

# Benchmark of identification methods for the estimation of building wall thermal resistance using active method: Numerical study for IWI and single-wall structures

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Benchmark of identification methods for the estimation of building wall 1 thermal resistance using active method: numerical study for IWI and single-2 3 wall structures 4 Thanh-Tung HA<sup>a</sup>, Vincent FEUILLET<sup>a\*</sup>, Julien WAEYTENS<sup>b</sup>, Kamel ZIBOUCHE<sup>c</sup>, Simon THEBAULT<sup>c</sup>, Rémi BOUCHIE<sup>c</sup>, Véronique LE SANT<sup>d</sup>, Laurent IBOS<sup>a</sup> 5 <sup>a</sup> Univ Paris Est Creteil, CERTES, F-94010 Creteil, France 6 7 <sup>b</sup> Univ Gustave Eiffel, IFSTTAR, Cité Descartes, 14-20 Boulevard Newton, 77420 Champs-sur-8 Marne, France 9 <sup>c</sup> Centre Scientifique et Technique du Bâtiment (CSTB), 84 Avenue Jean Jaurès, 77420 Champs-10 sur-Marne, France 11 <sup>d</sup> Laboratoire National de Métrologie et d'Essais (LNE), 29 Rue Roger Hennequin, 78197 Trappes, 12 France 13 14 \*corresponding author: vincent.feuillet@u-pec.fr; phone: +33 (0)1 45 17 18 43; fax: +33 (0)1 45 15 17 65 51 16 17 **Abstract:** 18 The determination of the thermal resistance of a building envelope is fundamental for the 19 evaluation of the thermal performance of buildings. This could help to evaluate and verify 20 the energy efficiency performance of constructions before renovation, during construction, 21 upon delivery and during use. Some methods exist in the scientific literature but they do not

allow a systematic, accurate and rapid evaluation. This paper presents a numerical

benchmark of identification methods used to estimate the thermal resistance of an opaque

wall. The robustness of each identification technique is investigated in terms of bias and

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uncertainties. The proposed estimation approach is based on an active method, in which the structure is heated in order to create a temperature gradient across the wall, and on the analysis in dynamic regime of the thermal response of the wall. The investigated walls are internal wall insulation (IWI) and single-wall structures (SWS). The results of the numerical study show that RC model-based identification techniques are the most suitable to estimate the thermal resistance of IWI at a very low computational cost. Nevertheless, the modelling error being larger for the SWS than for the IWI, 1D transient heat equations should be preferred for the identification of SWS thermal resistance. The active thermal strategy allows a relevant estimation of the thermal resistance with an observation time of less than 24 h.

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# **Keywords:**

- 37 Building envelope; Thermal resistance; Numerical benchmark; Active method;
- 38 Identification.

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## **Highlights:**

- Assessment of the thermal resistance of opaque building walls
- Comparison of identification methods within the scope of a numerical benchmark
- Analysis of the bias and uncertainties of the inverse methods
- 44 Influence of the wall structure, time observation, outdoor conditions and wall
- 45 orientation

#### 1. Introduction

Thermal insulation of buildings is a key factor to guarantee the thermal comfort of the occupants and to achieve high energy savings. Nowadays the number of uninsulated or insufficiently insulated existing buildings remains quite significant in France. A massive renovation operation is needed in order to upgrade the energy performance of these buildings. The thermal transmittance (*U*-value) of a building wall, closely related to the thermal resistance, can represent its thermal insulation quality. The consumption objectives imposed by the RT2012 in France [1] result in a minimum resistance value of about 4 m<sup>2</sup>.K.W<sup>-1</sup> for an opaque building wall. It is important to notice that these requirements will continue to increase in future regulations. Against this background, it is essential to be able to assess building wall thermal performance before the renovation, during construction, upon delivery, and during use. This would require undertaking an *in situ* measurement.

On the whole building level, methods already exist for identifying the overall thermal performance of the envelope. *In situ* evaluation of a building overall insulation has been a subject addressed in European projects [2] as well as by international research groups in Annex 58 of the IEA [3]. Currently, two approaches have been proposed in the literature to evaluate the overall performance of the envelope:

- identification methods based on indirect measurements used in occupied buildings and on modelling of the building in varying levels of detail: simple thermal balance [4], RC modelling with statistical analysis for the stochastic grey-box model [5];

- measurement methods in controlled heating conditions in unoccupied buildings, avoiding sunlight crossing windowed walls: co-heating method [3], ISABELLE transient state method [6] or Quick U-Building (QUB) method [7].

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The proposed paper concerns the thermal diagnosis at the wall scale. An article presented recently a review of the different passive measurement methods for obtaining the thermal transmittance of various elements of a house [8]: heat flow meter, guarded hot plate, guarded hot box and infrared thermography technique (IRT). Results of laboratory and in situ are under review. Quantitative IRT is considered as the most active area of research for building analysis but the influence of environment and surface characteristics should be quantified. Moreover, the authors show that IRT can be used as a support for other techniques in case of non-homogeneous structures. The determination of the thermal resistance of a wall (or of the U-value) is the subject of two standardized methods, both based on the analysis of a stationary thermal regime. ISO 8990 [9] uses a guarded hot box facility and requires one to four days of experimentation in laboratory, depending on wall thermal inertia, in particular to achieve steady conditions on both sides of the wall. This standard gives a stability criterion on temperatures: the temporal variation shall be less than 1% of the average temperature difference between hot and cold environments. ISO 9869-1 [10] relies on the heat flow meter method. It is an in situ direct method based on the measurement of mean values for internal heat flux and internal and external surface temperatures. However, it requires a measurement time greater than 3 days, stable meteorological conditions and a high temperature gradient across the wall. In addition, this standard indicates a significant measurement uncertainty (between 14 and 28% depending on the type of wall). Several works in literature were derived from the ISO 9869-1

standard. Rasooli et al. [11] proposed revisiting the standard to reduce the in situ measurement durations by using a method called the "Excitation Pulse Method" (EPM), based on the theory of thermal response factors [12]. Same authors recently used this method in [13] to assess several thermo-physical properties of a wall (thermal conductivity, volumetric heat capacity, thickness) but the authors noted that this method is less efficient with heavily insulated walls because of lateral effects. Nowoświat et al. [14] proposed a mean computation of U-value on the whole surface by using internal surface resistance which is evaluated by approximating the internal surface heat transfer coefficient, so as not to have to measure the heat flow rate. Depending on the type of wall, a list of correcting coefficients and disturbed values coming from surrounding conditions and physical characteristics of tested wall are introduced in order to complete all possible influences in computing. The obtained results showed absolute error less than 10 % compared to ISO 9869-1 method in all investigated cases. Certain authors focused on the estimation of the Uvalue when climate conditions change suddenly and proposed modifying the method recommended by the standard by applying moving averages. For this, Naveros et al. [15] used non-linear models that take these various phenomena into account.

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Other reference measurements are carried out with infrared thermography instead of contact sensors in the same context of a pseudo-stationary regime. In Danielski *et al.* [16], the envelope heat transfer coefficient of an external wall was measured thanks to interior infrared measurements over a period of two weeks and a half and steady-state heat transfer equations. Albatici *et al.* developed in several references [17,18] another passive thermographic approach allowing the *in situ* determination of the thermal transmittance of a wall. The method is based on a steady-state heat balance assuming that the conduction

exchange across the wall is equal to the radiation and convection exchange of the wall with the outside. The measurements are all done from the outside of the building. Nardi et al. [19] used the same infrared approach to measure from outside the thermal transmittance of a brick wall coated with an insulating layer of polystyrene. Similar work was developed in [20] but measurements are made from the inside of the building. A similar approach was used by Tejedor et al. [21] to determine in situ U-values of single-leaf walls and multi-leaf walls by means of quantitative internal IRT. The experimental set-up included an IR camera, a reflector, a blackbody, and a thermohygrometer. A temperature difference of 7°C between indoor and outdoor environments is required and only unoccupied buildings can be studied to best meet the steady-state hypothesis. The same authors studied in [22] the influence of operating conditions such as the interior-exterior temperature difference and the type of wall investigated. Kato et al. [23] used passive thermography with additional elements on the wall, i.e. heat transfer coefficient and environmental temperature sensors. An extension of ISO-9869-1 is based on this work and has been published recently [24]. This approach consists in observing the inside surface of the wall to be characterized using an infrared camera and recording a sequence of thermal images for several days (3 to 6 days in the proposed standard).

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Other works rely on identification methods based on contact measurements with thermocouples and flow meters or infrared thermography. Sassine [25] proposed an experimental tool for performing  $in\ situ$  measurements on walls based on a two-port formalism [26]. Authors proposed calculating the theoretical heat flux from R and C values in the literature, then using this theoretical curve to calibrate it to that of the experimental heat flux via ordinary least squares or the gradient descent method (non-linear

optimization) [27]. This approach was also used in [28] to determine the thermophysical properties of a wall using the simplex method. Biddulph et al. used a Bayesian estimation method [29] for simultaneously estimating two thermophysical properties: thermal resistance and thermal inertial. One of the advantages of this method is that it makes it possible to perform measurements in a few days since it does not require reaching steadystate or a minimum difference of 10°C between the interior and exterior temperatures. Another work [30] proposed the development of a Bayesian approach allowing the determination of the thermal properties of a wall (*U*-value and *C*-value) and their associated uncertainties from measurements of near-air internal and external temperatures and internal surface heat flux. The data came from a winter measurement campaign in an occupied UK dwelling over a 14 day period during the winter. The authors considered that a satisfactory estimate of U is possible over a period of one day. Petojević et al. [31] worked on the evaluation of the thermal transmittance based on the thermal impulse response (TIR) and Tikhonov regularization technique. Instead of using classic computations of passive methods, the authors proposed a numerical model of two inputs-two outputs for the tested wall by using the surface temperatures and heat fluxes on the internal and external facades in dynamic conditions. With 105 hours of measurement, this study confirmed the possibility for predicting the dynamic thermal characteristics, cumulative heat losses, heat accumulation, conductive part of thermal transmittance and surface heat fluxes. A measurement protocol of the thermal resistance of an insulated internal wall was established in [32] by using active infrared thermography. The panels were heated using halogen spots placed inside a heating reflector and a step heating excitation was used. Thermal quadrupoles were used to analyze thermogram sequences. An identification

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method led to the estimation of four parameters including the time constant of the insulating layer. The feasibility of this method was proven in laboratory for different multilayered panels fixed onto a building wall.

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The present study is a part of the French National Research project named RESBATI whose main objective is to develop a portable measurement device for evaluating the thermal resistance of opaque building walls on site. The result of the thermal resistance measurement should be provided with its uncertainty. The device will be used not only to assess opaque wall elements after construction, upon delivery of new buildings or for running diagnostics on existing buildings, but also for self-monitoring on construction sites. For new buildings, the assessment will enable auto control for building craftsmen and a guaranty of performance for householders. For existing buildings, assessment before and after refurbishment will allow estimating gain of performance. The device ought to be simple to use and of moderate cost so that it may be acquired and used by craftsmen. The active method is chosen in the project, which is an uncommon approach in the field of measuring the thermal resistance of a wall. It involves artificially producing a thermal excitation so as to create a temperature gradient across the wall being studied, and recording a sequence of temperatures, for instance by using infrared thermography. The RESBATI project aims to demonstrate the strengths of the active approach: the assessment should be able to be carried out at any time of year (low influence of meteorological conditions), for any type of building and use thereof (occupied or otherwise) and for quite short measurement times (around a few hours).

The task "Study of methods robustness" of the RESBATI project aimed to test the physical models and the identification methods of the project partners (CERTES, CSTB,

IFSTTAR, LNE) in the context of a thermal excitation of the wall and the analysis of its response in dynamic regime. This numerical step consisted in conducting an identification method benchmark to evaluate the identification capacity of the inverse methods (estimated value, uncertainty, calculation time) according to the test characteristics (wall type, weather conditions, duration of the test, etc.). This benchmark was a preliminary step to the sizing of the prototype currently tested. This article is devoted to the presentation of the main results of this numerical benchmark. It will focus on the estimation of thermal resistance on opaque walls of buildings with internal wall insulation (IWI) and single-wall structures (SWS).

The article is organized as follows. After the introduction, the considered approach for the comparative study of identification methods is outlined. In section 2, the wall test cases and the different Generating Physical Models (GPM) used to generate the numerical data set are presented. Then, the identification methods to assess the wall thermal resistance are described in section 3. Lastly, the results of the identification methods are analysed and compared in section 4.

#### 2. Methods

## 2.1 General Methodology

The proposed numerical identification benchmark aims to study the robustness of the identification methods used, by comparing:

- the bias of each identification method which is the difference between the thermal resistance value identified by each method and the exact value;
- the uncertainty on this identified thermal resistance value, which is estimated differently for each identification protocol.

It is crucial to investigate the bias to ensure that the exact value of the thermal resistance is inside the uncertainty interval predicted by the identification method. If not, the application field of the identification method should be restricted.

However, the bias estimate requires a perfectly known reference thermal resistance value. For this reason, the benchmark methodology is based on numerical experiments carried out by Generating Physical Models (GPM), in which the physical inputs for each material are perfectly controlled (thermal conductivity, thickness, etc.). By simulating an experiment using these GPMs and identifying the thermal resistance with one of the identification methods, the identified thermal resistance  $\hat{R}$  can be compared to the exact value  $\tilde{R}$  derived from the known input parameters used in the GPM. The reliability of the estimate is therefore verified by carrying out this comparison. It is important to note here that this work does not involve real measurement data, the identifications are based on data calculated in the context of numerical experiments. The global benchmark methodology is described in the following steps:

- Cross-checking the different Generating Physical Models used by each participant, by comparing transient results with well-known analytic solutions of the heat transfer equation (this part will not be presented in this article);
  - Describing several realistic test cases: wall components commonly present in French buildings, boundary conditions, solicitations, etc. (see section 2.2);
    - At a third step, GPMs are used to generate numerical experiments for each test case. The generated data set is then used by each participant in his identification protocol to guess the thermal resistance value and estimate the associated uncertainty. A blind process is considered (only the wall typology, i.e. IWI or SWS is known before conducting the identification). The CERTES was in charge of collecting all exact and identified *R*-values. The results of the blind process are presented in section 4.

# The blind process is summed up in figure 1:

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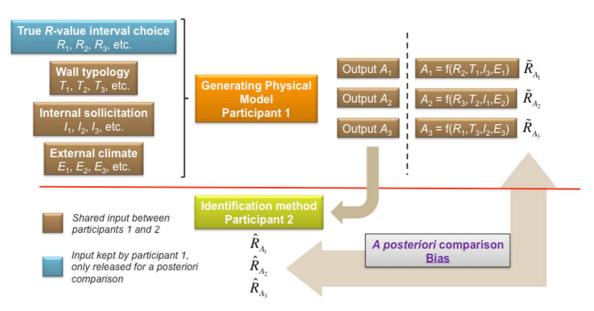


Fig. 1. Blind identification of R-value - benchmark principles.

# 2.2 Description of the test cases

This part presents the inputs and outputs of the test cases to be implemented in the GPMs (described in section 2.3).

#### 2.2.1 Wall structures and properties

The numerical benchmark is based on wall components that are common in French buildings, especially in dwellings. The composition of each layer of the studied wall typologies, i.e. internal wall insulation (IWI) and single-wall structures (SWS), are presented in figure 2. The physical properties of each layer (thermal conductivity, heat capacity, thickness, etc.) have to be chosen by each GPM user into a physical range. The precise chosen values are not sent to other participants so that they can blindly identify the thermal resistance. At the end of the blind process only the CERTES knows all the values in order to make the comparison between exact and identified *R*-values possible.

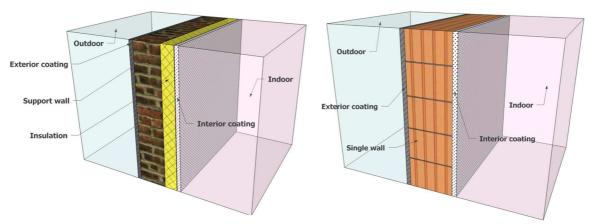


Fig. 2. Internal wall insulation (IWI, left) and single-wall structure (SWS, right) considered in the Generating Physical Models.

Table 1 contains the intervals derived from professional knowledge, for each parameter and each wall component, in which GPM users could choose one specific value

for blind benchmark. These intervals have been constructed for common materials used in these kinds of wall components, physical properties are mainly extracted from French thermal regulation default values [33]. Note that GPMs consider ideal situations regarding the materials constituting the walls. Thus the degradation of the building envelope (joints, bricks, etc.) or the effect of moisture are not taken into account in the simulations.

Wall typology	Layer - number	Thickness e <sub>i</sub> (m)	Thermal conductivity λ; (W.m <sup>-1</sup> .K <sup>-1</sup> )	Density ρ <sub>i</sub> (kg.m <sup>-3</sup> )	Heat capacity c <sub>i</sub> (J.K <sup>-1</sup> .kg <sup>-1</sup> )
	Plasterboard or internal coating - #1	$0.01 \le e_1 \le 0.03$	$0.2 \le \lambda_1 \le 0.8$	$600 \le \rho_1 \le 1500$	1000
IWI	Insulation - #2	$0.04 \le e_2 \le 0.2$	$0.02 \le \lambda_2 \le 0.06$	$30 \le \rho_2 \le 150$	$900 \le c_2 \le 1400$
7.1.7	Support wall - #3	$0.15 \le e_3 \le 0.3$	$0.1 \le \lambda_3 \le 2.3$	$650 \le \rho_3 \le 2500$	1000
	External coating - #4	$0.01 \le e_4 \le 0.03$	$0.3 \le \lambda_4 \le 1.8$	$500 \le \rho_4 \le 2000$	1000
SWS	Plasterboard or internal coating - #1	$0.01 \le e_1 \le 0.03$	$0.2 \leq \lambda_l \leq 0.8$	$600 \le \rho_1 \le 1500$	1000
	Single wall - #2	$0.3 \le e_2 \le 0.4$	$0.1 \le \lambda_2 \le 0.4$	$650 \le \rho_2 \le 1200$	1000
	External coating - #3	$0.01 \le e_3 \le 0.03$	$0.3 \le \lambda_3 \le 1.8$	$500 \le \rho_3 \le 2000$	1000

**Table 1.** Intervals of possible values for wall physical properties involved in the blind numerical benchmark.

#### 2.2.2 Indoor conditions

The active approach planned in the RESBATI project consists in heating a specific zone of the internal wall face (distant from openings and thermal bridges in order to study a 1D heat transfer zone through the wall) with a Heaviside thermal solicitation. A step excitation is thus applied on the heating zone in the simulations (figure 3), i.e. the heat flux  $\Phi_{si}$  applied on the internal wall surface is equal to 0 W.m<sup>-2</sup> during the first hour of the test, then 400 W.m<sup>-2</sup>. As the estimation of the thermal resistance must be rapid, the duration of

the thermal excitation is limited to 24 hours.

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The experimental prototype planned in the project will heat a 0.6 m by 0.6 m wall area. The entire section of the wall considered in GPMs is 2 m by 2 m in order to take into account the 3D effects inevitably encountered in a real measurement situation. The rest of the wall exchanges with the indoor air by convection and radiation. In all the numerical experiments, the indoor air temperature  $T_i$  is fixed at 20°C.

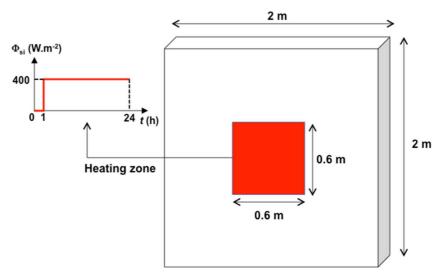


Fig. 3. Schematic view of the internal surface of the wall with the heating zone considered in the Generating Physical Models.

#### 2.2.3 Outdoor conditions

Two external climates over a 24-hour period are considered, extracted from the French thermal regulation inputs [34]:

- H1a (Trappes): from April the 1<sup>st</sup> at 4 pm to April the 2<sup>nd</sup> at 4 pm, north orientation;
- H2d (Carpentras): from October the 1<sup>st</sup> at 10 am to October the 2<sup>nd</sup> at 10 am, south orientation.

These two data sets are used to address different weather conditions, times of day, and wall orientations. The useful climatic inputs from these climate data sets, available for a time step of 5 minutes, are described in table 2.

Input	Unit	Description	
$T_{ m e}$	°C	External air temperature	
dirN	W.m <sup>-2</sup>	Direct normal solar radiation	
diff	W.m <sup>-2</sup>	Diffuse solar radiation	
Gamma	0	Solar altitude	
Psi	0	Solar orientation regarding the south direction (negative in the sunrise)	

**Table 2.** Climatic inputs considered in the Generating Physical Models.

The global incident solar radiation  $\Phi_{sol}$  on the vertical wall is obtained using the following equations, allowing computing direct, diffuse and reflected incident solar radiations on a given wall from climatic data sets [35]:

$$\Phi_{\text{sol}} = \Phi_{\text{dir}} + \Phi_{\text{diff}} + \Phi_{\text{ref}} \tag{1}$$

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$$\Phi_{\text{dir}} = \text{Max}(0; dirN \times \cos(Gamma) \times \cos(Psi - \alpha_z))$$
 (2)

$$\Phi_{\text{diff}} = \frac{\text{diff}}{2} \tag{3}$$

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$$\Phi_{\text{ref}} = \frac{alb}{2} \times (diff + dirN \times \sin(Gamma)) \tag{4}$$

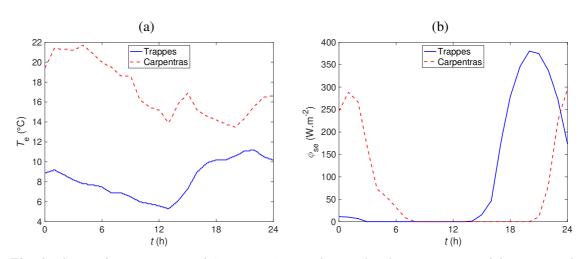
with  $\Phi_{\text{dir}}$ ,  $\Phi_{\text{diff}}$  and  $\Phi_{\text{ref}}$  respectively the direct, diffuse and ground reflected incident solar radiation on the wall,  $\alpha_z$  the wall orientation regarding the south direction (south = 0°, north = 180°) and *alb* the environment external albedo, assumed to be zero (*alb* = 0).

The solar radiation applied on the external surface of the wall  $\Phi_{se}$  is then:

$$\phi_{se} = \alpha_e \times \phi_{sol} \tag{5}$$

with  $\alpha_e$  the external solar absorption coefficient, supposed to be equal to 0.6 (medium color). It should be noted here that longwave radiation with the environment (ground, sky, other buildings, etc.) and latent effects due to moisture and rain are neglected.

Figure 4 shows the two climate data as a function of the observation time t of the numerical experiment in terms of external air temperature  $T_{\rm e}$  and solar radiation applied on the external surface  $\Phi_{\rm se}$ . Relatively different environmental conditions can be observed: the external air temperature for the Carpentras climate is significantly higher than in Trappes and the maximum solar flux occurs at different times of the numerical experiment.



*Fig. 4.* Climate data (Trappes and Carpentras) according to the observation time of the numerical experiment: (a) External air temperature, (b) Solar radiation applied on the external surface.

#### 2.2.4 Initial and boundary conditions

The temperature field inside the wall is initialized by a linear temperature evolution between the internal and external faces.

Boundary conditions are modelled by global indoor and outdoor heat exchange coefficients, taking both convection and radiation into account (see table 3). These conventional values are extracted from the French thermal regulation inputs, referring to [36].

Environment	Global heat exchange coefficients h (convection + radiation) (W.m <sup>-2</sup> .K. <sup>-1</sup> )			
Indoor	7.7			
Outdoor	25			

Table 3. Global heat exchange coefficients considered in the Generating Physical Models.

#### 2.2.5 Data set considered in the Generating Physical Models

In addition to indoor and outdoor conditions described previously, a numerical experiment data set is calculated using GPMs to be used as inputs for identification methods. These computed data include the evolutions of the internal and external wall surface temperatures ( $T_{\rm si}$  and  $T_{\rm se}$ ) and of the heat flux absorbed by heat conduction by the internal wall surface ( $\Phi_{\rm abs}$ ), and are taken at the center of the heating zone shown in figure 3. This data set is presented as time series with 30 seconds time step. Depending on the identification method, it may be resampled before applying the identification protocol. Figure 5 and table 4 describe all the data generated in the data set.

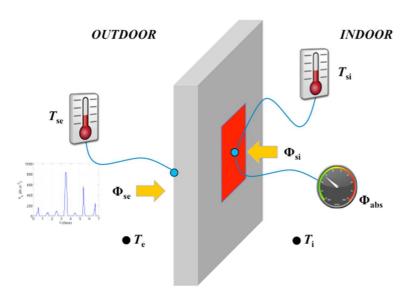


Fig. 5. Locations of data generated in the numerical experiments carried out by Generating Physical Models.

Environment	Data	Notation	Unit
	Internal air temperature	$T_{ m i}$	°C
Indoor	Internal wall surface temperature*	$T_{ m si}$	°C
Indoor	Heat flux applied on the heating zone	$\Phi_{ m si}$	W.m <sup>-2</sup>
	Heat flux absorbed in the wall*	$\Phi_{ m abs}$	W.m <sup>-2</sup>
	External air temperature	$T_{ m e}$	°C
Outdoor	External wall surface temperature*	$T_{ m se}$	°C
	Solar radiation applied on the external surface	$\Phi_{ m se}$	W.m <sup>-2</sup>

**Table 4.** Data set generated in the numerical experiments and used as inputs for identification methods (\*: data computed by the Generating Physical Model).

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After being generated, a realistic measurement noise is added on each computed temperature and heat flux data, in order to evaluate the robustness of each identification method (originally designed for noisy data sets from real measurements). These noises are

obtained experimentally on thermocouples and fluxmetric plates of characteristics similar to those planned in the experimental prototype and were recorded for 72 hours. The noisy data set is then the same for each participant.

#### 2.3 Generating Physical Models

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The Generating Physical Models are used to generate numerical experiments which provide data to be analyzed by each identification method (see section 3) to estimate the thermal resistance of the wall. All GPMs are 3D in order to take into account the transverse heat transfers occurring in the wall in a real measurement situation. Let us remind that a cross-check of each GPM has been performed in a preliminary stage to compare the numerical outputs to known analytical solutions. Each GPM (partners involved: CERTES, CSTB and LNE) is shortly described in the following sections.

#### 2.3.1 CERTES: Thermal quadrupole simulations

A semi-analytic model using the thermal quadrupole method has been developed as GPM (3D QUAD) by CERTES. This method is based on Laplace transform and integral transforms (for multidimensional simulations) of the theoretical heat transfer equation to represent the transient thermal state of a multilayer wall by a matrix relation [37].

Let us first consider a simple homogeneous wall of isotropic material which has limited size  $(L_x \times L_y \times e)$  and whose thermal conductivity and thermal diffusivity are noted respectively  $\lambda$  and a. By using Laplace transform on time variable and Fourier transform in space (see equation (7)), we can simplify 3D transient heat transfer equation by:

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$$\frac{\partial^2 \hat{\theta}}{\partial z^2}(\alpha_n, \beta_m, z, p) = \left(\frac{p}{a} + \alpha_n^2 + \beta_m^2\right) \hat{\theta}(\alpha_n, \beta_m, z, p) = \gamma^2 \hat{\theta}(\alpha_n, \beta_m, z, p) \quad (6)$$

339 with:

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$$\hat{\theta}(\alpha_n, \beta_m, z, p) = \int_0^\infty \int_0^{L_x} \int_0^{L_y} T(x, y, z, t) U(\alpha_n, x) V(\beta_m, y) e^{-pt} dx dy dt \quad (7)$$

where  $U(\alpha_n, x)$  and  $V(\beta_m, y)$  are the eigenfunctions corresponding to eigenvalues  $\alpha_n$  and  $\beta_m$  respectively. The expressions of these eigenfunctions depend on boundary conditions according to [37]. In this study, because of adiabatic condition on the boundaries, cosine and sinus functions are chosen for  $U(\alpha_n, x)$  and  $V(\beta_m, y)$ :  $U(\alpha_n, x) = \cos(\alpha_n, x)$  and  $V(\beta_m, y) = \sin(\beta_m, y)$ . Finally, we can write down a relation of thermal states of two sides of our considered wall using a matrix M, which is called quadrupole transfer matrix:

$$347 \qquad \begin{pmatrix} \hat{\theta}(\alpha_n,\beta_m,0,p) \\ \hat{\varphi}(\alpha_n,\beta_m,0,p) \end{pmatrix} = \begin{pmatrix} ch(e\gamma) & (\lambda\gamma)^{-1}sh(e\gamma) \\ \lambda\gamma sh(e\gamma) & ch(e\gamma) \end{pmatrix} \begin{pmatrix} \hat{\theta}(\alpha_n,\beta_m,e,p) \\ \hat{\varphi}(\alpha_n,\beta_m,e,p) \end{pmatrix} = M \begin{pmatrix} \hat{\theta}(\alpha_n,\beta_m,e,p) \\ \hat{\varphi}(\alpha_n,\beta_m,e,p) \end{pmatrix} \quad (8)$$

with  $\gamma = \sqrt{p/a + \alpha_n^2 + \beta_m^2}$ . The advantage of quadrupole computation is the linearity of matrix calculation. If we have a wall of *n* layers of different materials, the global transfer matrix of whole wall is the product of all individual transfer matrices.

However, the solution obtained is transformed, so several inverse transforms are used to bring this solution back to spatial and temporal spaces. The spatial integral transform is based on expansion of Fourier series of a function, so the inverse of this transform is only the direct Fourier expansion. For Laplace transform, there are several different approaches for inverse transform, theoretically or numerically. After an efficiency comparison, the numerical inversion of de Hoog [38] was chosen as the inverse of Laplace transform because of its accuracy and rapidity in computation.

In addition, external influences such as air temperature, solar radiation or thermal excitation of the internal wall surface, which are also considered in quadrupole computation need to be transformed in Laplace and Fourier spaces. However, they are measured data

which are hardly expressed by a simple analytic function. Therefore, a discrete Laplace transform is applied for these inputs by applying the principle of superposition of linear function transforms. In the case of the thermal excitation which is applied on a limited surface of the internal wall, we fit the spatial form of excitation by a polynomial then calculate theoretically its Fourier transform.

#### 2.3.2 CSTB: VOLTRA simulations

The CSTB used VOLTRA® software which is a thermal analysis program, developed by Physibel® for transient heat transfer in three-dimensional rectangular objects [39]. The time-dependent boundary conditions are described with functions, either built-in functions based on parameters, or external user-functions based on values given at a fixed time interval. Dynamic solar heat gains can be studied using a solar processor. An object image with shadows cast by direct sunlight at any time and any geographic location can be viewed. The direct and diffuse solar radiation from climate data is cast on the material surfaces. The absorbed solar radiation is converted to time dependent node powers, as additional boundary conditions to the system.

VOLTRA allows creating time-dependent graphic animations of moving shadow patterns, calculated temperature and heat flux fields in the studied object. Alphanumeric lists of time functions of temperatures in individual nodes or heat flow through given surfaces through the object can be made.

The transient heat conduction through solid layers is calculated using a semi-implicit finite difference method. Air layers are modelled by an equivalent solid layer, estimated a global thermal conductivity including convection and radiation as described in [36].

Concerning boundaries, two options are available: define global heat exchange transfer coefficients  $h_i$  and  $h_e$ , including convection and radiation or separate heat transfer coefficients between convection ( $h_{ci}$  and  $h_{ce}$ ) and radiation (calculated using emissivities of surfaces and radiant temperatures).

Two experimental validations of the program VOLTRA for simulating 3D transient heat transfer were done using an insulated test box with one transparent side [40]. The simulated temperatures were compared to thermocouple measurements (box surface and air temperatures). The first was carried out under indoor controlled laboratory conditions by investigating the transient heat transfer due to a sudden internal power source. In the second, the experiment box was put in outdoor conditions to validate the solar processor module in VOLTRA. These experimental validations were conducted in the framework of the SBO project IWT 050154 research program "Heat, air and moisture performance engineering. A whole building approach" [41]. Results showed that the software reproduced correctly thermal phenomena such as 2D/3D conduction, solar absorption, infrared radiation and air temperature gradient. Overall the correspondence between measured and simulated temperatures was quite good for the two experiments. The biggest deviations were less than 10 % and could be explained by a simplified empirical convection model and the inaccuracy of some of the boundary conditions.

#### 2.3.3 LNE: COMSOL simulations

A numerical model using the COMSOL Multiphysics® software [42] has been developed by the LNE to study heat transfer in multi-layer walls. The 3D time-dependent problem is solved using finite element method in space and backward differential formula

in time. The algorithm used to solve the system of linear equations is the iterative solver GMRES (generalized minimum residual method). Concerning the spatial discretization, the mesh of tetrahedral elements is automatically adapted according to a mesh quality criterion. Illustrations of the mesh quality and of an internal wall surface temperature are given in figure 6. Concerning the time discretization, a fixed time stepping of 30 s is considered.

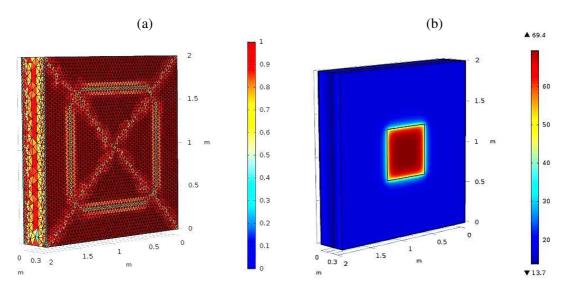


Fig. 6. Example of COMSOL simulation: (a) Mesh quality, (b) Internal wall surface temperature.

For example, for an IWI wall consisting of 4 layers: external coating (0.02 m thick), support wall (0.22 m thick), insulation (0.12 m thick) and internal coating (0.02 m thick), the complete mesh consists of 107170 tetrahedral elements which represents about 64000 degrees of freedom.

# 2.4 Summary of test cases generated in the numerical benchmark

The numerical benchmark of identification methods involves 26 test cases of IWI and SWS walls. Eighteen cases of IWI were generated: 4 walls by CERTES with two different climates, 5 walls by CSTB, and 5 walls by LNE. These cases are numbered from 1 to 18.

Eight cases of SWS were generated: 2 walls by CERTES for two different climates, 2 walls by CSTB, and 2 walls by LNE. They are numbered from 19 to 26. Table 5 details the test cases generated by each GPM user. The corresponding wall thermal resistances are calculated from the material properties of the wall layers chosen by GPM modeller in table 1 and will serve as exact values  $\tilde{R}$  for the estimates carried out by the identification methods.

Test case	Benchmark participant	Generating Physical Model	Wall typology	External climate	Wall orientation	Thermal resistance (m².K.W <sup>-1</sup> )
1						2.75
2	1		IWI	H2d (Carpentras)	South	3.52
3						3.58
4	GEDTEG	3D QUAD				3.90
5	CERTES					2.75
6	1			H1a	Month	3.52
7	1			(Trappes)	North	3.58
8	1					3.90
9		CSTB VOLTRA		H1a (Trappes)	North	0.92
10	CCEP			H2d	South	2.34
11	CSIB			(Carpentras)		4.72
12				H1a	North	5.66
13	1			(Trappes)		8.62
14		COMSOL		H1a (Trappes)	North	1.15
15						3.23
16	LNE					3.52
17						3.58
18	1					8.37
19		DEED 3D OHAD		H2d	South	1.05
20	CERTES			(Carpentras)		1.05
21	CEKIES	3D QUAD		H1a	North	1.05
22			SWS	(Trappes)		1.05
23	CCTD	VOLTRA		H1a	l North	1.53
24	CSTB			(Trappes)		3.34
25	LME	COMPOL		H1a	North	1.05
26	LNE	COMSOL		(Trappes)		3.08

**Table 5.** List of the test cases generated in the numerical benchmark of identification methods.

#### 3. Identification methods

 This section is devoted to the detailed presentation of the identification methods investigated in the numerical benchmark (partners involved: CERTES, CSTB and IFSTTAR).

# 3.1 CERTES: thermal quadrupoles and Bayesian estimation

An identification method, based on Bayesian approach by using the 1D thermal quadrupoles (1D QUAD) as direct model, has been developed by CERTES. With the same expression as equation (8), direct model has only one dimension, then  $\gamma = \sqrt{\frac{p}{a}}$  and only Laplace transform is in use. Because a lot of compositions of wall properties can lead to the same temperature evolution, searching in multidimensional space of parameters seems costly and less robust, so a fixed thickness is defined for each layer according to each type of wall (see table 6) and the identification process tries to estimate thermal conductivity  $\lambda$  and product of density with specific heat capacity  $\rho c$ . The total thickness of the wall  $e_{tot}$  is fixed at a realistic value (0.4 m) and is not estimated in the identification process.

	IWI		SWS		
Layer number	Layer	Thickness $e_i$ (m)	Layer number	Layer	Thickness $e_i$ (m)
#1	Internal coating	0.01	#1	Internal coating	0.01
#2	Insulation layer	$0.4 \times (e_{tot} - 0.02)$	#2	Support wall	e <sub>tot</sub> -0.02
#3	Support wall	$0.6 \cdot (e_{tot} - 0.02)$	#3	External coating	0.01
#4	External coating	0.01		·	

**Table 6.** Layer thicknesses for IWI and SWS ( $e_{tot}$  is the total thickness) considered in CERTES identification process.

Following a sensitivity test for the two types of wall, the temperature on the external surface  $T_{\rm se}$  shows a weak sensitivity related to the parameters of the two first layers in IWI case which are the willing targets to estimate. On the contrary, the temperature on the internal surface  $T_{\rm si}$  presents a high value of sensitivity coefficient in both IWI and SWS cases. Therefore,  $T_{\rm si}$  was chosen as minimization parameter. Bayesian inference is the core algorithm of the identification method. With the random walk of each parameter, we can draw a distribution (or Markov chain) of this parameter following direct model and measured minimization parameter. The most popular method of generating this random chain is Metropolis-Hasting [43,44]. For optimizing Markov chain generator, Vihola [45] proposed a new alternative to the Metropolis-Hastings approach called Robust Adaptive Metropolis (RAM). This algorithm uses a matrix factor S that captures the shape of the target distribution and at the same time allows reaching a given mean acceptance rate. The RAM process can be presented in 5 steps:

- Step 1: Defining a proposal density q which is spherically symmetric, a  $\mathbb{R}^{dxd}$  positive lower-diagonal matrix  $S_1$ , a step size sequence decaying to zero  $\{\eta_n\}_{n\geq 1}\subset (0,1]$ , the target distribution  $\pi$ , the initial point  $X_1\in\mathbb{R}^d$  and the target mean acceptance probability of the algorithm  $\alpha_*$ .
- Step 2: In n<sup>th</sup> iteration, computing  $Y_n := X_{n-1} + S_{n-1}U_n$ , where  $U_n \sim q$ .
- 460 **Step 3:** Computing the probability  $\alpha_n := \min\{1, \pi(Y_n)/\pi(X_{n-1})\}$ , if the proposal is accepted,  $X_n = Y_n$ . Otherwise,  $X_n = X_{n-1}$ .
- **Step 4:** Computing the positive lower-diagonal matrix S<sub>n</sub> which satisfying:

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$$S_{n}S_{n}^{T} = S_{n-1}(I_{d} + \eta_{n}(\alpha_{n} - \alpha_{*}) \frac{U_{n}U_{n}^{T}}{\|U_{n}\|^{2}})S_{n-1}^{T}$$

where  $I_d \in \mathbb{R}^{dxd}$  stands for the identity matrix.

- **Step 5:** Returning to step 2 with  $(n + 1)^{th}$  iteration.

Figure 7 presents step-by-step the identification process. Starting with a set of initial values of physical parameters (noted  $\lambda_{i-ini}$  and  $(\rho c)_{i-ini}$  for  $i^{th}$  layer), normalized parameters A whose initial values are fixed at 1 are considered as estimated parameters to avoid the mismatch of parameter magnitude during estimation. For each set of measurement data, a Markov chain is generated by proposed algorithm, then a nearly Gaussian histogram based on this chain is obtained for each estimated parameter, and mean value and standard deviation can be determined. The final values of  $\lambda_i$  and  $(\rho c)_i$  will be calculated from these values and initial values at the beginning, then the thermal resistance R and its uncertainty will be determined by the two final equations in figure 7. If we have new data set (for instance next hour of measurement), the initial values of normalized parameters for the next process will be replaced by estimation results of the previous data set. This replacement allows limiting seeking zone of Markov chain generation so that computation time can become less costly.

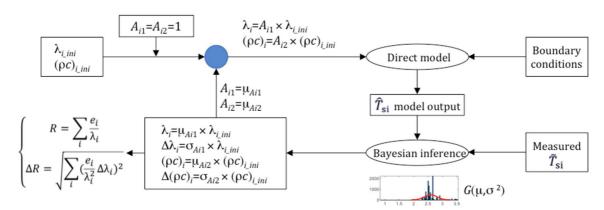


Fig. 7. Overview of the identification process used by CERTES.

#### 3.2 CSTB: RC networks and ISABELE method

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In the CSTB approach (based on the ISABELE method [6]), the thermal behavior of the wall is modelled by a variety of RC networks (all structures are detailed in Appendix A). The corresponding differential equations are converted into stochastic state-space models (of orders 1 to 3). These are simulated to estimate the internal wall surface temperature  $T_{\rm si}$ . The resistances, capacities, initial temperature of the nodes, and model error standard deviations are then adjusted by means of an optimization algorithm to maximize the following likelihood function:

487 
$$L(\theta, T_{si}) = \prod_{k=t_1}^{t_n} \frac{e^{-0.5\epsilon_k^T R_k^{-1} \epsilon_k}}{\sqrt{\det(S_k)}(\sqrt{2\pi})^l}$$
(9)

- 488 where k is the 1-dimensional prediction error, with corresponding covariance matrix  $S_k$ , 489 which is calculated by means of a Kalman filter.
  - All this procedure can be done using the CTSM-R package [46]. The most suitable model is then selected by using likelihood ratio tests [5,6]. The estimated *R*-value of the wall corresponds to the equivalent resistance between the internal and external surface nodes. Its uncertainty can be computed by using the direct formula:

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$$\hat{\sigma}_{R_{wall}} = \sqrt{Jcov(\hat{R}_k)J^T}$$
 (10)

where J corresponds to the Jacobian of the  $R_{wall}$  function (depending on the RC structure) and  $cov(\hat{R}_k)$  to the covariance matrix of the estimated resistances, that is obtained by using Bayesian inversion. In a nutshell, the principle is to decompose the likelihood profile of the optimum (Hessian  $H_{\theta}$ ) by a set of finite-difference derivatives and to decompose its inverse into the following form:

$$H_{\theta}^{-1} = \sigma_{\theta}^T G \sigma_{\theta} \tag{11}$$

where  $\sigma_{\theta}$  is the diagonal matrix of the fitted parameters standard deviations and G the corresponding matrix of correlation. It is assumed that all parameters uncertainties are Gaussian. More details can be found in the CTSM manual [47].

# 3.3 IFSTTAR: 1D finite element method and gradient descent algorithm with adjoint state

In the IFSTTAR approach, the thermal behavior of the wall is modelled by one-dimensional (1D) transient heat equations considering 4 layers (resp. 3 layers) for the IWI (resp. SWS). The system of partial differential equations is solved in a standard way using a finite element method in space and an Euler implicit time integration scheme. Concerning the wall identification, nor the thickness nor the thermal properties are known. To circumvent the inverse problem be ill-posed, we only identify the thermal conductivity and the specific heat capacity of each layer. The layer thicknesses are fixed to mean values derived from physical variation ranges given in table 1. The considered thicknesses of the layers are summarized in table 7. In summary, the strategy consists of identifying the overall thermal resistance of the wall by setting the thickness layers and updating the thermal conductivities.

	IWI		sws		
Layer number	Layer	Thickness $e_i$ (m)	Layer number	Layer	Thickness $e_i$ (m)
#1	Internal coating	0.02	#1	Internal coating	0.02
#2	Insulation layer	0.12	#2	Support wall	0.35
#3	Support wall	0.22	#3	External coating	0.02
#4	External coating	0.02			

Table 7. Layer thicknesses for IWI and SWS considered in IFSTTAR identification process.

The IFSTTAR inverse problem, presented in figure 8, reads as follows: "the model parameters are sought such that it minimizes a datamisfit functional including a Tikhonov regularization term [48]". We consider the internal and external wall surface temperatures in the identification process. The minimization problem is solved using a gradient descent algorithm where the functional gradient is estimated at a low computational cost using the adjoint state. The model updating process stops when the parameter modifications between two successive iterations are less than 0.1 %.

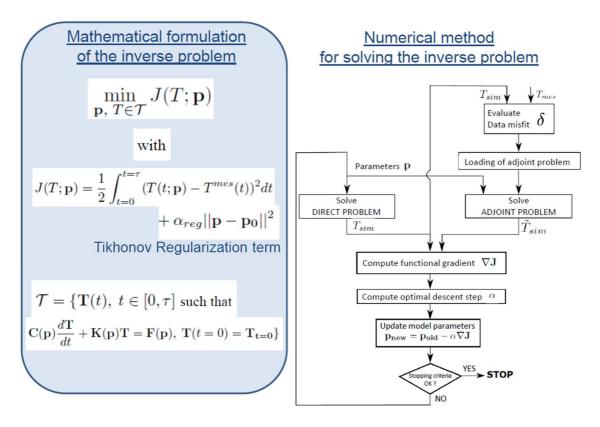


Fig. 8. Overview of the identification process used by IFSTTAR.

Let us note that the scaling regularization parameter  $\alpha_{reg}$ , involved in the functional J in figure 8, is chosen according to L-curve method [49] while ensuring an extended discrepancy principle taking into account both measurement and model errors. Hence, at

the end of the model updating process the data misfit has to be closed and strictly higher than the data misfit threshold defined by:

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$$J_s = \frac{1}{2} \left\{ \int_{t=0}^{t=t_f} (\varepsilon_{meas,ei}^2 + \varepsilon_{mod,ei}^2) dt + \int_{t=0}^{t=t_f} (\varepsilon_{meas,ee}^2 + \varepsilon_{mod,ee}^2) dt \right\}$$
 (12)

where  $\mathcal{E}_{meas,ei}$  (resp.  $\mathcal{E}_{meas,ee}$ ) denotes the measurement error of the temperature sensor at the internal wall surface (resp. at the external wall surface) provided by the numerical experiments and  $\mathcal{E}_{mod,ei}$  (resp.  $\mathcal{E}_{mod,ee}$ ) denotes the model error at the internal wall surface (resp. at the external wall surface). Herein, the model error comes from the simplification of the 3D transient heat problem by 1D transient heat equations. The estimation of the model errors for IWI and SWS is detailed in Appendix B.

The inverse technique provides a deterministic estimation of the model parameters. A confidence interval on the identified thermal resistance is derived from the calculations and the plots of functional iso-values according to the two most sensitive model parameters, i.e. the thermal conductivities of the insulation and the support wall for IWI (resp. the thermal conductivity and the specific heat capacity of the single-wall layer for SWS). For example, we present in figure 9 the iso-values of the data misfit functional for IWI case #15 considering a 12 h time observation, as a function of the dimensionless thermal conductivities of the insulation and the support wall. These dimensionless values, noted with a bar in figure 9, are defined as the ratio of the thermal conductivity and the initial guess of the thermal conductivity  $(0.04 \, \text{W.m}^{-1}.\text{K}^{-1})$  for the insulation layer and  $1.2 \, \text{W.m}^{-1}.\text{K}^{-1}$  for the support wall of the IWI). The model parameters identified by the deterministic IFSTTAR inverse approach are represented using a black cross. In this case, the data misfit functional at the end of the model updating process is  $1.06 \times 10^3 \, ^{\circ}\text{C}^2.\text{s}$ , which

is closed but strictly higher than the modelling error threshold determined in table B.1. Herein, let us note that the measurement error is negligible as regards to the modelling error. Lastly, from the iso-value contour at  $1.06\times10^3$  °C<sup>2</sup>.s, the minimum and the maximum values of the insulation thermal conductivity  $\lambda_2$  and the support wall thermal conductivity  $\lambda_3$  are obtained, which allow estimating a confidence interval on the wall thermal resistance.

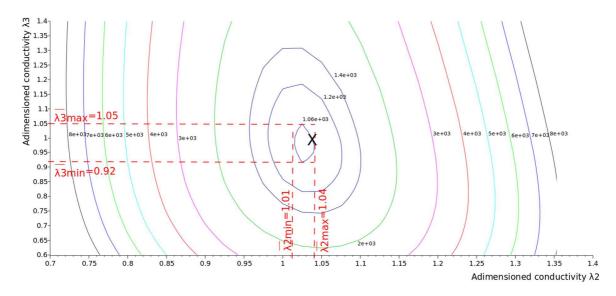


Fig. 9. Contour plot of data misfit functional for IWI case #15 considering 12 h time - the black cross denotes the model parameters identified by the IFSTTAR deterministic inverse approach.

#### 4. Results and discussion

This section presents the main identification results obtained by analyzing the data provided by Generating Physical Models using the three identification techniques detailed in section 3 (CERTES, CSTB, IFSTTAR). The simulations are carried out for 24 hours of thermal solicitation on the wall (step excitation) according to the active approach described in section 2.2.2. We recall that only the wall typology is known before identification.

# 4.1 Study of a particular test case: IWI case #15

Let us first discuss the results for IWI case #15 (see table 5 for details). The internal and external surface temperatures ( $\tilde{T}_{si}$  and  $\tilde{T}_{se}$ ) deduced from the numerical experiment generated by GPM are shown in figure 10(a) for 24 h of analysis. The temperature difference between the beginning and the end of the experiment for  $\tilde{T}_{si}$  is approximately 50°C, the active approach proposed therefore leads to a significant heating of the internal surface of the investigated wall. We can also notice that the external surface temperature  $\tilde{T}_{se}$  is above all sensitive to variations in weather conditions since its increase at the end of the analysis is due to the increase in incident solar radiation (see Trappes solar radiation data in figure 4(b)). On the other hand, the heating of the internal surface seems to have a negligible influence on  $\tilde{T}_{se}$ . Then, figure 10(b) shows the associated residuals at the end of identification processes. This corresponds to the difference between the "measured" temperature  $\tilde{T}_{si}$  (computed with GPM) and that estimated after minimization by each of the identification methods used  $\hat{T}_{si}$ . Overall, the residuals are very close to zero, which shows the ability of identification methods to accurately reproduce the response of the wall following the thermal solicitation. The highest residual values in absolute value appear at

the start of the thermal excitation (t=1 h). This can be explained by the fact that a constant time step is used to solve the direct problem in the identification techniques in order to guarantee a good compromise between the accuracy of the identification and the calculation time. A shorter time step in the vicinity of the thermal solicitation could make it possible to reduce the residuals. It should be noted that the bias appearing at the end of the analysis for the IFSTTAR method could be explained by discrepancy principle constraints of the corresponding identification method (see section 3.3).

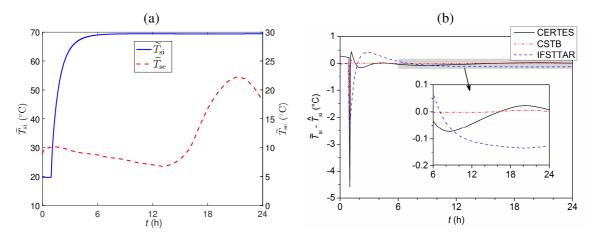


Fig. 10. Results for IWI case #15 of the numerical benchmark for 24 hours of analysis:
(a) Internal and external surface temperatures generated by GPM according to the observation time, (b) Residuals obtained by each identification method according to the observation time.

Let us analyze in figure 11 the evolution of the identified thermal resistance  $\hat{R}$  according to the observation time for the IWI case #15, the exact thermal resistance  $\hat{R}$  being marked by a horizontal line. We see that the active excitation on the internal wall surface and the monitoring of wall surface temperatures has to be conducted at least 8 h with the CSTB and IFSTTAR methods in order to properly determine the thermal resistance of this IWI case, CERTES method requires 20 h to be accurate. The identifications obtained for short analysis times (less than 6 h) lead to an overestimated or under-estimated resistance

depending on the method used. We also observe that the identified resistance by CSTB method undergoes a variation after 20 h of analysis. In fact the quick temperature rise of the external surface temperature due to the increase of the solar radiation at about 20 h (see figure 10(a)) disturbs the CSTB identification model. So it seems that the CSTB identification method is more sensitive to sudden changes in weather conditions.

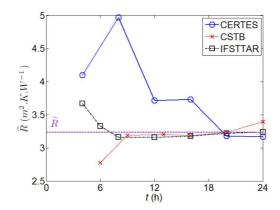


Fig. 11. Identified resistances for IWI case #15 according to the observation time.

#### 4.2 Main results of the numerical benchmark

The thermal resistance  $\hat{R}$  identified by the 3 inverse approaches for IWI and SWS and different observation times are summarized in figure 12. The exact value  $\tilde{R}$  of the thermal resistance is represented in the *x*-axis. For IWI (figures 12(a) and 12(b)), we observe that all the inverse approaches are able to identify the resistance within a 20 % precision, on a large physical range from about 1 m<sup>2</sup>.K.W<sup>-1</sup> corresponding to bad insulated wall to about 9 m<sup>2</sup>.K.W<sup>-1</sup>. Nevertheless, few IWI with a thermal resistance between 3 and 4 m<sup>2</sup>.K.W<sup>-1</sup> are not properly identified, the reason will be explained using figure 13. The increase of the observation time from 12 h to 24 h slightly improves the identification results, especially for the IWI cases, the ratios between the identified resistance and the exact resistance

getting closer to 1. Indeed, 22 identification results are within a 10 % precision for 12 h and 25 identification results are within a 10 % precision for 24 h. Also, as shown in figures 12(c) and 12(d), 1D thermal equations used in CERTES and IFSTTAR inverse techniques have to be preferred for the SWS identifications due to modelling error aspects. Indeed, in Appendix B we show that the modelling error, caused by the simplification of the 3D thermal problem by 1D thermal equations, is higher for SWS than IWI and that it builds up over time. Thus, the identified thermal resistances are less accurate for SWS than IWI, especially for the CSTB approach using the RC model.

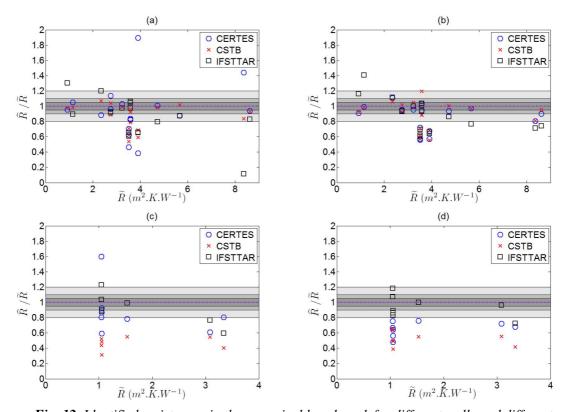


Fig. 12. Identified resistances in the numerical benchmark for different walls and different observation times as a function of the exact resistance:

(a) IWI-12 h, (b) IWI-24 h, (c) SWS-12 h, (d) SWS-24 h.

The identification results for IWI walls are presented according to the total thickness  $e_{\text{tot}}$  of the wall in figure 13. Even for a large observation time of 24 h, we note that all the

inverse techniques fail to identify the thermal resistance when the wall thickness exceeds 45 cm. Figures 12 and 13 show that cases with a large thickness correspond to the cases with a resistance between 3 and 4 m<sup>2</sup>.K.W<sup>-1</sup>. The bad thermal resistances identified for these cases can be explained by the presence of a significant lateral heat flow in the wall which is not taken into account in the simplified models used for the identification leading to an underestimation of the thermal resistance. The most limiting parameter for the identification seems to be the wall thickness, more than the thermal resistance, i.e. it is possible to estimate high thermal resistances with low bias, provided that the thickness of the wall remains less than about 45 cm. This may be due to the fact that transverse heat fluxes in the wall, not taken into account in RC and 1D thermal models, cannot be neglected when the ratio between the wall thickness and the solicitation area dimension is higher than 0.75. Hence, the identification results can be deteriorated because of the modelling error coming from transverse heat fluxes.

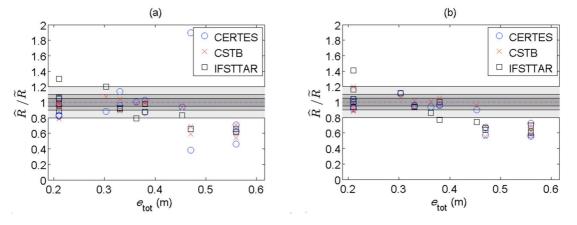


Fig. 13. Identified resistances in the numerical benchmark for IWI walls and different observation times as a function of the total thickness: (a) 12 h, (b) 24 h.

Figure 14 shows all the identification results of each partner in terms of resistance and associated uncertainties. We must note that the bias observed for IWI walls of high

thicknesses is not detected by the calculation of uncertainty. For both IWI and SWS identifications, the thermal resistance confidence intervals derived from IFSTTAR approach are too large for operational use except for few IWI cases around 3 m<sup>2</sup>.K.W<sup>-1</sup>.

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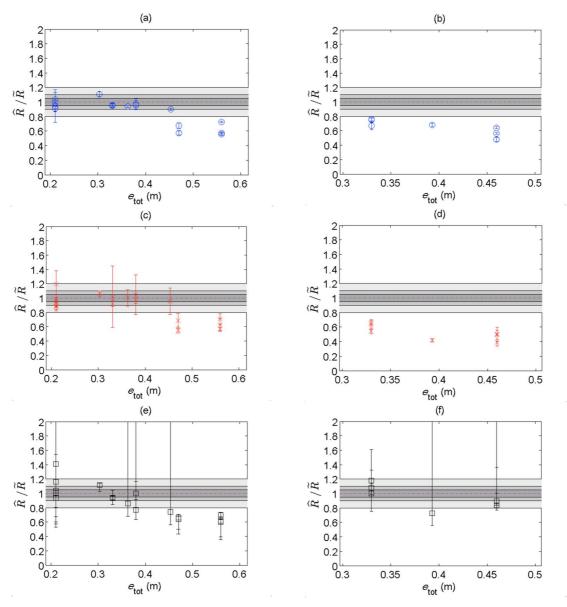


Fig. 14. Identified resistances with associated uncertainties for 24 h time observation as a function of the total thickness: (a) CERTES-IWI, (b) CERTES-SWS, (c) CSTB-IWI, (d) CSTB-SWS, (e) IFSTTAR-IWI, (f) IFSTTAR-SWS.

As all the lower values of IFSTTAR confidence intervals (except for thick wall cases discussed previously) are strictly less than the exact thermal resistance, these lower values can eventually be used as a thermal resistance lower bound. For IWI walls, let us note that the best identification results are obtained using CSTB technique. Indeed, the identified resistance ranges for all the studied cases, except the thickest considered walls, are accurate and include the exact thermal resistance value.

As shown in table 5, some IWI (cases 1 to 8) and SWS (cases 19 to 22) cases were generated by CERTES for two French climate scenarios (H1a/Trappes and H2d/Carpentras described in section 2.2.3) to study the influence of the weather and of the wall orientation on the identification process. The couple cases 1-5, 2-6, 3-7, 4-8 (IWI) and 19-21, 20-22 (SWS) refer to the same walls but with different climate scenarios and wall orientations. We can see in figure 15 that all the identified thermal resistances by the inverse techniques are almost the same for both climate scenarios and wall orientations. The differences observed between two different climates and wall orientations in terms of identified resistance for all the methods are on average 5.5 % and 7.4 % in absolute value, respectively for the IWI and SWS walls. These small differences show that the heating of the internal surface induced by the active approach (see figure 10(a)) is sufficient not to be dependent on weather conditions, time of day or wall orientation. This constitutes an important practical advantage compared to the passive methods of the literature.

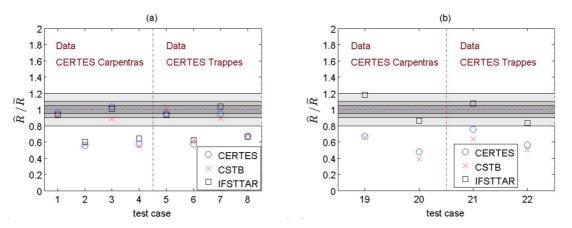


Fig. 15. Identified resistances for 24 h time observation and two French climate scenarios and wall orientations: (a) IWI, (b) SWS.

Tables 8 and 9 present a summary of the benchmark results. The first one provides the numbers of resistance values identified at plus or minus X % of the exact value. It shows that the identification technique proposed by CSTB is the most appropriate for characterizing IWI while it is preferable to use the IFSTTAR technique for SWS. Thus the RC model seems to be suitable for IWI but it is necessary to use more elaborate models (at least 1D transient heat equation) for SWS. In addition, we observe that the increase in the analysis time from 12 h to 24 h does not significantly improve the identification results. Concerning the calculation times involved in this benchmark (see table 9), we can underline that the RC model considered in the CSTB approach allows an identification of the thermal resistance at a very low computational cost.

## IWI - 18 test cases

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12 h	CERTES	CSTB	IFSTTAR
±5 %	5	7	3
±10 %	6	10	6
±20 %	12	12	9

24 h	CERTES	CSTB	IFSTTAR
±5 %	6	6	3
±10 %	10	9	6
±20 %	13	13	9

## SWS - 8 test cases

12 h	CERTES	CSTB	IFSTTAR
±5 %	0	0	2
±10 %	1	0	4
±20 %	4	0	5

24 h	CERTES	CSTB	IFSTTAR
±5 %	0	0	2
±10 %	0	0	3
±20 %	0	0	7

**Table 8.** Numbers of resistance values identified by the three identification methods at plus or minus X % of the exact value for each wall structure and different observation times (yellow color and bold font boxes refer to the identification method(s) that obtain(s) the best score at a given percentage).

		CERTES	CSTB	IFSTTAR
1	2 h	390	20	540
2	4 h	877	20	720

**Table 9.** Average calculation times (in seconds) for the three identification methods and different observation times.

## 5. Conclusion

The present work consists in a numerical benchmark of identification methods for estimating the thermal resistance of building walls and is dedicated to the study of internal wall insulation (IWI) and single-wall structures (SWS). This numerical study is a part of the ANR RESBATI project whose main objective is to develop a portable measurement device for evaluating the thermal resistance of opaque building walls on site. Methodologies exist in scientific literature but do not allow a systematic and rapid measurement. We propose an active method using a thermal excitation (step excitation) on the internal surface to create a temperature gradient across the wall and recording a sequence of temperatures. The originality of the proposed method consists in associating the active approach with a dynamic regime analysis of the temperature response of the wall using a robust identification method. The method should provide the value of the thermal resistance of the wall and its associated uncertainty. This purely numerical work represents an important task in the current context of improving energy efficiency of existing and new buildings.

The main goal of the numerical benchmark is to evaluate the robustness of different identification methods, by comparing the bias and uncertainties of each method. First, Generating Physical Models (thermal quadrupoles, COMSOL and VOLTRA softwares) are used to generate numerical experiment data as part of a blind process, that is to say benchmark participants do not know thermal resistances of the walls being studied. Then, three identification methods use data sets provided by the numerical experiments and the estimation results are examined. The first one (CERTES) uses thermal quadrupoles and

Bayesian estimation. The second method developed by CSTB involves RC networks and ISABELE method. The last one led by IFSTTAR is based on 1D finite element method and gradient descent algorithm with adjoint state.

Benchmark results show that RC models (0D model) used in the CSTB method are relevant to identify the thermal resistance of IWI at a very low computational cost. 1D transient heat equations (CERTES and IFSTTAR) should be preferred to RC models, due to modelling error, for the identification of SWS thermal resistance. Thanks to the active thermal strategy, we can expect a relevant *in situ* estimation of the thermal resistance with an observation time of less than 24 h. This numerical benchmark also shows that the meteorological conditions and the wall orientation do not impact the results of the three studied identification processes. This demonstrates the flexibility of using the active approach.

However, it appears that estimating the wall thermal resistance becomes difficult when the ratio between the wall thickness and the solicitation area dimension is higher than 0.75. This can be explained by significant transverse heat fluxes in the wall, the estimation results are in that case deteriorated due to an excessive modelling error. To tackle the issue of transverse heat flux, 2D axisymmetric thermal equations can be considered to improve the thermal resistance identification results, notably for SWS. A circular shape of the excitation area would be used instead of the square shape considered in the article which is more convenient for the experimental design. To drastically reduce the computation time to solve the 2D thermal equations and thus getting a fast thermal resistance identification process, we propose to use model order reduction techniques like the "Proper Generalized Decomposition" [50,51].

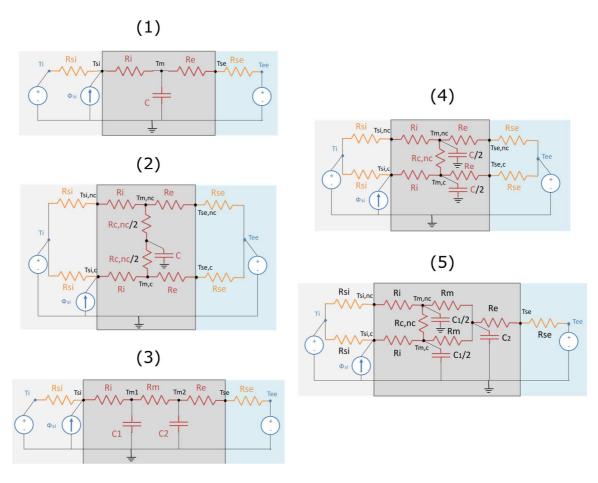
Other types of walls (External Thermal Insulation Composite System, wood frame wall) will be investigated in this numerical approach. After this numerical benchmark step, experiments on IWI and wood frame walls with sensor outputs will be conducted to test the robustness of the identification methods in real conditions, first under controlled laboratory conditions then *in situ*.

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# Appendix A: RC structures of the CSTB method and related equations

Figure A.1 presents all RC structures used in the CSTB method to evaluate the thermal resistance of a wall under dynamic conditions [52].



*Fig. A.1.* Illustration of proposed RC structures for the simplified thermal dynamics of the wall (CSTB method).

Parameters in blue correspond to the boundary conditions (measured temperatures, heat flows). Resistances in yellow refer to know resistances. Capacitances and resistances in red correspond to the unknown parameters to optimize. It is important to note that the uncertainty on these boundary conditions (temperatures, heat flows, known resistances)

- should be considered under real experimental conditions. Nevertheless, it can be neglected
- 742 under simulation conditions.
- 743 **Model 1:**
- Figure A.1(1) presents the simplest RC structure. The corresponding single state
- 745 equation is:

746 
$$C\frac{dT_m}{dt} = (R_e + R_{se})^{-1}(T_{ee} - T_m) + (R_i + R_{si})^{-1}(T_i - T_m) + \frac{R_{si}\Phi_{si}}{R_i + R_{si}} + \sigma_m \frac{d\omega_m}{dt}$$
(A.1)

747 The observation equation is:

$$T_{si} = \frac{R_i T_i + R_{si} T_m + R_i R_{si} \Phi_{si}}{R_i + R_{si}} + \varepsilon(\sigma_{Tsi,mes})$$
(A.2)

749 The corresponding *R*-value and uncertainty are calculated by the following equations:

$$\hat{R}_{wall} = \hat{R}_i + \hat{R}_e \qquad (A.3)$$

751 
$$\hat{\sigma}_{Rwall} = \sqrt{Jcov(\hat{R}_i, \hat{R}_e)J^T} = \sqrt{cov(\hat{R}_i, \hat{R}_e)} \text{ as } J = (1 \quad 1) \quad (A.4)$$

- 752 **Model 2**:
- Figure A.1(2) presents another RC structure taking into account the lateral heat
- 754 transfer within the inner face of the wall. The corresponding single state equation is:

755 
$$C\frac{dT_{m}}{dt} = \frac{4(T_{ee} - T_{m})}{2R_{e} + 2R_{se} + R_{cnc} + \frac{(R_{e} + R_{se})R_{cnc}}{R_{i} + R_{si}}} + \frac{4(T_{i} - T_{m}) + 2R_{si}\Phi_{si}}{2R_{i} + 2R_{si} + R_{cnc} + \frac{(R_{i} + R_{si})R_{cnc}}{R_{e} + R_{se}}} + \sigma_{m}\frac{d\omega_{m}}{dt}$$
756 (A.5)

757 The observation equation is:

$$T_{si,c} = \frac{R_i T_i + R_{si} T_{m,c} + R_i R_{si} \Phi_{si}}{R_i + R_{si}} + \varepsilon(\sigma_{Tsi,mes})$$
(A.6)

759 with:

760 
$$T_{m,c} = \frac{2(R_e + R_{se})(R_i + R_{si})T_m + R_{cnc}(R_i + R_{si})T_{ee} + R_{cnc}(R_e + R_{se})T_i + R_{cnc}(R_i + R_{si})(R_e + R_{se})\Phi_{si}}{2(R_e + R_{se})(R_i + R_{si}) + R_{cnc}(R_i + R_{si}) + R_{cnc}(R_e + R_{se})}$$
(A.7)

The corresponding R-value and uncertainty are calculated the same way as in Model 1.

## 763 - **Model 3**:

Figure A.1(3) presents a 2-order RC structure. The corresponding state equations are:

765 
$$C_{1} \frac{dT_{m1}}{dt} = R_{m}^{-1} (T_{m2} - T_{m1}) + (R_{i} + R_{si})^{-1} (T_{i} - T_{m}) + \frac{R_{si} \Phi_{si}}{R_{i} + R_{si}} + \sigma_{m1} \frac{d\omega_{m1}}{dt}$$
766 (A.8)

767 
$$C_2 \frac{dT_{m2}}{dt} = R_m^{-1} (T_{m1} - T_{m2}) + (R_e + R_{se})^{-1} (T_{ee} - T_{m2}) + \sigma_{m2} \frac{d\omega_{m2}}{dt}$$
768 (A.9)

769 The observation equation is:

770 
$$T_{si} = \frac{R_i T_i + R_{si} T_{m1} + R_i R_{si} \Phi_{si}}{R_i + R_{si}} + \varepsilon(\sigma_{Tsi,mes})$$
(A.10)

771 The corresponding *R*-value and uncertainty are calculated by the following equations:

$$\hat{R}_{wall} = \hat{R}_i + \hat{R}_m + \hat{R}_e \quad (A.11)$$

773 
$$\hat{\sigma}_{Rwall} = \sqrt{Jcov(\hat{R}_i, \hat{R}_m, \hat{R}_e)J^T} = \sqrt{cov(\hat{R}_i, \hat{R}_m, \hat{R}_e)} \text{ as } J = \begin{pmatrix} 1 & 1 & 1 \end{pmatrix}$$
 (A.12)

## 774 - **Model 4**:

- Figure A.1(4) presents another RC structure taking into account the lateral heat
- transfer within the inner face of the wall. The corresponding state equations are:

777 
$$\frac{C}{2}\frac{dT_{m,c}}{dt} = R_{c,nc}^{-1}(T_{m,nc} - T_{m,c}) + (R_e + R_{se})^{-1}(T_{ee} - T_{m,c}) + (R_i + R_{si})^{-1}(T_i - T_{m,c}) + \frac{R_{si}\Phi_{si}}{R_i + R_{si}} + \sigma_{m,c}\frac{d\omega_{m,c}}{dt}$$
778 
$$(A.13)$$

779
780 
$$\frac{C}{2} \frac{dT_{m,nc}}{dt} = R_{c,nc}^{-1} \left( T_{m,c} - T_{m,nc} \right) + \left( R_e + R_{se} \right)^{-1} \left( T_{ee} - T_{m,nc} \right) + \left( R_i + R_{si} \right)^{-1} \left( T_i - T_{m,nc} \right) + \sigma_{m,nc} \frac{d\omega_{m,nc}}{dt}$$
781 (A.14)

782 The observation equation is:

785

$$T_{si,c} = \frac{R_i T_i + R_{si} T_{m,c} + R_i R_{si} \Phi_{si}}{R_i + R_{si}} + \varepsilon(\sigma_{Tsi,mes})$$
(A.15)

784 The corresponding R-value and uncertainty are calculated the same way as in Model 1.

# 786 - **Model 5**:

- Figure A.1(5) presents the most complex RC structure taking into account the lateral
- heat transfer within the inner face of the wall. The corresponding 3 state equations are:

789 
$$\frac{C_1}{2} \frac{dT_{m,c}}{dt} = R_{c,nc}^{-1} \left( T_{m,nc} - T_{m,c} \right) + R_m^{-1} \left( T_{m2} - T_{m,c} \right) + (R_i + R_{si})^{-1} \left( T_i - T_{m,c} \right) + \frac{R_{si} \Phi_{si}}{R_i + R_{si}} + \sigma_{m,c} \frac{d\omega_{m,c}}{dt}$$
790 (A.16)

791

792 
$$\frac{C_1}{2} \frac{dT_{m,nc}}{dt} = R_{c,nc}^{-1} (T_{m,c} - T_{m,nc}) + R_m^{-1} (T_{m2} - T_{m,nc}) + (R_i + R_{si})^{-1} (T_i - T_{m,nc}) + \sigma_{m,nc} \frac{d\omega_{m,nc}}{dt}$$
793 (A.17)

794

800

795 
$$C_2 \frac{dT_{m2}}{dt} = R_m^{-1} (T_{m,c} - T_{m2}) + R_m^{-1} (T_{m,nc} - T_{m2}) + (R_e + R_{se})^{-1} (T_{ee} - T_{m2}) + \sigma_{m2} \frac{d\omega_{m2}}{dt}$$
796 (A.18)

797 The observation equation is:

$$T_{si,c} = \frac{R_i T_i + R_{si} T_{m,c} + R_i R_{si} \Phi_{si}}{R_i + R_{si}} + \varepsilon(\sigma_{Tsi,mes})$$
(A.19)

799 The corresponding *R*-value and uncertainty are calculated the same way as in Model 3.

# **Appendix B: Estimation of modelling error (IFSTTAR method)**

As described in section 3.3, IFSTTAR inverse procedure takes into account the modelling error due to the simplification of the three-dimensional (3D) thermal problem to one-dimensional (1D) transient heat equations. To estimate the modelling error on the temperatures at the internal and external wall surfaces, about 500 sets of parameters have been randomly drawn in agreement with the variation range of the considered wall typology given in table 1. For each set of parameters (corresponding to 4 layer thicknesses, 4 conductivities and 4 thermal capacities for a IWI wall), the 3D wall thermal problem is solved using standard finite methods and Implicit Euler time integration scheme with the software CESAR-LCPC [53] and the computed temperatures  $T3d_i(t)$  and  $T3d_e(t)$  at the inside and the outside faces of the wall are stored. Likewise, the numerical temperatures  $T1d_i(t)$  and  $T1d_e(t)$  at both faces of the wall are obtained solving a 1D transient heat problem. From that, we can evaluate on a time interval  $[0; t_f]$  the cumulative modelling error  $J_{ME}$  and the indicative temperature modelling error  $T_{ME}$  defined by:

815 
$$J_{ME} = \frac{1}{2} \int_{t=0}^{t=t_f} ((T3d_i - T1d_i)^2 + (T3d_e - T1d_e)^2) dt$$
 (B.1)

$$T_{ME} = \sqrt{\frac{J_{ME}}{t_f}}$$
 (B.2)

The cumulative and the temperature modelling errors are represented in figures B.1 and B.2 for the IWI wall and the single wall respectively for the time interval  $[0; t_f=12 \text{ h}]$ . A modelling error threshold is shown in red. It is defined such that 80 % of the IWI walls (resp. the single walls) have a cumulative modelling error less than this threshold. In practice, the modelling error threshold is used in the IFSTTAR inverse technique. We observe that the modelling error is higher for the single wall than the IWI wall. Indeed, on a

 $12\ h$  time interval,  $80\ \%$  of the single walls have a temperature modelling error less than

# 0.2°C, whereas it is less than 0.15°C for the IWI walls.

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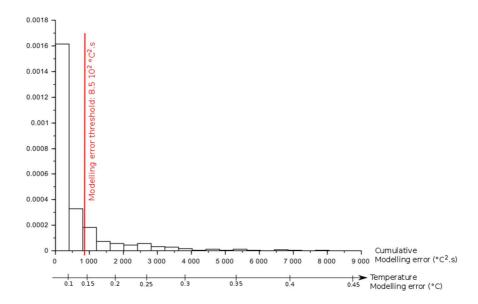


Fig. B.1. Distribution of cumulative and temperature modelling errors for IWI wall for a 12 h time interval, computed from about 500 numerical simulations.

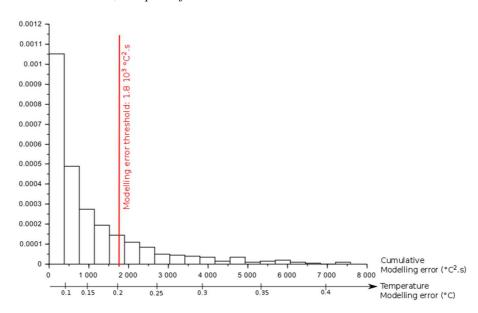


Fig. B.2. Distribution of cumulative and temperature modelling errors of Single wall for a 12 h time interval, computed from about 500 numerical simulations.

Finally, we summarize in tables B.1 and B.2 for IWI and single walls the modelling

error threshold and the associated temperature modelling error for several time intervals (also beyond 24 h). For IWI and single walls, we note an increase of the modelling error when considering bigger time intervals. Tables B.1 and B.2 also show that the modelling error is higher for the single wall than the IWI wall. For a 72 h time interval, the temperature modelling error of the single wall is four times bigger than the one of the IWI wall. To conclude, we highlight that the inverse procedure may lead to inaccurate identification results when considering a large time interval as 72 h and/or single wall typology due to excessive modelling error.

		12 h	24 h	48 h	72 h
Mo thr	odelling error eshold (°C <sup>2</sup> .s)	$8.5 \ 10^2$	4.2 10 <sup>3</sup>	1.5 10 <sup>4</sup>	2.8 10 <sup>4</sup>
	Cemperature elling error (°C)	0.14	0.22	0.29	0.33

**Table B.1.** Modelling error threshold and associated temperature modelling error for IWI for several time intervals.

	12 h	24 h	48 h	72 h
Modelling error threshold (°C <sup>2</sup> .s)	$1.8\ 10^3$	2.9 10 <sup>4</sup>	2.1 10 <sup>5</sup>	4.9 10 <sup>5</sup>
Temperature modelling error (°C)	0.2	0.58	1.1	1.37

**Table B.2.** Modelling error threshold and associated temperature modelling error for SWS for several time intervals.

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