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1 2	INTERNAL WAVE-DRIVEN MIXING: GOVERNING PROCESSES AND CONSEQUENCES FOR CLIMATE
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1. Abstract

Turbulent mixing from breaking oceanic internal waves drives a vertical transport of water, 16 heat and other climatically important tracers in the ocean, thereby playing an important role in 17 shaping the circulation and distributions of heat and carbon within the climate system. Linking 18 internal wave-driven mixing to its impacts on climate poses a formidable challenge, since it requires 19 understanding of the complex lifecycle of internal waves-including generation, propagation, and 20 breaking into turbulence—and knowledge of the spatio-temporal variability of these processes in the 21 diverse, rapidly evolving oceanic environment. This review traces the energy pathways from tides, 22 winds and geostrophic currents to internal wave mixing while attempting to connect this mixing 23

with the global climate system, with the aim of inspiring future work on internal wave-driven mixing
across all scales.

26	2. Key Points
27	• Tides, winds, and geographic currents can generate oceanic internal waves and as a result
28	are major sources of energy for the internal wave field.
29	• Interactions between internal waves and topography, currents, or other internal waves can
30	transfer energy to smaller spatiotemporal scales. However, how these processes combine to
31	yield the observed internal wave environment is not well understood.
32	• Eventually, internal waves can become unstable, causing them to turbulently dissipate en-
33	ergy and mix water across density classes, thereby altering ocean dynamics.
34	• The location and timing of internal wave generation, energy transfer to smaller scales, and
35	subsequent turbulent dissipation conspire to form the continually evolving global distribu-
36	tion of mixing from internal waves.
37	• The global climate is shaped by the magnitude and geography of internal wave mixing.
38	Future work can provide an integrated understanding of internal wave mixing in an evolving
39	climate system.

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3. Introduction

Just like surface waves exist along the sharp density interface at the boundary between the ocean and atmosphere, internal waves are often supported by smooth vertical gradients in density far beneath the ocean's surface. Internal waves often become unstable and break, generating turbulence. A single patch of ocean turbulence from an unstable internal wave dissipates energy, alters the stratification by mixing water of different densities, and thereby plays an important dynamical role in the local environment. Close to the surface and the seafloor, instabilities that are unrelated to internal waves often dominate the production of turbulence [1, 2]. However, away
from surface and bottom boundaries, internal waves are the primary cause of turbulent mixing.

In aggregate, such small (centimeter to meter) scale mixing from internal waves is essential for 49 sustaining the global overturning circulation [3, 4, 5, 6] and closing the global ocean energy budget 50 [7, 8, 9]. Internal wave-driven mixing is also important for transporting tracers such as nutrients, 51 greenhouse gases, and carbon [10, 11, 12, 13, 14] around the planet, thus shaping the biological 52 landscape of the global ocean [15]. Mixing from internal waves varies substantially in both space 53 and time throughout the ocean. Its distribution is set by the diverse processes that generate internal 54 waves (including tides, winds or larger-scale geostrophic ocean currents), alter their propagation, 55 and facilitate their dissipation. The complexity of the internal wave lifecycle leading to turbulent 56 mixing has inspired many avenues of inquiry. 57

Early work focused on understanding the local physics of internal waves [16, 17, 18, 19], and 58 hypothesized that the mixing caused by these waves has global implications [20]. More recent 59 efforts to study internal wave-driven mixing have advanced our understanding of the local physics, 60 and linked internal wave processes inducing mixing that are disparate in space and time to a 61 holistic view of the entire ocean system. Recent reviews have focused specific threads of areas of 62 rapid development, including parameterization of internal wave-driven mixing in climate models 63 [21], and reported on the current understanding of internal waves near the inertial frequency [22]. 64 This review will adopt a wider perspective by targeting internal wave physical processes and 65 how they contribute to setting the complex spatio-temporal structure of mixing in the ocean. After 66 describing the physics of mixing due to breaking internal waves, the review will examine internal 67 wave energy pathways, categorized according to the waves' energy source. Subsequently, the review 68 will outline implications of internal wave-driven mixing for global ocean circulation and climate, 69 emphasizing knowledge frontiers. 70

4. Physics of Mixing from Internal Waves

Internal waves are ubiquitous in the stratified ocean interior. Flow along the uneven seafloor, 72 perturbations at the base of the mixed layer, or fluctuating ocean currents can all generate internal 73 waves (Figure 1). The signature of the generation mechanism is imprinted on the internal waves' 74 spatial and temporal characteristics, leading to internal waves that have horizontal scales of order 75 0.1-100 kilometers and vertical scales that range from meters to scales comparable to the ocean 76 depth. The structure and behaviour of internal waves is often modeled using orthogonal modes 77 [G] [23]. Waves with vertical scales comparable to the ocean depth have small mode numbers 78 and are called 'low-mode internal waves', whereas waves with smaller vertical scales have large 79 mode numbers and are called 'high-mode internal waves' [23]. The high-mode internal waves can 80 often occur in packets with vertical extents of hundreds of meters. The horizontal group velocity 81 (that is, the velocity of energy propagation) is inversely proportional to mode number, such that 82 low-mode wave energy travels faster than high-mode energy. The frequencies of internal waves are 83 roughly bounded on the high end by the buoyancy frequency [G](N) and on the low side by the 84 local Coriolis frequency [G] (that is, the inertial frequency, f). A single generation event generally 85 produces a spectrum of waves with a range of spatial scales and frequencies. 86

Once the internal waves are generated, they propagate throughout the ocean, interacting with 87 other waves, currents and topography in ways that lead to a transfer of energy across scales and 88 a loss of coherence of the initial waves. Far from boundaries, wave-wave interactions are a major 89 process that can transfer energy to smaller scales [24, 25, 26]. Wave-wave interactions involve a 90 resonance or near-resonance between three or more internal waves, causing an exchange of energy 91 between waves of different wavelengths and frequencies that can shift energy to waves on smaller 92 spatiotemporal scales. A particularly efficient class of wave-wave interactions occurs when one or 93 more of the high-mode internal waves have near-zero group velocity, allowing sustained growth due 94

to energy transfer with a low-mode wave of approximately double their frequency, through a process 95 known as parametric subharmonic instability [27, 28, 29]. Additionally, as internal waves propagate 96 through variable background velocity and stratification, their length scales and group velocity may 97 change. For example, substantial variability in the background field can induce a rapid decrease 98 in the vertical scale of the wave, referred to as a critical layer [30, 31, 32]. Close to the seafloor, 99 the dominant dynamics change, and the scattering of internal waves off rough topographic features 100 or continental slopes is the most important class of processes that can turn larger-scale waves into 101 smaller-scale ones. 102

Ultimately, internal waves cascade to small enough scales to trigger a mixture of shear and 103 convective instabilities, turbulently dissipating wave energy through the internal wave equivalent 104 of breaking [33]. For example, shear instabilities can extract kinetic energy from an internal wave, 105 inducing turbulence (for example, Figure 2a-b). Alternatively, an internal wave can also generate 106 turbulence through convective instability that occurs when denser water at the wave crest moves 107 over lighter water [34], producing turbulence by extracting potential energy from the wave (for 108 example, Figure 2c-d). The turbulence generated by internal waves in the open ocean is typically 109 patchy and intermittent, exhibiting spatial scales of order 0.1-100 m and time scales of minutes to 110 hours [35, 36]. Where and when an internal wave dissipates energy depends strongly on the mode 111 number of the wave, since the mode sets the vertical scale, group velocity, and susceptibility to 112 wave-wave interactions [37, 38]. 113

Breaking internal waves create turbulent kinetic energy, which is then either lost to viscous dissipation (at a rate ϵ) [G] or to work against the ocean's density gradients (expressed as a buoyancy flux, J_b). The two are related by the flux coefficient $\Gamma = J_b/\epsilon$ [39, 40]. The buoyancy flux can be expressed as a down-gradient mixing of density at a rate given by a diapychal diffusivity [G] K, so 118 that $J_b = KN^2$, or

119 (1)
$$K = \frac{\Gamma \epsilon}{N^2}$$

120 K is the variable ultimately needed to model vertical mixing of oceanic tracers. Realistic repre-121 sentation of internal wave-driven mixing thus requires knowledge of the turbulent kinetic energy 122 dissipation rate ϵ and of the flux coefficient Γ [39]. In open-ocean internal wave environments, 123 the flux coefficient is often close to 0.2; however a number of studies do indicate that Γ can vary 124 throughout the ocean [40].

There are two primary observational approaches to estimate the intensity of turbulence associated 125 with internal waves: direct and indirect methods. Spectra of oceanic shear on centimeter scales 126 measured with microstructure probes can be compared directly to theoretical turbulence spectra 127 and used to calculate ϵ [41, 42]. Indirect methods use finescale measurements (on 1-10 m scales) that 128 are analogously compared to internal wave spectra via the adoption of more assumptions, in order to 129 provide the turbulent kinetic energy dissipation rate expected from an observed internal wave field 130 [43, 44, 45, 46]. Finescale measurements generally agree with microstructure measurements within 131 a factor of 2-3 [45, 47, 48] in the open-ocean thermocline when they are compared on equivalent 132 time and length scales, which is considered a strong agreement, since dissipation rates vary over 133 many orders of magnitude. 134

Next, we move from describing studies that target the physics of internal wave generation, propagation and breaking, to adopting a global perspective of the distribution and implications of internal wave-driven mixing.

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5. Global Internal Wave Energy Budget

Knowledge of the global budget, including the pathways to and from the reservoir of internal
wave energy, is key to fully characterize the impact of internal wave-driven mixing on global-scale

ocean dynamics. The estimated energy budget of the open-ocean internal wave field is shown in 141 Figure 3. Energy from three major sources contributes to internal waves: tides, surface winds 142 associated with synoptic and mesoscale atmospheric disturbances, and geostrophic currents. Tidal 143 flow moving water over uneven seafloor topography adds about 1 TW of power to the internal 144 wave field. A resonant response in the surface mixed layer to time-varying wind stress provides an 145 estimated 0.3-1.4 TW of power, part of which fuels the internal wave field. Geostrophic currents 146 flowing over small-scale topographic features, or losing balance, transfer energy to internal waves 147 at estimated global rates of 0.15-0.75 TW and 0.1-0.36 TW, respectively. 148

Once internal waves are generated, they enter the global reservoir of internal wave energy (Fig-149 ure 3). This reservoir has a remarkably consistent distribution of wavenumbers and frequencies. 150 presumably due to the prevalence of wave-wave interactions in distributing energy across length 151 and time scales [49], which is modeled by the empirically derived Garrett-Munk spectrum [50, 51]. 152 Observations reveal a more complex internal wave spectrum with considerable spatio-temporal vari-153 ability [52, 53], including peaks at the tidal and inertial frequencies that are respectively attributed 154 to generation by tides and time-variable winds, in addition to pronounced deviations near topogra-155 phy [54] and in shallow water [55, 56]. However, a complete understanding of what sets the energy 156 level and shape of the internal wave spectrum, in particular the 'continuum' of the spectrum where 157 there are no peaks, is still an area of active research. 158

Globally, the energy in the internal wave field is either lost through turbulent dissipation or transferred to the background ocean currents. Dissipation can occur close to the waves' generation sites, or up to thousands of kilometers away, making tracking energy through the system extremely challenging. Along the way, the internal waves are thought to exchange energy with the background current field, adding to the difficulty of closing the global internal wave energy budget and comprehensively mapping internal wave-driven mixing.

6. Tides

Energy from the tides is a major contributor to the internal wave field energy budget [57], globally converting about 1 TW of energy to open-ocean internal tides [58, 59]. Once internal waves at the tidal frequencies and their harmonics are generated, they travel through the ocean differently depending on their spatial scale; generally the high-mode waves dissipate in the near field (close to the generation site) and low-mode waves dissipate in the far field. The many pathways of internal tides from generation to dissipation yield a complex global geography of internal tide dissipation [60, 61, 62, 63], shown in Figure 4a.

6.1. Generation. Gravitational attraction of the moon and sun generates the ocean's batrotropic tides [G] [57], which uniformly span the full water column. Barotropic tidal currents dissipate about two thirds of their energy through friction and shear-driven mixing in shelf seas [64] and breaking coastal lee waves [65, 66]. The remainder of barotropic tidal energy is dissipated through the generation of internal (baroclinic) tides [G], resulting from the periodic displacement of density surfaces by barotropic tidal currents pushing stratified fluid along a sloping seafloor [19, 57].

The character of the topography plays a primary role in setting the dominant modes of the 179 internal tide: a tall and steep slope (e.g., a continental slope) tends to generate low-mode internal 180 tides, whereas a flatter but corrugated bottom (e.g., an abyssal ridge flank) favours high modes 181 [67, 68] (Figure 4b). A small number of sharp and steep topographic features contribute the 182 majority of the power going into the first few modes [69, 70]. Internal tides with the smallest 183 scales, corresponding to modes \gtrsim 50, are mostly generated by "abyssal hills" [71, 72] that have 184 typical widths of several kilometres and heights of a few hundred meters [73]. Generation by abyssal 185 hills has been estimated to amount to about 0.1 TW globally [72, 74], roughly 10% of the total 186 conversion rate from barotropic to baroclinic tides. 187

6.2. Near-field mixing. After internal tides are generated, a portion of the energy is dissipated in 188 the near-field, close to the rough topographic features of origin [75, 76, 71]. In particular, direct non-189 linear breaking and wave-wave interactions may both be responsible for the rapid energy transfer 190 from high-mode internal tides to turbulence in close proximity to topography [77, 78, 79] and in 191 the upper water column [60, 78, 74]. Evidence for this near-field mixing due to internal waves 192 include microstructure observations accumulated over the last 25 years showing that the turbulent 193 dissipation rate is elevated multiple kilometers above or away from irregular topography, and that 194 it often increases with greater proximity to that topography [75, 62]. Additionally, observations 195 and model studies suggest that abyssal hill roughness underpins the bulk of the bottom-enhanced 196 turbulence occurring over ridge flanks of the Pacific, Atlantic and Indian basins [78, 80, 74]. 197 The geography of near-field mixing is challenging to model because the fraction of energy dissi-198 pated in the near field, and its vertical distribution, are a function of numerous factors including the 199 local environment and the modal content of the internal tide. As a consequence of this complexity, 200 in situ observations and theory indicate that the fraction of energy dissipated in the near field may 201 range between 0.1 and 1 [81, 82, 78, 62, 74, 68]. The power input to modes ≥ 4 compares well with 202 depth-integrated dissipation rates measured with microstructure probes, suggesting that modes ≥ 4 203 dissipate mostly near their generation site [68]. These high modes represent an estimated 606 GW, 204 or 49% of the total generation at seafloor depths exceeding 500 m [68]. Parameterizations of the full 205 water column vertical distribution of near-field dissipation [78, 74] are often based on observations 206 from the eastern Brazil Basin. Since the accuracy of these parameterizations on a global scale is 207 largely unknown, observations across different regimes of high-mode internal tide generation [80, 83] 208 will help to develop and improve confidence in parameterizations. 209

6.3. Propagation and far-field mixing. The distance that low-mode internal tides travel before
dissipating their energy – often in the far field – depends on the mode number of the wave and the

oceanic environment along the wave's path. First-mode internal tides propagating up to several thousands of kilometres can be detected using acoustic tomography and satellite altimetry [84, 85] and are dominated by distinct beams 100-300 km wide [70, 86] (Figure 4c). By contrast, identified mode-2 beams are more numerous but weaker, narrower and an order of magnitude shorter [87]. Mode 1 accounts for the bulk of internal tide horizontal energy transport [88], though modes 2-5 also contribute substantially [89, 90]; however, the exact fraction of energy transport in each mode depends on a number of environmental factors described below.

First, as internal waves propagate, variable bathymetry plays an important role in the transfer 219 of low-mode energy to smaller scales, channeling the energy closer to the scale at which dissipation 220 occurs [91, 92, 63]. When a large-scale wave bounces off short-scale seafloor irregularities, part 221 of its energy is scattered into higher modes [93, 94], leading to bottom-intensified turbulence and 222 dissipation. Larger-scale seamounts or ridges can also cause scattering to higher modes, as well 223 as refraction of incident beams [52, 95, 96]. Beams that ultimately reach continental margins can 224 reflect backward, dissipate or shoal, depending in part on the local topographic slope. Backward 225 reflection dominates if the continental slope is significantly steeper than the wave [97, 98]. If the 226 topographic slope is approximately equal to the wave slope, energy is transferred to very high 227 modes that break into small-scale turbulence along the slope [99, 100, 101]. Gentler continental 228 slopes allow the internal tide to progress into shallow waters; however, as energy concentrates in 229 the vertical, shear increases and direct breaking of the wave is frequent, particularly at the shelf 230 break [102]. 231

In addition to interactions with bathymetry, wave-wave interactions may also be significant in attenuating the mode-1 internal tides, and are likely dominant in draining energy from modes \geq 234 2 [28, 103, 38, 63]. The energy transfer is most efficient equatorward of the latitude at which the tidal frequency is twice the inertial frequency—that is, equatorward of 29° for the dominant semidiurnal tidal constituent [29]. Resonant triads transfer energy to smaller vertical wavelengths,
and ultimately to dissipation focused in the stratified upper ocean [104, 105, 106].

Finally, the propagation and modal content of internal tides can additionally be altered by interactions with the shear, strain and varying stratification present in mesoscale eddies, equatorial jets and other background ocean currents [107, 108, 109, 110, 111, 112]. The interactions can potentially transfer energy to higher modes, leading to dissipation, or transfer energy between low-mode internal tides and the background ocean currents. Additional observational studies of low-mode internal tide energy loss via interactions with background currents are needed, since the significance of such interactions for internal tide-driven mixing is not yet well known.

Global estimates of the distribution of mode-1 internal tide energy dissipation suggest that large-245 scale topographic obstacles cause the bulk of that dissipation [91, 63]. Using Lagrangian tracking of 246 energy beams and parameterized energy sinks, it has been estimated that wave-wave interactions 247 explain about 25% of mode-1 dissipation, but 65-80% of the overall modes 1-5 dissipation [63]. 248 Hence, despite major topographic features hosting the bulk of mode-1 dissipation, much of the 249 observed open-ocean internal tide dissipation may originate from the far-field dissipation of modes 250 2-5. Scattering by abyssal hills could be responsible for about 10% of the dissipation of the first 251 five modes [63]. However, additional constraints on attenuation rates of low-mode internal tides by 252 wave-wave interactions, and improved understanding of interactions with rough topography and 253 background currents, are called for to narrow down uncertainties in these exploratory estimates. 254

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7. Wind

Time-variable winds, often associated with passing storms, can provide power for near-inertial waves [G] (internal waves near the inertial frequency) to grow [113]. As storm activity increases in the winter, so does the energy in the near-inertial wave field and associated mixing rates, suggesting that winds are a key driver of the seasonal variability of internal wave-driven mixing in the ocean [114, 115]. However, the main mechanisms leading near-inertial waves to dissipate their energy are
not yet well constrained, leaving ample opportunity for future work.

The following divides the lifecycle of near-inertial waves into a generation phase, namely how near-inertial energy injected into the mixed layer by the wind is transferred to the ocean interior, followed by an internal wave propagation and mixing phase. Note that this division is distinct from conceptually partitioning the wave's lifecyle into an active wind-forcing phase, followed by the ocean's response after the forcing ends—a framework employed by some studies of isolated events [116].

7.1. Generation. Time-varying wind stress on the ocean surface due to synoptic events, such as a 268 passing mid-latitude storm [116] or cyclone [117, 118, 119], can generate a resonant response in the 269 mixed layer of water oscillating horizontally at a frequency close to inertial. The signature of near-270 inertial oscillations can be observed in the circles traced by surface drifters distributed beneath a 271 storm [116]. One way that inertial oscillations decay is through energy dissipation by shear-driven 272 turbulence close to the mixed layer base [120, 121]; however, the importance of this mechanism is 273 poorly known. The second, potentially more important, mechanism is downward energy radiation 274 into the stratified interior ocean. Specifically, internal waves are radiated downward when horizontal 275 variability in the magnitude of near-inertial velocities creates divergences and convergences within 276 the mixed layer, generating pressure gradients that allow water to locally rise and fall at the inertial 277 frequency, thereby radiating energy [122] (Figure 5). 278

The portion of near-inertial energy escaping the mixed layer as internal waves is not well constrained. Combining two lower-bound observational estimates of the fraction of energy propagating away as low-mode [123] and high-mode [124] waves suggests that a minimum of 27-53% of the energy input into near-inertial oscillations radiates away as internal waves. Roughly consistent with this observation, seasonal cycles in the mixed-layer and deep-ocean near-inertial kinetic energy are all similar in magnitude [114, 125]. However, global modeling studies find that a smaller fraction of the wind work on near-inertial motions radiates downward, with estimates of 11-30% leaving the vicinity of the mixed layer [126, 127, 128]. Modeling studies with high spatio-temporal resolution suggest that resolving the interactions between the mesoscale eddy field and inertial oscillations may be important [129]; however, more work is needed to improve and reconcile observational and model-based estimates of downward near-inertial energy propagation.

Advancing our understanding of how the growth and decay of near-inertial oscillations can be 290 modified by the background oceanic environment may help constrain the magnitude of energy 291 leaving the mixed layer. For example, spatial variations in the Coriolis frequency may reduce the 292 internal wave length scales [116], increasing the rate at which near-inertial energy drains from the 293 mixed layer. Additionally, as near-inertial oscillations grow, energy transfer can occur with the 294 background flow due to strong horizontal convergence [130], and horizontal strain [131] at a rate 295 modulated by anticyclonic rotation [132, 131]. During the decay of near-inertial oscillations, strong 296 gradients in vorticity can increase the radiation of near-inertial energy from the mixed layer [133], 297 especially at sharp gradients in the background currents [134, 133, 135]. 298

Global studies commonly target a specific phase of the near-inertial wave generation process: 299 the energy flux from winds to near-inertial oscillations. Estimates of the power available for near-300 inertial wave generation are often made using atmospheric reanalysis-derived winds to force general 301 circulation models [136, 137], and 1-d slab models where the mixed layer is set to a fixed depth and 302 energy radiates away at an assigned timescale [113, 116, 138, 139, 140]. The slab model produces 303 estimates that agree well with observations, with caveats [140, 141]. Products with relatively high 304 temporal and spatial resolutions (reanalysis winds available at least every 4 hours, and satellite 305 altimetric data sets with 1 degree horizontal resolution or finer) yield 0.9-1.4 TW of global power 306 input from the winds [142, 137], while estimates from coarser temporal and/or spatial resolution 307 winds suggest 0.3-1 TW [143, 142, 139, 136, 137]. Both of these estimates are consistent with the 308

first drifter-based estimate that finds a lower bound of 0.3 TW [144]; however, more observational work is needed to reduce the large uncertainties in all estimates.

7.2. Local and Far field Mixing. Distinct high-mode near-inertial waves can be observed as 311 bands of alternating shear at vertical scales of metres to hundreds of metres. In the North Pacific, 312 observations reveal that high-mode near-inertial waves can attain vertical group velocities of 7-313 23 m/day [124] and horizontal scales of 10s to 100s of kilometers [145]. Observational estimates 314 indicate that the fraction of wind work on mixed layer oscillations that propagates away as high-315 mode near-inertial waves may range between 12-33% (reaching 800 m)[124], or 2-33% (reaching 100 316 m)[146]. Modelling studies provide the slightly smaller estimate that 10% [127] of the wind work 317 on the mixed layer reaches 230 m as high-mode internal waves. 318

In addition to high-mode internal waves, a large fraction of near-inertial energy is thought to 319 radiate away as low modes, with estimates ranging from 15-20% of the energy input into mixed 320 layer oscillations [123], to 33-45% of the near-inertial wave energy in the thermocline (modes 1-2) 321 [116]. Since the Coriolis frequency decreases towards the equator and sets the internal wave low-322 frequency limit, near-inertial waves are typically constrained to propagate equatorward [147, 123] 323 except in strongly sheared background flows [148]. As the low modes propagate, they are subject 324 to wave-wave interactions, including parametric subharmonic instability [149, 150], that can reduce 325 their length scales and lead to turbulent mixing. 326

Near-inertial wave activity is elevated beneath mid-latitude storm tracks, with a seasonal cycle that peaks in the winter months from the surface to the seafloor [114, 151] (Figure 5 a-b); however, the mechanisms underpinning such a deep seasonal cycle are not well understood. The stronger near-inertial wave activity during the winter months is correlated with an enhancement of inferred diapycnal mixing [48, 152, 115] to at least a depth of 2 km (Figure 5 c-d). Future work linking direct observations of mixing using microstructure methods to the seasonal cycle in near-inertial kinetic energy would be valuable to corroborate the implication of near-inertial waves in drivingseasonality in mixing.

The mesoscale flow field likely shapes the rate of near-inertial propagation and spatial distri-335 bution of the energy dissipation, in addition to influencing the generation processes described in 336 the previous subsection. Modelling and theory suggest that the mesoscale vorticity can reduce 337 the horizontal scales of the waves and funnel near-inertial energy into regions of anticyclonic vor-338 ticity [153, 154, 155, 156, 129]. Additionally, a positive strain rate in the mesoscale current field 339 can substantially alter the length scales and propagation velocities of internal waves [32, 109, 53]. 340 Finally, internal waves can encounter critical layers along steeply sloping isopycnals, triggering 341 energy dissipation [157, 153, 158, 159]. Observations support these general ideas, finding altered 342 internal waves and elevated dissipation rates at the boundaries of individual mesoscale eddies 343 [160, 161, 162, 163, 164], and relatively large inferred mixing in response to increased wind activity 344 345 in the presence of an energetic mesoscale eddy field [115].

346

8. Geostrophic Currents

Winds provide about 1 TW of power to the geostrophic current field in the ocean [165, 166]. A portion of the energy in ocean currents is then transferred to the internal wave field through interactions with topographic features, or by direct generation of internal waves. However, it has been suggested that the bulk of the energy in the geostrophic current field is not dissipated through internal wave processes, but by a combination of bottom friction [167, 168], hydraulic effects downstream of topography [169], and suppression by wind work [8, 170].

8.1. Quasi-steady lee wave generation at topographic features. When steady or eddying abyssal flows impinge on small-scale topographic features, they can generate internal waves, often called lee waves [G] [19]. Internal lee waves have frequencies and length scales set by the velocity of the currents and length scales of the bathymetry. Estimates made using linear wave theory [19] of the total global energy transfer rate from geostrophic currents into internal lee waves range from
0.15 to 0.75 TW [171, 172, 173, 174, 175], with a major contribution from the Antarctic Circumpolar
Current (ACC) region. These estimates' large range arises from uncertainties in ocean stratification,
bathymetric products and, principally, the representation of near-bottom current speeds in global
circulation models [173, 176].

Once generated, lee waves can travel upwards if the frequency in the wave's reference frame is 362 between f and N. In a steady current, propagating lee waves appear stationary in the ground 363 reference frame, but can shift upstream or downstream if the current varies in time or nonlinear 364 interactions are present [19, 177]. Most of the evidence for lee wave activity in the ACC has been 365 provided by indirect measurements of elevated upward-propagating internal wave energy in the 366 deepest 1-2 km of the water column [178, 179, 180]; however, an unambiguous observation was 367 made of the waves themselves [181] (Figure 6a). Observations in the western boundaries of mid-368 latitude ocean basins also show evidence for the generation and propagation of internal lee waves 369 there [182]. Lee wave radiation is highly intermittent due to changes in the intensity and position 370 of the background flow, resulting in temporal variability of the lee wave field on time scales up to 371 decadal [183, 184, 185]. 372

Lee waves' energy is dissipated as the waves encounter critical layers, or as the energy is trans-373 ferred to other waves via wave-wave interactions or reabsorbed into the background current field 374 [186]. Observations of elevated turbulence attributed to lee waves include studies in the ACC 375 [187, 188, 178, 179, 180], abyssal passages [189], and canyons [190]. Estimates of the amount of 376 radiated lee wave energy that is dissipated within 1 km of the bottom range from up to 50% using 377 2-d models [191] to 2-30% using observations [178, 179]. The discrepancy between these estimates 378 highlights that lee waves do not play as important a role in the internal wave global energy bud-379 get as early modeling studies suggested. Additional complexity, such as including 3-d flow effects, 380

is necessary to model lee wave generation, propagation, and dissipation more accurately than in current modelling efforts [47, 174, 179, 192, 169, 177, 186].

8.2. Internal wave generation from geostrophic currents. The generation of internal waves 383 directly from the geostrophic current field may contribute to sustaining turbulent dissipation and 384 mixing, although the contribution may be relatively small. Modelling results demonstrate that 385 internal waves near the inertial frequency can be generated through resonance with the rapidly 386 varying components of background currents [193, 194, 195, 196] and, more specifically, during 387 intense straining of small-scale fronts by the larger-scale currents [197, 198, 199]. Additionally, an 388 actively unstable front might radiate internal waves with a larger range of frequencies [200, 201]. 389 Finally, geostrophic currents can also transfer energy to existing near-inertial waves, providing an 390 additional energy pathway [202, 203]. Estimates of the global energy flux from geostrophic currents 391 to internal waves range between 0.1 and 0.36 TW [8, 204, 198]. However, only limited observations 392 of this internal wave generation pathway exist [205, 198], so the prevalence of these processes is 393 still unclear. 394

The eventual fate of the internal waves drawing energy from geostrophic flows is either turbulent 395 dissipation (Figure 6b) or re-absorption into the background current field. If a substantial portion 396 of the energy from these internal waves dissipates via wave breaking, then the waves may be 397 a significant energy sink for the mesoscale eddy field [206]. However, modelling results suggest 398 that only around 15% [198] or 30% [207] of the energy is dissipated through turbulence, with 399 the remainder returning to the background current field. The low fraction of dissipated energy 400 indicates that the internal waves generated from ocean currents may be an important mechanism 401 for redistributing energy, but contribute only modestly to the global internal wave and mesoscale 402 eddy kinetic energy budgets. 403

9. GLOBAL MIXING AND IMPLICATIONS

All the processes governing the generation, propagation, and dissipation of internal waves deriv-405 ing their energy from tides, winds and geostrophic currents conspire to shape the global distribution 406 of the turbulent dissipation rate and diapycnal diffusivity as observed using microstructure [62] and 407 finestructure [60, 61, 9, 115] measurements (Figure 7a). The intensity of the dissipation rate and 408 diffusivity both range over three orders of magnitude across the globe, so that the bulk of the 409 values span 10^{-11} - 10^{-8} [W/kg] and 10^{-6} - 10^{-3} [m²/s], respectively [60, 61, 62]. When the bottom 410 topography is rough, the dissipation rate is often elevated by an order of magnitude or more from 411 the seafloor to near the surface, due to near-field dissipation of internal tides or lee waves as well 412 as mixing from topographic scattering of remotely generated internal waves [60, 61, 106]. Regions 413 with strong sources of tidal and wind energy are also associated with elevated dissipation rates, 414 indicating that near-field dissipation plays an important role in shaping the global geography of 415 mixing [115, 68]. For example, mixing is elevated above the Hawaiian Ridge, Southwest Indian 416 Ridge and Mid-Atlantic Ridge due to tidal generation and scattering [82, 75, 63]. In the South-417 ern Ocean around the Kerguelen Plateau and Macquarie Ridge, lee waves and tides may both 418 contribute [178, 174, 92]. 419

As explained in the following, mixing from internal waves contributes to sustaining the deep ocean's meridional overturning circulation, and importantly influences the broader global climate system, in addition to impacting the oxygen distribution [12], the delivery of nutrients to the ocean's surface layers [14], and primary production [12].

9.1. Global Overturning Circulation. The cold, dense water that sinks to the ocean abyss
at high latitudes must eventually rise, returning to the ocean surface and thereby closing the
Meridional Overturning Circulation (MOC). The simplified model of the MOC has two major

branches. One of the branches transports deep water southward, and is primarily driven by windinduced upwelling in the Southern Ocean [208], although in models its strength is sensitive to changes in mixing [209, 210, 211, 129]. The second branch, in turn, transports abyssal water northward and upward [4], and is thought to be largely driven by internal wave mixing [3, 62, 5, 6], with additional contributions from geothermal heating along the seafloor [212, 213] and mixing along the deep western boundaries [214] and within constrictive passages [215].

In the northward branch of the abyssal MOC, turbulence from breaking internal waves transfers 433 buoyancy downward, progressively transforming the dense bottom water into lighter water. This 434 lightening enables new inflowing water to intrude below, such that the transformed water rises 435 above the new water, creating the upward branch of the abyssal MOC. The strength of this branch 436 has been estimated to be 20-30 Sverdrups (Sv; 1 Sv $\equiv 10^6 \text{ m}^3 \text{s}^{-1}$) [216, 217, 4]. Internal tides 437 are thought to drive a substantial portion of the abyssal upwelling, with estimates including both 438 near-field and far-field mixing that range between the entirety of the abyssal MOC transport to 7 439 Sv [218, 5], or 5 Sv with a spatially variable mixing efficiency [219]. Lee waves contribute a smaller 440 portion of the abyssal upwelling, with estimates ranging between 2-3 Sy [220, 5]. It is not known 441 if near-inertial waves play a significant role in driving the abyssal MOC. Both the horizontal and 442 vertical distributions of mixing alter the magnitude and vertical structure of the MOC in models 443 [221, 222, 218, 209, 223, 220, 210], an example of which is shown in Figure 7b, indicating that the 444 global spatial variability (Figure 7 a) is important for setting the observed properties of the MOC. 445

9.2. Climate. The broader climate system is sensitive to the distribution and magnitude of internal wave-driven mixing in the ocean, beyond the role of mixing in driving the MOC as discussed in the previous subsection. Since diffusivity from internal waves cannot be explicitly captured by global models, parameterizations are currently being developed to include the effects of the spatiotemporally varying diffusivity [21]. To explore how sensitive the ocean and atmosphere are to

mixing from breaking internal waves, climate models are run with a range of parameterizations 451 designed to represent mixing from the tides [106, 210, 224, 225], winds [106, 226, 225] and lee waves 452 [220, 227], in addition to changing the magnitude of the model-prescribed background diffusivity 453 [211]. These studies report that even small perturbations in the magnitude or distribution of the 454 diffusivity in global models can lead to substantial changes in the temperature, circulation, and 455 fluxes in the atmosphere and ocean. However, both the magnitude and the sign of these changes 456 vary between studies due to the range of mixing parameterizations and the details of each model, 457 thus the following focuses on the broad trends across all studies. 458

Altering the diffusivity changes the vertical profiles and horizontal distribution of temperature 459 and salinity throughout the ocean, and therefore the density and stratification [226, 220, 227, 210, 460 224, 211, 225]. The ocean's meridional heat transport is also sensitive to changing background 461 diffusivity and to the spatial distribution of mixing from internal tides [210, 211], but not to pa-462 rameterized mixing induced by near-inertial waves in one study that underestimates the magnitude 463 of mixing from the wind [226]. Changes in the properties and circulation of the ocean interior 464 lead to variations in the sea surface temperature [226, 210, 211, 225], mixed layer depth [226, 224]. 465 and air-sea fluxes [129, 211]. Perturbing interior diffusivity also has repercussions above the sea 466 surface, including sea ice extent and concentration [226, 224, 211], air temperature, atmospheric 467 circulation, and precipitation [226, 224, 211, 225]. For example, one study added diffusivity from 468 near-inertial internal waves and found notable changes in the sea ice extent and surface heat flux 469 (Figure 7c)[226]. The substantial sensitivity of both the ocean and the atmosphere to internal 470 wave mixing indicates that including its effects in climate-scale models is important for a realistic 471 representation of the climate system. 472

Beyond these widespread climatic impacts, internal wave mixing has been shown to exert a profound influence on regional and global climate via its localised effects on several important elements of the global ocean circulation. For example, the vertical density structure in the Indonesian Seas

is sensitive to the representation of tidal mixing in models—with implications for a range of aspects 476 of (sub-)tropical Indo-Pacific climate including volume transport of the Indonesian Throughflow, 477 ocean heat uptake, and rainfall [228, 229, 230]. In the equatorial Pacific, parameterizing internal 478 wave mixing in the thermocline yields changes in the equatorial upwelling, sea surface tempera-470 ture, and wind patterns [226, 225]. However, only representing mixing from tides or lee waves has a 480 negligible effect [220, 210], suggesting that including more processes than current tide and lee wave 481 parameterizations represent may be necessary to accurately model the equatorial Pacific. Finally, 482 the latitudinal distribution of deep mixing from lee waves and tides has been argued to alter the 483 ACC transport, the depth of the ocean thermocline and, by extension, many important features of 484 global climate [231, 232, 220]. As the operation of internal wave mixing in other pivotal elements of 485 the global ocean circulation is further unravelled, it is likely that more climatic impacts of localised 486 mixing will emerge. 487

488

10. Summary and Future Directions

Global and regional patterns of internal wave-driven turbulent mixing are controlled by the com-489 plex and convoluted processes of internal wave generation, propagation, interaction and dissipation. 490 Internal waves act as a conduit, eventually funneling energy from tides, winds, and currents into 491 turbulence, leading to both energy dissipation and mixing. In turn, the mixing plays a role in 492 driving the meridional overturning circulation and aids in setting many characteristics of the global 493 climate. While much progress has been made recently in understanding significant elements of 494 all stages of the internal wave lifecycle, several fundamental knowledge gaps remain. Here, we 495 synthesize these gaps into three broad priority challenges, which we encourage the oceanographic 496 community to address in coming years. 497

The first challenge entails advancing our understanding of the processes that transfer energy within the internal wave field, and which ultimately lead to dissipation and mixing. As discussed

here, investigations have improved constraints on the wave field's energy sources, and the magnitude 500 and placement of wave energy dissipation. However, the physics of how the energy is transferred 501 across length scales and frequencies along the pathway to dissipation is poorly understood. In 502 particular, we do not know why the observed internal wave spectrum varies only modestly in shape 503 across the global ocean [53]. Important likely candidates include wave-wave interactions [29, 26], 504 topographic scattering and reflection [93], and interactions with the background current field [233]. 505 Studies focused on these individual energy transfer processes, and on how they combine to form the 506 observed internal wave spectrum, would be valuable. For example, recent investigations suggest 507 that parametric subharmonic instability, the very efficient type of wave-wave interaction, is not 508 sufficient to explain the majority of the down-scale internal wave energy transfer [29], indicating 500 that other wave-wave interactions [26] or wave-wave interactions in the context of geostrophic 510 currents [83] may be important in shaping the spectrum. Additional theoretical and numerical 511 work constraining attenuation due to wave-wave interactions using an internal wave spectrum close 512 to that observed in the ocean is especially needed [38, 29]. 513

The second challenge concerns unravelling how internal waves interact with other types of ocean 514 currents, and how these interactions shape the distribution of mixing in the ocean. Interactions 515 between internal waves and currents deserve special consideration, since among the energy exchange 516 processes depicted schematically in Figure 3 and discussed in challenge one, they have the largest 517 uncertainties. The mildest form of this interaction is a gradual shift in the wave phase as waves 518 travel through a current field; for example, this de-phasing may occur as low-mode internal tides 519 propagate through a variable mesoscale flow. De-phasing of low modes renders them invisible to 520 detection by satellite altimetry, increasing the uncertainty in estimates of low-mode attenuation and 521 subsequent energy dissipation [111, 234, 235]. An improved understanding of the weak modulation 522 of internal waves by background currents is needed, especially with a view to constraining low-mode 523 internal tide attenuation and dissipation in global models [210, 63]. 524

Moderate interactions involve the impact of spatio-temporal variability of background currents. 525 which present a variable medium for internal waves to exist in and propagate through. Background 526 current flow and vorticity affect internal wave generation by, for example, altering the rate of energy 527 transfer to both internal lee waves and wind-driven near-inertial internal waves. Then, as waves 528 propagate, structure in the background current shear, strain or stratification can lead to significant 529 wave refraction, reflection or, in extreme cases, wave breaking as propagation slows down to a 530 halt in critical layers or sharp fronts. Theoretical, modelling and observational studies are needed 531 to understand the influence of these moderate interactions on the generation, propagation, and 532 dissipation of internal waves, in addition to their prevalence in the ocean and cumulative impact 533 on energy pathways. 534

The strongest form of interaction involves substantial two-way energy exchanges between inter-535 nal waves and geostrophic flows. For example, for internal lee waves, accurate understanding of 536 refraction in sheared background flows like the ACC is key to predict where and how the waves will 537 deposit their momentum to accelerate or decelerate the background flow [236]. Two-way energy 538 exchanges between internal waves and background flows are also likely to be important where the 530 spatio-temporal scales of both classes of flows overlap, for example in submesoscale (0.1-10 km 540 scales) flows on the edges of mesoscale eddies, or near-inertial waves with slow group velocities 541 and large horizontal wavelengths. The small-scale and quickly varying energy exchanges in these 542 settings are extremely difficult to observe, calling for the development of new, multi-platform mea-543 surement approaches and numerical simulations of increased complexity. We anticipate that a step 544 change in understanding of how the ocean's mesoscale eddy field loses its energy to internal waves 545 and turbulence will result in major improvements in the realism of climate-scale ocean models. 546 some of whose key features (for example, deep-ocean MOC, ACC transport, stratification) are now 547 understood to depend on the eddy-internal wave energy transfer [206]. 548

Building on these challenges, the overarching (and arguably most daunting) task is to reformulate 549 internal wave-driven mixing as a fully interactive component of ocean circulation and the climate 550 system [106], rather than the essentially passive and unchanging diffusivity field as which wave 551 mixing has been traditionally viewed. More work is needed to further develop parameterizations 552 of mixing and quantify their effects on global ocean circulation and climate. For example, more 553 studies are needed that include parameterized mixing from near-inertial waves and explore the 554 impact of time-varying mixing so that feedbacks on the climate system are represented. To drive 555 this transformation, we require new ways to measure internal wave mixing over the annual or longer 556 time scales that are most climatically relevant. In addition, the next generation of physically robust 557 representations of the key wave mixing processes will need to be incorporated into climate-scale 558 ocean models. The spark for this shift in view has been lit by a number of recent studies mentioned 559 in this review, but much work remains to be done for the shift to be realized. 560

561 11. GLOSSARY OF KEY TERMS

Internal wave orthogonal modes: Theoretical framework used to describe the vertical structure of internal waves, where low-mode internal waves have larger vertical scales and high-mode internal waves have smaller vertical scales.

565 Buoyancy frequency (N): The oscillation frequency of a vertically displaced water parcel, 566 which scales with the local vertical stratification gradient.

Coriolis/inertial frequency (f): The oscillation frequency of a horizontally displaced water parcel influenced solely by the earth's rotation and defined by $2\Omega \sin \phi$, where Ω is the angular velocity of the earth and ϕ is the latitude.

Turbulent kinetic energy dissipation rate (ϵ): Rate of energy dissipation due to viscosity with units W kg⁻¹.

572 Diapycnal diffusivity (K): Diffusivity across density surfaces with units $m^2 s^{-1}$.

Barotropic tides: Nearly full-depth periodic rise and fall of ocean water due to the gravitational
attraction of the moon and sun.

Baroclinic/internal tides: Depth-varying oscillations at tidal frequencies arising from barotropic
tides impinging on topographic features.

Near-Inertial internal waves: Internal waves at or near the Coriolis/inertial frequency, often
but not always generated by the wind.

Lee waves: Internal waves often generated by deep geostrophic flow encountering topographic
features.

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13. Authorship

- ⁵⁸⁶ CW led the design and writing of the review. CL, ANG, JK, JM, and KS all contributed to the ⁵⁸⁷ writing.
- 588 14. Competing Interests

589 The authors declare no competing interests.

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Internal Wave Driven Mixing

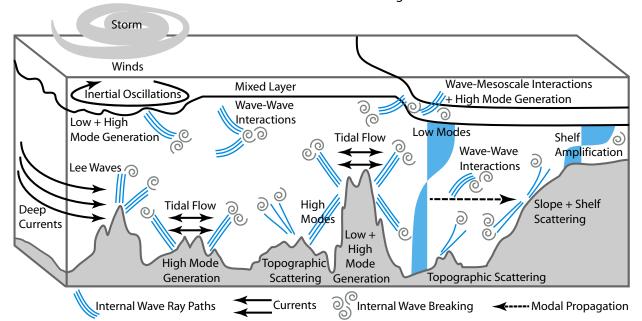


FIGURE 1. The primary internal wave mechanisms leading to ocean mixing. Tides flow over many forms of topography, from abyssal hills to tall steep ridges, generating both high-mode and low-mode internal waves. Time-varying winds cause near-inertial oscillations in the mixed layer, radiating high- and low-mode internal waves. Lee waves are generated when deep currents impinge on topographic features. Time-varying surface currents can also generate internal waves. Both high and low modes propagate, undergo wave-wave interactions, and scatter off topographic features, eventually leading to dissipation. Low modes generated in the open ocean can also propagate and dissipate on continental slopes and shelves. Modified from Ref [21].

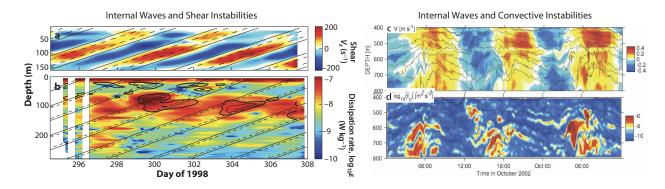


FIGURE 2. Turbulent mixing in two different internal wave environments. Meridional component of vertical shear (a) and dissipation rate (b) in the presence of a near-inertial internal wave from Ref [138]. Elevated dissipation rates are associated with strong vertical shear in the internal wave field, and turbulent mixing is attributed to shear instabilities. Adapted from Meridional velocity (c) and dissipation rate (d) during tidal flow over the Hawaiian ridge from Ref [237]. Peaks in the dissipation rate are in phase with the tidal cycle and are indicative of convective instabilities.

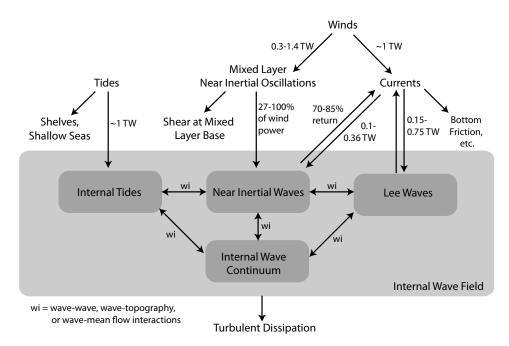


FIGURE 3. A simplified global energy budget of internal waves. Included are the sources of internal wave energy and the pathways of energy transfer until it is dissipated through turbulence. References for numbers quantifying energy transfers are provided in the main text.

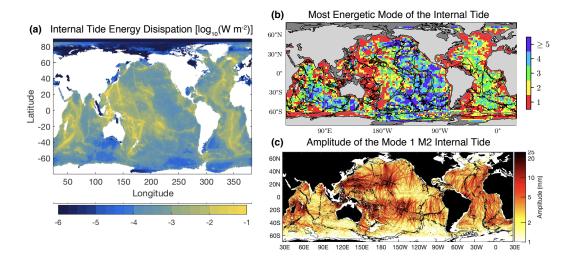


FIGURE 4. The lifecycle of internal tides, including generation, propagation, and turbulent dissipation. (a) A global map of the dissipation of the internal tide from a modelling study modified from Ref [63], (b) The most energetic mode (that is, vertical length scale) of internal tide generation varies throughout the globe, depending primarily on the geometry of the seafloor from Ref [68]. (c) The propagation of the first mode (the largest vertical length scale) M_2 internal tide can be tracked using sea surface height from altimetry up to thousands of kilometers away from the steep topographic generation sites [70] using an updated model [238] as explained in Ref [86].

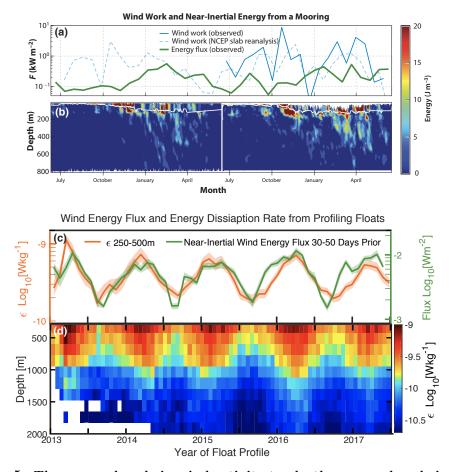


FIGURE 5. The seasonal cycle in wind activity tracks the seasonal cycle in nearinertial wave energy and dissipation rate in the North Pacific. (a-b) Mooring data show that the wind energy input into the mixed layer is elevated in the winter months, followed by an invigoration of the near-inertial internal wave field in the thermocline below, suggesting that the mixed layer oscillations radiate near-inertial internal waves (Modified from Ref[124]). A fraction of these waves will undergo turbulent dissipation locally. In fact, (c-d) the energy dissipation rate estimated using profiling float data also peaks in the winter, (c) lagging the wind energy flux from Ref [115].

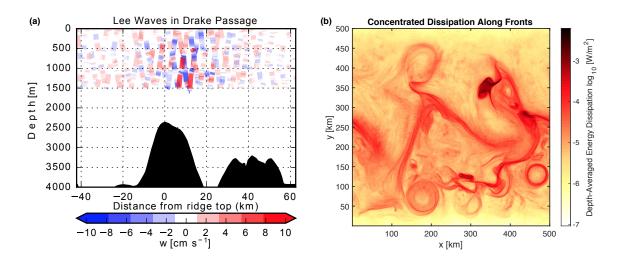


FIGURE 6. Two mechanisms for internal wave generation from geographic current. (a) Vertical velocity associated with lee waves in Drake Passage observed using profiling floats. (b) The vertically integrated energy dissipation in a high-resolution ocean model. Internal waves generated at fronts preferentially dissipate along those fronts. (a) Is from Ref [181] and (b) is modified from Ref [207].

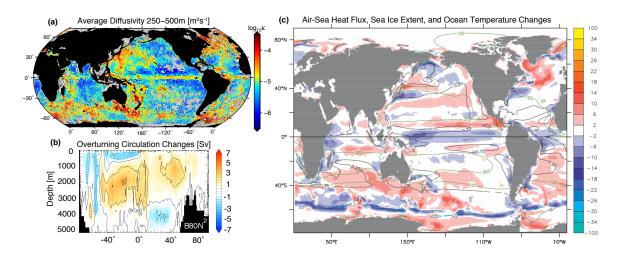


FIGURE 7. Global diapycnal mixing from internal waves and implications for circulation and climate. (a) The diffusivity estimated from profiling floats averaged between 250-500 m exhibits large geographic variability throughout the ocean (modified from Ref [115]). (b) The overturning circulation changes significantly when far-field tidal mixing is assigned to the basins compared to distributed across the basins, continental slopes and shelves (modified from Ref [210]). (c) Adding diffusivity from wind-generated near-inertial waves changes the downward surface heat flux (colors), sea ice extent (blue lines) and temperature on the 26 kg m⁻³ density surface (black line). The depth of 26 kg m⁻³ density surface is contoured in green, modified from Ref [226].