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Abdelhak Mekahlia, Eric Semail, Franck Scuiller, Hussein Zahr

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Impact of Winding Parameters on Torque Level under Harmonic Injection in Multiphase Induction Machine

Abdelhak Mekahlia
Univ. Lille, Centrale Lille, Arts et
Metiers ParisTech, HEI, HeSam, EA
2697 - L2EP - Laboratoire
d'Electrotechnique et d'Electronique
de Puissance.
Lille, France.
Institut Vedecom.
Versailles, France.
abdelhak.mekahlia@vedecom.fr

Eric Semail
Univ. Lille, Centrale Lille, Arts et
Metiers ParisTech, HEI, HeSam, EA
2697 - L2EP - Laboratoire
d'Electrotechnique et d'Electronique
de Puissance.
Lille, France.
eric.semail@ensam.eu

Franck Scuiller
IRENAV – Research Institute of Naval
Academy, BCRM Brest – EN/GEP
Brest, France
franck.scuiller@ecole-navale.fr

Hussein Zahr
Institut Vedecom.
Versailles, France.
hussein.zahr@vedecom.fr

Abstract—Multiphase induction machines have the advantage of producing torque under different current harmonics. Theoretically, with some simplifications, the maximum produced torque can be considered proportional to the harmonic winding factor related to the injected current harmonic. However previous work has shown that this theoretical proportionality between the maximum developed torque and harmonic winding factors is not obtained in the case of a five-phase induction machine with eight-poles and fractional-slot tooth concentrated winding. This paper aims to investigate the effect of winding parameters, especially phase number, fundamental polarity and stator slots number, on the torque production in multiphase induction machine under harmonics injection. A comparative study is done between four five-phase winding configurations, with the same geometry and copper volume, under both first and third harmonic injection. Finally, a special 15-phase winding presenting better consistency between maximum developed torque and harmonic winding factors is proposed.

Keywords—Multiphase Induction Machine, Harmonic Winding Factors, Harmonics Injection, Fundamental Polarity.

I. NOMENCLATURE

- s_{pp} : Number of slots per pole and per phase
- N_s : Number of stator slots
- p_1 : Number of pole-pairs under first harmonic injection (called fundamental polarity in the paper)
- p_h : Number of pole-pairs (or the polarity) under injection of harmonic “h”
- k_{hi} : Winding factor related to harmonic “i”
- D_{ph-pp} : Coils distribution vector per phase and per pole-pair
- ω_s : Stator pulsation (stator current fundamental frequency multiplied by 2π)
- ω_r : Rotor pulsation (rotor current fundamental frequency multiplied by 2π)
- Ω_{mec} : Mechanical speed
- s : Slip.
- F-E: Finite Element

II. INTRODUCTION

The multiphase induction machine is becoming more and more attractive in several applications as automotive [1], naval

[2] and aeronautics [3]. Thanks to the possibility of producing smooth torque by more than one current harmonic, unlike the three-phase machine, the multiphase machines offer more degrees of freedom, especially regarding torque density improvement [4] [5], speed-range extension [6] and fault-tolerant operating [7] [8]. This kind of machines is supplied by multiphase inverters for variable speed operations.

Classically in a three-phase induction machine, overlapping windings with distributed coils are widely used, thanks to their sinusoidal winding function which permits to optimize machine performance especially reduction of torque ripple [9]. More attractive windings regarding the ease of manufacturing like tooth concentrated windings, have a rich space harmonics content, and they are not considered appropriate for three-phase machines, where the presence of harmonics impacts negatively the performances.

In multiphase machines, the harmonics are separated into different sets. A harmonic of one set does not interact with other harmonics from another set. Hence, the main harmonic from each set can be injected to produce torque without impacting its quality. In this case, not only overlapping windings can be chosen, but also other configurations like tooth-concentrated windings. In fact, the presence of harmonics is useful for torque production and enhancement [10], [11].

While torque is produced by more than one current harmonic, one should determine which harmonics have a high torque capability. This is possible by calculating the harmonic winding factors resulting from the winding distribution. Considering classical theoretical approach these factors reflect the level of developed torque for each injected harmonic. Nevertheless, a previous study with F-E modeling has shown that in the case of five-phase induction machine with a fundamental polarity $p_1=4$, and a tooth concentrated winding with $s_{pp}=0.5$, even though the third harmonic winding factor is higher than the first one, the developed torque under third current harmonic injection is lower than the one under first current harmonic supply [12].

In this paper, the impact of winding parameters on torque level in multi-phase induction machines is investigated. Firstly, the consistency between harmonic winding factors and maximum developed torque under both first and third current

harmonics supply is studied for different five-phase integral-slot pole-concentrated windings.

These windings are chosen, because they allow to maximize the first and third harmonics winding factors and cancel even-order winding factors.

Finally, a special 15-phase winding, with relatively short end-coils, and which leads to a better consistency between harmonic winding factors and torque capability under different current harmonics injection is proposed.

All the machines presented in this paper are supplied by sequential current harmonics. This supply mode allows to improve the speed range of multiphase machines [6][13][14].

III. CHOSEN FIVE-PHASE WINDINGS

In a previous paper on the effect of the rotor bar number on the performance of five-phase induction machine [12], F-E simulation results were presented for a five-phase induction machine, with the following parameters :

- 20 stator slots
- 4 pole-pairs (fundamental polarity)
- Tooth concentrated winding with $spp = 0.5$
- First harmonic winding factor $k_{h1} = 0.59$
- Third harmonic winding factor $k_{h3} = 0.95$
- 5 different rotor bar numbers: 13, 18, 35, 64, 65

This study has shown that the maximum developed torque under the third current harmonic supply is lower than that under the first harmonic for all bar numbers, while the third harmonic winding factor k_{h3} (0.95) is higher than k_{h1} (0.59).

The winding chosen in this study generates both odd and even space harmonics [12], and the second space harmonic has the same winding factor as the third harmonic. In this case the interaction between the second space harmonic and the third current harmonic produces a negative torque [10] (both are in the same harmonics set) which complicates the interpretation of torque production under third current harmonic injection.

To avoid that, in this paper, we have chosen four overlapping windings, that do not generate space harmonics of order multiple of $2p_1$.

A. Windings specifications

Four five-phase winding configurations are chosen:

- Winding 1: $N_s = 40$, $p_1 = 4$, $spp = 1$
- Winding 2: $N_s = 20$, $p_1 = 2$, $spp = 1$
- Winding 3: $N_s = 40$, $p_1 = 2$, $spp = 2$
- Winding 4: $N_s = 20$, $p_1 = 1$, $spp = 2$

Fig. 1 shows the four machines geometry with coils distribution for phase 1.

To determine the harmonic winding factors, the Discrete Fourier Transform (DFT) of conductor distribution function inside the slots can be used [15], TABLE I shows the calculation of these factors from the first to the fourth space harmonic.

In a five-phase induction machine, there are two independent sets of harmonics [16]. The primary set contains the harmonics: 1, 4, 6, 9..., the secondary set contains the harmonics: 2, 3, 7, 8..., and all the multiples of 5 (number of phases) belong to the zero sequence. In the case of overlapping

windings all even harmonics are null, so if the first current harmonic is injected, it interacts with the 1st, 9th, 11th ... space harmonics, and the third current harmonic interacts with the 3rd, 7th, 13th ... space harmonics.

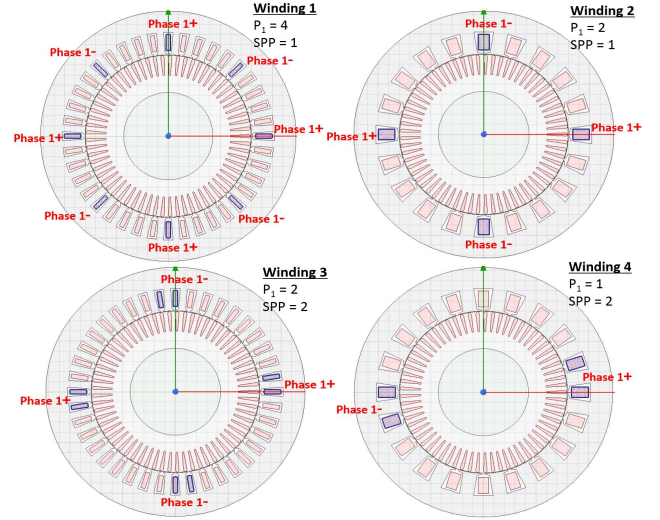


Fig. 1: Machines geometry and coils distribution in phase 1.

TABLE I. HARMONIC WINDING FACTORS DETERMINATION

Winding	D_{ph-pp}	k_{h1}	k_{h2}	k_{h3}	k_{h4}
1	[1 0 0 0 0 -1 0 0 0 0]	1	0	1	0
2	[1 0 0 0 0 -1 0 0 0 0]	1	0	1	0
3	[1 1 0 0 0 0 0 0 0 0 -1 -1 0 0 0 0 0 0 0 0]	0.99	0	0.89	0
4	[1 1 0 0 0 0 0 0 0 0 -1 -1 0 0 0 0 0 0 0 0]	0.99	0	0.89	0

B. Machines dimensions

For the 4 winding configurations, the same stator and rotor dimensions and the copper volume are taken. Global dimensions and parameters are specified in the TABLE II.

TABLE II. GLOBAL MACHINES DIMENSIONS AND PARAMETERS

Parameters	Value
Stator external diameter	246 mm
Stator internal diameter	160 mm
Shaft diameter	86 mm
Airgap length	0.5 mm
Machine length	157 mm
Rotor bar number	65
Stator copper volume (without considering end coils)	484 cm ³
Rotor copper volume (without considering end connection)	458 cm ³
Rated phase current (RMS)	173 A

These dimensions are close to some examples of machines used in traction applications like Tesla Model-S asynchronous motor and ISCAD concept [14].

Rotor bar number is chosen from results of previous work [12].

IV. FINITE-ELEMENT SIMULATIONS

The objective of these simulations is to study the torque capability of the four machines under both first and third current harmonic supply.

For each machine, the torque curves in function of rotor pulsation are determined using Maxwell software (Ansys), under the rated stator RMS current.

All simulations are done with a time step size equal to the period of the injected stator current divided by 20. An element length-based mesh refinement is imposed on: the stator coils, rotor bars and on a circle drawn in the middle of the airgap.

A. Poles distribution under first and third harmonic supply

Cartographies of flux lines in the 4 machines are shown in Fig. 2. These maps clearly show the number of magnetic poles induced in the machine by the current supply, that changes from p_1 to $3p_1$ when the third current harmonic supplies the winding.

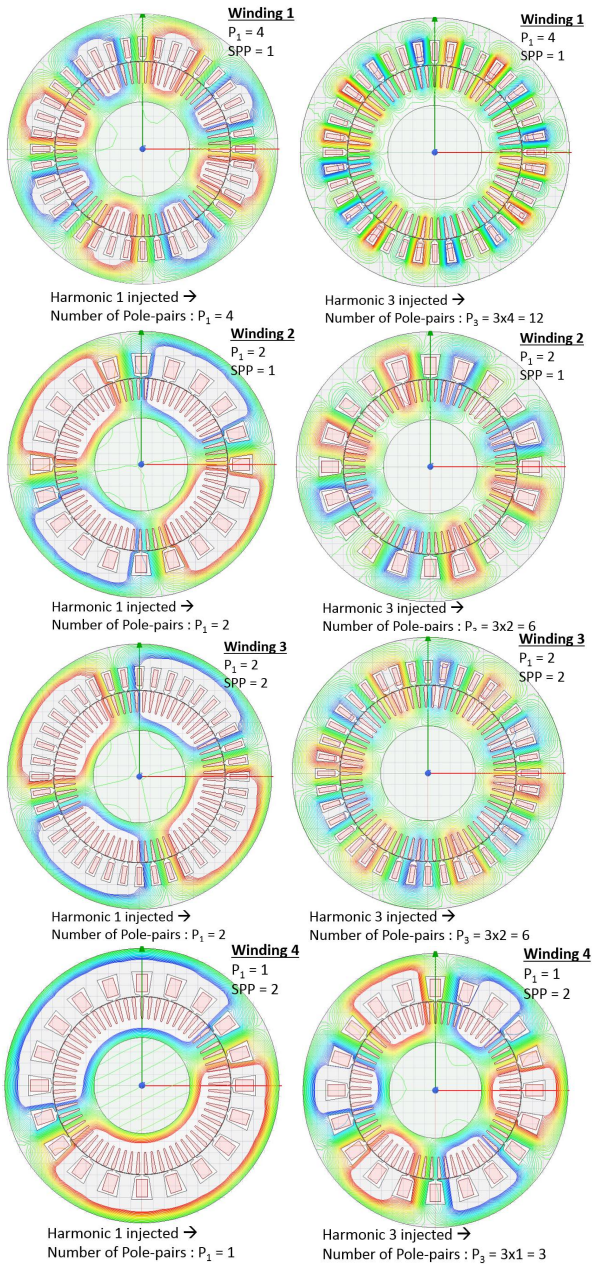


Fig. 2: Poles distribution under first and third harmonic supply

B. Torque analysis under rated current

To determine the maximum torque that can develop the machines in steady state, F-E simulations, with parametric variation of the slip, have been done. The slip is defined for all supply modes as below:

$$s = \frac{\omega_s - p_h \cdot \Omega_{mec}}{\omega_s} \quad (1)$$

Where the stator pulsation ω_s is defined as:

$$\omega_s = h \cdot 2 \cdot \pi \cdot f_{s1} \quad (2)$$

f_{s1} is the stator current frequency under the first harmonic supply, equal to 50 Hz for all simulations.

The number of pole-pairs changes with injected harmonic range. It can be defined as:

$$p_h = h \cdot p_1 \quad (3)$$

Where “h” is the rank of the injected harmonic.

So, the rotor currents fundamental pulsation can be defined as:

$$\omega_r = s \cdot \omega_s \quad (4)$$

In the next four figures (from Fig. 3 to Fig. 6) the torque curves for the 4 machines are drawn according to the rotor currents fundamental pulsation defined in equation (4).

F-E simulations with parametric variation are time-consuming, especially for induction machine where it takes relatively long time to reach the numerical steady-state due to rotor currents establishing (around 20 stator current periods, which takes many hours depending on the step time). For the chosen machines, to determine precisely the torque variation, for a given slip value, a transient simulation of more than 600 time-points (for example simulation time of 600 ms with a step of 1 ms) must be done. Hence only some slip-points are simulated (slip values around the maximum torque point), that explains why the torque curves in the next figures do not start from zero-slip point, and do not have the same length.

TABLE III reports the obtained maximum torque points for the 4 machines under first and third harmonic supplies. Torque ripple values are determined basing on torque variation after numerical steady-state is reached by dividing the peak-to-peak value by the mean value. The obtained torque ripple levels are considered acceptable for the 4 machines.

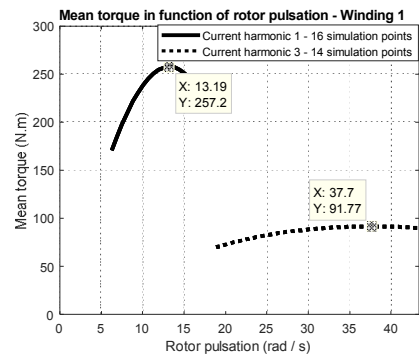


Fig. 3: Mean torque curves for the winding 1

For the winding 1 (Fig. 3), the fundamental polarity is $p_1=4$, the maximum torque mean value under the first

harmonic supply is 257 N.m, even though the first and third space harmonic winding factors k_{h1} and k_{h3} are equal to 1, the maximum developed torque under the third harmonic supply is just 36% lower than the torque with the first current harmonic.

By using the winding 2 (Fig. 4), the fundamental polarity is reduced to $p_1=2$, the first current harmonic maximum torque is reduced to 236 N.m (8% of reduction from winding 1) due to the number of stator slots which is going from 40 to 20 (coupling factor between stator and rotor is better with a higher number of slots). However, the maximum torque developed under the third harmonic supply is enhanced with this winding (92% of enhancement comparing to winding 1), but it is still lower than the first current harmonic maximum torque, whereas $k_{h3}=k_{h1}=1$. Flux leakages are probably increased with the third harmonic current supply, thus justifying this reduction.

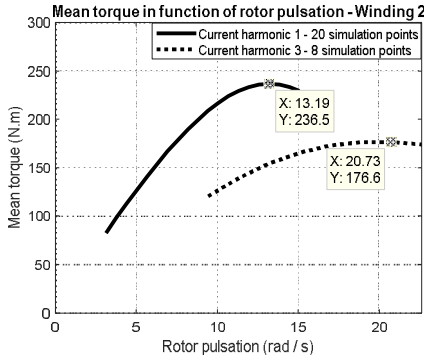


Fig. 4: Mean torque curves for the winding 2

So, we can analyze the low torque capability under the third harmonic injection in winding 1, by the high number of pole-pairs $p_3=12$ (24 magnetic poles) which induces important rotor losses, in Fig. 2 it can be observed that the number of induced magnetic poles under 3rd harmonic for this winding is very high for the 40 stator slots. Furthermore, the rotor pulsation at third harmonic maximum torque for the winding 1 is 37.7 rad.s⁻¹ (almost double of the value for winding 2), hence the rotor losses are more important for a higher rotor currents pulsation.

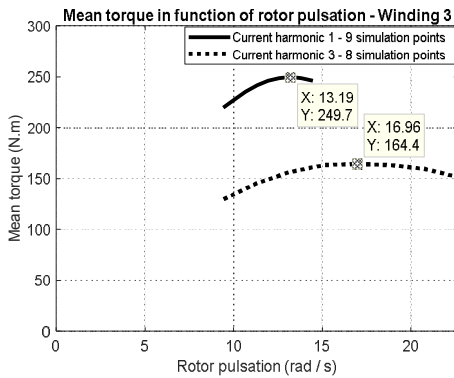


Fig. 5: Mean torque curves for the winding 3

For the winding 3 (Fig. 5), the fundamental polarity is kept $p_1=2$, and the number of stator slots is again 40. In this case the number of slots per pole and per phase equals two, thus reducing the winding factors ($k_{h1}=0.99$ and $k_{h3}=0.89$). Maximum developed torque under first harmonic supply reaches 250 N.m (6% of enhancement comparing to winding 2) thanks to a higher number of stator slots, whereas torque

level under third harmonic supply is slightly reduced due to a lower third harmonic winding factor (k_{h3} -winding3 is 89% of k_{h3} -winding2).

For the winding 4 (Fig. 6), the harmonic winding factors are the same as with the winding 3 ($k_{h1}=0.99$ and $k_{h3}=0.89$), as shown in TABLE I. The fundamental polarity is $p_1=1$ so the polarity under third harmonic injection passes from 6 to 3 pole-pairs, thanks to that the torque level under this harmonic is enhanced comparing to the winding 3 (33% of enhancement). However, the torque under the first harmonic supply is significantly reduced (55% of reduction). In fact, the stator and rotor yoke height are not well adapted to a such low polarity ($p_1=1$), so the saturation effect is very significant in these regions.

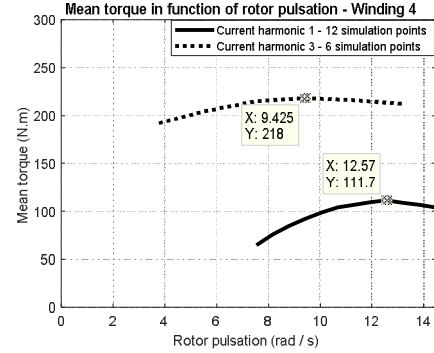


Fig. 6: Mean torque curves for the winding 4

TABLE III. MAXIMUM DEVELOPED TORQUE AND ROTOR PULSATIONS VALUES

	Winding 1		Winding 2		Winding 3		Winding 4	
Harmonic	H1	H3	H1	H3	H1	H3	H1	H3
Pole-pairs	4	12	2	6	2	6	1	3
k_{hi}	1	1	1	1	0.99	0.89	0.99	0.89
Max torque (N.m)	257	92	236	177	250	164	112	218
Torque Ripple (%)	1.3	3.8	1.2	6	0.5	2.5	4.3	7.3
Rotor pulsation @Max torque (rad.s ⁻¹)	13.2	37.7	13.2	20.7	13.2	17	12.6	9.4

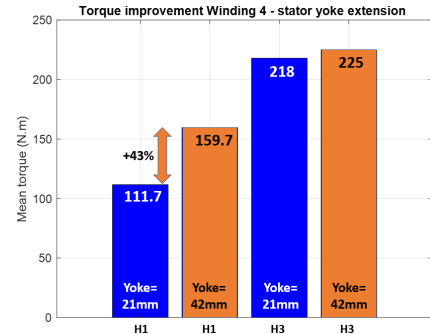


Fig. 7: Maximum torque improvement by stator yoke extension with the winding 4

To confirm the reason of the torque reduction under first current harmonic for the winding 4, new simulations are done with an extended stator yoke height (from 21 mm to 42 mm),

so the volume of the machine is increased of 17.8% (copper volume is not increased). The results are shown in Fig. 7. Torque enhancement thanks to stator yoke extension is of 43% under first harmonic supply, and the torque level is still lower than the one under 3rd harmonic supply. In fact, it is not only stator yoke that must be extended, but also rotor yoke which is highly saturated, as seen in Fig. 2 (Map for “Winding 4” under 1st harmonic). That was not done in this study because it would modify completely the dimensions of the machine.

For the winding 4, we can conclude that the machine volume and weight must be increased to obtain the suitable torque level under first harmonic, so the torque density of the machine is very low comparing to winding 2 and 3, even if it develops a higher torque under 3rd harmonic.

Through this investigation of five-phase windings, it can be concluded that it is complicated to conceive a five-phase machine with the suitable consistency between maximum developed torque and harmonic winding factors. For this reason, a higher number of phases, could offer more degrees of freedom regarding the winding design, as presented in the next section.

V. 15-PHASE PROPOSED WINDING

As seen in the previous section, in the case of five-phase induction machine, even with overlapping windings (where even harmonics are null) it is difficult to choose a winding ensuring a consistency between developed torque under harmonics injection and harmonic winding factors.

With a higher number of phases, the harmonics are more and more separated into different sets, so the presence of even space harmonics could be advantageous, on the contrary of three-phase or five-phase machines.

If we take the example of 15-phase machine, the harmonics are separated into 7 sets (and one zero-sequence) [16], as described in TABLE IV. In this case, the even harmonics are useful and could be injected to produce a torque of good quality thanks to the reduced harmonics interactions (comparing to 3-phase and 5-phase machines), so the use of overlapping winding is no longer preferable.

TABLE IV. DISTRIBUTION OF HARMONICS INTO 7 SETS FOR 15-PHASE WINDING

Sets	Harmonics ranges
1 st set	1, 14, 16...
2 nd set	2, 13, 17...
3 rd set	3, 12, 18...
4 th set	4, 11, 19...
5 th set	5, 10, 20...
6 th set	6, 9, 21...
7 th set	7, 8, 22...
Zero-sequence	15, 30, 45 ...

As seen before, the fundamental polarity of a multiphase winding for induction machine must be as low as possible. In the case of a five-phase winding, if we choose $p_1=1$ we can only increase the number of stator slots, thus resulting in higher “spp”, and consequently reducing the harmonic winding factors. In the other hand, with $p_1=1$ the stator and rotor yokes must be enlarged to develop the suitable torque level (as seen for the winding 4). However, in the case of 15-

phase winding, we can choose a fundamental polarity $p_1=1$, with an acceptable number of stator slots and a low “spp” (for example: $N_s=30$, $p_1=1$ and $spp=1$). Furthermore, the use of the first current harmonic is not necessary because we could have higher harmonic winding factors for the other harmonics which is the case of the proposed winding shown in Fig. 8. The 15-phase machine has the same global dimensions and copper quantity as the simulated five-phase machines (TABLE II).

This winding has the advantage of short end-coils comparing to overlapping winding (especially when $p_1=1$), the harmonic winding factors are shown in TABLE V.

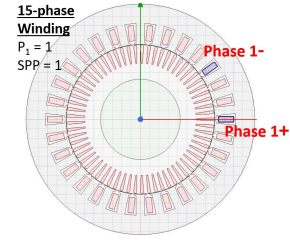


Fig. 8: 15-phase machine geometry and coils distribution in phase 1.

TABLE V. HARMONIC WINDING FACTORS OF THE PROPOSED 15-PHASE WINDING.

Harmonic	1	2	3	4	5	6	7
Winding factors	0.31	0.59	0.81	0.95	1	0.95	0.81

This machine was simulated under 3rd and 4th current harmonics injection ($k_{h3} = 0.81$, $k_{h4} = 0.95$). The amplitude of current was calculated to keep the same current density per conductor and the obtained RMS value is 69 A.

Poles distribution under both injected harmonics is shown in Fig. 9.

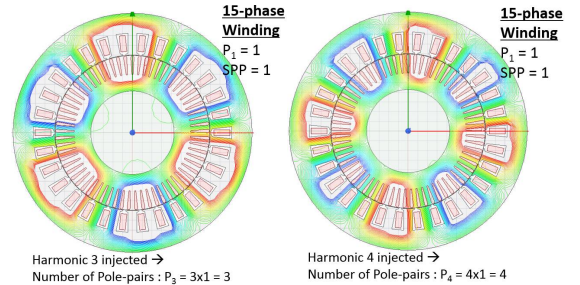


Fig. 9: Poles distribution under third and fourth harmonic supply

By the same way as explained previously, the torque curves in function of rotor pulsation are determined by FE parametric simulations, and shown in Fig. 10.

Maximum developed torque under third harmonic supply is 209.3 N.m, the torque ripple was calculated, and it is of 2%. For the fourth harmonic supply the maximum torque is 237.4 N.m with torque ripple of 2.8%. So, for both supplying modes the torque is of a good quality. As expected by the harmonic winding factors, we develop more torque with the 4th current harmonic than the 3rd one.

$$\frac{k_{h3}}{k_{h4}} = 0.85 \quad \& \quad \frac{\text{Torque}_{h3}}{\text{Torque}_{h4}} = 0.88 \quad (5)$$

We can conclude that the developed torque under each current harmonic injection, is coherent with the harmonic winding factors for the proposed 15-phase winding.

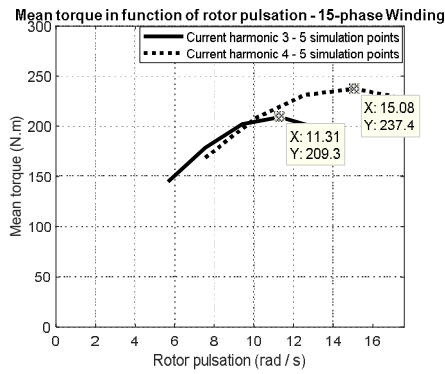


Fig. 10: Mean torque curves for the proposed 15-phase machine

VI. CONCLUSION

In multiphase induction machines, several current harmonics can be injected to produce torque. Hence, to design a multiphase winding for induction machine, the coils distribution must be chosen according to the suitable torque capability under different current harmonics. In fact, maximum torque level under a harmonic “i” is reflected by the harmonic winding factor “ k_{hi} ” according to the classical theoretical approach.

In this study, the torque capability under first and third harmonic supplies was investigated with four different five-phase windings, with the same machine geometry and copper volume. F-E simulations were done to determine the maximum torque under rated phase current for each machine. The results have shown that:

- A high fundamental polarity impacts the torque capability under the third harmonic supply (due to the important level of rotor losses).
- A high number of stator slots enhances slightly the torque capability.
- A very low fundamental polarity ($p_1 = 1$) requires a bigger magnetic circuit (extended stator and rotor yokes) to develop the suitable torque under first harmonic supply.

Through the study of the chosen five-phase windings, it has been concluded that is complicated to design a five-phase induction machine with a good consistency between torque capability, under harmonics injection, and harmonic winding factors. In fact, the number of induced magnetic poles in the machine must be in an acceptable range. In our case, for the winding with $p_1=2$, the torque capability is good under first harmonic supply but not under the third one, where 12 magnetic poles are induced ($p_3=6$), in the other hand, the winding with $p_1=1$ had a relatively good torque capability under third harmonic supply, but not under the first one, where the stator and rotor yokes must be extended due to the very low polarity.

The raise of number of phases, offers more degrees of freedom regarding the winding choice. The harmonics are separated more and more into independent sets, which allow to choose winding distributions with both odd and even space harmonics. An example of 15-phase winding was presented, and it has been shown that the developed torque under 3rd and 4th current harmonics supplies, had a good consistency with

the harmonic winding factors. In fact, for this machine, the used harmonics induce an acceptable number of magnetic pole-pairs (3 and 4).

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