

# Optimization of Criteria for an Efficient Screening of New Thermoelectric Compounds: The TiNiSi Structure-Type as a Case-Study

Céline Barreteau, Jean-Claude Crivello, Jean-Marc Joubert, Eric Alleno

## ► To cite this version:

Céline Barreteau, Jean-Claude Crivello, Jean-Marc Joubert, Eric Alleno. Optimization of Criteria for an Efficient Screening of New Thermoelectric Compounds: The TiNiSi Structure-Type as a Case-Study. ACS Combinatorial Science, 2020, 22 (12), pp.813-820. 10.1021/acscombsci.0c00133 . hal-03007720

# HAL Id: hal-03007720 https://hal.science/hal-03007720v1

Submitted on 16 Nov 2020

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Optimization of criteria for an efficient screening of new thermoelectric compounds: the TiNiSi structure-type as a case-study

Celine Barreteau<sup>1</sup>, Jean-Claude Crivello, Jean-Marc Joubert and Eric Alleno

5

6

4

1 Univ Paris Est Créteil, CNRS, ICMPE, UMR7182, F-94320, Thiais, FRANCE

### 7 ABSTRACT

High-throughput calculations can be applied to a large number of compounds, in order to 8 discover new useful materials. In the present work, ternary intermetallic compounds are 9 investigated, to find new potentially interesting materials for thermoelectric applications. The 10 screening of stable non-metallic compounds required for such applications is performed by 11 calculating their electronic structure, using DFT methods. In the first section, the study of the 12 13 density of states at the Fermi level, of pure elements, binary and ternary compounds, leads to empirically chose the selection criterion to distinguish metals from non-metals. In the second 14 section, the TiNiSi structure-type is used as a case-study application, through the investigation 15 of 570 possible compositions. The screening leads to the selection of 12 possible 16 semiconductors. The Seebeck coefficient and the lattice thermal conductivity of the selected 17

<sup>&</sup>lt;sup>1</sup> Corresponding author: barreteau@icmpe.cnrs.fr

18 compounds are calculated in order to identify the most promising ones. Among them, TiNiSi,

19 TaNiP or HfCoP are shown to be worth a detailed experimental investigation.

20 KEYWORDS: Thermoelectricity, DFT calculations, Semiconductors, Intermetallic

### 21 INTRODUCTION

Thermoelectricity may be used as an interesting technology able to reduce the energy consumption through the recycling of waste heat. The conversion efficiency of thermoelectric devices is related to the dimensionless figure of merit ZT of their constituting materials, which is defined as

$$26 ZT = \frac{S^2 \sigma T}{\kappa} (1)$$

where: S represents the Seebeck coefficient;  $\sigma$  the electrical conductivity;  $\kappa$  the thermal 27 conductivity and T the absolute temperature. Even though efficient thermoelectric devices exist, 28 they are limited to niche markets because of their quite high cost compared to their conversion 29 30 yield. One way to improve this technology is to find new materials based on more abundant, less toxic and less expensive elements. These limitations led us to define a set of elements, we 31 could investigate to search for new interesting compounds <sup>1</sup>. For this set of elements, hundreds 32 33 of compounds have already been reported in crystallographic databases, and even if some of them are known to be good thermoelectric compounds, there is still a very large number of 34 possibly unknown compounds. In order to screen more efficiently the possible combinations, 35 we use high-throughput calculations. We will present an efficient method to screen ternary 36 intermetallic compounds in order to find new promising thermoelectric compounds. In this 37 38 article, we will focus on the equimolar compounds and use the orthorhombic TiNiSi structure type as a case-study. We choose the TiNiSi structure-type because even though it is a large 39 family with more than 70 compounds already reported in the crystallographic databases <sup>2-3</sup>, it 40

has been less subject of investigations compared with other equimolar structure-types. In
contrast, numerous high-throughput calculations and screenings have already successfully
shown very promising results for the equimolar half-Heusler family <sup>4-8</sup>.

Before estimating the thermoelectric properties of the compounds pertaining to the TiNiSi 44 family, the main goal of the present work is to define an efficient method to discriminate among 45 the investigated compounds those, which might be both stable and semiconducting. In our 46 previous investigation <sup>1</sup>, we compared the enthalpy of formation of the same combination of 47 48 elements in four structure types to determine the most stable one. In the present work, for the compounds stable in the TiNiSi structure-type, investigation of the electronic band structure 49 will be carried out, to exclude the metallic compounds and keep only the possible 50 semiconductors and semi-metals. A definition and the application of our exclusion criterion 51 52 will be presented in this article. For the most remarkable compounds, the Seebeck coefficient and the thermal conductivity will be estimated using calculations based on the BoltzTrap 53 package <sup>9-10</sup> and the Slack equation <sup>11-12</sup> respectively. All the results will be compared with the 54 literature and the selected compounds will be highlighted. 55

### 56 COMPUTATIONAL DETAILS AND METHODOLOGY

In our previous work <sup>1</sup>, a combinatorial approach has been implemented to screen all possible 57 *T-M-X* combinations with the 1:1:1 stoichiometry generated within a restrained set of chemical 58 elements. In this set of elements, T is a transition metal from the Ti, V, and Cr columns or Sr, 59 Ba, Y and La. *M* is an element from the first line of transition metals and *X* a *sp* element (Al, P, 60 Si, Sn, and Sb). All *T-M-X* combinations have been calculated in four different structure-types: 61 62 the orthorhombic TiNiSi (Pnma), the cubic MgAgAs (F-43m, half-Heusler), the two hexagonal ZrNiAl (P-62m) and BeZrSi (P6<sub>3</sub>/mmc). The 570 possible configurations have been calculated 63 in these 4 structure-types by systematically assigning an unique element from our T-M-X 64

nomenclature to each crystallographic site, discarding "inverse" configurations or site mixing,
yielding 2280 different compounds.

The calculations of the stability and ground-state properties are based on the density functional 67 theory (DFT). This technique allows us to obtain the enthalpy of formation at 0 K for each 68 compound (by total energy difference with the elemental reference state) as well as its electronic 69 structure. The calculations were conducted using the projector augmented wave (PAW) 70 method, implemented in the Vienna Ab initio Simulation Package (VASP)<sup>13-16</sup>. The exchange 71 correlation was described by the generalized gradient approximation modified by Perdew, 72 Burke, and Ernzerhof (GGA-PBE)<sup>17</sup>. An energy cut-off of 600 eV was used for the plane wave 73 basis set. A high-density k-points meshing was employed for Brillouin zone integrations in the 74 TiNiSi structure-type ( $7 \times 11 \times 6$ ), MgAgAs ( $21 \times 21 \times 21$ ), ZrNiAl ( $19 \times 19 \times 37$ ) and BeZrSi 75  $(21 \times 21 \times 10)$ . These parameters ensured robust results in the total energy within convergence 76 tolerance for the calculations set within 10<sup>-6</sup> eV of difference. We performed volume and ionic 77 relaxation steps for each structure-type, and we considered spin polarization for all the 78 configurations. Blöchl correction was applied in a final step calculation <sup>18</sup>. Phonon dispersion 79 bands were obtained by computing the atomic forces for different, finite atomic displacements 80 <sup>19</sup> and a subsequent calculation and integration over the corresponding phonon frequencies, 81 within the harmonic approximation. i.e. without any volume dependence, using the Phonopy 82 code  $^{20-21}$ . The phonon calculations were carried out within a  $1 \times 2 \times 1$  supercell (24 atoms) 83 84 with 12 atomic displacements for the TiNiSi structure-type.

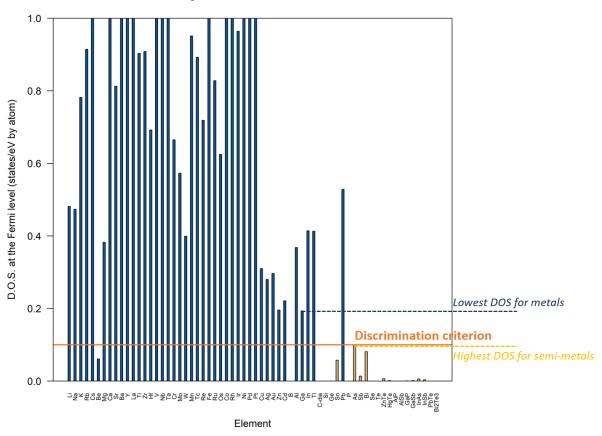
The Seebeck coefficient was calculated from the Boltzmann transport theory <sup>22</sup> as implemented in the BoltzTrap simulation package (v2)  $^{9-10}$ . The BoltzTrap code uses the electronic structure calculated with a dense k-mesh (12 x 20 x 10) from VASP as an input data and assumes a constant relaxation time for the electrons. The first step of our selection concerns the stability of the calculated compounds. A positive enthalpy of formation leads to the exclusion of the combination, as it is obvious that the ternary compound is unstable toward the decomposition into its pure elements. In the second step, the most negative enthalpy of formation of the four-competing structure-types at the same composition, allows the selection of the most probable stable structure. Comparison with the literature and the crystallographic database has confirmed the robustness of our model <sup>1</sup>.

### 95 Definition of the non-metallic criterion

In addition to the stability criterion, it is important to find a simple and robust way to exclude 96 97 metallic compounds for thermoelectric application. For this purpose, we decided to focus our screening method on the density of states (DOS) at the Fermi level  $(E_F)$ . By definition, when 98 the DOS is zero at the  $E_{\rm F}$ , a semiconducting or insulating ground-state is expected. However, 99 DFT-PBE is known<sup>23-24</sup> to not only systematically underestimate the gap magnitude but also 100 to provide a non-zero DOS for known semiconductors. To compensate for this spurious effect, 101 102 a non-zero discrimination criterion to select semiconductors is thus required to assess an unknown ground state (not too strict so as to miss interesting compounds and not too high for 103 being efficiently selective). To estimate this value, preliminary calculations have been 104 105 performed on the chemical elements in their stable structure (table S1) at 0 K and on known semiconducting binary compounds. Most of the elements of the periodic table have been 106 investigated, except the 4f elements and the noble gas, whereas the investigated binary 107 compounds have been chosen among known semiconductors or semi-metals. 108

The calculated DOS are presented in Fig. 1. As expected, all the metallic elements (*s*, *d* blocks) have a non-zero DOS at  $E_F$ , consistent with their metallic ground-state. In group *III*, (B, Al, Ga, In), the last three elements present a non-zero DOS at  $E_F$  in agreement with their metallic ground-state whereas B has a zero DOS consistent with its semiconducting ground-state <sup>25</sup>.

When looking at the first elements from group IV(C, Si, Ge), it is obvious that all the DOS at 113  $E_{\rm F}$  exhibit a zero value. The last two elements of this group, Sn and Pb, have a non-zero DOS 114 at  $E_{\rm F}$ , 0.05 state eV<sup>-1</sup> by atom and 0.5 state eV<sup>-1</sup> by atom, respectively. This very low DOS at 115  $E_{\rm F}$  for Sn agrees with previous results <sup>26</sup> which have shown that "gray tin", the  $\alpha$  form of Sn 116 (A4), which is the stable allotrope at low temperature  $^{27}$ , is semiconducting. Elemental Pb 117 displays a DOS at  $E_F$  similar to the metals of the block d. In group V (P, As, Sb, Bi), P has a 118 zero DOS at  $E_F$  whereas As, Sb, and Bi have a DOS smaller than 0.1 state eV<sup>-1</sup> by atom. This 119 confirms the semi-metallic ground-state of these last three elements, while elemental P is a 120 semiconductor as reported in reference <sup>28</sup>. In group VI with Se and Te, the DOS at  $E_{\rm F}$  is zero as 121 these elements are reported as semiconductors <sup>29-30</sup>. In addition, all the binary compounds 122 presented in Figure 1 exhibit a zero DOS or a very low DOS at  $E_F$ , smaller than 0.005 state eV<sup>-</sup> 123 <sup>1</sup> by atom, which is consistent with their semiconducting ground states. 124



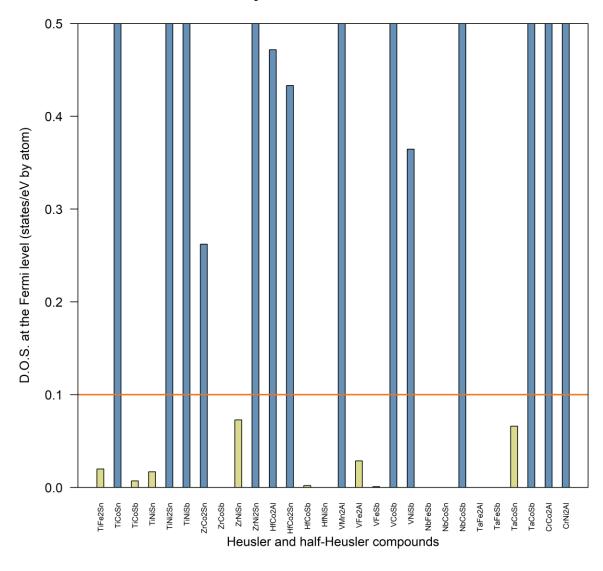
Density of states at the Fermi level

Figure 1. Density of states (DOS) at  $E_F$  for a selection of pure elements and binary compounds; reported semiconductors and semi-metals are in yellow and metals are in blue.

Reported results in Figure 1 allow to show an interval between the DOS at  $E_{\rm F}$  for known 128 semiconductor or semi-metallic elements such as Sn or As and these of Ga and Zn, two metallic 129 elements. Thus, with a selection limit set at 0.1 state  $eV^{-1}$  by atom for the DOS at  $E_{\rm F}$ , 130 semiconductors, as well as elements with a semi-metallic ground state such as As or Sb, are 131 kept whereas metals are excluded. Only one exception to this criterion is found: with this limit, 132 Be, which is known as a metal is also selected. However, Be is known to exhibit a very low 133 DOS at  $E_{\rm F}$ , despite its metallic behaviour <sup>31-34</sup>. Overall, this limit ensures a judicious selection 134 with a very small number of ambiguous results. 135

These calculations on elemental and known binary semiconductors allowed to establish an empirical discrimination criterion. However, before using it to screen unknown compounds, an additional test has been made on reported compounds from the Heusler family (full and half-Heusler). This family has been chosen because it has already been the object of several studies <sup>4-5, 35</sup>, Heusler compounds are very similar chemically to our screened compounds and metallic, semi-metallic and semiconductors compounds are reported in this family. The results are presented in the figure 2 with the DOS at  $E_{\rm F}$  for the considered ternary intermetallic compounds.

Density of states at the Fermi level



144Figure 2 : Density of states (DOS) at  $E_F$  for a selection of half-Heusler and Heusler compounds;145reported semiconductors and semi-metals are in yellow and metals are in blue.

As presented in *Figure 2*, our discrimination criterion is efficient to sort metals for semiconductors. Most of the reported semiconductors in the Heusler family exhibit a zero DOS at  $E_F$ . However, some reported semiconductors or semi-metals do not and would be excluded without our criterion, even though, according to the literature, they are promising thermoelectric compounds. This is the case for ZrNiSn, TaCoSn or Fe<sub>2</sub>VAl <sup>36-39</sup>. Indeed, ZrNiSn is a very good example of both the necessity and the relevance of our discrimination criterion. As presented **Figure 2**, the DOS( $E_F$ ) is equal to 0.07 states/eV by atom, which is not strictly zero, however when looking at the density of states as a function of the energy, it is clear that the value falls down to zero in the vicinity of the Fermi energy (see figure 4 in reference <sup>1</sup>). A non-zero criterion is therefore essential to get rid of the calculation errors and uncertainties on both the density of states and the position of the Fermi level. Finally, our criterion allows to screen efficiently the Heusler family by excluding only metallic compounds. The robustness of our model being proven, another intermetallic family can be investigated.

### 159 Twelve selected compounds in the TiNiSi structure type

Among the 570 unique configurations calculated in the 4 structures type, 317 compounds are more stable in the TiNiSi structure-type than in any other structure type. But only 12 compounds are found to be non-metallic, according to the electronic criterion set at 0.1 state  $eV^{-1}$  by atom for the DOS at  $E_F$ . They are reported in Table 1. All of these compounds are mechanically stable (no imaginary frequency is observed in their phonon bands, figure S2).

Half-metals<sup>40</sup>, which can be interesting for spintronic applications have also been searched. For 165 these compounds, the majority-spin electrons are metallic whereas the minority-spin electrons 166 are semiconducting. The criterion was applied to each spin directions. Eleven compounds 167 complied with this criterion but only four are stable in the TiNiSi structure-type: CrNiSi, 168 SrTiSn, BaVSb and BaCrSn (the DOS of these compounds are presented in figure S3 and 169 phonon bands in figure S4). Nonetheless, these compounds are not interesting for 170 thermoelectricity since they display a metallic total DOS and will not be investigated in detail 171 in the following. 172

### 173 *Table 1* Non-metallic compounds in the TiNiSi structure type.

TMX Compounds	Crystal databases	Enthalpy of formation (kJ mol <sup>-1</sup> )	DOS at the Fermi level (state. eV <sup>-1</sup> by atom)
TiCuSb	Unreported	-20.90	0.092

ZrZnSi	Unreported	-62.22	0.098	
HfMnSb	Unreported	-26.15	0.098	
HfCuSb	Unreported	-27.12	0.015	
HfZnSi	Unreported	-52.84	0.098	
TaCuSi	Unreported	-44.15	0.043	
MoZnSi	Unreported	-15.53	0.062	
TiMnSb	BeZrSi	-23.06	0.071	
TiCoP	TiNiSi	-109.95	0.068	
TiNiSi	TiNiSi	-88.47	0.061	
HfCoP	TiNiSi	-109.99	0.032	
TaNiP	TiNiSi	-73.48	0.062	

We will first review the existence and structure of each selected compound. Then, for each candidate, a more specific study of the electronic structure will be presented. Finally, to assess their thermoelectric properties, the calculated values of the Seebeck coefficient and the thermal conductivity, will be examined.

Seven compounds among the 12 have not been reported in crystal structure databases. However, a careful study of phase diagrams may provide additional information. For the Ti-Cu-Sb, Zr-Zn-Si, Hf-Cu-Sb, and Ta-Cu-Si systems, no equimolar compound has been reported in the ternary phase diagram <sup>41-45</sup>. It is therefore unlikely that an equimolar compound is stable in the ternary orthorhombic structure, but it cannot be formally discarded. For the 3 other unreported compounds, HfMnSb, MoZnSi, and HfZnSi, no phase diagram is available for the corresponding systems, it is therefore difficult to conclude on their existence.

Among the 5 reported compounds, TiMnSb has been reported in the literature to crystallize in the BeZrSi structure type <sup>46</sup> in contrast with our calculations of a stable TiNiSi prototype. However, as discussed in our previous work <sup>1</sup>, this discrepancy can be explained by the experimental conditions for the synthesis. Indeed, Noda *et al.* <sup>46</sup> have obtained TiMnSb under extreme conditions (high pressure and high temperature) possibly giving rise to a nonequilibrium phase.

Finally, four compounds are reported in the crystallographic databases in the orthorhombic 192 193 TiNiSi structure. In the cases of TiCoP and TaNiP, the literature only deals with their crystal structure and there is no investigation of their electronic properties <sup>47-48</sup>. More information is 194 provided for the other two compounds: TiNiSi and HfCoP. Recently, Huang et al. 49 195 investigated the thermoelectric properties of TiNiSi-based solid solutions. Theoretical results, 196 based on DFT calculations with PBE-GGA, confirmed the presence of a pseudo-gap in the 197 electronic band structure of TiNiSi. Measurements of the electric conductivity versus the 198 temperature confirmed that TiNiSi is a semi-metal while thermoelectric properties were 199 improved by the substitution of Ti by V<sup>49</sup>. These results confirm a previous report by Kong et 200 al. 50 who have also highlighted the semi-metallic ground state of TiNiSi, thanks to their 201 calculations. HfCoP, based on an extended Hückel calculation by Kleinke et al. <sup>51</sup>, was 202 considered as a metal. However, neither the electronic density of states nor the electrical 203 204 resistivity was reported in this reference. The ground state of HfCoP is hence currently unknown. 205

### 206 Seebeck coefficient and lattice thermal conductivity at finite temperature

The Seebeck coefficient was calculated at finite temperatures within the semi-classical Boltzmann transport theory with the BoltzTrap package, assuming a constant relaxation time. The possibility of calculating the electronic thermal conductivity and electrical conductivity offered by the package was not implemented because these quantities depend on the electronic relaxation time, which then plays the role of an adjustable parameter. This is not the case for the Seebeck coefficient, which is independent on the relaxation time when it is assumed to be constant.

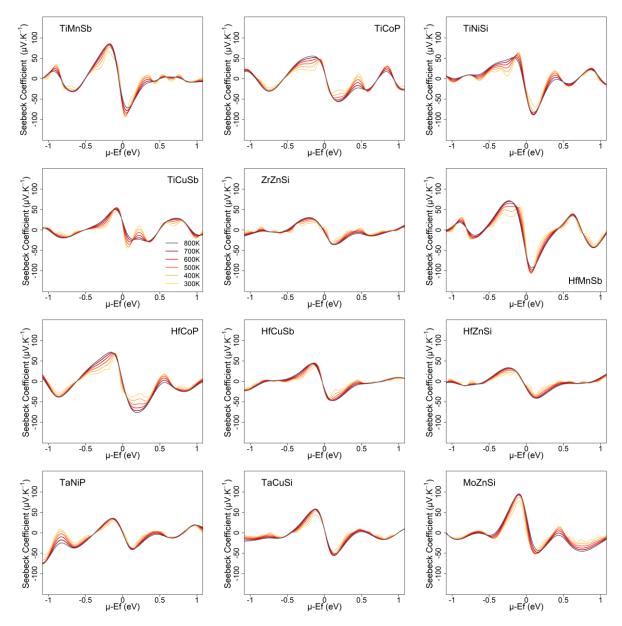


Figure 3. Calculated Seebeck coefficient as a function of the chemical potential for each
compound. Each curve corresponds to a temperature varying by steps of 100K in the range 300
K (yellow) to 800 K (black).

The Seebeck coefficient has been plotted as a function of the chemical potential ( $\mu$ ) for each selected compound in the energy window [-1; +1 eV], which systematically covers the charge carrier concentration range [-10<sup>22</sup> – 10<sup>22</sup> cm<sup>-3</sup>], well beyond the experimental doping concentrations conventionally achieved. Figure 3 presents for each compound the variations of *S* for several temperatures varying by steps of 100 K in the range 300 K and 800 K. For the positive values of the Seebeck coefficient, increase with the temperature rise is generally observed. Only, TiNiSi and TiCuSb exhibit a different behaviour with Seebeck coefficient at

300 K higher than at 800 K. Even though this trend is maintained for the negative Seebeck
coefficient, with the absolute value at 800 K higher than at 300 K, four compounds exhibit an
opposite behaviour, TiMnSb, TiCuSb, MoZnSi and HfMnSb.

Several compounds like ZrZnSi or HfZnSi do not show values of the Seebeck coefficient larger than  $\pm$  50  $\mu$ V K<sup>-1</sup> and therefore do not seem to be very promising in contrast with TiMnSb or MoZnSi for example. First extremum of the calculated Seebeck coefficient close to the Fermi level are listed in Table 2. In this table, values at 700 K are reported, to compare the compounds in the same way as it will be done for the lattice thermal conductivity (values at 300 K are reported in table S2). We choose to focus on the maximal values of the Seebeck coefficient when  $\mu$  is near the Fermi level for an easy comparison.

TMX compounds	$S_{\max} (\mu V K^{-1}) > 0$ (700K)	$S_{\max} (\mu V K^{-1}) < 0$ (700K)	Slack's lattice Thermal conductivity at 700K (W m <sup>-1</sup>
	(10011)	(10011)	K <sup>-1</sup> )
TiMnSb	85	-78	5.4
TiCoP	52	-55	15.7
TiNiSi	54	-87	13.7
TiCuSb	52	-28	3.9
ZrZnSi	30	-36	9.9
HfMnSb	70	-98	6.1
HfCoP	71	-72	11.6
HfCuSb	44	-47	3.7
HfZnSi	33	-41	7.4
TaNiP	41	-76	7.6
TaCuSi	58	-54	9.7
MoZnSi	95	-48	6.5

As mentioned before, ZrNiSi, HfZnSi, HfCuSb, and TaCuSi present quite low Seebeck coefficient near the Fermi energy, regardless their conduction type. Considering both positive and negative values, TiMnSb and HfMnSb can be considered as the best compounds when other compounds could be promising at most in one of the two conduction types. For example, TiNiSi has a negative Seebeck coefficient twice as large as its positive counterpart whereas it is the

opposite for MoZnSi. These results are comparable at other temperatures where similar trend can be noticed (table S2). No clear tendencies can be noticed in the evolution of the Seebeck coefficient regarding the nature of each T, M or X element in these compounds.

Lattice thermal conductivity, which is essential for the determination of *ZT*, can be estimated by the Slack's equation <sup>11-12</sup> by assuming that heat is conducted only by acoustic phonons <sup>52-53</sup>, through the equation 2:

249 
$$K_L = 3.1 \times 10^{-6} \frac{M \,\theta_D^3 \delta}{\gamma^2 n_3^3 T}$$
(2)

where  $\theta_D$  is the Debye temperature in K,  $\delta^3$  is the volume per atom in Å<sup>3</sup>, *n* is the number of 250 atoms in the primitive unit cell,  $M_{ay}$  is the average atomic mass in the atomic unit and y is the 251 average Grüneisen parameter. The Debye temperature and the Grüneisen parameter are 252 evaluated from the transverse and longitudinal sound velocity, which are obtained from the 253 calculated elastic modulus. The calculated elastic properties (table S3) have been obtained from 254 the phonon calculations for each compound (see figure S2). Slack's model neglects the transport 255 256 of heat by optical phonons and this could lead to underestimated values of lattice thermal conductivity. However, it also assumes that the acoustic phonons are scattered only by acoustic 257 phonons, neglecting all the other scattering mechanisms (isotopes, impurities, vacancies, charge 258 carriers, dislocations, grain boundaries, crystal boundaries, etc.) This last approximation has the 259 strongest impact on Slack's values <sup>12</sup>, which are systematically overestimated (up to an order 260 of magnitude) as soon as the relative atomic mass difference of the constituting elements is 261 larger than roughly  $\sim 100\%$  <sup>12</sup>: this condition is indeed fulfilled for the 12 screened compounds. 262 Despite these drawbacks, Slack's model provides reliable trends at temperatures larger than the 263 264 Debye temperature, when phonon – phonon scattering dominates over the other scattering processes. To fulfil this condition for all the compounds, the values presented in Table 2 were 265 calculated at 700 K. 266

The range of lattice thermal conductivity values is quite broad with estimated values between 267 3 and 15 W m<sup>-1</sup> K<sup>-1</sup> which cannot be compared to experimental values due to lack of data. These 268 values are quite large compared to the best thermoelectric materials such as Bi<sub>2</sub>Te<sub>3</sub> or Sb<sub>2</sub>Te<sub>3</sub> 269 which exhibit low thermal lattice thermal conductivity (~  $2 \text{ W m}^{-1} \text{ K}^{-1}$ )<sup>54</sup>. They are, nonetheless, 270 still promising because they were calculated for a perfect crystal and thus as above discussed, 271 overestimated. Moreover, it is known that defects or impurities can strongly decrease the lattice 272 thermal conductivity. For instance, the half-Heusler HfNiSn displays a thermal conductivity of 273 10 W m<sup>-1</sup> K<sup>-1</sup> at 300 K <sup>55</sup> while the solid solution Hf<sub>0.75</sub>Zr<sub>0.25</sub>NiSn<sub>0.99</sub>Sb<sub>0.02</sub>displays a thermal 274 conductivity of 5 W m<sup>-1</sup> K<sup>-1</sup> at 300 K and ZT = 0.9 at 800 K <sup>56</sup>. 275

Keeping the *X*-element constant and considering the *T* element, as expected, the lattice thermal conductivity is, in general, lower for "heavier" *T* in the same columns of the periodic table as for *T*CuSb or *T*CoP. In the case of *T*MnSb, the trend is reversed as  $\kappa_L$ (TiMnSb) is lower than  $\kappa_L$ (HfMnSb). Keeping the *T* element constant and considering the *X* element, we noticed-that the antimonides present the lowest thermal conductivity compared to the silicides or the phosphides, in accordance with the larger atomic mass of antimony.

### 282 DISCUSSION

Keeping in mind that the values presented here are from calculations based on DFT-PBE and 283 constant relaxation time approximation implemented in a perfect crystal, our study offers the 284 possibility to identify the most promising compounds among the 12 selected TiNiSi-type 285 compounds from our screening of 570 possible compositions. For example according to Table 286 2, even though, lattice thermal conductivity is quite low for the two TCuSb compounds, their 287 288 Seebeck coefficients are also systematically low. ZrNiSi and TaCuSi exhibit also low Seebeck coefficient, which are for these compounds accompanied by high lattice thermal conductivity 289 values. Thus, if one adds to these low values the fact that, according to the reported ternary 290

291 phase diagram, these four compounds are not stable, it is probably not worth trying their292 synthesis.

On the other hand, HfMnSb and MoZnSi combine large Seebeck coefficients and a small lattice
thermal conductivity that could lead to interesting properties. Nonetheless, their existence is not
established.

296 Regarding the four compounds which have already been reported in the literature, a ranking is 297 also possible. The highest value of the Seebeck coefficient is reached in TiNiSi, which has already been reported as interesting for its thermoelectric properties in the solid solution 298 Ti<sub>1-x</sub>V<sub>x</sub>NiSi<sup>49</sup>. The presently calculated values of the Seebeck coefficient seem to confirm the 299 calculated values calculated by Huang et al. <sup>49</sup>, with  $S \approx \pm 65 \,\mu\text{V}$ . K<sup>-1</sup> at 300 K for both type of 300 charge carrier whereas our calculation gives  $S = 64 \mu V$ . K<sup>-1</sup> and  $S = -69 \mu V$ . K<sup>-1</sup> at 300 K. 301 However, the measured values (-16 µV. K<sup>-1</sup> at 300K) in Ref. <sup>49</sup> differ from the calculated one, 302 but this difference can be explained by the charge carrier concentration of the pristine TiNiSi, 303 which is around  $2 \times 10^{21}$  cm<sup>-3</sup>. This relatively large value indicates the presence of intrinsic 304 defects in the sample. Finally, HfCoP seems to be more interesting than TiCoP as its Seebeck 305 coefficient is larger and associated with a lower lattice thermal conductivity. TaNiP exhibits 306 the lowest lattice thermal conductivity of the four reported compounds and negative Seebeck 307 coefficient of the same order of magnitude as in HfCoP. 308

### 309 CONCLUSION

After determining the stability of thousands of *TMX* compositions in 4 structure types, a more focused investigation has been undertaken on the compounds which crystallize in the TiNiSi structure type. In a second stage, the electronic band structure has been examined and an effective criterion of the DOS at the Fermi level has been established by comparing calculated DOS of known semiconducting elements and compounds. Then, this empirical criterion of 0.1

state eV<sup>-1</sup> by atom has been applied to the TMX compounds, stable in the orthorhombic 315 316 structure. It has led to the selection of 12 non-metallic compounds among the 317 possible compounds while it was commonly admitted that all the TiNiSi are metallic <sup>57</sup>. Additional 317 phonon and BoltzTrap calculations allowed to rank the 12 selected compounds to identify those 318 which are the most interesting to be synthesized from the point of view of their anticipated 319 thermoelectric properties. Although MoZnSi could be an interesting compound as it presents 320 321 the highest Seebeck coefficient associated with a small lattice thermal conductivity, there is no information about its possible stability. So, it seems more relevant to focus on HfCoP and 322 TaNiP as starting points. Both compounds are already reported in the literature as crystallizing 323 in the TiNiSi structure type <sup>48, 51</sup> and present the best compromise between high Seebeck 324 coefficient and a low lattice thermal conductivity. 325

### 326 ACKNOWLEDGEMENTS

327 DFT calculations were performed using HPC resources from GENCI-CINES (Grant 2019-328 A0060906175) and financial support from the Agence Nationale de la Recherche is 329 acknowledged (ANR-18-CE05-0010-01).

### 330 SUPPORTING INFORMATION AVAILABLE

**Table S1**: Elemental, binaries and ternaries compounds information's

Figure S1: Electronic density of states for the twelve TMX compounds calculated by DFT
using GGA-PBE approximation. The Fermi level is chosen as the origin of energies. The
discrimination criterion is represented by the red dotted line.

Figure S2: Phonon curves dispersion of the twelve TMX compounds calculated using thePhonopy code.

337	Figure S3:	Electronic	density	of states	for the	four	(half-metals)	TMX	compounds	calculated
-----	------------	------------	---------	-----------	---------	------	---------------	-----	-----------	------------

by DFT using GGA-PBE approximation. The Fermi level is chosen as the origin of energies.

Both spin directions are presented.

340 Figure S4: Phonon curves dispersion of the four (half-metals) TMX compounds calculated

341 using the Phonopy code.

342 Table S2: Values of the first extremum of the calculated Seebeck coefficient close to the Fermi

343 level at 300 K for the TiNiSi compounds.

**Table S3**: The bulk modulus (B), shear modulus (G), Young's modulus (E) and Poisson ratio

- 345 (v) of the screened TMX compounds.
- 346 REFERENCES

Barreteau, C.; Crivello, J.-C.; Joubert, J.-M.; Alleno, E., Looking for new thermoelectric materials
 among TMX intermetallics using high-throughput calculations. *Comput. Mater. Sci* 2019, *156*, 96-103.
 Villars, P.; Cenzual, K., Pearson's Crystal Data: Crystal structure database for inorganic

350 compounds. International, A., Ed. Materials Park: Ohio, USA, 2017/2018.

Belsky, A.; Hellenbrandt, M.; Karen, V. L.; Luksch, P., New developments in the Inorganic Crystal
 Structure Database (ICSD): accessibility in support materials research and design. *Acta Crystallogr. B* **2002**, *58*, 364-369.

Feng, Z.; Fu, Y.; Putatunda, A.; Zhang, Y.; Singh, D. J., Electronic structure as a guide in screening
 for potential thermoelectrics: demonstration for half-Heusler compounds. *Phys. Rev. B* 2019, *100*,
 085202.

5. Guo, S.; Jia, T.-T.; Zhang, Y., Electrical properties dominated promising half-Heusler thermoelectrics through high-throughput materials computations. *J. Phys. Chem. C* **2019**, *123*, 18824-18833.

Legrain, F.; Carrete, J.; van Roekeghem, A.; Madsen, G. K. H.; Mingo, N., Materials screening
for the discovery of new half-Heuslers: Machine learning versus *ab initio* methods. *J. Phys. Chem. B* **2017**, *122*, 625-632.

- 363 7. Ma, J.; Hegde, V. I.; Munira, K.; Xie, Y.; Keshavarz, S.; Mildebrath, D. T.; Wolverton, C.; Ghosh,
  364 A. W.; Butler, W. H., Computational investigation of half-Heusler compounds for spintronics
  365 applications. *Phys. Rev. B* 2017, *95*, 024411.
- 366 8. Zeeshan, M.; Singh, H. K.; van den Brink, J.; Kandpal, H. C., *Ab initio* design of new cobalt-based
  367 half-Heusler materials for thermoelectric applications. *Phys. Rev. Mater.* **2017**, *1*, 075407.

Madsen, G. K. H.; Singh, A. K., BoltzTrap. A code for calculating band-structure dependent
 quantities. *Comput. Phys. Comm.* 2006, 175, 67-71.

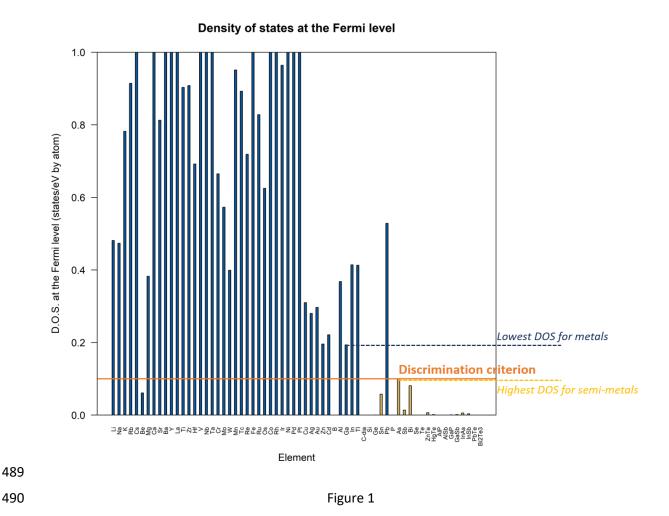
Madsen, G. K. H.; Carrete, J.; Verstraete, M. J., BoltzTrap2, a program for interpolating ban
structures and calculating semi-classical transport coefficients. *Comput. Phys. Comm.* 2018, 231, 140145.

- 373 11. Slack, G. A., Nonmetallic crystals with high thermal conductivity. *J. Phys. Chem. Solids* 1973, *34*,
  374 321-335.
- Slack, G. A., The thermal conductivity of nonmetallic crystals. *Solid State Physics* 1979, *34*, 171.
- 13. Kresse, G.; Hafner, J., *Ab-initio* molecular dynamics for liquid metals. *Phys. Rev. B* **1993**, *47*, 558(R).
- Kresse, G.; Joubert, D., From ultrasoft pseudopotentials to the projector augmented-wave
  method. *Phys. Rev. B* 1999, *59* (3), 1758-1775.
- 15. Kresse, G.; Furthmüller, J., Efficient iterative schemes for an *ab-initio* total-energy calculations
  using plane-wave basis set. *Phys. Rev. B* 1996, *54*, 11169-11186.
- 16. Hafner, J.; Kresse, G.; Vogtenhuber, D.; Marsman, M. The Vienne *Ab-Initio* Simulation Package (VASP).
- Perdew, J. P.; Burke, K.; Ernzerhof, M., Generalized gradient approximation made simple. *Phys. Rev. Lett.* **1996**, *77*, 3865-3868.
- 18. Blöchl, P. E.; Jepsen, O.; Andersen, O. K., Improved tetrahedron method for Brillouin-zone
  integrations. *Phys. Rev. B* 1994, *49* (23), 16223-16233.
- Parlinski, K.; Li, Z. Q.; Kawazoe, Y., First-principles determination of the soft mode in cubic ZrO<sub>2</sub>. *Phys. Rev. Lett.* **1997**, *78*, 4063-4066.
- Togo, A.; Tanaka, I., First-principles phonon calculations in materials science. *Scr. Mater.* 2015,
   *108*, 1-5.
- Togo, A.; Oba, F.; Tanaka, I., First-principles calculations of the ferroelastic transition between
   rutile-type and CaCl<sub>2</sub>-type SiO<sub>2</sub> at high pressures *Phys. Rev. B* **2008**, *78*, 134106.
- Ashcroft, N. W.; Mermin, N. D., *Solid State Physics*. Saunders College Publishing: Orlando, 1976.
   Tran, F.; Blaha, P., Importance of the kinetic energy density for band gap calculations in solids
- with density functional theory. J. Phys. Chem. A **2017**, 121, 3318-3325.
- Yakovkin, I. N.; Dowben, P. A., The problem of the band gap in LDA calculations. *Surface Review and Letters* 2007, *14* (3), 481-487.
- 400 25. Greiner, E. S.; Gutowski, J. A., Electrical Resistivity of Boron. *J. Appl. Phys.* 1957, *28*, 1364-1365.
  401 26. Yu, C.; Liu, J.; Lu, H.; Chen, J., Ab initio calculation of the properties and pressure induced
- 402 transition of Sn. *Sol. State. Commun.* **2006**, *140*, 538-543.
- 403 27. Busch, G. A.; Kern, R., Seminducting properties of gray tin. *Sol. Stat. Phys.* **1960**, *11*, 1-40.
- 404 28. Goodman, N. B.; Ley, L.; Bullett, D. W., Valence-band structures of phosphorus allotropes. *Phys.*405 *Rev. B* 1983, *27*, 7440-7450.
- 406 29. Reitz, J. R., Electronic band strucuture of Selenium and Tellurium. *Phys. Rev.* **1957**, *105*, 1233407 1240.
- 408 30. Gaspar, R., Electronic structure of semi-conducting selenium and tellurium. *Acta Physica* 1957,
  409 7, 289-311.
- 410 31. Loucks, T. L.; Cutler, P. H., Band structure and Fermi surface of Beryllium. *Phys. Rev.* 1964, 133,
  411 A819-A829.
- 412 32. Mitchell, M. A., Electrical resistivity of beryllium. J. Appl. Phys. **1975**, 46, 4742-4746.
- 413 33. Chou, M. Y.; Lam, P. K.; Cohen, M. L., *Ab initio* study of structural and electronic properties of
  414 beryllium. *Phys. Rev. B* 1983, *28*, 4179-4185.
- 415 34. Papaconstantopoulo, D. A., *Handbook of the band structure of elemental solids*. Springer US:
  416 2015; Vol. 3, p 655.
- 417 35. Gillessen, M.; Dronskowski, R., A combinatorial study of full Heusler alloys by first-principles
  418 computational methods. *J. Comput. Chem.* 2009, *30*, 1290-1299.
- 419 36. Li, S.; Zhu, H.; Mao, J.; Feng, Z.; Li, X.; Chen, C.; Cao, F.; Liu, X. J.; Singh, D. J.; Ren, Z.; Zhang, Q., 420 n-type TaCoSn-based half-Heusler as promising thermoelectric materials. *Appl. Mater. Interfaces* **2019**,
- 421 *11*, 41321-41329.
- 422 37. Maier, S.; Denis, S.; Adam, S.; Crivello, J.-C.; Joubert, J. M.; Alleno, E., Order-disorder transitions
  423 in the Fe<sub>2</sub>VAI Hesuler alloy. *Acta Materialia* **2016**, *121*, 126-136.

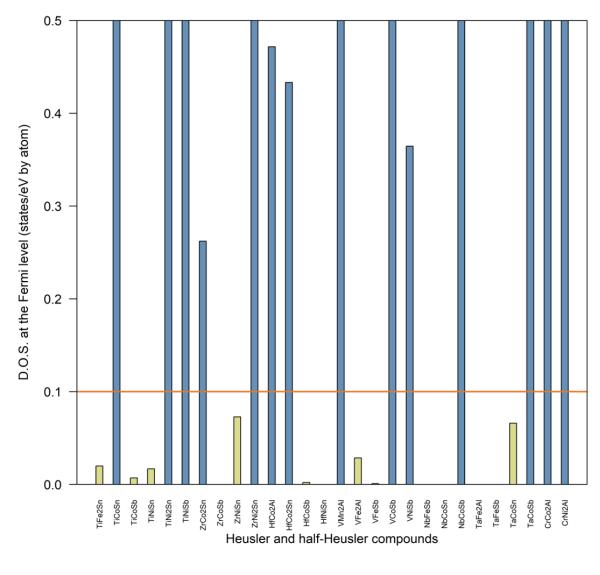
- 424 38. Kuentzler, R.; Clad, R.; Schmerber, G.; Dossmann, Y., Gap at the Fermi level and magnetism in 425 RMSn ternary compounds (R= Ti, Zr, Hf and M= Fe, Co, Ni). *J. Magn. Magn. Mater.* **1992**, *104-107*, 426 1976-1978.
- Hu, T.; Yang, D.; Su, X.; Yan, Y.; You, Y.; Liu, W.; Uher, C.; Tang, X. F., Interpreting the combustion
  process for high-performance ZrNiSn thermoelectric materials. *ACS Appl. Mater. Interfaces* 2018, 10,
  864-872.
- 430 40. de Groot, R. A.; Mueller, F. M.; van Engen, P. G.; Buschow, K. H. J., New class of materials: half-431 metallic ferromagnets. *Phys. Rev. Lett.* **1983**, *50*, 2024-2027.
- 432 41. Dolotko, O. V.; Dmytriv, G. S.; Pavlyuk, V. V., Interaction of Components in the Zr-Zn-Si System 433 at 600 °C. *Pol. J. Chem.* **2001**, *75*, 453-455.
- 434 42. Kobluyk, N. A.; Romaka, L. P.; Bodak, O. I., Interaction between the components in the Ti-Cu-435 Sb system at 770 K. *J. Alloys Compd.* **2000**, *309*, 176-178.
- 43. Melnychenko-Koblyuk, N.; Romaka, L.; Akselrud, L. G.; Romaka, V. V.; Stadnyk, Y., Interaction
  437 between components in Hf-Cu-Sb ternary system at 770K. *J. Alloys Compd.* **2008**, *461*, 147-149.
- 438 44. Savitskii, E. M.; Efimov, Y. V.; Frolova, T. M., Copper effect on structure and superconductive
  439 properties of transition metal silicides [V(Nb, Ta, Cr, Mo, W)-Si-Cu alloy systems]. *Izv. Akad. Nauk SSSR*,
  440 *Neorg. Mater.* 1979, *15*, 654-657.
- 441 45. Reid, J. S.; Kolawa, E.; Nicolet, M.-A., Thermodynamics of (Cr, Mo, Nb, Ta, V or W)-Si-Cu ternary 442 systems. *J. Mater. Res.* **1992**, *7* (9), 2424-2428.
- 443 46. Noda, Y.; Shimada, M.; Koizumi, M., High-pressure synthesis and magnetic properties of 444 MMnSb (M= Ti, V, Cr) with Ni<sub>2</sub>In type structures. *Inorg. Chem.* **1984**, *23*, 628-630.
- 445 47. Rundqvist, S.; Nawapong, P. C., The Crystal Structure of ZrFeP and Related Compounds. *Acta* 446 *Chem. Scand.* **1966**, *20*, 2250-2254.
- 447 48. Lomnytska, Y. F.; Agatinskaya, L. P.; Kuz'ma, Y. B., Component interaction in the system 448 titanium-cobalt-phosphorus. *Sov. Prog. Chem.* **1981**, *47*, 29-32.
- 449 49. Huang, Y.; Nagai, H.; Hayashi, K.; Miyazaki, Y., Preparation and thermoelectric properties of 450 pseudogap intermetallic (Ti<sub>1-x</sub>V<sub>x</sub>)NiSi solid solutions. *J. Alloys Compd.* **2019**, *771*, 111-116.
- 451 50. Kong, B.; Chen, X.-R.; Cai, L.-C.; Zhu, J., Structural and elastic properties of typical equiatomic
  452 ternary intermetallic compound TiNiSi under pressure. *Physica B: Condensed Matter* 2010, 405 (6),
  453 1591-1595.
- 454 51. Kleinke, H.; Franzen, H. F., Synthesis Crystal Structure and Properties of HfM'P (M'= Fe, Co, Ni) 455 in Comparison to ZrNiP. *Z. Anorg. Allg. Chem.* **1996**, *622*, 1893-1900
- Hou, Z.; Takagiwa, Y.; Shinohara, Y.; Xu, Y.; Tsuda, K., Machine-Learning-assisted development
  and theoritical consideration for the Al<sub>2</sub>Fe<sub>3</sub>Si<sub>3</sub> thermoelectric material. *Appl. Mater. Interfaces* 2019,
  11, 11545-11554.
- Shiota, Y.; Muta, H.; Yamamoto, K.; Ohishi, Y.; Kurosaki, K.; Yamanaka, S., A new semiconductor
   Al<sub>2</sub>Fe<sub>3</sub>Si<sub>3</sub> with complex crystal structure. *Intermetallics* **2017**, *89*, 51-56.
- 461 54. Elsheikh, M. H.; Shnawah, D. A.; Sabri, M. F. M.; Said, S. B. M.; Hassan, M. H.; Bashir, M. B. A.;
  462 M., M., A review on thermoelectric renewable energy: Principle parameters that affect their
  463 performance. *Renewable and Sustainable Energy Reviews* 2014, *30*, 331-355.
- 464 55. Uher, C.; Yang, J.; Hu, S.; Morelli, D. T.; Meisner, G. P., Transport properties of pure and doped
  465 MNiSn (M=Zr, Hf). *Phys. Rev. B* 1999, *59*, 8615.
- Yan, X.; Joshi, G.; Liu, W.; Lan, Y.; Wang, H.; Lee, S.; Simonson, J. W.; Poon, S. J.; Tritt, T. M.;
  Chen, G.; Ren, Z. F., Enhanced Thermoelectric Figure of Merit of p-Type Half-Heuslers. *Nano Letters* **2011**, *11*, 556.
- 469 57. Landrum, G. A.; Hoffmann, R. D.; Evers, J.; Boysen, H., The TiNiSi Family of Compounds:
  470 Structure and Bonding. *Inorg. Chem.* **1998**, *37*, 5754-5763.
- 471
- 472

### 473 TABLE OF CONTENTS

- 474
- Figure 1. Density of states (DOS) at  $E_F$  for a selection of pure elements and binary compounds; reported semiconductors and semi-metals are in yellow and metals are in blue.
- 477 Figure 2: Density of states (DOS) at *EF* for a selection of half-Heusler and Heusler
  478 compounds; reported semiconductors and semi-metals are in yellow and metals are in blue.
- Figure 3. Calculated Seebeck coefficient as a function of the chemical potential for each
  compound. Each curve corresponds to a temperature varying by steps of 100K in the range
  300 K (yellow) to 800 K (black).
- 482 **Table 1** Non-metallic compounds in the TiNiSi structure type.
- 483 Table 2. Values of the first extremum of the calculated Seebeck coefficient close to the
- 484 Fermi level and Slack's lattice thermal conductivity at 700 K for the TiNiSi compounds.
- 485
- 486

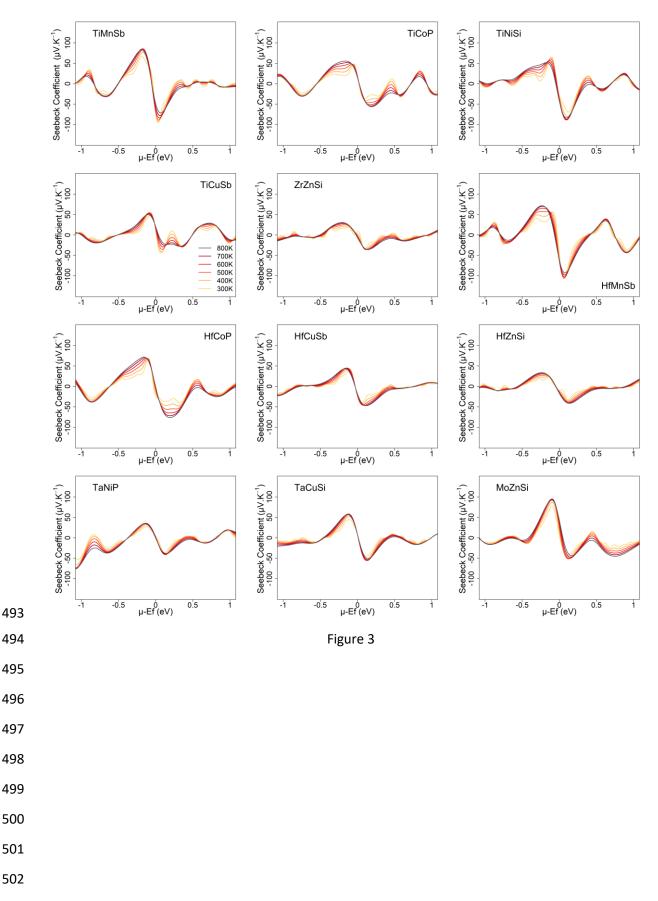


Density of states at the Fermi level



491 492

Figure 2



TMX Compounds	Crystal databases	Enthalpy of formation (kJ mol <sup>-1</sup> )	DOS at the Fermi level (state. eV <sup>-1</sup> by atom)
TiCuSb	Unreported	-20.90	0.092
ZrZnSi	Unreported	-62.22	0.098
HfMnSb	Unreported	-26.15	0.098
HfCuSb	Unreported	-27.12	0.015
HfZnSi	Unreported	-52.84	0.098
TaCuSi	Unreported	-44.15	0.043
MoZnSi	Unreported	-15.53	0.062
TiMnSb	BeZrSi	-23.06	0.071
TiCoP	TiNiSi	-109.95	0.068
TiNiSi	TiNiSi	-88.47	0.061
HfCoP	TiNiSi	-109.99	0.032
TaNiP	TiNiSi	-73.48	0.062

Table 2

TMX compounds	$S_{\max} (\mu V K^{-1}) > 0$ (700K)	$S_{\max} (\mu V K^{-1}) < 0$ (700K)	Slack's lattice Thermal conductivity at 700K (W m <sup>-1</sup> K <sup>-1</sup> )
TiMnSb	85	-78	5.4
TiCoP	52	-55	15.7
TiNiSi	54	-87	13.7
TiCuSb	52	-28	3.9
ZrZnSi	30	-36	9.9
HfMnSb	70	-98	6.1
HfCoP	71	-72	11.6
HfCuSb	44	-47	3.7
HfZnSi	33	-41	7.4
TaNiP	41	-76	7.6
TaCuSi	58	-54	9.7
MoZnSi	95	-48	6.5