrector integrator.⁷⁴ The initial simulation time step and duration were $\Delta t_1 = 0.1$ fs and $t_1 = 10(1 + \xi)$ ps for initial randomization in the neutral cluster, with ξ a random number between 0 and 1; $\Delta t_2 = 0.1$ fs and $t_2 = 100$ ps for the nonadiabatic dynamics of the ionic cluster; $\Delta t_3 = 1$ fs and $t_3 = 400$ ps for the final adiabatic dynamics. The justification of this choice for t_2 and t_3 is given in the Results section. Data are stored every 0.1 ps during the nonadiabatic run and every 1 ps during the adiabatic run.

In both nonadiabatic and adiabatic runs, the integration of the classical equations of motion is very accurate because the potential derivatives of $V_{neut}(\mathbf{R})$ and $V_{ion}(\mathbf{R})$ are known analytically. Only the derivatives of the charges $q_i^{(j)}$ are numerical (see Appendix). Furthermore, many fragmentation and recombination processes occur during the simulations. Individual fragments are identified by applying a distance criterion $d_{\text{frag}} = 15$ au ($\sim 8 \text{ \AA}$) to decide whether a bond is broken or not, and taking care that all the atoms belonging to a fragment are at least at d_{frag} from any of the atoms belonging to other fragments.⁷⁵ We have checked that the resulting fragment distributions are only barely sensitive to the value of d_{frag} .

III. RESULTS

A. Electronic relaxation of the Ar_4^+ parent ion

The average relaxation time of Ar_4^+ to its ground electronic state (whether fragmented or not) is plotted in Figure 2 as a function of the initial excited electronic state. For most

states (the 8 lowest ones), relaxation to the ground electronic state is faster than 2 ps. This relaxation time increases with excited state energy, and electronic relaxation takes somewhat longer when the dynamics starts on one of the upper states. However, it does not exceed a few tens of picoseconds on average. These observations validate our two-step simulation composed of a nonadiabatic simulation during 100 ps, to allow for electronic relaxation, followed by an adiabatic simulation on the ground electronic state up to 500 ps.

The average initial energy of the electronic states involved is also depicted as a function of electronic state number as an inset in Figure 2. There is a relationship between the electronic state initial energy and its relaxation time, in the sense that higher electronic states have more available energy to dissipate, which on average takes longer. However, the relationship is not simple, as the dispersion of relaxation times is also highest for these excited states. For instance, the relaxation times for state 12 range from about 2 ps to 77 ps. This is because electronic relaxation rates strongly depend not only on the static nonadiabatic couplings, but also on velocity vectors in the regions of strong couplings (see Eq. (8)). In addition, the number of intermediate states visited by a trajectory also depends on the dynamics.

B. Ionic fragment abundances

A number of ionic species are formed during the fragmentation of the ionized doped helium droplet. To clarify the discussions on fragmentation mechanisms and fragment abundances below, the term “dopant” will refer to all the host argon atoms inside the (initial or shrunk) helium droplet, whether ionic or not. “Ionic fragments” will designate the most general ionic fragments containing argon and helium atoms, namely Ar_n^+He_q ($2 \leq n \leq 4$, $q \leq 1000$) fragments reported in theoretical mass spectra. “Ionic core” will only refer to the compact charged argon cluster within an ionic fragment, since no helium atom can carry a charge in our simulation, which is a very good approximation given the difference in ionization potential between Ar and He. A “roaming” argon atom will designate a neutral argon atom, whether dissociated from the ionic dopant or barely bound to it, which moves inside the droplet.

Figure 3 shows the mass spectra obtained at the end of the 100 ps nonadiabatic simulation step, during which electronic relaxation can occur, and at the end of the overall 500 ps simulation. Two main results emerge from their analysis: the absence of Ar^+ and Ar^+He_q

fragments, and the production of two families of ionic fragments. The first family gathers small Ar_2^+He_q and Ar_3^+He_q ($q \leq 50$) ions with a significant preference for the Ar_2^+ core and a cloud of helium atoms often below twenty atoms. It mainly appears as a relatively narrow set of peaks extending from 80 to 140 amu. The second family gathers large ions that can contain up to four argon atoms. It is represented by a broad distribution of peaks extending from a few hundreds amu to more than three fourth of the initial droplet mass and gradually shifts to lower masses between 100 ps and 500 ps.

The absence of Ar^+ and Ar^+He_q fragments appears to be in stark contradiction with the intense signal observed for Ar^+ and Ar^+He_q in experimental mass spectra by Bartl *et al.*⁴⁴ However, argon clusters are not size selected in these experiments, so the Ar^+ containing ions could originate from Ar_n dopants with $n < 4$. Indeed, in previous simulations on gas phase argon cluster ionization,¹⁹ the ionic monomer fragment was observed for small parent sizes only. Its abundance was $9.1 \pm 0.4\%$ for Ar_4 with no inclusion of spin-orbit coupling and $13.8 \pm 0.6\%$ when this interaction was taken into account. Hence, the intense monomer peak observed in experiments most probably originates from cluster sizes smaller than the tetramer studied here. Other explanations could be the occurrence of double ionization^{9,76} or possible secondary ionization of neutral Ar fragments.¹⁹ Radiative relaxation on a longer (microsecond) time scale explored for heavier rare gases by Janeček *et al.*⁷⁷ would not apply here since electronic relaxation is complete at the end of the nonadiabatic step of the simulation.

More details on the ionic fragment abundances are given in Figure 4. As can be seen in this figure, the most abundant “bare” (*i.e.* with no helium attached) argon ion is the dimer, a reminiscence of the high propensity for Ar_n clusters to form Ar_2^+ ions upon gas phase ionization.^{19,20} Some Ar_4^+ ions are detected but they come from secondary geminate recombinations²² of the dopant possibly favored by helium evaporation, as detailed later.

Ar_2^+He_q and Ar_3^+He_q are more abundant than the bare ions Ar_2^+ and Ar_3^+ . Ar_4^+He_q are also present in mass spectra, especially at the early times of the dynamics, but the ionic dopant is a very loose $\text{Ar}_2^+ \cdots \text{Ar} \cdots \text{Ar}$ or $\text{Ar}_3^+ \cdots \text{Ar}$ complex and its abundance progressively vanishes during the 0.5 nanosecond of the simulations.

Based on abundances, we can divide up Ar_n^+He_q fragments into three families: small fragments ($q \leq 50$) which, as will be discussed in Section III D, are mainly due to fast ejections of an ionic argon cluster, large fragments ($q > 500$) which will be shown in the same

section to be signatures of trapped ionic argon clusters, and intermediate-sized fragments ($50 < q \leq 500$).

A histogram of the Ar-Ar distances, when the ionic dopant is trapped in a large helium cluster ($q > 500$) at the end of the 500-ps simulation, is depicted in Figure 5. When only two argon atoms remain trapped, the ionic core is Ar_2^+ with an average Ar-Ar distance of 2.45 Å, very close to the equilibrium distance of the gas phase dimer in its ground electronic state ($R_{eq} \approx 2.40$ Å). However, when more argon atoms are trapped in what remains of the droplet, they do not necessarily form a bound argon cluster and the average Ar-Ar distance increases: 9.4 Å for three argon atoms and 13.3 Å for four argon atoms. A closer inspection of the histograms for Ar_3^+ or Ar_4^+ dopants reveals a peak around the equilibrium Ar-Ar distance of Ar_2^+ at 2.40 Å, but no peak arises at twice this distance as could be expected for linear Ar_3^+ ionic cores (the most stable structure for Ar_3^+ in the gas phase). If any Ar_3^+ ionic core exists it is rather vibrationally excited and far from its linear equilibrium configuration. The width of the peak around 2.40 Å can therefore be due to warmer Ar_2^+ or warm Ar_3^+ core.

More specifically, in the case where the remaining ionic dopant is Ar_3^+ , the peak around 3 Å roughly represents one third of the number of Ar-Ar distances. The other two thirds mainly correspond to much larger distances, with a distribution extending from 9 to 21 Å. Hence, the ionic dopant is rather a combination of Ar_2^+ and a roaming, nearly free, additional Ar atom. In the case where the remaining ionic dopant is Ar_4^+ , only 26% of the distances lie within the range of Ar_n^+ equilibrium distances ($2 \leq n \leq 4$), namely 2-4 Å. The predominance of roaming argon atoms is thus also confirmed in this case, although discriminating between an Ar_2^+ or Ar_3^+ core is rather involved.

In order to validate our interpretation of the presence of argon atoms roaming inside the droplet, we first have to rule out the possibility that they are simply loose structures formed by the clustering of “snowballs” rigidly attached to the argon atoms, and in particular to the ones belonging to the ionic core, which would prevent the formation of compact argon clusters. Such structures were found in a recent ^4He -TDDFT theoretical study⁷⁸ on the dynamics of argon atoms clustering by collision with helium nanodroplets. Figure 6 displays the radial distributions of Ar-He distances between argon atoms, isolated or belonging to the ionic core of the cluster (*i.e.*, Ar_2^+ or Ar_3^+), and all helium atoms of the system at the end of the dynamics ($t = 500$ ps). The resulting distributions are similar to the ones obtained

for Cs^+ or Rb^+ solvated in helium nanodroplets,⁷⁹ with a small shell of helium atoms (the number of helium atoms is estimated at 12 about an Ar_2^+ core, 15.5 about an Ar_3^+ core, and 10 about an isolated argon atom) with radius $3.5-4 \text{ \AA}$ about the ion and $4-4.5 \text{ \AA}$ about the neutral argon atoms. These solid-like first shells about the dopant atoms could account for Ar-Ar distances of the order of $10-13 \text{ \AA}$ (taking into account the equilibrium He-He distance of $\sim 4.4 \text{ \AA}$) found in Figure 5. However, the rest of the distribution at larger distances, up to 21 \AA for Ar_3^+ dopants and 23 \AA for Ar_4^+ dopants, is clearly due to the roaming of argon atoms. Hence, the resulting picture is that of an ionic core surrounded by a rigid snowball, and one or two neutral argon atoms (possibly also surrounded by a snowball) roaming inside the droplet.

Visual inspection of the configurations subject to ion trapping at the end of the simulation revealed that the dopant is mainly Ar_2^+ (40%) and $\text{Ar}_2^+ + \text{Ar}$ (42.5%), with smaller contributions of warm (triangular) Ar_3^+ (2.5%), $\text{Ar}_2^+ + \text{Ar} + \text{Ar}$ (10%), warm $\text{Ar}_3^+ + \text{Ar}$ (2.5%) and $\text{Ar}_2^+ + \text{Ar}_2$ (2.5%). The affinity for charge localization on Ar_2^+ can be confirmed by noting that, after Ar_4^+ has decayed to its ground electronic state, 97% of the charge is carried by only two argon atoms, on average.¹⁹ The other argon atoms can (i) dissociate and get expelled from the droplet; (ii) dissociate but slow down because of the surrounding helium atoms and remain in the droplet; or (iii) get stabilized and join the Ar_2^+ core to build an Ar_3^+ cluster (no compact Ar_4^+ cluster has been observed). Note that mass spectrometry experiments cannot discriminate either between a compact Ar_3^+ or Ar_4^+ cluster and an Ar_2^+ core with one or two argon atoms roaming within the shrunk droplet. Hence, the large argon-doped droplets detected in the mass spectra of Figure 3 at $t = 500 \text{ ps}$ contain Ar_2^+ and $(n-2)$ Ar atoms roaming in the droplet rather than a compact Ar_n^+ cluster. However, these roaming argon atoms may recombine with the Ar_2^+ core. The experimental timescale being much longer than our simulations, there is more time for the system to relax, recombine or get ejected, which should account for some deviations between theoretical and experimental mass spectra.

C. Characteristic times of the dynamics

In this section we discuss qualitatively the sequential fragmentation dynamics of $\text{Ar}_4^+ \text{He}_{1000}$ by providing approximate characteristic times deduced from exponential fitting (Figure 7a)

or linear fitting (Figures 7b and 7c) of the curves representing the time evolution of relative fragment abundances. A more quantitative kinetic analysis will be performed in future works, when optimization of the programs will make it feasible to increase the number of trajectories by a significant factor in order to get better statistics.

At the earlier times of the dynamics, the abundance of Ar_4^+He_q ($q > 500$) rapidly decreases with an approximate lifetime of 15 ps. The quick disappearance of these large Ar_4^+He_q clusters is related to electronic relaxation of the Ar_4^+ dopant that may release ~ 1.5 eV within the droplet since the global minimum of Ar_2^+ , the main ionic argon core observed in mass spectra, is about -1.39 eV with respect to the dissociation into $\text{Ar}^+(^2\text{P}) + \text{Ar}$.¹⁹ This electronic relaxation is often followed by the ejection of one or two neutral argon atoms that yields the production of large fragments containing Ar_2^+ or Ar_3^+ , as shown by the sharp increases of the abundances in large Ar_n^+He_q ($n = 2-3$, $q > 500$) fragments in Figure 7b. The formation of these Ar_n^+He_q fragments starts at about $t \lesssim 5$ ps and evolves with characteristic times of 86 ps for Ar_2^+He_q and 19 ps for Ar_3^+He_q . The corresponding ionic dopants, namely Ar_2^+ and Ar_3^+ , can in turn be ejected from the large Ar_n^+He_q fragments as obvious from the fast productions of small Ar_2^+He_q and Ar_3^+He_q ($0 < q \leq 50$) fragments in Figure 7c. The formation of these small fragments starts at $t \approx 10$ ps and grows with characteristic times of 82 ps and 107 ps, respectively.

A closer inspection of the decay of Ar_n^+He_q ($q > 500$) clusters points to the secondary dissociation of Ar_3^+ dopants into Ar_2^+ as origin of most of the small Ar_n^+He_q fragments: the curve for Ar_3^+He_q ($q > 500$) clusters drops from 50% to 20% between $t \approx 10$ ps and $t \approx 40$ ps parallel to the increase of Ar_2^+He_q and Ar_3^+He_q ($0 < q \leq 50$) abundances from 0% to $\sim 40\%$ within the first 40 ps. However, some of the small fragments must also originate from very fast dissociation of Ar_4^+ in large Ar_4^+He_q clusters, whether sequential or not, in order to explain these increases of Ar_n^+He_q ($n = 2-3$, $0 < q \leq 50$) abundances.

After $t \gtrsim 40$ ps, the abundance of large Ar_n^+He_q ($2 \leq n \leq 4$) fragments only slightly decreases (characteristic decay times of about 11.7 ns and 4.3 ns for Ar_2^+He_q and Ar_3^+He_q , respectively) both due to the rarefaction of fast ejections and the long-term trapping of ionic dopants. Helium atom evaporation therefore becomes the main fragmentation process governing the dynamics. In particular, bare Ar_2^+ and Ar_3^+ fragments seem to originate from gradual helium atom evaporation from Ar_3^+He_q and Ar_2^+He_q , as their abundances start increasing distinctly slower at $t \gtrsim 20-30$ ps. The abundance in Ar_2^+ keeps increasing, as

expected owing to the evaporation of helium atoms from small Ar_2^+He_q fragments, while bare Ar_3^+ fragments reach a plateau somewhat parallel to that of small Ar_3^+He_q fragments.

Finally, it is worth noting that a small abundance of Ar_4^+He_q ($q > 500$) persists at long times. As explained before, this is not a compact Ar_4^+ cluster but rather an Ar_2^+ or a warm Ar_3^+ ionic core with two or one argon atom(s) roaming within the droplet. Droplet evaporation then makes it more and more likely for the roaming neutral argon atoms to meet the ionic core and recombine, the energy released by this recombination inducing helium evaporation and possible additional argon-cluster fragmentation. The slow decrease of Ar_4^+He_q abundance at later times is due to these processes.

D. Fast ejections and long-term trappings

Based on the elements already discussed (kinetics of fragment appearances, Ar-Ar distances for trapped ion cores), three types of dynamical processes emerge:

1. *Fast ejection* of a small ionic fragment. This process, already observed in the simulation of neon-doped helium clusters ionization,^{37,38} occurs within the first 100 ps. “Small ionic fragments” refers to Ar_n^+He_q with $q \leq 50$.
2. *Long-term ion trapping*. An ionic dopant remains in helium droplets of at least 500 helium atoms for more than 500 ps. This longer-term dynamics can involve possible recombinations and/or dopant release in the gas phase, leading to ionic fragments with a broad distribution of helium atoms observed at the end of our 500 ps simulations. This longer timescale is reminiscent of the nanosecond time scale estimated experimentally for helium evaporation and CH_3I recombination following CH_3IHe_N ($N=2000-20000$) photodissociation.³¹
3. *Intermediate processes*. They include all the other processes, namely fragmentation processes that release small ionic fragments in the gas phase after 100 ps (eg, delayed ejections and recombinations) and ion trappings in small nanodroplets (containing a few hundreds helium atoms at $t = 500$ ps) that might lead to recombinations.

Fast ejections and long-term trappings are illustrated in Figure 8. The upper part shows a trajectory in which Ar_2^+ is ejected, with a small number of helium atoms attached. Ar_4^+

starts fragmenting inside the droplet at $t \approx 6.3$ ps into $\text{Ar}_3^+ + \text{Ar}$, then into $\text{Ar}_2^+ + 2 \text{Ar}$ ($t \approx 8$ ps), and the recoil energy is high enough for Ar_2^+ to leave the droplet, which occurs at $t \approx 20$ ps. It is accompanied by several helium atoms but, since it is vibrationally excited, the helium atoms keep dissociating. Indeed, visual inspection of the trajectory frame by frame shows that the ejected ionic fragment is Ar_2^+He_2 at $t = 50$ ps and Ar_2^+ at $t > 100$ ps.

The lower part of Figure 8 shows a trajectory in which Ar_2^+ remains trapped inside the droplet. As in the previous trajectory, Ar_4^+ dissociates very early on into $\text{Ar}_3^+ + \text{Ar}$ ($t \approx 2$ ps) and then into $\text{Ar}_2^+ + 2 \text{Ar}$ ($t \approx 7$ ps). However, in this case, Ar_2^+ is no longer ejected; most of the recoil energy is taken away by the two neutral argon fragments which leave the droplet, while Ar_2^+ remains trapped inside (final snapshot at $t \approx 13$ ps). Ar_2^+ internal excitation is then slowly cooled down through helium atom evaporation, leading to a gradual decrease of the droplet size.

The difference between these two processes is also clearly visible from the kinetic energy of the Ar_2^+ center of mass: 643 cm^{-1} (926 K) for the former and 21 cm^{-1} (30 K) for the latter.

Figure 9 shows an example of intermediate process involving several fragmentations and recombinations. Ar_4^+ fragmentation occurs somewhat later in this case since it takes ~ 30 ps to get $\text{Ar}_2^+ + 2 \text{Ar}$. Then, the argon atoms and the Ar_2^+ cluster remain inside the droplet which starts shrinking by evaporating helium atoms. The argon atoms are thus roaming inside a smaller and smaller droplet and a first recombination, $\text{Ar}_2^+ + \text{Ar} \rightarrow \text{Ar}_3^+$, occurs at $t \approx 220$ ps. However, the newly formed Ar_3^+ ion is too warm and cannot be cooled fast enough by the surrounding helium atoms, so it dissociates again into $\text{Ar}_2^+ + \text{Ar}$ at $t \approx 225$ ps. The helium droplet keeps shrinking even more and one of the two neutral argon atoms leaves the droplet, the other remains trapped and eventually recombines with the ionic Ar_2^+ core to form Ar_3^+ at $t \approx 395$ ps. The internal energy of Ar_3^+ is dissipated inside what remains of the droplet and a linear Ar_3^+ cluster is finally released in the gas phase at $t \approx 420$ ps.

In order to quantify the importance of the three processes identified above, we have classified the trajectories with respect to their propensity for fast ejection, long-term ion trapping or intermediate processes. This sorting is of course somewhat arbitrary, but the two extreme cases are clear and intuitive. Quantitatively, 56.3% of the trajectories lead to fast ejections, 25.3% to long-term trappings, and 18.4% correspond to intermediate processes, these percentages being subject to variations depending on the effective He-He potential or velocity

adjustment technique considered (see Figure S6 of the Supplementary Material). These percentages can be simply derived from Figure 10a by summing over all the percentages of trajectories for a given dynamical process (fast ejection, long-term trapping, or intermediate process). As can be seen in that figure, fast ejection is on average the most probable event in these simulations. It is about twice as probable as long-term trapping when summed over all electronic states. It is also clear from Figure 10a that the highest initial energy states are more prone to fast ejection, like the trajectory in the top plot of Figure 8 which was initiated on the highest electronic state. On the other hand, the lowest-lying electronic states tend to favor trapping like the trajectory in the bottom plot of Figure 8 which was initiated on the lowest electronic state. Intermediate processes are distributed somewhat uniformly over the whole energy range, with a local maximum for state 5. This overall picture could somewhat be expected since, at time $t = 0$, Ar_4^+ has by definition more available energy in the highest electronic states than in the lowest ones. However, it is worth noting that the probability for ejection is not negligible for the lowest initial electronic states. In this case, visual examination of the corresponding trajectories revealed that if Ar_2^+ is the ejected ion, it always brings along several helium atoms, and the droplet left behind is relatively intact. Some neutral argon atoms can even remain trapped in the droplet, generally as single argon atoms although dimers were also found. Ar_3^+ (linear or not) can be ejected as a bare ion even when the initial electronic state is one of the lowest ones, but it can also bring along helium atoms.

Trapping covers a broad range of processes that account for the width of the distribution of peaks observed in the theoretical mass spectra of Figure 3. When the Ar_4 dopant is ionized to its lower energy states, its internal energy may not be sufficient to eject all the neutral argon atoms upon fragmentation. The ionic core (usually Ar_2^+) may remain trapped within the nanodroplet together with one or two argon atoms, and is then subject to later recombinations as the droplet shrinks due to helium atoms evaporation. This is what happened in the trajectory presented in Figure 9. Ionization to the upper energy states can also lead to ion trapping, but the helium droplet severely shrinks as many helium atoms evaporate to dissipate the internal energy. The droplet size is then below 500 and the trajectory is classified among intermediate processes.

The ionic core of the droplet can recombine with argon atoms if they were not ejected. This recombination process releases a lot of energy in the droplet, which induces even more

helium evaporation. This can eventually result in the gas phase release of Ar_3^+ or Ar_4^+ , possibly surrounded by a few helium atoms. This influence of droplet shrinking, limiting the volume in which fragments can move and thereby inducing dynamics pathways different from the gas phase, is known for instance in proteomics where doped droplets are ionized by electrospray ionization. In this case, as proposed by the charged residue model,^{80,81} solvent evaporation induces higher charge density which in turn leads to further fragmentation.

To provide a more precise picture of the relationship between the initial excitation of the dopant and the mechanisms of ion formation, Figure 10b reports the mass of the ionic fragments at $t = 500$ ps as a function of the initial Ar_4^+ electronic state populated. As previously discussed fast ejections (red symbols) can occur for a wide range of initial energies, although the higher ones are preferred. Two large fragments, whose masses do not lie within the range allowed by the definition of fast ejections (ie, less than 50 helium atoms), are also attributed to this fragmentation mechanism (see electronic states 10 and 11) which can appear contradictory. They correspond to small ions ejected after an extensive droplet fragmentation before $t = 100$ ps but captured later by one helium cluster in its course to get a more stable spherical shape. This is an example of the wide variety of processes at play that can hardly be interpreted from a single analysis of mass spectra, the final ionic fragment mass being not always representative of the fragmentation process primarily triggered upon ionization of the doped helium nanodroplet. Figure 10b also reveals that the trapping of Ar_2^+ is favored by the higher electronic states, whereas trapped Ar_3^+ and Ar_4^+ (or lightly bound complexes like $\text{Ar}_2^+ \cdots \text{Ar}$ and $\text{Ar}_2^+ \cdots \text{Ar} \cdots \text{Ar}$) are more common at lower energies. Intermediate processes yield fragment masses in between fast ejections and long-term trappings and Ar_n^+ -containing ions ($n = 3 - 4$) remain favored by the lower-energy states.

These observations enable us to predict that for larger Ar_n^+ dopants ($n > 4$), cycles of recombinations and helium evaporations will yield mass spectra significantly different from those observed in the gas phase.

E. Kinetic energy of fragments

In a previous work on neon clusters,³⁸ the analysis of helium kinetic energy distributions revealed a biexponential behavior that was attributed to the existence of two different frag-

mentation processes to account for the loss of helium atoms, namely thermal evaporation and ejection. Thermal evaporation was characterized by a kinetic energy release of 3-7 $\text{cm}^{-1}/\text{atom}$, while helium atom ejection corresponded to much faster helium atoms with kinetic energies of 28-45 cm^{-1} . The latter was attributed to fast ejection of the embedded ionic neon fragment, leading to energetic collisions with helium atoms, while the former was attributed to common helium atom evaporation that typically removes 5 cm^{-1} from the droplet for each helium atom lost. The ability for helium atoms to dissipate more than their binding energy to the droplet upon ejection was already known from experimental work on TPM²⁷ and HCN,²⁸ where the first thousands helium atoms were found to remove on average 22 $\text{cm}^{-1}/\text{atom}$ and 19 $\text{cm}^{-1}/\text{atom}$, respectively. They correspond to “prompt” atom emission observed in ^4He -TDDFT simulations.⁴⁸

The helium kinetic energy distribution obtained in this work for Ar_4 ionization inside a $^4\text{He}_{1000}$ droplet is plotted in Figure 11. There is a similarity with the case of neon cluster ionization inside a small (100 ^4He atoms) droplet, in that the low energy part of the distribution can be approximately fitted with a Boltzmann distribution corresponding to 4 $\text{cm}^{-1}/\text{atom}$, and there is a long tail extending to higher kinetic energies. However the whole distribution could not be fitted by a simple biexponential function. We believe that this is because evaporation and ejection are not the only fragmentation processes at play in larger droplets. When the ionic dopant is trapped, there can be different processes: fragmentation during and after electronic relaxation, helium atom evaporation to cool down the droplet and the dopant, possible recombinations after some roaming period of neutral argon atoms, which can in turn lead to new fragmentations. Hence, it is not very surprising that the kinetic energy distribution of the dissociating helium atoms could not be fitted to a simple analytical expression. However, we can assert that helium atoms evaporated during fast ejections are, on average, a bit more energetic ($\sim 8 - 9 \text{ cm}^{-1}/\text{atom}$) than those evaporated during long-term trapping ($\sim 6 \text{ cm}^{-1}$). Long-term trapping is characterized by thermal evaporation of helium atoms once the energy due to electronic relaxation has been dissipated. On the contrary, ejections can severely destabilize the droplet, by creating a partial burst of the droplet, and the energy of departing helium atoms is a reflect of the remaining large helium clusters rearrangements (as spheres to minimize their surface tension) and of the later progressive helium evaporation.

Since helium kinetic energy distributions could not unambiguously discriminate between

thermal evaporation, ion ejection, and trapping, we turned to an alternate observable, the translational energy of fragments. This is what Braun et al. used to investigate the photodissociation dynamics of alkyl iodides in helium nanodroplets.^{29,30} For each group of trajectories (*i.e.*, those subject to fast ejection, long-term trapping, or intermediate processes) we calculated the average center-of-mass kinetic energy of the ejected or embedded charged argon cluster. Focusing on the center of mass enables us to discard the vibrational energy of argon complexes, such as $\text{Ar}_2^+ \cdots \text{Ar} \cdots \text{Ar}$, trapped in helium nanodroplets. The average translational energy of ejected ions is 72 cm^{-1} in our simulations, whereas that of the trapped species is only $\sim 1.3 \text{ cm}^{-1}$. Intermediate processes correspond to a translational energy of $\sim 7 - 9 \text{ cm}^{-1}$, which is in between. Hence, the translational energy of the ions can be used as a criterion to distinguish between ejection and trapping: it gives a clearer signature than the velocity of evaporating helium atoms.

IV. DISCUSSION AND CONCLUSION

In this work we have studied the fragmentation dynamics following electron-impact ionization of Ar_4 inside a $1000\text{-}^4\text{He}$ atom droplet, using a mixed quantum-classical simulation in order to describe electronic transitions in Ar_4^+ , and the ZPAD method to take into account, at least approximately, quantum delocalization effects for helium atoms. Our simulations have revealed that the parent ions electronically relax on a picosecond time scale before fragmenting, as expected from their gas phase behavior. Ar_n^+ ($n = 2$ or 3) can be ejected from the droplet, as observed in the case of neon cluster ionization in smaller $100\text{-}^4\text{He}$ atom droplets,^{37,38} or be cooled through helium atom evaporation. They have also evidenced three dynamical processes: fast ejection of small ionic fragments, long-term ion trapping, and intermediate processes.

The most original result is the occurrence of a rich variety of trapping processes, in which an Ar_n^+ ion (mostly Ar_2^+) can be trapped together with one or two neutral roaming argon atoms in a shrinking helium droplet: this possibly yields recombinations and further dissociations, which in turn can release a small argon ion in the gas phase. To the best of our knowledge, this is the first theoretical work evidencing trapping and recombination. The fact that these processes were not observed in previous studies on chlorine photodissociation or dissociative ionization of small neon clusters in helium droplets is due to the fact that the

droplet size was limited to $\sim 100 - 200$ helium atoms in order to include realistic quantum effects in the simulations,^{32,37,38} or that the kinetic energy of the departing atoms was too high.³³ The importance of helium atom cooling and confinement inside a shrinking droplet can only be reproduced for larger helium nanodroplets like those considered in the present work.

Extending our studies to larger dopant sizes would also provide valuable clues to correlate the fragments observed in experimental mass spectra with parent cluster sizes. In addition, typical helium nanodroplet sizes range between 10^3 and 10^6 helium atoms, or even up to 10^{11} in recent applications devoted to quantum vortex lattices⁸² or silver doping.⁸³ Improving our simulation method for handling much larger droplets, for instance by implementing “smart” cutoff distances to neglect long-range He-He interactions, will therefore become a requirement in the near future. In our mixed quantum-classical approach, a surface hopping method is coupled to a DIM model, corrected by adding induced dipole-induced dipole interactions, and effective He-He interactions modified to take into account average zero-point effects. No significant effect of the velocity adjustment techniques has been identified but changes in atom-atom interaction potentials do have an influence on the relative propensity for ejections and trappings (see Figures S2-S7 of the Supplementary Material). More sophisticated methods that would include spin-orbit couplings in the DIM matrix,^{41,84-86} or quantum effects in the He-Ar and He-Ar⁺ interaction potentials, might be needed to get a more precise picture of the fragmentation dynamics of argon-doped nanodroplets.

This work constitutes the first step toward a realistic modeling of the dynamics of large doped helium nanodroplets upon electron impact ionization. The wealth of observed processes, from small fragment ejection to trapping, geminate recombination and helium evaporation extending on the nanosecond time scale, make Ar₄⁺He₁₀₀₀ a valuable prototype system to evaluate the relevance of our dynamical approach. However, experiments deal with a wide size distribution of argon clusters and helium nanodroplets. In particular, the increased intensity at the mass of Ar⁺He₁₂, Ar⁺He₃₂, and Ar⁺He₄₄ observed in experimental data, which was attributed to an increased stability of the icosahedral structure of helium atoms about an Ar⁺ ion,⁴⁴ would require additional simulations on smaller dopant sizes (*i.e.*, Ar_{*n*}⁺, $n \leq 3$) to check whether such fragments only originate from the ionization of embedded argon monomers or can be produced by ionizing Ar₂ or Ar₃.

Large neutral ArHe_{*q*} and Ar₂He_{*q*} fragments were also observed in our 0.5 ns simulations,

although in much lower abundance than helium atoms (see Figure S3 of the Supplementary Material). Evaluating the probability for such clusters to be ionized in experimental setups might provide additional clues to rationalize the large amount of Ar^+He_q fragments detected in mass spectrometers.

Although complete electronic relaxation of Ar_4^+ was achieved within a few tens of picoseconds and most of ion ejections occurred within one hundred picoseconds, the dynamics of $\text{Ar}_4^+\text{He}_{1000}$ clusters may last nanoseconds or more since the systems were not fully thermalized after 500 ps simulations. This is in contrast with small neon-doped helium nanodroplets whose fragmentation dynamics was generally completed within ~ 30 ps owing to the ejection of ions.³⁸ This longer timescale comes from ion trapping and can be confirmed by following the time evolution of fragment abundances. Trapped species include Ar_2^+ , Ar_3^+ , and Ar_4^+ but the latter two are slightly bound $\text{Ar}_2^+ \cdots \text{Ar}$ and $\text{Ar}_2^+ \cdots \text{Ar} \cdots \text{Ar}$ complexes, or an Ar_2^+ ion with one or two neutral argon atoms roaming around it, rather than the corresponding compact clusters. The helium nanodroplet then acts as a confined low-temperature medium that can favor the recombination of an ionic complex that would otherwise dissociate in the gas phase. Moreover, a number of experimental studies have stressed the nonthermal cooling exerted by the first thousands evaporating helium atoms.²⁷⁻³⁰ In the simulations presented here, there is a significant proportion of helium atoms which dissociate with a kinetic energy higher than expected from thermal evaporation. This occurs upon ion ejection or early dopant electronic relaxation. The average energy taken away by each helium atom can be up to 10 cm^{-1} .

In addition, we have found that the kinetic energy of the center of mass of the Ar_n^+He_q fragments could be used as a characteristics of the dynamical process: fast ejection of small ionic fragments, long-term ion trapping, or intermediate processes. For all these reasons, comparison with an experiment using velocity map imaging of the fragments would be very valuable.

V. SUPPLEMENTARY MATERIAL

The effective He-He interaction potential obtained for a wavefunction cutoff radius $R = 1.5 \text{ \AA}$ is plotted in Figure S1 and the corresponding parameters fitted on Eq.(3) are collected in Table S1. The influence of the He-He interaction potential and velocity adjustment tech-

nique is discussed on the basis of polar plots for abundances of ionic and neutral fragments at $t = 500$ ps (Figures S2 and S3), relaxation times (Figure S4), time evolution of Ar_n^+He_q relative abundances (Figure S5), and figures showing the propensity for the different dynamical processes as a function of the initial Ar_4^+ electronic state number (Figures S6 and S7).

VI. DATA AVAILABILITY STATEMENT

The data that support the findings of this study are available from the corresponding author upon reasonable request.

VII. ACKNOWLEDGMENTS

Prof. Marius Lewerenz is gratefully acknowledged for providing us with the set of routines devoted to the convergence of the effective He-He potential. DAB warmly acknowledges Dr Raphaël Vallon for logistical support and the regional supercomputing centre of Champagne-Ardenne (ROMEIO) for computational resources and technical support.

Appendix: Derivative of atomic charges $q_i^{(j)}$

Assuming an Ar_4^+ cluster excited in its adiabatic state V_j , the charge $q_i^{(j)}$ carried by argon atom i is given by

$$q_i^{(j)} = \sum_{\alpha \in \{x,y,z\}} |\langle p_{i\alpha} | \Phi_j \rangle|^2$$

where $\{|p_{i\alpha}\rangle\}$ ($i \in [1, n]$, $\alpha \in \{x, y, z\}$) is the basis set of reference p orbitals in the Cartesian space-fixed frame and $|\Phi_j\rangle$ is the Ar_4^+ eigenstate j . Since $\left\langle \frac{dp_{i\alpha}}{dx_l} \middle| \Phi_j \right\rangle = 0$

$$\frac{dq_i^{(j)}}{dx_l} = 2 \sum_{\alpha \in \{x,y,z\}} \langle p_{i\alpha} | \Phi_j \rangle \left\langle p_{i\alpha} \middle| \frac{d\Phi_j}{dx_l} \right\rangle.$$

Introducing the closure relationship,

$$\begin{aligned} \left\langle p_{i\alpha} \middle| \frac{d\Phi_j}{dx_l} \right\rangle &= \left\langle p_{i\alpha} \middle| \left(\sum_{k=1}^{3n} |\Phi_k\rangle \langle \Phi_k| \right) \middle| \frac{d\Phi_j}{dx_l} \right\rangle \\ &= \sum_{k=1}^{3n} \langle p_{i\alpha} | \Phi_k \rangle \left\langle \Phi_k \middle| \frac{d}{dx_l} \middle| \Phi_j \right\rangle = \sum_{k=1}^{3n} \langle p_{i\alpha} | \Phi_k \rangle d_{kj}^{(l)} \end{aligned}$$

where $d_{kj}^{(l)}$ is the l^{th} component of the $3n \times 3n$ nonadiabatic coupling vector \mathbf{d}_{kj} . Finally, we conclude that

$$\frac{dq_i^{(j)}}{dx_l} = 2 \sum_{\alpha \in \{x,y,z\}} \sum_{k=1}^{3n} \langle p_{i\alpha} | \Phi_j \rangle \langle p_{i\alpha} | \Phi_k \rangle d_{kj}^{(l)}. \quad (\text{A.1})$$

This expression is not fully analytical since the eigenstates $|\Phi_j\rangle$ are determined numerically by diagonalizing the DIM matrix of Ar_4^+ . However, its accuracy is confirmed by the proper energy conservation during the dynamics of $\text{Ar}_4^+\text{He}_{1000}$.

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TABLE I. Parameters of $V_{\text{He-He}}^{\text{eff}}(R)$ for the cutoff radius $R_{\text{cut}} = 1.6 \text{ \AA}$. The standard deviation between the fitted curve and the original data points for the regions of positive and negative energies are denoted SD^+ and SD^- , respectively.

Parameters	Values
R_e (\AA)	4.42712
A (cm^{-1})	1981.27
α_1	-7.86239
α_2	17.1145
c_6 (cm^{-1})	-2.34448
c_8 (cm^{-1})	7.45859
c_{10} (cm^{-1})	-14.879
c_{12} (cm^{-1})	8.51457
a (\AA^{-1})	18.347
b (\AA)	3.6356
SD^- (cm^{-1})	2.5×10^{-3}
SD^+ (cm^{-1})	0.71

LIST OF FIGURES

- 1 Diatomic interaction potentials used in our model. a) Ar-Ar and He-Ar interaction potentials; b) Average He-Ar⁺ interaction potential given by Eq.(7); c) Convergence of the effective He-He interaction potential as a function of the iteration number of the ZPAD method (see text) for $R_{\text{cut}} = 1.6 \text{ \AA}$. Convergence is assumed to be reached when the energy minima of two successive steps differ by less than 10^{-3} cm^{-1} 36

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- 3 Theoretical mass spectra of Ar₄⁺He₁₀₀₀ at the end of the 100 ps nonadiabatic simulation (plot a) and at the end of the overall 500 ps simulation (plot b). Ar₂⁺He_q and Ar₃⁺He_q fragment progressions for masses below 160 amu are reported as insets. When two peaks are nearly superimposed their intensities are summed, the corresponding peak is put at the average mass, and a label “×2” is added on top of this peak. Sum peaks occur for the pairs (Ar₃⁺, Ar₂⁺He₁₀), (Ar₃⁺He, Ar₂⁺He₁₁), (Ar₃⁺He₃, Ar₂⁺He₁₃), and (Ar₃⁺He₄, Ar₂⁺He₁₄). The relative abundances of the fragments belonging to these four pairs are as follows:
Inset of plot a: (25%,75%), (50%,50%), (75%,25%), and (50%,50%).
Inset of plot b: (83%,17%),(67%,33%), and (80%,20%). 38

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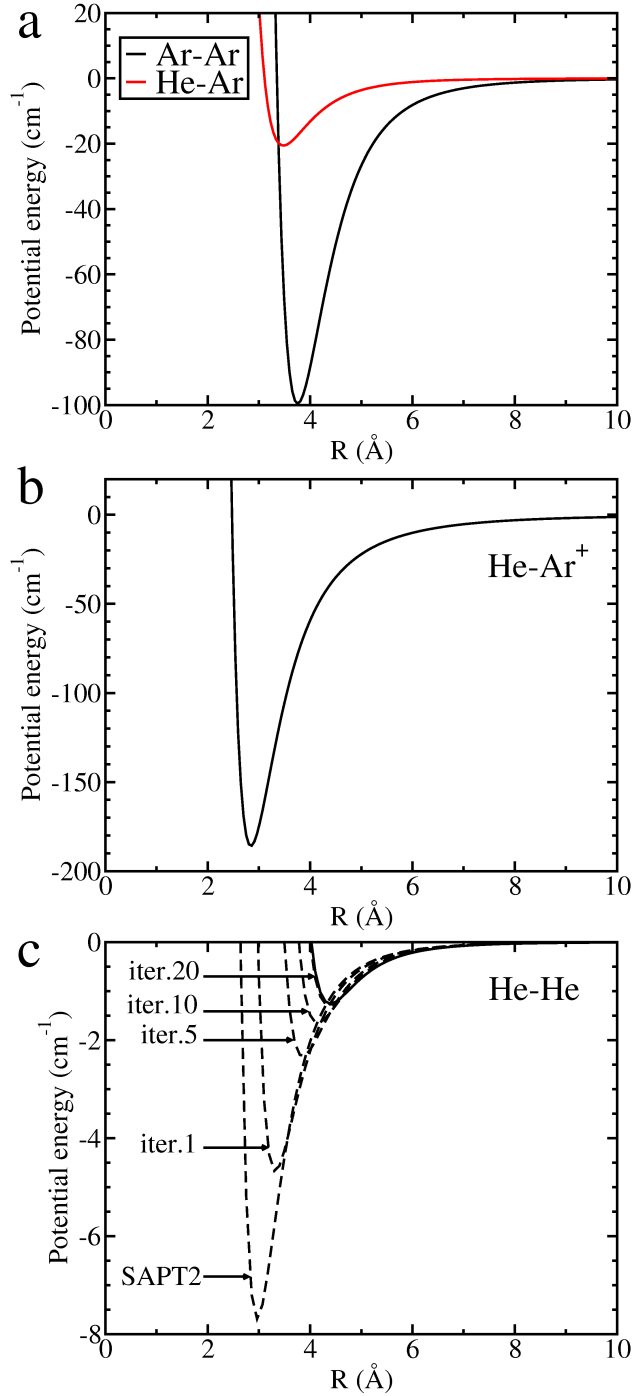


FIG. 1. Diatomic interaction potentials used in our model. a) Ar-Ar and He-Ar interaction potentials; b) Average He-Ar⁺ interaction potential given by Eq.(7); c) Convergence of the effective He-He interaction potential as a function of the iteration number of the ZPAD method (see text) for $R_{\text{cut}} = 1.6 \text{\AA}$. Convergence is assumed to be reached when the energy minima of two successive steps differ by less than 10^{-3} cm^{-1} .

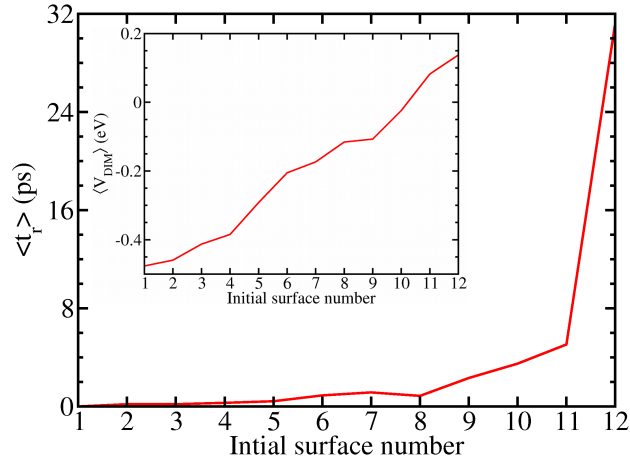


FIG. 2. Average electronic relaxation time of Ar_4^+ to its ground electronic state as a function of the initial Ar_4^+ electronic state. Electronic states are labeled in order of increasing energy. The average DIM energies of Ar_4^+ (in eV), obtained from the diagonalization of the DIM matrix at $t = 0$, are depicted in the inset. The $\text{Ar}^+(^2\text{P}) + 3\text{Ar}$ total dissociation threshold is the reference for energies.

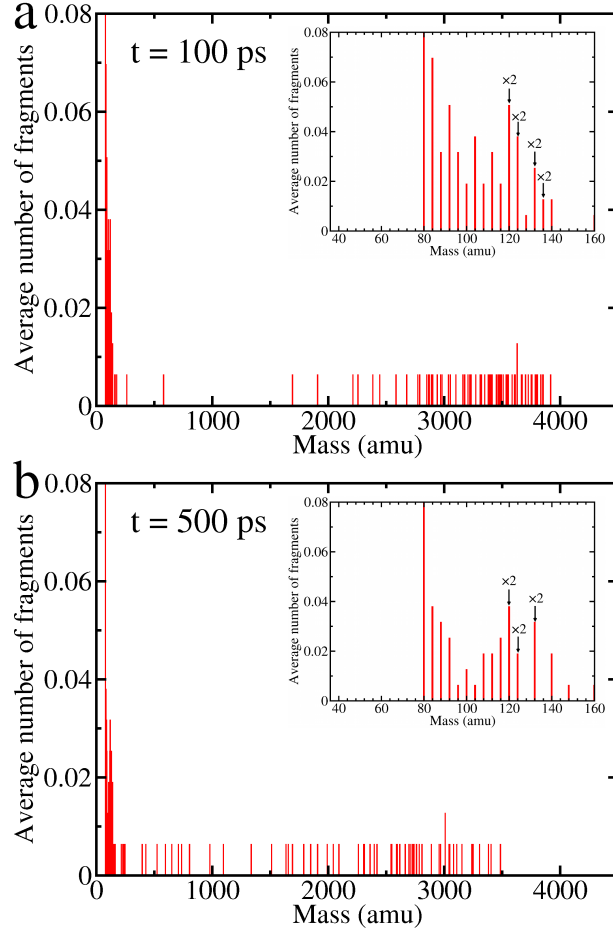


FIG. 3. Theoretical mass spectra of $\text{Ar}_4^+\text{He}_{1000}$ at the end of the 100 ps nonadiabatic simulation (plot a) and at the end of the overall 500 ps simulation (plot b). Ar_2^+He_q and Ar_3^+He_q fragment progressions for masses below 160 amu are reported as insets. When two peaks are nearly superimposed their intensities are summed, the corresponding peak is put at the average mass, and a label “ $\times 2$ ” is added on top of this peak. Sum peaks occur for the pairs $(\text{Ar}_3^+, \text{Ar}_2^+\text{He}_{10})$, $(\text{Ar}_3^+\text{He}, \text{Ar}_2^+\text{He}_{11})$, $(\text{Ar}_3^+\text{He}_3, \text{Ar}_2^+\text{He}_{13})$, and $(\text{Ar}_3^+\text{He}_4, \text{Ar}_2^+\text{He}_{14})$. The relative abundances of the fragments belonging to these four pairs are as follows:

Inset of plot a: (25%,75%), (50%,50%), (75%,25%), and (50%,50%).

Inset of plot b: (83%,17%),(67%,33%), and (80%,20%).

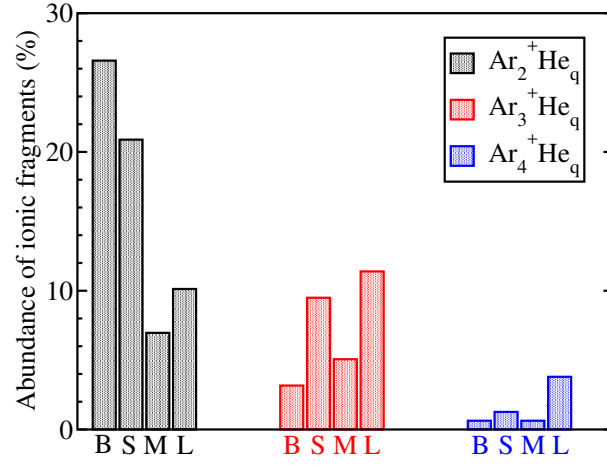


FIG. 4. Relative abundances (in %) of Ar_n^+He_q ($2 \leq n \leq 4$, $0 \leq q \leq 1000$) fragments at the end of the dynamics. The histogram boxes correspond to four groups of ionic fragments, namely bare ions: $q=0$ (label B); small ions: $0 < q \leq 50$ (label S); medium-sized ions: $50 < q \leq 500$ (label M); large ions: $500 < q \leq 1000$ (label L).

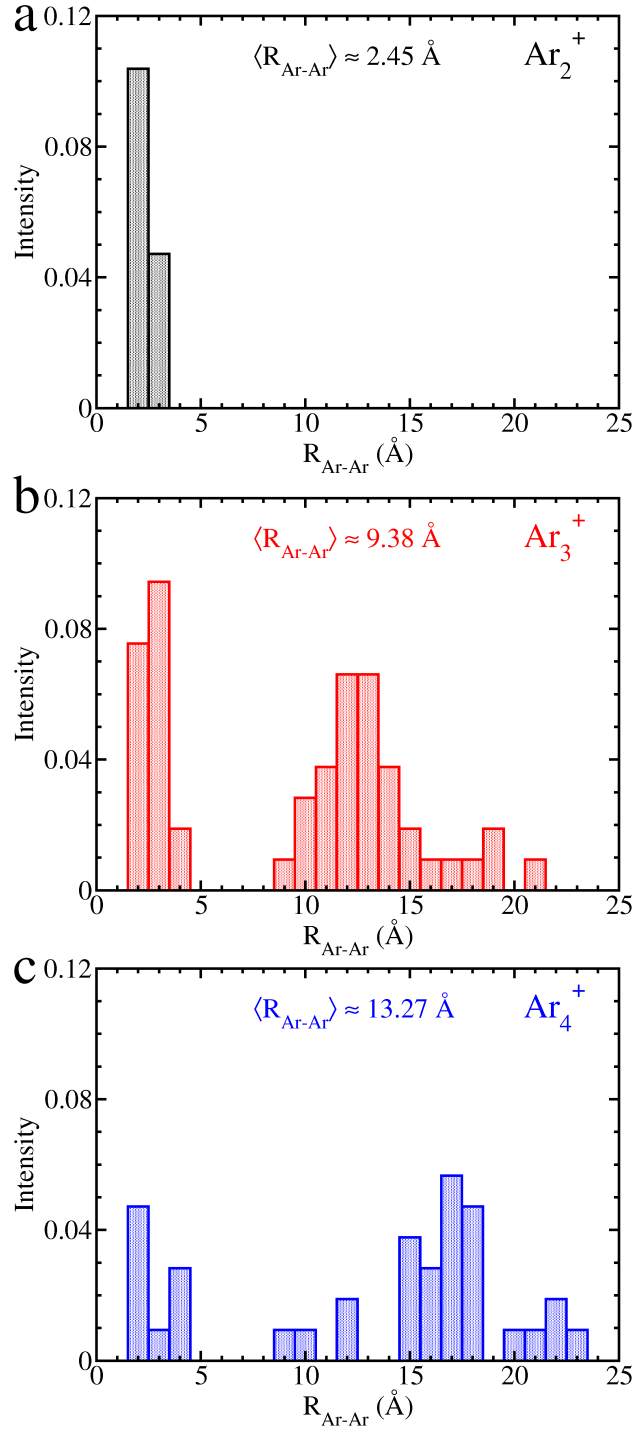


FIG. 5. Average Ar-Ar distance within a) Ar_2^+ , b) Ar_3^+ , and c) Ar_4^+ dopants in large Ar_n^+He_q clusters ($2 \leq n \leq 4$, $q > 500$) at $t = 500$ ps.

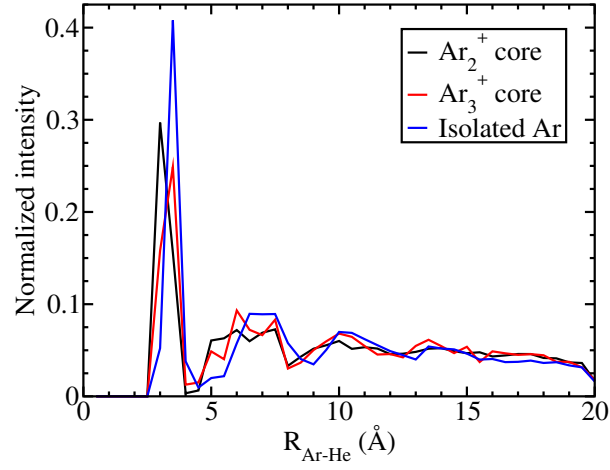


FIG. 6. Radial distributions of Ar-He distances between argon atoms within Ar_2^+ or Ar_3^+ cores (black and red lines, respectively) or isolated neutral argon atoms (blue line) and surrounding helium atoms in large Ar_n^+He_q fragments ($2 \leq n \leq 4$, $q > 500$) at $t = 500$ ps.

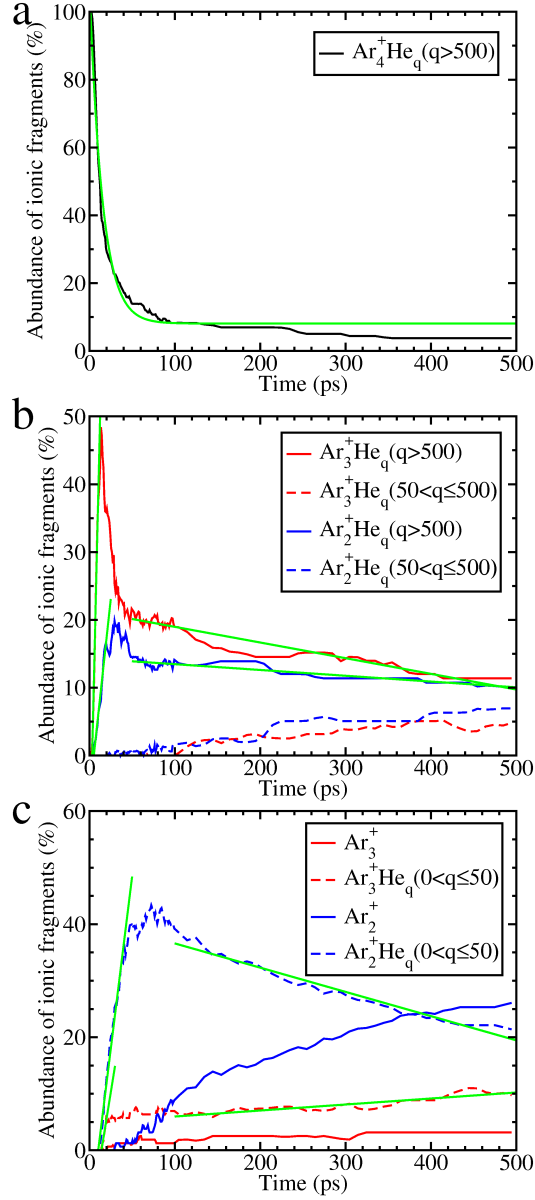


FIG. 7. Time evolution of relative abundances (in %) of Ar_n^+He_q ($2 \leq n \leq 4, q \leq 1000$) fragments upon electron impact ionization of Ar_4 inside a ${}^4\text{He}_{1000}$ droplet. a) Large fragments (or remaining droplets, $q > 500$) containing an Ar_4^+ ion; b) Large ($q > 500$, full lines) or intermediate-sized ($50 < q \leq 500$, dashed lines) ionic fragments for $n = 2$ (blue) and $n = 3$ (red); c) Small ionic fragments ($0 < q \leq 50$, dashed lines) or bare ions ($q = 0$, full lines) for $n = 2$ (blue) and $n = 3$ (red). The green lines are linear or exponential fits (see text). In order to avoid congestion, Ar_4^+He_q fragments with less than 500 helium atoms were not plotted because of their negligible abundances ($< 0.7\%$).

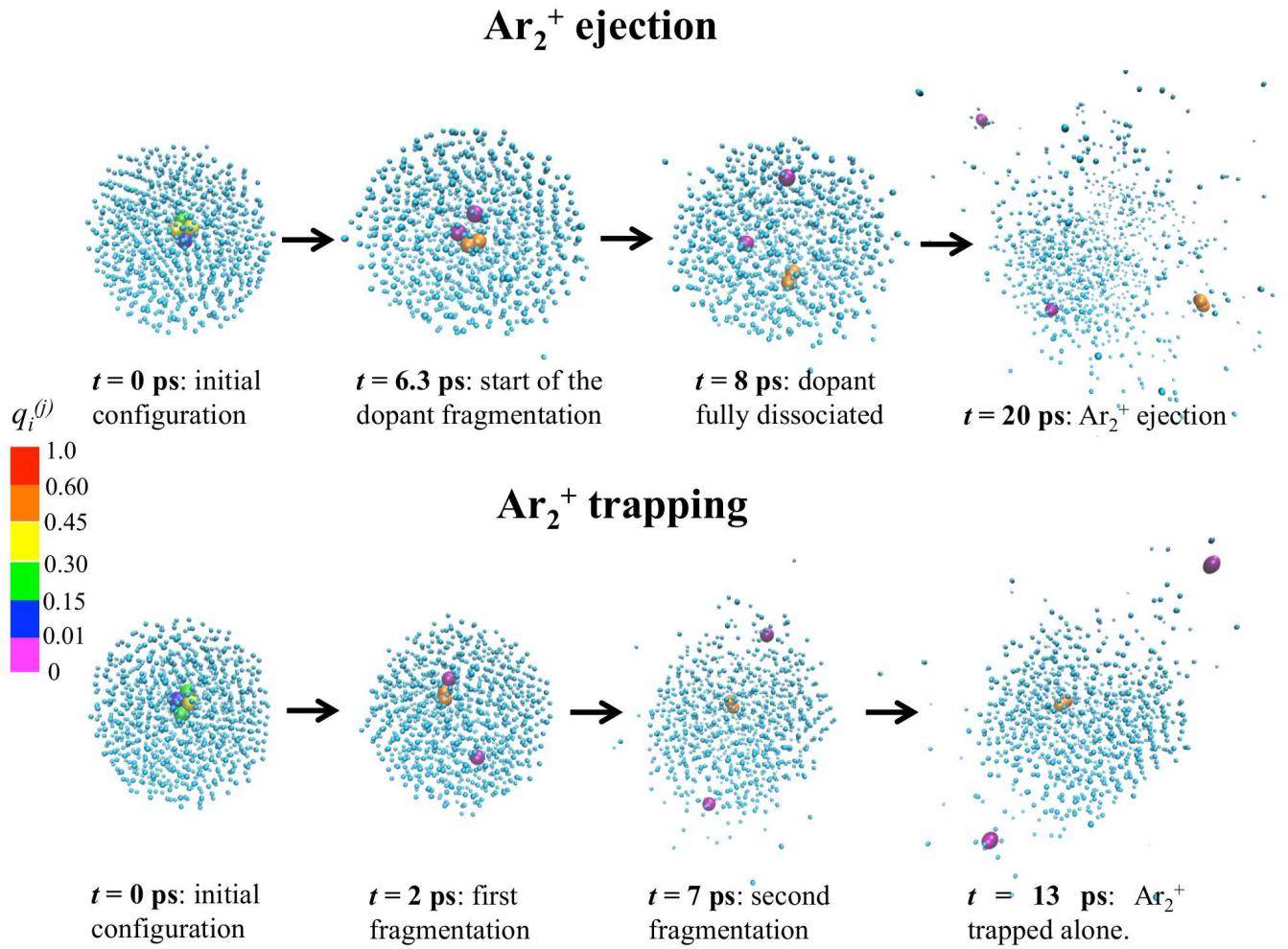


FIG. 8. Selected snapshots of trajectories showing the fast ejection of Ar₂⁺ upon Ar₄ ionization to the Ar₄⁺ electronic state of highest energy (state 12, $V_{12} \approx 0.141$ eV), and the trapping of Ar₂⁺ upon Ar₄ ionization to the Ar₄⁺ electronic state of lowest energy (state 1, $V_1 \approx -0.478$ eV). The color scale on the left aims to provide a visual estimate of charge $q_i^{(j)}$ carried by the four argon atoms, from purple for Ar to red for Ar⁺.

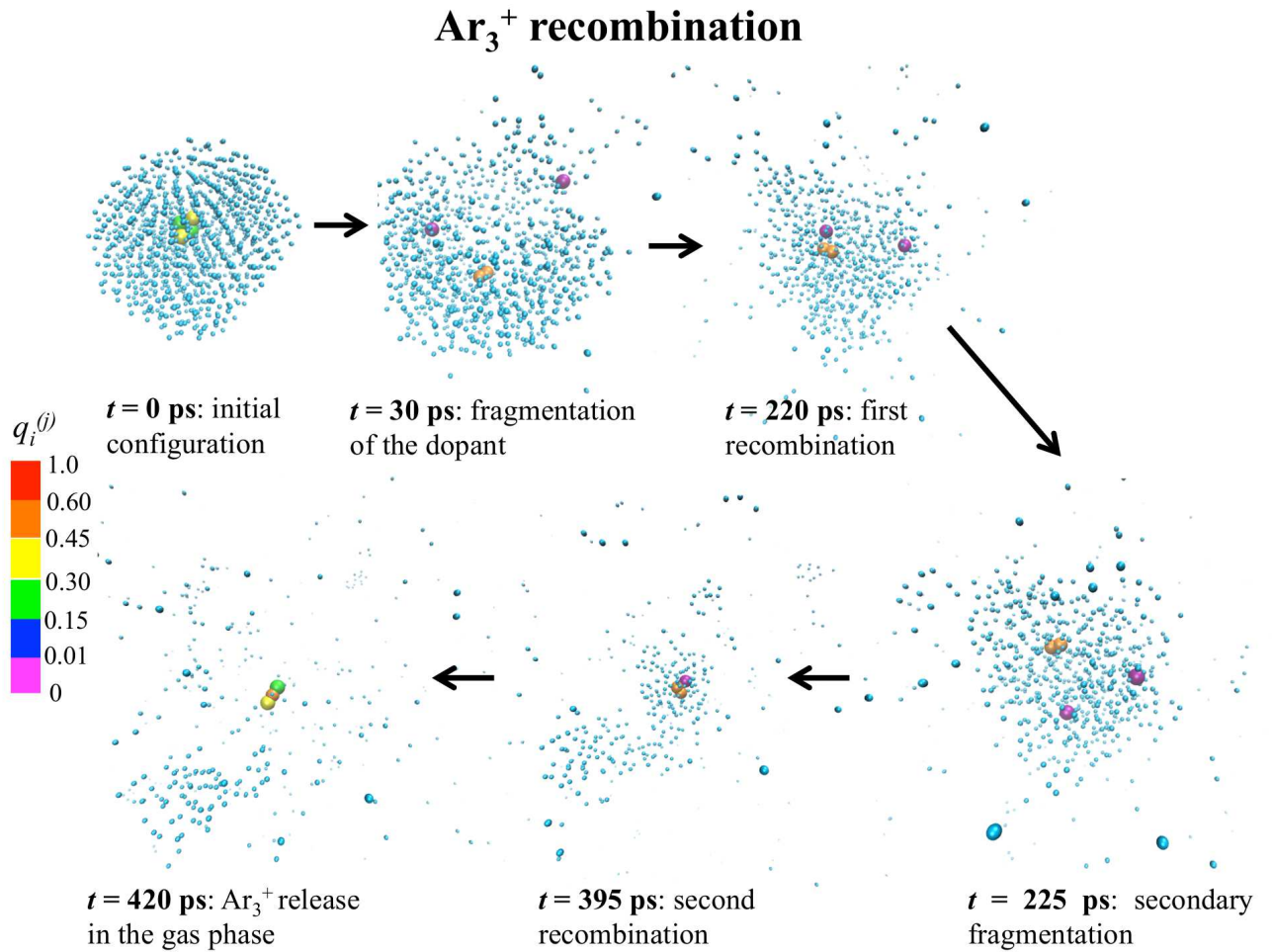


FIG. 9. Selected snapshots of trajectories showing geminate recombinations yielding a secondary fragmentation event and the release of Ar₃⁺ in the gas phase for an initial ionization in the Ar₄⁺ electronic state 6 ($V_6 \approx -0.209$ eV). The color scale on the left aims to provide a visual estimate of charge $q_i^{(j)}$ carried by the four argon atoms, from purple for Ar to red for Ar⁺.

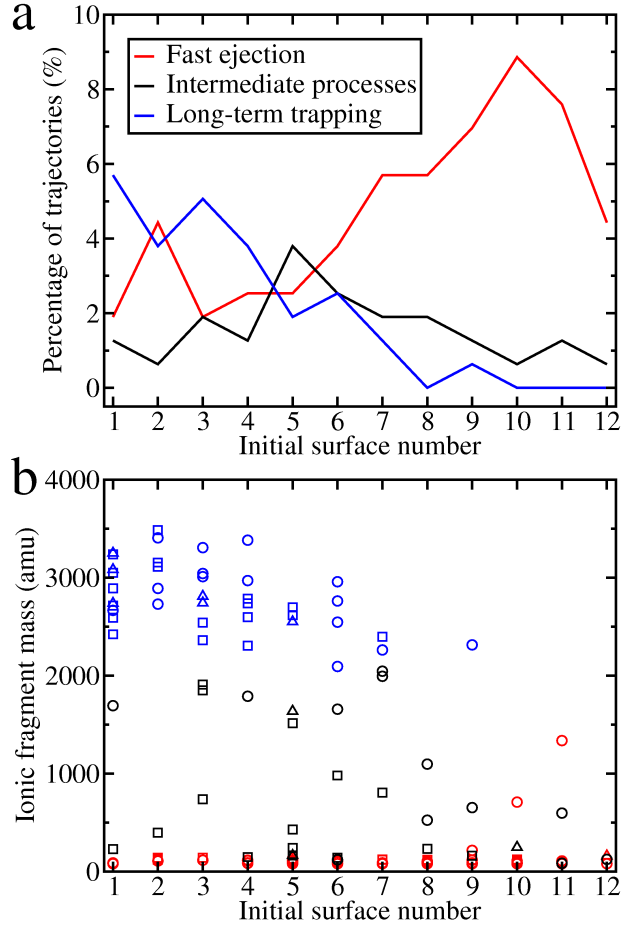


FIG. 10. a) Percentage of trajectories subject to fast ejection of small ionic fragments (red lines), long-term trapping of Ar_n^+ ($2 \leq n \leq 4$, blue lines), or intermediate processes (black lines) as a function of the initial Ar_4^+ electronic state number, these states being sorted in ascending order of energy. The value of 100% is obtained by summing the percentages of the three curves and twelve electronic states. b) Point-cloud diagram showing the mass of ionic fragments containing Ar_2^+ (circles), Ar_3^+ (squares), and Ar_4^+ (triangles) as a function of the initial Ar_4^+ electronic state number at $t = 500$ ps. The color of symbols refers to the dynamical process involved to produce these fragments (red = fast ejection, blue = long-term trapping, black = intermediate process).

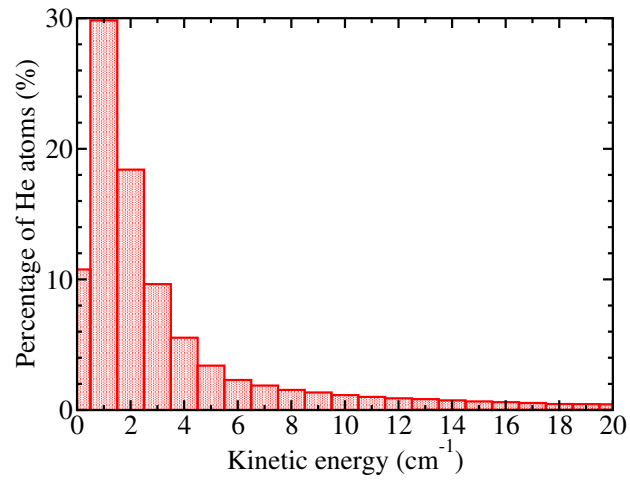


FIG. 11. Typical kinetic energy distribution of helium atoms. The intensity of the distribution is a percentage of the total number of ejected helium atoms.