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A thin shell of ionized gas as the explanation for infrared excess among classical Cepheids

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ABSTRACT

Context. The infrared (IR) excess of classical Cepheids is seldom studied and poorly understood despite observational evidence and the potential for its contribution to induce systematics on the period-luminosity (PL) relation used in the calibration of the extragalactic distance scale.

Aims. This study aims to understand the physical origin of the IR excess found in the spectral energy distribution (SED) of 5 Cepheids: RS Pup (P = 41.46d), ζ Gem (P = 10.15d), η Aql (P = 7.18d), V Cen (P = 5.49d) and SU Cyg (P = 3.85d).

Methods. A time series of atmospheric models along the pulsation cycle were fitted to a compilation of data, including optical and near-IR photometry, *Spitzer* spectra (secured at a specific phase), interferometric angular diameters, effective temperature estimates, and radial velocity measurements. *Herschel* images in two bands were also analyzed qualitatively. In this fitting process, based on the SPIPS algorithm, a residual was found in the SED, whatever the pulsation phase, and for wavelengths larger than about $1.2 \,\mu$ m, which corresponds to the so-determined infrared excess of Cepheids. This IR excess was then corrected from interstellar medium absorption in order to infer the presence (or absence) of dust shells and was, ultimately, used in order to fit a model for a shell of ionized gas.

Results. For all Cepheids, we find a continuum IR excess increasing up to approximately -0.1 magnitudes at $30 \mu m$, which cannot be explained by a hot or cold dust model of CircumStellar Environment (CSE). However, a weak but significant dust emission at $9.7 \mu m$ is found for ζ Gem, η Aql and RS Pup, while clear interstellar clouds are seen in the *Herschel* images for V Cen and RS Pup. We show, for the first time, that the IR excess of Cepheids can be explained by free–free emission from a thin shell of ionized gas, with a thickness of $\approx 15\%$ of the star radius, a mass of $10^{-9} - 10^{-7} M_{\odot}$ and a temperature ranging between 3500 and 4500 K.

Conclusions. The presence of a thin shell of ionized gas around Cepheids must be tested with interferometers operating in the visible or mid-IR, or using radio telescopes. The impact of such CSEs of ionized gas on the PL relation of Cepheids also calls for further investigation.

Key words. stars: variables: Cepheids - circumstellar matter - stars: atmospheres

1. Introduction

Cepheids have been the keystone of distance scale determination in the Universe for a century because of the direct correlation between their pulsation period and their luminosity as per the Leavitt law (Leavitt 1908; Leavitt & Pickering 1912), also referred to as the period-luminosity relation (hereafter PL relation).

The recent determination of one percent precision for the Large Magellanic Cloud distance (Pietrzyński et al. 2019) has led to a new value for the Hubble constant H_0 (Riess et al. 2019). Moreover, upcoming space and ground-based telescopes such as the *James Webb* Space Telescope (JWST) and the Extremely Large Telescope (ELT) will make it possible to obtain light curves of extragalactic Cepheids up to one hundred megaparsecs. However, this distance ladder is still largely based on a PL

relation for Cepheids whose uncertainties on both zero point and slope today stand as one of the largest contributors to the error on H₀ (Riess et al. 2019). One possible bias could be due to IR excesses from CSEs, such as those discovered using near- and mid-infrared interferometry around nearby Cepheids (Kervella et al. 2006; Mérand et al. 2006). Indeed, if the brightness of CSEs is found to be significantly different in the Milky Way, SMC, LMC, as well as in galaxies hosting SNIa due to metallicity effects, for instance, then the use of an universal PL relation could introduce a bias in the distance scale calibration.

Envelopes around Cepheids have been discovered by longbaseline interferometry in the *K*-Band with VLTI and CHARA (Kervella et al. 2006; Mérand et al. 2006), and four Cepheids CSEs have been observed in the *N* band with VISIR and MIDI (Kervella et al. 2009; Gallenne et al. 2013), as well as one with NACO in the near-IR (Gallenne et al. 2011). The presence of a motionless H α absorption component using high-resolution spectroscopy around l Car (Nardetto et al. 2008) has also been attributed to a CSE, and, recently, a CSE was detected in the visible domain with the VEGA/CHARA facility around δ Cep (Nardetto et al. 2016). These various studies determine a CSE radius of around 3 stellar radii and a flux contribution in the *K* band, ranging from 2 to 10% of the continuum, for mediumand long-period Cepheids respectively, while it is around 10% or more in the *N* band. However, we still do not know how these CSEs are produced, nor do we understand their nature or their characteristics (density and temperature profiles, chemical composition...).

This paper is aimed at building a phase-dependent spectral energy distribution (SED) of a sample of Cepheids from visible to mid-IR wavelengths and comparing it with dedicated atmospheric models in order to quantify and study their IR excess. We present the IR excess of the stars in the sample in Sect. 2 using photometric and Spitzer observations in various bands, and we study qualitatively far-infrared images from Herschel. In Sect. 3 we correct the spectra from interstellar foreground absorption along the line-of-sight and seek residuals at 9.7 μ m that could be attributed to a dusty CSE. In Sect. 4, we use the radiative transfer code DUSTY (Ivezic et al. 1999) to model the IR excess continuum and to show that such continuum cannot be attributed to a dusty CSE. In Sect. 5, we propose, instead, a model of CSE composed of ionized gas in order to reproduce the observed IR excess. Our results are discussed in Sect. 6 and we present our conclusions in Sect. 7.

2. Observations and data reduction of RS Pup, ζ Gem, η Aql, V Cen, and SU Cyg

2.1. Star sample

In order to study the IR excess of Cepheids we selected a sample of Galactic Cepheids with *Spitzer* observations. The combination of its sensitivity and wide IR wavelength coverage, from 5 to $38 \,\mu$ m, makes it the best tool for studying dust features and IR excess continuum emission. We selected the five Cepheids with *Spitzer* low resolution spectra and the highest signal-to-noise ratio: RS Pup (P = 41.46d); ζ Gem (P = 10.15d); η Aql (P = 7.18d); V Cen (P = 5.49d); and SU Cyg (P = 3.85d). In addition, we retrieved *Herschel* data at 70 and 160 μ m to study larger cold environments of dust. These space-based observations have the advantage of avoiding biases caused by the Earth atmosphere, meaning the entire flux is preserved and not hidden by the ozone band, which is essential for the study of dust spectral features.

2.2. Building the infrared excess using the SPIPS algorithm

SpectroPhoto-Interferometric modeling of Pulsating Stars (SPIPS) is a model-based parallax-of-pulsation code which includes photometric, interferometric, effective temperature and radial velocity measurements in a robust model fit (Mérand et al. 2015). In order to compute synthetic photometry to match what is drawn from the dataset, SPIPS uses a grid of ATLAS9 atmospheric models¹ (Castelli & Kurucz 2003) with solar metallicity and a standard turbulent velocity of 2 km s⁻¹.

SPIPS models are available for η Aql (Mérand et al. 2015), ζ Gem (Breitfelder et al. 2016) and RS Pup (Kervella et al. 2017). We updated them with new datasets, including *Gaia* photometry (Gaia Collaboration 2018), and we also applied the SPIPS algorithm to SU Cyg and V Cen. Figures A.1–A.5 show the results of the fitting process. For each star in the sample, SPIPS provides a fit of the photometry along the pulsation cycle, which is in agreement with the observational data. While the fit is satisfactory from the visible domain to the near infrared, a disagreement results for wavelengths larger than about $1.2 \,\mu$ m. For $\lambda > 1.2 \,\mu$ m, while the observed photometries (m_{obs}) are indeed significantly brighter than the synthetic ones (m_{kurucz}), which corresponds to an infrared excess. SPIPS does not physically model this IR excess, but instead takes it into account using an ad hoc analytic power law IR_{ex}, which is defined as:

$$IR_{ex} = \Delta mag = m_{obs} - m_{kurucz} = \begin{cases} 0, & \text{for } \lambda < 1.2 \,\mu\text{m} \\ \alpha(\lambda - 1.2)^{\beta}, & \text{for } \lambda \ge 1.2 \,\mu\text{m} \end{cases}$$
(1)

with two parameters, α and β . These ad hoc laws take the visible domain as a reference, and thus assume that there is no excess nor deficit in this wavelength domain due to the CSE ($\Delta \mathbf{m} = 0$ for $\lambda < 1.2 \,\mu$ m). The choice of the ad hoc analytic power law in Eq. (1) was adopted originally in SPIPS modeling because it provides a reasonable description of the IR excess without impacting the results of the fit.

In Fig. 1, we show the IR excess analytic law obtained for the star sample together with the measurements. These measurements correspond to the cycle-averaged magnitude difference $\Delta \text{mag} = m_{\text{obs}} - m_{\text{kurucz}}$ (in a specific band), while the uncertainties are the corresponding standard deviations. Since these deviations over the cycle are quite small ($\approx 0.05 \text{ mag}$) from Fig. 1, we conclude that the IR excess of Cepheids is not time-dependent or only time-dependent in the slightest.

In the fitting process described above, the photometric band corresponding to the carbon-monoxyde (CO) band-head at 4.6 μ m has to be considered with a special care. Indeed, CO can form at low temperature (Scowcroft et al. 2016) and this is, indeed, probably what is seen in IRAC I2 *Spitzer* bands for ζ Gem and V Cen (see Figs. A.1 and A.2, respectively). In these bands, the relation between the ATLAS9 model and the observations is in disagreement at certain phases. Even if ATLAS9 includes the modeling of CO molecules, these models are static and do not reproduce the dynamic structure of the atmosphere of Cepheids satisfactorily. However, the cycle-averaged infrared excess we obtain at this specific wavelength of 4.6 μ m is consistent with the general trend of the IR excess law (see Fig. 1), and is considered in the following part of the analysis.

In addition, the photometric bands longward of 5 μ m are problematic for two reasons. First, their cycle coverage is poor, meaning there is only one data point in each band with an undetermined phase, as is the case for η Aql, ζ Gem and RS Pup at $\lambda > 5 \mu$ m (see, for instance, the A MSX band of RS Pup in Fig. A.3). Hence, the reliability of the fitted ad hoc IR excess model depending on pulsation phase is questionable. Secondly these bands are more sensitive to interstellar dust emission around the star than *Spitzer* because of their lower spatial resolution. Thus we have decided to discard these photometric bands from the analysis. The measurements which have not been considered are indicated by orange bars in Fig. 1.

2.3. Spitzer data

The spectroscopic observations were made with the InfraRed Spectrograph (IRS; Houck et al. 2004) on board the *Spitzer* telescope (Werner et al. 2004) and the full spectra were retrieved

http://www.ser.oats.inaf.it/castelli/grids.html

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(a) RS Pup, IR_{ex} = $-0.061(\lambda - 1.2)^{0.350}$ mag



Fig. 1. IR excess analytic law for all star sample together with measurements. IR excess as derived from the SPIPS algorithm and represented by ad hoc analytic laws (Eq. (1)) for each star in the sample. For each photometric band, red dots with error bars are the mean excess value over the cycle of the Cepheid and the corresponding standard deviation. Red point with orange bars are photometric band discarded in this work (see Sect. 2.2). The green zone is the error on the magnitude obtained using the covariance matrix of SPIPS fitting result.

from the CASSIS atlas (Lebouteiller et al. 2011). CASSIS identified the five stars as point-like sources, therefore we retrieved the best flux calibrated spectrum obtained from the optimal extraction method (Lebouteiller et al. 2010). The *Spitzer* dataset of this paper is presented in Table 1. Short-Low (SL) and Long-Low (LL) are IRS modules placed in the focal plane instrument providing low spectroscopic resolution (R = 60-128) from

5.2 to 38 μ m. In this study, we use low-resolution IRS spectra obtained with the SL and LL modules, for which aperture sizes, together with covered spectral ranges, are described in Table 2.

We derive the IR excess of each star in the sample at the specific phase of *Spitzer* using:

$$\Delta mag = m_{Spitzer} - m_{kurucz} [\phi_{Spitzer}]$$
⁽²⁾

Table 1. Spitzer data set.

AORs	Date	MJD	ϕ
26 021 120	2009.05.04	54 955.160	0.938
27 579 392	2008.11.11	54 781.833	0.410
27 579 136	2008.06.07	54 624.819	0.408
27 566 336	2008.10.01	54 740.445	0.960
27 592 960	2008.11.06	54 776.575	0.013
	AORs 26 021 120 27 579 392 27 579 136 27 566 336 27 592 960	AORsDate26 021 1202009.05.0427 579 3922008.11.1127 579 1362008.06.0727 566 3362008.10.0127 592 9602008.11.06	AORsDateMJD26 021 1202009.05.0454 955.16027 579 3922008.11.1154 781.83327 579 1362008.06.0754 624.81927 566 3362008.10.0154 740.44527 592 9602008.11.0654 776.575

Notes. The table lists: astronomical observation requests (AORs) used in this paper, date of observation, corresponding Modified Julian Date (MJD), and pulsation phase (ϕ). RS Pup is from observation program number 50 346 and others stars are from program number 485 (Ardila et al. 2010).

 Table 2.
 Properties of the Spitzer/IRS AORs Short-Low (SL) and Long-Low (LL) modules used.

Module	Aperture size (")	Orders	$\lambda_{\min} - \lambda_{\max}$
SL	3.7×57	1	7.4–14.5
		2	5.2-7.7
LL	10.7×168	1	19.5-38.0
		2	14.0-21.3

 Table 3. Physical parameters of stars derived by SPIPS at Spitzer observation phase.

	$T_{\rm eff}(\phi_{Spitzer})$	$\log g(\phi_{Spitzer})$	$\theta(\phi_{Spitzer})$
RS Pup	5860^{+15}_{-15}	$1.03^{+0.10}_{-0.10}$	$0.792^{+0.002}_{-0.002}$
ζ Gem	5178^{+7}_{-7}	$1.52^{+0.15}_{-0.15}$	$1.699^{+0.002}_{-0.002}$
η Aql	5543^{+6}_{-6}	$1.68^{+0.17}_{-0.17}$	$1.784^{+0.002}_{-0.002}$
V Cen	6368^{+15}_{-15}	$1.89^{+0.19}_{-0.19}$	$0.510\substack{+0.001\\-0.001}$
SU Cyg	6781^{+17}_{-17}	$2.03^{+0.20}_{-0.20}$	$0.353^{+0.001}_{-0.001}$

Notes. $T_{\rm eff}$ and log g are used to interpolate a ATLAS9 atmosphere model. The limb-darkened angular diameter θ is then used to derived the observed flux. Temperature and angular diameter are in Kelvin and milliarcsecond respectively. Uncertainties on $T_{\rm eff}$ and θ are provided by SPIPS, whereas uncertainty on log g is arbitrarily set to 10%.

where $m_{Spitzer}$ is the magnitude of the Spitzer observation and $m_{\text{kurucz}}[\phi_{\text{Spitzer}}]$ is the magnitude of the ATLAS9 atmospheric model interpolated at the phase of *Spitzer* observations ($\phi_{Spitzer}$). The $T_{\rm eff}$ and log q values of the star at the phase of *Spitzer* are provided by the SPIPS algorithm, while the interpolation is then done in a ATLAS9 grid of models with steps of 250K in effective temperature and 0.5 in log g, respectively. The angular diameter derived by SPIPS is then used to calculate $m_{kurucz}[\phi_{Spitzer}]$. The corresponding stellar parameters are summarized in Table 3 and the Δ mag values we ultimately obtain are indicated by green dots and red uncertainties in Fig. 2. The same method is applied to all the photometric bands of observations, meaning that we do not use the average IR excess values shown in Fig. 1, but instead we recalculate the actual values corresponding to the phase of Spitzer observations (red dot with blue uncertainties in Fig. 2). Please note that in Fig. 2, the cycle averaged ad hoc analytic IR excess law is shown only for comparison.

First, we correct several discontinuities in the *Spitzer* spectra. Even if absolute uncertainties (Lebouteiller et al. 2011; Sloan et al. 2015) are not excluded, we find a discontinuity at $14 \mu m$ between SL and LL spectra, indicated by a dashed line in Fig. 2. According to CASSIS atlas, a residual offset appears in the case of slightly extended sources (Lebouteiller et al. 2011) because more flux enters the larger LL aperture. Indeed the two *Spitzer* detectors have indeed different fields of view (FOV, see Table 2) with different orientations on the sky (see Fig. 3), which explains the different level of flux measured. As an indication, the FOV of both detectors are overlaid on *Herschel* images (see Fig. 3 in Sect. 2.4).

For RS Pup, we obtain a jump of 7% in flux between the SL and LL detectors, while for other stars we find a difference of around 2% (1.3% in the case of ζ Gem). Extended dust emission has been discovered around RS Pup (Westerlund 1961; McAlary & Welch 1986) so this jump is not surprising.

We correct these discontinuities at $14 \mu m$ in the spectra by scaling up SL flux (with the latter flux ratio) so that it corresponds to LL flux at $14 \mu m$. This correction assumes that the LL flux calibrated by the CASSIS pipeline is reliable and the emission of the environment is homogeneous between SL and LL apertures.

In addition, order mismatches may appear because of telescope pointing accuracy and ensuing discontinuity in the spectra between 2 adjacent orders. We corrected this feature in SU Cyg and ζ Gem spectra at 7.5 μ m between SL orders 1 and 2 by scaling up the lower part. We also note that the *Spitzer* data at larger wavelengths than 30 μ m were not considered due to their extremely large scopes of uncertainties.

Second, for the five stars in the sample, we find an agreement between the level of IR excess at $5\,\mu$ m in all photometric bands ($\lambda < 5\,\mu$ m) and in the *Spitzer* spectroscopic observation ($\lambda > 5\,\mu$ m). This is verified at the 0.05 magnitude level, prior to the correction of different *Spitzer* discontinuities (see Fig. 6 for a detailled analysis of corrected IR excess). The agreement between IR excesses from SPIPS models and *Spitzer* data demonstrates the consistency of this approach. It reveals that Cepheids exhibit a continuum IR excess from about $2\,\mu$ m up to $30\,\mu$ m in the star sample. This result is different from that obtained by Schmidt (2015), where no IR excess was found for short-period classical Cepheids (see Sect. 6.1). We, however, find that the ad hoc analytic laws of SPIPS overestimate the IR excess in the *Spitzer* wavelength domain (see Fig. 2).

Third, RS Pup, SU Cyg and V Cen present unambiguous silicate absorption bands at 9.7 and $20 \,\mu$ m. The latter absorption is known to usually peak at $18 \,\mu$ m, however it can be shifted to a longer wavelength depending on various conditions, such as temperature or mineral proportions indicated by silicates (Koike et al. 2006; Henning & Mutschke 1997). These silicate absorptions are likely due to the presence of interstellar clouds in the line of sight.

2.4. Herschel images

We retrieved *Herschel* images from the PACS instrument at 70 and $160\,\mu\text{m}$ to study the presence of extended environment around Cepheids. No data have been found for SU Cyg. *Herschel* observation products are ordered according to the level of the data processing, ranging from raw data (level 0) to highly processed scientific data (level 3). All the images in the sample are highly processed data with a level of 2.5. The FOV of *Herschel* is of 8' and its spatial resolution is of 7" at $100\,\mu\text{m}$. As an indication, we performed aperture photometry measurements of

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Fig. 2. Photometric observations interpolated at specific phases of *Spitzer* data using SPIPS algorithm. Transition between SL and LL detectors is indicated by a dashed line at $\approx 14 \,\mu$ m. The cycle-averaged ad hoc analytic laws from SPIPS are represented by a dashed green for comparison only. Pulsation phase ϕ of the *Spitzer* observations is indicated in the caption of each panel.

the flux within 1' in order to include most of the emission that is due to the environment of the Cepheids. Then we derived the IR excess at 70 and $160\,\mu\text{m}$ through comparisons with the atmospheric model in the same way as in Eq. (2).

Observations are presented in Fig. 3 and the derived photometry in Table 4. From these data we observe important IR excesses at 70 and 160 μ m, which are associated with cold environments of temperatures of about 40 and 20 K, respectively, according to Wien's displacement law ($\lambda T = 2900 \,\mu$ mK). Cold dust material around RS Pup was already observed, while the large cloud observed around V Cen (see Fig. 3d) at 160 μ m could be related to a star forming region since V Cen is likely a member of the open cluster NGC 5662 (Turner 1982; Claria et al. 1991; Anderson et al. 2013). *Herschel* is sensitive not only to emission from the star itself and a potential CSE, but also to that of cold extended emission from the interstellar medium.



(a) RS Pup



(b) ζ Gem



(c) η Aql



(d) V Cen

Fig. 3. Herschel images of Cepheids and overlaid Spitzer FOV. Left and right panels correspond to 70 and $160 \,\mu$ m, respectively. The FOV is 8' large. Short and long green rectangles are SL and LL modules in the Spitzer focal plane detector respectively.

Table 4. Herschel data set.

	RS Pup	ζ Gem	η Aql	V Cen
$F_{70}(Jy)$	$11.5^{+3.4}_{-3.4}$	$0.7^{+0.8}_{-0.8}$	$0.7^{+0.8}_{-0.8}$	$0.9^{+0.9}_{-0.9}$
$F_{160}(Jy)$	$6.7^{+2.6}_{-2.6}$	$0.4^{+0.6}_{-0.6}$	$0.4^{+0.6}_{-0.6}$	$5.2^{+2.3}_{-2.3}$
Δmag_{70}	$-6.5^{+0.3}_{-0.3}$	$-1.9^{+1.2}_{-1.2}$	$-1.7^{+1.2}_{-1.2}$	$-4.6^{+1.1}_{-1.1}$
Δmag_{160}	$-7.7^{+0.4}_{-0.4}$	$-3.1^{+1.6}_{-1.6}$	$-2.9^{+1.6}_{-1.6}$	$-8.3^{+0.5}_{-0.5}$

Notes. F_{70} and F_{160} are the flux in Jansky at 70 and $160 \,\mu\text{m}$, respectively integrated within a 1' circle centered on the star. Δmag_{70} and Δmag_{160} are the corresponding IR excess derived following the definition of Eq. (2) but for *Herschel* observations.

Thus, we do not consider the *Herschel* photometry in the rest of this paper.

Interestingly, we find a qualitative correlation between silicate absorption features in *Spitzer* data and the presence of extended emission in the *Herschel* images. For instance, both RS Pup and V Cen show strong silicate absorptions and extended emission in the *Herschel* data at the same time (see Figs. 3a and d), while η Aql and ζ Gem present no obvious silicate absorption and weaker interstellar environment (Figs. 3b and c).

3. Correcting the interstellar silicate absorption in Spitzer data

Absorption of silicates at 9.7 μ m is easily identified in the *Spitzer* spectra of RS Pup, V Cen and SU Cyg, whereas it is not observed in η Aql and ζ Gem data (see Fig. 2). Such a level of absorption has, in principle, two components: an emission due to a CSE close to the star (if present) which is then absorbed by interstellar environment. Thus, the silicate absorption observed by *Spitzer* $A_{9.7}^{Spitzer}$, if it is corrected from the expected silicate absorption from the ISM ($A_{9.7}^{ISM}$), can indicate, in case of residual emission, whether there is a silicate emission from the CSE $E_{9.7}^{CSE}$ or not. Thus, we come to the following relation:

$$A_{9,7}^{Spitzer} - A_{9,7}^{\rm ISM} = E_{9,7}^{\rm CSE}$$
(3)

All values are presented at magnitudes of $9.7 \,\mu\text{m}$. We then determine $A_{9.7}^{Spitzer}$ (Sect. 3.1) and $A_{9.7}^{ISM}$ (Sect. 3.2) in order to estimate the CSE emission at $9.7 \,\mu\text{m}$ (Sect. 3.3) and we extend our correction to the whole wavelength range of *Spitzer* (Sect. 3.4).

3.1. Quantifying the observed silicate absorption from Spitzer

In order to estimate the apparent silicate absorption at $9.7 \,\mu m$ $(A_{9.7}^{Spitzer})$, we have to define the IR excess continuum. For that, we fit the IR excess continuum on each side of the absorption feature over the wavelength range $[6,7] \cup [12,13]$ (dashed line in Fig. 4), and we interpolate the excess continuum value at $9.7 \,\mu m$ (blue dot in Fig. 4). We then subtract the IR excess corresponding to the core of the silicate absorption at $9.7 \,\mu m$ (red dot). The uncertainty on $A_{9.7}^{Spitzer}$ is derived by adding in quadrature both the error on the continuum and the error on the *Spitzer* observation at $9.7 \,\mu m$. For ζ Gem we do not find any evidence for absorption.



Fig. 4. Silicate absorption features from *Spitzer* spectra. The black dashed line represents the continuum. Blue and red points are the continuum and *Spitzer* excesses at 9.7 μ m respectively. For ζ Gem no evidence of silicate absorption was found, thus for this star $A_{9.7}^{Spitzer}$ is set to 0.000 ± 0.002.

3.2. Estimation of the interstellar medium (ISM) silicate absorption

The ISM extinction theory can be used to estimate the silicate absorption directly from the color excess E(B-V). In order to select the most reliable E(B-V) values, we compared for each star: (1) the E(B-V) fitted by the SPIPS algorithm; (2) the E(B-V) from the David Dunlap Observatory Database of Galactic Classical Cepheids² (hereafter DDOD; Fernie et al. 1995) which computes the mean extinction and standard error from various values obtained in the literature; (3) the E(B-V)obtained with the Stilism 3D map (Capitanio et al. 2017) using the Bayesian inversion method to a wide color excess dataset and parallaxes; and (4) the 2D map from Schlegel et al. (1998) (hereafter SFD98) using 100 µm data from COBE/DIRBE and IRAS. In the latter 2D map we have corrected the extinction by taking into account the star's location using a three-dimensional model of the Milky Way from Drimmel & Spergel (2001). We present these E(B-V) values in Table 5. The best agreement is obtained when comparing SPIPS and DDOD values, which are based on two enitrely independent methods, which reinforces the reliability of the SPIPS fitting. For the Stilism and SFD98 2D maps, the E(B-V) values are based on models of dust distribution within the Milky Way and, thus, they cannot be applied to local over- or under-densities in the vicinity of the Cepheids, which probably explains the large discrepancies found in particular for RS Pup, SU Cyg, and also V Cen. For these stars, the uncertainty on E(B-V) is also particularly large in the case of Stilism. The E(B-V) values provided by SPIPS are the most precise by an order of magnitude, but uncertainties are underestimated (Mérand et al. 2015). Therefore, we decided to adopt an independent and more conservative approach using the DDOD values.

As a second step, we derive the visible absorption A_{y} assuming an extinction law of $A_v = R_v E(B-V)$ with a ratio of total-toselective extinction of $R_v = 3.1$, which corresponds to a diffuse ISM along the line of sight (Savage & Mathis 1979). Then we used the relation $A_v/\tau_{9.7} = 18.5$ (Roche & Aitken 1984) which is suited to diffuse ISM in the solar vicinity, in order to derive $\tau_{9.7}$. This was done for each star except RS Pup. Indeed, RS Pup is known for being embedded in a large environment which is most probably the remnant of the molecular clouds in which the star formed (Kervella et al. 2009, 2012). Hence we treated RS Pup as a special case since the extinction towards dense clouds is different from diffuse ISM (Whittet et al. 1988; Indebetouw et al. 2005; Flaherty et al. 2007; Chiar et al. 2007; van Breemen et al. 2011). We assumed most of the extinction is due to a dense cloud and we used $R_v = 5$ and $A_v/\tau_{9.7} = 11.46$ following the empirical work in star-forming regions by McClure (2009). Finally, the extinction A_{λ} is given by the intensity absorption along the line of sight considering an optical depth τ_{λ} . Combining both the Beer-Lambert law and absorption definitions for any wavelength λ we have $A_{\lambda} = 1.086\tau_{\lambda}$, thus $A_{9.7} = 1.086\tau_{9.7}$ at the specific wavelength 9.7 μ m.

This approach can ultimately be summarized on the basis of two equations, referring to stars in diffuse ISM Eq. (4) and for RS Pup Eq. (5):

$$A_{9.7}^{\text{ISM}} = 1.086 \frac{3.1}{18.5} = 0.182 E(B-V),$$
 (4)

$$A_{9.7}^{\text{ISM}} = 1.086 \frac{5}{11.46} = 0.474 \, E(B-V),$$
 (5)

² http://www.astro.utoronto.ca/DD0/research/cepheids/

able 5.	Comparison of $E(B-V)$ values of stars in sample considering different approaches.

	SPIPS (a)	DDOD ^(b)	<i>(n)</i>	Stilism 3D map	SFD98 2D map (c)
RS Pup	$0.550^{+0.005}_{-0.005}$	$0.480^{+0.011}_{-0.011}$	(9)	$0.217^{+0.447}_{-0.207}$	$0.260^{+0.038}_{-0.038}$
ζ Gem	$0.021^{+0.003}_{-0.003}$	$0.044^{+0.020}_{-0.020}$	(6)	$0.013^{+0.024}_{-0.024}$	$0.034^{+0.002}_{-0.002}$
η Aql	$0.149\substack{+0.002\\-0.002}$	$0.152\substack{+0.012\\-0.012}$	(12)	$0.155\substack{+0.050\\-0.050}$	$0.065\substack{+0.008\\-0.008}$
V Cen ^(d)	$0.298^{+0.004}_{-0.004}$	$0.282^{+0.017}_{-0.017}$	(8)	$0.283^{+0.480}_{-0.480}$	$0.220^{+0.024}_{-0.024}$
SU Cyg	$0.109\substack{+0.002\\-0.002}$	$0.133^{+0.031}_{-0.031}$	(6)	$0.257^{+0.113}_{-0.113}$	$0.350\substack{+0.050\\-0.050}$

Notes. ^(a)E(B-V) values are calculated from the SPIPS algorithm. ^(b)David Dunlap Observatory Database. Standard error is the deviation of the number (*n*) of measurements present in the literature. ^(c)Values were corrected by taking into account the star location using three-dimensional model for the Milky Way. ^(d)Extinction values are in agreement with extinction of others members of the open cluster NGC 5662 giving in average $E(B-V) = 0.31 \pm 0.04$ (Claria et al. 1991).

Table 6. Result of residual silicate CSE emission at $9.7 \,\mu$ m.

	DDOD ^(a)	Sect. 3.2	Observation ^(b)	Result ^(c)
	E(B-V)	$A_{9.7}^{\mathrm{ISM}}$	$A_{9.7}^{Spitzer}$	$E_{9.7}^{\mathrm{CSE}}$
RS Pup	$0.480^{+0.011}_{-0.011}$	$0.227^{+0.005}_{-0.005}$	$0.117^{+0.057}_{-0.057}$	$-0.110^{+0.057}_{-0.057}$
ζ Gem	$0.044^{+0.020}_{-0.020}$	$0.008\substack{+0.004\\-0.004}$	$0.000\substack{+0.002\\-0.002}$	$-0.008^{+0.004}_{-0.004}$
η Aql	$0.152\substack{+0.012\\-0.012}$	$0.028\substack{+0.002\\-0.002}$	$0.009^{+0.003}_{-0.003}$	$-0.019^{+0.004}_{-0.004}$
V Cen ^(d)	$0.282^{+0.017}_{-0.017}$	$0.051\substack{+0.003\\-0.003}$	$0.043^{+0.010}_{-0.010}$	$-0.008^{+0.010}_{-0.010}$
SU Cyg	$0.133\substack{+0.031\\-0.031}$	$0.024^{+0.005}_{-0.005}$	$0.028^{+0.025}_{-0.025}$	$0.004^{+0.025}_{-0.025}$

Notes. The silicate absorption due to interstellar extinction $A_{9,7}^{\text{ISM}}$ is calculated (using Eq. (4)) based on reddenings from DDOD. Observed absorption of silicate from *Spitzer* $A_{9,7}^{Spitzer}$ is used together with Eq. (3) in order to derive $E_{9,7}^{\text{CSE}}$, the silicate emission due to a CSE. ^(a)David Dunlap Observatory Database. Standard error is the deviation of the measurement. ^(b)Errors correspond to *Spitzer* uncertainties (see error bars in Fig. 4) ^(c)Errors are given by summing quadratically the precedent absorption uncertainties. ^(d)If Eq. (5) for V Cen is considered we obtain $A_{9,7}^{\text{ISM}} = 0.134_{-0.008}^{+0.008}$ and $E_{9,7}^{\text{CSE}} = -0.091_{-0.013}^{+0.013}$ (see Fig. 5).

The final values of $A_{9,7}^{\text{ISM}}$ we have considered are listed in Table 6, along with their corresponding uncertainties.

3.3. Residual silicate CSE emission at 9.7 μ m

Using values of $A_{9,7}^{Spitzer}$ (Sect. 3.1) and $A_{9,7}^{ISM}$ (Sect. 3.2), we now calculate $E_{9,7}^{CSE}$ using Eq. (3). The results are illustrated in Fig. 5. Using this method, silicate emission from CSE exists only when $E_{9,7}^{CSE} < 0$. We find no residual CSE emission for SU Cyg and V Cen, along with significant but weak emissions for ζ Gem (-0.008 mag ± 0.004), η Aql (-0.019 ± 0.004 mag) and RS Pup (-0.110 ± 0.057 mag). In the case of V Cen, the emission is likely underestimated when using Eq. (4). If we assume, instead, the presence of dense clouds in the line of sight using Eq. (5), we obtain a silicate emission of -0.091 ± 0.013 mag (see Fig. 5).

From this figure (and Table 5), it is difficult to conclude whether there is a dusty CSE of silicate around the Cepheids in the sample or not, particularly because our method is sensitive to the used Eq. (4) or (5) when correcting the silicate ISM absorption (case of V Cen for instance), as well as to various sources of uncertainties, especially in the E(B-V) estimate. We also assume that the IR excess does not vary in time, as has been suggested by the SPIPS analysis referred to in Sect. 2.2. Still, using this method, we find residual dust emission at 9.7 μ m for the long-period Cepheids in the sample (η Aql, ζ Gem and RS Pup).



Fig. 5. The CSE emission at 9.7 μ m is calculated from Eq. (3) and indicated for each star in the sample (in magnitude). Cepheids are ordered by increasing pulsation period. If one uses Eq. (5) for V Cen, instead of Eq. (4), than the $E_{9.7}^{\text{CSE}}$ value is larger (orange bar in the figure). CSE emission appears when $E_{9.7}^{\text{CSE}} < 0$.

3.4. Extending the correction of the silicate absorption from $9.7 \,\mu m$ to the whole wavelength range of Spitzer

We correct the entire scope of *Spitzer* observations by subtracting a synthetic interstellar medium composed of silicates. Since

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Fig. 6. IR excess for all stars in sample at a specific phase is presented here, including (1) interpolated IR excess model from SPIPS, (see Sect. 2.2), (2) *Spitzer* observations stripped of various camera effects (see Sect. 2.3) and also corrected with regard to silicate absorption due to the ISM (orange curve, see Sect. 3.4).

we assumed an averaged ISM temperature of 20 K, the dust emission is negligible in the *Spitzer* wavelength range according to Wien's law. Thus, we must simply derive the absorption A_{λ}^{ISM} analytically using Mie theory. In the calculation, we take into account only the effective absorption cross-section C_{λ}^{abs} and we neglect the scattering effects since the radius of grain *a* is small compared to the mid-IR wavelength. Hence, we adopt the following expression for λ between 5 and 30 μ m

$$A_{\lambda}^{\rm ISM} \propto \kappa_{\lambda} = \int C_{\lambda}^{\rm abs}(a) \pi a^2 n(a) da.$$
 (6)

We first derive C_{λ}^{abs} using complex refractive index for silicates from Draine & Lee (1984; hereafter DL84), assuming an uniform



Fig. 7. Opacity efficiencies of typical dust encountered in circumstellar envelopes of oxygen-rich stars. These opacities are from aluminium oxide Al_2O_3 (Begemann et al. 1997), iron Fe (Henning & Stognienko 1996), gelhenite $Ca_2Al_2SiO_7$ (Mutschke et al. 1998), astronomical silicate from (Draine & Lee 1984)(DL84), and forsterite Mg₂SiO₄ (Jäger et al. 2003). The *N*-band between 8 and 14 μ m is represented by a grey strip and highlights the silicate vibrational modes.

distribution of ellipsoidal shapes given by Bohren & Huffman (1983). Then we derived the absorption coefficient κ_{λ} by taking into account a standard grain size distribution $n(a) \propto a^{-3.5}$ (Mathis et al. 1977). Finally we normalize A_{λ}^{ISM} using its specific value $A_{9.7}^{\text{ISM}}$ at 9.7 μ m that we already derived in Sect. 3.2.

For all the stars in the sample, we plot the IR excess (found to be constant with the pulsation phase, see Sect. 2.2) corrected from the ISM silicate absorption in Fig. 6. In the following sections, we first show that a dust envelope cannot reproduce the IR continuum excess, then we explore the possibility of a thin envelope of partially ionized gas in order to model the IR excess continuum.

4. Incompatibility of dust CSE model to explain IR excess continuum

Cepheids are oxygen-rich stars and so, most of the carbon in their envelopes is locked in CO molecules. In the condensation sequence described by Gail & Sedlmayr (1999) corundum (Al₂O₃) is expected to form first because of its high condensation temperature of about 1400 K in typical pressures encountered in circumstellar shells. For lower temperatures, Al₂O₃ is depleted and silicates such as gehlenite (Ca₂Al₂SiO₇) and forsterite (Mg₂SiO₄) can form. All these components present emission components mostly observed in the N band (8–13 μ m, see Fig. 7), with a width of at most a few microns. The IR excess we observe in Spitzer and SPIPS data does not present any clear spectral feature and is broader than 20 μ m. Figure 8 shows the best fit we obtain with silicate dust. Silicate dust features are clearly unlikely to explain the observed IR excess continuum from near- to mid-IR. This conclusion is in agreement with the work carried out by Schmidt (2015) in finding that CSE made of silicate dust cannot explain IR excess of 132 classical and type-II Cepheids. However, since the opacity of iron exhibits no particular feature, but rather a continuum (see Fig. 7), we investigate whether a warm dust envelope of iron could explain the IR excess continuum observed with the SPIPS and Spitzer dataset.

The CSEs were modeled using DUSTY (Ivezic et al. 1999), which solves the radiative transfer equations in a dusty



Fig. 8. IR excess of a silicate circumstellar envelope modeled with DUSTY around η Aql. Green curve is the silicate model with silicate grains from DL84.

environment. The method is based on a self-consistent equation for spectral energy density, including dust scattering, absorption, and emission. We present two CSE models with different inner shell temperatures. Iron is a component in oxygen-rich star mineralogy with a condensation temperature of $\approx 1000 \text{ K}$ for circumstellar pressures. Hence, the cold model takes into account the typical condensation temperature of iron ($\approx 1000 \text{ K}$) as the inner shell temperature which is thought to be realistic. A reduced χ^2 fitting is applied to adjust the optical opacity $\tau_{0.55}$. The hot model lets both the inner shell temperature and the optical opacity as free parameters during χ^2 fitting. In both hot and cold model we used a standard MRN size distribution (Mathis et al. 1977), and we computed the density distribution in the case of an envelope expansion which is driven by radiation pressure on the dust, the wind structure is derived taking into account the dust drift and the star's gravitational attraction. The outer shell radius is set to 500 times the inner shell radius. We test the consistency of these models on η Aql using interpolated ATLAS9 atmospheric models (see Table 3 in Sect. 2.3) as central source radiation in the DUSTY computation. The results of the computation are summarized in Table 7 and the computed IR excess is presented Fig. 9. Both models fails to reproduce the IR excess continuum modeled with SPIPS and observed with Spitzer. The cold model is well below the observed IR excess and the temperature required for iron in the hot model is much higher than the iron condensation temperature for circumstellar shell pressures. In that case, solid iron would not form or would be sublimated. Last, we can also argue that a CSE made of iron exclusively for each Cepheid is very unlikely. In conclusion, we do not expect a warm dust envelope to be the cause of IR excess continuum for Cepheids in the 1–30 μ m range.

5. The IR excess from a thin shell of ionized gas

The next step in our investigation considers whether an ionized, spherical gas shell can simultaneously explain at the near-(~1 μ m < λ < 5 μ m) and mid- (5 μ m < λ < 30 μ m) IR excess of Cepheids. As a first step, this study is conducted only at the specific pulsation phase of *Spitzer* data. We discuss the possible time variability of such a shell in Sect. 6.3.

We consider the emission of a thin gas shell around the star with its density and temperature constant for the sake of

 Table 7. Warm dust envelope parameters.

	Hot model	Cold model
Grain size	MRN	MRN
$T_{\rm in}$ (K) $^{(a)}$	2238 ^(a)	1000
$ au_{0.55}$	0.038 ^(a)	0.006 ^(a)
θ_{in} (mas)	10	109
$\dot{M} \left(M_{\odot} \mathrm{yr}^{-1} ight)$	2.04×10^{-7}	9.72×10^{-8}
χ^2	7.3	50.3

Notes. $T_{\rm in}$ and $\theta_{\rm in}$ are the inner temperature and diameter in milliarcseconds respectively. $\tau_{0.55}$ is the opacity at 0.55 μ m. Mass loss \dot{M} derived by DUSTY is also indicated. ^(a)Fitted parameters.



Fig. 9. IR excess of an iron circumstellar shell modeled with DUSTY around η Aql.

simplicity. The shape of the mid-IR excess, saturating to a constant flux ratio at large wavelengths (see Fig. 6), suggests an opacity source increasing with wavelength. We used the freefree and bound-free opacities for a pure H shell presenting such behaviour. The combined absorption coefficient (in m^{-1} ; SI(MKS) unit system) for these two opacity sources is given by (e.g. Rybicki & Lightman 2008)

$$\kappa_{\lambda} = 3.692 \times 10^{-2} \left[1 - e^{-\frac{\hbar c}{\lambda k T_{s}}} \right] T_{s}^{-1/2} \times (\lambda/c)^{3} \\ \times (\gamma \rho/m_{\rm H})^{2} [g_{\rm ff}(\lambda, T_{s}) + g_{\rm bf}(\lambda, T_{s})],$$

$$(7)$$

where *h*, *c*, and *k* hold their usual values, γ is the degree of ionization (between 0 and 1), T_s the temperature of the shell, m_H the hydrogen mass, and $g_{\rm ff}$ and $g_{\rm bf}$ are the free–free and bound-free Gaunt factors, respectively. These factors were computed mainly from approximation formulas given by Brussaard & van de Hulst (1962), Hummer (1988), and references therein. As an example, we present a typical shape of the absorption coefficient κ_{λ} computed for V Cen in Fig. 10 using the shell parameters from Table 8.

We compute the SED of the star plus the gas shell as described in Appendix B, taking into account the latter absorption coefficient κ_{λ} . In order to match the SPIPS photometries, in addition to the corrected *Spitzer* spectra presented in Sect 3, we perform a χ^2 fitting using the Levenberg–Marquardt method. We use bandpass filters to convert the flux of the physical model into the corresponding SPIPS photometries for the fitting procedure. In addition, since the SPIPS fitting assumes that there



Fig. 10. Bound-free and free–free absorption coefficient κ_{λ} computed for V Cen from 0.1 to 30 μ m. Bound-free absorption is characterized by saw teeth shapes which are sharper for shorter wavelength. Free–free absorption dominates wavelength above 1 μ m.

is no excess in the visible domain, that is, $\Delta m = 0$ for $\lambda < \infty$ 1.2 μ m (see Sect. 2.2), it is necessary to relax this assumption to allow the data to present deficit or excess in the visible domain depending on the physical behaviour of the ionized shell. This assumption is often considered equivalent to the suggestion for an improvement in the SPIPS physical treatment of the circumstellar environment. As a first step, we consider a simple thin, spherical, and partially ionized gas shell in order to reproduce the IR excess of the Cepheids in the sample. Hence, we fitted four parameters: three parameters from the gas shell (the ionized shell mass γM_s , its temperature T_s , and radius R_s) plus one parameter corresponding to the IR excess offset equal to $\Delta m \neq 0$ for $\lambda < 1.2 \,\mu$ m. Since *Spitzer* data have a higher statistical weight than SPIPS data, we first considered the different parameters by hand as first guesses to find the main ones for our study. The results are presented in Table 8 and in Fig. 11.

In Fig. 11 we observe discontinuities at short wavelengths, from visible to near-IR, which are due to bound-free opacities (see Fig. 10). Bound-free opacity decreases for longer wavelength, whereas free–free opacity increases. Beyond 5 μ m the bound-free contribution is negligible compared to the free–free contribution which explains the observed smooth continuum. For the Cepheids in the sample, we obtained shell temperatures between 3500 and 4500 K and an envelope thickness of ~15% of the radius of the star, while γM_s ranges from 10^{-9} to $10^{-7} M_{\odot}$. The IR excess correction offsets are found have positive values, which means $\Delta m \ge 0$ for $\lambda < 1.2 \,\mu$ m for all stars except for SU Cyg, which presents a slight negative value. Indeed, the several models computed present absorption in the visible domain (see Fig. 11), thus correction offsets have positive values to allow a deficit in the visible due to ionized shell absorption.

Within the prospect of JWST observations, we provide the synthetic IR excess anticipated from the shell of ionized gas in several bands (Table 9). We use filter transmissions of wide filters: F070W and F200W from Near-Infrared Camera (NIRCam)³ and F560W and F1000W from Mid-Infrared Instrument (MIRI)⁴. These filters, centered on 0.70, 2, 5.6 and 10 μ m,

³ https://jwst-docs.stsci.edu/display/JTI/NIRCam+ Filters

⁴ https://jwst-docs.stsci.edu/display/JTI/MIRI+

Filters+and+Dispersers

	T_{shell} (K)	$R_{\rm shell} (R_{\rm star})$	$\gamma M_{ m shell} (M_{\odot})$	Offset (mag)	χ^2
RS Pup	4011 ± 88	1.170 ± 0.014	$2.13 \times 10^{-7} \pm 1.1 \times 10^{-8}$	0.071 ± 0.002	3.46
ζ Gem	3780 ± 85	1.087 ± 0.013	$9.50 \times 10^{-9} \pm 9.0 \times 10^{-10}$	0.059 ± 0.001	3.23
η Aql	3569 ± 61	1.164 ± 0.010	$1.17 \times 10^{-8} \pm 4.0 \times 10^{-10}$	0.132 ± 0.002	2.73
V Cen	4353 ± 106	1.156 ± 0.012	$3.61 \times 10^{-9} \pm 2.0 \times 10^{-10}$	0.057 ± 0.004	0.28
SU Cyg	4402 ± 204	1.176 ± 0.027	$7.89 \times 10^{-9} \pm 8.6 \times 10^{-10}$	-0.010 ± 0.004	0.36

Table 8. Fitted parameters of the thin circumstellar shell of partially ionized gas, with constant temperature and density.

respectively, are suitable to measure the IR excess continuum from the ionized shell model.

of the PL relation when using instruments such as the JWST, as well as forthcoming mid-infrared instruments set on future 40 meter-class telescopes.

6. Discussion

6.1. The IR excess and dust environment

We estimate the infrared excess of Cepheids using the SPIPS algorithm ($\lambda < 5 \,\mu$ m) and *Spitzer* data ($5 < \lambda < 30 \,\mu$ m). The observed IR excess presented in Fig. 6 is thus calculated at the specific phases of *Spitzer* and makes the assumption that there is no excess or deficit in the visible domain due to the CSE ($\Delta m = 0$ for $\lambda < 1.2 \,\mu$ m). This leads to the following conclusions:

First, these IR excess emissions exhibit a continuum which is consistent across the wavelength range for all stars. It ranges in the data from about 2 to $30\,\mu\text{m}$ and corresponds to differences in magnitude of up to -0.1, and even -0.2 magnitudes for RS Pup and η Aql, between visible and far-infrared. Importantly, this IR excess rises in the near-infrared (around $2\,\mu\text{m}$) from about 0 magnitude of difference (assuming $\Delta m = 0$ for $\lambda < 1.2\,\mu\text{m}$) to -0.1 magnitude around $5\,\mu\text{m}$ for each star, which brings strong constrains on the models and in particular invalidate a pure CSE of dust to explain the IR excess continuum.

Second, in order to unveil CSE emission in the *N*-band we performed an independent correction of the ISM silicate absorption (Sect. 3) which seems to fill almost perfectly the silicate absorption seen in the *Spitzer* data. We have determined the excess at 9.7 μ m and we have found that there is no emission within the uncertainty for SU Cyg and V Cen, while weak emissions are found for ζ Gem, η Aql and RS Pup. The slight residuals that we found from our spectroscopic analysis at 9.7 μ m could be attributed to faint dusty CSE around Cepheids with a flux contribution (compared to the stellar flux) of a few percents, which is, on average, ten times less than what was predicted by other studies based on interferometry (Gallenne et al. 2012, 2013), and consistent with Schmidt (2015) who found no silicate emission for a large sample of Cepheids.

Third, using photometric bands and the same basic approach, but without considering the pulsation of the Cepheids, Schmidt (2015) found that 21 of 132 classical and type 2 Cepheids in his sample demonstrate a clear or weak IR infrared excess. Moreover, these 21 Cepheids have periods larger than 11 days. Conversely, we have 4 short-period Cepheids in the sample (except RS Pup) and all of them show a clear IR excess. However, there is no star in common between the two studies to delve deeper into the analysis.

Four, we find a large, cold and inhomogeneous circumstellar environment around the Cepheids RS Pup, V Cen, which is seen in the *Herschel* images. As Cepheids are relatively young stars, they are still likely close to the cloud where they formed and such an environment can contribute to the overall IR excess, either in absorption or emission. This could also affect the mid-infrared photometry of Cepheids and, thus, potentially affect estimations

6.2. The IR excess explained by a thin shell of ionized gas

We show that a thin shell of ionized gas with a temperature ranging from 3500 to 4500 K, depending on the Cepheid considered, and with a width of typically $\approx 15\%$ of the radius of the star can reproduce the IR excess. Up to now, the only attempt to detect ionized material was carried out using the Very Large Array (VLA) at 5 GHz on η Aql and four other classical Cepheids (Welch & Duric 1988). Since no 3σ detection has been reported, only upper limits on flux density were derived. From the ionized shell model presented in this paper, we derived a flux density between 0.01 and 0.1 μ Jy at 5 GHz ($\approx 20\%$ above the star continuum) which is below the upper limit on flux density of $\approx 100 \mu$ Jy estimated by Welch & Duric (1988).

On the other hand, interferometric observations have resolved CSEs around Cepheids. The first detection was reported around 1 Car (Kervella et al. 2006) followed by δ Cep and Polaris (Mérand et al. 2007). These CSEs were modeled with a ring at a distance of 2–3 R_{\star} , that is, close to the star, in a region where the temperature is high enough (>2000 K) to prevent dust condensation (Gail & SedImayr 1999). Thus, these observations are more likely explained by a shell of partially ionized gas. This finding in detection by interferometry appears to support a widespread phenomenon among classical Cepheids.

Also, extensive studies of $H\alpha$ profiles in the atmosphere of short-, mid- and long-period Cepheids have shown that strong increases of turbulence occur when the atmosphere is compressed during its infalling movement or because of shock waves dynamics (Breitfellner & Gillet 1993a,c,b; Fokin et al. 1996). In the case of long-period Cepheids, several shock waves can be observed and P Cygni profiles show that there is an expanding shell of $H\alpha$ emission which is detached from the photosphere (Gillet 2014). In addition, analytical works by Neilson & Lester (2008) have shown that mass loss is enhanced by pulsations and shocks in the atmosphere. Our study suggests that this loss in mass could be due to the effects of partially ionized gas.

The model of the ionized gas shell could also be linked to the chromospheric activity of Cepheids. Sasselov & Lester (1994) report HeI λ 10830 observation on seven Cepheids, providing the evidence of a high temperature plasma and steady material outflow in the highest part of the atmosphere. In addition, high resolution profiles of Mg II h and k lines (2900 A) of five Cepheids using the International Ultraviolet Explorer instrument (Schmidt & Parsons 1984) revealed extended dynamical chromospheres up to a tenth of stellar radii composed of rising and falling material. Such extensions could be compatible with the shell thickness presented in this paper. Outflowing materials with velocity of 50–100 km s⁻¹ can, in turn, eject material to several stellar radii if the velocity lasts through the pulsation cycle.

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Fig. 11. IR excess fitting results of ionized gas shell (red curve, see Sect. 5 and Appendix B) presented with residuals. Yellow region is the error on the magnitude obtained using the covariance matrix of the fitting result. Pulsation phase ϕ of *Spitzer* observations and SPIPS interpolation is indicated.

 Table 9. IR excess from the ionized shell models in various bands of the JWST.

	Δ F070W	Δ F200W	Δ F560W	Δ F1000W
RS Pup	0.110	0.009	-0.074	-0.100
ζ Gem	0.090	0.016	-0.029	-0.034
η Aql	0.220	0.030	-0.038	-0.037
V Cen	0.069	0.004	-0.071	-0.101
SU Cyg	0.063	0.001	-0.071	-0.105

Notes. Wide filters F070W, F200W, F560W and F1000W centered respectively on 0.70, 2, 5.6 and $10\,\mu$ m are presented. Values are given in magnitudes.

These strong mass transfers could explain the enigmatic X-rays detections with *Chandra* and *XMM-Newton* (Engle et al. 2017).

In parallel, it is interesting to compare Cepheids to very longperiod Mira stars for which a radiosphere near $2R_{\star}$ attributed to free-free emission has been reported (Reid & Menten 1997).

6.3. Limit of the model and perspectives

We have found relatively low temperatures for hydrogen ionization (between 3500 and 4500 K see Table 8) and only a small fraction of the gas should be ionized according to the Saha equation. In particular, for gas temperatures below 4000 K, the number of free electrons should be mostly provided by metals, such as iron or aluminum, which have low ionization potential. This effect could in turn produce a fainter ionized shell for lowmetallicity Cepheids in the Magellanic clouds. Thus, it would be interesting to theoretically quantify the impact of metallicity on the shells of ionized gas, and the PL relation. Moreover, our model does not take into account temperature or density gradients in the star's atmosphere, nor, in particular, compression or shock waves which could also heat up the shell and ionize the gas.

There are indications from SPIPS analysis that the IR excess of Cepheids is not time-dependent at all, or only slightly. Evidence of slight cycled variations exist due to the opacity change at 4.5 μ m caused by periodic formation and destruction of CO molecules in the atmosphere (Scowcroft et al. 2016). As we have *Spitzer* data only at a specific phase of pulsation for each Cepheid, we cannot firmly conclude a figure for the timedependency of the mid-IR excess. Nevertheless, if we assume that the IR excess is constant, then, as our thin shell of ionized gas is close to the star ($\approx 15\%$ of the radius of the star), it is supposed to be dynamic and its parameters should vary in time. In conducting the test for η Aql, we find a rather stable relative size for the shell ($\approx 15 \pm 2\%$) and a temperature variation from about 3500 to 4500 K, which is similar to the values we obtained from one star to the other in the sample.

Last, our simple model suggests that the thin gas shell absorbs the light coming from the star in the visible domain (from 0.01 up to 0.13 mag), which invalidates the initial assumptions of $\Delta m = 0$ for $\lambda < 1.2 \,\mu$ m in the SPIPS algorithm. We obtain satisfactory results only if we apply a correction offset $\Delta m > 0$ for all wavelengths (except for SU Cyg with a slight negative offset). To explain this shift, we suggest that the distance found by the SPIPS algorithm might be too large by few percents (factor $10^{\Delta m/2.5}$), all other parameters being unchanged. In other words, if obscured by a shell of ionized gas, Cepheids could be slightly closer than expected by SPIPS. On the interferometric side, the angular diameter of the star would also be lower by few percents, but this can be compensated by the actual size of the shell, and would have little impact within the SPIPS fitting. Thus, a spatial and chromatic analysis of the shell, including interferometric constraints in all available bands, in particular VEGA/CHARA (visible), PIONIER/VLTI (infrared) and MATISSE/VLTI (*L*, *M*, *N* bands), is still necessary to better understand the environment of Cepheids and, ultimately, to survey the impact on the PL relation.

7. Conclusion

- 1. For the five Cepheids, we report a continuum IR excess increasing up to approximately -0.1/-0.2 magnitude at $30\,\mu$ m, which cannot be explained by a hot or cold dust model of CSE.
- 2. Within the limits of our assumptions, we do not assert a firm conclusion regarding the presence of CSE emission in the *N*-band, but we assume it is likely to prove weak (>-0.1mag) according to our results.
- 3. We demonstrate for the first time that the IR excess of Cepheids can be explained by a free-free emission of a thin shell of ionized gas with a thickness of a $\approx 8-17\%$ star radius, an ionized mass of $10^{-9}-10^{-7}M_{\odot}$, and a temperature of 3500-4500 K. In this simple model, density and temperature have a constant radial distribution.
- 4. The presence of a thin shell of partially ionized gas around Cepheids must be tested with interferometers operating in the visible domain, in the mid-IR, or in the radio domain. The impact of such CSEs of ionized gas on the PL relation of Cepheids also requires futher investigation.

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⁵ Available at http://cdsweb.u-strasbg.fr/

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Appendix A: SPIPS data set and fitted pulsational model of the star sample

Fig. A.1. The SPIPS results of ζ Gem. Velocity: Bersier et al. (1994). Effective temperature: Luck et al. (2008). Angular diameter: Lane et al. (2002), Kervella et al. (2004). Photometry: ESA (1997), van Leeuwen et al. (1997), Price et al. (2001), Wright et al. (2010), Berdnikov & Turner (2002a), Feast et al. (2008), Monson et al. (2012), Gaia Collaboration (2018).

The plots are organized as follows: pulsational velocity, effective temperature and angular diameter curves according to the pulsation phase are shown on the left panels, while the right panels display photometric data in various bands. Above each figure, the projection factor set to p = 1.270 is indicated, along with the fitted distance d using parallax-of-pulsation method, the fitted color excess E(B-V), and the ad hoc IR excess law. In the photometric panels, the gray dashed line corresponds to the magnitude of the SPIPS model without CSE. It actually corresponds to the magnitude of a Kurucz atmosphere model, m_{kurucz} , obtained with the ATLAS9 simulation code from Castelli & Kurucz (2003) with solar metallicity and a standard turbulent velocity of 2 km s⁻¹. The gray line corresponds to the best SPIPS model, which is composed of the latter model without CSE plus an IR excess model. Note that for WISE, MSX and IRAS filters observations above 5 μ m, only one data point is obtained without information on the phase. Hence, it is represented by a horizontal gray strip for which the vertical width is the uncertainty of the measurement. In the angular diameter panels, the gray curve corresponds to limb-darkened (LD) angular diameters. For metallic stars, when effective temperature is low enough, CO molecules can form in the photosphere and absorb light in the CO band-head at 4.6 μ m (Scowcroft et al. 2016). This effect is observed in the Spitzer I2 IRAC dataset of ζ Gem and V Cen (see Figs. A.1 and A.2). In this case, these data were ignored during the fitting of SPIPS. When no effective temperatures and no angular diameters are included in the SPIPS model, there is a degeneracy between the mean temperature and E(B-V). We estimate that SPIPS can make an error of +/-200 K on the effective temperature and +/-0.05 on E(B-V). Only V Cen has no data for both effective temperature and angular diameter, nevertheless the fitting of SPIPS is thought to be a reliable (for example see E(B-V) value compared with those provided in the literature in Table 5).



Fig. A.2. The SPIPS results of V Cen. Velocity: Gieren (1981). Effective temperature: No data. Angular diameter: No data. Photometry: Walraven et al. (1964), Welch et al. (1984), Laney & Stobie (1992), Berdnikov & Turner (2002b), Monson et al. (2012), Gaia Collaboration (2018).



Fig. A.3. The SPIPS results of RS Pup. Velocity: Anderson (2014). Effective temperature: No data. Points are nodes for a spline interpolation. Angular diameter: Kervella et al. (2017). Photometry: Moffett & Barnes (1984), Welch et al. (1984), Laney & Stobie (1992), ESA (1997), Price et al. (2001), Berdnikov & Turner (2002a), Gaia Collaboration (2018).

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Fig. A.4. The SPIPS results of η Aql. Velocity: Storm et al. (2004), Barnes et al. (2005). Effective temperature: Luck & Andrievsky (2004), Kovtyukh et al. (2010). Angular diameter: Lane et al. (2002), Kervella et al. (2004). Photometry: Pel (1976), Welch et al. (1984), Neugebauer et al. (1984), Barnes et al. (1997), ESA (1997), van Leeuwen et al. (1997), Kiss (1998), Rieke et al. (2004), Wright et al. (2010), Monson et al. (2012).



Fig. A.5. The SPIPS results of SU Cyg. Velocity: Gorynya et al. (1992), Effective temperature: Andrievsky et al. (2005). Angular diameter: No data. Photometry: Szabados (1977), Welch et al. (1984), Moffett & Barnes (1984), Szabados (1991), ESA (1997), van Leeuwen et al. (1997), Kiss (1998), Berdnikov (2008), Monson & Pierce (2011), Gaia Collaboration (2018).

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Appendix B: The IR excess of a thin gas shell at constant temperature and density

The shell emission is obtained integrating the radiative transfer equation along rays defined by their impact parameter p (see Fig. B.1) according to the method described in Panagia & Felli (1975).

We assume a constant shell temperature T_s and density ρ_s . The gas opacities (see Eq. (7)) can be written under the form $\kappa(\lambda, T_s) = \rho_s^2 \chi_\lambda(T_s)$.

According to Fig. B.1 we have to take into account two cases corresponding to the impact parameter p respectively larger and smaller than the stellar radius R_* .

For $p \ge R_*$, taking into account the symmetry of the problem the optical depth along the ray is given by

$$\tau_{\lambda}(p) = 2 \int_{0}^{\sqrt{R_{\text{out}}^2 - p^2}} \kappa(\lambda, T_s) \mathrm{d}s, \tag{B.1}$$

which, for a constant T_s and density ρ_s gives

$$\tau_{\lambda}(p) = 2\rho_{\rm s}^2 \chi_{\lambda}(T_{\rm s}) \sqrt{R_{\rm out}^2 - p^2}.$$
 (B.2)

Similarly, for $p \leq R_*$ we have

$$\tau_{\lambda}(p) = \rho_{\rm s}^2 \chi_{\lambda}(T_{\rm s}) \left[\sqrt{R_{\rm out}^2 - p^2} - \sqrt{R_{*}^2 - p^2} \right].$$
(B.3)

For $p \ge R_*$, the specific intensity is given by

$$I_{\lambda}(p) = B_{\lambda}(T_s)(1 - e^{-\tau_{\lambda}(p)}), \tag{B.4}$$

since T_s is assumed to be constant along the ray.

For $p \leq R_*$, both the shell and the stellar photosphere contribute to the specific intensity

$$I_{\lambda}(p) = B_{\lambda}(T_s) \left(1 - e^{-\tau_{\lambda}(p)}\right) + I_{\lambda}^* e^{-\tau_{\lambda}(p)}, \tag{B.5}$$

where I_{λ}^{*} is the stellar specific intensity.

The observed total emerging flux at a distance d is then computed numerically by quadrature with the following integral

$$F_{\lambda} = \frac{2\pi}{d^2} \int_0^{R_{\text{out}}} pI_{\lambda}(p) \mathrm{d}p.$$
(B.6)



Fig. B.1. Circumstellar shell model. The blue line represents a ray along which the radiative transfer equation is integrated. p is the corresponding impact parameter. s is the distance along the ray R_* is the stellar radius. R_{out} is the external radius of the shell.

From the result of the integral in Eq. (B.6) we can deduce the magnitude excess defined by

$$\Delta \text{mag} = -2.5 \log\left(\frac{F_{\lambda}}{F_{\lambda}^*}\right),\tag{B.7}$$

with $F_{\lambda}^* = \pi \left(\frac{R_*}{d}\right)^2 I_{\lambda}^*$.

Note that in the particular case where we have $I_{\lambda}^* = B_{\lambda}(T_*)$ with $T_s = T_*$, Eq. (B.6) can be integrated analytically to give

$$F_{\lambda} = \pi \left(\frac{R_*}{d}\right)^2 B_{\lambda}(T_s)$$

$$\times \left[1 + \left[\left(\frac{R_{\text{out}}}{R_*}\right)^2 - 1\right] \left[1 + \frac{2}{\tau_{\lambda}^{*2}} \left[(1 + \tau_{\lambda}^*)e^{-\tau_{\lambda}^*} - 1\right]\right]\right], \quad (B.8)$$

with τ_{λ}^* defined as $2\rho_s^2 \chi_{\lambda}(T_s) R_* \sqrt{\left(\frac{R_{out}}{R_*}\right)^2 - 1}$. The corresponding magnitude excess is given by

$$\Delta \text{mag} = 2.5 \log \left[1 + \left[\left(\frac{R_{\text{out}}}{R_*} \right)^2 - 1 \right] \left[1 + \frac{2}{\tau_{\lambda}^{*2}} \left[(1 + \tau_{\lambda}^*) e^{-\tau_{\lambda}^*} - 1 \right] \right] \right]$$
(B.9)