Optimal configuration of a far-infrared radiometer to the study the Arctic winter atmosphere

Laurence Coursol¹, Quentin Libois², Pierre Gauthier¹, Jean-Pierre Blanchet¹

 $^1 \rm Université$ du Québec à Montréal (UQAM), Montréal, Canada $^2 \rm CNRM,$ Université de Toulouse, Météo-France, CNRS, Toulouse, France

6 Key Points:

1

2

3

4 5

7	• FIR channels add information for UTLS water vapor compared to standard MIR channels
9	• IC is used to optimize the channels frequencies and widths of a FIR radiometer
10	• A high DFS is reached with only a few channels of an optimized FIR radiometer

 $Corresponding \ author: \ Laurence \ Coursol, \verb"laurence.coursol@gmail.com"$

11 Abstract

Several FIR satellite missions are planned for the next decade, with a special in-12 terest for the Arctic region. A theoretical study is performed to help about the design 13 of a FIR radiometer, whose configuration in terms of channels number and frequencies 14 is optimized based on information content analysis. The problem is cast in a context of 15 vertical column experiments (1D) to determine the optimal configuration of a FIR ra-16 diometer to study the Arctic polar night. If only observations of the FIR radiometer were 17 assimilated, the results show that for humidity, 90% of the total information content 18 is obtained with 4 bands whereas for temperature 10 bands are needed. When the FIR 19 measurements are assimilated on top of those from the Advanced Infrared Sounder (AIRS), 20 the former bring in additional information between the surface and 850 hPa and from 21 550 hPa to 250 hPa for humidity. Moreover, between 400 hPa and 200 hPa, the FIR ra-22 diometer is better than AIRS at reducing the analysis error variance for humidity. This 23 indicates the potential of FIR observations for improving water vapor analysis in the Arc-24 tic. 25

²⁶ 1 Introduction

Since the beginning of meteorological satellites, temperature profiling has been per-27 formed with sounders in the infrared (IR) (Wark & Hilleary, 1969). The state-of-the-art 28 instruments that probe the mid-infrared (MIR) are the Infrared Atmospheric Sounding 29 Interferometer (IASI) (Blumstein et al., 2004), the Atmospheric Infrared Sounder (AIRS) 30 (Aumann et al., 2003) and the Cross-track Infrared Sounder (CrIS) (Bloom, 2001). Those 31 instruments use the 15 μ m CO₂ absorption band to probe atmospheric temperature and 32 the water vapor vibrational band at 6.3 μ m to retrieve humidity profiles (Rizzi et al., 33 2002). This humidity profiling capability results from the strong spectral variations of 34 the water vapor absorption in that band. 35

Water vapor also exhibits an extended rotational absorption band as well as a con-36 tinuum in the far-infrared (FIR; 15 $\mu m < \lambda < 100 \mu m$). This absorption band is broader 37 than the vibrational band, hence there is more energy in this region. Previous studies 38 have pointed out the potential of FIR for atmospheric profiling, particularly in cold re-39 gions. First, a direct consequence of the temperature dependence of the Planck function 40 in the radiative transfer equation, emission is shifted to the FIR as the temperature of 41 the scene decreases, offering a greater capability for cold scenes (M. Mlynczak et al., 2007), 42 in contrary to the traditional 6.3 μ m band quickly loses energy as the scene gets colder 43 (Susskind et al., 2003). Practically, more than half of the radiation is lost to space in the 44 FIR in the polar regions (M. Mlynczak et al., 2007). Second, the water vapor rotational 45 absorption band in the FIR has many absorption lines with larger optical depth than 46 the MIR, which leads to an increased sensitivity to small water vapor variations (Harries 47 et al., 2008). The increased sensitivity is especially important in the upper troposphere, 48 where the water vapor concentration is scarce (Clough et al., 1992). Thus, the FIR re-49 gion can be valuable for profiling the atmosphere and particularly in the stratosphere 50 and the upper troposphere (Shahabadi & Huang, 2014). 51

Despite these acknowledged advantages of the FIR over the MIR for water vapor 52 profiling, no direct spectrally resolved measurements of the atmospheric radiation have 53 been made recently from space. The last measurements in the FIR, up to 25 μ m, were 54 made 40 years ago on two Russian Meteor spacecrafts and 45 years ago by the IRIS (In-55 frared Interferometer Spectrometer and Radiometer) instruments on the NASA Nimbus 56 III and IV (M. G. Mlynczak et al., 2002), data that has been used to identify changes 57 in spectral outgoing longwave radiation (?, ?). However at the time, the spectral and spa-58 tial resolutions of the observations, along with the large noise, prevented from getting 59 much geophysical information out of the data. Since then, low noise liquid helium cooled 60 bolometers operating in the far-IR have been developed, and used for instance in the Far-61 Infrared Spectrometer of the Troposphere (FIRST) instrument (M. G. Mlynczak et al., 62

2006). Such systems are however too delicate, massive and expensive to be but on a satel lite. This, in combination with the intrinsic higher sensitivity of MIR sensors compared
 to FIR sensors, explains why no FIR satellite has been flying for decades now.

Only with the recent advent of uncooled systems operating at room temperature 66 that have space missions in the FIR seen a renewal of interest. The series of satellite mis-67 sions Climate Absolute Radiance and Refractivity Observatory (CLARREO) (Wielicki 68 et al., 2013) is intended to measure spectrally-resolved Earth emission spectrum between 69 5 - 50 μ m with a spectral resolution of 0.5 cm⁻¹ to determine small changes in the spec-70 tral outgoing radiation (infrared and reflected solar). The mission aims at detecting decadal 71 changes in climate forcings, responses and feedbacks and to serve for reference intercal-72 ibration in space. It thus focuses on global or regional averages and their variations on 73 annual timescales. As a consequence the noise-equivalent temperature difference (NETD), 74 has the requirement to be smaller than 10 K in the FIR since averaged over a year it will 75 be reduced to 0.01 K globally. The requirements on the absolute accuracy are on the con-76 trary much more stringent. ESA candidate mision, called FORUM (Far Infrared Out-77 going Radiation Understanding and Monitoring) (Palchetti et al., 2016) focuses on study-78 ing the forcings and the feedbacks of atmospheric water vapor and of ice clouds on the 79 climate. The recently funded NASA PREFIRE (Polar Radiant Energy in the Far-InfraRed 80 Experiment) CubeSat, to be launched in 2022, intends to measure in the 0-45 μ m range 81 to measure spatial and temporal variations in spectral fluxes on hourly to seasonal timescales 82 (L'Ecuyer, 2019). Merrelli and Turner (2012) used the technical characteristics of CLARREO 83 to compare two interferometers for remote sensing of temperature and humidity, with 84 a spectral resolution of 0.5 cm⁻¹, one measuring in the MIR and another measuring in 85 the FIR even though CLARREO was not designed to measure temperature and water 86 vapor. They showed that there is more information content in the FIR compared to the 87 MIR when the noise is equal in both spectral regions. However, if the uncertainty of the 88 actual CLARREO is used for the FIR region, the advantage of the FIR is lost (Shahabadi 89 et al., 2015). 90

Only a limited selection of channels among those in the water vapor absorption band 91 of interferometers at high resolution is used in data assimilation (Fourrié & Thépaut, 2003). 92 Supposedly, adjacent bands could thus be merged into larger bands to refine the remote 93 sensing capability. The Arctic was selected since around 60~% of the outgoing longwave 94 radiation is in the FIR region. Also, there is a need for precise water vapor measurements 95 in the troposphere (Müller et al., 2016) and especially in the Arctic (Boullot et al., 2016) 96 and the FIR upwelling spectrum contains a large amount of potential profiling informa-97 tion. The objective of the present study is to design an optimal FIR radiometer to study 98 the Arctic polar night by examining different configurations, noise levels and the tradeoff between spectral resolution and noise level. Thus, this study considers a radiometer 100 in the Arctic region using different filters or a gratings to allow different bandwiths within 101 a spectral region. As in Observing System Simulation Experiments (OSSEs), synthetic 102 measurements are created for different configurations of the FIR radiometer. The radio-103 metric noise of the Far InfraRed Radiometer (FIRR) is used as a baseline to constrain 104 the detector's performance (Libois et al., 2016). The optimal configuration is selected 105 with information content as a metric to lead to the best temperature and humidity anal-106 vses. The impact of FIR measurements is also evaluated in terms of their added value 107 when assimilated on top of currently assimilated AIRS data. The experiments are done 108 under the assumption that AIRS and the FIR radiometer are collocated and assimilated 109 in a simple 1D assimilation system. 110

The paper is organized as follows. Section 2 presents the information content framework, the characteristics of the instrument, and the context of the experiments. Section 3 presents the results of the evaluation of different instrument configurations. Section 4 compares the impact of measurements of the FIR radiometer with that of AIRS measurements. A discussion and conclusions are presented in section 5.

116 2 Methods

This section first presents the characteristics of the FIR radiometer and the atmospheric conditions used in this study. Finally, we present the method used to evaluate the information content of measurements which is based on the reduction of analysis error obtained in the context of data assimilation using a numerical weather forecast as an *a priori* background state.

122

159

2.1 Instrument characteristics

A synthetic spaceborne FIR radiometer is considered in this study. The goal is not 123 to investigate a particular instrument, but to explore the potential of such a novel in-124 strument, in the framework of the prepartaion of the TICFIRE mission. Nevertheless, 125 the characteristics of this radiometer are based on the FIRR instrument. The charac-126 teristics of the optics are fixed (field of view, spatial resolution, F-number, etc), only those 127 of the detector are changed. The detector performance explore a realistic range, although 128 the feasibility study for such performance is left to the industry. The two principal char-129 acteristics considered are its number of bands and its noise-equivalent radiance (NER). 130 The bands are adjacent and fully cover the range of 15 - 100 μ m. The transmittance is 131 one in the bands and zero outside. The bandwidths are set in three different ways here-132 after referred as 'equi-energetic', 'constant wavelength' and 'constant wavenumber'. Equi-133 energetic means that each band receives the same amount of energy at the top of the at-134 mosphere (TOA), this is calculated for each atmospheric profile used. This implies that 135 the spectral widths of the bands are not constant. Constant wavelength and constant 136 wavenumber bands means that each bands has the same spectral width in microns or 137 cm^{-1} respectively. The NER is varied through the experiments, but two specific NER 138 will be highlighted, called baseline NER and target NER. The baseline NER is equal to 139 $0.01 \text{ Wm}^{-2} \text{sr}^{-1}$, according to the findings of Libois et al. (2016). Those detector char-140 acteristics are consistent with a microbolometer sensor coated with gold black for a in-141 tegration time of 1 s (Proulx et al., 2009) The other specific value of NER used, target 142 NER, is equal to $0.002 \text{ Wm}^{-2} \text{sr}^{-1}$, which is the expected NER in a few years from now 143 , expected from efforts by the industry, mainly on the electronics and on the analog to 144 digital conversion. Also, band splitting is achievable with a grating or filters. It was cho-145 sen to use NER instead of NETD for the radiometric resolution in order to work at the 146 sensor level. This allows to evaluate the gain of changing the radiometric resolution and 147 the spectral width of the bands independently. NER remains constant independently of 148 the instrument spectral configuration, while NETD would change. Since the NER is con-149 stant, this results in less energy per band when the bandwidth is reduced. It needs to 150 be noted the correlation between radiometric and spectral resolutions, when the num-151 ber of bands increases, the signal-to-noise ratio decreases as the energy per band decreases. 152

Figure 1 shows the NETD for a blackbody at 250 K for a constant NER of 0.01 Wm⁻²sr⁻¹ for an instrument with 10, 15, 20, 25 and 40 equi-energetic bands. The NETD is not constant for the bands of a configuration. This allows to compare this experiment with other studies using NETD. It shows that the NETD, for a configuration with 10 bands, is comparable to the NETD of AIRS, below 0.5 K (Garand et al., 2007), and of MODIS, less than 0.35 K (Xiong et al., 2008).

2.2 Atmospheric profiles

The radiosonde profiles are from the Integrated Global Radiosonde Archive (IGRA) database (http://www.ncdc.noaa.gov/oa/climate/igra/) (Durre et al., 2006). Figure 2 shows the locations of the eight stations where the different vertical profiles were taken. Those stations are the same as in Serreze et al. (2012) and were selected to represent the various atmospheric conditions in the Arctic. It needs to be noted that the Arctic region was chosen, but those results would be similar for the Antarctic region. For each station, 6 profiles were selected randomly from the months of January or February of 2015



Figure 1. NETD for different configurations of equienergetic bands for a blackbody at 250 K with a constant NER of 0.01 $Wm^{-2}sr^{-1}$. The vertical lines represent the widths of equi-energetic bands.



Figure 2. Locations of the eight Arctic stations. The letter codes are: JM- Jan Mayen; BN-Bjornoya; SD- Scoresbysunde; DM- Danmarkshavn; BW- Barrow, AL- Alert; EU- Eureka; RB-Resolute Bay.

or 2016 in order to sample Arctic winter conditions. The profiles were truncated at 20 167 km altitude. Table 1 shows the vertical resolution of the atmospheric profiles selected. 168 Figure 3 shows the averaged 48 temperature and humidity profiles selected with the red 169 and blue lines respectively and the shaded area of the same color shows the correspond-170 ing standard deviation. The natural variability in the profiles seen through the standard 171 deviation can be associated with different meteorological situations. The larger spread 172 near the surface is expected since there is more variability in that region. Also, the peak 173 seen at 4 km in the standard deviation is due to the averaged water vapor mixing ra-174 tio being almost equal to the standard deviation at that point. 175

Altitude interval (km)	Vertical resolution (km)
0 - 0.1	0.01
0.1 - 1	0.025
1 - 3	0.1
3 - 5	0.2
5 - 8	0.5
8 - 12	0.5
12 - 20	2

 Table 1. Vertical resolution of the atmospheric profiles from IGRA



Figure 3. Temperature and humidity profiles averaged for the 48 radiosoundings at eight Arctic stations shown with the red and blue lines respectively. The shaded area shows the standard deviation associated with the variables.

176 **2.3 Theoretical framework**

In this section, the theoretical framework used is explained. This study is based
on linear statistical estimation theory in the context of numerical weather prediction (NWP)
(Rodgers, 2000). The different notations, definitions, approximations and data used are
described in this section (Lewis et al., 2006).

The atmospheric state is represented by a vector **x** and the satellite radiance measurements at different wavelengths at the TOA are represented by the vector **y**. The observation is related to the atmospheric state through the equation

$$\mathbf{y} = H(\mathbf{x}) + \epsilon_o,\tag{1}$$

where H is the forward model linking the observation to the atmospheric profile 184 and ϵ_{o} is the observation error. In this case, the state corresponds to atmospheric pro-185 files of temperature, \mathbf{T} , and logarithm of specific humidity $\ln \mathbf{q}$ defined on k vertical lev-186 els on which the model state is defined. The dimension of the model state \mathbf{x} is thus 2k. 187 The ozone and other trace gases are kept constant. The assimilation seeks to correct an 188 a priori estimate of the state of the atmosphere, $\mathbf{x}_{\mathbf{b}}$, also referred to as the background 189 state, using the information contained in the observations. It takes into account the rel-190 ative accuracies of \mathbf{x} and \mathbf{y} to obtain a minimum variance estimate, $\mathbf{x}_{\mathbf{a}}$, called the *anal*-191 ysis. 192

A linearization of the forward model around the atmospheric profile, \mathbf{x}_b is done, which gives, assuming that the radiative-transfer equation is weakly nonlinear near the background state

$$H(\mathbf{x}) \cong H(\mathbf{x}_b) + \mathbf{H}(\mathbf{x} - \mathbf{x}_b),\tag{2}$$

¹⁹⁶ where $H(\mathbf{x}_b)$ is the background state in the observations space and $\mathbf{H} = \frac{\partial H(x)}{\partial x}\Big|_{x_b}$ ¹⁹⁷ is the linearized observation operator with respect to \mathbf{x} evaluated at $\mathbf{x} = \mathbf{x}_b$, referred ¹⁹⁸ to as the Jacobian.

The analysis, \mathbf{x}_a , which represent the corrected atmospheric state after the observations and the model are taken into consideration, is given by

$$\mathbf{x}_a = \mathbf{x}_b + \mathbf{K}(\mathbf{y} - \mathbf{H}\mathbf{x}_b) \tag{3}$$

201

205

with $\mathbf{K} = \mathbf{B}\mathbf{H}^{T}(\mathbf{R}+\mathbf{H}\mathbf{B}\mathbf{H}^{T})^{-1}$ being the gain matrix. **B** is the background error covariance matrix and **R**, the observation error covariance matrix (Rodgers, 2000). The superscript T and -1 denote respectively the transpose and inverse of a matrix.

2.3.1 Jacobians

For each band, the Jacobian indicates how temperature and humidity variations 206 in each band impact the radiance measured at the TOA. The Jacobians were obtained 207 by finite difference with the radiative-transfer model MODTRAN v 5.4 (Berk et al., 2005) by perturbing the background state \mathbf{x}_b , in this case a temperature and humidity profile. 209 The Jacobians were computed for each band of the FIR radiometer and AIRS. A sub-210 set of 142 channels were used for AIRS. It is assumed that the FIR radiometer and AIRS 211 are collocated on a pixel with the same spatial response and taht the lag between the 212 instruments is negligible. More specifically, for the temperature Jacobians, \mathbf{H}_{Ti} , at the 213 level i, a perturbation of ± 0.5 K was done (Garand et al., 2001). Perturbations of 1 K 214 have been deemed sufficiently small for this experiment. This gives the variation of ra-215 diance seen at the TOA for a variation of 1 K in the atmospheric profile at each atmo-216 spheric level. In the same manner, the humidity Jacobians in logarithm of specific hu-217 midity, s = ln q, at the level i, were obtained by perturbations of ± 0.05 q, where q is the 218 specific humidity and $s = \ln(q)$. As shown with the following equation, in order to ob-219 tain a Jacobian with respect to a logarithm, the perturbations are done on the profile 220 in q. Thus by multiplying the difference of perturbations by 10, this results in Jacobians 221 with the units of $Wm^{-2} sr^{-1} \log(L L^{-1})^{-1}$. 222

$$\mathbf{H}_{s,i} = \frac{\partial R}{\partial lnq} = \frac{\partial q}{\partial lnq} \frac{\partial R}{\partial q} = q \frac{\partial R}{\partial q}$$
(4)

2.3.2 Background error covariance matrix

The matrix \mathbf{B} is the background error covariance matrix associated with the back-224 ground state \mathbf{x}_{b} . Figure 4 represents the **B** matrix used for temperature (left) and hu-225 midity (right). The **B** matrices are the stationary components of the background term 226 of the Environment Canada assimilation system (Buehner et al., 2015). Those matrices 227 were evaluated for a latitude of $79^{\circ} 59' 20''$, which corresponds to Eureka, Canada for 228 the month of February. The units used are K^2 and $\log(L L^{-1})^2$ for temperature and hu-229 midity respectively. The cross-terms \mathbf{B}_{Ts} and \mathbf{B}_{sT} are considered equal to zero, and thus 230 only the components \mathbf{B}_{TT} and \mathbf{B}_{ss} of the **B** matrix are considered. Making this approx-231 imation allows to calculate the DFS and analysis error for temperature and humidity sep-232 arately. In this study, the matrices \mathbf{B}_{TT} and \mathbf{B}_{ss} are kept constant. 233



Figure 4. Background error covariances matrices **B** for temperature (left) and logarithm specific humidity (right) at a latitude of $79^{\circ} 59' 20''$ for the month of February

234

223

2.3.3 Observation error covariance matrix

The matrix **R** is the observation error covariance matrix. Normally, the matrix **R** 235 takes into consideration the measurement error, the forward-model error, the represen-236 tativeness error and the error associated with quality control to name a few (Bormann 237 et al., 2010) but for this study, only the measurement error was considered. This approx-238 imation was taken to be consistent with previous studies in the FIR region such as Merrelli 239 and Turner (2012), Shahabadi and Huang (2014) and Mertens (2002). They show that, 240 in the thermal IR region, the main contribution to the observation error is the measure-241 ment error and also, the interchannel correlation error is small (Garand et al., 2007). The 242 measurement error is assumed to be gaussian and unbiased, assumptions used especially 243 in data assimilation (Rodgers, 2000). Therefore, the matrix \mathbf{R} is assumed to be diag-244 onal with the NER values on the diagonal. The spectral NER for the instrument AIRS 245 was taken from the AIRS website (https://airs.jpl.nasa.gov/index.html) version 5 L1B 246 data. The NER for the synthetic instrument is assumed to be constant for each config-247 uration and each band since it comes from the sensor. 248

249 2.3.4 Information content

The impact of measurements is estimated from the analysis error covariance and the degrees of freedom per signal (DFS). The analysis error, assumed here to be unbiased, is $\varepsilon_a = \mathbf{x}_a - \mathbf{x}_t$ where \mathbf{x}_t is the true state of the atmosphere. So, $\mathbf{A} = \langle \varepsilon_a \varepsilon_a^T \rangle$, with $\langle ... \rangle$ being the statistical average, is the analysis error covariance matrix and can be shown to be

$$\mathbf{A} = (\mathbf{I} - \mathbf{K}\mathbf{H})\mathbf{B}.\tag{5}$$

The reduction of analysis error due to the assimilation of observations is measured by

$$tr(\mathbf{AB}^{-1}) = N - tr(\mathbf{KH}),\tag{6}$$

where $tr(\mathbf{KH}) = tr(\mathbf{HK})$. The gain in information, or the DFS is defined as

$$DFS = tr(\mathbf{HK}). \tag{7}$$

The DFS can then be viewed in two ways, in the observation space and in the model space. In the observation space, the DFS measures the independent degrees of freedom measured by the observations and take into account redundancy. In the model space, it measures the reduction of analysis error with respect to the background error.

It is an evaluation technique based on the relative errors between the observations and the prior information (Purser & Huang, 1993). It has also been used to quantify the added value of a new set of observations by comparison with other types of measurements and also on top of measurements already assimilated (McNally et al., 2006; Lupu et al., 2011)

Thus, the analysis error variance matrix **A** and the DFS depend on the background 267 error covariance matrix \mathbf{B} , the observation error covariance matrix \mathbf{R} and the Jacobian 268 matrix **H**. The DFS will be used as a metric for obtaining the optimal configuration of 269 the FIR radiometer and to discuss the trade-off between spectral resolution and noise 270 level. The analysis error variance matrix will be used to see the vertical impact when 271 the FIR radiometer is assimilated. Those calculations for the DFS and analysis error vari-272 ance were done for the 48 atmospheric profiles individually, and are then averaged. The 273 calculations for 48 atmospheric profiles show the added value on average and also its vari-274 ability for the different possible atmospheric situations in the Arctic. The standard de-275 viation spread for the DFS and the analysis error variance will be shown in figures 7 and 276 10 respectively. 277

278

257

3 Evaluation of configurations

279

3.1 Optimization under constraints

In this section, the DFS is used to discuss the trade-off between spectral resolution and noise level.

Figure 5 shows the total DFS for temperature of different configurations for a syn-282 thetic FIR radiometer with constant wavenumber configuration when the NER error level 283 varies between 0.0003 and 0.02 $\mathrm{Wm^{-2} sr^{-1}}$ and a spectral range of 15 to 100 $\mu\mathrm{m}$. The 284 total number of bands varies between 1 and 200 bands. The color represents the value 285 of the DFS for this configuration. Hence, this figure shows that for a fixed NER, the DFS 286 increases and then decreases as the number of bands increases. This figure can be use-287 ful when there are technological constraints for example. If the NER is imposed by the 288 available technology, taking a horizontal line on the top panel of figure 5 highlights the 289



Figure 5. Top panel: The averaged total DFS is shown for variations of the NER level (y-axis) and variations of the total number of bands for temperature of the constant wavenumber bands configuration. The DFS for each configuration is shown with the colorbar. Bottom panel: The number of bands that maximizes DFS as a function of the NER (blue dots) and the DFS maximum as a function of the NER (purple line).

available spectral configurations. The maximum DFS is not with smaller bands (right 290 side of the figure) but always with a configuration which has less than 50 bands. This 291 is due to the constant NER. By having smaller bands, the amount of energy per band 292 decreases and hence the signal-to-noise ratio decreases. This is also shown in the bot-293 tom panel, which shows with blue dots the number of bands of the configuration with 294 the maximal DFS for a variation of the NER. This shows that having more bands is not 295 always the best configuration, since the DFS is not increasing as the number of bands 296 increases. The number of bands with the peak DFS gets larger as the NER decreases. 297 Another interesting way to analyze this map is by having a constraint on the number 298 of bands an instrument can have. A radiometer can be operated with a filter-wheel and 299 as the number of bands increases, the rate of repetition decreases and also the cost in-300 creases. 301

Figure 6 is similar to figure 5 but for humidity, but was cut off at 100 bands to better see the shift in the DFS peak. It has a lot more variability in the DFS for an horizontal line compared to temperature. This variability is partly due to spectral features of transmittance. For humidity, the maximum DFS is always obtained with a configuration which has less than 55 bands.

307 **3.2** M

3.2 Maximisation of the total DFS

In this section, the DFS is used to find an optimal configuration for the FIR radiometer considered in this study. Three different splitting of the bands are considered, equi-energetic, constant wavelength bands and constant wavenumber bands. The instrument will be split between 1 and 250 bands.

³¹² Considering those three configurations, figure 7 shows the total DFS averaged over ³¹³ the 48 profiles for temperature and humidity. Two values of the NER were used for the ³¹⁴ level of error, namely $0.01 \text{ Wm}^{-2}\text{sr}^{-1}$ and $0.002 \text{ Wm}^{-2}\text{sr}^{-1}$. To show the variability, the ³¹⁵ standard deviation is shown with the shaded area. Note that several papers have inves-³¹⁶ tigated the channel selection and information content of AIRS (e.g. Fourrié and Thépaut



Figure 6. Top panel: The averaged total DFS is shown for variations of the NER level (y-axis) and variations of the total number of bands for humidity of the constant wavenumber bands. The DFS for each configuration is shown with the colorbar. Bottom panel: The number of bands that mazimizes DFS as a function of the NER (blue dots) and the DFS maximum as a function of the NER (purple line).

(2003); Divakarla et al. (2006); Garand et al. (2007)). However, different **B** and **R** matrices were used, which prevents direct comparison with this previous work.

For temperature, for the three cases, as the number of bands increases the total 319 DFS decreases. This is due to the constant NER, which results in less energy when the 320 bandwidth is reduced. For the configuration having constant wavelength bands, the peak 321 in DFS is reached with more bands compared to the other configurations. The bands 322 being too wide near 15 μ m, there is not enough resolution to capture the variation in 323 the transmittance in this part of the spectrum. Table 2 shows the maximum DFS for 324 each configuration with the corresponding number of bands for both temperature and 325 humidity for the target noise. When the NER is reduced, there is a large increase in the 326 DFS as expected since it means that the measurements are more accurate. For exam-327 ple, there is an increase by a factor of 2.00 in the DFS for the constant wavenumber band 328 configuration when the NER goes from $0.01 \text{ Wm}^{-2}\text{sr}^{-1}$ to $0.002 \text{ Wm}^{-2}\text{sr}^{-1}$. For the dif-329 ferent configurations, the standard deviation varies between 0.209 to 0.247 which is less 330 than for AIRS which is equal to 0.513 for temperature. The highest DFS is with the con-331 stant wavenumber band configuration with 22 bands for the NER level of $0.002 \text{ Wm}^{-2} \text{sr}^{-1}$. 332 This is the configuration that will be used for temperature for the remainder of this study. 333 The individual DFS of the optimal configuration of the 22 constant wavenumber bands 334 is 20 % smaller than AIRS. However, when those bands are assimilated on top of AIRS, 335 (table 2), the value of the DFS increases by 13.2 % compared to when AIRS is assim-336 ilated alone. This means that even after the information in the thermal IR is assimilated, 337 there is still value in assimilating data in the FIR. 338

For humidity, the highest DFS is also with the constant wavenumber bands con-330 figuration with now 7 bands and a total DFS of 3.594 for the NER error of 0.002 $Wm^{-2}sr^{-1}$. 340 For the remainder of the study, this configuration will be considered as the optimal configuration. 341 Similarly to temperature, there is more variability for the constant wavelength config-342 uration. For humidity, the standard deviation is larger compared to temperature, i.e. it 343 varies between 0.318 and 0.354 depending on the configuration while it is 0.666 for AIRS. 344 Also, when compared individually to AIRS (table 2), the DFS for the optimal config-345 uration with 7 constant wavenumber bands is smaller than the DFS of AIRS by 14%. 346



Figure 7. The averaged total DFS as a function of the total number of bands for three configurations which are equi-energetic bands (blue line), constant bandwidths in terms of wavelength (green line) and wavenumber (orange line) for temperature (left) and humidity (right). The dashed lines are for a NER of $0.01 \text{ Wm}^{-2}\text{sr}^{-1}$ whereas the full lines are for the target NER of $0.002 \text{ Wm}^{-2}\text{sr}^{-1}$. The shaded area represent the standard deviation of the 48 atmospheric profiles which are shown for all configurations except for AIRS. The standard deviation of AIRS is equal to 0.53 and 0.67 for temperature and humidity respectively. The purple line represents the averaged total DFS of AIRS for the 48 atmospheric profiles.

When those 7 bands in the FIR are assimilated on top of AIRS (table 2), the DFS increases by 11.5%, compared to assimilating only AIRS, which shows that measurements in the FIR add information when assimilated on top of AIRS data.

3.3 Selection of the bands with most information

350

Considering a fixed number of bands for the FIR radiometer, following Rabier et 351 al. (2002), we now evaluate the DFS sequentially. First, for each atmospheric profile, the 352 DFS is calculated for each band of the configuration and the one that maximises the DFS 353 is selected. It is shown as the first position in figure 8. The next band selected is the one 354 that, when added to the previous one, adds the largest information content. This pro-355 cess is done until all the bands are selected. Each new band thus optimally increases the 356 DFS. This type of calculation was also done for ice cloud properties for AIRS by Chang 357 et al. (2017). This selection was done for each of the 48 atmospheric profiles and for both 358 temperature and humidity. Thus, figure 8 shows the frequency each band is selected at 359 each position for the optimal configuration of the FIR radiometer with 22 constant wavenum-360 ber bands for temperature. It shows that 50 % of the time, the first band selected cor-361 respond to the first band (dark orange) in the splitting with the bandwidth 15.02-15.62 362 μ m. In first and second position, the bands selected are always between 15.02 μ m and 363 $20.58 \ \mu\text{m}$. Also, in the last position, the last band (dark pink) with bandwidth 79.53-364 100 μ m is selected 66.67 % of the times whereas the second to last band in the splitting 365 (bandwith 66.03-79.53 μ m) is selected 33.33 % of the time. 366

Similarly for humidity, figure 9 shows the order of selection of the 7 constant wavenumber bands with respect to humidity through the atmospheric profiles. It shows that the first band selected is 58.3 % of the time the third band (mint green) which has boundaries of 19.83 - 23.62 μ m whereas the second band (yellow) is selected 22.92 % of the times. For the second band selected, 62.5 % of the time, it is the 5th band (dark blue) that is selected. The last band selected is always the first band (orange) which has boundaries between 15.02 - 17.09 μ m.

	Temperature			
Constant wavenumber bands	22	4.399	12.64	
Constant wavelength bands	138	3.996	-	
Equi-energetic bands	10	4.294	-	
AIRS	-	5.488	10.58	
Background error	-	-	19.62	
AIRS + constant wavenumber bands	22	6.213	9.97	
	Humidity			
Constant wavenumber bands	7	3.594	1.09	
Constant wavelength bands	15	3.482	-	
Equi-energetic bands	10	3.569	-	
AIRS	-	4.173	1.03	
Background error	-	-	1.96	
AIRS + constant wavenumber bands		4.714	0.95	

Number	of	bands	DFS	Analysis	error	variance
rumber	or	banas	DID	7 1101 y 515	CITOI	variance

Table 2. Total averaged DFS for a NER of 0.002 $\text{Wm}^{-2}\text{sr}^{-1}$ and analysis error variance. The units for the analysis error variance is K^2 and $\log(LL^{-1})^2$ for temperature and humidity respectively



Figure 8. Probability of each band to be selected at each position for the 22 constant wavenumber bands with respect to temperature.

374 4 Analysis error

The impact of the observations can be seen with the analysis error variance since it provides information about the vertical distribution. The DFS previously discussed gives information integrated through the profile. Equation 2.3 is used to obtain the analysis error variance. To show the added value of the FIR radiometer when other types of instruments are assimilated, the instrument AIRS is considered.

Figure 10 shows the analysis error variance profile for temperature and humidity when the optimal FIR radiometer and AIRS are assimilated. The dark green curve represents the background error, the dark blue curve is the average over the 48 atmospheric profiles for the FIR radiometer whereas the shaded area represents the standard deviation associated with the variability obtained through the different profiles. The dark



Figure 9. Probability of each band to be selected at each position for the 7 constant wavenumber bands with respect to humidity.

pink curve represents the averaged analysis error variance for AIRS whereas the peach 385 curve shows when the FIR radiometer is assimilated with AIRS. For temperature, AIRS 386 is better at reducing the error compared to the FIR radiometer except at 300 hPa. It 387 is also at this height that the gain in assimilating the FIR radiometer on top of AIRS 388 is seen. Also, the sum of the analysis error variance through the profile is shown in ta-389 ble 2, which allows to see the impact of the observations in the model space. Hence, as-390 similating the FIR radiometer after AIRS allows to reduces by 5.65 % the analysis er-391 ror variance. The main gain of the FIR radiometer is with respect to humidity. The FIR 392 radiometer is better at reducing the error in the upper atmosphere, between 400 hPa and 393 200 hPa, than AIRS. When the 7 bands of the FIR radiometer are assimilated on top 394 of AIRS, there is a non negligible gain near the surface (between the surface and 850 hPa) 395 and in the upper part of the atmosphere (between 400 hPa and 200 hPa). The gain near 396 the surface is due to the FIR radiometer being sensitive to the temperature inversion layer. 397 For the different profiles, there is some variability in the atmospheric conditions which 398 is seen with the standard deviation, especially between the surface and 600 hPa which 399 is expected. In the same way, with table 2, it shows that assimilating the FIR radiome-400 ter after AIRS allows to reduce by 12.84 % the analysis error variance for humidity. Mertens 401 (2002) did a similar study on the ability of the FIR to improve water vapor retrievals. 402 The conclusions are similar in the sense that both studies find that the main reduction 403 in the analysis error variance is between 1000 hPa and 100 hPa and that there is a gain 404 in using both the MIR and the FIR. 405

To show the impact of each individual band on the analysis error variance profile, 406 the humidity Jacobians of the FIR radiometer (left panels) and the analysis error vari-407 ance associated with each of these bands when assimilated sequentially (right panels) 408 is shown in figure 11 for two specific atmospheric cases with (top panel) and without (bot-409 tom panel) a temperature inversion. The colors of the bands of the Jacobians are asso-410 ciated with the colorbar. The top left panel of figure 11 shows the signature of two ef-411 fects: the greenhouse effect and the presence of a temperature inversion layer. The neg-412 ative peak is due to the greenhouse effect of water vapor. Increasing the humidity tends 413 to reduce emission of radiance by masking the lower warmer layers. The positive part 414 near the surface is due to an inversion. Increasing humidity elevates the effective emmi-415 sion altitude, where the atmosphere is warmer due to the inversion (?, ?). Moreover, as 416 the wavelength of the band increases, the peak's height increases from around 600 hPa 417



Figure 10. Analysis error variance profile for temperature (left) and humidity (right) for the optimized FIR radiometer. The green curve represents the background error **B**, the dark blue curve the average on the 48 atmospheric profile whereas the shaded area represents its associated standard deviation. The dark pink line is the analysis error variance of AIRS whereas the peach line represents when the optimized FIR radiometer is assimilated after AIRS.

to 350 hPa. The top right panel of figure 11 shows, as in figure 10, the analysis error vari-418 ance for the background error, when all the bands of the FIR radiometer and AIRS are 419 assimilated separetely which is represented by the dark green, blue and dark pink lines 420 respectively. To show the impact on the analysis error of each band of the FIR radiome-421 ter, bands were sequentially assimilated and the analysis error variance was calculated 422 after each new band of the FIR radiometer was assimilated. The order of assimilation 423 of each band is the same as in section 3.3. It shows that the first band assimilated, the 424 pale green one, reduces the error between 800 hPa and 300 hPa, which is where the Ja-425 cobian's peak is. The second band, navy blue one, has a higher Jacobian's peak (at around 426 400 hPa) and it is mainly where the analysis is reduced, between 650 hPa and 200 hPa. 427 The next two bands assimilated, vellow and purple lines respectively, are also shown in 428 the figure. The reduction of the analysis error near the surface is mainly due to the yel-429 low band (17.1-19.8 μ m), which is interesting since it allows to restrain the uncertainty 430 in the inversion layer. This illustrates the complementarity of these bands to obtain the 431 best analysis over the whole vertical extent. Compared to AIRS (dark pink line), the FIR 432 radiometer is better at reducing the error between 350 hPa and 250 hPa. To show the 433 impact of the temperature inversion, the bottom panels of figure 11 shows the Jacobians 434 and the analysis error variances for an atmospheric case without a temperature inver-435 sion. The left panel shows that the Jacobians are more spread out and sample the at-436 mosphere from near the surface up to 300 hPa. Also, compared to the other case, there 437 is no positive peak in the Jacobians which is expected since it is due to a temperature 438 inversion layer. For the analysis error variance (bottom right panel), with the Jacobians 439 peak being lower, the analysis error variance is less reduced compared to the case with 440 an inversion. Even though, the FIR radiometer reduces more the analysis error variance 441 than AIRS between 350 hPa and 200 hPa. Also, near the surface, the FIR radiometer 442 is better at reducing the analysis error variance when there is an inversion. 443



Figure 11. Left panels show the humidity Jacobians for the FIR radiometer associated with two atmospheric cases, which are with (top panel) and without (bottom panel) a temperature inversion. The different colors are the 7 associated bands of this configuration shown by the colorbar which is valid for both panels. The right panel show the analysis error variance for the two cases. The curves from right to left are the background error, when the bands of the FIR radiometer are assimilated one at the time from one band to four (light green, dark navy, yellow and purple), when all the 7 bands are assimilated and AIRS is assimilated.

444 5 Conclusions

The objective of the present study is to design an optimal FIR radiometer to study 445 the Arctic polar night by examining different configurations, noise levels and the trade-446 off between spectral resolution and noise level. This was investigated through an infor-447 mation content analysis based on optimal estimation method. The optimal configura-448 tion for the synthetic FIR radiometer is with 22 constant wavenumber bands for tem-449 perature and 7 constant wavenumber bands for humidity. It was shown that too many 450 bands with a large noise do not give enough information on the atmosphere. With a few 451 bands, it was possible to get a DFS similar to AIRS when compared individually. Given 452 that AIRS provides information also on both temperature and humidity, the impact of 453 assimilating FIR measurements on top of AIRS data was evaluated by the reduction in 454 analysis error variance. With respect to temperature, there is a small impact in assim-455 ilating the FIR radiometer measurements over AIRS between 400 and 250 hPa. On the 456 contrary, for humidity, there is a non negligible gain near the surface (between the sur-457 face and 850 hPa) and in the upper part of the atmosphere (between 400 hPa and 200 458

hPa). Something else that is worth noting is that between 400 hPa and 200 hPa, taken
individually, the FIR radiometer is better at reducing the humidity analysis error variance than AIRS.

Measurements in the FIR are unlikely to be assimilated in the next few years in 462 NWP systems, however the results shown in this paper highlight the potential of this 463 new type of observations which may become available in the next decade. It is non neg-464 ligible to get results similar to AIRS in reducing the analysis error for humidity with only 465 7 bands compared to a subset of 142 bands from AIRS. FIR measurements could be used 466 in regions where there is still large uncertainties in water vapor retrieval or assimilation. 467 It was shown to be useful for retrieval of water vapor in the 400 hPa to 200 hPa region 468 for the Arctic, but FIR radiometry can be useful in other regions as well. 469

The results presented here, are based on a 1D assimilation of two collocated instru-470 ments. Another interesting aspect of this study is the method, which facillitates test-471 ing rapidly multiple configurations of an instrument. Also, it allowed to compare the rel-472 ative impact of measurements in the FIR and the MIR. However, there are limitations 473 to this approach that need to be kept in mind. Because a satellite does provides mea-474 surements over the whole globe, it would be mortant to examine the impact one could 475 expect in other regions such as the Tropics for instance. Finally, complex Observing Sim-476 ulated Systems Experiments (OSSEs) would be needed to evaluate the global impact in 477 a context including all observations currently assimilated. 478

479 Acknowledgments

This research has been funded in part by the Canadian Space Agency (CSA) through

the FAST program, the Grants and Contribution program of Environment and Climate

482 Change Canada (ECCC) and the Natural Sciences and Engineering Research Council

⁴⁸³ of Canada (NSERC) Discovery Grant program. The radiative transfer simulations were

all performed with MODTRAN v. 5.4 (http://modtran.spectral.com). The atmospheric

⁴⁸⁵ profiles used are from 48 radiosondes taken from the IGRA database (ftp://ftp.ncdc.noaa.gov/pub/data/igra/).

- ⁴⁸⁶ These simulations and the codes used to generate the figures are available from Laurence
- 487 Coursol.

508

509

488 References

489	Aumann, H. H., Chahine, M. T., Gautier, C., Goldberg, M. D., Kalnay, E.,
490	McMillin, L. M., others (2003). Airs/amsu/hsb on the aqua mission:
491	Design, science objectives, data products, and processing systems. <i>IEEE</i>
492	Transactions on Geoscience and Remote Sensing, 41(2), 253–264.
493	Berk, A., Anderson, G. P., Acharya, P. K., Bernstein, L. S., Muratov, L., Lee, J.,
494	others (2005). Modtran 5: a reformulated atmospheric band model with
495	auxiliary species and practical multiple scattering options: update. In Proc. of
496	<i>spie vol</i> (Vol. 5806, p. 663).
497	Bloom, H. (2001). The cross-track infrared sounder (cris): A sensor for operational
498	meterological remote sensing. In Fourier transform spectroscopy (p. JTuB1).
499	Blumstein, D., Chalon, G., Carlier, T., Buil, C., Hebert, P., Maciaszek, T., oth-
500	ers (2004). Iasi instrument: Technical overview and measured performances. In
501	<i>Proc. of spie vol</i> (Vol. 5543, p. 197).
502	Bormann, N., Collard, A., & Bauer, P. (2010). Estimates of spatial and interchannel
503	observation-error characteristics for current sounder radiances for numerical
504	weather prediction. ii: Application to airs and iasi data. Quarterly Journal of
505	the Royal Meteorological Society, 136(649), 1051–1063.
506	Boullot, N., Rabier, F., Langland, R., Gelaro, R., Cardinali, C., Guidard, V.,
507	Doerenbecher, A. (2016). Observation impact over the southern polar area

510	Buehner, M., McTaggart-Cowan, R., Beaulne, A., Charette, C., Garand, L., Heilli-
511	ette, S., others (2015). Implementation of deterministic weather forecast-
512	ing systems based on ensemble-variational data assimilation at environment
513	canada. part i: The global system. Monthly Weather Review, 143(7), 2532–
514	2559.
515	Chang K-W L'Ecuver T S Kahn B H & Natrai V (2017) Information
515	content of visible and midinfrared radiances for retrieving tropical ice cloud
510	properties Journal of Geophysical Research: Atmospheres 199(0) 4044-4066
517	Clough S A Jacono M I & Monget I I (1002) Jine by line calculations of
518	etmospheria fluxes and cooling rates: Application to water vapor — Lowrad of
519	atmospheric nuxes and cooling rates. Application to water vapor. $Journal of$
520	Diversela M. C. Derrett, C. D. Caldharr, M. D. McMillin, I. M. Madda, F.
521	Welf W. J. Lin, V. (2006) Well detion of stream baris informal soundar toru
522	wolf, w., Liu, A. (2006). Validation of atmospheric infrared sounder tem-
523	perature and water vapor retrievals with matched radiosonde measurements
524	and forecasts. Journal of Geophysical Research: Atmospheres, 111(D9).
525	Durre, I., Vose, R. S., & Wuertz, D. B. (2006). Overview of the integrated global ra-
526	diosonde archive. Journal of Climate, $19(1)$, 53–68.
527	Fourrié, N., & Thépaut, Jn. (2003). Evaluation of the airs near-real-time channel
528	selection for application to numerical weather prediction. Quarterly Journal of
529	the Royal Meteorological Society, 129(592), 2425–2439.
530	Garand, L., Heilliette, S., & Buehner, M. (2007). Interchannel error correlation
531	associated with airs radiance observations: Inference and impact in data assim-
532	ilation. Journal of applied meteorology and climatology, 46(6), 714–725.
533	Garand, L., Turner, D., Larocque, M., Bates, J., Boukabara, S., Brunel, P.,
534	others (2001). Radiance and jacobian intercomparison of radiative transfer
535	models applied to hirs and amsu channels. Journal of Geophysical Research:
536	Atmospheres, 106(D20), 24017–24031.
537	Harries, J., Carli, B., Rizzi, R., Serio, C., Mlynczak, M., Palchetti, L., Masiello,
538	G. (2008). The far-infrared earth. Reviews of Geophysics, $46(4)$.
539	L'Ecuver, T. (2019). The polar radiant energy in the far infrared experiment (pre-
540	fire): A far infrared mission to improve estimates of the polar energy budgets.
541	In Geonhusical research abstracts (Vol 21)
542	Lewis J. M. Lakshmiyarahan S. & Dhall S. (2006) Dunamic data assimilation: a
542	least squares approach (Vol 13) Cambridge University Press
545	Libois O. Prouly C. Ivanoscu I. Coursel I. Polletior I. S. Bouzid V.
544	Blanchot I P (2016) A microholometer based far infrared radiometer to
545	study thin ice clouds in the artic
546	Study thin ice clouds in the arctic. Atmospheric measurement rechniques, $O(\Lambda)$ 1917
547	$\mathcal{P}(4)$, 1017.
548	Lupu, C., Gautiner, P., & Laroche, S. (2011). Evaluation of the impact of obser-
549	Warthen Devices (190/2), 726–727
550	Weather Review, $139(3)$, $120-131$.
551	McNally, A., Watts, P., A Smith, J., Engelen, R., Kelly, G., Thepaut, J., & Matri-
552	cardi, M. (2006). The assimilation of airs radiance data at ecmwi. Quarterly
553	Journal of the Royal Meteorological Society, 132(616), 935–957.
554	Merrelli, A., & Turner, D. D. (2012). Comparing information content of upwelling
555	tar-intrared and midintrared radiance spectra for clear atmosphere profiling.
556	Journal of Atmospheric and Oceanic Technology, $29(4)$, $510-526$.
557	Mertens, C. J. (2002). Feasibility of retrieving upper tropospheric water vapor from
558	observations of far-infrared radiation. In Optical spectroscopic techniques, re-
559	mote sensing, and instrumentation for atmospheric and space research iv (Vol.
560	4485, pp. 191–201).
561	Mlynczak, M., Johnson, D. G., & Kratz, D. P. (2007). The far-infrared spectrum:
562	Exploring a new frontier in the remote sensing of the earth's climate. In Hy-
563	perspectral imaging and sounding of the environment (p. HMA1).

perspectral imaging and sounding of the environment (p. HMA1).
 Mlynczak, M. G., Harries, J. E., Rizzi, R., Stackhouse, P. W., Kratz, D. P., John-

565	son, D. G., Soden, B. J. (2002). Far-infrared: a frontier in remote sensing
566	of earth's climate and energy balance. In International symposium on optical
567	science and technology (pp. 150–158).
568	Mlynczak, M. G., Johnson, D. G., Latvakoski, H., Jucks, K., Watson, M., Kratz,
569	D. P., others (2006). First light from the far-infrared spectroscopy of the
570	troposphere (first) instrument. Geophysical research letters, 33(7).
571	Müller, R., Kunz, A., Hurst, D. F., Rolf, C., Krämer, M., & Riese, M. (2016). The
572	need for accurate long-term measurements of water vapor in the upper tro-
573	posphere and lower stratosphere with global coverage. Earth's Future, $4(2)$,
574	25-32.
575	Palchetti, L., Olivieri, M., Pompei, C., Labate, D., Brindley, H., Di Natale, G., &
576	Bianchini, G. (2016). The far infrared fts for the forum mission. In <i>Fourier</i>
577	transform spectroscopy (pp. FTu3C–1).
578	Proulx, C., Williamson, F., Allard, M., Baldenberger, G., Gay, D., Garcia-Blanco,
579	S., others (2009). The earthcare broadband radiometer detectors. In Proc.
580	<i>spie</i> (Vol. 7453, p. 74530S).
581	Purser, R., & Huang, H. (1993). Estimating effective data density in a satellite re-
582	trieval or an objective analysis. Journal of applied meteorology, $32(6)$, 1092–
583	1107.
584	Rabier, F., Fourrié, N., Chafäi, D., & Prunet, P. (2002). Channel selection methods
585	for infrared atmospheric sounding interferometer radiances. Quarterly Journal
586	of the Royal Meteorological Society, 128(581), 1011–1027.
587	Rizzi, R., Serio, C., & Amorati, R. (2002). Sensitivity of broadband and spec-
588	tral measurements of outgoing radiance to changes in water vapor content.
589	In Optical spectroscopic techniques, remote sensing, and instrumentation for
590	atmospheric and space research iv (Vol. 4485, pp. 181–190).
591	Rodgers, C. D. (2000). Inverse methods for atmospheric sounding: theory and prac-
592	tice (Vol. 2). World scientific.
593	Serreze, M. C., Barrett, A. P., & Stroeve, J. (2012). Recent changes in tropospheric
594	water vapor over the arctic as assessed from radiosondes and atmospheric
595	reanalyses. Journal of Geophysical Research: Atmospheres, 117(D10).
596	Shahabadi, M. B., & Huang, Y. (2014). Measuring stratospheric h20 with an air-
597	borne spectrometer. Journal of Atmospheric and Oceanic Technology, 31(7),
598	1502–1515.
599	Shahabadi, M. B., Huang, Y., & Moreau, L. M. (2015). Measuring stratospheric h
600	2 o with an airborne spectrometer: Simulation with realistic detector charac-
601	teristics. IEEE Journal of Selected Topics in Applied Earth Observations and
602	Remote Sensing, $\mathcal{S}(7)$, $3541-3545$.
603	Susskind, J., Barnet, C. D., & Blaisdell, J. M. (2003). Retrieval of atmospheric and
604	surface parameters from airs/amsu/hsb data in the presence of clouds. $IEEE$
605	Transactions on Geoscience and Remote Sensing, 41(2), 390–409.
606	Wark, D., & Hilleary, D. (1969). Atmospheric temperature: Successful test of remote
607	probing. Science, $105(3899)$, $1250-1258$.
608	Wielicki, B. A., Young, D., Mlynczak, M., Thome, K., Leroy, S., Corliss, J., oth-
609	ers (2013). Achieving climate change absolute accuracy in orbit. Bulletin of the American Meteorological Society $O(10)$, 1510, 1520.
610	Une American Meleorological Society, 94 (10), 1519–1539.
611	Arong, A., weiniy, D. N., wu, A., Darnes, W. L., & Salomonson, V. V. (2008).
612	Aqua mouls thermal emissive band off-orbit calibration, characterization, and performance $IFFF$ Transactions on Consisting and Demote Service $I^{(2)}$
613	performance. IEEE transactions on Geoscience and Remote Sensing, $47(3)$, $903, 914$
614	003-014.