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Analysis of strain and disordering kinetics based on combined RBS-channeling and X-ray diffraction atomic-scale modelling

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Abstract

Ion beams delivered by particle accelerators are routinely used to emulate harsh, radiative environments and they also constitute the foundations of the modern microelectronics industry. To characterize irradiated materials, numerous experimental and computational techniques can be implemented, but it is extremely difficult to effectively intertwine them, and to compare the associated data. In the present work, we present an integrated, experimental and computational approach that uses a same set of molecular dynamics simulations to generate signals of Rutherford backscattering spectrometry in channelling condition and X-ray diffraction, with UO_2 as a test-case material. From these signals, parameters to monitor the damage level are computed, compared and confronted with experimental data. Although the evolution of the strain and disordering kinetics obtained by simulations differ on an absolute scale from those obtained experimentally (a discrepancy inherent to the method used to generate the atomic-scale data), a very good relative agreement is obtained, which demonstrates the validity of the approach, hence providing a new tool for the fine study of irradiation effects in materials.

Keywords: Irradiation effect; RBS/C; X-ray diffraction (XRD); Molecular dynamics simulations; Defects

1 Introduction

In our modern society, there is an increasing number of activities involving the use of energetic ions delivered by particle accelerators, which encompass (but are not limited to) health (with hadrontherapy) [1], high-energy and nuclear physics [2, 3], astronomy [4], and materials science. In this latter domain, several industries and research fields have benefited greatly from the ion irradiation process which can result in both the controlled introduction of foreign atoms in the lattice materials and the tailored modifications of the atomic structure. Ion doping of semiconductors, for instance, represents one vital step for modern integrated-circuit manufacturing [5, 6], and it is considered as a promising route for developing materials with applications in novel optoelectronic devices [7] as well as in spintronics [8] and nanophotonics [9]. In a broader framework, ion irradiation is explored to tailor various properties of nanomaterials including mechanical, electrical and magnetic properties [10–12]. Ion irradiation can also be used to shape materials down to the nanoscale [13–15]. In the field of nuclear energy, ion irradiation is used worldwide as a proxy to neutron irradiation for testing and qualifying nuclear materials [16–18].

Ion irradiation clearly represents a powerful tool in materials science because it allows driving the materials in out-of-equilibrium conditions. This process has a large number of advantages that span from the possibility to perfectly control the nature and the quantity (also called fluence, i.e. (ion)/ cm^2) of the ions, the flux and energy of the beam, to applicability to nearly all types of materials. However, it has its drawbacks, the main one being the quasi-systematic disordering of the perfect stacking of the lattice atoms because of the permanent displacement of these latter during the energy deposition process. Indeed, if the energy transferred to target atoms is larger than a threshold displacement energy, the primary knock-on atom is ejected, sometimes with a velocity sufficient to induce a subsequent collective displacements of target atoms; this phenomenon is referred to as a collision cascade [19]. After this collisional stage, an energy dissipation phase occurs, followed by a diffusional phase, and defect recombination may occur. At the end of this multi-step process, the target atoms may remain displaced, inducing a residual disorder. Increasing the irradiation fluence usually leads to defect clustering and formation of extended defects or even amorphous clusters [20]. As a consequence, the irradiation process can result in macroscopic changes of the material properties that include mechanical [21], thermal [22], and chemical properties (e.g., dissolution rate [23]), as well as frequent significant volume change [24, 25]. Therefore, it is of crucial importance to have a comprehensive understanding of the basic mechanisms underlying defect formation, accumulation and reorganization during ion irradiation. For this purpose, advanced tools for material characterization and modelling are required.

Investigating irradiation effects in materials has fueled a huge amount of experimental and computational studies over the last decades. Experimentally, transmission electron microscopy (TEM) is an invaluable tool for direct defect imaging. Techniques such as Raman spectroscopy, positron annihilation spectroscopy, Rutherford backscattering spectrometry in channeling mode (RBS/C), and X-ray diffraction (XRD) are widely used to evaluate the disorder level in irradiated materials (see ref. [26] and references therein). Most of the time, they rely on a phenomenological approach where disorder is quantified through a simple parameter such as the weakening of the Raman lines, the fraction of positron annihilations

with core or shell electrons, the backscattering yield in RBS/C, or the intensity attenuation in XRD. Simulation methods for modelling irradiation effects encompass a vast range of time and length scales, from the femtoseconds to centuries, from the atomic level to macroscopic dimensions (see refs. [27, 28] for reviews). Most widely used methods are molecular dynamics (MD) for the study of primary defects, kinetic Monte-Carlo (KMC) that addresses the defect migration, dislocation dynamics to handle complex extended defects, and finite element modelling (FEM) for predicting the elastoplastic response of large systems. Note that these techniques can be parameterized using quantum-mechanical calculations. Ideally, experiments and simulations are intertwined, which allows validating computational techniques and interpreting experimental data. Another step towards an integrated experimental and computational approach lies in the generation of experimental-like signals using computational data as input data. This approach provides an efficient way to establish direct connections between actual defective structures (hardly accessible by experiments) and phenomenological parameters (derived from experiments).

In the present paper, we propose such an integrated approach. MD defective cells, used to mimic irradiated materials, serve as input data to dedicated codes to produce RBS/C and XRD signals. Uranium dioxide, UO_2 , has been chosen as a test-case material, as it is the most widely used nuclear fuel worldwide and has thus received a considerable attention during the past 50 decades. A recent review of irradiation effects in UO_2 can be found in, e.g., ref. [29]. The well documented behavior of this material under irradiation, as well as the substantial quantity of corresponding data (including our own data), were two major reasons to select this material to implement our integrated approach. We show here that RBS/C and XRD signals can be generated from a same set of MD data and used to compare the computed results with experimental characterizations.

2 Simulation and analysis methods

2.1 MD simulations and defect analysis methods

Radiation damage was reproduced with the Frenkel pair (FP) accumulation method which has the advantage of bypassing the collision cascade stage and directly simulates the evolution of defects by continuously introducing FP or by reaching a final concentration of FP at once, resulting in considerably shorter computing times [30, 31]. It has proven efficient to study the complete disordering processes in Ni and Ni-based alloys [32], in UO_2 [33], but also the amorphization processes in lanthanum pyrozoirconate [30] and SiC [34], and the complex defects in irradiated Fe [35].

The cells used in the MD simulations have a cubic shape. The side length of a pristine one is 21.6 nm. Each cell contains 768000 atoms. The z direction of the MD cell is along the [001] direction of a UO_2 unit-cell. The nominal disorder of the cell is defined as the displacements (of uranium atom) per uranium atom (dpU, similar to the displacements per target atoms (dpa) but referring only to uranium atoms) which ranges here from 0.01 to 7.85. More details about the MD simulations can be found in ref. [33]. The conversion of

dpa to dpU can be calculated as follows:

$$dpU = dpa \frac{N_t}{N_U} \frac{d_U}{d_t} \quad (1)$$

in which N_t is the total target atom number, N_U is the total Uranium atom number, d_t is the displacements of total atoms at a certain position and d_U is the displacements of Uranium atoms at the same position. According to SRIM Full-Cascade calculations [36], the displacement threshold energies, E_d , for U and for O can significantly affect the ratio of d_U over d_t . When $E_d(U)$ equals to 40 eV and $E_d(O)$ equals to 20 eV [37], for experimental data used at Section 3 (20 keV He ions, 500 keV La ions and 500 keV Ce on UO_2), the ratios of d_U over d_t are similar, which are around 0.253 at the position of maximum damage. So 1 dpa is equivalent to 0.760 dpU at that position.

We must highlight that there is a true difference between, on the one hand, the dpU level obtained in the current MD cells produced by the FP accumulation method (MD-dpU) and, on the other hand, the dpU level derived from the SRIM Full-Cascade calculations (SRIM-dpU) which we performed in the framework of the irradiation experiments. It is known that SRIM simulations (using the Kinchin-Pease model or the Full-Cascade option, see ref.[38]) overestimate the actual number of stable defects. Indeed, they rather provide the total number of displaced atoms without considering any physical mechanism for a potential recombination, as it occurs, based on MD simulations, during the thermal spike phase of collision cascades [39]. In addition, all the FPs introduced in the MD cells, in the current work, do contribute to defect evolutions, whereas even part of the stable defects surviving at the end of the collision cascade may further recombine or annihilate due to thermal migration. Hence, we cannot compare directly MD-dpU and SRIM-dpU levels, and we can expect onsets of defect changes to take place at MD-dpU lower than SRIM-dpU. These remarks will be used in the following to explain the difference between computed and experimental strain and disordering kinetics.

The OVITO code [40] was used to visualize and analyze the MD cells. Concentrations of point defects, namely interstitials (I) and vacancies (V), were derived from a Voronoi analysis method [41]. Dislocation types and densities were determined by the dislocation analysis (DXA) method [42, 43]. Fig.1(a) presents the visualization of dislocations in damaged MD cells, in which $1/3\langle 111 \rangle$ Frank dislocations (blue) are clearly in the form of loops, whereas it is difficult to distinguish $1/2\langle 110 \rangle$ perfect loops and lines (green).

2.2 RBS/C simulations and analysis

RBS/C simulations were performed with a recently developed Monte-Carlo code called RBSADEC which stands for Rutherford Backscattering Simulation in Arbitrary Defective Crystals [44]. This code was subsequently improved by us in order to extend its applicability to more simulation conditions [45]. The code is based on the Binary Collision Approximation (BCA) and can simulate RBS/C spectra from targets containing arbitrary atomic structures. The trajectories of probing ions are determined by a search-and-collide process taking into account actual target crystalline structures [46], while an algorithm describing the interaction between ions and amorphous targets is used to calculate the trajectories of backscattered ions in order to accelerate the simulations.

For the current simulations, the probing ion was defined as a 3.085 MeV He ion (corresponding to most available experiments). The detector energy resolution was fixed at 15 keV. The one-dimensional root mean square (rms) thermal vibration magnitudes for U and O atoms were set to 6.5 pm and 9 pm respectively [47]. For each simulation, periodic boundary conditions were applied to the x and y directions of the MD cells, while the projectile entered the target along the z direction. Thus, the simulated target can be regarded as a thin layer with a 22 nm thickness. Three sets of simulations were performed. For each set, before applying the periodic boundary conditions, the cells were rotated in order to have the z direction along, alternatively, the [001], [010] and [100] directions. The purpose was to detect a potential anisotropy of material response to defect formation. In addition, a simulation in a random configuration was also performed for each cell in order to have the maximum backscattering yield as a normalization criterion. Considering that the total number of the cells was high (897 cells), a TRIM-based amorphous slowdown approach was used, which allowed a quicker calculation in RBSADEC, see ref. [?] for more details.

Fig.1(b) depicts several examples of RBS/C spectra generated with RBSADEC using MD cells of different dpU levels. Blue lines represent the RBS/C spectra of 3.085 MeV He ions on UO_2 in a random configuration, and orange lines represent the RBS/C spectra along the $\langle 001 \rangle$ aligned direction. Unlike usual experimental spectra measured for bulk targets, the spectra in Fig.1(b) are peak-shaped, since the target thickness is very small (~ 22 nm). In this case, it is reasonable to assume that, essentially, direct scattering events contribute to the yield, and the dechanneling component can be neglected. This assumption facilitates the determination of the (RBS/C) disorder fraction, f_d , in each of the MD cells, which can be calculated as follows:

$$f_d = \frac{y_a - y_p}{y_r - y_p} \quad (2)$$

in which y_r represents the total yield of a random spectrum, y_a represents the total yield of an aligned spectrum for a defective cell, and y_p represents the total yield of an aligned spectrum generated from a pristine sample.

2.3 XRD simulations and analysis

Similar to the RBS/C simulations, the MD cells were used to generate XRD signals and the three [001], [010] and [100] directions have been considered. For each orientation, two sets of calculations have been performed with the x direction of the MD cell parallel to two different directions of the unit-cell, and the corresponding strain and disorder were averaged. For instance, for a [001] orientation of UO_2 , the [100] and [010] directions are successively set parallel to the x direction. For each data set, the three-dimensional (3D) amplitude distribution, A , was calculated in the vicinity of the 004 Bragg reflection using the following equation [48]:

$$A = \sum_j f_j(\mathbf{S}) \exp(2\pi i \mathbf{S} \cdot \mathbf{r}_j) \quad (3)$$

where \mathbf{S} is the scattering vector, f_j is the atomic scattering factor of atom j , \mathbf{r}_j is the position of atom j . Since in the disordered cell the atoms are not regularly distributed on a 3D lattice, fast Fourier transform algorithms can not be used. Instead we used a direct

summation approach accelerated by the use of a general purpose graphical processing unit (GPU).

The 3D amplitude distribution is converted to a 2D intensity distribution (i.e., a Reciprocal Space Map, RSM) with [49]:

$$I(S_x, S_z) = \int dS_y \cdot A(\mathbf{S})A^*(\mathbf{S}) \quad (4)$$

where the S_i represents the component of \mathbf{S} along the direction indicated by the subscript i . Complete details concerning this approach will be given in a separate article. For the sake of the present article, it is sufficient to mention that this approach allows to derive the lattice strain and the disorder parameter (the Debye-Waller (DW) factor) for all orientations of the MD cells. Examples of 004 RSMs of UO_2 MD cells for increasing damage levels are given in Fig.1(c). These RSMs display the 2D intensity distribution in a (H, L) reference frame where H and L are the coordinates of the scattering vector [50]:

$$\mathbf{S}(H, K, L) = H\mathbf{a}^* + K\mathbf{b}^* + L\mathbf{c}^* \quad (5)$$

where \mathbf{a}^* , \mathbf{b}^* and \mathbf{c}^* are the reciprocal space basis vectors.

The inspection of Fig.1(c) reveals several features. The RSM from the pristine cell correspond to the theoretical signals of a perfect crystal, i.e., a 2D Laue function. For increasing fluence, we observe both a shift of reciprocal lattice point towards lower L values, and a spread of the intensity out of the specular row (characterized by $H = 0$). The former is indicative of the development of tensile strain, e , within the MD cell, which can be directly quantified through [50]:

$$e = \frac{L_0 - L}{L_0} \quad (6)$$

where L_0 is the L value of the Bragg peak in a pristine sample (here $L_0 = 4$). The weakening of the specular intensity is quantified by the DW factor and can be estimated from the RSMs via:

$$DW = \sqrt{\frac{I^{H_{max}}}{I_0^{H_{max}}}} \quad (7)$$

in which $I^{H_{max}}$ is the intensity integrated along the row $H = H_{max}$ where the spot of the maximum intensity is located, and the subscripts 0 refers to the pristine material for which $H_{max} = 0$. The disorder fraction obtained from the XRD simulations is defined as $1 - DW$.

3 Results

3.1 Defect evolution sequence

Let us first consider the defect evolution obtained by a direct analysis of the MD cells in which radiation damage was mimicked by the Frenkel pair (FP) accumulation method. Fig.2(a) gives the point defect concentration and Fig.2(b) gives the dislocation densities expressed in m^{-2} (which corresponds to the total dislocation length of a given type, divided by the cell volume) as a function of irradiation dose - dpU.

The defect evolution follows a sequence that has been previously identified, and, overall, confirmed by TEM analysis [33]. The sequence can be decomposed as follows. Below 0.09 dpU, point defects are predominant, and the dislocation density is very low. From 0.09 dpU, $1/3\langle 111 \rangle$ Frank dislocation loops form and constitute the main defect type up to 0.25 dpU. Formation of these dislocation loops is accompanied with a decrease in the interstitial concentration, which strongly suggests that the loops are of interstitial type. At around 0.12 dpU, $1/6\langle 112 \rangle$ Shockley partial dislocations are detected, but they rapidly react with Frank loops to form $1/2\langle 110 \rangle$ perfect dislocations [51]. These latter initially form as loops, but gradually coalesce and transform into lines. Note that, unlike Frank loops which are easily distinguishable among other defects, perfect loops and lines can be hardly separated. Above 1 dpU, $1/2\langle 110 \rangle$ perfect dislocation lines are predominant over the other types of dislocations. At the same time, the point defect concentration reaches a steady state, with vacancies found in a much larger concentration than interstitials. These results indicate that at this stage, interstitial point defects are efficiently trapped at dislocation lines. This general sequence of defect evolution is in accordance with recent combined experimental and computational results [33, 52–54]. A question that now arises is how this sequence of transformations affect the XRD and RBS/C signals, and what can we learn from the latter?

3.2 Disorder kinetics

In order to compare the results of the simulations of the two techniques, we first plotted disordering kinetics using the disorder parameters obtained by XRD and RBS/C. Fig.3(a) shows the disorder obtained from XRD, while Fig.3(b) shows that derived from RBS/C; results along the [001], [010] and [100] directions of the UO_2 unit-cell are presented. In inset of the figures, the abscissa is in linear scale. The two disordering kinetics exhibit a very similar shape, which means that the two techniques could be used interchangeably to monitor the disordering process in irradiated materials. From a practical standpoint, this is an important result because, although RBS/C is to date more popular to evaluate the disorder in irradiated materials, XRD is more easily accessible and this could facilitate the characterization.

Specificities of the techniques in terms of defect sensitivity are given in the following. The absolute values of disorder obtained by XRD and RBS/C differ; this is expected as both techniques rely on very different physical phenomena, namely the interference of scattered X-rays on the one hand and the backscattering of energetic ions on the other hand. Moreover, the disorder measured by XRD is dependent on the considered HKL reflection since the Debye-Waller factor, which is used to quantify the disorder [55], is a function of the scattering vector $\mathbf{S}(\mathbf{H}, \mathbf{K}, \mathbf{L})$, while the backscattering yield changes with the probing ion energy.

Nonetheless, the relative evolution of both disorders remains perfectly comparable. Both kinetics show common features that can be related to the stages of the sequence of defect evolution above-described (a quantitative support for this correlation is given in the Discussion part). First, the disorder grows at a relatively low rate with increasing dpU when, principally, point defects are present. Then, when dislocation loops form, the disordering rate considerably increases and the disorder reaches a maximum value at around 0.4 dpU. Finally, after this maximum, the disorder starts to decrease (at least with the current evalua-

tion tools), which can be related to the presence of, essentially, dislocation lines surrounding defect-depleted regions.

It should be noted that at high dpU, for both techniques, the disorder in the different directions start to diverge and exhibit seemingly random fluctuations. Presumably, these features could be due to the so-called polygonization process, in which dislocations pile-up and lead to the formation of sub-crystallites with slightly different orientations [56, 57]. Such resulting boundaries can act as efficient defect sinks. An in-depth analysis of the MD cells (not shown here) indeed indicates that, depending on the orientation of the cell, 2 to 3 rotated sub-crystallites co-exist within the MD cells, i.e., at high fluences the structure of the cells differs depending on the direction. It can be expected that in larger cells, such divergence would statistically disappear. A detailed investigation of that point will be given in a forthcoming paper.

Fig.3(c) presents the disordering kinetics obtained from RBS/C experiments on UO_2 irradiated with 500 keV La ions at room temperature (see the supplemental material in ref. [58]). The displacements per target atoms (dpa) obtained from SRIM Full Damage cascade (FD) calculations [36] were converted into dpU. Qualitatively, the curve from the RBS/C simulations and the experimental one exhibit very similar trends, and even the apparent decrease in disorder at high dpU is reproduced.

Quantitatively, there are some differences we address hereafter. Compared with the simulation results, the maximum disorder in the experiment is almost 4 times lower. As explained in ref. [33], this is because the dislocation density in the MD simulations is much higher than that in the experiments due to a very high damage rate, K_0 , in the simulations. According to SRIM calculations, the experimental dose rate is around 3×10^{-3} dpU/s at the damage peak, while it is 1.5625×10^9 dpU/s for the MD simulations. Assuming that the dislocation density is proportional to $K_0^{1/6}$ [59], the dislocation density in the MD cells is thus around 100 times higher than that in the real samples.

Another difference is that it takes around 20 times more dpU to reach the maximum level in the experiments. The first reason for this is, obviously, the higher defect densities resulting from the higher damage rate in the simulations. Thus, defect transformations can occur earlier in the MD cells. The second reason is due to the very definition of SRIM-dpU and MD-dpU as mentioned in Sec.2.1. The former corresponds to displaced atoms calculated in SRIM, whereas the latter is related to the actual number of defects introduced in the MD cells, which fully contribute to the evolution of defects. It is known that the SRIM results tend to overestimate the actual defect numbers, i.e., the remaining displacements after potential recombination [60, 61].

Nonetheless, and above all, it is important to emphasize that the computed and experimental disordering kinetics agree qualitatively, which represents a notable result because it demonstrates the relevance of our procedure and in the same time, it provides a support to previous interpretations of experimental data that were based on phenomenological descriptions. Furthermore, considering the good agreement between the computed RBS/C and XRD data, we can conclude that the whole integrated approach is valid. A very similar disordering kinetics has been observed in other materials including cubic yttria-stabilized

zirconia (YSZ) [62, 63], MgO [64], Ni [65] and Ni-based equiatomic binary alloys [66]. One common feature of these materials is that either the entire crystal or the cationic sub-lattice has a face-centered-cubic (FCC) structure, indicating the possibility of having similar defect evolutions (as already partly shown). Therefore, the present qualitative description of the defect transformation sequence should hold for these materials as well, and this conclusion can be based on experimental data only (there is no need to perform MD calculations).

3.3 Elastic strain kinetics

In addition to disorder, XRD permits the determination of the elastic strain, which can be considered as another quantity to monitor the radiation damage. Fig.4(a) shows the irradiation-induced elastic strain kinetics derived from the XRD simulations using MD cells as input data. As for RBS/C, the [001], [010] and [100] directions were studied. Similar to the disorder, the strain kinetics displays distinct features that can be ascribed to a given type of defects (a quantitative support for this correlation is given in the Discussion part as well). When point defects are dominant, the elastic strain buildup is fast. When dislocation loops dominate, the strain keeps on increasing (with a slightly lower rate), to reach a maximum of 1.9 % at around 0.28 dpU. From this point, the strain is partially relieved, which can essentially be related to perfect dislocations being the dominant defects. A slightly anisotropic evolution is observed in the three crystallographic directions, similarly to what is observed in the disordering kinetics. It is also worth noting that the maximum of the elastic strain is reached at a lower dpU value as compared to that of the disorder (0.28 instead of 0.4 dpU); we will comment this difference hereafter.

Fig.4(b) and Fig.4(c) show the elastic strain kinetics from UO_2 irradiated with 20 keV He ions and 500 keV Ce ions, respectively. As for the disorder addressed earlier (with La ions, which are equivalent to Ce), the computed strain kinetics exhibit a qualitative agreement with the experiments. Due to the very high dislocation density in the MD cells, the maximum strain computed from the simulations is around 3 to 4 times higher than that in the experiments. Regarding the delay in reaching the maximum level, since Ce and La are similar in terms of mass and solubility in UO_2 , a same explanation as for the disordering kinetics holds for the strain. In contrast, the strain kinetics from 20 keV He irradiations is shifted towards higher dpU values by only a factor of 6 (instead of 20 for the disorder). As shown in ref. [61], the discrepancy between BCA models and MD calculations intensifies with increasing the primary knock-on atoms (PKA) energy, with much less surviving defects in MD (than for BCA) at high energy. In the current case, the median PKA energy of 500 keV Ce ions is obviously larger than that of 20 keV He ions. Therefore, it is expected that the difference between SRIM-dpU and MD-dpU is smaller for He than for Ce irradiations, explaining why the delay is reduced for the He irradiation experiment.

4 Discussion

From the previous section, it can be concluded that strain and disorder are remarkably correlated with the defect densities derived from the quantitative defect analysis of the MD cells. On the one hand, strain develops as soon as point defects are formed, and keeps increasing when interstitial defects agglomerate into Frank dislocation loops. When the

concentration of Frank loops decreases, the strain decreases as well. On the other hand, disorder is more related to the presence of dislocations than point defects. To go beyond these simple qualitative observations, we propose hereafter to decompose the computed strain and disordering kinetics into components associated with the concentration of each type of defects. We averaged the results obtained along the three main directions to smooth out the observed fluctuations.

Let us start with the strain. The elastic strain kinetics is fitted assuming a linear relationship between the defect concentration or density and the induced strain. Note however that this assumption is valid only if interactions between elastic strain fields are limited, which might not be entirely justified for high defect concentrations, but which yet proves to be reasonable considering the results presented below. For point defects, the elastic strain is proportional to their so-called relaxation volume [54, 67, 68]. For dislocation loops, not only is it affected by the loop density, but it is also dependent on the size of the loops [69, 70]. However, the characteristic features of the dislocation loops are not completely known in the current work in terms of size, geometry, etc., because they are often significantly entangled. Moreover, as stated earlier, there is no simple way to detect the loop character of a dislocation in an automated way. We therefore rely on the Burgers vector and visualization of dislocations to determine the loop character: $1/3\langle 111 \rangle$ are (Frank) loops, but for perfect dislocations $1/2\langle 110 \rangle$, as stated above, we are unable to distinguish between loops and lines. Henceforth, for the sake of simplicity, we assumed that the elastic strain induced by dislocations is simply proportional to their density. Finally, the total elastic strain, ε_{def} , reads:

$$\varepsilon_{def} = \frac{1}{3} [C_V \frac{V_V^{rel}}{\Omega} + C_I \frac{V_I^{rel}}{\Omega} + (S_F \rho_F + S_p \rho_p)] \quad (8)$$

where C_V and C_I are concentrations of vacancies and interstitials, respectively, V_V^{rel} and V_I^{rel} are the relaxation volumes expressed in atomic volume unit Ω , ρ_F is the density of the Frank loops and ρ_p is the density of perfect dislocations; the terms S_F and S_p , which have the dimension of a surface, are the proportionality factors between concentration of Frank loops and perfect dislocations, and the corresponding strain, respectively.

It should be noticed that the sign of the relaxation volume of U vacancy-type defects is still the object of debate in the literature [71, 72]. In the present study, we performed a pressure relaxation (MD) simulation to have direct access to this value. We obtained an average 0.6Ω value for V_V^{rel} , where the average assumes an equiprobable distribution of single U vacancies, U divacancies and Schottky defects ($2U+O$). We therefore performed fittings imposing a positive sign for V_V^{rel} . The fitting of the strain kinetics with Eq.8, shown in Fig.5, was performed using a non-linear least squares optimization algorithm by minimizing the root-mean-square deviations (RMSD). Overall, the elastic strain kinetics is well fitted using Eq.8, demonstrating that the elastic strain determined from the MD simulations can be straightforwardly connected to the defect densities. Table I reports the values of the fitting parameters of Eq.8. It can be noticed that the value of V_V^{rel} was kept free during the fitting in order to allow for deviations from the simple equiprobable defect averaging.

S_F is found to be 75 \AA^2 while S_p is 10 \AA^2 . These values demonstrate that the contribution of Frank loops to the overall strain level is around 8 times larger than that of perfect loops.

This finding was expected since Frank loops, in contrast to perfect loops, have a non-vanishing average Burgers vector of $1/3\langle 111 \rangle$. This difference implies that, while Frank loops essentially generate homogeneous (elastic) strain, perfect loops principally produce local (i.e., heterogeneous) strain. The same reasoning holds for perfect lines, where a random spatial distribution of dislocations or their arrangement into dipoles yield a vanishing average Burgers vector. Therefore, because of their limited contribution to the overall strain level, the inability to distinguish perfect dislocation loops from perfect dislocation lines does not have any measurable consequence. We show below that the situation is far different for the disorder.

Let us now consider the disorder, both derived from XRD and RBS/C. In a first step, similarly to what was done for the elastic strain, we assumed a linear relationship between defect densities and the induced disorder. Contrarily to the strain, vacancies do not contribute significantly to the disorder; their role was therefore neglected in the following. Fig.6 presents the corresponding fitting of the RBS/C disordering kinetics averaged over the three directions. It can be readily observed that this model provides a good description of the disordering process up to 0.4 dpU, which corresponds to the fluence at which the density of perfect dislocations reaches a maximum. Above 0.4 dpU, the model fails to describe the disorder, the most likely reason being that perfect loops and lines contribute significantly, but differently, to disorder, as opposed to their contribution to the strain. Being able to distinguish between perfect dislocation loops and lines is therefore crucial to get an accurate, quantitative description of the disordering process.

One solution to cope with this problem lies in the introduction of an *ad hoc* perfect line density, ρ_p^{line} , as a parameter that can be fitted and from which the perfect loop density, ρ_p^{loop} , can be derived, following the relationship: as $\rho_p^{loop} = \rho_p - \rho_p^{line}$. Based on the fit presented in Fig.6, we can safely assume that ρ_p^{line} is not significant until around 0.4 dpU, i.e. where the fit quality deteriorates, and ρ_p^{line} reaches a saturation level in the final line stage. This qualitative description of ρ_p^{line} indicates that the shape of the corresponding disorder component should feature a high incubation time most likely followed by a sigmoidal growth spanning from 0.4 to 1.5 dpU range, and a height determined by the final dislocation density, i.e. $0.26 \times 10^{17} m^{-2}$. The total disorder, f_d , can finally be represented by:

$$f_d = r_I C_I + r_F \rho_F + r_p^{loop} \rho_p^{loop} + r_p^{line} \rho_p^{line} \quad (9)$$

where r_I is the disorder constant for the interstitials, and r_F , r_p^{loop} and r_p^{line} are the disorder constants for the Frank loops, perfect loops and perfect lines, respectively, with a m^2 unit.

Fig.7 shows the fits of the disordering kinetics obtained from (a) RBS/C and (b) XRD simulations using Eq.9. By comparing Fig.6 and Fig.7 (a), we observe that the quality of the fit in the high dpU region (> 0.4 dpU) is significantly improved after separating the contributions of perfect loops and lines. The decrease in disorder observed after 0.4 dpU can therefore be ascribed to the reduction of the loop density at the expense of the perfect lines. The disorder constants are given in Table II. A feature worth putting forward from these constants is the different sensitivity of the two techniques, in terms of estimated disorder, to the nature of the dislocation loops. While RBS/C is more sensitive to perfect loops, with a r_F/r_{loop}^p ratio of 0.8, the XRD phenomenon is more affected by Frank loops, with a

corresponding ratio of 1.4. The reason for this difference is not entirely clear. We can note however that none of the RBS/C-derived and XRD-derived disorder values used here are absolute. As briefly above-mentioned, it is known that the backscattering yield depends on the probing-ion energy, and this dependence varies with the defect nature. Similarly, the Debye-Waller factor in XRD is a complex function of the scattering vector Q , and defects of different nature exhibit specific Q dependencies. A careful inspection of both disorder parameters may hence allow to get very detailed and complementary information about the nature of the defects present in the MD cells but also in actual samples.

Examination of the constants in Table II provides another important result: dislocation lines have the largest influence on the disorder, as compared to the other defects, including perfect dislocation loops. This finding illustrates the complementarity between strain and disorder for the evaluation of the level of damage in irradiated materials. Indeed, because of the very nature of these two types of defects, namely perfect dislocation loops and lines, their effect on the disorder and on the strain is different. Dislocation loops are quasi 0-dimensional defects, so their strain fields have a finite spatial extension and the long-range order (LRO) of the crystal is weakly affected [73]. On the contrary, dislocation lines are 1-dimensional defects with a diverging $\ln(r)$ term in the displacement field that significantly alters the LRO of the crystal. The fact the strain kinetic reaches its maximum earlier (in terms of dpU) than the disorder can be entirely explained by this different sensitivity to the defect type. As a final comment, it is worth mentioning that the number of damage metrics, two in the current work, namely the strain and the disorder, defines the number of defect transformations that can be studied. If there were an additional type of defect, say stacking faults or precipitates, then another metric would be needed to monitor the defect evolution with time. In the present case, we limited the use of XRD data to the intensity and the strain. However, additional parameters, such as the reflection broadening also conveys information regarding the defect structure. This will be the topic of a forthcoming paper. Another solution to deal with a higher number of defect types would be to implement additional techniques, such as Raman [74] or positron annihilation spectroscopy [75] for which it is possible to generate computed signals.

5 Conclusions

Summarizing, we generated experimental-like signals of RBS/C and XRD techniques using the same MD dataset produced with the Frenkel pair accumulation method. We then computed disordering kinetics, with disorder and strain parameters to monitor the damage accumulating in the MD cells. We demonstrated that, on the one hand, both techniques can be used interchangeably to quantify the disorder in defective cells and in actual materials. On the other hand, because they have a different sensitivity on the probed defects, their combination can provide complementary information about the defect nature. Despite discrepancies in terms of absolute values of fluence range and levels of strain and disorder, on a relative scale, the computed strain and disordering kinetics agree well with those determined from actual experiments, which demonstrates the validity of the integrated approach. Additional work is in progress with other materials to provide further support and improve the methodology. Nonetheless, the results provided in this paper can be transposed to materials exhibiting the same disordering behaviour.

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Competing interests

The authors declare no conflict of interest.

Figures

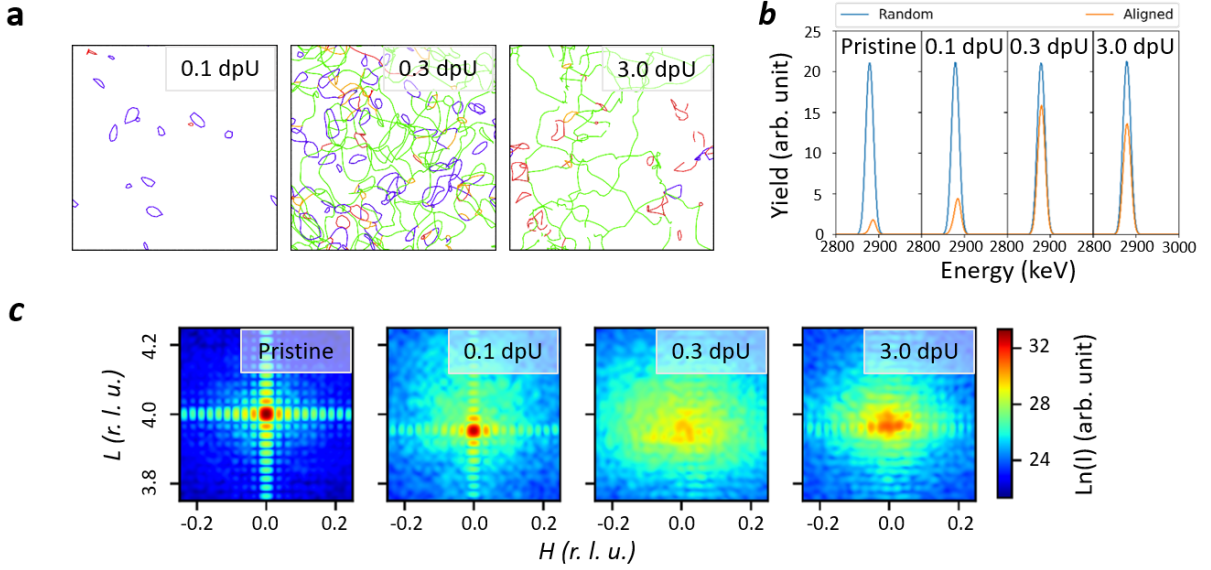


Figure 1: Characteristic microstructures obtained by MD simulations and corresponding RBS/C and XRD signals generated from the UO_2 MD cells. **a** Snapshots of UO_2 MD cells analyzed by the DXA method with different damage levels: 0.1 dpU, 0.3 dpU and 3.0 dpU. Only dislocations including Frank loops (blue), perfect dislocations (green) and Shockley partial dislocations (orange) in the cells are visualized. (Other types of dislocations including stair-rod dislocations and ill-defined dislocations are represented by red lines.) **b** RBS/C spectra of 3.085 MeV He on the [001]-oriented UO_2 MD cells presented in **a**. Blue lines represent random spectra, and orange lines represent aligned spectra. **c** RSMs calculated in the vicinity of the [004] Bragg reflection of the UO_2 MD cells presented in **a**. Units of H and L are reciprocal lattice units (r.l.u) along the x and z directions, respectively. Intensities indicated by the color bar are represented on a logarithmic scale.

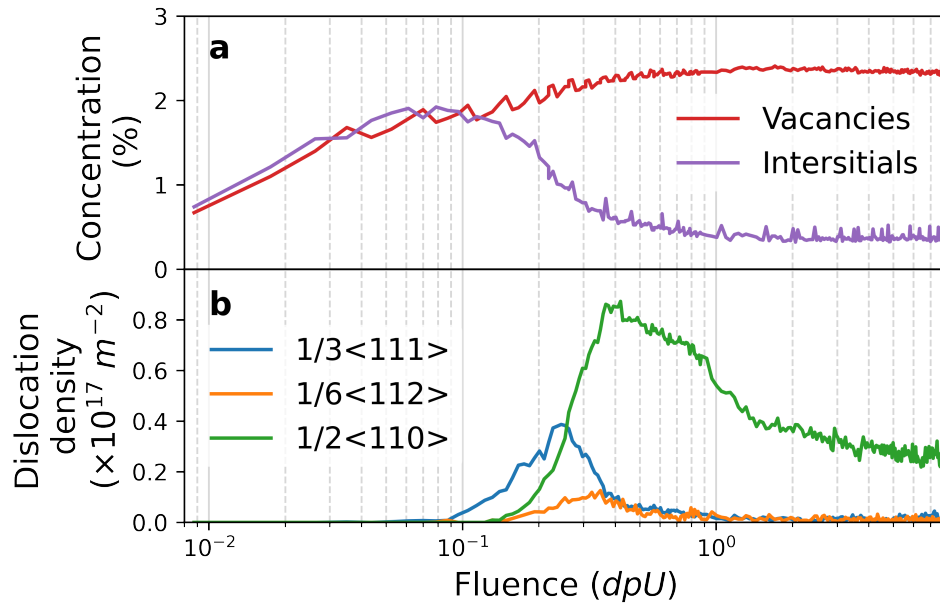


Figure 2: Defect quantities as a function of fluence (dpU). **a** Concentrations of vacancies and of interstitials, **b** Densities of $1/3\langle 111 \rangle$ Frank loops, of $1/6\langle 112 \rangle$ Shockley partial dislocations and of $1/2\langle 110 \rangle$ perfect dislocations.

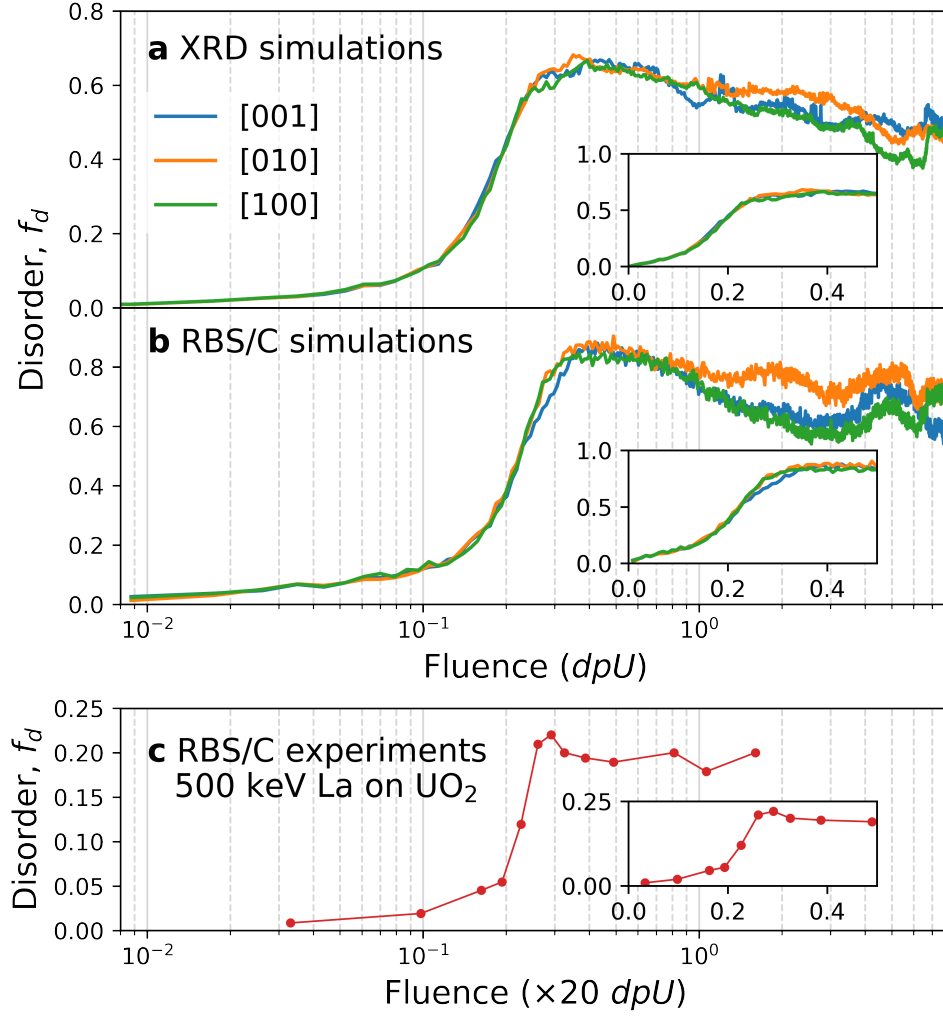


Figure 3: Disorder kinetics obtained from: **a** The XRD simulations on the UO_2 MD cells, **b** the RBS/C simulations on the UO_2 MD cells, **c** RBS/C experiments on UO_2 crystals irradiated with 500 keV La ions. In the simulations, the MD cells were characterized along three major directions: [001] (blue lines), [010] (orange lines) and [100] (green lines). Insets show part of the kinetics using a linear scale for the x axis.

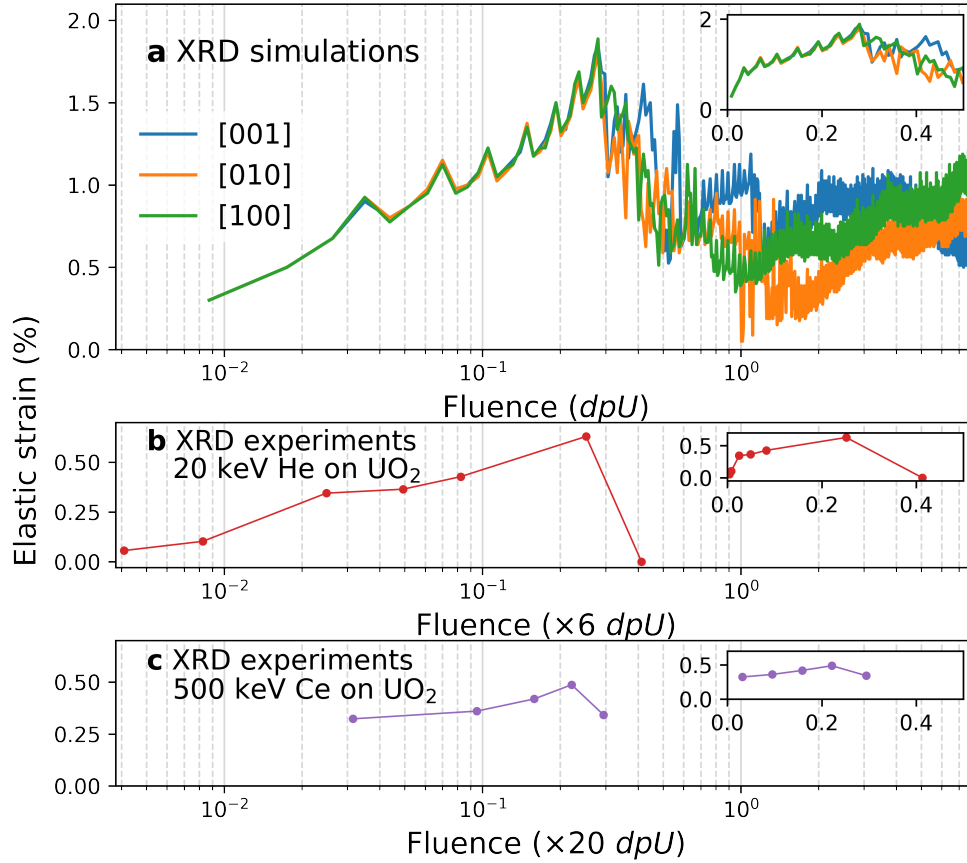


Figure 4: Elastic strain kinetics obtained from: **a** The XRD simulations on the UO_2 MD cells, **b** XRD experiments of 20 keV He on UO_2 crystals, **c** XRD experiments of 500 keV Ce on UO_2 samples. In the simulations, the MD cells were characterized along three major directions: [001] (blue lines), [010] (orange lines) and [100] (green lines). Samples in experiments were characterized along $\langle 001 \rangle$ directions. Insets show part of the kinetics using a linear scale for the x axis.

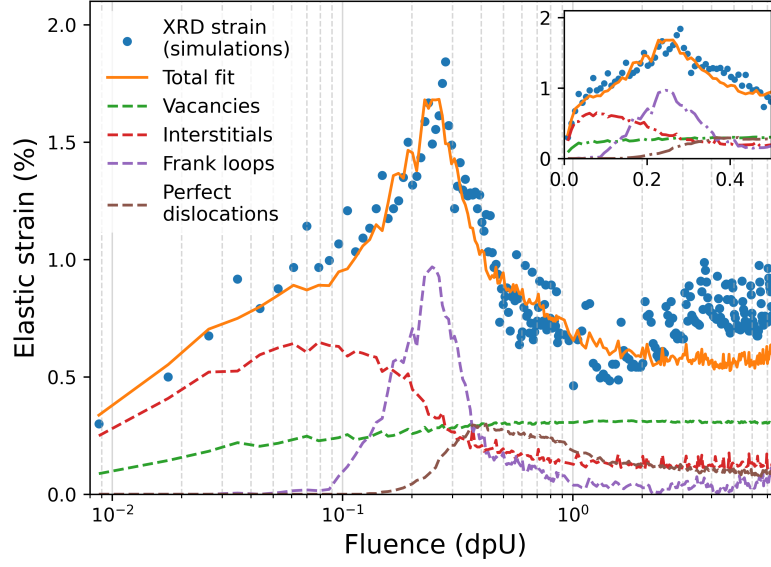


Figure 5: Fit of the elastic strain kinetics. The blue dots represent the elastic strain computed from the XRD simulations and averaged over the three $\langle 001 \rangle$ directions. The solid line represents the total fit by combining contributions of the different defects (dashed lines). The RMSD value equals to 1.7×10^{-1} . The inset shows part of the kinetics using a linear scale for the x axis. (In order to avoid a dense overlap, only one value in every five simulation results is shown when the fluence is larger than 1.0 dpU.)

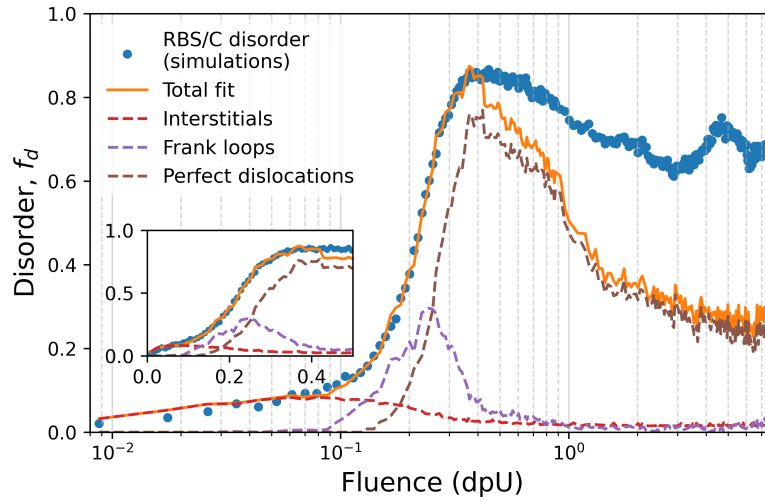


Figure 6: Fit of the disordering kinetics assuming proportionality between defect quantities and the induced disorder. The blue dots represent the disorder computed from the RBS/C simulations and averaged over the three $\langle 001 \rangle$ directions. The solid line represents the total fit by combining the contributions of the different defects (dashed lines). The inset shows part of the kinetics using a linear scale for the x axis. (In order to avoid a dense overlap, only one value in every five simulation results is shown when the fluence is larger than 1.0 dpU.)

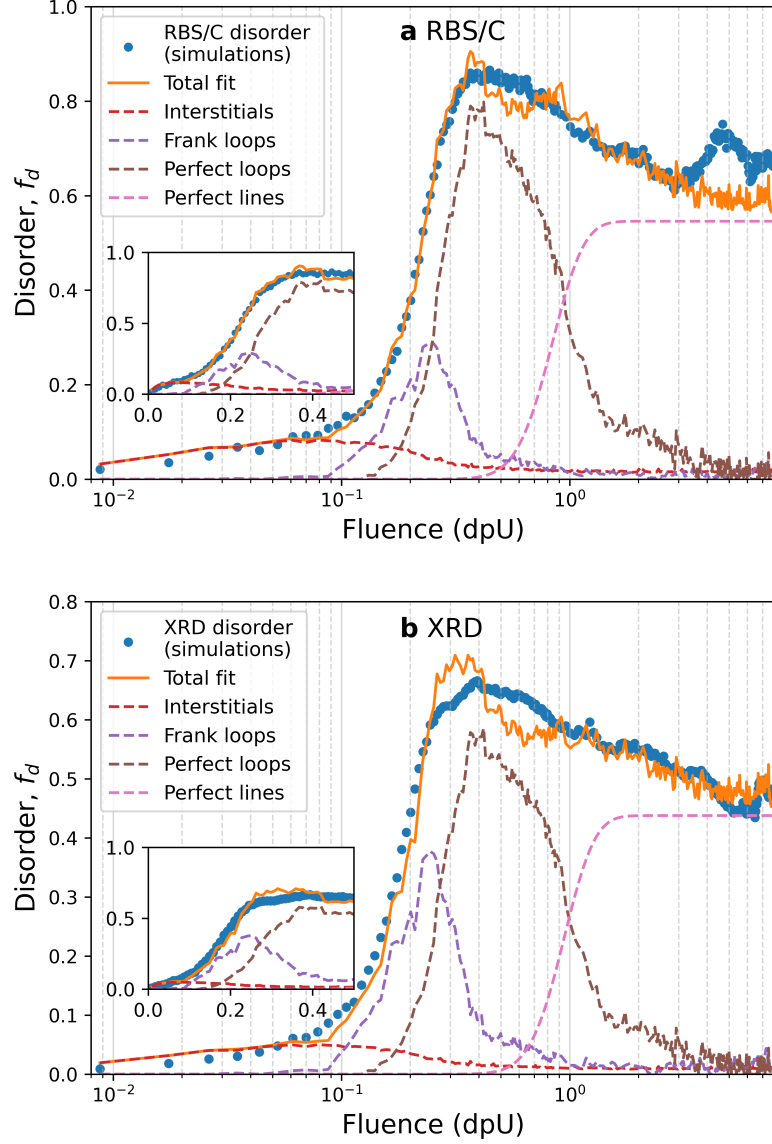


Figure 7: Fits of the disordering kinetics assuming proportionality between defect quantities and the induced disorder and separating the perfect loop and line contributions. The blue dots represent the averaged disorder computed from **a** RBS/C simulations ($\text{RMSD} = 6.5 \times 10^{-2}$) and **b** XRD simulations ($\text{RMSD} = 3.2 \times 10^{-2}$). Insets show part of the kinetics using a linear scale for the x axis. (In order to avoid dense overlap, only one value in every five simulation results is shown when the fluence is larger than 1.0 dpU.)

Tables

Table I: Relaxation volumes, V^{rel} , of point defects and strain constants, S , of dislocations. The errors are obtained from the non-linear least squares fitting algorithm.

$V_V^{rel} (\Omega)$	$V_I^{rel} (\Omega)$	$S_F (\text{\AA}^2)$	$S_p (\text{\AA}^2)$
0.4 ± 0.1	1.0 ± 0.1	75.1 ± 3.5	10.3 ± 2.4

Table II: Disorder constants, r , for defects used in the fits. **a RBS/C disordering kinetics, **b** XRD disordering kinetics.** The errors are obtained from the non-linear least squares fitting algorithm.

	r_I	$r_F (\times 10^{-17} m^2)$	$r_p^{loop} (\times 10^{-17} m^2)$	$r_p^{line} (\times 10^{-17} m^2)$
RBS/C	4.31 ± 0.96	0.75 ± 0.07	0.92 ± 0.02	2.10 ± 0.08
XRD	2.60 ± 0.47	0.97 ± 0.03	0.67 ± 0.08	1.71 ± 0.05

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