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## Undercooled Phase Behind the Glass Phase with Superheated Medium-Range Order above Glass Transition Temperature Robert F. Tournier<sup>\* (1)</sup>, Michael I. Ojovan <sup>(2,3)</sup>

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**Abstract**: Rapidly quenched glass formers are amorphous and transformed into glass phases by relaxing enthalpy during the first heating. Two liquids give rise, at first, to an intermediate Phase 3 below  $T_3 < T_g$  respecting the entropy constraints and then, the enthalpy increases towards that of the glass phase up to  $T_g$ . The negative activation energy shows that Phase 3 is hidden behind the glassy phase acting as an intermediate invasive phase during the second cooling. Phase 3 carries a medium-range order above  $T_g$  which can be superheated above the melting temperature up to  $T_{n+}$ . The two-liquid state model predicts the thermodynamic properties as well as the relaxation times from liquids 1 to 2. The configuron model is successfully applied to 54 glasses explaining the transitions by percolation and an 'ordered' fraction equal to the critical threshold  $\Phi_c = 0.15 \pm 0.01$  from  $T_g$  to  $T_{n+}$ .

## Introduction

Microscopically liquids are dynamically inhomogeneous media because there is always a tendency to form microscopic metastable ordered structures whose size and lifetime grow with decreasing temperature. Thus, a liquid is homogeneous and disordered at large time and spatial scales, however it can have a short- and medium-range order locally at distances of the size of metastable clusters and over the lifetime of metastable formations [1]. Typical examples of this ordering are tetrahedral structures in silica and icosahedral structures in metallic glasses [2,3]. Local ordering in liquids is confirmed by Fischer clusters, which are associated with long-wavelength density fluctuations and revealed in glassforming liquids and polymers [4]. Bakai has shown that density fluctuations have correlation lengths of up to 300 nm and proved to be fractal with the dimension D < 3 [5]. These fluctuations result from domain aggregation and their lifetime is close to the  $\alpha$  relaxation time. A tendency to ordering is also observed in liquids above the melting temperature (liquidus). An analysis of the atomic structure of melts of simple metals demonstrates that the dense part of the liquid in molecular-dynamic models represents branched chains of almost regular tetrahedra linked in pairs by faces. The resulting clusters are fractal with the dimension D = 2.6 [6]. These observations are in contradiction with the commonly accepted notions that the structure of a liquid above the liquidus temperature is completely disordered and has neither long-range nor middle-range order. However, experimental observations confirm the occurrence of local ordering in liquids [7-9]. For example, ordered structures possessing the effect of remembering the thermal evolution of the melt state were found above the liquidus in glass-forming melts of silicate systems [10].

A supercooled liquid undergoes a glass transition after reheating the quenched melt. The knowledge of the melt state after quenching from temperatures higher than the melting temperature  $T_m$  is important to understand the phase transformations occurring during heating. There are two main views in the literature. The melt may be frozen in an amorphous state after quenching in the absence of thermodynamic transition at the freezing temperature  $T_g$  or may undergo a true phase transition at  $T_g$  leading to a glass state of the melt. It is considered [11,12], in contradiction with many experiments, that a melt does not contain any intrinsic nucleus above  $T_m$  as shown by the classical nucleation equation. Consequently, melts are not highly superheated above  $T_m$  [8]. Medium-range order of melts

exists in glass-forming liquids heated above  $T_m$ , after cooling far below  $T_g$ , in contradiction with the classical nucleation equation [10,13-15]. This equation, when completed and applied to liquids 1 and 2, predicts the formation of stable superclusters and the existence of a melting temperature of liquid "order" at  $T = T_{n+}$  [16]. Superheating above  $T_{n+}$  melts this medium-range order induced after quenching giving rise to short-range order and individual superclusters only containing few atoms which disappear at much higher temperatures than  $T_{n+}$  [17]. Consequently, rapid quenching of the melt from  $T > T_{n+}$  or atom deposition on substrate cooled at low temperature leads to an amorphous instead of a glass state [18] due to an absence of superclusters acting as building bricks of the glass phase.

The glass phase is created by recovering enthalpy during reheating the amorphous state up to  $T_g$  [19-22]. A liquid medium-range order is maintained after heating from  $T_g$  to  $T_{n+}$  and disappears above  $T_{n+}$  [13,22]. The medium-range order may come back after cooling at a second temperature  $T_{n+} < T_m$ , symmetrical of the first  $T_{n+}$  regarding to  $T_m$  because the new superclusters grow around the residual nuclei surviving above  $T_{n+} > T_m$  [13,17]. Reheating a glass up to a temperature T respecting  $T_m < T < T_{n+}$  does not melt the medium-range order and directly leads by cooling to a glass phase characterized by an entropy higher than -S<sub>m</sub> the crystal entropy with the entropy origin fixed at  $T_m$ .

The amorphous state obtained after hyper-quenching does not respect the Kauzmann's entropy constraint [18-24]. Superclusters and the glass phase are built by reheating the amorphous liquid from a nucleation temperature  $T_{n-}$  far below  $T_g$  and up to a second homogeneous nucleation temperature  $T_{n-}$  =  $T_g$  with formation of a new phase called Phase 3 respecting the Kauzmann constraints [13,16]. The thermodynamic parameters of this new supercooled phase are obtained in a model involving two liquid states separated by their Gibbs free energy difference determined from the value of  $T_g$  [23,25,26]. This model has some analogy with the concept of two liquids applied to supercooled water transformations [27]. Desgranges and Delhommelle show that methanol under shear also reveals the existence of liquid polymorphism in this system driven out-of-equilibrium by undercooling [28] and that liquid polymorphs play a pivotal role during the crystallization of silicon. This implies that, theories, like the classical nucleation theory, should be modified to account for the role of liquid polymorphs in the nucleation process [29]. A two-liquid model describes the supercooled water as a glacial phase. These two liquids give rise to a third liquid called Phase 3 having a Gibbs free energy equal to the difference of their own Gibbs free energies, a glass transition at  $T_g$ , and a medium range order up to  $T_{n+}$ . The completed classical nucleation equation predicts the Phase 3 transformation in glacial phases of supercooled water, triphenyl phosphite, n-butanol, and d-mannitol in perfect quantitative agreement with experiments just knowing the initial value of their  $T_g$  before transformation in glacial phases [13,16].

The phase transition assumption viewed as a percolation phenomenon at  $T_g$  is examined using all the thermodynamic parameters accumulated in many publications. Wool et al shows that the liquid-to-glass transformation results from percolation phenomenon of atom groups formed above  $T_g$  during cooling [30-32]. Angell and Rao's congruent bond lattice model of topologically disordered oxide systems analyze the connectivity of disordered systems accounting for the threshold degree  $\Phi$  of connectivity [33]. Ojovan et al treat the liquid–glass transition during heating as a percolation phase transition in the system of broken bonds called configurons [34-36]. The critical density is evaluated from Scher-Zallen's predictions leading to  $\Phi = 0.15 \pm 1$  at  $T_g$  [37]. They still predict that the first sharp diffraction minimum in the pair distribution function is expected to contain information on structural changes in amorphous materials at  $T_g$  and  $T_{n+}$  [38]. Moreover, the configuron percolation theory naturally treats the known behavior of heat capacity which drops continuously on cooling of melts and diverges i.e. it is seen as a very sharp and narrow peak at  $T_g$  on heating of glasses evidencing the phase transformation as due to configuron association in macroscopic percolating clusters.

The work developed here is devoted to Phase 3 and configurons. For that purpose, several methods are successively used without forgetting Souletie and Tholence's conclusion that the power law gives a better account of the available experimental evidence than the Vogel-Fulcher-Tammann law [39]. One method is based on previous studies of Rammal and Benoit and Henley devoted to spin glasses predicting that the relaxation time  $\tau/\tau_0 \sim \exp(W/T)$  increases with  $W \sim \ln\xi$  where  $\xi$  is the coherence length of percolating clusters [40,41]. The energy W also contains the delocalization energy  $\Delta e_e$  of atoms calculated by Sanditov, Ojovan and Darmaev which is related to the ultimate displacement of a bridging atom at T<sub>g</sub> and above T<sub>g</sub>[42]. This occurs when the energy of thermal vibrations of the lattice per atom

becomes equal or lower than  $\Delta e_e$ . The value of  $\Delta e_e$  is deduced from the contribution of  $D^*T^2/(T-T_0)^2$  to  $\ln(\tau/\tau_0)$  where  $T_0$  is predicted with a thermodynamic law from the knowledge of  $T_g$  instead of being measured [26]. The delocalization energy, proportional to the temperature T, varies as  $\ln\xi$  in a wide range of temperatures when the Vogel-Fulcher-Tammann (VFT) law is used for fragile liquids. This VFT law only works at  $T_g$  for strong liquids. These observations confirm that  $Ln (\xi^v)$  is equal to  $vLn (1-T_g/T)$  without confirmation of an exponent v which could be equal to -0.88. A critical temperature  $T_c < T_g$  was proposed in few glasses by Souletie in 1990 claiming that  $T_c$  could be determined by extrapolating to zero the reverse of  $d(\log T)/d(\log \eta)$  versus T (K) where  $\eta$  is the viscosity or by plotting  $\log(\eta)$  versus  $\log(\xi)$  [ (43)]. He found  $T_c = 568$  K with  $T_g = 637$  K [44] for Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> in agreement with the value of  $T_3 = 572$  K predicted in this paper,  $T_c = 169$  K for  $T_g = 190$  K for glycerol in agreement with Birge and Nagel predictions and  $T_3 = 174$  K [45,46]. The existence of Phase 3 was anticipated 30 years ago using the dynamical scaling near a transition at  $T_c$  characterized by a power law for  $\tau/\tau_0$  [47]. The negative activation energy  $E_a$  of Phase 3 reveals that its formation at  $T_3 < T_g$  is masked during cooling by an intermediate phase acting at the temperature  $T_g$  where  $E_a$  is equal to zero. An analogous phenomenon is known in gaz-phase reactions [48].

The Gibbs free energy of "ordered" liquid phase 3 is predicted below and above  $T_g$  including the critical anomaly associated with the phase transition which has a weak contribution as shown by a very-narrow specific heat peak when it is detected around  $T_g$  [44,49-51]. The theoretical Gibbs free energy of configurons is also used and successfully introduced in that of Phase 3 [36]. It is proportional to the temperature as predicted by Sanditov et al and determine the fraction of configurons involved in kinetic units having a coherence length ratio of  $\xi/\xi_0$  [42]. The threshold degree  $\Phi \cong 0.15 \pm 0.01$  of configuron percolation involved in kinetic units associated with medium-range order in phase 3 is confirmed.

## 1- The glass transition temperature 1.1 Critical phenomena are observed around T<sub>g</sub>.

Several experimental proofs exist. A critical phenomenon is observed in few measurements of heat capacity. The most spectacular peaks have been obtained by Alba et al in 1990 with molecular glasses such as toluene, m-xylene, and m-toluidine [49,50] confirmed by Wilde et al in 2004 with the bulk metallic glass Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> [44], Hassine et al with n-butanol and Mandanici et al with ethylcyclohexane [51,52]. As an example, the heat capacity of m-toluidine is represented in Figure 1:



**Figure 1**. Heat capacity vs temperature for liquid, glass, and crystal states of m-toluidine according to DSC measurements from [50] [C. Alba-Simonesco, J. Fan, and C.A. Angell, J. Chem. Phys.110 (1999) 5262] with permission of AIP Publishing.

A very sharp and narrow peak is measured in Figure 1 accompanied by precursory effects below  $T_g$ . Interestingly that heat capacity behavior is characterized by a hysteresis curve - the peak is seen on heating and not seen on cooling down the material although the capacity jump is kept unchanged. In

addition, the jump at  $T_g$  covers all the difference of heat capacity between those of liquid and crystal as expected.

#### 1-2 The jump of heat capacity is not always fully accomplished at T<sub>g</sub>.

As an example, the heat capacity of 1-propanol is reproduced in Figure 2 from Takahara et al [53]



**Figure 2**. Heat capacities of glassy-liquid (o) and crystalline (o) states of 1-propanol at 108.4 MPa. The dashed lines represent the extrapolation of the heat capacities determined by the least-squares. Reproduced from [53] [S. Takahara, O. Yamamuro, H. Suga, J. Non-Cryst. Sol. 171 (1994) 259-270].

Many other heat capacity measurements reproduce this phenomenon without critical phenomenon [54-56]. The applied cooling rate below  $T_g$  is too high compared to the duration of the transition. A part of the sample could be frozen without contribution to the jump and to the total thermodynamic transition [57]. Thin film deposition at too low temperatures below  $T_g$  leads to a constant volume far above that of the glass state [18].

## 1-3 The thermodynamic glass transition occurs at a temperature where the heat capacity difference between those of Liquid 1 and crystal becomes equal to that of Phase 3.

The heat capacity jump is equal to  $1.5 \times S_m/T_m$  in many glasses as shown in 1960 by Wunderlich [58] and confirmed for many glasses [26] (where  $S_m$  is the crystal entropy of fusion). In Figure 3, the glass transition is pushed at higher temperatures by increasing the heating rate up to a temperature where the glass formation time is equal to the heating time across the transition width. The new glass transition is accompanied by a weak latent heat as represented in Figure 3. The latent heat is equal to the surface of triangle ABC. This phenomenon is shown by heat capacity measurements at high heating rates [59]



**Figure 3.** The heat capacity and latent heat induced by an increase of  $T_g$ . A high heating rate increases the glass transition temperature from A to B and produces a latent heat equal to the triangle area ABC accompanying a heat capacity jump equal to  $1.5 \times S_m$ .

The latent heat coefficient  $\Delta \epsilon$  associated with a transition at  $T \neq T_g$  is calculated using the following equations predicting two reduced homogeneous nucleation temperature  $\theta_{n-}$  in fragile Liquid 2 resulting from the completed classical nucleation equation [13,16]:

$$\theta_{n-} = (-3 \pm [9 - 4(2 - \varepsilon_{gs0} - \Delta \varepsilon) \varepsilon_{gs0} / \theta_{0g}^2]^{0.5}) \theta_{0g}^2 / 2\varepsilon_{gs0}, \qquad (1)$$

where 
$$\varepsilon_{gs}(\theta) = \varepsilon_{gs0} \left( 1 - \theta^2 \times \theta_{0g}^{-2} \right) + \Delta \varepsilon,$$
 (2)

$$\varepsilon_{gs}(\theta = 0) = \varepsilon_{gs0} = 1.5\theta_2 + 2 = 1.5\theta_g + 2,$$
(3)

$$\theta_{0g}^2 = \frac{8}{9} \varepsilon_{gs0} - \frac{4}{9} \varepsilon_{gs0}^2. \tag{4}$$

For a latent heat coefficient  $\Delta \epsilon = 0$ ,  $\theta_{n-} = \theta_g = (T_g - T_m)/T_m$  while there are two homogeneous nucleation temperatures  $\theta_{n-}$  for the same value of  $\Delta \epsilon$ , one above  $\theta_g$  leading to an increase of  $T_g = T_{n-}$  even to glacial phase transitions for high values of  $\Delta \epsilon$  and a decrease symmetrical from the first one with regard to  $T_g$ . This equation leads to  $\Delta \epsilon \times H_m = 0.024 \times H_m$  for an increase of  $T_g$  of 21 K of triphenyl phosphite using a heating rate of 1000 K/s (H<sub>m</sub> being the crystal melting heat) [13].

## 1-4 Thermodynamic origin of the glass transition

The glass transition is now recognized as being a thermodynamic transition instead of a liquid freezing. The glass transition is seen as a manifestation of critical slowing down near a second-order phase transition with the possible existence of several classes of universality [43]. A model predicting the specific heat jump is based on a percolation-type phase transition with the formation of dynamical fractal structures near the percolation threshold [30,31,34-36]. Macroscopic percolating clusters formed at the glass transition have been visualized [32]. High precision measurements of third- and fifth-order non-linear dielectric susceptibilities lead to a fractal dimension  $d_F = 3$  for the growing transient domains [60]. An observation of the structural characteristics of medium-range order with neutrons and X-rays leads to  $d_F = 2.31$  [61]. The heat capacity jump of  $1.5 \times S_m$  is predicted for many liquids [62] having an enthalpy coefficient  $\varepsilon_{ls}$  ( $\theta$ ) for fragile Liquid 1 respecting (5-7) and a = 1:

$$\varepsilon_{ls}(\theta) = \varepsilon_{ls0}(1 - \theta^2 \times \theta_{0m}^{-2}),\tag{5}$$

$$\varepsilon_{ls}(\theta=0) = \varepsilon_{ls0} = 1.5\theta_1 + 2 = a\theta_g + 2,\tag{6}$$

$$\theta_{0m}^2 = \frac{8}{9} \varepsilon_{ls0} - \frac{4}{9} \varepsilon_{ls0}^2.$$
(7)

## 2- The enthalpy coefficients 2-1 The enthalpy coefficients of Phase 3

New Phase 3 is viewed as having an enthalpy coefficient equal to the difference  $\Delta \epsilon_{lg}$  between those of liquids 1 and 2 and given in (8) [13,16,23]:

$$\Delta \varepsilon_{lg}(\theta) = \varepsilon_{ls} - \varepsilon_{gs} = \varepsilon_{ls0} - \varepsilon_{gs0} + \Delta \varepsilon - \theta^2 (\varepsilon_{ls0}/\theta_{0m}^2 - \varepsilon_{gs0}/\theta_{0g}^2).$$
(8)

This phase undergoes the glass transition at  $T_g$  and obeys (8) up to the temperature  $T_{n+}$  of homogeneous nucleation respecting  $\Delta \epsilon_{lg} = \theta_{n+}$  where the liquid mean-range order is broken giving rise to short-range order inside the residual coherence length  $\xi_0$ . This enthalpy difference belongs to the Gibbs free energy

## 2-2 The enthalpy coefficients of strong liquids 1 and 2

A strong liquid 1 has a reduced temperature  $\theta_{0m} \leq -2/3$  equal to its VFT temperature determined from viscosity measurements. The VFT temperature of Liquid 2 is fixed to  $T_{VFT} = 0$  K ( $\theta_{0g} = -1$ ) because the relaxation time follows an Arrhenius law. The enthalpy coefficients are calculated from (9-10);

$$\varepsilon_{ls0} = (3\theta_g + 2) / \left( 1 - \frac{\theta_g^2}{\theta_{0m}^2} \right),$$
(9)  
$$\varepsilon_{gs0} = (3\theta_g + 2) / \left( 1 - \frac{\theta_g^2}{\theta_{0g}^2} \right).$$
(10)

There are some cases where Liquid 1 is fragile above  $T_g$  and Liquid 2 is strong. In these conditions,  $\theta_{0g}$  is equal to -2/3 and  $T_{0g} = T_m/3$ . This event occurs in Mg<sub>69</sub>Zn<sub>27</sub>Yb<sub>4</sub> and leads to a quasi-crystalline phase through a first-order transition [63] as shown in Chapter 4

#### 3- Two examples of liquid relaxation times

## 3.1- Relaxation times of fragile liquids Au<sub>49</sub>Ag<sub>5.5</sub>Pd<sub>2.3</sub>Cu<sub>26.9</sub>Si<sub>16.3</sub> above T<sub>g</sub>

There are two relaxation times associated with liquids 1 and 2 at each temperature. The nucleation times 1-Liq1 and 2-Liq2 are equal at T = 389 K for  $T_g = 377$  K [64,65]:

$$Ln(^{\tau}/\tau_0) = {B_1}/(T - T_{0m}) = {B_2}/(T - T_{0g})$$
(11)



**Figure 4.** Relaxation times  $\tau$  of liquids  $Au_{49}Ag_{5.5}Pd_{2.3}Cu_{26.9}Si_{16.3}$ . 1-Liq1 obeys the first VFT law  $(T_{0m}, B_1)$  with  $\tau_0 = 10^{-14}$  s. 2-Liq2 and 3-Liq2 obeys the second VFT law  $(T_{0g}, B_2)$  with  $\tau_0 = 10^{-14}$  s and  $\tau_0 = 2.76 \times 10^{-16}$  s.

Using (3,4,6,7) with a = 1,  $T_m = 610$  K, and  $T_g = 377$  K, we predict the VFT laws with  $T_{0m} = 304.43$  K,  $T_{0g} = 242.28$  K;  $B_1 = T_{0m} \times 10.68$  and  $B_2 = T_{0g} \times 23.29$  with  $\tau = 504$  s and  $\tau_0 = 10^{-14}$  s in good agreement with experiments of Gallino et al [64] and Hechler et al [65]. The relaxation times of 1-Liq1 and 3-Liq2 are equal at  $T_{Br-} = 419.8$  K as defined by the enthalpies of liquid 1 and 2 given by (12,13) calculated with (3,4,6,7) and  $T_g = 377$  K:

$$\varepsilon_{ls}(\theta) = 1.61803 \left( 1 - \frac{\theta^2}{0.27468} \right),$$
 (12)

$$\varepsilon_{ls}(\theta) = 1.42705 \left( 1 - \frac{\theta^2}{0.36339} \right),$$
 (13)

where  $\varepsilon_{ls}(\theta) = \varepsilon_{gs}(\theta)$  for  $\theta = \theta_{Br} = -0.31188$ .

The relaxation time 3-Liq2 is parallel to 2-Liq2 with  $\tau_0 = 2.76 \times 10^{-16}$  s instead of  $10^{-14}$  s because the timelag required for an equilibrium distribution of atoms to be established during the transition from liquid 1-to-liquid 2 is much longer above than below 389 K.

A cooling rate of 5 K/min leads to an uncomplete heat capacity jump extending from 340 to 400 K [56] because the relaxation times are high in this range of temperatures as shown in Figure 4.

A much weaker cooling rate from 394 to 383 K lowers the enthalpy of Liquid 1 towards that of liquid 2. The recovered enthalpy  $0.2 \times 383$  J/g-atom [65] is much smaller than the enthalpy difference between those of Liquid 1 and Liquid 2 which is equal to  $\Delta \epsilon_{lg} \times H_m = 395$  J in (14) with  $H_m = 5100$  J/mole:

$$\Delta \varepsilon_{lg}(\theta) = 0.19098(1 - \theta^2 \times 10.28).$$
<sup>(14)</sup>

The structural changes observed by Hechler et al [65] prove the existence of two liquid phases as predicted by this two-liquid model.

## 3.2- Relaxation of fragile liquid Au<sub>49</sub>Ag<sub>5.5</sub>Pd<sub>2.3</sub>Cu<sub>26.9</sub>Si<sub>16.3</sub> after quenching

The change of properties during aging and slow heating after the first quenching has been investigated by Gallino et al. The glass transition initially equal to about 401 K [66,67] becomes equal to 377 K after storage at 290 K in a freezer and after slow heating. They also observe a heat capacity decrease of the liquid after heating above  $T_g = 377$  K. This is due to a weak decrease  $\Delta \epsilon = 0.00776$  of liquid 1 enthalpy coefficient during aging because Phase 3 and glass phase are built after the first quenching and do not preexist before heating. The glass transition expected after the first quenching and during the first annealing occurs close to the Kauzmann temperature  $T_{K1} = 402.5$  K of Liquid 1,  $T_{K1}$  also being the temperature where the enthalpy difference of liquids 1 and 2 would be equal to that between liquid 1 and crystal for  $T_g = T_{K1}$ . The enthalpy coefficients of liquids 1, 2 and 3 after classical annealing would be given in (15-17):

$$\varepsilon_{gs} = 1.48978 \times (1 - \theta^2 / 0.33783), \tag{15}$$

$$\varepsilon_{ls} = 1.65985 \times (1 - \theta^2 / 0.25093), \tag{16}$$

$$\Delta \varepsilon_{lg}(\theta) = 0.17008(1 - \theta^2 \times 12.965).$$
<sup>(17)</sup>

The phase 3 enthalpy coefficient given in (17) using (1) is represented in Figure 5 with the glass transition at 377 K after aging. The temperature of sample storage must be lower than the nucleation temperature  $T_{n-} = 282.7$  K (deduced from (1) with  $\Delta \epsilon = \Delta \epsilon_{lg0} = 0.17008$ ) to stabilize the glass transition at  $T_g = 402.5$  K without relaxed enthalpy  $\Delta \epsilon \times H_m$ .

A cooling rate of 5 K/min shows that the slope of  $\Delta C_p$  (T) changes twice: the first time between 340 and 365 K and the second time above 385 K. It may indicate two distinctly different glass-transition processes revealed by an uncomplete glass transition [56]. These double transitions could be due to the presence of Phase 3 transition in the sample fraction which is not transformed into a glass phase at 389 K. A similar double-stage glass transition is still observed in a metallic glass [68].



**Figure 5.** The glass transition at  $T_g$  of  $Au_{49}Ag_{5.5}Pd_{2.3}Cu_{26.9}Si_{16.3}$  plotted versus the relaxed-enthalpy coefficient  $\Delta \varepsilon$ .  $T_g = 377$  K obtained with  $\Delta \varepsilon = 0.00775$  using (1).

#### 3.3- Relaxation times of liquid Zr<sub>65</sub>Cu<sub>27.5</sub> Al<sub>7.5</sub>

The glass transition occurs at T = 666 K with  $T_m = 1180$  K [69]. The heat capacity jump is equal to  $1.5 \times S_m$ . The enthalpy coefficients calculated using (3,4,6,7) obey (18-20):

$$\varepsilon_{ls} = 1.5644 \times (1 - \theta^2 / 0.30286), \tag{18}$$

$$\varepsilon_{as} = 1.3466 \times (1 - \theta^2 / 0.39105), \tag{19}$$

$$\Delta \varepsilon_{lg}(\theta) = 0.2178 - \theta^2 \times 1.7218.$$
<sup>(20)</sup>

The relaxation times are represented in Figure 6 using (11).



**Figure 6.** Relaxation times of liquids  $Zr_{65}Cu_{27.5}Al_{7.5}$ . 2-Liq1 obeys the first VFT law  $(T_{0m}, B_1)$  with  $\tau_0 = 10^{-14}$  s. 1-Liq2 and 3-Liq2 obeys the second VFT law  $(T_{0g}, B_2)$  with  $\tau_0 = 10^{-14}$  s and  $\tau_0 = 2.4 \times 10^{-16}$  s.

1-Liq2 and 2-Liq1 have the same relaxation time  $\tau \cong 1.5$  s at T<sub>g</sub> using VFT laws with T<sub>0m</sub> = 530.61 K, T<sub>0g</sub> = 442.1 K, B<sub>1</sub> = T<sub>0m</sub>×8.33, B<sub>2</sub> = T<sub>0g</sub>×16.53, and  $\tau_0 = 10^{-14}$  s in good agreement with experiments of Zhou et al [69] and Kuchemann et al [70]. The relaxation times of 2-Liq1 and 3-Liq2 are equal to 5×10<sup>-7</sup> s at T<sub>Br-</sub> = 760.3 K defined by the enthalpies of liquid 1 and 2 given by (18,19) calculated with (3,4,6,7) and T<sub>g</sub> = 666 K. The glass transition temperature is expected to increase from 666 up to 760 K with a heating rate varying from 0.67 K/s to 2×10<sup>6</sup> K/s in perfect agreement with [70]. The latent heat coefficient  $\Delta\epsilon$  calculated with (1) at T<sub>Br-</sub> = 760.3 K corresponds to 2.2% of the melting heat.

The Kauzmann temperature of Liquid 1 is much higher than  $T_g$ . The glass transition cannot occur at higher temperature because the specific heat of Phase 3 would be too weak to accommodate a glass transition at  $T_{K1} = T_g = 778$  K ( $\theta_{K1} = -0.34$ ).

## 4- A fragile-to-strong liquid transformation in Mg<sub>69</sub>Zn<sub>27</sub>Yb<sub>4</sub>

For Mg<sub>69</sub>Zn<sub>27</sub>Yb<sub>4</sub>, T<sub>g</sub> is equal to 373 K, T<sub>m</sub> to 663 K and the melting heat  $H_m = 7600$  J/K/mole [63]. In Figure 7, the enthalpy coefficient of Phase 3 is plotted versus temperature. The enthalpy coefficients of liquids 1, 2 and 3 are given in (21-23) and (21) is calculated with (3,4,6,7) and a = 0.97 because liquid 1 is fragile while Liquid 2 with (22) is strong and calculated with (9) and  $\theta_{0g}^2 = 0.44444$  (T<sub>0m</sub> = T<sub>m</sub>/3) instead of one for other strong glasses:

$$\varepsilon_{ls} = 1.5757 \times (1 - \theta^2 / 0.29713), \tag{21}$$

$$\varepsilon_{gs} = 1.20765 \times (1 - \theta^2 / 0.44444), \tag{22}$$

$$\Delta \varepsilon_{la}(\theta) = 0.36807 - \theta^2 \times 2.58584.$$
<sup>(23)</sup>

The enthalpy coefficient of Phase 3 is given by (23) and equal to 0.35865 at 623 K. Its enthalpy coefficient at the temperature where  $\varepsilon_{ls} = 0$  (T<sub>0m</sub> = 301.6 K,  $\theta_{0m} = -0.5451$ ) is -0.40027. The latent heat coefficient is expected to be -0.35865-0.40027 = -0.75982 in perfect agreement with the measured value -0.76.

This transformation temperature is predicted and expected to lead in principle to a new strong glass phase having  $T_g = 655.78$  K as shown by (1) using (21) and  $\Delta \epsilon = 0.76$ . This temperature cannot be attained because the entropy available at this temperature is too small to accommodate the entropy increase at the phase melting. This event occurs at 623 K when the available entropy in Phase 3 with  $T_g = 655.78$  K is equal to the entropy variation from 623 K to  $T_m$ . This new phase is quasi-crystalline [63] instead of being a glassy glacial phase [13]. Rapid superheating of this phase escaping from crystallization could lead to melting at  $\theta_{n+} = \Delta \epsilon_{lg} = 0.2306$  ( $T_{n+} = 816$  K). The missing enthalpy for crystal formation is about  $0.24 \times H_m = 1800$  J/mole in agreement with the experiments.



**Figure 7.** The phase 3 enthalpy coefficient of  $Mg_{69}Zn_{27}Yb_4$ , versus T(K). 1- Enthalpy coefficient of Phase 3 for fragile liquid 1 and strong liquid 2. 2- Enthalpy coefficient for fragile liquids 1 and 2. 3- A first-order transformation predicted at 623 K with a latent heat coefficient equal to 0.75982 and to  $\Delta \varepsilon_{lg}(T_{0m})$  +  $\Delta \varepsilon_{lg}(623K)$ . 4- This new QC phase expected to melt at  $T_{n+} = 816$  K if crystallization is avoided.

## 5- Entropy of fragile liquids respecting a = 1 ( $\Delta C_p$ (T<sub>g</sub>) = 1.5×S<sub>m</sub>)

The Phase 3 and Liquid 1 entropies  $S_3(T)$  and  $S_1(T)$  are calculated from their heat capacity and are given in (24,25) knowing that the liquid entropy  $S_2(T)$  is equal to the difference  $S_1(T)$ - $S_3(T)$ :

$$S_1(T) = -2\left(\frac{\varepsilon_{ls0}}{\theta_{0m}^2}\right) S_m \frac{(T_m - T)}{T_m} + 2S_m Ln(\frac{T_m}{T})(\frac{\varepsilon_{ls0}}{\theta_{0m}^2}),\tag{24}$$

$$S_3(T) = -2\left(\frac{\varepsilon_{ls0}}{\theta_{0m}^2} - \frac{\varepsilon_{gs0}}{\theta_{0g}^2}\right) S_m \frac{(T_m - T)}{T_m} + 2S_m Ln(\frac{T_m}{T})(\frac{\varepsilon_{ls0}}{\theta_{0m}^2} - \frac{\varepsilon_{gs0}}{\theta_{0g}^2}).$$
(25)

The quantities  $\varepsilon_{ls0}$ ,  $\varepsilon_{gs0}$ ,  $\theta_{0m}^2$  and  $\theta_{0g}^2$  are calculated from (3,4,6,7) for each value of  $\theta_g$  and  $S_m$  and the coefficients a into (6) are equal to 1. The entropies in Figure 8 are for liquids having a heat capacity jump of  $1.5S_m$  at  $T_g$ .  $S_1(\theta_g)$  is minimum and equal to the crystal entropy (-1) for  $\theta_g = -0.3402$  and  $S_2(\theta_g)$  for  $\theta_g = -0.4544$ .  $S_3(\theta_g)$  being far above its minimum value authorizes Phase 3 formation. There is no more fragile liquid for  $\theta_g < -0.5$  [62].



**Figure 8.** Entropy of fragile liquids 1, 2, and 3 versus reduced glass transition temperature  $\theta_g$ . The entropy unit is  $S_m$ . The Kauzmann temperature of liquid 1,  $\theta_{K1} = -0.3402$ , that of liquid 2,  $\theta_{K2} = -0.4544$ . The crystal entropy  $S_m = -1$ . Phase 3 entropy  $S_3 = -0.5$  for  $\theta = -0.4544$ .

## 6- Characteristic temperatures of 50 liquids 1 and 2 with $\Delta C_p(T_g) = 1.5 \times S_m (a = 1)$

Fifty fragile liquids [26] are characterized by  $\varepsilon_{ls0}$ ,  $\varepsilon_{gs0}$ ,  $\theta_{0m}^2$  and  $\theta_{0g}^2$  calculated from (3,4,6,7) for each value of  $\theta_g$ . The characteristic temperatures  $T_g$ ,  $T_m$ ,  $\theta_g$ ,  $T_{0g}$ ,  $T_{0m}$ ,  $T_3$  and  $T_{n+}$  are given in Table 1. The hidden transition of Phase 3 at  $T_3 < T_g$  occurs at the reduced temperature  $\theta_3$  given in (26):

$$\theta_3 = -\left(\frac{\Delta \varepsilon_{lg0}}{\varepsilon_{ls0}} \frac{\varepsilon_{gs0}}{\theta_{0g}^2}\right)^{0.5},\tag{26}$$

where  $\Delta \varepsilon_{lg} = -\Delta \varepsilon_{lg0}$  in (8) [13]. The reduced temperature  $\theta_{n+}$  is equal, above  $T_m$ , to the reduced homogeneous nucleation temperature of Phase 3 where  $\theta = \Delta \varepsilon_{lg}(\theta)$  using (8) [23]. The temperatures  $T_{0g}$  and  $T_{0m}$  are determined from (3,4) and (6,7).

## Table 1 Data of fragile liquids with $\Delta C_p(T_g) \cong 1.5S_m$

The following informations can be completed referring to [26].

	Materials	$T_g(K)$	$T_m(K)$	$\theta_{\rm g}$	$T_{0g}$	$T_{0m}(K)$	$\Delta \epsilon_{lg0}$	T <sub>3</sub> (K)	$T_{n+}(K)$	Ref.
	Molecular glasses									
1	β-D-fructose	286	378	-0.24339	183	213	0.12169	271.8	414	[71-73]
2	Probucol	295	399	-0.26065	188	220	0.13033	278.9	439	[54,74,75]
3	Griseofulvin	364	493	-0.26166	232	271	0.13083	344.0	543	[74,75]
4	D-glucose	309	420	-0.26429	197	230	0.13214	291.8	463	[71-73,76]
5	1,3,5-tri-a-Naphtylbenzene	340	475	-0.28421	216	254	0.14211	319.1	527	[76,77]
6	Phenobarbital	319	447	-0.28635	202	238	0.14318	299.2	497	[74,75]
7	Isopropyl benzene	125	177	-0.29379	79	93	0.14689	117.0	197	[78]
8	Hydro-chloro-thiazide	385	547	-0.29616	244	288	0.14808	359.9	610	[74,75]
9	3-Methylpentane	77	110	-0.30000	49	58	0.15000	71.9	123	[53,79]

10 m-Cresol	199	286	-0.30420	126	149	0.15210	185.5	320	[49,50]
11 Xylitol	244	358	-0.31844	154	183	0.15922	226.4	402	[80]
12 Phenolphthalein	363	533	-0.31895	230	273	0.15947	336.7	599	[71,76]
13 9-Bromophenanthrene	225	331	-0.32024	142	169	0.16012	208.6	372	[81]
14 α-Phenyl -O-cresol	220	328	-0.32927	139	166	0.16463	203.3	370	[82]
15 H <sub>2</sub> SO <sub>4</sub> -3H <sub>2</sub> O	158	237	-0.33333	100	119	0.16667	145.8	268	[71,83,84]
16 Diethylphthalate	178	267	-0.33333	113	134	0.16667	164.2	301	[85]
17 m-Fluorotoluene	123	184	-0.33152	78	93	0.16576	113.6	208	[49,50,86]
18 2-methyl tetrahydrofuran	91	137	-0.33577	58	69	0.16788	83.9	155	[87,88]
19 n-Butene	58	88	-0.34091	37	44	0.17045	53.4	100	[89,90]
20 Toluene	117	178	-0.34270	74	89	0.17135	107.6	202	[24,49,50,91]
21 Glycerol	190	292	-0.34932	121	144	0.17466	174.2	332	[71,81]
22 2-Methylpentane	78	120	-0.35000	50	59	0.17500	71.5	136	[71,92]
23 Ethylbenzene	114.5	178.1	-0.35710	73	87	0.17855	104.7	203	[18,91]
24 n-Propanol	96	150	-0.36000	61	73	0.18000	87.6	171	[53,93,94]
25 3-Bromopentane	106	167	-0.36527	68	81	0.18263	96.6	191	[87]
26 CaAl <sub>2</sub> Si <sub>2</sub> O <sub>8</sub>	1160	1830	-0.36612	741	886	0.18306	1056.4	2090	[95-97]
27 2-methyl-1-propanol	107	172	-0.37791	69	82	0.18895	96.9	197	[94]
28 Selenium	309	494	-0.37449	198	237	0.18725	280.4	566	[98,99]
29 CaMgSi <sub>2</sub> O <sub>6</sub>	1005	1665	-0.39640	650	780	0.19820	902.9	1921	[95,100]
30 Butyronitrile	97	161	-0.39752	63	75	0.19876	87.1	186	[101,102]
31 cis-/trans-Decalin	137	231	-0.40693	89	107	0.20346	122.5	267	[81,86]
32 Ethanol	94	160	-0.41250	61	74	0.20625	83.8	186	[76,86,103-105]
33 Methanol	100	172	-0.41860	66	79	0.20930	88.9	200	[71,76]
34 Ethylene glycol	151	260	-0.41923	99	119	0.20962	134.1	302	[71,104]
35 m-Xylene	126	225	-0.44000	84	101	0.22000	110.7	263	[49,50]
Bulk metallic glasses									
36 Pd <sub>40</sub> Ni <sub>10</sub> Cu <sub>30</sub> P <sub>20</sub>	578	798	-0.27569	367	431	0.13784	544.0	883	[106,107]
37 Pdus Nine Culas Pag	576	802	-0.28180	365	430	0 14090	541.0	890	[57 108]
$\frac{37}{38}  \Delta u_{10} \Delta g_{2} \cdot Pd_{2} \cdot Cu_{20} \cdot Si_{10}$	402 F	C10		505	430	0.14050		090	[37,100]
$\frac{30}{30} \frac{Pd_{40}Ni_{40}P_{20}}{Pd_{40}Ni_{40}P_{20}}$	402.5	610	-0.34016	255	304	0 17008	370.4	690	[64-67]
	402.5 582	884	-0.34016	255 369	304 440	0.17008	370.4 535.3	690 1001	[64-67]
40 Pt <sub>57,3</sub> Cu <sub>14,6</sub> Ni <sub>5,3</sub> P <sub>22,8</sub>	402.5 582 509	884 820	-0.34016 -0.34163 -0.37927	255 369 327	304 440 391	0.17008 0.17081 0.18963	370.4 535.3 460.9	690 1001 940	[64-67] [109]
$\frac{40}{40} Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8}$	402.5 582 509 715	884 820 1163	-0.34016 -0.34163 -0.37927 -0.38521	255 369 327 460	304 440 391	0.17008 0.17081 0.18963 0.19261	370.4 535.3 460.9 645.7	690 1001 940 1337	[64-67] [109] [110] [69-70]
$\begin{array}{c} 40  Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ \hline 41  Zr_{46}Cu_{46}A_{18} \\ \hline 42  Zr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ \end{array}$	402.5 582 509 715 675	884 820 1163 1110	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189	255 369 327 460 436	304 440 391 552 523	0.17008 0.17081 0.18963 0.19261	370.4 535.3 460.9 645.7 607.7	690 1001 940 1337	[64-67] [109] [110] [69-70]
$\begin{array}{c} 40  Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ 41  Zr_{46}Cu_{46}A_{18} \\ 42  Zr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ 43  Pd_{77.5}Cu_6Si_{16.5} \end{array}$	402.5 582 509 715 675 637	810 884 820 1163 1110 1056	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678	255 369 327 460 436 412	304 440 391 552 523 495	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839	370.4 535.3 460.9 645.7 607.7 572.2	690 1001 940 1337 1279 1218	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112]
$\begin{array}{c} 40  Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ \hline 41  Zr_{46}Cu_{46}A_{18} \\ \hline 42  Zr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ \hline 43  Pd_{77.5}Cu_{6}Si_{16.5} \\ \hline 44  Zr_{45}Cu_{39.3}Al_{7}Ag_{8.7} \end{array}$	402.5 582 509 715 675 637 691	810 884 820 1163 1110 1056 1148	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808	255 369 327 460 436 412 448	304 440 391 552 523 495 537	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839 0.19904	370.4 535.3 460.9 645.7 607.7 572.2 620.3	690 1001 940 1337 1279 1218 1325	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114]
$\begin{array}{cccc} & & & \\ & & & \\ 40 & & & \\ Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ & & \\ 41 & & & \\ Tr_{46}Cu_{46}A_{18} \\ & & \\ 42 & & & \\ Tr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ & & \\ 43 & & & \\ Pd_{77.5}Cu_{6}Si_{16.5} \\ & \\ 44 & & \\ Tr_{45}Cu_{39.3}Al_{7}Ag_{8.7} \\ & \\ 45 & & Cu_{47}Ti_{34}Zr_{11}Ni_{8} \end{array}$	402.5 582 509 715 675 637 691 673	810 884 820 1163 1110 1056 1148 1128	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808 -0.40337	255 369 327 460 436 412 448 437	304 440 391 552 523 495 537 525	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839 0.19904 0.20168	370.4 535.3 460.9 645.7 607.7 572.2 620.3 602.6	690 1001 940 1337 1279 1218 1325 1304	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114] [115,116]
$\begin{array}{rrrr} & 40 & Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ & 41 & Zr_{46}Cu_{46}A_{18} \\ & 42 & Zr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ & 43 & Pd_{77.5}Cu_{6}Si_{16.5} \\ & 44 & Zr_{45}Cu_{39.3}Al_{7}Ag_{8.7} \\ & 45 & Cu_{47}Ti_{34}Zr_{11}Ni_{8} \\ & 46 & Mg_{65}Cu_{25}Y_{10} \end{array}$	402.5 582 509 715 675 637 691 673 428	810 884 820 1163 1110 1056 1148 1128 739	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808 -0.40337 -0.42084	255 369 327 460 436 412 448 437 281	304 440 391 552 523 495 537 525 337	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839 0.19904 0.20168 0.21042	370.4 535.3 460.9 645.7 607.7 572.2 620.3 602.6 379.9	690 1001 940 1337 1279 1218 1325 1304 859	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114] [115-116] [117]
$\begin{array}{cccc} & & & \\ & & $	402.3 582 509 715 675 637 691 673 428 657	810 884 820 1163 1110 1056 1148 1128 739 1145	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808 -0.40337 -0.42084 -0.42620	255 369 327 460 436 412 448 437 281 433	304 440 391 552 523 495 537 525 337 520	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839 0.19904 0.20168 0.21042 0.21310	<ul> <li>370.4</li> <li>535.3</li> <li>460.9</li> <li>645.7</li> <li>607.7</li> <li>572.2</li> <li>620.3</li> <li>602.6</li> <li>379.9</li> <li>581.5</li> </ul>	690 1001 940 1337 1279 1218 1325 1304 859 1334	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114] [115-116] [117] [55,118]
$\begin{array}{ccccccc} & & & & & \\ & & & \\ & & & & \\ & &$	402.3 582 509 715 675 637 691 673 428 657 466	810 884 820 1163 1110 1056 1148 1128 739 1145 822	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808 -0.40337 -0.42084 -0.42620 -0.43309	255 369 327 460 436 412 448 437 281 433 309	304       440       391       552       523       495       537       525       337       520       371	0.17008 0.17081 0.18963 0.19261 0.19595 0.19839 0.19904 0.20168 0.21042 0.21310	370.4 535.3 460.9 645.7 607.7 572.2 620.3 602.6 379.9 581.5 410.9	690 1001 940 1337 1279 1218 1325 1304 859 1334	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114] [115-116] [117] [55,118] [119,120]
$\begin{array}{c} 40  Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8} \\ \hline 41  Zr_{46}Cu_{46}A_{18} \\ \hline 42  Zr_{58.5}Cu_{15.6}Ni_{12.8}Al_{10.3}Nb_{2.8} \\ \hline 43  Pd_{77.5}Cu_6Si_{16.5} \\ \hline 44  Zr_{45}Cu_{39.3}\ Al_7Ag_{8.7} \\ \hline 45  Cu_{47}Ti_{34}Zr_{11}Ni_8 \\ \hline 46  Mg_{63}Cu_{25}Y_{10} \\ \hline 47  Zr_{65}Cu_{17.5}Ni_{10}Al_{7.5} \\ \hline 48  La_{55}Al_{25}Ni_5Cu_{10}Co_5 \\ \hline 49  Zr_{65}Cu_{27.5}Al_{7.5} \\ \end{array}$	402.5 582 509 715 675 637 691 673 428 657 466 666	810 884 820 1163 1110 1056 1148 1128 739 1145 822 1180	-0.34016 -0.34163 -0.37927 -0.38521 -0.39189 -0.39678 -0.39808 -0.40337 -0.42084 -0.42620 -0.43309 -0.43559	255 369 327 460 436 412 448 437 281 433 309 442	304 440 391 552 523 495 537 525 337 520 371 531	0.17008 0.17081 0.19261 0.19595 0.19839 0.19904 0.20168 0.21042 0.21310 0.21655 0.21780	<ul> <li>370.4</li> <li>535.3</li> <li>460.9</li> <li>645.7</li> <li>607.7</li> <li>572.2</li> <li>620.3</li> <li>602.6</li> <li>379.9</li> <li>581.5</li> <li>410.9</li> <li>586.5</li> </ul>	690 1001 940 1337 1279 1218 1325 1304 859 1334 960 1379	[64-67] [109] [110] [69-70] [14,110,111] [43,44,112] [113,114] [115-116] [117] [55,118] [119,120] [69,70]

## Table 2. Strong liquids data

These data are based on the following works [26]: SiO<sub>2</sub> [95,121], GeO<sub>2</sub> [76,121,122], N-butanol [123-125], and BeF<sub>2</sub> [51,76,86,126].

		SiO <sub>2</sub>	GeO <sub>2</sub>	N-butanol	BeF <sub>2</sub>
1	Ν	3	3	15	3
2	Tg	1473	830	111	590
3	T <sub>m</sub>	1996	1388	184	825
4	H <sub>m</sub> (J/mole)	9000	16700	9280	4770
5	θ <sub>g</sub>	-0.26202	-0.40202	-0.39674	-0.28485

6	$\epsilon_{ls0}$	1.39096	1.0182	1.14756	1.32078
7	ε <sub>gs0</sub>	1.30342	0.947	0.96105	1.2466
8	$\Delta \epsilon_{ m lg0}$	0.08754	0.0712	0.18651	0.074179
9	T <sub>0g</sub>	0	0	0	0
10	T <sub>0m</sub>	530	199	51.9	180
11	$\theta_{0m}^2$	0.53945	0.73381	0.51546	0.61124
12	$\theta_3$	-0.38397	-0.62092	-0.58804	-0.42025
13	T <sub>3</sub>	1256	599	84.1	493
14	$\theta_{n+}$	0.07948	0.0691	0.15579	0.06973
15	$T_{n+}$	2154.6	1483.9	212.7	882.5
16	X3	0.03709	0.0993	1.0812	0.04159
17	x <sub>3</sub> /N	0.01236	0.0331	0.07208	0.013863
18	$B_2$	53080	29900	4000	21255
19	$\mathbf{B}_1$	33980	22730	2129	14770
20	$\Delta e_2$ (J/g.atom)	441307	248589	33256	176714
21	$\Delta \epsilon_1 (J/g.atom)$	689311	326969	62431	254289
22	<b>i</b> 1	112.5	94.8	135.3	103.7
23	i <sub>2</sub>	72.07	72.05	72.07	72.05
24	i3	40.4	22.8	63.2	31.7
25	ξ/ξ0	2.75	2.06	1.91	2.64

The reduced melting temperature  $\theta_{n+}$  of medium-range order (phase 3) is plotted in Figure 9 as a function of the reduced glass temperature and obeys (27) [23]:

$$\theta_{n+} = -0.38742 \times \theta_g \,.$$

The average value of  $\Delta \epsilon_{lg}$  at this temperature is 0.13746 for fragile liquids and corresponds to a volume fraction of ordered phase given by the critical threshold equal to 0.15  $\pm$  0.01 (see chapter 9). For the strong liquids, the average is 0.0728 for SiO2, GeO<sub>2</sub> and BeF<sub>2</sub> indicating that their kinetic entities have a lower enthalpy for the same critical volume fraction.



**Figure 9.** The reduced melting temperature  $\theta_{n+} = \Delta \varepsilon_{lg}(\theta_{n+})$  of Phase 3 medium-range order versus  $\theta_g$  for 50 fragile liquids and for 4 strong liquids.

## 7- Activation energy and atom delocalization energy $\Delta e$ (J/g-atom)

## 7-1 Equations

The relaxation time is viewed as being temperature dependent through a VFT law given in (28):

(27)

$$Ln(^{\tau}/\tau_0) = {}^{B}/(T - T_0) = {}^{D^*T_0}/(T - T_0).$$
(28)

The VFT temperatures  $T_0$  of liquids 2 and 1 are  $T_{0g}$  and  $T_{0m}$  given by (4,7). The parameters B are determined to lead to  $\tau$  values of 44-45 s with  $\tau_0 = 10^{-14}$  s when (28) is applied.

The activation energies of liquids 1, 2 called  $W_1$  and  $W_2$  are given in (29,30)

$$W_1 = B_1 RT / (T - T_{0m}), (29)$$

$$W_2 = B_2 RT / (T - T_{0g}). ag{30}$$

The difference  $W_3$  between  $W_1$  and  $W_2$  in (31) corresponds to the activation energy of Phase 3:

$$W_3 = \frac{B_1 RT}{(T - T_{0m})} - \frac{B_2 RT}{(T - T_{0g})},$$
(31)

 $B_1$  and  $B_2$  are determined from a relaxation time of 44-45 s in Table 2 at  $T_g$ .

The difference between an Arrhenius law (W/T) and a VFT law (B/(T-T<sub>0</sub>) is w/T for liquids 1 and 2 as defined in (33)

$${}^{B}/_{(T-T_{0})} = {}^{W}/_{RT} - {}^{W}/_{RT},$$
(33)

where W and w are constants at each temperature. This gap is considered as due to the bonds which are broken or built at the temperature T in the formation model of moving entities. The change of Arrhenius law appears in the derivative of this relation as already shown with other phenomenological laws for the viscosity [34,35,42]:

$$-{}^{B}/(T-T_{0})^{2} = -{}^{W}/_{RT^{2}} + {}^{W}/_{RT^{2}}.$$
(34)

The delocalization energies  $\Delta e_1$  and  $\Delta e_2$  (J/g-atom) during heating in liquids 1 and 2 are:

$$\Delta e_1 = R B_1 T^2 / (T - T_{0m})^2 \tag{36}$$

$$\Delta e_2 = RB_2 T^2 / (T - T_{0g})^2$$
(37)

The delocalization energy  $\Delta e_3$  (J/g-atom) during heating in Phase 3 is:

$$\Delta e_3 = \Delta e_1 - \Delta e_2. \tag{38}$$

The energy  $\Delta e_3$  in (39) is used to calculate the number i of freedom degrees of kinetic units associated with heating at T<sub>g</sub> [42]:

$$i = \frac{2\Delta e_3}{RT},\tag{39}$$

where  $\Delta e_3$  is the delocalization energy per mole of atoms in the melt. The theoretical values of i given in Table 2 are the upper limits predicted by VFT laws at T<sub>g</sub>.

## 7-2 The atom delocalization energy and the number of freedoms degrees

Values of  $\Delta e_1$ ,  $\Delta e_2$  and  $\Delta e_3$  and i are given in J/g-atom for many fragile glass-forming melts in Table 3 for which the specific heat jump is equal to  $1.5 \times S_m$ .

## Table 3. Materials data used in and resulting from calculations

*	Materials	<b>B</b> <sub>2</sub>	<b>B</b> <sub>1</sub>	$\Delta e_2$	$\Delta e_1$	$\Delta e_3$	$\mathbf{i}_1$	<b>i</b> 2	i <sub>3</sub>	$\theta_{n^+}$	ξ/ξ٥
1	b-D-fructose	3700	2622	238612	336691	69520	283.2	200.7	82.5	0.09429	2.81

2	Probucol	3855	2706	243716	347101.4	72641	283.0	198.7	84.3	0.10098	2.66
3	Griseofulvin	4758	3338	300511	428235.4	89686	283.0	198.6	84.4	0.10137	2.66
4	D-glucose	4045	2834	254859	363764.5	76300	283.2	198.4	84.8	0.10239	2.63
5	1,3,5-tri-a-Naphtylbenzene	4480	3104	278346	402111	85492	284.5	196.9	87.6	0.11011	2.49
6	Phenobarbital	4206	2910	261051	377564.3	80438	284.7	196.9	87.9	0.11094	2.47
7	Isopropyl benzene	1651	1137	102174	148379.3	31840	285.6	196.6	88.9	0.11382	2.42
8	Hydro-chloro-thiazide	5087	3496	314593	457469.3	98392	285.8	196.6	89.3	0.11474	2.41
9	3-Methylpentane	1017.5	698	62868	91699.37	19741	286.5	196.4	90.1	0.11623	2.38
10	m-Cresol	2630	1799	162454	237466	51311	287.1	196.4	90.7	0.11785	2.36
11	Xylitol	3225	2185	199200	294057.6	64238	289.9	196.4	93.5	0.12337	2.27
12	Phenolphthalein	4797	3250	296324	437733.2	95562	290.1	196.4	93.7	0.12357	2.27
13	9-Bromophenanthrene	2973	2012	183695	271541.2	59378	290.3	196.4	93.9	0.12407	2.26
14	a-Phenil -cresol	2904	1952	179903	267532	58976	292.5	196.7	95.8	0.12757	2.21
15	H2SO4-3H2O	2084	1397	129326	192935.9	42633	293.7	196.9	96.8	0.12914	2.19
16	Diethylphthalate	2347	1574	145647	217380.9	47970	293.8	196.8	96.9	0.12914	2.19
17	m-Fluorotoluene	1623	1089	100636	149878.9	33111	293.1	196.8	96.3	0.12844	2.20
18	2-methyl tetrahydrofuran	1199.5	803	74525	111363.5	24666	294.4	197.0	97.4	0.13008	2.18
19	n-Butene	763.3	509	47563	71350.01	15865	295.9	197.3	98.7	0.13208	2.16
20	Toluene	1539	1025	96008	144255	32096	296.6	197.4	99.2	0.13277	2.15
21	Glycerol	2493	1651	156272	236025.9	52780	298.8	197.9	101.0	0.13533	2.12
22	2-Methylpentane	1023	677	64161	96942.77	21701	299.0	197.9	101.1	0.13560	2.11
23	Ethylbenzene	1486	971	94485	143592.1	33023	301.7	198.5	103.2	0.13852	2.08
24	n-Propanol	1253.5	823	79345	120908.1	27250	303.0	198.8	104.1	0.13947	2.07
25	3-Bromopentane	1380	902	87855	134484.4	30431	305.2	199.4	105.8	0.14151	2.04
26	CaAl2Si2O8	15093	9860	961819	1473715	333479	305.6	199.5	106.2	0.14184	2.04
27	2-methyl-1-propanol	1382	893	89435	138456.7	31645	311.3	201.1	110.2	0.14641	1.99
28	Selenium	3992	2582	257555	397441.8	91130	309.4	200.5	108.9	0.14606	1.99
29	CaMgSi2O6	12780	8105	853041	1344574	312048	321.8	204.2	117.7	0.15357	1.92
30	Butyronitrile	1232	781	82411	130117.3	30182	322.7	204.4	118.3	0.15401	1.91
31	cis-/trans-Decalin	1723	1081	117522	187517.5	43789	329.3	206.4	122.9	0.15765	1.88
32	Ethanol	1175	732	81169	130270.8	30603	333.4	207.7	125.7	0.15981	1.86
33	Methanol	1240.5	767	86987	140672.9	33182	338.4	209.3	129.1	0.16218	1.84
34	Ethylene glycol	1872	1157	131480	212788.2	50218	339.0	209.5	129.5	0.16242	1.84
35	m-Xylene	1516	910	113092	188121.8	45177	359.2	215.9	143.2	0.17046	1.77
	BMG										
36	$Pd_{40}Ni_{10}Cu_{30}P_{20}$	7600	5288	474571	681561.7	144370	283.7	197.5	86.1	0.10681	2.55
37	Pd <sub>43</sub> Ni <sub>10</sub> Cu <sub>27</sub> P <sub>20</sub>	7585	5262	471865	680569.9	144514	284.2	197.1	87.2	0.10917	2.50
38	Au49Ag5.5Pd2.3Cu26.9Si16.3	5328	3565	330040	499229.6	108564	298.4	197.3	101.1	0.13179	2.16
39	$Pd_{40}Ni_{40}P_{20}$	7656	5102	477275	716716.3	159216	296.2	197.3	99.0	0.13274	2.15
40	$Pt_{57.3}Cu_{14.6}Ni_{5.3}P_{22.8}$	6565	4238	425693	660081.1	150889	312.0	201.2	110.8	0.14924	1.99
41	Zr46Cu46Al8	9180	5890	600764	936502.1	215306	315.1	202.1	113.0	0.15183	1.96
42	Zr <sub>58.5</sub> Cu <sub>15.6</sub> Ni <sub>12.8</sub> Al <sub>10.3</sub> Nb <sub>2.8</sub>	8620	5493	570589	895282.7	206987	319.1	203.3	115.7	0.15372	1.94
43	Pd <sub>77.5</sub> Cu <sub>6</sub> Si <sub>16.5</sub>	8095	5135	540724	853184.9	197720	322.2	204.2	118.0	0.15423	1.92
11	Zr45Cu39.3Al7Ag8.7	8771	5555	587261	927964 0	215264	372.0	204.5	110.0	0.15(27	1.01
-+++		1	5555	30/301	527004.0	213304	525.0	204.3	110.5	0.13027	1.91

45	$Cu_{47}Ti_{34}Zr_{11}Ni_8$	8498	5350	575213	913670.5	213082	326.6	205.6	121.0	0.16304	1.89
46	Mg65Cu25Y10	5295	3265	373446	605414.2	143172	340.3	209.9	130.4	0.16512	1.83
47	Zr <sub>65</sub> Cu <sub>17.5</sub> Ni <sub>10</sub> Al <sub>7.5</sub>	8068	4943	577316	942827.2	223614	345.2	211.4	133.8	0.16779	1.82
48	La55Al25Ni5Cu10Co5	5665	3439	413545	681761.2	162498	351.9	213.5	138.5	0.16876	1.79
49	Zr <sub>65</sub> Cu <sub>27.5</sub> Al <sub>7.5</sub>	8065	4878	593270	981345.2	234439	354.5	214.3	140.2	0.17074	1.79
50	La55Al25Ni10Cu10	5610	3368	419486	699075.4	167645	360.1	216.1	144.0	0.18424	1.77

## 7-3 The negative activation energy of Phase 3 in melts

Phase 3 is formed from Liquid 1 and vitrified by heating the quenched amorphous liquid up to  $T_3$ , relaxing an enthalpy equal to  $\Delta \epsilon_{lg0}H_m$  and forming two liquids. The transition at  $T_3$  is viewed as resulting of the formation of broken bonds before attaining the formation temperature of the glass phase at  $T_g$  during the first heating. The glass phase appears as being an intermediate between Phase 3 and liquid during the second cooling. This phenomenon is known in chemistry and characterized by a transition from a positive to a negative activation energy [48]. The occurrence of negative activation energies in gas-phase reactions is explained as being due to the formation of an intermediate complex. Here, the reactants are Liquids 1 and 2, Phase 3 being the product and the glass being the intermediate. We learn from this work that the activation energy equal to zero at  $T_g$  results from the difference between the average energy of the transition state and the delocalization energy  $\Delta e_3$  at  $T_g$ . This property is used to calculate the delocalization energy above  $T_g$ .

The quantities W<sub>3</sub>/RT of five phases 3 are plotted as a function of temperature in Figure 10 for 1ethylbenzene, 2- Au<sub>49</sub>Ag<sub>5.5</sub>Pd<sub>2.3</sub>Cu<sub>26.9</sub>Si<sub>13.3</sub>, 3- Pd<sub>43</sub>Ni<sub>10</sub>Cu<sub>27</sub>P<sub>20</sub>, 4- Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub>, 5- Zr<sub>65</sub>Cu<sub>27.5</sub>Al<sub>7.5</sub>. They are equal to zero at T<sub>a</sub>. The characteristic temperatures T<sub>g</sub>, T<sub>3</sub> and T<sub>a</sub> of these materials and of SiO<sub>2</sub> are given in Table 4. The glass transition occurs at the temperature T<sub>a</sub> for 1, 2, 3, 5 and SiO<sub>2</sub> and at a lower temperature for Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub>. This could also explain why the glass heat capacity is often higher that of crystal below T<sub>g</sub>. The slopes (dW<sub>3</sub>/dT)<sub>Ta</sub> in J/K are used to calculate i for temperatures above and close to T<sub>g</sub> with (33) and they still work at temperatures very close to T<sub>g</sub>. These values of i are the same than those presented in Tables 2 and 3 using  $\Delta e_3$ .



**Figure 10.** The phase 3 activation energy  $W_a/RT = W_3/RT$  plotted versus T (K). Negative activation energy at the temperature  $T_3$  of Phase 3 formation. Activation energy equal to zero at  $T_g$  for the glassy intermediate phase: 1, 2, 3, and 5. 1-ethylbenzene, 2-  $Au_{49}Ag_{5.5}Pd_{2.3}Cu_{26.9}Si_{13.3}$ , 3-  $Pd_{43}Ni_{10}Cu_{27}P_{20}$ , 4-  $Pd_{77.5}Cu_6Si_{16.5.5}$ , 5-  $Zr_{65}Cu_{27.5}Al_{7.5.5}$ 

### Table 4. Characteristic temperatures and enthalpy data

					$(dW_a/dT)_{Ta}$		$\Delta \epsilon_{lg0} H_m / N (J/g-$
	Material	$T_{g}(K)$	$T_3(K)$	$T_a(K)$	(J/K/g-atom)	$i(T \cong T_g)$	atom))
1	Ethylbenzene	114.5	105	114.5	429.6	103.3	91
2	Au49Ag5.5Pd2.3Cu26.9Si16.3	377	370	377	464.3	111.7	974
3	$Pd_{43}Ni_{10}Cu_{27}P2_0$	576	541	576	362	87.1	966
4	Pd <sub>7.5</sub> Cu <sub>6</sub> Si <sub>16.5</sub>	637	572	646.2	421.8	101.5	1696
5	Zr <sub>65</sub> Cu <sub>27.5</sub> Al <sub>7.5</sub>	666	587	666.1	581.7	139.9	2723
6	SiO <sub>2</sub>	1473	1256	1473	168.4	40.5	197

The numbers i determined by the VFT laws used in (32) and applied above  $T_g$  are already high because these numbers associated with kinetic entities are diverging when the temperature tends to  $T_g$  and are expected to be infinite with power laws.

#### 8- The dynamic scaling near a phase transition using VFT laws

The standard statement near a transition at  $T_c$  is the power law given in (40) for the relaxation time [47]:

$$\tau/\tau_0 = (\xi/\xi_0)^z = (1 - T_c/T)^{-z_v} , \qquad (40)$$

where v is the coherence length exponent which is expected to be equal to 0.88 [ (36)]. The coherence length diverges at the transition temperature for a percolation phenomenon and the exponent z is much higher than v [43]. The divergences of the delocalization energies  $\Delta e_1$  and  $\Delta e_2$  of liquids 1 and 2 in ethylbenzene are searched near  $T_3$  and  $T_g$  in Figure 11 using (36,37). The lines  $y_1$  and  $y_2$  are plotted versus  $x_1 = \text{Ln}(1-104.66/\text{T})$  and  $x_2 = \text{Ln}(1-114.5/\text{T})$  respectively following the scaling versus  $\text{Ln}(\xi)$  proposed for percolation phenomena in spin glasses [40,41]. These representations using VFT laws work for 107 K < T < 136 K and 121 K < T < 202.7 K respectively. The exponent value v cannot be confirmed. The ratio  $B_2/T_g$  is expected to be equal to zv [43];  $zv \approx 13$  for the average value in molecular liquids, and 12.7 for metallic glasses while  $B_1/T_3$  is equal to an average value  $zv \approx 9.4$  for molecular liquids, and 9 for metallic glasses. Ratios  $\xi/\xi_0$  are predicted in Table 3 at the melting temperature  $T_{n+}$  of medium-range order applying (40) for  $T_c/T = T_g/T_{n+}$ . Its average value is 2 for BMG and 2.2 for molecular liquids. These values lead to ratios  $\xi/\xi_0$  varying from 135 to 2 and 148.5 to 2.2 when the temperature increases from  $T_g = 114.5$  to 202.74 K while the energy  $\Delta e_3$  is decreased from 429.6T<sub>g</sub> to 24.5T<sub>n+</sub>. The divergence of  $\xi/\xi_0$  towards infinite cannot be attained with VFT laws.



**Figure 11.** Atom delocalization energy  $\Delta e_1$  and  $\Delta e_2$  in liquids 1 and 2 versus  $x_1 = Ln(1-104.66/T)$ and  $x_2 = Ln(1-114.5/T)$ .  $\Delta e_1$  and  $\Delta e_2$  are reduced multiplying them by a numerical coefficient to obtain v = -0.88. Temperature in Kelvin.

# 9- The configuron Gibbs free energy of ethylbenzene, Pd77.5Cu<sub>6</sub>Si<sub>16.5</sub>, and SiO<sub>2</sub> as a function of temperature

This chapter is devoted to the Gibbs free energies of configurons and Phase 3 without using VFT laws. Configurons, which result from bond breaking processes and can be revealed via the minima of X-ray pair distribution functions [38], agglomerate in macroscopic percolating clusters at  $T_g$ . The coherence length in the configuron model is given in (41) [34-36]:

$$\xi(T) = \xi_0 / (f(T) - f_c)^{\nu}, \tag{41}$$

where 
$$f(T) = \frac{\exp\left(\frac{-G_d}{RT}\right)}{\left[1 + \exp\left(\frac{-G_d}{RT}\right)\right]}$$
. (42)

The ground state corresponding to unbroken bonds and the excited state corresponding to broken bonds are separated by an energy interval  $G_d$  which is deduced from (41) and (42):

$$exp\left(\frac{-G_d}{RT}\right) = \frac{f(T)}{[1-f(T)]} , \qquad (43)$$

where

$$f(T) = (1 + f_c - \frac{T_c}{T})$$
(44)

is assumed to be followed by Phase 3 from  $T_c$  to  $T_{n+}$  the melting temperature of medium-range order.

 $G_d$  is the Gibbs free energy of one configuron mole when  $f_c = 0.15 \pm 0.01 = f(T_g)$  is the critical threshold at  $T_g$ . Consequently,  $G_d$  (J/mole) is expected to be equal to (45) at  $T_c$  if this critical threshold value is respected:

$$G_d = 1.7346RT_g = (14.42 \pm 1) \times T_c \quad . \tag{45}$$

Equations (46) and (47) determines the value of  $x_3$  and  $x_g$  depending on equilibrium enthalpies of the glass at  $T_g$  and of Phase 3 at  $T_3$ :

$$\Delta \varepsilon_{lg0} H_m = x_3 \times 14.42 \times T_3 , \qquad (46)$$

$$\frac{\Delta\varepsilon_{lg0}}{2}H_m = x_g \times 14.42 \times T_g , \qquad (47)$$

where  $x_3$  and  $x_g$  are the fractions of  $G_d$  associated with glass-forming melts and  $H_m$  is the melting heat per molecule mole. The atom number N per molecule is given in Table 3. The fraction of configuron mole per g-atom is much weaker and equal to  $x_3/N$  or to  $x_g/N$ .

The phase 3 enthalpy H<sub>3</sub> formed from a fragile liquid is known and equal to  $(-\Delta\epsilon_{lg0}/2\times H_m)$  at T<sub>g</sub>,  $(-\Delta\epsilon_{lg0}\times H_m)$  at T<sub>3</sub> and  $(+\Delta\epsilon_{lg0}\times H_m)$  at T<sub>m</sub>. The Phase 3 entropy being equal to the difference S<sub>1</sub>-S<sub>2</sub> is equal to zero at T<sub>m</sub> and its Gibbs free energy equal to its enthalpy  $\Delta\epsilon_{lg0}\times H_m$ . The configuron entropy is assumed to be equal to zero below the critical temperature. The Gibbs free energy (H<sub>3</sub>-TS<sub>3</sub>)<sub>c</sub> of Phase 3 adapted to that of configurons is represented in Figure 12 along Line 2 from T<sub>3</sub> = 104.66 K to T<sub>n+</sub> = 202.74 K for ethylbenzene starting from an entropy (25.796 J/K/mole +S<sub>3</sub>) = 0 and H<sub>3</sub> = -0.17855 × H<sub>m</sub> = -1637.3 J/mole at T<sub>3</sub>. The Gibbs free energy at T<sub>m</sub> is now equal to -2957 J/mole.



**Figure 12**. *Ethylbenzene: Gibbs free energies of Phase 3 in J/mole and configurons versus T (K). 1- The configuron contribution with a constant fraction*  $x_3 = 1.085$ . 2- *Contribution of configurons to Phase 3 Gibbs free energy. 3- The configuron contribution increase with temperature equal to the difference between (2) and (1).* 

The configuron Gibbs free energy  $G_d$  represented along Line 1 in Figure 12 is calculated assuming that (44) is respected from  $T_c$  to  $T_{n+}$  without change of f(T) = 0.15 and then the Gibbs free energy  $G_d$  given in (43) for all glasses is only depending on  $T_c$  through (45).  $G_d$  is equal to (-1509) J per configuron mole in (45) at  $T_3 = 104.66$  K. In these conditions,  $G_d$  is equal to (-1637.3) J/mole in Figure 12 after applying (46) with  $x_3 = 1.0848$ .

The difference between Line 2 and Line is represented by Line 3 obeying 46.7( $T_3$  -T) in perfect agreement with a thermal dependence of  $\Delta e_3 = -46.3T$  (i = 11.1 using (39)) associated with atom delocalization above  $T_g$  with the freedom degree number i constant up to  $T_{n+}$ .

The same analysis is applied at  $T_g = 114.5$  K in Figure 13 for ethylbenzene. The Gibbs free energy (H<sub>3</sub>-TS<sub>3</sub>)<sub>c</sub> of Phase 3 adapted to configurons is represented in Figure 13 along Line 2 from  $T_g = 114.5$  K to  $T_{n+} = 202.74$  K starting from an entropy (18.311 J/K/mole +S<sub>3</sub>) = 0 and H<sub>3</sub> = -0.08928×H<sub>m</sub> = (-818.7) J/mole at T<sub>g</sub>. The effective value of G<sub>d</sub> is now 818.7 J/mole applying (47) with  $x_g = 0.4958$ . The Gibbs free energy at T<sub>m</sub> is equal to -1624 J/mole. The difference between Line 2 and Line 1 is still represented by Line 3 obeying 27(T<sub>g</sub>-T) and  $\Delta e_{3=}$ -27T in good agreement with the prediction of VFT laws developed in the previous chapter.



**Figure 13.** Ethylbenzene: Gibbs free energies of Glass phase in J/mole and configurons versus T(K). 1- The configuron contribution with a constant fraction  $x_g = 0.496$ . 2- Contribution of configurons to Glass Gibbs free energy. 3- The configuron contribution increase with temperature equal to the difference between (2) and (1).

The Gibbs free energy  $(H_3-TS_3)_c$  per mole of Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> adapted to configurons is represented in Figure 14 along Line 2 from  $T_3 = 572.2$  K to  $T_{n+} = 1218.3$  K starting from an entropy (4.7328 J/K/mole  $+S_3$ ) = 0 and  $H_3 = -0.19839 \times H_m = -1696.1$  J/mole at  $T_3$ . The Gibbs free energy at  $T_m$  is now equal to -3302 J/mole. The Gibbs free energy G<sub>d</sub> is equal to 8251.7 J per configuron mole at  $T_3 = 572.2$  K. In this liquid alloy, the effective Gd is equal to 1696.1 J/mole multiplying 8251 by  $x_3 = 0.2055$  in Figure 14. The difference between Line 2 and Line 1 is represented by Line 3 obeying 8.39 (T<sub>3</sub>-T) and  $\Delta e_3 = -8.39T$  (i = 2.02 using (39)).



**Figure 14.**  $Pd_{77.5}Cu_6Si_{16.5}$ : Gibbs free energies of phase 3 in J/mole and configurons versus T (K). 1-The configuron contribution with a constant fraction  $x_3 = 0.2055$ . 2- Contribution of configurons to Phase 3 Gibbs free energy. 3- The configuron contribution increase with temperature equal to the difference between (2) and (1).

The phase 3 enthalpy H<sub>3</sub> formed from a strong liquid is equal to  $(-\Delta\epsilon_{lg0}\times H_m)$  at T<sub>g</sub>,  $(-\Delta\epsilon_{lg0}\times H_m)$  at T<sub>a</sub> and  $(+\Delta\epsilon_{lg0}\times H_m)$  at T<sub>m</sub>. The Gibbs free energy G<sub>3</sub> = (H<sub>3</sub>-TS<sub>3</sub>) of SiO<sub>2</sub> Phase 3 adapted to configurons is represented in Figure 15 along Line 2 from T<sub>3</sub> = 1256.36 K. The Phase 3 entropy at T<sub>m</sub> being equal to the difference S<sub>1</sub>-S<sub>2</sub> is equal to zero and its Gibbs free energy equal to its enthalpy  $\Delta\epsilon_{lg0}\times H_m$ . G<sub>3</sub> per mole of SiO<sub>2</sub> is represented in Figure 15 along Line 2 from T<sub>3</sub> = 1256.36 K to T<sub>n+</sub> = 2154.6 K starting from (1.062+S<sub>3</sub>) = 0 and H<sub>3</sub> = -0.08754×H<sub>m</sub> = -787.9 J/mole at T<sub>3</sub>. The Gibbs free energy at T<sub>m</sub> is now equal to -1331.9 J/mole. The Gibbs free energy G<sub>d</sub> is equal to 18117 J per configuron mole at T<sub>3</sub> = 1256.36 K. In this liquid alloy, the effective G<sub>d</sub> is equal to -787.9 J/mole multiplying 18117 by x<sub>3</sub> = 0.04348 in Figure 15. The difference between Line 2 and Line 1 is represented by Line 3 obeying 1.88 (T<sub>3</sub>-T) and  $\Delta\epsilon_3$  = -1.88T (i = 0.45 using (39)).



SiO<sub>2</sub>: Configuron Gibbs free energy, T<sub>3</sub> = 1256 K

**Figure 15.**  $SiO_2$ : Gibbs free energies of Phase 3 in J/mole and configurons versus T (K). 1- The configuron contribution with a constant fraction  $x_3 = 0.04348$ . 2- Contribution of configurons to Phase

# *3 Gibbs free energy. 3- The configuron contribution increase with temperature equal to the difference between (2) and (1).*

The Gibbs free energy  $G(H_3-TS_3)_c$  per mole of SiO<sub>2</sub> adapted to configurons is represented in Figure 16 along Line 2 from  $T_g = 1473$  K to  $T_{n+} = 2154.6$  K starting from an entropy  $(0.48084+S_3) = 0$  and an enthalpy equal to zero at  $T_g$ . The Gibbs free energy at  $T_m$  is now equal to -171.9 J/mole. The Gibbs free energy  $G_d$  is equal to (-21243) J per configuron mole at  $T_g = 1473$  K. The effective  $G_d$  is equal to -787.9 J/mole multiplying 21243 by  $x_g = 0.037086$  in Figure 16. The difference between Line 2 and Line 1 with adding +787.9 J is represented by Line 3 obeying 1.376( $T_g$ -T) and  $\Delta e_3 = -1.376$  T (i = 0.33 with (39)) while the VFT model leads to  $\Delta e_3 = 2.06$  T.



**Figure 16.**  $SiO_2$ : Gibbs free energies of Glass phase and configurons versus T(K). 1- The configuron contribution with a constant fraction  $x_g = 0.0371$ . 2- Contribution of configurons to Glass Gibbs free energy with an endothermal latent heat  $\Delta \varepsilon_{lg0} \times H_m$  at  $T_g$ . 3- The configuron contribution increase with temperature equal to the difference between (2) and (1) after transition.

The number i characterizing the entities moving into the melt from  $T_g$  up to  $T_{n+}$  is small and still much smaller for strong than for fragile liquids. It does not depend on temperature due to the medium-range order of Phase 3. The fraction of volume being ordered is constant and equal to  $f_c = 0.15 \pm 0.01$ . The configuron Gibbs free energy  $G_d$  (T) starting from  $T_3$  with zero entropy in strong liquids is viewed as having an equilibrium enthalpy equal to  $-\Delta\epsilon_{lg0} \times H_m$ . It cannot start from  $T_g$  with an entropy and an enthalpy equal to 0 and consequently a latent heat at  $T_g$  is needed to explain the formation of configurons. This latent heat also exists at equilibrium in fragile liquids,  $G_d(T)$  starting with a zero entropy at  $T_3$  and an equilibrium enthalpy equal to  $-\Delta\epsilon_{lg0} \times H_m$  up to  $T_g$ . This case is not considered but even it would lead to a latent heat equal to  $\Delta\epsilon_{lg0} \times H_m$ . This analysis still show that the supplementary configuron number induced above  $T_c$  is proportional to  $(T_c - T)$  in agreement with predictions of Sanditov et al [42] and with the configuron model. A frozen enthalpy equal to the equilibrium enthalpy  $-\Delta\epsilon_{lg0} \times H_m$  of Phase 3 and of glasses is needed up to  $T_g$  to explain the negative value of  $G_d$  at  $T_c$  [34-36]. The Phase 3 formation and configuron models are inseparable.

The main conclusion of this chapter is that the volume fraction of Phase 3 being "ordered" from  $T_3$  up to  $T_{n+}$  involve 15% of all atoms building the 'ordered' melt. The delocalization energy evaluation comparing the Gibbs free energies of Phase 3 and configurons leads to the same value for a fragile liquid than that obtained from VFT laws. The agreement between the two models is not as good for a strong liquid. The two models developed here predict that the atom delocalization energy is proportional to the temperature in agreement with predictions of Sanditov et al [42].

### 10- Gibbs free energy of configurons in 54 glasses at T<sub>3</sub>

The phase 3 enthalpies of 54 melts equal to  $-\Delta \epsilon_{lg0}H_m$  below  $T_3$  are those of configurons. The fraction  $x_3$  has to be multiplied by the configuron Gibbs free energy  $G_d$  at  $T_3$  to obtain  $-\Delta \epsilon_{lg0}H_m$ . The values of  $x_3$  and  $x_3/N$  are given in Table 5 where N is the atom number of each molecule. The melting heat  $H_m$  in

kJ/mole, the enthalpy coefficient  $\Delta\epsilon_{lg0}$ , the Gibbs free energy  $\Delta\epsilon_{lg0}H_m/N$  in J/g.atom equal to  $G_dx_3/N$  and the Gibbs free energy  $G_d$  in Joules per configuron mole calculated with (45) are given in Table 5.

	Materials	N	Hm	<b>X</b> 3	x <sub>3</sub> /N	$\Delta \epsilon_{lg0}$	$\Delta\epsilon_{lg0}*H_m/N$	Gd	G <sub>d</sub> x <sub>3</sub> /N
1	b-D-Fructose	24	32	1.01	0.0420	0.12169	164	3919	164
2	Probucol	83	36	1.16	0.0139	0.13033	56	4022	56
3	Griseofulvin	41	38	1.00	0.0243	0.13083	120	4961	120
4	D-glucose	24	32	1.02	0.0424	0.13214	178	4208	178
5	1,3,5-tri-α-Naphtylbenzene	60	33	1.03	0.0171	0.14211	79	4602	79
6	Phenobarbital	29	28	0.93	0.0319	0.14318	138	4314	138
7	Isopropyl benzene	21	7	0.64	0.0304	0.14689	51	1686	51
8	Hydro-chloro-thiazide	25	34	0.96	0.0383	0.14808	199	5190	199
9	3-Methylpentane	20	5	0.77	0.0384	0.15000	40	1037	40
10	m-Cresol	16	11	0.60	0.0376	0.15210	100	2676	100
11	Xylitol	22	34	1.66	0.0754	0.15922	246	3264	246
12	Phenolphthalein	38	47	1.55	0.0407	0.15947	198	4855	198
13	9-Bromophenanthrene	34	15	0.79	0.0233	0.16012	70	3008	70
14	a-Phenil -cresol	26	23	1.31	0.0503	0.16463	148	2931	148
15	H2SO4-3H2O	16	24.22	1.92	0.1200	0.16667	252	2102	252
16	Diethylphthalate	30	17.99	1.27	0.0422	0.16667	100	2368	100
17	m-Fluorotoluene	15	8.3	0.84	0.0560	0.16576	92	1638	92
18	2-methyl tetrahydrofuran	16	6.65	0.92	0.0577	0.16788	70	1210	70
19	n-Butene	16	3.96	0.88	0.0548	0.17045	42	769	42
20	Toluene	12	6.64	0.73	0.0611	0.17135	95	1551	95
21	Glycerol	15	18.3	1.27	0.0848	0.17466	213	2512	213
22	2-Methylpenthane	14	6.26	1.06	0.0759	0.17500	78	1031	78
23	Ethylbenzene	20	9.17	1.08	0.0542	0.17855	82	1509	82
24	n-Propanol	18	5.4	0.77	0.0427	0.18000	54	1264	54
25	3-Bromopenthane	11	8.4	1.10	0.1001	0.18263	139	1392	139
26	CaAl <sub>2</sub> Si <sub>2</sub> O <sub>8</sub>	17	135.6	1.63	0.0959	0.18306	1460	15233	1460
27	2-methyl-1-propanol	23	6.32	0.85	0.0371	0.18895	52	1398	52
28	Selenium	15	5	0.23	0.0155	0.18851	63	4043	63
29	CaMgSi <sub>2</sub> O <sub>6</sub>	10	138.1	2.10	0.2102	0.19820	2737	13020	2737
30	Butyronitrile	10	5.02	0.79	0.0794	0.19876	100	1256	100
31	cis-/trans-Decalin	12	9.46	1.09	0.0908	0.20346	160	1766	160
32	Ethanol	18	4.98	0.85	0.0472	0.20625	57	1208	57

## Table 5. Materials data used in and resulting from calculations

33	Methanol	9	3.85	0.63	0.0699	0.20930	90	1281	90
34	Ethylene glycol	6	11.86	1.28	0.2142	0.20962	414	1934	414
35	m-Xvlene	10	11.56	1.59	0.1593	0.22000	254	1596	254
	BMG								
36	Pdue Nius Cuas Pas	1	6.82	0.12	0 1 1 9 9	0 13784	940	7844	940
27	$\mathbf{P}_{\mathbf{d}_{0}}^{\mathbf{l}_{10}} \mathbf{V}_{10}^{\mathbf{l}_{10}} \mathbf{C}_{\mathbf{u}_{30}}^{\mathbf{l}_{20}} \mathbf{P}_{\mathbf{u}_{30}}^{\mathbf{l}_{20}}$	1	7.01	0.12	0.1266	0.14000	088	7802	099
37	$Pa_{43}N1_{10}Cu_{27}P_{20}$	1	7.01	0.13	0.1200	0.14090	988	7802	988
38	$Au_{49}Ag_{5.5}Pd_{2.3}Cu_{26.9}Si_{16.3}$	1	5.1	0.16	0.1624	0.17008	867	5341	867
39	$Pd_{40}Ni_{40}P_{20}$	1	9.4	0.21	0.2080	0.17131	1610	7719	1610
40	Pt57.3Cu14.6Ni5.3P22.8	1	11.4	0.33	0.3252	0.19261	2196	6646	2196
41	$Zr_{46}Cu_{46}A_{18}$	1	8.04	0.17	0.1663	0.19595	1575	9311	1575
42	Zr58 5Cu15 6Ni12 8Al10 3Nb2 8	1	8.7	0.19	0.1945	0.19839	1726	8763	1726
43	Pd77 5Cu_Si14 5	1	8.55	0.21	0.2055	0 19904	1702	8251	1702
14	7r, Cu20 2 A 17 A cg 7	1	7.02	0.19	0.1764	0.20169	1500	8045	1500
44	Z145Cu39.3A1/Ag8.7	1	7.95	0.18	0.1704	0.20108	1399	6943	1399
45	Cu47Ti <sub>34</sub> Zr <sub>11</sub> Ni <sub>8</sub>	1	11.3	0.26	0.2623	0.21042	2378	8690	2378
46	$Mg_{65}Cu_{25}Y_{10}$	1	8.65	0.33	0.3322	0.21310	1843	5478	1843
47	Zr <sub>65</sub> Cu <sub>17.5</sub> Ni <sub>10</sub> Al <sub>7.5</sub>	1	10.3	0.26	0.2618	0.21655	2230	8385	2230
48	La55Al25Ni5Cu10C05	1	6.08	0.22	0.2221	0.21780	1324	5926	1324
49	Zt 65Cll 27 5 Al 7 5	1	12.8	0.33	0.3296	0.22036	2821	8457	2821
50	$La_{55}Al_{25}Ni_{10}Cu_{10}$	1	6.82	0.25	0.2542	0.23778	1622	5913	1622

The values of  $x_3$  are plotted in Figure 17 as a function of their number in Table 5 varying from zero to 50; the numbers 51 to 54 are those of SiO<sub>2</sub>, GeO<sub>2</sub>, N-butanol and BeF<sub>2</sub>. There is one configuron mole per mole of Phase 3 for  $x_3 = 1$ . This is true for many glasses in agreement with the configuron model [34-36]. The values  $x_3$  are much smaller for all BMG even for selenium N°28. The Gibbs free energy of BMG configurons is much smaller than those of insulating molecular glasses. Short-range order tends to reduce the configuron contribution and the melting heat by a fraction recovered at higher temperatures than T<sub>m</sub>. The broken bond fraction  $x_3$  is enhanced above 1 in several molecular glasses.



Configuron mole number x<sub>3</sub> per mole of Phase 3

**Figure 17**. Configuron mole number  $x_3$  at the formation temperature  $T_3$  of Phase 3 versus the number in column 1 of Table 5 and vs 51 to 54 for SiO<sub>2</sub>, GeO<sub>2</sub>, N-butanol and BeF<sub>2</sub>.

#### 11- Melt memories

Glass and configuron phases are described by their enthalpy and entropy at equilibrium. They give rise to memory effects up to a temperature  $T_{n+} > T_m$  through medium-range order. Enthalpy relaxation is measured after hours or days and even 1.5 year of isothermal aging in various glasses [127-133]. All these results imply that enthalpy recovery exhibits two times scales of equilibrium in agreement with two activation energies as shown in chapter 7-3. Other high enthalpy reductions are still observed below  $T_{g1}$  after vapor deposition with glass transition temperatures increasing from  $T_{g1}$  to  $T_{g2} \cong 1.1T_{g1}$  and even up to  $T_{g3} \cong 1.2 T_{g1}$ . Thermodynamic properties of isothermally annealed and vapor-deposited glasses characterized by a heat capacity jump equal to  $1.5S_m$  at  $T_g$  are successively analyzed. In all examples, the authors have considered, up to now, that all melts reproduce the enthalpy and the specific heat of the initial liquid and consequently they consider that these melts have no memory of the glass phase transition giving rise to the melt. Our model predicts that the glass phase characterizes and determines the thermodynamic properties of the melt. The following experimental results agree with this assumption.

#### 11-1 Enthalpy recovery of polystyrene PS85k after isothermal aging below Tg1.

The specific heat of this polymer is obtained by D.C. Cangialosi et al using DSC measurements after aging at T = 363 K and represented in Figure 18. Its maximum duration attains 322 days. Its initial glass transition temperature before aging is  $T_{g1} = 379.5$  K and the specific heat difference between melt and glass is 0.3075 J/K/g [128]. The melting entropy is  $S_m = \Delta C_p / 1.5 = 0.205$  J/K/g. The melting temperature  $T_m$  is assumed to be 548 K [134] and the melting enthalpy  $H_m = 112.34$  J/g. The enthalpy coefficients of liquids 1, 2 and 3 are given in (48-50) applying (3-8) for a = 1 and  $T_{g1} = 379.5$  K:

$$\varepsilon_{ls} = 1.69252(1 - 4.3234 \times \theta^2) , \tag{48}$$

$$\varepsilon_{gs} = 1.53878(1 - 3.1703 \times \theta^2), \tag{49}$$

$$\Delta \varepsilon_{lg} = 0.15374 - 2.439 \times \theta^2 \,. \tag{50}$$

The recovered enthalpy after 322 days of aging is 3.2 J/g/K [127]; the corresponding enthalpy coefficient is  $3.2/H_m = 0.0284$ . The glass transition temperature after aging is predicted equal to  $T_{g2} = 389.9$  K with (3) and an increase of  $\varepsilon_{gs0}$  equal to 0.0284. The recovered enthalpy is evaluated from the difference between the specific heat shown in Figure 18 and that of the same sample quenched after aging from  $T_g + 30$  K down to 363 K, the quenched sample having the specific heat of the glass with  $T_{g2} = 389.9$  K instead of  $T_{g1} = 379.5$  K. Consequently, there is a constant difference of enthalpy between the two glass phases which does not contribute to the specific heat.



**Figure 18**: Reproduced from [127] [D. Cangiolasi, V.M. Boucher, A. Alegria, and J. Colmenero, Phys. Rev. Lett. 111 (2013) 095701] with permission of APS. The  $C_p$  scale is equal to 0.5 J/g/K with the agreement of authors. Specific heat versus temperature as obtained by DSC for Polystyrene 85k at different aging times.

The enthalpy coefficients of the aged sample with  $T_{g2} = 389.9$  K are given in (51-53):

$$\varepsilon_{ls} = 1.7115(1 - 4.5568 \times \theta^2) \quad , \tag{51}$$

$$\varepsilon_{gs} = 1.56724(1 - 3.3174 \times \theta^2), \qquad (52)$$

$$\Delta \varepsilon_{lg} = 0.14425 - 2.5998 \times \theta^2) \ . \tag{53}$$

The enthalpy coefficients  $\Delta \epsilon_{lg}$  of configurons before and after aging are represented in Figure 19. After aging, the temperature  $T_{n+}$  and the enthalpy are weakened at high temperature.



## Polystyrene PS85k

**Figure 19**: The enthalpy coefficients  $\Delta \varepsilon_{lg}$  of Phase 3 represented on blue Line 1 before aging and on red Line 2 after aging.  $T_{g1} = 379.5 \text{ K}$ ,  $T_{g2} = 389.9 \text{ K}$ ,  $T_{Br} = 418.9 \text{ K}$ ,  $T_m = 548 \text{ K}$ ,  $T_{n+} = 609.2$  and 613.3 K.

## 11-2 Formation of stable phases by vapor deposition with $T_{g2} \cong 1.1 T_{g1}$

Many new phases with reduced enthalpy have been discovered by vapor deposition below  $T_{g1}$ . The glass transition temperatures  $T_{g2}$  of these thin films are higher than those of bulk materials [135-146]. Cooling these films from above  $T_{g2}$  does not lead to a glass transition at  $T_{g1}$ . The transition after new cooling and reheating leads to a transition at  $T_{g2}$  instead of  $T_{g1}$  in contradiction with all expectations and author conclusions. All these melts are transformed at the new glass transition temperatures  $T_{g2}$ . Melt enthalpy is changed by the increase of  $T_g$ . In Figure 20, the specific heat of ethylene glycol is reproduced as an example among many other vapor-deposited materials with  $T_{g2} = 167$  K,  $T_{g1} \cong 150$  K and  $T_m = 260.5$  K [136,147].



**Figure 20**: Temperature ramping AC nanocalorimetry experiments of ethylene glycol glass. Reproduced from [136] [M. Tylinski, Y.Z. Chua, M.S. Beasley, C. Schick, and M.D. Ediger, J. Chem. Phys. 145 (2016) 174306] with permission of AIP Publishing. The solid colored lines are as-deposited glass while the dashed black curves are liquid-cooled glasses. The curves for different substrates temperatures have been shifted. The noted value of  $T_g$  is the temperature when  $\tau_{\alpha} = 100$  s.

The enthalpy coefficients of liquids 1, 2 and 3 in ethylene glycol are given in (54-59) applying (3-8) for a = 1,  $T_{g1} = 150$  K and  $T_{g2} = 167$  K:

For 
$$T_{g1} = 150 \text{ K}$$
,  
 $\varepsilon_{ls} = 1.57582(1 - 3.3661 \times \theta^2)$ , (54)  
 $\varepsilon_{gs} = 1.36372(1 - 2.593 \times \theta^2)$ , (55)  
 $\Delta \varepsilon_{lg} = 0.21209 - 1.7682 \times \theta^2)$ . (56)  
For  $T_{g2} = 167 \text{ K}$ ,  
 $\varepsilon_{ls} = 1.64107(1 - 3.8199 \times \theta^2)$ , (57)  
 $\varepsilon_{gs} = 1.46161(1 - 2.859 \times \theta^2)$ , (58)

$$\Delta \varepsilon_{lg} = 0.17946 - 2.0904 \times \theta^2) \ . \tag{59}$$

The enthalpy coefficients  $\Delta \epsilon_{lg}$  of configurons before and after aging are represented in Figure 21. After vapor deposition, the temperature  $T_{n+}$  and the enthalpy are weakened above  $T_{g2}$ . The enthalpy coefficient of a lot of vapor-deposited films is nearly equal to  $\Delta \epsilon_{lg0}/2$ . In fact, it is equal to the  $\Delta \epsilon_{lg0}/2$  of the deposited glass at  $T_{g2}$  as shown in Figure 21.



**Figure 21**: The enthalpy coefficients  $\Delta \varepsilon_{lg}$  of Phase 3 represented on blue Line 1 for a bulk material and on red Line 2 after vapor deposition. Temperatures  $T_3 = 132.9$  K,  $T_{g1} = 150$  K,  $T_{g2} = 167$  K,  $T_m = 260.5$  K,  $T_{n+} = 296.7$  and 303.3 K. The enthalpy coefficients of three glass phases are zero,  $-\Delta \varepsilon_{lg0}/2$  and  $-\Delta \varepsilon_{lg0}$ . The third one is not obtained.

## 11-3 Formation of stable phases by vapor deposition with $T_{g3} \cong 1.2T_{g1}$

Highest enthalpy variations and higher values of  $T_{g3}/T_{g1}$  are observed using growth rates spanning 0.001 to 0.1 nm/s for vapor deposition [148,149]. The glass enthalpy is now equal to the enthalpy (- $\Delta\epsilon_{lg0}$ ) of Phase 3. The specific heat of ethylbenzene deposited glass is represented as a function of temperature in Figure 22 and measured during first and second heating separated by slow cooling from temperature higher than  $T_m = 178.1$  K. The melt enthalpy is changed after a glass transition temperature increase from  $T_{g1}=114.5$  K [18,91] to  $T_{g3}=135.7$  K. ( $T_{g3}$ ) is calculated from (1) with  $\Delta\epsilon = 0.17855$ ,  $\epsilon_{gs0} = 1.6429$  and  $\theta_{0g}^2 = 0.34862$  as given by (3,4).



**Figure 22.** Melting temperature of Phase 3 after stabilization by vapor deposition of ethylbenzene films. Reproduced from [148] [E. Leon-Gutierrez, A. Sepulveda, G. Garcia, M.T. Clavaguera-Mora, and J. Rodriguez-Viejo, Phys. Chem. Chem. Phys.12 (2010) 14693-14698] with the permission of Royal Society of Chemistry. Second and subsequent calorimetric upscans (Fast-Cooled samples and FC after SC Slow-Cooling) from vapor deposited samples at different temperatures. Transition temperature at  $T_{g3} = 135.7$  K instead of  $T_g = 114.5$  K for the bulk glass phase.

The enthalpy coefficients of liquids 1, 2 and 3 in ethylbenzene are given in (60-65) applying (3-8) for a = 1,  $T_{g1} = 114.5$  K and  $T_{g3} = 135.7$  K:

$$T_{g1} = 114.5 \text{ K},$$

$$\varepsilon_{ls} = 1.6429 \times (1 - \theta^2 / 0.26075),$$
(60)  

$$\varepsilon_{gs} = 1.46435 \times (1 - \theta^2 / 0.34861),$$
(61)  

$$\Delta \varepsilon_{ls} = 0.17855 - 2.1002 \times \theta^2.$$
(62)  

$$T_{g3} = 135.7 \text{ K},$$
(63)  

$$\varepsilon_{ls} = 1.7619 \times (1 - \theta^2 \times 5.3634),$$
(63)  

$$\varepsilon_{gs} = 1.64285 \times (1 - \theta^2 \times 3.8346),$$
(64)  

$$\Delta \varepsilon_{ls} = 0.11905 + 0.11905/2 - 3.15 \times \theta^2.$$
(65)

The quantity 0.11905/2 is added in (65) to obtain a glass transition with  $\Delta \epsilon_{lg} = 0$  at  $T = T_{g3}$  and an enthalpy change equal to  $\Delta \epsilon_{lg0} \times H_m$  in agreement with Figure 22. The glass transition temperature  $T_{g3}$  is predicted using (1) and  $\Delta \epsilon = \Delta \epsilon_{lg0} = 0.17855$  given in (62). The enthalpy coefficients  $\Delta \epsilon_{lg}$  in (62,65) are represented in Figure 23. After vapor deposition, the temperature  $T_{n+}$  and the enthalpy above  $T_{g3}$  are weakened.



**Figure 23:** The enthalpy coefficients  $\Delta \varepsilon_{lg}$  of configurons represented in black (upper line) for a bulk material and in red (lower line) after vapor deposition. Temperatures  $T_3 = 104.7$  K,  $T_{g1} = 114.5$  K,  $T_{g3} = 135.7$  K,  $T_m = 178.1$  K,  $T_{n+} = 200.8$  and 202.7 K. The enthalpy coefficients of three glass phases 1, 2 and 3 are zero,  $-\Delta \varepsilon_{lg0}/2$  and  $-\Delta \varepsilon_{lg0}$ . The third one is obtained by vapor deposition [148] as shown in Figure 22.

## **Conclusions:**

A new description of glasses is proposed as being intermediate phases masking the initial formation of a supercooled thermodynamic phase which can be superheated. A two-liquid model is

applied, after quenching a melt from high temperatures to a frozen amorphous state, without undergoing any phase transition during the rapid cooling. A subsequent annealing always induces an enthalpy recovery leading to the equilibrium of a new thermodynamic phase called Phase 3 and to that of the glass phase, followed by the glass transition at  $T_g$ . The Gibbs free energy of Phase 3 is equal to the difference of Gibbs free energy  $G_3$  of two liquids. Phase 3 is a new liquid characterized by a mediumrange order which can be superheated up to a temperature  $T_{n+}$  higher than  $T_m$  where this order disappears accompanied by latent heat. The temperatures  $T_3$  and  $T_{n+}$  and the enthalpies changes at these temperatures are predicted for 54 glasses. The existence of this new phase has been searched, thirty years ago, with the power law coming from the dynamic scaling theory which is successfully applied to the phase transition of spin glasses.

An 'ordered' phase 3 now cooled from a temperature weaker than  $T_{n+}$  undergoes a glass transition at  $T_g$  without attaining the equilibrium enthalpies of glass and Phase 3. The glass phase masks the existence of Phase 3 as shown in other chemical transformations. The activation energy of Phase 3 is negative between  $T_3$  and  $T_g$ . The glass transition occurs in many glasses at a temperature where this activation energy is equal to zero. These properties confirm the phase 3 existence behind the glass phase.

The Phase 3 properties are successfully analyzed in the light of configuron percolation theory with a percolation threshold  $\Phi = 0.15 \pm 0.01$ . The Gibbs free energy  $x_3 \times G_d$  of configurons at the critical temperature  $T_c$  is determined from the Gibbs free energy  $G_3$  J/mole of Phase 3 from the assumption that the kinetic 'ordered' entities of Phase 3 involve 15% of all atoms present in the melt up to  $T_{n+}$ . The coefficient  $x_3$  is chosen to equalize  $x_3 \times G_d$  with the equilibrium enthalpies of Phase 3 and glass just below the critical temperature  $T_c$ . The coefficient  $x_3$  is equal to 1 for many molecular glasses in quantitative agreement with the theoretical value of  $G_d$  J/g-atom. This coefficient is much smaller for all metallic glasses. Other molecular glasses have weaker and higher  $x_3$  than one. Another consequence from model proposed is that the glass phase characterizes and determines the thermodynamic properties of the melt.

The enthalpy at  $T_{n+}$  is reduced toward the equilibrium enthalpy of the liquid without mean-range order for which  $\Delta\epsilon_{lg} = 0$ . The average value of the enthalpy coefficient variation  $\Delta\epsilon_{lg}$  at  $T_{n+}$  of 50 fragile liquids is 0.13746 and corresponds to a volume fraction of ordered phase given by the critical threshold equal to 0.15  $\pm$  0.01. The corresponding average for SiO<sub>2</sub>, GeO<sub>2</sub> and BeF<sub>2</sub> is 0.0728.

The size of specific heat jump at  $T_g$  is discussed and the heating rate dependence of the glass transition is accompanied by weak latent heats. The relaxation times above  $T_g$  from fragile Liquid 1 to fragile Liquid 2 of Au<sub>49</sub>Ag<sub>5.5</sub>Pd<sub>2.3</sub>Cu<sub>26.9</sub>Si<sub>13.3</sub> and Zr<sub>65</sub>Cu<sub>27.5</sub> Al<sub>7.5</sub> are predicted in agreement with experiments. The glass transition temperature is lowered when the sample is stored after liquid quenching at a temperature higher than the lowest nucleation temperature in liquid 2 or submitted to long aging before attaining  $T_g$  with the first slow heating. The first-order transition, recently observed, towards a quasi-crystalline phase of Mg<sub>69</sub>Zn<sub>27</sub>Yb<sub>4</sub> is quantitatively predicted at the right temperature with the same equations than those used to explain the formation of glacial phases in water, d-mannitol, triphenyl phosphite, and n-butanol.

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