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Acoustic Radiation Force is commonly used to create stable large-scale aggregates of 1 particles in levitation (so-called "acoustic levitation") in a micro cavity. We show in 2 the following work that this well-known and well-controlled aggregation process can 3 be reversed without contact or external flow if the aggregated particles are enlight-4 ened with the proper optical wavelength. This coupled optics and acoustics effect has 5 been observed with various kinds of particles and different optic wavelengths, show-6 ing high reproducibility. The phenomenon is studied using fluorescent micro-metric 7 polystyrene particles without flow, and the effects of acoustic energy and illumina-8 tion power have been quantitatively assessed. It is then exploited to separate a mix 9 of particles with identical mechanical properties, based on their different optic ab-10 sorption. If the phenomenon is not well understood, we propose and discuss some 11 possible mechanisms that could be responsible for the rapid ejection of the objects in 12 levitation from the illuminated area. Since it is a tag free phenomenon which does not 13 need high energies to happen and since it works with biological objects such as algae, 14 red blood cells and bacteria, it may open the way to a broad range of applications. 15

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## 16 I. INTRODUCTION

Acoustic manipulation of micro-objects (particles, cells, bacteria, micro-bubbles, etc.) can 17 be realized using ultrasonic standing waves in a fluidic or microfluidic resonator<sup>1-4</sup>. Acoustic 18 focusing of suspensions (or "acoustophoresis") is a complex phenomenon which has been the 19 subject of many theoretical studies during the last decade. It occurs in a micro-channel or 20 a micro-cavity when an acoustic wave of frequency  $f_{ac}$ , emitted into the cavity through a 21 vibrating wall and reflected by the opposite wall, matches the resonance condition  $\lambda_{ac} = 2h$ , 22 h being the height of the device (Fig. 1). In this case, particles such as plastic beads or 23 living cells are drawn toward the acoustic pressure node created at mid-height of the cavity 24 by the so-called Acoustic Radiation Force (ARF). 25

The ARF is the primary effect of the standing ultrasonic wave on the particles in suspen-26 sion, and it rises from a second-order non-linearity. The ARF is different for each particle 27 because it depends on their physical characteristics and size. The second effect of the ultra-28 sonic standing wave is called acoustic streaming5-7. The acoustic wave transfers momentum 29 to the fluid, leading to global motions of the particles through the Stokes force. The third 30 effect is a Bjerknes force. It is basically a short distance force between particles<sup>8</sup>, attractive 31 in most of the cases for the kind of particles used here, that contributes to the stabilization 32 of the aggregate. 33

There are different theoretical models describing the ARF, based on more or less simplifying hypotheses<sup>9–15</sup>. King<sup>12</sup> was the first to propose computations on the forces on particles in a sound field based on several simplifying hypotheses. In particular, he considered the JASA/ Observation of selective optical manipulation of particles in acoustic levitation <sup>37</sup> particles as rigid spheres. In the following, we will use the Yosioka model<sup>13</sup> which takes <sup>38</sup> into account the compressibility of the spherical particles in the modeling. In this case, the <sup>39</sup> primary Acoustic Radiation Force (ARF)  $F_{ac}$  responsible of particle acoustic levitation can <sup>40</sup> be defined as:

$$\overrightarrow{F}_{ac} = \frac{\pi}{4} \langle E_{ac} \rangle \ k \ d_p^3 \ F_Y \ \sin\left(2 \ k_{ac} \ z\right) \ \overrightarrow{e}_z \tag{1}$$

where  $\langle - \rangle$  denotes time averaging,  $d_p$  is the particle diameter,  $\langle E_{ac} \rangle$  is the time-averaged acoustic energy density inside the channel,  $k = \frac{2\pi}{\lambda_{ac}} = \frac{2\pi f_{ac}}{c}$  is the wave number of the acoustic plane wave of frequency  $f_{ac}$ ,  $F_Y$  is the contrast factor, a positive (for polystyrene particles in water) numerical constant, and z is the axial (or vertical) position of the particle, z = 0 being at the bottom of the channel and z = h being at the top of the channel (Fig. 1). The z axis also corresponds to the wave propagation direction.

47 The acoustic contrast factor of a given particle of density  $\rho_p$  in a medium of density  $\rho_f$ 48 is defined as:

$$F_Y = \frac{1 + \frac{2}{3} \left(1 - \frac{\rho_f}{\rho_p}\right)}{2 + \frac{\rho_f}{\rho_p}} - \frac{\rho_f c_f^2}{3 \rho_p c_p^2}$$
(2)

where  $c_p$  is the speed of sound in the particles material and  $c_f$  is the speed of sound in the fluid. In this investigation we are dealing with an ultrasonic standing wave with a frequency  $f_{ac} \sim 2$  MHz. The amplitude of the corresponding acoustic force typically ranges from  $10^{-12}$ to  $10^{-14}$  N. For instance, with polystyrene particles ( $\rho_p = 1060 \text{ kg.m}^{-3}$ ,  $c_p = 2350 \text{ m.s}^{-1}$ ,  $Z_{ps} = 2.5 \text{ MPa.s.m}^{-1}$ ) dispersed in our resonator filled with water ( $\rho_f = 1000 \text{ kg.m}^{-3}$ ,



FIG. 1. (color online) Side view of an acoustic resonator showing the principle of acoustic focusing of a suspension of particles in an acoustic resonator (a, b) leading to the creation of an aggregate in acoustic levitation (c). Red lines denote the standing ultrasonic wave pressure profile. (d) The aggregate of fluorescent particles can then be broken up if illuminated with the proper optical wavelength, through the microscope internal light source.

 $c_f = 1500 \text{ m.s}^{-1}$ ),  $F_Y$  equals 0.2244, and if particle diameter is 1 µm, the primary acoustic radiation force equals  $2.8 \times 10^{-13}$  N.

<sup>56</sup> Once the particles have reached the nodal plane, the axial component of the force becomes <sup>57</sup> null and the transverse component  $F_T$  is no longer negligible. Indeed it has been shown that <sup>58</sup> this component is about one hundred times weaker than the axial component and is then JASA/ Observation of selective optical manipulation of particles in acoustic levitation <sup>59</sup> negligible during the focusing step<sup>16,17</sup>. Whitworth<sup>18</sup> derived the transverse component of <sup>60</sup> the ARF for a radially symmetric acoustic wave in the nodal plane:

$$F_T = d_p^3 \frac{3(\rho_p - \rho_f)}{\rho_f + 2\rho_p} \nabla \langle E_{ac} \rangle \tag{3}$$

This transverse component depends directly on the radial gradient of the acoustic energy 61  $\nabla \langle E_{ac} \rangle$  and is responsible for the aggregation of particles in the levitation plane toward the 62 local maximum of acoustic energy, which are the final equilibrium positions that we observe. 63 After a short description of the experimental setup, we will present the first observa-64 tions of the ejection of particles in acoustic levitation when illuminated at specific optical 65 wavelengths. The ejection velocity of the particles from the illuminated area is then stud-66 ied quantitatively, especially by varying the amplitude of the acoustic force field and the 67 power of the light wave. The phenomenon is then applied to a binary mixture of particles, 68 illustrating the great potential of this phenomenon as a new highly selective separation tech-69 nique. Finally the different possible mechanisms that could explain our observations and 70 measurements are discussed, before coming to the conclusion. 71

#### 72 II. MATERIALS AND METHODS

#### 73 A. Acoustic resonator

In the following, all the experiments have been carried out in the same acoustic resonator whose dimensions are summarized on Fig. 2 a). We use a homemade aluminum circular cavity of diameter D = 20 mm and height h = 400 µm. The cavity is closed by a round

quartz cover plate (reflector thickness  $h_{ref} = 1.1 \text{ mm}$ ) while the bottom is made of a 77 silica wafer (transmitter thickness  $h_{trans} = 0.30$  mm). The cover plate is easily removable 78 and allows fast changes of the medium. The 2 MHz piezoeletric transducer (PZT) (square 79 ceramic, 1 mm thick, 10 mm wide) is glued directly on the silica wafer using a water soluble 80 glue. The PZT is powered by a wave generator (Tabor Electronics 5200) connected to an 81 amplifier (Tabor Electronics 3222) allowing the variation of the applied voltage between 82 a few mV to more than 10 V peak to peak. A correlation is made between the acoustic 83 energy carried by the generated standing ultrasonic field and the voltage applied to the 84 piezoelectric transducer, by measuring the axial focusing velocity  $v_z(z)$  of a spherical bead, 85 which is directly proportional to the acoustic energy. Using polystyrene spheres of known 86 compressibility and density, we can find the acoustic energy density<sup>19</sup>. We will thus speak of 87 acoustic energy when referring to the amplitude of the acoustic field in the remaining of the 88 article. The frequency  $f_{ac}$  of the sinusoidal signal is tuned to maximize the acoustic radiation 89 force which corresponds to the resonance condition  $\lambda_{ac} = 2h$ . We find this resonance 90 by monitoring the reflected electric signal through an oscilloscope (LeCroy WaveAce 214), 91 and minimizing the amplitude of said signal. In our case, the optimal frequency is  $f_{ac} \simeq$ 92 1.85 MHz, but day-to-day fluctuations can occur, caused by small room temperature change, 93 or slight errors in the position of the quartz cover plate. These fluctuations are on the order 94 of  $0.5\% f_{ac} \simeq 10$  kHz. 95



FIG. 2. (color online) a) Sketch of the acoustic resonator, showing the piezoelectric transducer (PZT) glued under a silicone wafer, establishing a standing acoustic field in the cavity above, enclosed by aluminum walls and a quartz top cover plate. b) Sketch of the experimental setup showing the acoustic generation devices, the acoustic resonator placed on the moving stage of a microscope.

#### 96 Optical setup

The acoustic resonator described above was then placed on the moving stage of a fluores-97 cence microscope (Olympus BX-2 and Olympus BXFM). The observations were made using 98 objectives with different magnification, depending on the size of the aggregates. The light 99 source for white light and fluorescence experiments is a LED source (CoolLED pE-300-W) 100 allowing a reasonably good control of the wavelength range and power of illumination. The 101 microscope is equipped with two filter cubes allowing the monitoring of the green or red 102 fluorescences. The filter 1 is centered on the Green Fluorescent Protein (GFP) range, i.e. 103 an excitation wavelength  $\lambda_{abs} = 488$  nm and an emission wavelength  $\lambda_{fluo} = 525$  nm, 104 while filter 2 is centered on *Discosoma* RED protein (DsRED) range, i.e.  $\lambda_{abs} = 545$  nm 105 and an emission wavelength  $\lambda_{fluo} = 620$  nm. Color movies presented here for qualita-106 tive observations were recorded using a INFINITY3-3UR Lumenara camera at 50 fps. The 107 quantitative experiments were recorded using a PCO Dimax CS3 (c) fast camera at 100 fps. 108 The images resulting from experiments were post-treated with the free software ImageJ 109 (https://imagej.nih.gov/ij/), to adjust contrast, crop areas of interest and to produce 110 the spatio-temporal diagrams illustrated on Fig.6. The intensity delivered by the illumi-111 nation lamp has been measured with a ThorLabs PM16-130 Probe (Spectral range 400 to 112 1100 nm, 1 cm  $\times$  1 cm silicon sensor area, optical power range 5 pW - 500 mW) connected 113 to the same computer controlling the other instruments. 114

# III. CREATION OF LARGE-SCALE AGGREGATES UNDER ACOUSTIC RADI ATION FORCE

As explained in the previous sections, the ARF is a simple and fast process to create 117 large aggregates of particles in acoustic levitation. Once the ultrasonic wave is generated 118 with the proper frequency into the cavity, the ARF forces the suspended particles to move 119 toward the nodal plane, at mid-height of the cavity. Once the particles have reached the 120 focusing plane, the transverse component of the ARF forces the particles to move toward 121 the location of the maximum of acoustic energy and then create an aggregate. When the 122 particles are close enough from each other than the Bjerknes force keep the particles close 123 together, making the aggregate more compact and stable. The creation of a large aggregate 124 of particles is illustrated on Fig. 3 a) with  $1.62 \ \mu m$  polystyrene beads. The focusing time 125  $T_{foc}$  can be very short (a few tenths of second), depending on the amplitude of the ARF. 126 Once the aggregate is formed, it can be kept in acoustic levitation as long as needed and 127 will remain stable, with the same spatial organization<sup>20</sup>. The aggregation process is efficient 128 on particles as well as cells or active matter (bacteria). It can be used as a tool for creating 129 an acoustic trap, especially for self-propelled organisms like bacteria that can be held in 130 levitation in acoustic confinement<sup>21</sup>. 131

In previous works<sup>20</sup> we demonstrated that it is also possible to generate and sustain a 2D aggregate of particles using burst mode acoustic, or pulsed acoustic, i.e. applying a low-frequency square wave modulation with a given duty-cycle. We also demonstrated that it helps suppressing the acoustic streaming for particles smaller than 1 µm. It is also of great JASA/ Observation of selective optical manipulation of particles in acoustic levitation help to control the amount of acoustic energy injected in the setup as well as limiting the possible thermal heating of the piezoelectric element when running long-time experiments, therefore reducing the potential thermal detuning of the resonator. It will be useful in the following to evaluate the possible influence of acoustic streaming on the phenomenon.

#### 140 IV. BREAKUP OF AGGREGATES

As mentioned previously, once an aggregate of passive particles is formed using ARF, it remains stable and can be kept in levitation as long as needed. Without the use of an external flow or force, there is no way to break it up, apart from lowering enough or turning off the acoustics. In that case the aggregate either disintegrates in small aggregates and particles which all sediment, or the entire aggregate sediments, with particles still being stuck to each other by short distance hydrodynamic interactions.

There can be other behaviors with active matter, for instance when aggregating bacteria (active) or Janus particles (pseudo active). Indeed, when aggregated bacteria kept in levitation are released from the confinement imposed by the acoustic field, the aggregate inner active pressure triggers an explosion-like breakup, radially ejecting bacteria confined in the acoustic field<sup>21</sup>. In the case of Janus particles, as demonstrated by Takatori et al.<sup>22</sup>, the relaxation of an active crystal has been observed and described when the acoustic confinement is released.

<sup>154</sup> What we shall report in the following is a breakup process of aggregates of particles kept <sup>155</sup> in acoustic levitation using specific illuminations.



FIG. 3. (color online) Time steps between frames is 200 ms. a) The three first pictures show the formation of a large stable aggregate of 1.62 µm polystyrene particles under a  $f_{ac} = 1.86$  MHz acoustic field. It can be kept stable as long as needed. b) When the same aggregate is illuminated with a green light ( $\lambda_{light} = 545$  nm) at a much higher intensity, the particles are quickly ejected from the illuminated region (see SI Movie 1). c) We observe the same phenomenon with 1.75 µm polystyrene particles fluorescing in green and illuminated with a blue ( $\lambda_{light} = 488$  nm) light at the same intensity (see SI Movie 2).

### <sup>156</sup> V. BREAKUP OF AGGREGATES OF FLUORESCENT PARTICLES BY LIGHT

#### 157 A. First observations

We use fluorescent polystyrene particles of diameter  $d_p = 1.62 \ \mu m$  which can be excited with green light and fluoresce in red light ( $\lambda_{abs} = 545 \ nm$  and  $\lambda_{em} = 620 \ nm$ ). Large aggregates of particles are created in acoustic levitation in the cylindrical resonator described on Fig. 2 using  $f_{ac} = 1.86$  MHz resonant frequency. As mentioned previously, the aggregates can be kept stable as long as needed when observed with a white light and at standard microscope illumination power, below 5 mW.mm<sup>-2</sup> (The regular aggregation process can be seen in Fig. 3 a) ).

Interestingly, when using a monochromatic ( $\lambda = 545$  nm) illumination, and gradually 165 increasing the light intensity, the aggregation process is stopped. For even higher intensities, 166 the aggregate starts to eject particles from its periphery. This ejection process goes on until 167 disruption of the entire aggregate. If the light intensity is still increased, then this ejection 168 process takes the form of an explosion, as can be seen on Fig. 3 b) and associated movie 169 (see SI Movie 1, 4). One astonishing effect is that the particles escape the aggregate while 170 remaining in the focal plane of the camera, i.e. in levitation. This result suggests that 171 the primary radiation force (responsible for the acoustic focusing) is not affected, but that 172 transversal and Bjerknes forces seems to be completely counterbalanced or screened by 173 another force. 174



FIG. 4. Movie (MM1)showing the formation of an aggregate made of 1.62 µm beads under the influence of a 1.86 MHz acoustic field. This aggregate is then disrupted when illuminated with a high intensity monochromatic green light. As soon as the standard white illumination is restored the aggregate recovers its initial shape.

<sup>175</sup> MM.1. Observation of the standard process of formation of an aggregate in acoustic lev-<sup>176</sup> itation. It is then disrupted under monochromatic illumination. The aggregate is reformed <sup>177</sup> quickly when the white light illumination is restored. This is a file of type "mp4" (4.5 Mb) <sup>178</sup> The disaggregation only occurs in acoustic levitation (no effect observed on beads that are <sup>179</sup> on the bottom or top of the cavity) and when the particles are illuminated with the proper <sup>180</sup> wavelength corresponding to the fluorescent particle absorption wavelength. In this case, for <sup>181</sup> instance, the aggregate remains unchanged if illuminated with a blue light ( $\lambda = 488$  nm).

Another interesting point is that the effect is reversible: once the light intensity is lowered under a given threshold, then the standard acoustic aggregation process starts again with the same dynamics (as demonstrated at the end of SI Movie 1).

This phenomenon is highly reproducible and not limited to a given type of fluorescent bead. It has been tested with various fluorescent particles, all experiments leading to the

same observations. Another example is shown Fig.  $3 \, c$ ), where an aggregate made from a 187 solution of particles of diameter  $d_p = 1.75 \ \mu m$  which can be excited with blue light and 188 fluoresce in green light ( $\lambda_{abs} = 450 \text{ nm}$  and  $\lambda_{em} = 532 \text{ nm}$ ) is formed under an acoustic 189 field of frequency  $f_{ac} = 1.85$  MHz. As soon as we illuminate this aggregate with a blue light 190  $(\lambda = 488 \text{ nm at } 50 \text{ mW}.\text{mm}^{-2})$ , the aggregate starts to eject particles from its periphery, as 191 was observed before (see SI Movie 2, 5). The same expulsion phenomenon could be observed 192 in a very reproducible way using these different fluorescences and with various diameters  $d_p$ , 193 ranging from 0.883 to 5 µm, when the aggregate was illuminated with the right wavelength. 194



FIG. 5. Movie (MM2) showing the disruption of an aggregate made of 1.75 µm beads under the influence of a 1.85 MHz acoustic field, illuminated by a strong blue light.

<sup>195</sup> MM.2. Disruption of an aggregate made of green fluorescent 1.75 µm polystyrene beads. <sup>196</sup> This is a file of type "m4v" (4.1 Mb)

#### <sup>197</sup> B. Influence of the light intensity

As mentioned in the previous section, one can find a critical illumination intensity  $I_{crit}$ for which the acoustic radiation force and the opto-acoustic force seem to balance each



FIG. 6. Principle for spatio-temporal analysis. A given line across an aggregate is chosen and plotted as a function of time. The resulting picture gives an overall view of the expulsion process. The ejection velocity is then measured as the slope of the cone frontier in the spatio-temporal diagram.

<sup>200</sup> other. To further investigate the dependence of the effect on the amount of light injected in <sup>201</sup> the aggregate, we did vary the light intensity for a given aggregate of 1.62 µm beads, at a <sup>202</sup> fixed amplitude of the acoustic field ( $f_{ac} = 1.85$  MHz). In the following the amplitude of <sup>203</sup> the acoustic force is considered proportional to the acoustic energy inside the resonator (cf. <sup>204</sup> Eq. 1). In this case, this energy is constant ( $\langle E_{ac} \rangle = 10$  J.m<sup>-3</sup>).

To quantify the disaggregation dynamics, we use spatio-temporal diagrams as explained in Fig. 6. A line crossing the stable aggregate is chosen before illumination. The aggregate

JASA/ Observation of selective optical manipulation of particles in acoustic levitation being a bright spot over a dark background, the line crossing it shows a clear frontier between 207 the aggregate and surrounding fluid. The time-evolution of these lines is then plotted as a 208 function of time, leading to a spatio-temporal diagram (left part of Fig. 6). The disruption 209 of the aggregate is then visualized as a cone in the spatio-temporal diagram. The slope of 210 the cone frontier in the spatio-temporal diagram leads directly to the expulsion velocity  $v_{ei}$ . 211 It is then possible to measure the ejection velocity for each illuminations. The evolution 212 of  $v_{ej}$  as a function of the illumination power  $P_{light}$  is plotted on Fig. 7 a). A linear evolu-213 tion is found suggesting a direct proportionality of the ejection velocity with the injected 214 illumination power:  $v_{ej}(P_{light}) \propto P_{light}$ . 215

#### <sup>216</sup> C. Influence of the amplitude of the ARF

Similarly, the influence of the acoustic force amplitude has been investigated. We also found that the phenomenon was no longer observed when the acoustic field is turned off. This time, we did explore a range of ARF amplitudes ranging form 8 to 200 J.m<sup>-3</sup> at  $f_{ac} = 1.85$  MHz for a given illumination power (50 mW.mm<sup>-2</sup>), all other parameters being kept constant.

Using the same spatio-temporal analysis, we plot on Fig. 7 b) on logarithmic scale the evolution of  $v_{ej}$  as a function of the acoustic energy in  $J.m^{-3}$  for a given illumination power  $P_{light}$ . In this case, a linear evolution is found suggesting a scaling of the ejection velocity as a 3/4 power law of the acoustic energy:  $v_{ej}(\langle E_{ac} \rangle) \propto \langle E_{ac} \rangle^{3/4}$ . Combining both results, and considering that both parameters are independent, one can define the following scaling law for the ejection velocity:  $v_{ej}(P_{light}, \langle E_{ac} \rangle) \propto P_{light} \cdot \langle E_{ac} \rangle^{3/4}$ .



FIG. 7. Evolution of the ejection velocity as a function of the illumination power (constant  $\langle E_{ac} \rangle = 106 \text{ J.m}^{-3}$ ) (a) or of the amplitude of the ARF (constant illumination power of 50 mW.mm<sup>-2</sup>) (b) for a given suspension of  $r_p = 1.62 \text{ }\mu\text{m}$  polymer beads under the influence of a  $f_{ac} = 1.85 \text{ MHz}$  acoustic field.

#### 228 D. Influence of acoustic streaming

Acoustic streaming is a common phenomenon when using standing acoustic waves in resonant cavities. It could be considered as a possible explanation for the breakups of the aggregates, so we did investigate this effect.

As briefly described in section III, it is possible to control the onset of acoustic streaming in our resonators using a burst signal. The duty cycle DC of the ultrasonic wave can be JASA/ Observation of selective optical manipulation of particles in acoustic levitation defined as the ratio between the time when the ultrasounds are emitted over the total period of the excitation :

$$DC = \frac{T_{ON}}{T_{OFF} + T_{ON}} \tag{4}$$

<sup>236</sup> When we vary this parameter, we are modifying the temporal average of the acoustic en-<sup>237</sup> ergy that plays a role in the ARF. Fig. 8 represents the ejection speed of 1.62 µm polystyrene <sup>238</sup> particles, when submitted to a 1.908 MHz ultrasonic standing field, with an acoustic energy <sup>239</sup> of 160 J.m<sup>-3</sup>, and enlightened with a light power of 50 mW.mm<sup>-2</sup>. The acoustic field is <sup>240</sup> then modulated by a square signal of period  $T_{burst} = 1$  ms, and we then vary the duty <sup>241</sup> cycle of the resulting field. As can be seen on this figure, at low duty cycles, we observe a <sup>242</sup> linear evolution of the ejection speed with an increase of the duty cycle.

Defining a threshold for the acoustic streaming<sup>23</sup> (below which no acoustic streaming 243 is affecting the aggregates in levitation), we can find a critical duty cycle for these burst 244 parameters, that is represented by a gray bar on Fig. 8. Below this threshold, we do not 245 observe any streaming in the cavity $^{20}$ . Interestingly enough, when we cross the acoustic 246 streaming threshold, we do not observe any change in the evolution of the ejection velocity. 247 The fact that we do observe breakups of aggregates, with the same coupling between acoustic 248 energy and light power below its threshold means that the origin of this phenomenon is not 249 acoustic streaming. 250



FIG. 8. Influence of the duty cycle on the ejection speed. The grey bar indicates the critical duty cycle below which we do not observe acoustic streaming. Error bars are smaller than the dots size.

## 251 VI. SEPARATION OF A BINARY MIXTURE

To demonstrate the ability of the opto-acoustic effect to separate a binary mixture, we 252 used a mixed solution of two colloidal particles: polystyrene particles of mean diameters 253  $d_{p1} = 1.62 \ \mu\text{m}$  and  $d_{p2} = 0.883 \ \mu\text{m}$ , with absorption wavelengths  $\lambda_1 = 532 \ \text{nm}$  and 254  $\lambda_2 = 450$  nm with an equal volume fraction of 0.025 %. First we created a large ag-255 gregate in acoustic levitation, following the same process as in the previous experiments 256  $(1.903 \text{ MHz and } 200 \text{ J.m}^{-3})$  and using the same resonator. After a relatively short focus-257 ing time, the aggregate becomes stable in acoustic levitation. The aggregate contains an 258 homogeneous mixture of both particles. 259

The upper row of Fig. 9 shows the aggregates in acoustic levitation but using different filters. Fig. 9 a) corresponds to an observation without filters. It shows a large aggregate in stable acoustic levitation. When using a green (Fig. 9 b) or red filter (Fig. 9 c) one can see that both types of particles are rather homogeneously distributed over the entire aggregate. To our knowledge, it is impossible to separate such a mixture of particles once they are so well mixed using acoustics alone.

The aggregate has then been illuminated with a blue light ( $\lambda_{light} = 488 \text{ nm}$ ) at a constant 266 power of  $30 \text{ mW.mm}^{-2}$  during 10 seconds, then the illumination has been turned off. The 267 resulting aggregate has then been observed once the particles have aggregated again under 268 the influence of ARF. The result is shown on the lower part of Fig. 9. Fig. 9 d) shows 269 the aggregate after a few seconds without any optical excitation. One can see that the 270 aggregate has changed from its original shape. Fig. 9 e) and Fig. 9 f) shows the pictures 271 of the aggregate when observed respectively with a green and red filter. We can clearly see 272 that the aggregate no longer contains an homogeneous mixture of both particles. The red 273 fluorescent beads are now on one side of the aggregate while the green are now on the other 274 side of the aggregate. This is a clear demonstration that the two types of particles have 275 indeed been separated by the photoacoustofluidic effect. The separation was very fast (a 276 few seconds) and efficient. The particles absorbing the illumination wavelength (the smaller 277 ones in this case) have indeed been extracted from the aggregate before being attracted 278 again toward the aggregate of larger particles, which did not breakup, because of the ARF. 279



FIG. 9. (color online) Separation of a binary mixture of 1.62 µm red fluorescent particles, and 0.883 µm green fluorescent particles. a), b) and c) pictures show the stable aggregate created by the acoustic force. The three pictures corresponds to observations without selective filter (a) and with respectively green (b) and red (c) filters. The pictures d), e) and f) show the aggregate after applying a strong illumination to the green fluorescent particles during 10 seconds and after all the ejected particles had time to focus again toward the aggregate. One can see that the new aggregate is no longer an homogeneous mixture of the two types of particles. It is now made of two clearly separate regions: one containing the red particles, the other one containing the green particles.

#### 280 VII. DISCUSSION

#### A. Coupled dependency on acoustic and illumination

The previous experiments show a clear correlation between acoustics energy and illumi-282 nation power for the breakdown of aggregates. To evaluate this coupling, we studied the 283 evolution of the ejection speed from the aggregates when varying the illumination power 284 and amplitude of the ARF for a given suspension of particles ( $d_p = 1.62 \text{ }\mu\text{m}$ ). The result 285 is shown on Fig. 10 as a phase diagram: we represent the initial ejection speed of particles 286 from the aggregate as a function of illumination power and acoustic energy applied to the 287 aggregate, i.e. a contour plot of  $v_{ej}(P_{light}, \langle E_{ac} \rangle)$ , the color bar being proportional to  $v_{ej}$ . 288 The 1 µm.s<sup>-1</sup> speed contour line is highlighted in red, and corresponds to the Brownian mo-289 tion speed at experiment temperature (20 degrees Celsius) for these particles and has been 290 identified as the threshold between stable aggregate and aggregate breakup zones. As one 291 can observe, the aggregate is locked in a stable state, provided that the illumination power 292 is below 10 mW.mm<sup>-2</sup>, or the acoustic energy of the ultrasound field is below 25 J.m<sup>-3</sup>. 293 Once this threshold is crossed (solid red line on the phase diagram, corresponding to the 294 Brownian motion at the experiment temperature, for these particles), then we have a more 295 or less linear evolution of the ejection speed as light power or acoustic energy is increased. 296 Interestingly, there seem to be a threshold on acoustic energy density at  $160 \text{ J.m}^{-3}$ , above 297 which the light dependence of the ejection speed changes. It seems to be an optimum on illu-298 mination power dependence, as it is the point where the highest ejection speeds are reached 299 using the lowest illumination power. After this threshold, we need to put more illumination 300

JASA/ Observation of selective optical manipulation of particles in acoustic levitation <sup>301</sup> power to reach the same ejection speed. One possible explanation for this behavior is that <sup>302</sup> for these high acoustic energies, the acoustic streaming is no longer negligible, and may <sup>303</sup> interact with the expulsion process, leading to some errors in the estimation of the initial <sup>304</sup> ejection velocity (leading to a no longer isotropic ejection).



FIG. 10. (color online) Determination of the phase diagram for an assembly of 1.62  $\mu$ m red fluorescent particles. The ejection speed of particles from the aggregate are represented with a color scale, against the power of the light used on the aggregate and the squared voltage applied to the piezoelectric ceramic, representing the acoustic energy inside the resonator. The 1  $\mu$ m.s<sup>-1</sup> speed contour is the thermal agitation speed at experiment temperature (20 degrees Celsius) and has been identified as the threshold between stable aggregate and aggregate breakup zones.

JASA/ Observation of selective optical manipulation of particles in acoustic levitation These results show that both acoustic and light excitation are needed to observe this phenomenon. Particles need to absorb light at the specific optic excitation wavelength used to be ejected from the aggregates, and to be trapped at the same time in an acoustic field carrying enough acoustic energy. This means that the optic energy absorbed by the particles needs to play a role in the explanation of the phenomenon.

#### B. Influence of heating on particles properties

The most plausible explanation is that optical illumination at specific wavelength leads to 311 absorption and conversion of incident light  $(E_{\lambda})$  into thermal heating. One basic explanation 312 could be that while absorbing light, particles heat up, thus modifying their mechanical 313 properties, potentially affecting the sign of the acoustic contrast factor in Eq. 2. However, 314 after calculation, compressibility and density of polystyrene and water do not change that 315 much between 20 and 100 degrees Celsius. Moreover, if the acoustic contrast factor were to 316 change sign, then the principal component of the ARF (responsible for the vertical focusing 317 of the particles) would also be affected, and we do not observe a movement out of the focal 318 plane. 319

#### 320 C. Heating of the fluid itself

One could argue that it is the fluid itself that heats up when exposed to a strong illumination, under the confinement of the acoustic field. Having the fluid directly react to the coupled excitation could then create a large scale flow dragging away the particles. To try this, we have performed experiments using coloured beads. Two types of particles having



FIG. 11. (color online) Illustration of how the particle (or an aggregate, as depicted on the right side of the graphic) once illuminated by an optical wave might heat up the surrounding liquid, thus generating an asymmetrical thermal layer around it, which might generate motion by convection or acoustic instability.

the exact same mechanical properties (same radii  $= 10 \ \mu m$ , made of polystyrene), in the 325 same acoustic field ( $\langle E_{ac} \rangle = 106 \text{ J.m}^{-3}, f_{ac} = 1.90 \text{ MHz}$ ), have been illuminated with 326 the same optical wave ( $\lambda = 550$  nm or 580 nm, P = 50 mW.mm<sup>-2</sup>). The only difference 327 between the two populations was their optical absorption, one of the particle type being red-328 dyed while the other was transparent (plain polystyrene). Everything else being equal, the 329 acoustic force is the same on the two species. When illuminated with the same wavelength 330 and power, the dyed particles are almost instantly dispersed, while the transparent ones are 331 not affected by the light (see SI Movie 3, 12). That confirms that the particles need only 332

JASA/ Observation of selective optical manipulation of particles in acoustic levitation absorbing the illumination wavelength and that they are the source of the phenomenon, and not the fluid itself.



FIG. 12. Movie (MM3) Side to side comparison of the evolution of (left) an aggregate of plain polystyrene particles being 10 µm in diameter, and (right) the same particles red-dyed. They are both confined in the same acoustic field ( $\langle E_{ac} \rangle = 106 \text{ J.m}^{-3}$ ,  $f_{ac} = 1.90 \text{ MHz}$ ) and enlightened with the same optical wave (580 nm, P=50 mW.mm<sup>-2</sup>). As the aggregate made of dyed particles is instantly disersed, nothing happens to the particles that do not absorb the optical wave.

MM.3. Side to side comparison of an aggregate of plain polystyrene particles and another one being red dyed, under the same acoustic confinement and optical illumination. This is a file of type "mp4" (6.3 Mb)

338 D. Soret effect

Another effect that could affect the stability of the aggregate in acoustic levitation is related to the Soret effect, or Ludwig-Soret effect<sup>25</sup>, or thermodiffusion, namely, particle migration under temperature gradients. The Soret coefficient is the ratio between the thermal diffusion coefficient and the molecular coefficient of colloidal objects suspended in a liquid. The Soret coefficient is well understood in gases when molecules of different size differentially

JASA/ Observation of selective optical manipulation of particles in acoustic levitation migrate under a thermal gradient. Nevertheless, Soret effect is visible and measurable in 344 suspensions of polymers in organic solvents, but the theoretical models are still poorly devel-345 oped. Concerning Soret effect of non colloidal particles (10 µm) in water, to our knowledge 346 only one study has been undertaken<sup>25</sup>. The thermophoretic mobility of 10 µm polystyrene 347 particles has been estimated in water, in a thermal gradient corresponding to 0.25 °C/  $\mu$ m, 348 yielding to a migration velocity of 5 µm/s. In our case, the red fluorescent particles being 349 1.62 µm in diameter, 10 µm is a good approximation of our thermal layer thickness. Having 350 even a few additional degrees in the aggregate will yield thermal gradients on this order of 351 magnitude. At the periphery of the aggregate, particles could be pushed away by a Soret-like 352 effect. When illuminated, the temperature in the aggregate is higher than that in the sur-353 rounding liquid. With a Soret effect of non-colloidal species, particles migrate from higher 354 to lower temperatures, in qualitative agreement with our observations. Once particles are 355 far apart from each other, with distances longer than the Bjerknes acoustic forces range<sup>26,27</sup>, 356 the aggregate starts to disrupt. Unfortunately, thorough investigations would be needed to 357 precisely quantify the thermal gradient generated in the boundary layer surrounding the 358 particles in levitation and illuminated with the proper wavelength. 359

#### 360

#### E. A thermal boundary fluid layer

Nevertheless, another thermal effect may originates from the heating of a layer of fluid directly surrounding the particles, leading to a local change in the fluid properties this time. It would create around the particle a soft shell-like boundary layer, reminding the results obtained by Yasuda and Kamakura<sup>28</sup>. While in their work magnitude of forces are discussed,

JASA/ Observation of selective optical manipulation of particles in acoustic levitation we believe such shell could lead to a different direction of the force. As shown on Fig. 11, 365 it is probable that the local increase of the temperature on the upper part of the particles 366 leads to a local increase of the temperature of the fluid layer close to the particle. This 367 would lead to a local change of the fluid density around the particles. A "convection-like" 368 instability could be triggered with a decrease of the fluid density which would then lead to 369 an upward motion to the fluid layer. We did not observe an axial motion of the particles. 370 It would be possible that the axial motion is stopped by the much stronger axial radiation 371 force (justifying the acoustic coupling), leading to a lateral escape motion of the fluid layer, 372 dragging the particles while staying in the levitation plane. 373

#### <sup>374</sup> F. Acoustic instability of the thermal boundary layer

It has been shown recently that fluid layers with even a relatively small contrast factor 375 can undergo ARF effects<sup>24</sup>. This is a side effect that can be a strong limitation to the 376 separation of species if they are transported in different layers of fluid of different densities. 377 If the temperature of a particle  $T_{part}$  is different from the one of the surrounding fluid then 378 a thermal boundary layer  $\delta_{therm}$  is created around the particle, or around an aggregate of 379 particles (See Fig. 11). It is then possible that there exist a fluid layer with a density 380  $\rho_f(T_1)$  lower than the one of the surrounding fluid  $\rho_f(T_0)$ . Gradients of fluid density  $\nabla \rho_f$ 381 will appear, leading to the following expression for the volume force  $F_{ac-flu}$  exerted on the 382

JASA/ Observation of selective optical manipulation of particles in acoustic levitation fluid (we denote  $\hat{\rho}_f$  the dimensionless perturbation in the density, following the analytical development stated above<sup>24</sup>):

$$F_{ac-flu} = -\cos(2ky)E_{ac}\nabla\hat{\rho_f} \tag{5}$$

One can see that if there is density gradient, then the fluid layer will undergo an acoustic 385 force aligned with density gradients, leading to a possible motion of the fluid layer. It 386 may be that this fluid layer drags particle alongs, while these ones are still subject to the 387 axial acoustic force (much larger than the lateral one), thus moving sideways. The resulting 388 ejection speed would then be a competition between the transverse component of the acoustic 389 force and the viscous drag imposed by this fluid layer. The scaling in this case would be 390 interesting, since as described in Eq. 3 the lateral acoustic force scales with  $d_p^3$ , and the drag 391 at this  $R_e$  would scale with  $d_p$  only. 392

#### <sup>393</sup> G. Heating process and size

If the motion origin is indeed related to an instability, either thermal or acoustic, of the surrounding fluid layer, one could expect that the effect will be weaker for larger particles. Indeed, the thickness of the thermal boundary layer will be the same, if all parameters are kept constant apart from the radius of the particle. The ratio  $\delta_{ac}/r_p$  will decrease and the entrainment of the particles will become weaker.

We carried out preliminary experiments with a given type of fluorescent beads, made from the same material (polystyrene, green fluorescent), trapped in the same acoustic field  $\langle 401 \rangle = 106 \text{ J.m}^{-3}$  for a frequency of  $f_{ac} = 1.90 \text{ MHz}$  and illuminated with the same

JASA/ Observation of selective optical manipulation of particles in acoustic levitation optical wave (488 nm with a power of 50 mW.mm<sup>-2</sup>), but with three different diameters. 402 We observed a reduction of the ejection velocity when increasing particle diameter, as can 403 be seen on Fig. 13. The aggregate made of 1 µm particles undergoes the expansion effect, 404 as described before. But this effect is less noticeable on the 3 µm particles aggregate after 405 the same exposition time, and the 10 µm aggregate seems not to have been affected at all 406 after the same manipulation. This result can be considered as a first hint of a possible 407 mechanism associated to the heated fluid layer surrounding the particle. However, it could 408 also stem from a competition between a fluid drag and the transverse component of the 409 ARF as denoted in VIIF. 410



FIG. 13. Evolution of the aggregate behavior in acoustic levitation under illumination for different particle diameters, every other parameters being kept constant. The particles were green fluorescent polystyrene beads of various diameters, illumination was done at 488 nm with a power of 50 mW.mm<sup>-2</sup>, acoustic energy density was  $\langle E_{ac} \rangle = 106 \text{ J.m}^{-3}$  for a frequency of  $f_{ac} = 1.90 \text{ MHz}$ .

JASA/ Observation of selective optical manipulation of particles in acoustic levitation We mentioned and discussed many possible explanations for the light induced ejection of particles in acoustic levitation. A plausible scenario seems to be the heating of the surrounding fluid layer leading to instability mechanisms. To further clarify this hypothesis, more experiments are needed, especially temperature controlled ones.

#### 415 VIII. CONCLUSION

Choosing the proper geometric and acoustic parameters, it is possible to control the 416 aggregation process of micro particles using our in-house ultrasonic resonators. Once the 417 aggregates are formed, it is possible to keep them in acoustic levitation as long as desired. 418 The only way to break the aggregates is to turn off the ultrasounds. Nevertheless we show 419 that it is possible to destroy an aggregate of fluorescent particles just by illuminating it at 420 the proper absorption wavelength. This phenomenon depends on both the acoustic force 421 amplitude and the illumination power: the expulsion of the particles can only be observed 422 in acoustic levitation, suggesting a strong coupling between acoustics and photonics effects. 423 Above a given critical illumination power, the aggregate literally explodes. The expulsion 424 of the particles from the illuminated area can be very fast with an expulsion velocity which 425 depends on the injected power (acoustic amplitude and illumination power). Early observa-426 tions also show that the phenomenon is affecting living cells such as red blood cells, opening 427 the path to many applications of these findings. This phenomenon, which may be named 428 optoacoustophoresis due to its dependence on both excitations, opens the path to many new 429 manipulations and sorting processes of suspensions, combining both acoustic and optical 430 properties of particles or cells. This new branch of acoustofluidics could be called *optoa*-431

JASA/ Observation of selective optical manipulation of particles in acoustic levitation coustofluidics. The potential applications are numerous for both diagnosis or production, 432 such as fine cell separation for analysis or rare cell tagging in continuous flow systems. 433

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