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Analysis and Cancellation of Mixed-Numerologies Interference for Massive MIMO-OFDM UL

Xinying Cheng, *Student Member, IEEE*, Rafik Zayani, *Member, IEEE*, Hmaied Shaiek, *Member, IEEE*, and Daniel Roviras, *Senior Member, IEEE*

Abstract

The extremely diverse service requirements is an important challenge for the future generations of wireless communication technologies. As promising solutions, orthogonal frequency division multiplexing (OFDM)-based massive multiple-input multiple-output (MIMO) and mixed numerologies transmission are proposed. This letter investigates the transmission of different users, sharing the same bandwidth while they are associated to different numerologies. A transceiver design which aims to manage the mixed numerology spectrum sharing (SS) transmission is first presented. Then, we analyze the inter-numerology interference (INI) and derive its corresponding theoretical expressions. Based on the derived closed-form expressions, a new INI cancellation scheme is introduced, which efficiently mitigates the INI and enhances the performance of massive MIMO-OFDM uplink systems.

Index Terms

Inter-numerology interference (INI), Massive MIMO-OFDM, Mixed numerology (MN), Spectrum sharing (SS)

I. INTRODUCTION

THE future wireless communication systems are expected to support a wide range of services with diverse requirements, where massive MIMO technology is recently recognized as a key feature. The concept was presented in [?], where the base station (BS), equipped with a large number of antennas, serves simultaneously several single-antenna users. The number of users are much smaller than the number of antennas in the BS so that spectral and energy efficiency is improved [?].

The mixed-numerologies transmission is another solution which brings more flexibility in the communication system [?], where the numerology varies based on the requirement of the service characteristics. Different numerologies refer to different parameters setting in OFDM such as subcarrier spacing (SCS), symbol duration and cyclic prefix (CP) length, which are studied in many papers [?][?]. While the implementation of numerology multiplexing significantly improves the system flexibility, the interference between users belonging to different numerologies appears and the INI affects the system performance.

A mixed-numerologies INI model is built, in [?], for single-input single-output (SISO) Windowed-OFDM systems, in which the two users occupy two adjacent subbands. Some works, such as [?][?], proposed the mixed-numerologies SS transmission but they are mainly done in a SISO system on downlink. To the best of our knowledge, general analysis and analytical expressions of the INI in massive MIMO-OFDM systems are still not presented yet. Besides, the efficient INI cancellation algorithm are needed to achieve good performance. Regarding the previous works and motivations behind this work, the main contributions of this letter are:

- A new transceiver scheme is introduced for massive MIMO-OFDM uplink system to enable flexible management of mixed numerology SS transmission.
- An analytical INI model is built for massive MIMO-OFDM system with mixed numerologies. The theoretical INI expressions are derived in closed-form to analyze theoretically the impact of INI.
- An INI cancellation method is investigated, based on the derived theoretical expressions of INI between different numerologies.

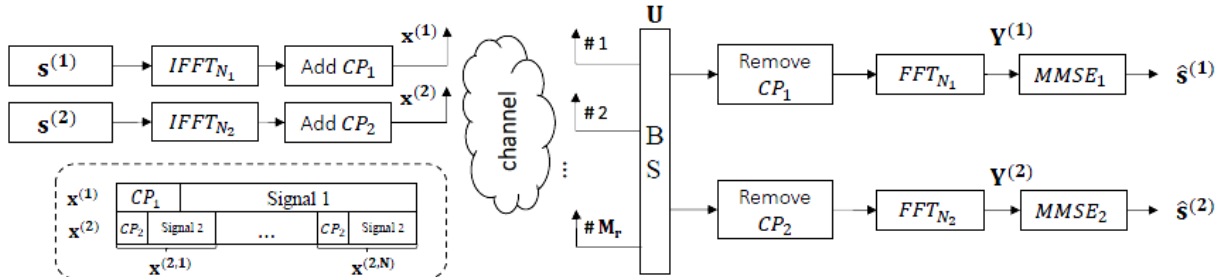


Fig. 1: System model of the massive MIMO OFDM uplink with two different numerologies: M_r receiving antennas at the BS, two single-antenna terminals, two blocks illustrate two different numerologies with OFDM of N_1 and N_2 subcarriers.

The rest of this letter is structured as follows. Section II presents the system model investigated in this study. Section III analyses the INI between different numerologies and gives the theoretical INI expressions and the patterns which influence the INI. Section IV introduces the INI cancellation based on the previous analysis. Simulation results are provided in section V. Finally, the conclusion is given in section VI.

Notations: Lower-case letters (e.g. x), bold lower-case letters (e.g. \mathbf{x}) and bold upper-case letters (e.g. \mathbf{X}) stand for scalars, vectors and matrices, respectively. \mathbf{H} denotes a $M \times N \times K$ 3-dimension matrix. We denote the transpose and conjugate transpose by \mathbf{X}^T and \mathbf{X}^H , respectively. The k -th element in the vector \mathbf{x} is denoted as $\mathbf{x}[k]$. For a $M \times N$ matrix \mathbf{X} , $\mathbf{X}(m, :)$ denote the m -th line and $\mathbf{X}(:, n)$ denote the n -th column. $N \times N$ identity matrix, $M \times N$ all-zeros matrix, $N \times N$ discrete Fourier transform (DFT) matrix and $N \times N$ inverse discrete Fourier transform (IDFT) matrix are denoted by \mathbf{I}_N , $\mathbf{0}_{M \times N}$, \mathbf{DFT}_N and \mathbf{IDFT}_N , respectively. $\text{Diag}(\mathbf{x})$ represents the matrix where the diagonal elements are vector \mathbf{x} and all off-diagonal elements are zero. We use $\|\mathbf{x}\|^2$ and \otimes to denote l_2 -norm of vector \mathbf{x} and the convolution, respectively. $\mathbb{E}\{\cdot\}$ stands for the expectation operation.

II. SYSTEM MODEL

We consider, in this letter, a single-cell massive MIMO-OFDM uplink system, where M_t single-antenna users that are using different numerologies, transmit signals to a BS equipped with M_r antennas, over a frequency-selective channel. M_r is significantly larger than M_t . The M_t users can be divided into I groups using I numerologies, represented by index i , where $i = 1, \dots, I$. N_i and CP_i denote the IFFT/FFT size and CP size of group i , respectively. The BS receives, via the m_r -th antenna, from the m_t -th user over channel $\sqrt{\alpha_{m_t}} \mathbf{h}_{m_r, m_t}$, where α_{m_t} is the large-scale fading, $\mathbf{h}_{m_r, m_t} \in \mathbb{C}^{1 \times D}$ is the time-domain channel impulse response between user m_t and receiving antenna m_r , $m_t = 1 \dots M_t$, $m_r = 1 \dots M_r$ and D is the number of taps.

Then, $\mathbf{h}_{m_r, m_t}^{(i)} = \text{FFT}(\sqrt{\alpha_{m_t}} \mathbf{h}_{m_r, m_t}, N_i)$ is the channel frequency response with FFT size N_i . For a massive MIMO-OFDM system, the channel frequency response is denoted by $\bar{\mathbf{H}}^{(i)} \in \mathbb{C}^{M_r \times M_t \times N_i}$, where

$$\bar{\mathbf{H}}^{(i)}(m_r, m_t, :) = \mathbf{h}_{m_r, m_t}^{(i)} \quad (1)$$

In order to simplify and without loss of generality, we consider, in this letter, two users ($M_t = 2$) using two different numerologies as shown in Fig. 1. $\mathbf{s}^{(1)}, \mathbf{s}^{(2)} \in \mathbb{C}^{1 \times N_1}$ are signals generated by M-quadrature amplitude modulation (QAM) for user 1 and user 2, respectively, with power σ_s^2 . Considering the generalized synchronized scenario, we assume that $N_1 = N \times N_2$, $CP_1 = N \times CP_2$, where $N = 2^\mu$ and μ is an integer [?].

The received signal at the BS, $\mathbf{U} \in \mathbb{C}^{M_r \times (N_1 + CP_1 + D - 1)}$, is the superposition of the signals coming from all users. The noise power at each antenna is $\frac{\sigma_n^2}{M_r}$.

In order to enable flexible management, we consider two detection branches, each for one numerology, at the BS, where two MMSE detectors $\bar{\mathbf{P}}^{(1)} \in \mathbb{C}^{2 \times M_r \times N_1}$ and $\bar{\mathbf{P}}^{(2)} \in \mathbb{C}^{2 \times M_r \times N_2}$ are used.

The received signal is separated into two branches, then, CP_1/CP_2 removing and $\text{FFT}_1/\text{FFT}_2$ are implemented respectively to generate the received signal for user 1 and user 2 (i.e. $\mathbf{Y}^{(1)}$ and $\mathbf{Y}^{(2)} \in \mathbb{C}^{M_r \times N_1}$).

Then, the data streams from the users are detected through linear processing. For n_i -th column of received signal matrix $\mathbf{Y}^{(1)}$ and $\mathbf{Y}^{(2)}$, MMSE detections are implemented by

$$\mathbf{r}_{n_1}^{(1)} = \mathbf{P}_{n_1}^{(1)} \mathbf{Y}^{(1)}(:, n_1) \quad n_1 = 1 \dots N_1 \quad (2)$$

$$\mathbf{r}_{n_2}^{(2, n)} = \mathbf{P}_{n_2}^{(2)} \mathbf{Y}^{(2)}(:, (n-1)N + n_2) \quad n_2 = 1 \dots N_2, n = 1 \dots N \quad (3)$$

where $\mathbf{Y}^{(1)}(:, n_1) \in \mathbb{C}^{M_r \times 1}$, $\mathbf{Y}^{(2)}(:, (n-1)N + n_2) \in \mathbb{C}^{M_r \times 1}$ are the n_1 -th, $((n-1)N + n_2)$ -th column of received signal matrix $\mathbf{Y}^{(1)}$, $\mathbf{Y}^{(2)}$, respectively. $\mathbf{r}_{n_1}^{(1)}, \mathbf{r}_{n_2}^{(2, n)} \in \mathbb{C}^{2 \times 1}$. $\mathbf{P}_{n_i}^{(i)} = \bar{\mathbf{P}}^{(i)}(:, :, n_i) \in \mathbb{C}^{2 \times M_r}$, $i = 1, 2$ denotes the MMSE detection matrix for the n_i -th OFDM subcarrier of numerology i , which can be given as

$$\mathbf{P}_{n_i}^{(i)} = \left(\mathbf{H}_{n_i}^{(i)H} \mathbf{H}_{n_i}^{(i)} + \zeta \mathbf{I}_{M_t} \right)^{-1} \mathbf{H}_{n_i}^{(i)H} \quad (4)$$

where $\mathbf{H}_{n_i}^{(i)} = \bar{\mathbf{H}}^{(i)}(:, :, n_i) \in \mathbb{C}^{M_r \times 2}$, $i = 1, 2$ is the frequency-domain MIMO channel of the n_i -th OFDM subcarrier with numerology i . $\zeta = \frac{\sigma_n^2}{M_r \sigma_s^2}$ is chosen according to the noise level.

After the detection, the estimated signal streams are extracted from $\mathbf{r}_{n_1}^{(1)}$ and $\mathbf{r}_{n_2}^{(2, n)}$, according to the following mapping for each subcarrier

$$\hat{\mathbf{s}}^{(1)}[n_1] = \mathbf{r}_{n_1}^{(1)}[1] \quad (5)$$

$$\hat{\mathbf{s}}^{(2, n)}[n_2] = \mathbf{r}_{n_2}^{(2, n)}[2] \quad (6)$$

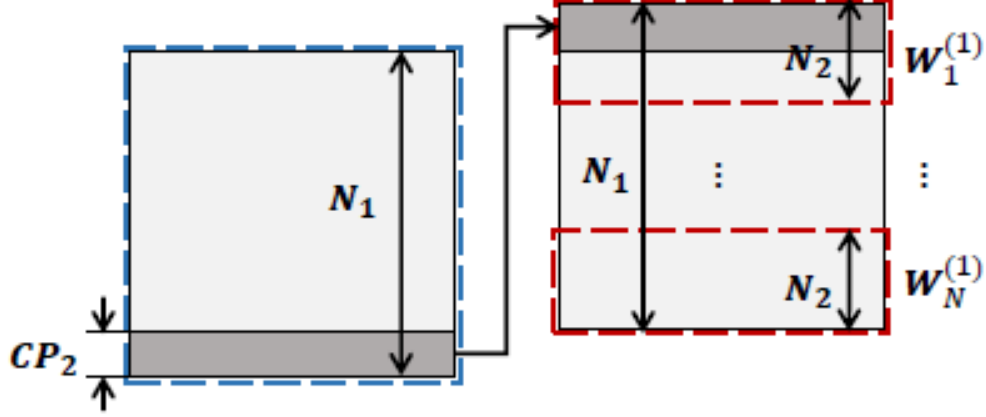


Fig. 2: Structure of matrix $\mathbf{W}^{(1)}$ and matrices $\mathbf{W}_n^{(1)}$.

For the analysis of INI in the following parts, we assume a noise free transmission so that the detections become zero forcing (ZF) detection ($\zeta = 0$). In this case, the following equations are valid:

$$\sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(1)}(2, m_r, n_1) \mathbf{h}\mathbf{f}_{m_r,1}^{(1)}[n_1] \mathbf{s}^{(1)}[n_1] = 0 \quad (7)$$

$$\sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(2)}(1, m_r, n_2) \mathbf{h}\mathbf{f}_{m_r,2}^{(2)}[n_2] \mathbf{s}^{(2,n)}[n_2] = 0 \quad (8)$$

The detection matrices are designed to remove multi-user interference (MUI) within the same numerology. However, in a mixed-numerologies system, INI occurs for each user due to the usage of different numerologies in the same band. Analysis of the INI and its radiation pattern will be given in the next section.

III. INTER-NUMEROLOGY INTERFERENCE ANALYSIS

A. INI from numerology 1 with N_1 to numerology 2 with $N_2 = N_1/N$

First, we consider the INI on user 2 with numerology 2, which uses small IFFT/FFT size. In order to only focus on the INI caused by user 1, we consider a noise-free transmission channel and $\mathbf{s}^{(2)} = 0$.

After the transmission, the signal on the m_r -th line of matrix $\mathbf{Y}^{(2)}$ can be written, in frequency domain, as

$$\mathbf{y}_{m_r}^{(2,n)} = \mathbf{G}^{(1)} \mathbf{W}_n^{(1)} \text{Diag}(\mathbf{h}\mathbf{f}_{m_r,1}^{(1)}) (\mathbf{s}_1)^T \quad (9)$$

where $\mathbf{G}^{(1)} = \mathbf{DFT}_{N_2} \in \mathbb{C}^{N_2 \times N_2}$, $\mathbf{h}\mathbf{f}_{2,m_t}^{(1)} \in \mathbb{C}^{1 \times N_1}$ is the MIMO channel frequency response between user 1 and the m_r -th receiving antenna. $\mathbf{W}_n^{(1)} \in \mathbb{C}^{N_2 \times N_1}$ is the n -th $N_2 \times N_1$ part of matrix $\mathbf{W}^{(1)}$, where $\mathbf{W}^{(1)} \in \mathbb{C}^{N_1 \times N_1}$ is a rotated version of matrix IDFT. The structure of matrix $\mathbf{W}^{(1)}$ is shown on Fig. 2, where the blue dash block is \mathbf{IDFT}_{N_1} , we rotate the last $CP_2 \times N_1$ part above to get $\mathbf{W}^{(1)}$ as shown on the right side. Then, $\mathbf{W}_n^{(1)}, n = 1 \dots N$ is part of $\mathbf{W}^{(1)}$ as the red dash blocks.

Then, the BS uses $\bar{\mathbf{P}}^{(2)}$ for the detection of user 2's signal and the interference of each subcarrier in n -th symbol can be expressed as

$$\mathbf{ini}_n^{(1,2)}[n_2] = \sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(2)}(2, m_r, n_2) \mathbf{y}_{m_r}^{(2,n)}[n_2] \quad (10)$$

From equation (10), the INI on user 2 is caused by all subcarriers of user 1.

B. INI from numerology 2 with N_2 to numerology 1 with $N_1 = N \times N_2$

In this subsection, we focus on the received INI signal on user 1 with numerology 1, which uses large IFFT/FFT size. Similarly, we consider a noise-free transmission channel and $\mathbf{s}^{(1)} = 0$. The signal at the m_r -th line of matrix $\mathbf{Y}^{(1)}$ can be written, in frequency domain, as

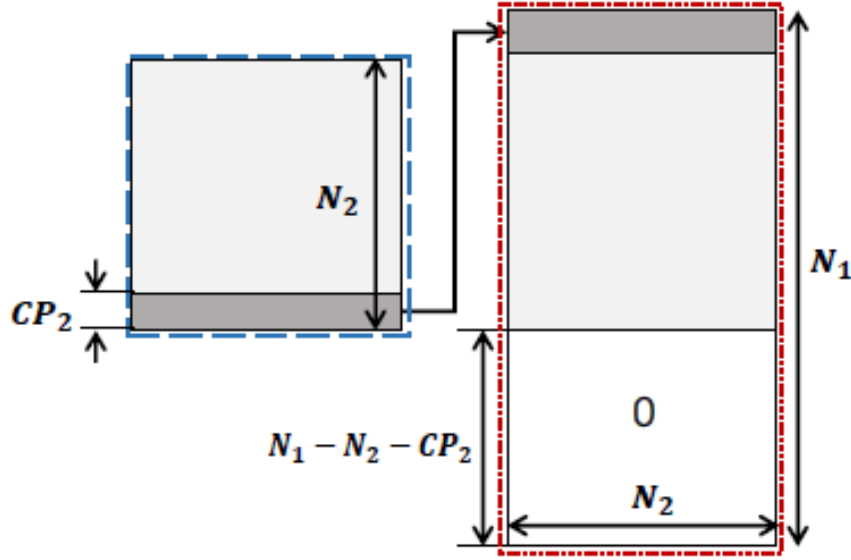


Fig. 3: Structure of matrix $\mathbf{W}_2^{(2)}$ with red dash box.

$$\mathbf{y}_{m_r}^{(1)} = \sum_{n=1}^N \mathbf{E}_n \text{Diag}(\mathbf{h}\mathbf{f}_{m_r,2}^{(1)}) \mathbf{Z}(\mathbf{s}^{(2,n)})^T \quad (11)$$

where $\mathbf{Z} = \mathbf{G}_2^{(2)} \mathbf{W}_2^{(2)} \in \mathbb{C}^{N_1 \times N_2}$,

$$\mathbf{E}_n \in \mathbb{C}^{N_1 \times N_1} = \begin{cases} \mathbf{G}_1^{(2)} \mathbf{W}_1^{(2)} & \text{for } n = 1 \\ \mathbf{G}_2^{(2)} \mathbf{ID}_n^{(2)} \mathbf{W}_3^{(2)} & \text{for } n = 2, \dots, N \end{cases} \quad (12)$$

Structure of matrix $\mathbf{W}_2^{(2)}$ is shown on Fig. 3 with red dot block on the right side, where the blue dash block is \mathbf{IDFT}_{N_2} , we add the last $CP_2 \times N_2$ part above and zeros below to extend the dimension to $N_1 \times N_2$. All the other matrices in the expression are

$$\mathbf{G}_1^{(2)} = [\mathbf{0}_{N_1 \times CP_1} \quad \mathbf{DFT}_{N_1}] \in \mathbb{C}^{N_1 \times (N_1 + CP_1)},$$

$$\mathbf{G}_2^{(2)} = \mathbf{DFT}_{N_1} \in \mathbb{C}^{N_1 \times N_1},$$

$$\mathbf{W}_1^{(2)} = \begin{bmatrix} \mathbf{IDFT}_{N_1} \\ \mathbf{0}_{CP_1 \times N_1} \end{bmatrix} \in \mathbb{C}^{(N_1 + CP_1) \times N_1},$$

$$\mathbf{W}_3^{(2)} = \mathbf{IDFT}_{N_1} \in \mathbb{C}^{N_1 \times N_1},$$

$$\mathbf{ID}_n^{(2)} = \begin{bmatrix} \mathbf{0}_{\xi_1 \times (N_1/2)} & \mathbf{0}_{\xi_1 \times (N_1/2)} \\ \mathbf{I}_{\xi_2} & \mathbf{0}_{\xi_2 \times (N_1 - \xi_2)} \\ \mathbf{0}_{\xi_3 \times (N_1/2)} & \mathbf{0}_{\xi_3 \times (N_1/2)} \end{bmatrix} \in \mathbb{C}^{N_1 \times N_1}$$

for matrix $\mathbf{ID}_n^{(2)}$, we have

$$\begin{cases} \xi_1 = N_1 - (N - n + 1)(N_2 + CP_2) \\ \xi_2 = \begin{cases} N_2 + CP_2 + D & \text{for } n = 2, \dots, N - 1 \\ N_2 + CP_2 & \text{for } n = N \end{cases} \\ \xi_3 = \begin{cases} (N - n)(N_2 + CP_2) - D & \text{for } n = 2, \dots, N - 1 \\ (N - n)(N_2 + CP_2) & \text{for } n = N \end{cases} \end{cases} \quad (13)$$

Then, the BS uses $\bar{\mathbf{P}}^{(1)}$ for the detection of user1's signal and the interference of each subcarrier can be expressed as

$$\mathbf{ini}^{(2,1)}[n_1] = \sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(1)}(1, m_r, n_1) \mathbf{y}_{m_r}^{(1)}[n_1] \quad (14)$$

$\mathbf{ini}^{(2,1)}[n_1]$ is caused by all subcarriers of user 2.

C. INI influencing patterns

Corollary 1: In a constant channel, the purposed transceiver scheme for massive MIMO-OFDM based mixed numerologies SS uplink transmissions, do not generate any INI for both user 1 and user 2 (i.e. $\mathbf{ini}_n^{(1,2)} = 0$, $\mathbf{ini}^{(2,1)} = 0$), due to the

channel frequency response characteristics.

Proof: For a constant channel (i.e. the number of channel taps $D = 1$), different size of FFTs return to the same result. For any $mt = 1 \dots M_t$ and $mr = 1 \dots M_r$, We have

$$\mathbf{h}\mathbf{f}_{mr,mt}^{(1)}[n_1] = \mathbf{h}\mathbf{f}_{mr,mt}^{(2)}[n_2] \quad (15)$$

for all $n_1 = 1, \dots, N_1, n_2 = 1 \dots N_2$.

From (4), the MMSE detection matrices originate from the channel frequency response, which, in a constant channel,

$$\bar{\mathbf{P}}^{(1)}(m_t, m_r, n_1) = \bar{\mathbf{P}}^{(2)}(m_t, m_r, n_2) \quad (16)$$

for all $n_1 = 1 \dots N_1, n_2 = 1 \dots N_2$.

Then, we could rewrite equation (10) and (14) in detail, to indicate the INI on each subcarrier. The INI on each subcarrier of user 1, and user 2 are expressed, respectively, in equation (20) and (19). From (15) and (16), in a constant channel, elements in vector $\mathbf{h}\mathbf{f}_{m_r,2}^{(1)}$ and vector $\mathbf{h}\mathbf{f}_{m_r,2}^{(2)}$ are identical, which leads to $\bar{\mathbf{P}}^{(1)}(1, m_r, n_1) = \bar{\mathbf{P}}^{(2)}(1, m_r, n_2)$, $\bar{\mathbf{P}}^{(1)}(2, m_r, n_1) = \bar{\mathbf{P}}^{(2)}(2, m_r, n_2)$ for all $n_1 = 1 \dots N_1, n_2 = 1 \dots N_2$. With these substitution and equation (7), (8), one can easily observe that $\mathbf{ini}_n^{(1,2)} = 0$ and $\mathbf{ini}_n^{(2,1)} = 0$, for $n = 1 \dots N$.

$$\mathbf{ini}_n^{(1,2)}[n_2] = \sum_{k_2=1}^{N_2} \sum_{n_1=1}^{N_1} \mathbf{G}^{(1)}(n_2, k_2) \mathbf{W}_n^{(1)}(k_2, n_1) \underbrace{\sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(2)}(2, m_r, n_2) \mathbf{h}\mathbf{f}_{m_r,1}^{(1)}[n_1] \mathbf{s}^{(1)}[n_1]}_{\text{equals to 0 in constant channel (7)}} \quad (19)$$

$$\mathbf{ini}^{(2,1)}[n_1] = \sum_{n=1}^N \sum_{k_1=1}^{N_1} \sum_{n_2=1}^{N_2} \mathbf{E}_n(n_1, k_1) \mathbf{Z}(k_1, n_2) \underbrace{\sum_{m_r=1}^{M_r} \bar{\mathbf{P}}^{(1)}(1, m_r, n_1) \mathbf{h}\mathbf{f}_{m_r,2}^{(1)}[k_1] \mathbf{s}^{(2,n)}[n_2]}_{\text{equals to 0 in constant channel (8)}} \quad (20)$$

Corollary 2: Channel selectivity and difference between N_1 and N_2 increase the INIs for both user 1 and user 2

Proof: When the channel is frequency-selective, for all $m_t = 1 \dots M_t$ and $m_r = 1 \dots M_r$, vector $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(1)} \in \mathbb{C}^{1 \times N_1}$ is the interpolation of vector $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(2)} \in \mathbb{C}^{1 \times N_2}$, where $N - 1$ values are added between every two points in $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(2)}$ to construct vector $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(1)}$. From this characteristic, we have

$$\mathbf{h}\mathbf{f}_{m_r,m_t}^{(1)}[(n_2 - 1)N + 1] = \mathbf{h}\mathbf{f}_{m_r,m_t}^{(2)}[n_2] \quad (21)$$

where $n_1 = 1, \dots, N_1, n_2 = 1, \dots, N_2$.

Equation (21) indicates that, for the same time-domain channel between user m_t and receiving antenna m_r , there are limited same-values inside the two channel frequency responses. For other values (i.e. $n_1 \neq (n_2 - 1)N + 1$), the difference between $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(1)}[n_1]$ and $\mathbf{h}\mathbf{f}_{m_r,m_t}^{(2)}[n_2]$ has a close relationship with the channel selectivity and the difference between N_1 and N_2 . Greater selectivity and greater difference between N_1 and N_2 cause greater difference on the two channel frequency responses, which leads to greater interference.

Corollary 3: Power allocation for different users has a direct influence on the INIs at user 1 and user 2.

Proof: For the sake of simplicity and to focus on the INI analysis, in this letter, we adopt a simple power allocation scheme, where the transmitting power of the m_t -th user are equal. As noted before, the received signal matrix \mathbf{U} , is the summation of all the transmitted signals. Thus, the unequal receiving power for each user influences the power of INIs it generates. For example, greater large-scale fading in user m_t (represented by α_{m_t}) leads to smaller receiving power and smaller INI power on other users. The most remote user in the cell suffer the greatest INI.

In our system, having two users with different path-loss (α_1 and α_2), the generated INI power from user 1 on user 2 ($p^{(1,2)}$) and that from user 2 on user 1 ($p^{(2,1)}$) satisfy

$$\frac{p^{(1,2)}}{p^{(2,1)}} = \frac{\alpha_1}{\alpha_2} \quad (22)$$

For example, if $\alpha_2 < \alpha_1$, which indicates that user 2 is farther away from the BS than user 1. Then, the received INI power on user 2 at the BS is higher than the INI received on user 1. On the contrary, if $\alpha_1 < \alpha_2$, user 1 suffers greater INI than user 2.

IV. INI CANCELLATION

As analysed in the previous sections, INIs are generated for each user in a frequency-selective channel. In this section, we introduce an INI cancellation scheme, with the aid of the analytical results of INI presented before. One of the main idea, in massive MIMO uplink transmission, is to reduce the complexity of the transmitters (users) while maintaining the good

transmission quality, by doing all processing at the BS [?]. Also, in massive MIMO, the full channel state is estimated on uplink and can be used in MMSE detection and INI cancellation. In this regard, the proposed INI cancellation method is implemented at the BS side and does not add any complexity to the users. The main method is to calculate the INIs from the estimated signal $\hat{\mathbf{s}}^{(1)}$ and $\hat{\mathbf{s}}^{(2,n)}$.

Then, the signals after INI cancellation are

$$\tilde{\mathbf{s}}^{(1)} = \hat{\mathbf{s}}^{(1)} - \mathbf{ini}^{(2,1)} \quad (23)$$

$$\tilde{\mathbf{s}}^{(2,n)} = \hat{\mathbf{s}}^{(2,n)} - \mathbf{ini}_n^{(1,2)} \quad (24)$$

What is more is that, the proposed INI cancellation scheme can be adapted to any system using more than two numerologies. For a given numerology, the INI cancellation can be efficiently applied by calculating and removing the INIs from all the other users, who use different numerologies. However, it is worth noticing that the proposed INI cancellation method is as sensitive to the imperfect channel state information (CSI) as the MMSE detections.

V. SIMULATION RESULTS

In this section, we evaluate the accuracy of the derived analytical expressions for INI in a mixed numerologies SS massive MIMO-OFDM uplink system. The BS is equipped with $M_r = 100$ antennas and two single-antenna users ($M_t = 2$) that are using two different numerologies, but sharing the same band. A 16-QAM with Gray mapping is considered. Two pairs of numerologies ($N_1 = 1024, N_2 = 512, CP_1 = 72, CP_2 = 36$ and $N_1 = 1024, N_2 = 256, CP_1 = 72, CP_2 = 18$) and four different channel models ($D = 1, 2, 8, 18$) are considered, where the time-domain channel responses $\mathbf{h}_{mr,mt}[d] = c_d$ have i.i.d. circularly symmetric Gaussian distributed values with zero mean and unit variance. It has to be noted that in all cases, the CP length are sufficient to suppress the inter-carrier interference (ICI) and inter-symbol interference (ISI) induced by the channel.

To evaluate the INI, we first consider the transmission without noise. We define the normalized mean-square error (NMSE) as $NMSE_i = \frac{\|\hat{\mathbf{s}}^{(i)} - \mathbf{s}^{(i)}\|^2}{\|\mathbf{s}^{(i)}\|^2}, i = 1, 2$.

The NMSE values in dB, under different conditions for the user of interest with the transmission system introduced in this letter, are shown on TABLE I. Note that all simulation results shown in TABLE I are with $\alpha_1 = \alpha_2$. One can note on TABLE I, that, INIs occur on both user except for the constant channel. Also, these results match perfectly with the analysis done in section III.C, showing that channel selectivity and difference between N_1 and N_2 increase the INIs. For example, for the same pair of numerologies, $N_1 = 1024, N_2 = 512$, there is 9 dB of degradation on $NMSE_1$ under channel $D = 8$ compared to channel $D = 2$ and 13 dB under channel $D = 18$. Meanwhile, when we compare the results under the same channel selectivity, different pairs of numerologies give different performance, where users suffer more INI when the difference between IFFT/FFT size increases. For example, over the same frequency-selective channel with $D = 2$, the performance of user 1 is worse when the interference is from $N_2 = 256$ than that from $N_2 = 512$ (4 dB difference).

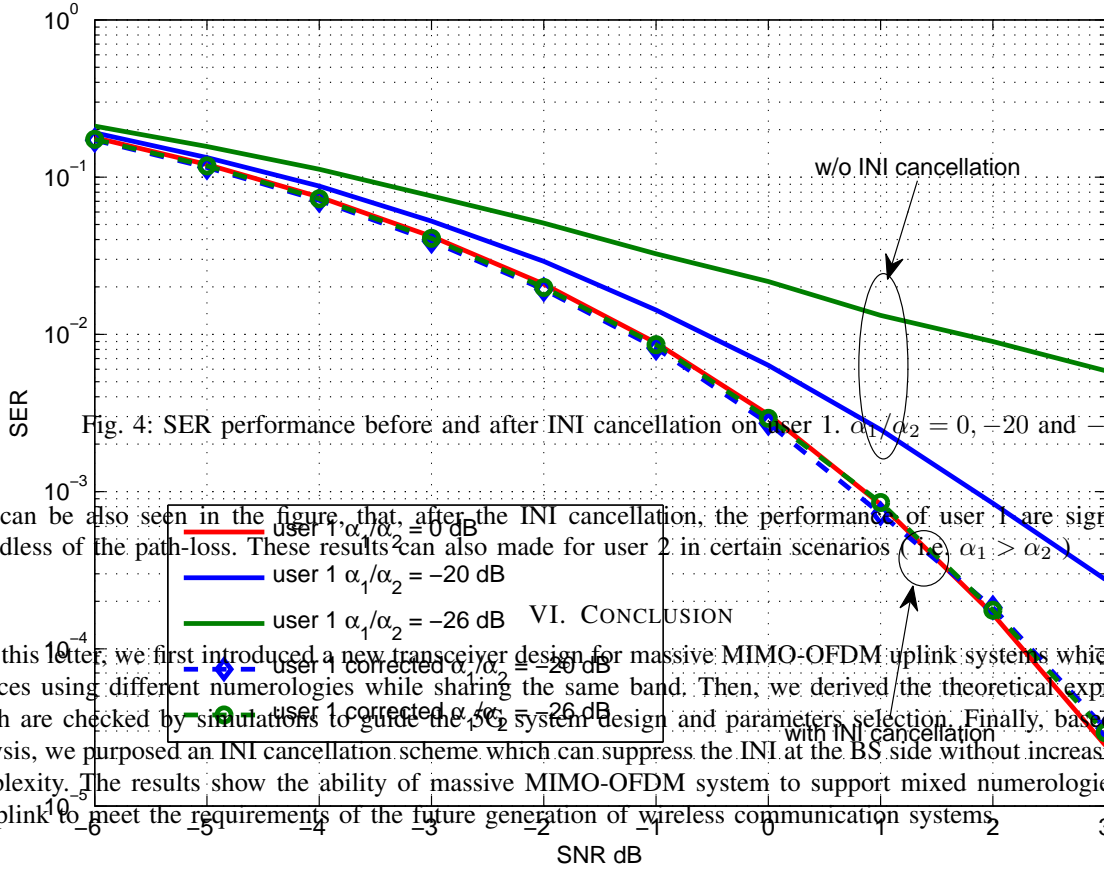
TABLE I: NMSE (dB) of user of interest with interfering numerology and different channels

User of Interest	user1 ($N_1 = 1024$)		user2($N_2 = 512$)	user2($N_2 = 256$)
Interfering User	user2($N_2 = 512$)	user2($N_2 = 256$)	user1($N_1 = 1024$)	
$D = 1$	-300	-300	-300	-300
$D = 2$	-56	-52	-52	-49
$D = 8$	-47	-45	-44	-40
$D = 18$	-43	-40	-39	-36

Looking at TABLE I, the NMSE of INI is always very small (-36 dB for the maximum value) and should have a limited impact for classical SNRs encountered in real wireless communication systems. Nevertheless, it has to be pointed out that these values are for users with same path-loss: $\alpha_1 = \alpha_2$. If we consider a more realistic scenario with the long term evolution (LTE) path-loss model given by [?] $\alpha_{mt,dB} = 128.1 + 37.6 \log_{10}(d_{mt})$, where d_{mt} is the distance from the user mt to the BS in km. Then, values of α_1 and α_2 will change. Note that $\alpha_{mt,dB}$ is the value α_{mt} in dB, with the relationship $\alpha_{mt,dB} = 10 \log_{10} \alpha_{mt}$. To confirm the analysis of INI with the influence of path-loss pattern, in a scenario with a cell radius equals to 1 km, we suppose three different pair of locations: $d_1 = d_2 = 1$, $d_1 = 1, d_2 = 0.3$ and $d_1 = 1, d_2 = 0.2$, which correspond to $\alpha_1/\alpha_2 = 0$ dB, -20 dB and -26 dB, respectively.

Fig. 4 presents the symbol error rate (SER) vs. signal-to-noise ratio (SNR) of different users with/without INI cancellation, using $N_1 = 1024, N_2 = 512, D = 8$, under the three different pair of locations. The SNR is defined as $SNR = M_t \frac{\mathbb{E}\{\|\mathbf{x}^{(i)}\|^2\}}{\sigma_n^2}$.

We can observe that the performance of user 1 is significantly declined when its path-loss increases compared with user 2. For example, when $SNR = 3$ dB, user 1 can achieve $SER \leq 10^{-5}$ when $\alpha_1/\alpha_2 = 0$ dB while this SER is improved to 10^{-3} when $\alpha_1/\alpha_2 = -26$ dB.



It can be also seen in the figure, that, after the INI cancellation, the performance of user 1 are significantly improved, regardless of the path-loss. These results can also be made for user 2 in certain scenarios (i.e., $\alpha_1 > \alpha_2$).

VI. CONCLUSION

In this letter, we first introduced a new transceiver design for massive MIMO-OFDM uplink systems which supports different services using different numerologies while sharing the same band. Then, we derived the theoretical expressions of the INI, which are checked by simulations to guide the system design and parameters selection. Finally, based on the theoretical analysis, we proposed an INI cancellation scheme which can suppress the INI at the BS side without increasing the transmitter's complexity. The results show the ability of massive MIMO-OFDM system to support mixed numerologies SS transmissions on uplink to meet the requirements of the future generation of wireless communication systems.

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