Using the Sensor Noise Model to Design Better Steganographic Schemes

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Part 1: Motivations / Inspirations / Problems

Part 2: Covariance matrix of the sensor noise in the DCT domain

Part 3: Two Embedding strategies and associated results

Part 4: Conclusions

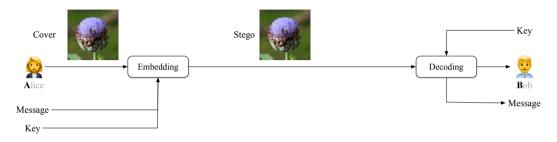
Part 1: Motivations / Inspirations / Problems

Part 2: Covariance matrix of the sensor noise in the DCT domain

Part 3: Two Embedding strategies and associated results

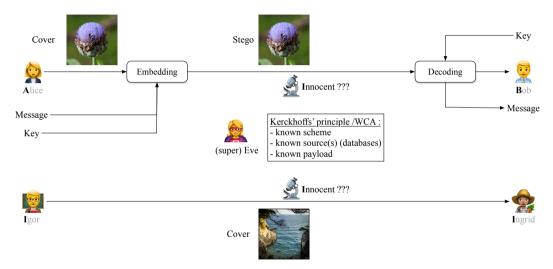
Part 4: Conclusions

Alice's steganographic game





Alice's steganographic game



Alice's steganographic game





Alice's goals:

- maximize embedding capacity
- maximize Eve's error rate

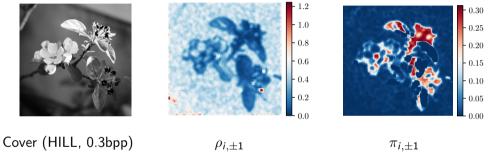
Inspiration #1: Adaptive/Additive embedding - Sampling

Fridrich's group [Filler2010]

- Adaptive:
 - Associate to each sample i a cost $\rho_{i,k}$ for modification k
 - Associate to each sample i a modification probability $\pi_{i,k}$ for modification k
 - Additive:
 - ► Embed and minimize $\sum_{i,k} \pi_{i,k} \rho_{i,k}$
 - Practical solution: STC [Filler2011]
 - Equivalent to sampling (nearly, see [Kin-Cleaves2020]):
 - ► Sample *k* from:

$$\pi_{i,k} = rac{\exp\left(-\lambda
ho_{i,k}
ight)}{\sum_{k}^{Q/2} \exp\left(-\lambda
ho_{i,k}
ight)}$$

Inspiration #1: Adaptive/Additive embedding - Sampling



Problem:

- ► How to **sample** from multivariate probabilities?
- ▶ How to **embed** from multivariate probabilities?

Coding view:

► Non-additive costs

Statistical view:

▶ Non-independent modifications

Signal processing view:

- Induce **correlations** between embedding changes (ex: Pr(+1;+1) > Pr(+1;-1))
- ► a.k.a. synchronizations

Related schemes:

- ▶ Synch [Filler2010] , spatial, Gibbs
- ► CMD [Li2015] , spatial
- DeJoin [Zhang2017], spatial, joint costs, conditional probabilities
- ► GINA [Wang2019], spatial extension of CMD, Color
- ► BBC, BBM [Wang2020], DCT

Principles:

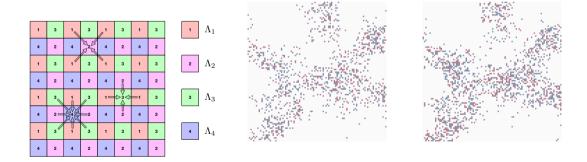
- 1. Decompose the image samples (pixel/DCT) into disjoint lattices/groups $\{\Lambda_1, \ldots, \Lambda_n\}$
- 2. compute costs in Λ_1 (additive)
- 3. embed in Λ_1 (additive)
- 4. compute costs in Λ_2 given the modifications in Λ_1 (non-additive)
- 5. embed in Λ_2 (additive)
- 6. iterate until Λ_n



Updating "rules" (CMD):

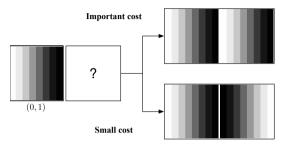
Emb. on 4 lattices

$$\rho'_{i}(+1) = \frac{1}{9}\rho_{i}(+1)$$
, if $\mu_{i} > 0$, $\rho'_{i}(+1) = \rho_{i}(+1)$, else



HILL, 0.3bpp

CMD, 0.3bpp



BBM and BBC

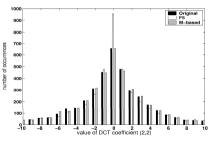
Problem:

▶ Theoretical justifications behind theses synchronization heuristics?

Inspiration #3: Steganography mimicking a statistical model

Model based steganography [Sallee2003]

- \triangleright $D_{KL}(C, S) = 0$ (Stego-security in watermarking [Cachin1998][Cayre2008])
- Steganography mimicking the sensor noise of a scanner [Franz2002]
- \Rightarrow High capacity: source S, capacity = H(S)



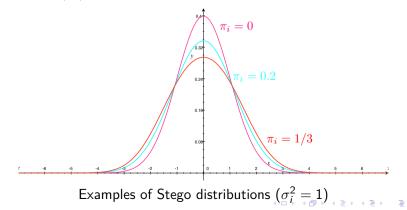
From [Sallee2003]

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Inspiration #4: Steganography distorting a statistical model

MiPod [Sedighi2016]

- ► Image noise estimated using Wiener prediction
- Noise Variance σ_i^2 (Gaussian model) \Rightarrow GLRT \Rightarrow deflection coefficient $\delta_i^2 = \pi_i^2/\sigma_i^4$ \Rightarrow Cost $\rho_i = \pi_i/\sigma_i^4$



Inspiration #3/#4: Steganography mimicking/distorting a statistical model

Problems:

- ▶ What's the "good" model of the noise in the JPEG domain?
- ► How to compute it?
- ► How to use the noise model in steganography?

Raised questions

Q1: What's the good model of the noise in the JPEG domain? and how to compute it?

Q2: Is there a theoretical justification behind the synchronization heuristics?

► See part 2

Q3: How to use the noise model in steganography?

Q4: How to sample from multivariate probabilities? How to embed from multivariate probabilities?

► See part 3

Why do you bother us with problems?

Teaser:

ightharpoonup Natural Steganography: QF100, 2 bits per non-zero-AC coef, SRNet, $P_E=37\%$

 Σ – JMiPod: QF100, $P_E = +15\%$ w.r.t. SI-Uniward at 0.4 bit per coefficient

Part 1: Motivations / Inspirations / Problems

Part 2: Covariance matrix of the sensor noise in the DCT domain

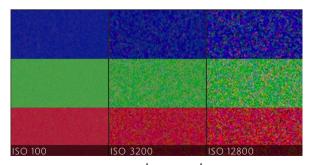
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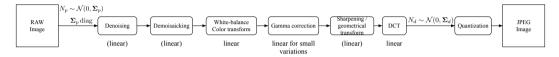
What's the sensor noise?

Poisson-Gaussian sensor noise

- ▶ additive **independent** noise $N_i \sim \mathcal{N}(0, a\mu_i + b)$
- $\blacktriangleright \mu_i$ "clean" photo-site value at location i
- ▶ parameters a and b constant for a given camera and a given sensitivity (ISO parameter), can be easily estimated on RAW images



Noise processing: from RAW to JPEG



Generic development pipeline

Sensor noise in the DCT domain:

- Multivariate Gaussian (linear approximation)
- lacktriangle Covariance matrix $oldsymbol{\Sigma}_d$

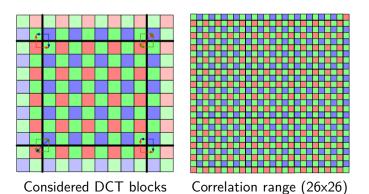
Q1: What's the good model of the noise in the JPEG domain? and how to compute it?

- ► This model!
- See the 4 next slides

How to compute it? The algebraic way [Taburet2020]



Linear development pipeline



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How to compute it? The algebraic way [Taburet2020]



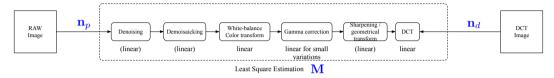
Linear development pipeline

Algebra:

$$ightharpoonup \Sigma_d = \mathsf{M} \Sigma_p \mathsf{M}^t$$

- ightharpoonup size of \mathbf{n}_p and \mathbf{n}_d : 26^2 and 24^2
- ▶ size of Σ_d : $(24^2 \times 24^2)$

How to compute it? The estimation way [Giboulot2020]



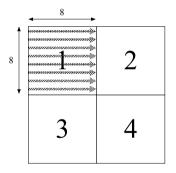
Development pipeline

Estimation setup:

- ightharpoonup pairs $(\mathbf{n}_p, \mathbf{n}_d)$
- ightharpoonup (a, b) known
- ▶ M can be estimated by Least Square Estimation
- ► More versatile!

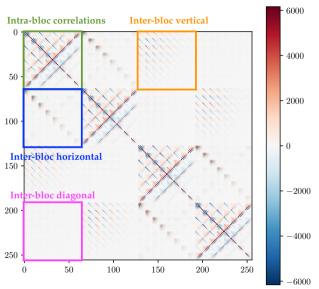
Analysis of the covariance matrix

- $\mu = \operatorname{cst} \Leftrightarrow \Sigma_p \propto \mathbf{I}$
- Linear pipeline, luminance
- ► Only 4 blocks, row scan:

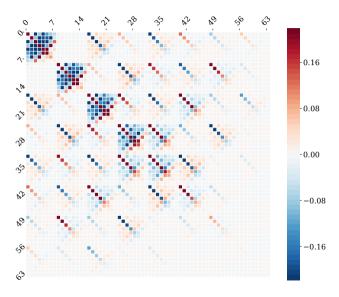


 \triangleright Size of $\Sigma'_d = 256 \times 256$

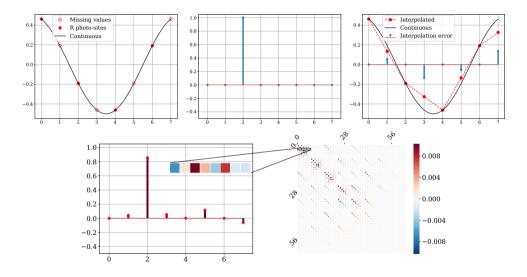
Analysis: whole covariance



Analysis: intra-block correlations

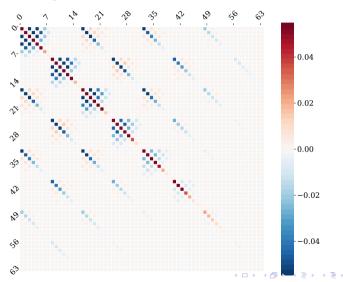


Analysis (intra-block): correlations due to demosaicking artifacts

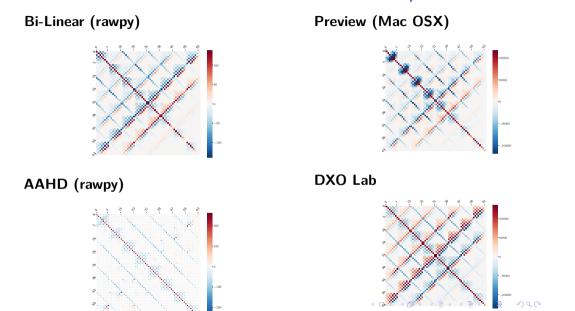


Analysis (intra-block): correlations due to low pass filtering

Effect of low-pass filtering of heteroscedastic noise:

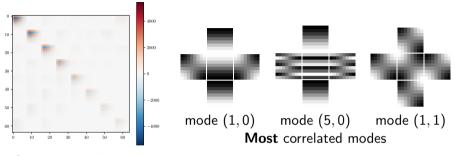


Intra-block Covariance matrix after different developments



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Analysis (inter-block)



Covariance sub matrix

Inter-block correlations encode block continuities!

► Rational for BBC [Wang2020]

Q2: Is there a theoretical justification behind the synchronization heuristics?

▶ Yes, preserve the natural correlations of the development pipeline

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Strategy 1: Steganography mimicking a statistical model

Q3: How to use the noise model in steganography?

▶ Natural steganography : The stego signal mimics the sensor noise [Bas2016]



Note:

Strategy 1: Steganography mimicking a statistical model

Principle of Model-Based steganography (RAW domain):

► Cover at *ISO*₁:

$$X_i^{(1)} \sim \mathcal{N}(\mu_i, \mathsf{a}_1\mu_i + b_1)$$

► Cover at *ISO*₂:

$$X_i^{(2)} \sim \mathcal{N}(\mu_i, a_2\mu_i + b_2)$$

- ▶ Steganographic signal $S_i \sim \mathcal{N}(0, (a_2 a_1)x_i + b_2 b_1)$

Requirement in the DCT domain (before quantization):

$$\mathbf{S} \sim \mathcal{N}(0, \mathbf{\Sigma}_d)$$



How to sample from multivariate probabilities?

Q4: How to sample from multivariate probabilities? How to embed from multivariate probabilities?

► See the 8 next slides

Three probabilistic properties:

- 1. Independency rule:
 - \triangleright {**B**₁,..., **B**_n} independent blocks

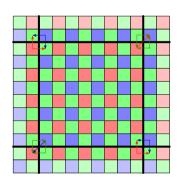
$$\Pr(\mathbf{B}_1,\ldots,\mathbf{B}_n)=\Pr(\mathbf{B}_1)\ldots\Pr(\mathbf{B}_n)$$

- 2. Dependency and chain rule of conditional probabilities:
 - $ightharpoonup \{B_1, \ldots, B_n\}$ dependent blocks

$$\Pr(\textbf{B}_1,\ldots,\textbf{B}_n) = \Pr(\textbf{B}_1)\Pr(\textbf{B}_2|\textbf{B}_1)\ldots\Pr(\textbf{B}_n|\textbf{B}_{n-1},\ldots,\textbf{B}_1)$$

3. Computing $Pr(\mathbf{B}_n|\mathbf{B}_{n-1},\ldots,\mathbf{B}_1)$ is easy on Gaussian distributions (Schur and Cholesky decompositions)

Independent blocks?



⇒ Two non-connected blocks are independent

Embedding at the block level

Decomposition into 4 macro-lattices $\{\Lambda_1, \Lambda_2, \Lambda_3, \Lambda_4\}$

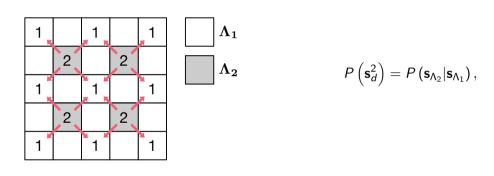
1	1	1
1	1	1
1	1	1



$$P\left(\mathbf{s}_{d}^{1}\right)=P\left(\mathbf{s}_{\Lambda_{1}}\right),$$

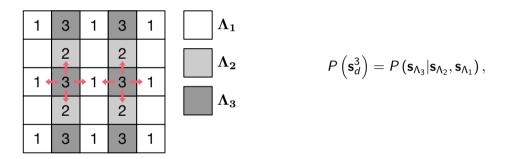
Embedding at the block level

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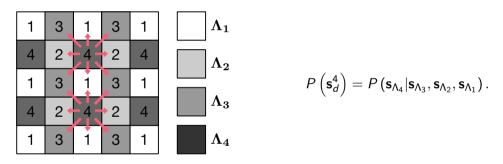
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Embedding at the block level

Decomposition into 4 macro-lattices $\{\Lambda_1, \Lambda_2, \Lambda_3, \Lambda_4\}$



Compliant with the chain rule:

$$\begin{split} P\left(\mathbf{s}_{d}\right) &= P\left(\mathbf{s}_{\Lambda_{1}}, \mathbf{s}_{\Lambda_{2}}, \mathbf{s}_{\Lambda_{3}}, \mathbf{s}_{\Lambda_{4}}\right), \\ &= P\left(\mathbf{s}_{\Lambda_{1}}\right) P\left(\mathbf{s}_{\Lambda_{2}}|\mathbf{s}_{\Lambda_{1}}\right) P\left(\mathbf{s}_{\Lambda_{3}}|\mathbf{s}_{\Lambda_{1}}, \mathbf{s}_{\Lambda_{2}}\right) P\left(\mathbf{s}_{\Lambda_{4}}|\mathbf{s}_{\Lambda_{1}}, \mathbf{s}_{\Lambda_{2}}, \mathbf{s}_{\Lambda_{3}}\right). \end{split}$$

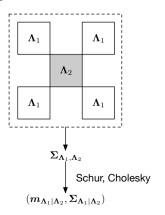


Embedding at the coefficient level

Example $(\Lambda_2 \mid \Lambda_1)$:

$$m{s}_{m{\Lambda}_2|m{\Lambda}_1} \sim \mathcal{N}(m{m}_{m{\Lambda}_2|m{\Lambda}_1}, m{\Sigma}_{m{\Lambda}_2|m{\Lambda}_1})$$

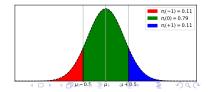
1. Compute the conditional matrix



Sample/Embed within each block

$$\begin{cases} s_{0} = m_{0} + L(0,0) \cdot n_{0} \\ s_{1|0} = \underbrace{m_{1} + L(1,0) \cdot n_{0}}_{m_{1|0}} + \underbrace{L(1,1)}_{\sigma_{1|0}^{2}} \cdot n_{1} \\ \vdots \end{cases}$$

with $n_i \sim \mathcal{N}(0,1)$ Compute the PMFs $\pi_i(k)$, the costs, the Capacity Q-arry embedding



Embedding scheme (J-Cov-NS)

Algorithm 1 J-Cov-NS

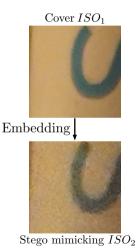
- **Inputs**: Cover RAW \mathbf{X}_p , message, key, developed Cover \mathbf{X}_d (DCT domain) and JPEG \mathbf{X}_J ;
- For each sub-lattice $\Lambda_i \in \{\Lambda_1, \Lambda_2, \Lambda_3, \Lambda_4\}$ and For each DCT block do:
 - ightharpoonup Compute the covariance matrix Σ_d
 - ► Compute $\mathbf{m}|\mathbf{\Lambda}_{i-1}...\mathbf{\Lambda}_1$ and $\mathbf{\Sigma}|\mathbf{\Lambda}_{i-1}...\mathbf{\Lambda}_1$
 - ► **For** each JPEG coefficient of **X**_J **do**:
 - Compute the conditional (Gaussian) distribution
 - ▶ Compute the PMF $\pi(k)$;
 - Sample w.r.t. $\pi(k)$ or embed w.r.t the costs;
 - Sample in the continuous domain (needed for conditioning)
- Output JPEG stego Y.

Embedding on 4×64 lattices

Benchmark: steganalysis

Dedicated setup:

Cover ISO_2



Setup (E1Base), $ISO_1 = 100$, $ISO_2 = 200$:

- ▶ 10000 covers *ISO*₂
- ► 10000 stegos ISO_{1→2}

Classifier train on covers/stego 5000 pairs and tested on 5000 pairs

$$P_E = min(\frac{P_{FA} + P_{MD}}{2})$$

Empirical security for NS [Taburet2020]

P _E (%) /	SI-Uniward	Н	J-Cov-NS	Intra-block
QF	1 bpnzAC	(bpnzAC)		only
100	0.0	2.0	42.9	0.0
95	0.4	2.2	41.2	0.2
85	12.3	2.4	41.2	15.8
75	24.8	7.0	41.6	25.2

Linear Classifier with DCTR

P _E (%) / QF	J-Cov-NS
100	37.4
95	31.2
75	35.0

QF / P _E in %	K = 1	K = 2	K = 3	K = 5
100	1.0	12.9	28.7	40.4
95	3.5	23.6	39.3	40.9
85	39.8	39.8	39.8	41.8
75	40.4	40.4	40.4	41.2

SRNet

Q-arry embedding

Strategy 2: Steganography distorting a statistical model [Giboulot2020]

Minimize the **multivariate** deflexion

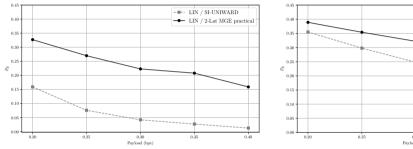
- ▶ Sensor noise distributed as $\mathcal{N}(0, \Sigma_d)$
- ▶ Additive stego-signal minimizing the D_{KL} for a given payload size distributed as $\mathcal{N}(0, \alpha \Sigma_d)$

Embedding mechanism:

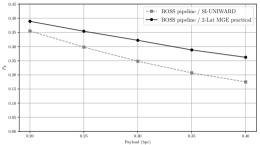
- \blacktriangleright Very similar to NS (but only 2 imes 64 lattices, diagonal correlations are negligible)
- ► Can be applied on any (estimated) pipeline

Strategy 2: Steganography distorting a statistical model [Giboulot2020]

Results, Effcicient-net B3-stride 1, BOSSBase



Linear development pipeline



BOSS development pipeline

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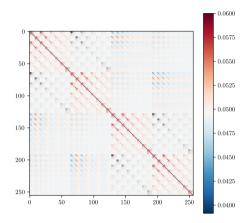
Part 4: Conclusions

Conclusions

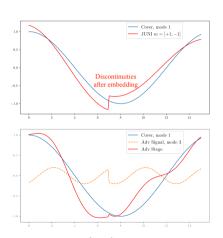
- ► Correlations matters (especially for high QF or in the spatial/color domain)
- Correlations are due to demosaicking, resizing, denoising, DCT transform, ...
- Joint probabilities matters (correlations within a block and between a block)
- ► The development pipeline matters
- Assumptions matters (doesn't work on Sigma sensors, on Leica/Kodak sensors which is not Gaussian)

One more correlation!

Correlations are everywhere [Bernard2020]



Covariance matrix of the stego signal after Adv-Emb [Tang2019]



Analysis (canceling discontinuities)

Inspirations / References

(Taburet2019)

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