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Deep rule-based classifier for finger knuckle pattern recognition system

Abdelouahab Attia^{1,3}  · Zahid Akhtar² · Nour Elhouda Chalabi³ · Sofiane Maza¹ · Youssef Chahir⁴

Abstract

In this paper, we proposed a novel finger knuckle pattern (FKP) based personal authentication system using multilayer deep rule based (DRB) classifier. The presented approach is completely data-driven and fully automatic. However, the DRB classifier is generic and can be used in variety of classification or prediction problems. In particular, from the input finger knuckle, two kinds of features (i.e., Binarized Statistical Image Features and Gabor Filter bank) are extracted, which are then fed to fuzzy rules based DRB classifier to determine whether the user is genuine or impostor. Experimental results in the form of accuracy, error equal rate (EER) and receiver operating characteristic (ROC) curves demonstrate that presented DRB classifier is a powerful tool in FKP based biometric identification system. Experiments are reported using publicly available FKP PolyU database provided by University of Hong Kong. Experiments using this database show that the presented framework, in this study, can attain performance better than previously proposed methods. Moreover, score level fusion of all FKP modalities with BSIF + DRB yielded an equal error rate of 0.19% and an accuracy of 99.65%.

Keywords Deep rule based classifier · BSIF · Gabor filter bank · Finger knuckle pattern

1 Introduction

In today's highly interconnected society, automated personal identification methods have become crucial for security and privacy (Angelov and Gu 2018; Bao et al. 2018; Angelov and Sperduti 2016). One of person recognition methods is biometrics, which is considered as an alternative security system to traditional authentication and identification methods such as ID card, passwords, code PIN. Biometrics facilitate the process of recognizing a person based on their physiological, behavioral or chemical characteristics

(Adeoye 2010). Numerous biometric traits have been used in diverse applications ranging from border crossing to mobile authentication (Zhang et al. 2018; Akhtar et al. 2011a, b). In fact, many different biometric traits have been investigated widely such as fingerprint, iris, ear, finger knuckle print, palm print, face etc. (Chaa et al. 2017; Jaswal et al. 2017a). Recently, finger knuckle print (FKP) (Cappelli et al. 2010), which is included in the hand based biometric traits, have been studied in order to improve the consistent authentication system with higher accuracy (Jaswal et al. 2016). FKP has distinctive anatomical structures that can be recorded with low cost and small size imaging devices without using an extra hardware (Cappelli et al. 2010).

Generally, FKP biometrics system can be operated either in identification or verification mode. In identification mode, the given FKP sample is compared with all the available samples to determine the true identity of the subject. In verification mode, the given FKP sample is compared with samples of the claimed identity to determine whether it belongs to the same person. In addition, the FKP verification task is more difficult than the FKP identification because in matching stage it is required to give a global threshold in order to make a decision (Zhang et al. 2011; Aoyama et al. 2014).

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The FKP recognition system over recent years has been attracting considerable attention of researchers. The first team of researchers who introduced the use of finger knuckle surface in biometric systems are Woodard and Flynn (2005). Ferrer et al. (2005) have proposed a ridge features-based algorithm that extracted ridge features from FKP images and evaluated their similarity by applying Hidden Markov Model (HMM) or Support Vector Machine (SVM). Zeinali et al. (2014) have proposed a FKP recognition system, where directional filter bank (DFB) was used to extract feature followed by linear discriminate analysis (LDA) to reduce the dimensionality of the large feature vector. Attia et al. (2018) studied bank of binarized statistical image features (B-BSIF) on FKP trait. Zhang et al. (2012) developed a new computation framework focused on mounting new efficient feature extraction method for FKP recognition. The authors analyzed three commonly used local features, the local orientation, the local phase, and the phase congruency systematically. Also, they presented a method for computing all features efficiently using the phase congruency. Moreover, Hammouche et al. (2020) have proposed a new system for FKP authenticate based on phase congruency with Gabor Filter bank. Heidari and Chalechale (2020) introduced a novel FKP biometric system, where the feature extraction is combination of the entropy-based pattern histogram (EPH) and a set of statistical texture features (SSTF). The genetic algorithm (GA) was employed to locate the superior features among the extracted features. This has been tested on PolyU FKP dataset. While, Muthukumar and Kavipriya (2019) investigated Gabor feature with SVM classifier for FKP identification system. Singh and Kant (2019) have designed a multimodal biometric system based on FKP and iris traits for person authentication, where the PCA method has been used for feature extraction with the Neuro fuzzy neural network (NFNN) classifier in identification step. Malarvizhi et al. (2019) proposed a system named adaptive fuzzy genetic algorithm (AFGA) for Biometric authentication. Wang et al. (2014) investigated depth neural network for finger print classification. Lately, deep learning (i.e., deep neural networks) (Angelov and Soares 2020) have been explored for classification (Gu and Angelov 2018; Sargano et al. 2017) and FKP based biometrics (Chalabi et al. 2020). For instance, Qian et al. (2016) have proposed novel biometric image feature representation technique for FKP, known as deep gradient information (DGI). Jaswal et al. (2017b) considered a new FKP based biometric system that extracted the Region Of Interest (ROI) of FKP trait. Then, the ROI image has been improved and transformed by the invented several methods including, Bubble Ordinal Pattern (BOP), Star Ordinal Pattern (SOP), and Image Ray Transform (IRT). Furthermore, a new Deep Matching method has been used in the matching stage. Zhai et al. (2018) have been planned a new batch-normalized Convolutional Neural

Network (CNN) for FKP authentication system. The data augmentation techniques of random histogram equalization and dropout layer have been implemented to prevent over fitting during training of the proposed scheme.

Thapar et al. (2019) designed a scheme based on deep learning named FKIMNet for Finger Dorsal Image Matching Network. Chlaoua et al. (2019) have investigated a simple deep learning method named principal component analysis Network (PCANet) with SVM classifier. In the proposed scheme, PCA has been used to learn two-stages of filter banks then a simple binary hashing and block histograms for clustering of feature vectors. The output features are finally fed to classification step.

This paper introduces a new FKP system for person authentication based on multilayer deep rule-based classifier. The DRB Classifier is a novel approach that has not been applied before on a biometric system. Further, DRB generates a set of self-organized, transparent IF...THEN FRB (Fuzzy Rule Based) system structure. Each IF...THEN... fuzzy rule of the DRB system contains a various number of prototypes (templates stored in database) that are not pre-determined, recognized via a fully independent, online, non-iterative and non-parametric training process. Also, to their simplicity, the used technique provides a reasonable prototype (templates stored in database), which are then fed to fuzzy rules based of DRB classifier to determine whether the user is genuine or impostor.

The rest of this paper is organized as follows. Section 2 describes the architecture of the DRB classifier. The proposed FKP recognition methodology is outlined in Sect. 3. Section 4 presents the experimental results. The conclusions and future work are given in Sect. 5.

2 The DRB classifier architecture and algorithm

The presented system consists of four principle stages: pre-processing of FKP trait, feature extraction, (training) the DRB classification scheme and decision making. These stages are explained in detail in the following section.

2.1 The architecture of DRB classifier

The architecture of DRB classifier was first proposed by Angelov and Gu (2018). Figure 1 depicts the architecture of DRB classifier. In Fig. 1, it can be seen that the DRB classifier consists of four layers: (i) pre-processing block—the pre-processing block of the DRB classifier generally requires just the basic and commonly used pre-processing methods such as normalization, scaling, rotation and image segmentation; (ii) feature extraction layer—the feature extraction layer of the DRB classifier can use (any) diverse type of feature

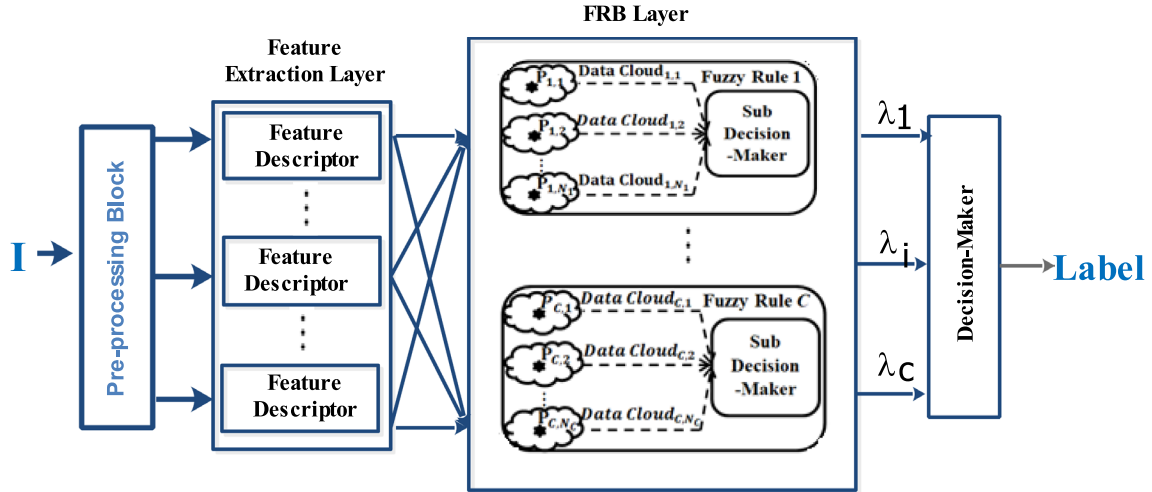


Fig. 1 General architecture of the DRB classifier (Angelov and Gu 2018)

descriptors, which are used in the field of biometric systems. The feature descriptors have some advantages and some limitations (Soltanpour et al. 2017); (iii) fuzzy rule based layer—massively parallel ensemble of highly interpretable IF...THEN... rules. These rules are based on the in parallel self-developing fuzzy rule-based models (Angelov and Yager 2012; Gu et al. 2018) that has been also expressed in Angelov and Gu (2017) by singletons in the consequent part (0-order models); and (iv) the decision-maker layer—its role is to decide the class label that won based on the partial suggestions of the massively parallel local/sub-decision makers as per IF...THEN... rule/per class. This layer is only used during the validation stage and it applies the “winner-takes-all” principle. As a result, one can see that the proposed

DRB classifier actually utilizes a two-stage decision-making structure. The validation process is described in Sect. 3.

2.2 The DRB classifier algorithm

The general architecture of the DRB classifier is illustrated in Fig. 1. The DRB classifier algorithm consists of four steps, which are detailed below. Before that, for simplicity, we describe the key notations used in DRB classifier algorithm in Table 1 (Angelov and Gu 2018). For the interested reader, the source code for DRB classifier algorithm can find at (<https://www.mathworks.com/matlabcentral/fileexchange/67772-deep-rule-based-classifier>).

Main steps of DRB classifier algorithm:

Table 1 Description of the key notations used in the algorithm

Notations	Description
C	The number of classes in dataset
d	The dimensionality of the feature vector
k	The number of the observed training images/current time instance
I	A single image
x	The corresponding feature vector of I
N_c	The number of identified prototypes of the c th class
μ_c	The global mean of feature vectors of the training images of the c th class
$I_{c,k}$	The k th training image of the c th class
$x_{c,k}$	The corresponding feature vector of $I_{c,k}$
$P_{c,i}$	The i th prototype of the c th class
$P_{c,i}$	The mean of feature vectors of the training images associated with $P_{c,i}$
$S_{c,i}$	The number of training images associated with $P_{c,i}$
$r_{c,i}$	The radius of the area of influence of <i>data cloud</i> associated with $P_{c,i}$
λ_C	The score of confidence given by the local decision-maker of the c th fuzzy rule

- Step 1. Pre-processing block: DRB classifier generally requires just the basic and commonly used pre-processing methods, including normalization, scaling, and rotation and image segmentation.
- Step 2. Feature extraction layer: DRB classifier can employ diverse type of feature descriptors.
- Step 3. Massively Parallel Fuzzy Rule Base (FRB) layer: This step is based on four stages, i.e., initialization, preparation, update of the system, and Fuzzy rules generation.

$$D(P_{c,i}) = \frac{1}{1 + \|C - \mu_c\|^2 / \sigma_c^2}$$

Stage 2: Updating system

After preparation stage, for each image of stage 1, DRB algorithm checks two conditions to update their parameters. If condition one is verified, add a new data cloud else find the nearest prototype $P_{c,n}$ corresponding to $I_{c,k}$ and go to the condition two. For the condition two, if it is verified Update $P_{c,n}$, $S_{c,n}$, and $r_{c,n}^2$. If condition two is not satisfied add a new data cloud.

Condition 1

Stage 0: Initialization

Initialize all parameters of DRB classifier algorithm such as:

```

IF
  ( $D(I_{c,k}) > \max_{j=1,2,\dots,N_c} (D(P_{c,i}))$ ) OR ( $D(I_{c,k}) < \min_{j=1,2,\dots,N_c} (D(P_{c,i}))$ )
Then
   $I_{c,k}$  Is new prototype
     $N_c \leftarrow N_c + 1;$ 
     $P_{c,N_c} \leftarrow I_{c,k}; P_{c,N_c} \leftarrow \bar{x}_{c,k}; S_{c,N_c} \leftarrow 1; r_{c,N_c} \leftarrow r_0$ 
Else
  Find  $P_{c,n}$  by  $P_{c,n} = \operatorname{argmin}(\|\bar{x}_{c,k} - P_{c,j}\|)$  where  $j =$ 
   $1, 2, \dots, N_c$ 

```

Condition 2

```

IF ( $\|\bar{x}_{c,k} - P_{c,n}\| < r_{c,N_c}$ ) Then
  ( $I_{c,k}$  is assigned to  $P_{c,n}$ )
Else
   $N_c \leftarrow N_c + 1; P_{c,N_c} \leftarrow I_{c,k}; P_{c,N_c} \leftarrow \bar{x}_{c,k}; S_{c,N_c} \leftarrow$ 
   $1; r_{c,N_c} \leftarrow r_0$ 
Endif
Endif

```

$k \leftarrow 1; \mu_c \leftarrow \bar{x}_{c,1}; N_c \leftarrow 1; P_{c,N_c} \leftarrow I_{c,1}; P_{c,N_c} \leftarrow \bar{x}_{c,1}; S_{c,N_c} \leftarrow 1; r_{c,N_c} \leftarrow r_0;$

Stage 1: Preparation

For each image $I_{c,k}$: $\bar{x}_{c,k}, \mu_c$, and $D(P_{c,i})$ is calculated such as:

$$\bar{x}_{c,k} = \frac{x_{c,k}}{\|x_{c,k}\|}; \mu_c = \frac{k-1}{k} \mu_c + \bar{x}_{c,k}$$

Stage 3: Fuzzy rules generation

Generate rule type

Rule_c: $IF(I \sim P_{c,1}) OR \dots OR(I \sim P_{c,N_c}) THEN(classe c)$

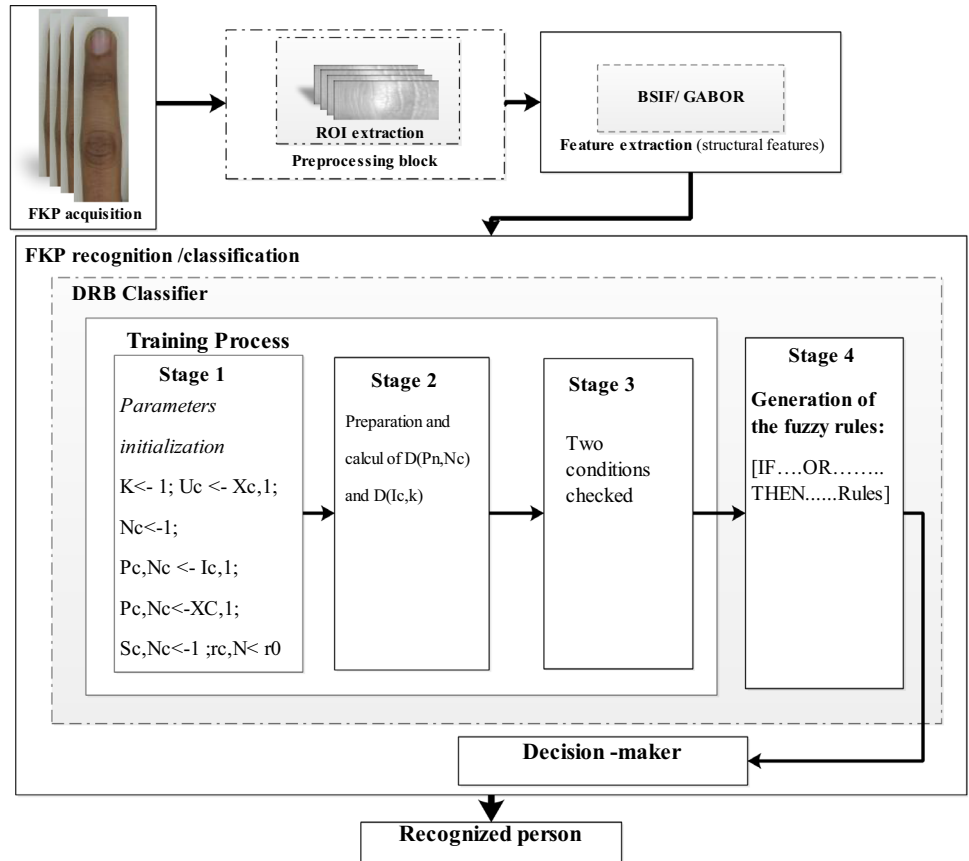
Stage 4: Decision maker layer

After the generation of C fuzzy rules to the C classes, for each image I in test data, generate a score of confidence $\tilde{\lambda}_c(I)$ based on the feature vector of image I such as:

$$- \tilde{\lambda}_c(I) = \operatorname{arg max} \left(\exp \left(-\|x - P_{c,j}\|^2 \right) \right), \quad j = 1, 2, \dots, N_c.$$

- Identified label by: $Label(I) = \operatorname{arg max} (\tilde{\lambda}_c(I)), \quad c = 1, 2, \dots, c.$

Fig. 2 The architecture of the proposed recognition system



3 The proposed FKP biometric system based on DRB classifier

The global architecture of the proposed FKP biometric system, including BSIF and Gabor based methods as main feature extractions and DRB classifier, is illustrated in Fig. 2, the global architecture of the proposed method is composed of a sequence of four main phases starting with the acquisition of FKP images, ROI extraction operations, and then the extraction of descriptive features that are fed to the proposed classifier multilayer deep rule based (DRB) to determine whether the user is genuine or impostor.

3.1 ROI extraction

The extraction the region of interest ROI for FKP (Jaswal et al. 2017a) consists of few steps. Firstly, the Gaussian smoothing operation is applied to the original image, and then the smoothed image is down sampled to 150 dpi. Secondly, the x-axis of the coordinate system fitted from the bottom boundary of the finger is determined; note that the bottom boundary of the finger can be easily extracted by a canny edge detector. Thirdly, the y-axis of the coordinate system is selected by applying a canny edge detector on the cropped sub-image that is previously extracted from the original image base on x-axis, then the convex direction coding scheme is found. Finally, the ROI is extracted,

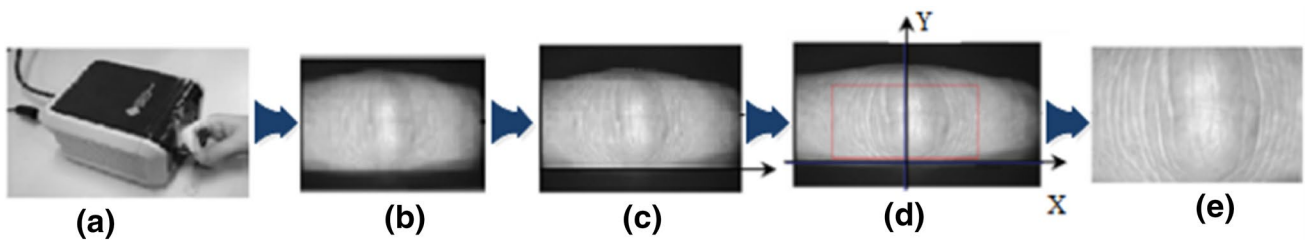


Fig. 3 The steps of extraction of FKP ROI image

where the rectangle indicates the area of the ROI, which will be extracted and used further user recognition as shown in Fig. 3.

3.2 Feature extraction

Feature extraction is another important stage. There are various kinds of feature descriptors presented in the literature. However, in this paper we chose the BSIF descriptor (binarized statistical image features) and Gabor feature extraction because these two have been successfully employed widely for object detection and recognition.

3.2.1 BSIF descriptor (binarized statistical image features)

Binarized statistical image feature (BSIF) is a textural local descriptor presented in Kannala and Rahtu (2012a). This feature descriptor basically utilizes a set of filters of fixed size that describes the neighborhood configuration of the central pixel. BSIF filters a given image J of size $m \times n$ with a set of filters $\phi_i^{k \times k}$ then the responses are binarized. The filter response is obtained as follows:

$$r_i = \sum_{m,n} \phi_i^{k \times k} J(m,n) \quad (1)$$

where $\phi_i^{k \times k}$ is a linear filter of size k and $i = \{1, 2, \dots, n\}$ denotes the number of statistically independent filters whose response can be computed together and binarized to obtain the binary string as follows (Kannala and Rahtu 2012b):

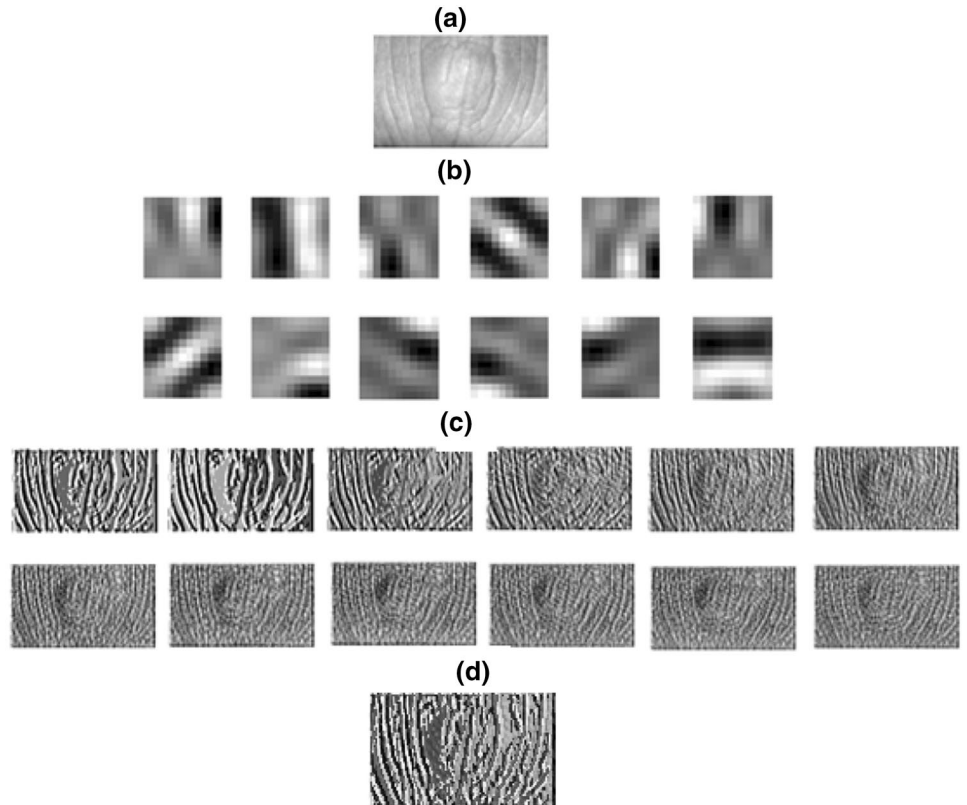
$$b_i = \begin{cases} 1 & \text{if } r_i < 0 \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

Lastly, the BSIF features are obtained as the histogram of pixel's binary codes that can effectively characterizes the texture components in the FKP image. There are two important factors in BSIF descriptor namely: the filter size k and the filter length (n). The corresponding BSIF code (<https://www.ee.oulu.fi/~jkannala/bsif/bsif.html>) depth and intensity images are shown in Fig. 4. Thus, Fig. 4a indicates the input ROI FKP image. Figure 4b shows the learned BSIF filter with a size 11×11 and of length 12. Figure 4c shows the results of the individual convolution of the ROI FKP image with BSIF filter. Figure 4d shows the final BSIF feature encoded.

3.2.2 Gabor feature extraction

Gabor wavelet is another useful tool in image analysis and computer vision thanks to its optimal localization properties in spatial analysis as well as frequency domain. Broadly speaking, the family of 2D Gabor wavelets (<https://es.mathw>

Fig. 4 **a** Sample of the FKP ROI image, **b** BSIF filter with a size 11×11 and of length 12, **c** BSIF features **d** final BSIF



orks.com/matlabcentral/fileexchange/44630-gabor-feature-extraction) can be described in the spatial domain (Liu and Wechsler 2002; Shen and Bai 2006) as follows:

$$H_{\mu,\theta} = \frac{f_{\mu}^2}{\pi n \lambda} \exp \left[-\left(\frac{f_{\mu}^2}{n^2} \right) x_p^2 - \left(\frac{f_{\mu}^2}{\lambda^2} \right) y_p^2 \right] \exp(j2\pi x_p) \quad (3)$$

where $x_p = x \cdot \cos(\theta_{\theta}) + y \cdot \sin(\theta_{\theta})$, $y_p = -x \cdot \sin(\theta_{\theta}) + y \cdot \cos(\theta_{\theta})$, $f_{\mu} = f_{max}/2^{(\mu/2)}$ and $\theta_{\theta} = \nu\pi/8$ with f_{μ} and f_{max} are the center and the maximal frequency of Gabor filter, respectively, and θ_{θ} denotes the orientation. The parameters η and λ explain the size of the Gaussian envelope along x-axis and y-axis correspondingly. The factors of the Gabor filter bank are experimentally selected as: $f_{max} = 0.25$ and $\lambda = \eta = \sqrt{2}$. The Gabor representation of a J-image can be done by convolving this image with the bank of Gabor filter (5 scales, 8 orientations) as defined by:

$$Y_{\mu,\theta} = J(x, y) * H_{\mu,\theta} \quad (4)$$

where $J(x,y)$ is considered as complex structure of two images real and imaginary denoted as R-image or I-image and $*$ is the product convolution. The output $Y_{\mu,\theta}$ has the complex structure; the augmented magnitude feature vector of the J-image is extracted.

First for each J-image, special Gabor filter bank is applied with 5 scales (μ) and 8 orientations (ν) to obtain 40 filtered images. Then, the calculation of 40 magnitudes responses from 40 filtered image where each magnitude response is then down-sampling by a factor $\rho = 64$ and preprocessed by normalization to zero mean with unit variance Fig. 5 shows an example. Lastly, each down-sampled magnitude response $M_{\mu,\theta}$ is reorganized into a vector $W_{\mu,\theta}$ by scan columns. The 40 vectors are concatenated to construct the feature vector of R-image or I-image as it can be seen in the following equation:

$$Y = [W_{0,0}, W_{0,1}, \dots, W_{4,7}]^T \quad (5)$$

3.3 Classification

Once the selection of the discriminative and pertinent characteristics of each image is done, the different classes are separated, and the decision is made in order to accept the user as genuine or reject as an impostor.

In order to carry out this stage in our system, we have employed Deep Rule-Based (DRB) based classification technique.

3.3.1 DRB training architecture

Deep Rule-Based classifier is a process that works with four main phases representing its global system mechanism (Angelov and Gu 2018), which are initialization phase, preparation phase, updating phase, fuzzy rules generation phase.

Table 2 Parameters initialization

Parameter	Description
$K \leftarrow 1;$	k is the current time instance
$\mu_c \leftarrow X_{c,1};$	μ_c is the global mean of all the observed data of the class c
$N_c \leftarrow 1;$	N_c is the number of prototypes
$P_{c,N_c} \leftarrow I_{c,1}; P_{c,N_c} \leftarrow X_{c,1};$	P_{c,N_c} prototypes of the class c
$S_{c,N_c} \leftarrow 1;$	S_{c,N_c} number of images of the data cloud
$r_{c,N_c} \leftarrow r_0$	r_{c,N_c} is the radius of the area of the data cloud

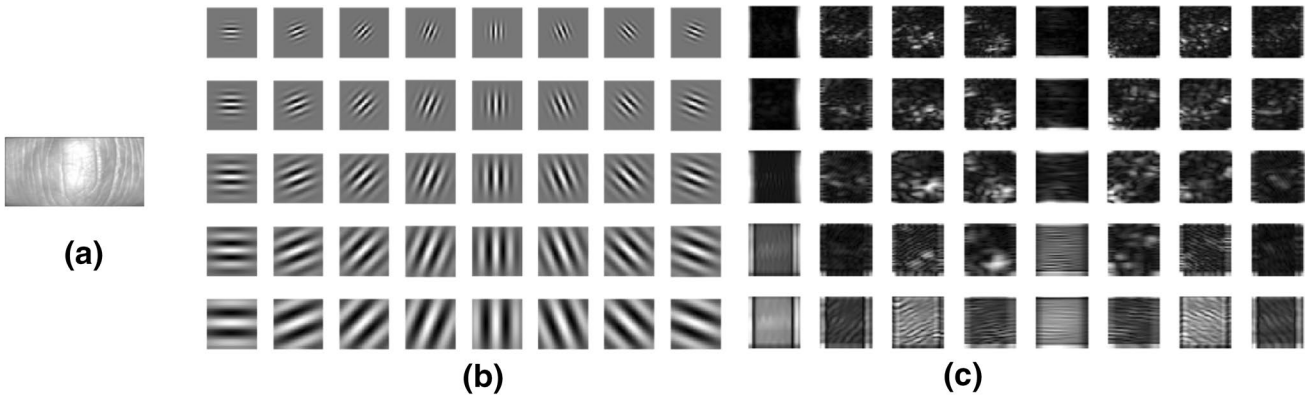


Fig. 5 a original FKP image, b 40 Gabor filter bank with different scales and orientations, c magnitude of the image filtered by every Gabor filter

3.3.2 Initialization phase

In this phase, the classifier begins with a vector normalization operation $X_{c,1}$ applied to the global feature vector of the first image of the class “c” $I_{c,1}$ with an initialization of the different meta-parameters of the system as shown in Table 2:

3.3.3 Preparation phase

For all the images of all the classes $I_{c,k}$, $X_{c,k}$ is the normalization vector applied to its corresponding feature vectors, the global mean μ_c is updated as shown in the following instruction:

$$\mu_c = \frac{K-1}{K} \mu_c + \frac{1}{K} \bar{X}_{c,k} \quad (6)$$

Then, the density of all the existing prototypes P_{c,N_c} of the new image $I_{c,k}$ is calculated as denoted by: $D(P_{c,N_c})$ and $D(I_{c,k})$.

3.3.4 Updating stage

From the previously calculated μ_c , $D(P_{c,N_c})$ and $D(I_{c,k})$, two conditions are identified:

Condition 1: IF $[D(I_{c,k}) > \max D(P_{c,N_c})]$ OR $[D(I_{c,k}) < \min D(P_{c,N_c})]$ THEN $(I_{c,k})$ is set to a new prototype and initializes a new data cloud. however if this condition is not verified, $P_{c,n}$ look for the nearest prototype to $I_{c,k}$ as shown in Eq. 7:

$$P_{c,n} = \arg \min \left(\|\bar{X}_{c,k} - P_{c,j}\| \right) \quad \text{where } j = 1, 2, \dots, N_c \quad (7)$$

where *argmin* is function that gives the nearest prototype by minimizing the distance between the normalized feature vector denoted by $\bar{X}_{c,k}$ and the mean of feature vectors of the training images $P_{c,j}$.

Condition 2: IF $[\|X_{c,k} - P_{c,n}\| < r_{c,N_c}]$ THEN $[I_{c,k}$ is assigned to $P_{c,n}]$ ELSE $[I_{c,k}$ is out of the area of $P_{c,n}]$.

A new data cloud is added, the next image is grabbed at phase 2 (preparation phase) with the processing of all the training samples.

3.3.5 Fuzzy rules generation stage

In this last phase, the system generate one Anaya rule based on the identified prototypes

$$R : IF(I \sim P_{c,1}) OR \dots OR(I \sim P_{c,N_c}) THEN(classc) \quad (8)$$

where ‘ \sim ’ denotes similarity; I is a particular image with its corresponding vector feature vector x ; P is the prototype; N_c is the number of prototypes of the c th class;

4 Experiments

In this section, we provide an experimental evaluation of the proposed FKP based person recognition system.

4.1 FKP database

The proposed method has been tested on the publicly available FKP dataset that provided by Hong Kong Polytechnic University (PolyU) (2010). This database has 7920 images collected from 165 persons with 125 males and 40 females, their age is in the range of 20–50 years old. The images were captured in two sessions, 48 different FKP images of each individual. Four finger types of every person have been collected that are: Left Index Finger (LIF), Left Middle Finger (LMF), Right Index Finger (RIF) and Right Middle Finger (RMF). Every finger type has 6 images in each session. There are total 1980 number of images for each finger type.

4.2 Experiment results

In this section, we report two different experiments: Experiment I—where we tested the approach on single modality, and Experiment II—where we tested the approach on Multi-trait (Multi modalities) FKP system.

4.3 Experiment I: single modality

The main goal of this experiment is to test and evaluate the introduced scheme on FKP single modality (LIF, RIF, RMF, LMF) using DRB classifier with different distances such as Euclidean, Cos, Correlation as well as Gabor filter bank and BSIF descriptor. In this sets of experiments, we highlight the

Table 3 Single modalities results

Modality	Distance	Gabor-DRB		BSIF-DRB	
		Acc (%)	EER (%)	Acc (%)	EER (%)
RIF	Euclidean	93.43	5.55	93.94	4.20
	Cosine	93.08	5.61	93.43	4.10
	Correlation	93.08	5.61	93.08	6.63
RMF	Euclidean	94.09	5.21	94.14	4.13
	Cosine	94.19	5.10	92.98	3.99
	Correlation	94.19	5.10	93.28	6.98
LIF	Euclidean	94.34	4.95	92.73	4.72
	Cosine	93.94	4.99	91.46	5.23
	Correlation	93.94	4.99	91.77	8.34
LMF	Euclidean	93.43	5.96	93.54	4.19
	Cosine	93.08	5.91	92.47	4.40
	Correlation	93.08	5.91	92.78	6.77

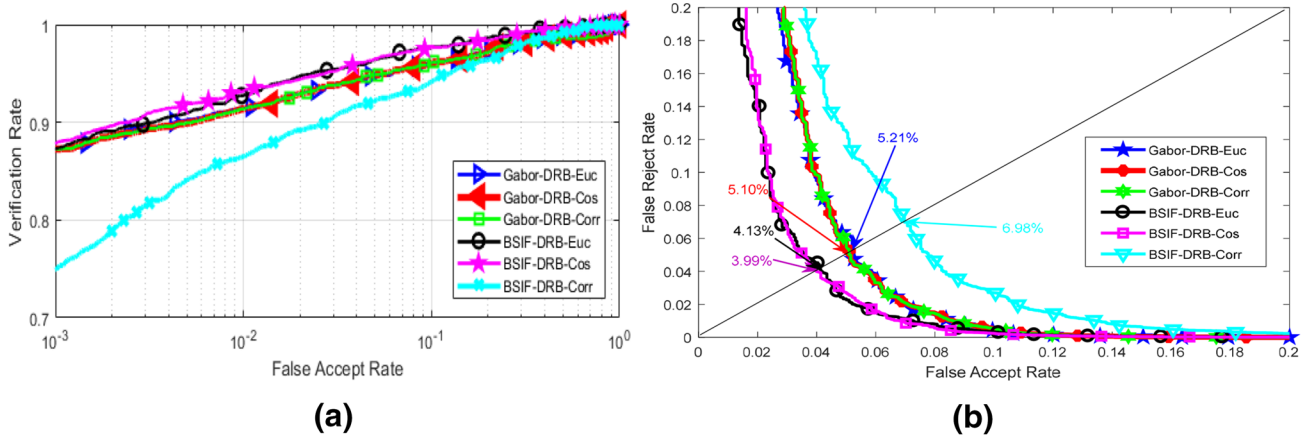


Fig. 6 RMF modality results: a ROC, b EER curves

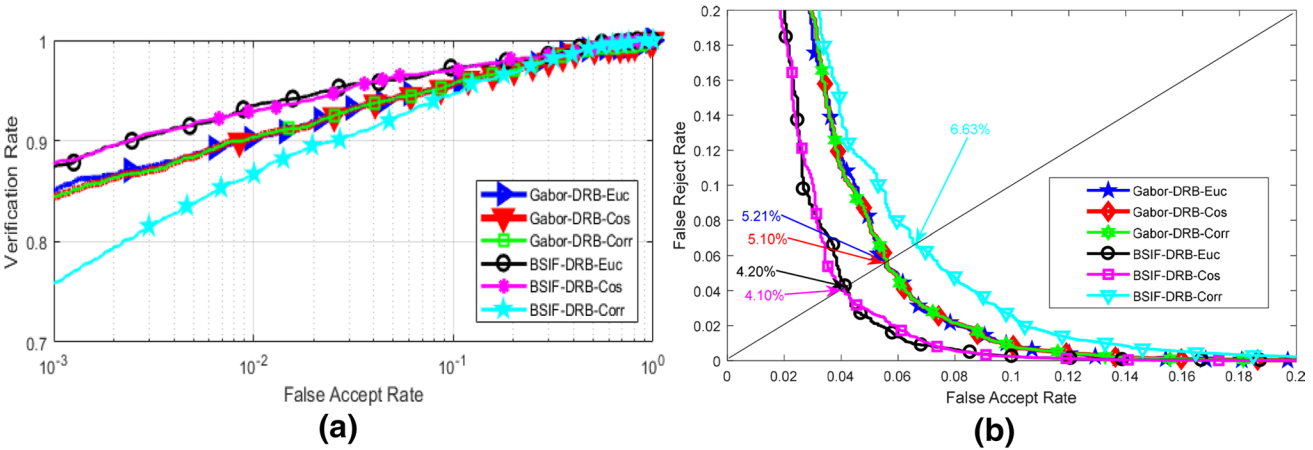


Fig. 7 RIF modality results: a ROC, b EER curves

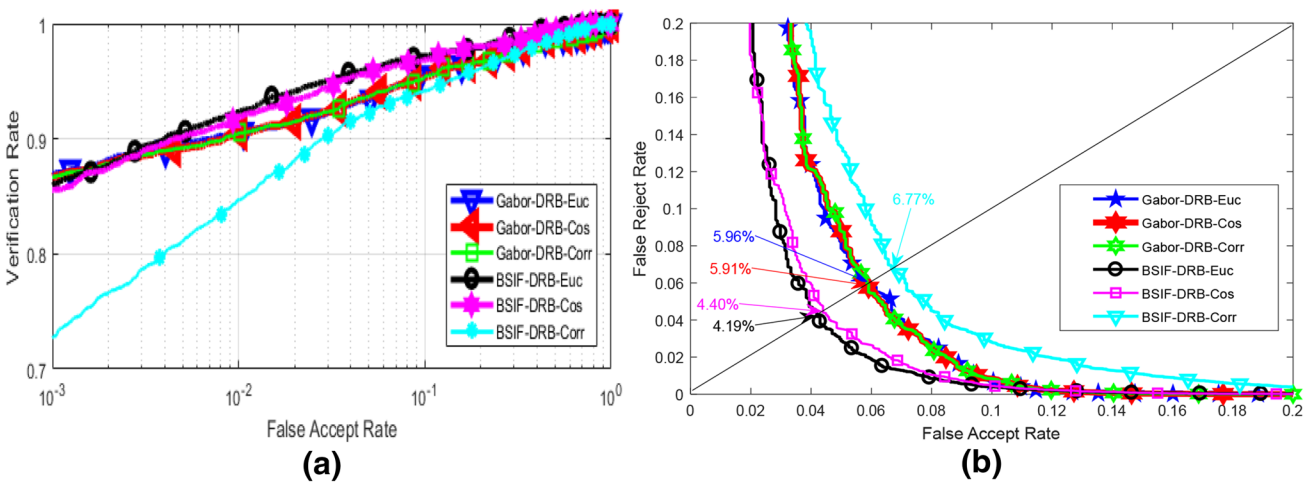


Fig. 8 LMF modality results: a ROC, b EER curves

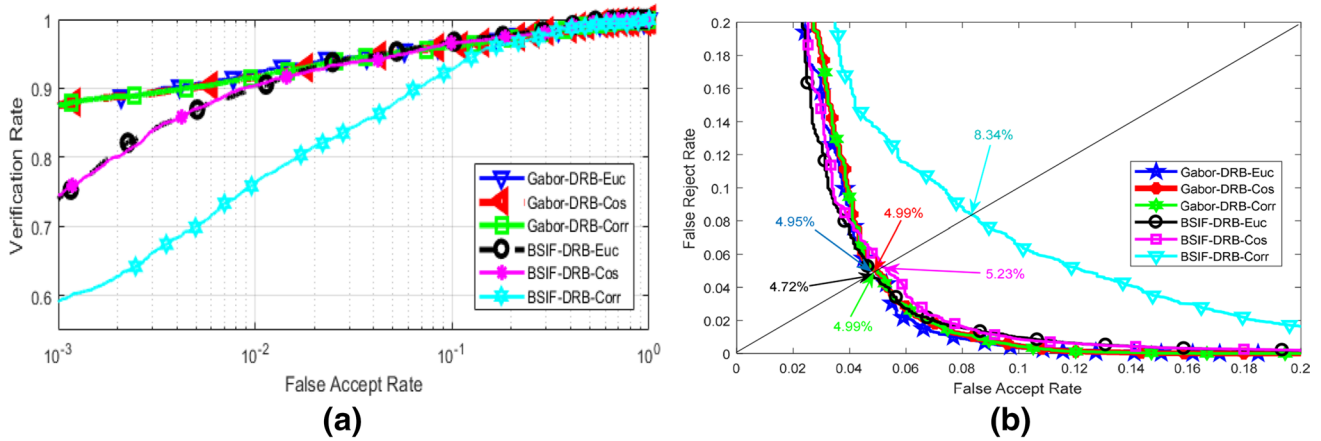


Fig. 9 LIF modality results: a ROC, b EER curves

Table 4 Comparative of proposed personal recognition method with the existing approaches for FKP using PolyU dataset

Identification (Rank-1)					
References	Year	LMF (%)	LIF (%)	RIF (%)	RMF (%)
El-Tarhouni et al. (2014)	2014	94.70	93.80	92.20	94.80
Shariatmadar and Faez (2013)	2013	95.54	94.33	95.93	96.72
Zeinali et al. (2014)	2014	90.30	88.68	89.79	89.79
Proposed method	2020	93.54	94.34	93.94	94.19

Our achieved results are indicated in bold

comparison between distances and descriptors that achieve good accuracy.

The results of BSIF-DRB and Gabor-DRB on individual FKP traits are presented in Table 3. We can observe in Table 3 that BSIF-DRB performs better than Gabor-DRB. The proposed method using BSIF-DRB achieves higher accuracy on the RIF, LMF, and RMF, modalities, e.g., on RMF modality the system achieved EER = 4.13% and accuracy = 94.14% using Euclidean distance in verification and identification modes, respectively. Gabor-DRB performs better than BSIF-DRB on the LIF modality using the three distances.

To further explore our findings, the BSIF-DRB and Gabor-DRB comparison results are also presented in term of EER and ROC curves, which can be seen in Figs. 6, 7, 8, 9. These graphs also report comparison study between the proposed method BSIF-DRB and Gabor-DRB with different distances using FKP modality. The results clearly show that the performance is better when the system uses the features of the BSIF descriptor with Euclidean distance.

To further demonstrate the efficacy of the proposed system, the comparison of the proposed framework has been done with prior works in the literature on individual FKP modalities, as shown in Table 4. The proposed scheme achieves accuracy in range of 91.46% to 94.34%, which is a good result compared to the existing FKP person recognition

Table 5 Two fingers fusion results using min rule score level fusion

Modality	Distance	Gabor-DRB		BSIF-DRB	
		Acc (%)	EER (%)	Acc (%)	EER (%)
RIF-RMF	Euclidean	98.43	2.17	97.27	2.21
	Cosine	98.48	2.21	96.52	2.67
	Correlation	98.48	2.21	95.91	3.69
RIF-LMF	Euclidean	97.63	2.93	96.82	1.97
	Cosine	97.42	2.83	96.52	2.27
	Correlation	97.42	2.83	96.67	2.70
RIF-LIF	Euclidean	98.28	2.28	96.67	2.67
	Cosine	98.08	2.51	95.76	2.84
	Correlation	98.08	2.51	94.95	2.51
RMF-LMF	Euclidean	98.08	2.27	97.37	1.99
	Cosine	97.63	2.37	96.82	2.16
	Correlation	97.63	2.37	96.36	2.43
RMF-LIF	Euclidean	98.08	2.24	97.32	2.68
	Cosine	97.73	2.42	96.82	2.42
	Correlation	97.73	2.42	95.61	3.54
LMF-LIF	Euclidean	96.87	2.13	96.62	2.84
	Cosine	96.72	2.29	95.86	2.86
	Correlation	96.72	2.29	95.05	3.02

systems. For instance, the proposed method on LIF modality is able to attain 94.34% in identification mode. While, FKP

Table 6 Two finger fusion results using sum rule score level fusion

Modality	Distance	Gabor-DRB		BSIF-DRB	
		Acc (%)	EER (%)	Acc (%)	EER (%)
RIF-RMF	Euclidean	98.03	1.84	97.63	2.37
	Cosine	97.32	2.13	97.17	2.63
	Correlation	97.32	2.13	97.17	2.93
RIF-LMF	Euclidean	97.53	2.34	97.58	2.11
	Cosine	96.52	2.63	96.62	2.74
RIF-LIF	Euclidean	98.13	1.44	97.93	2.43
	Cosine	97.78	1.98	96.82	2.82
RMF-LMF	Euclidean	97.78	1.92	98.32	1.82
	Cosine	97.42	2.24	97.42	2.07
	Correlation	97.42	2.24	96.72	2.69
RMF-LIF	Euclidean	97.73	1.79	98.13	1.47
	Cosine	97.22	2.44	97.07	2.83
	Correlation	97.22	2.44	97.12	2.69
LMF-LIF	Euclidean	97.32	2.08	97.12	2.01
	Cosine	96.92	2.34	96.92	2.13
	Correlation	96.92	2.34	96.21	2.57

Table 7 Three finger and all fingers fusion results using min rule score level fusion

Modality	Distance	Gabor-DRB		BSIF-DRB	
		Acc (%)	EER (%)	Acc (%)	EER (%)
RIF-RMF-LMF	Euclidean	99.34	1.17	98.48	1.51
	Cosine	98.99	1.22	97.68	1.58
	Correlation	98.99	1.22	97.53	2.22
RIF-RMF-LIF	Euclidean	99.29	1.47	98.13	1.17
	Cosine	99.29	1.41	97.53	1.97
	Correlation	99.29	1.41	96.31	2.38
RIF-LMF-LIF	Euclidean	98.48	1.92	98.48	1.82
	Cosine	98.33	1.87	97.53	1.67
	Correlation	98.33	1.87	96.57	2.44
RMF-LMF-LIF	Euclidean	99.14	1.51	98.64	1.92
	Cosine	98.64	1.56	98.03	1.58
	Correlation	98.64	1.56	97.02	2.61
All finger	Euclidean	99.65	0.91	99.09	1.51
	Cosine	99.39	0.91	98.28	1.42
	Correlation	99.39	0.91	97.42	1.69

based person recognition systems proposed in El-Tarhouni et al. (2014) achieved 93.80%.

Table 8 Three finger and all fingers fusion results using sum rule score level fusion

Modality	Distance	Gabor-DRB		BSIF-DRB	
		Acc (%)	EER (%)	Acc (%)	EER (%)
RIF-RMF-LMF	Euclidean	98.89	1.07	98.94	1.47
	Cosine	98.33	1.43	98.69	1.47
	Correlation	98.33	1.43	98.59	1.69
RIF-RMF-LIF	Euclidean	98.84	1.12	98.99	1.52
	Cosine	98.28	1.57	98.84	1.92
	Correlation	98.28	1.57	98.79	1.68
RIF-LMF-LIF	Euclidean	98.69	1.19	99.19	1.81
	Cosine	98.13	1.82	98.28	1.12
	Correlation	98.13	1.82	98.43	1.67
RMF-LMF-LIF	Euclidean	98.38	1.27	99.24	1.02
	Cosine	97.98	1.93	98.84	1.87
	Correlation	97.98	1.93	98.38	1.14
All finger	Euclidean	99.24	0.82	99.65	0.19
	Cosine	98.64	1.58	99.44	0.40
	Correlation	98.64	1.58	98.89	1.48

4.4 Experiment II: multi-traits (multimodal) biometrics system

Our main aim for this experiment is to investigate the performance of proposed system in the case of information fusion, given that multimodal systems that combine information from different sources are able to overcome some limitations (e.g., accuracy, noise, etc.) of the unimodal biometric systems. Thus, further tests were carried out, where we studied different scenarios when the information presented by different finger types (LIF, LMF, RIF, and RMF) modality are integrated.

The experiments were performed using level score fusion, where the information were fused by applying two score rules min rule and sum rule. We distinguish three experimental investigation were conducted by (i) fusing only two types of fingers as shown in Tables 5, 6, (ii) three types of fingers as revealed in Tables 7, 8, (iii) all types of fingers as it can be seen in Tables 7, 8. Finally, a comparison with existing FKP multimodal methods in reported in Table 9.

4.4.1 Experiment 1: two fingers

In this experiment, we have used 6 different combinations of two fingers: RIF-RMF, RIF-LMF, RIF-LIF, RMF-LMF, RMF-LIF employing DRB classifier with different distances such as Euclidean, Cos, Correlation as well as Gabor filter bank and BSIF descriptor, and two rules, i.e., min and sum score level fusion. From the results of BSIF-DRB and Gabor-DRB of two fingers presented in Table 5,

Table 9 Comparison of the proposed multimodal system with the existing approaches for FKP

References	Year	Method	Performance	LIF-RIF	LIF-LMF	All finger
Thapar et al. (2019)	2019	FKIMNet	EER (%)	–	–	2.03%
			Rank-1 (%)	–	–	94.02%
Zeinali et al. (2014)	2014	DFB + LDA	Rank-1 (%)	97.27%	95.55%	99.29%
Chlaoua et al. (2019)	2019	PCANet + SVM	EER (%)	–	0.404%	0.00%
			Rank-1 (%)	–	97.84%	100%
Jaswal et al. (2017b)	2017	DeepMatching	EER	–	–	0.92%
Proposed system	2020	Gabor-DRB	EER (%)	2.44%	3.01%	1.82%
			Rank-1 (%)	98.13%	97.32%	99.24%
		BSIF-DRB	EER (%)	2.33%	3.08%	0.19%
			Rank-1 (%)	97.93%	97.12%	99.65%

Our achieved results are indicated in bold

we can observe that one modality trait using BSIF-DRB performs better than Gabor-DRB. Here, the proposed method using Gabor-DRB achieves higher accuracy on all combination of two fingers (RIF-RMF, RIF-LMF, RIF-LIF, RMF-LMF, RMF-LIF) by applying min rules score level fusion. The accuracy ranges from 96.72 to 98.48% including all distances, and in comparison, to BSIF-DRB where the accuracy ranges from 95.05 to 97.37% including all distances. We also can see that the best fusion of two fingers according to the accuracy belongs to the first combination that is RIF-RMF for Gabor-DRB. The EER ranges from 2.17 to 2.93% including all distances for Gabor-DRB, and EER that ranges from 1.97 to 3.69% including all distances for BSIF-DRB, where we can see that the best EER achieved belongs to BSIF-DRB that equals to 1.99% but over all Gabor-DRB results were better.

The results of BSIF-DRB and Gabor-DRB of two fingers are presented in Table 6 using sum rule score level fusion. We can see that results over all are quite similar for both Gabor-DRB and BSIF-DRB including all distances, where the best accuracy belongs to RIF-RMF using Euclidean distance by accuracy equals to 98.03% for Gabor-DRB. While, for BSIF-DRB, the best accuracy is attained by RMF-LMF Euclidean distance, i.e., 98.32% EER. We can observe more stability regarding Gabor-DRB, where it ranges from 1.79 to 2.63% for all distances and combinations. While, BSIF-DRB ranges from 1.47 to 2.83% for all distances and combinations. We can state that the best EER achieved belongs to BSIF-DRB by RMF-LM Fusing Euclidean distance.

Overall in comparison of min score level fusion results in Table 5 and sum rule score level fusion results in Table 6. For two fingers, it appears that min rule has achieved slightly better results in general; it was able to get an accuracy of 98.48% as best, while sum rule got 98.32%.

4.4.2 Experiment 2 and 3: three fingers and all fingers

In this experiment, we have used 4 different combinations of three fingers: RIF-RMF-LMF, RIF-RMF-LIF, RIF-LMF-LIF, RMF-LMF-LIF and all fingers combined employing DRB classifier with different distances such as Euclidean, Cos, Correlation as well as Gabor filter bank and BSIF descriptor and two rules, i.e., min and sum score level fusion.

In Table 7, we can see clearly the catching increase in the accuracy, regardless of the descriptor employed, using three fingers and all fingers fusion by applying min rule score level fusion. The best accuracy achieved by three fingers equals to 99.34% with RIF-RMF-LMF fingers fusion using Gabor-DRB and Euclidean distance, and 98.64% using BSIF-DRB and Euclidean distance by RMF-LMF-LIF three fingers. Whereas, the best EER equals to 1.17% with RIF-RMF-LMF three finger fusion using Gabor-DRB and Euclidean distance, and 1.51% using BSIF_DRB and Euclidean distance by RIF-RMF-LMF fingers fusion. All in all, we can conclude that the Gabor-DRB is better than BSIF-DRB.

For all fingers fusion, we can observe in Table 7 that fusion using min score level fusion rule was able to attain the highest results, where the accuracy reached 99.65% using Gabor-DRB and Euclidean distance and EER equals to 0.91%.

Table 8 shows the accuracy and EER achieved using three finger and all fingers fusion by applying sum rule. The best accuracy via three fingers equals to 98.89% with RIF-RMF-LMF fingers fusion using Gabor-DRB and Euclidean distance, and 99.24% using BSIF-DRB and Euclidean distance by RMF-LMF-LIF three fingers. While, the best EER equals to 1.07% for RIF-RMF-LMF three finger fusion using Gabor-DRB and Euclidean distance, and 1.62% using BSIF-DRB and Euclidean distance by RIF-RMF-LMF fingers fusion. Therefore, we can conclude that BSIF-DRB is better than Gabor-DRB using sum score level fusion rule. For all fingers fusion, we can observe in Table 8 that fusion

Fig. 10 Curve ROC for all min score level fusion

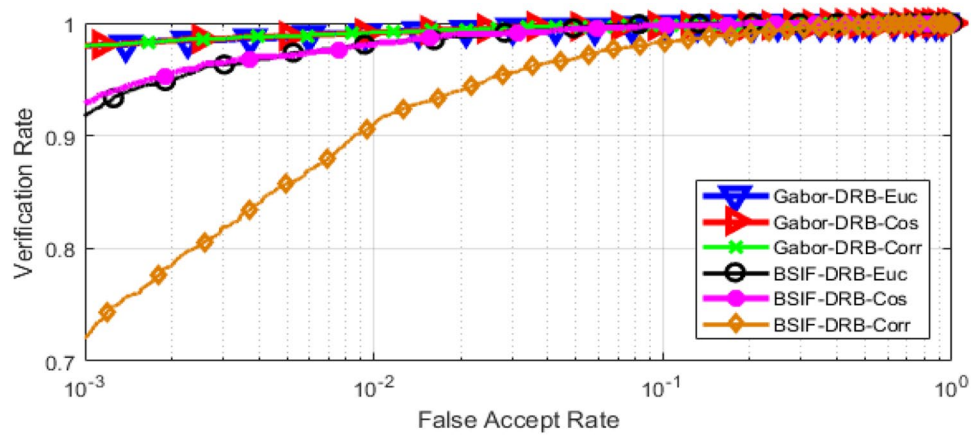
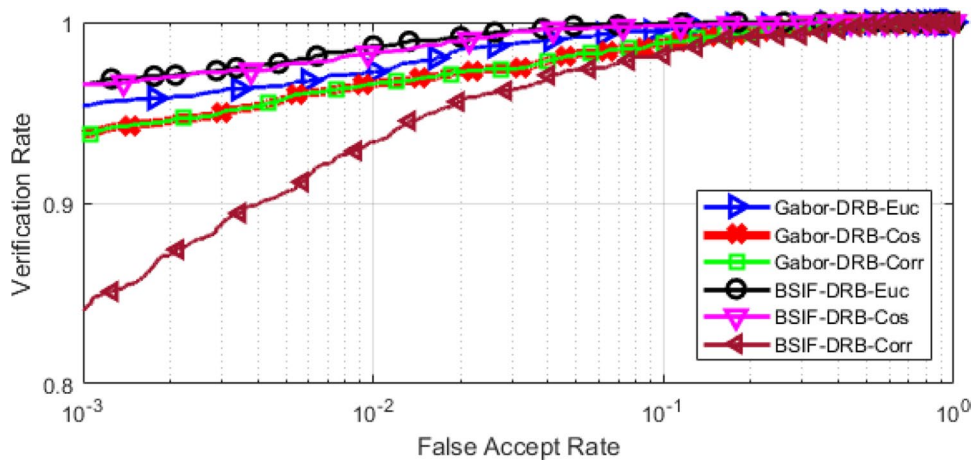


Fig. 11 Curve ROC for all sum score level fusion



utilizing sum score level fusion rule has shown best results, where the accuracy reached 99.65% using BSIF_DRB and Euclidean distance and EER equals to 0.19%.

By comparing the min score level fusion rule results in Table 7 with sum score level fusion rule results in Table 8 for three fingers, we can state that min rule has achieved better results in general where it was able to get an accuracy of 99.34% as the best, while sum rule reached 99.65% as highest accuracy. But overall min rule performed better. For all fingers, it was able to top all results obtained using two and three finger fusion such that it was able to get a 99.65% accuracy for both rules.

For further analysis of the results, we have obtained ROC curves to report comparison between the proposed method BSIF-DRB and Gabor-DRB with different distances utilizing FKP modality fusion and min rule in Fig. 10 and sum rule in Fig. 11. The results clearly show that the performance

is better when the system uses the features of the Gabor filter bank with Euclidean distance.

Lastly, we can conclude from the previous experiment of single modality and the experiment using multi-trait (multimodal) that a multi-trait system has improved the performance of the proposed method, and as the number of modalities increases as the accuracy of the system.

4.4.3 Comparison with prior studies on FKP

The comparison of proposed multimodal system with existing systems in the literature is presented in Table 9. We can notice in Table 9 that the proposed system under verification mode attained lowest EER that is 0.19%. compared to EER by systems in Jaswal et al. (2017b) and Thapar et al. (2019) for all fingers. In identification mode, for the modalities (LIF-RIF), (LIF-LMF) and all finger the proposed system

achieved highest recognition rate (rank-1) compared to scheme designed in Zeinali et al. (2014). In addition, the presented system in this study achieved 99.65% of rank-1, which is better than FKIMNet proposed in Thapar et al. (2019). It can also be noted that work in Chlaoua et al. (2019) achieved the highest recognition rate 100% for all fingers, but if we observe for two fingers (e.g., LIF-RIF or LIF-LMF) the proposed system reached a good performance.

5 Conclusion

This paper presents a new method for recognizing individuals based on their finger knuckle patterns (FKP). Specifically, the proposed method applied deep rule based (DRB) classifier on FKP. Together with DRB, two different feature extraction methods (i.e., Binarized Statistical Image Features and Gabor Filter bank) have been used. The results obtained on public PolyU dataset are quite impressive. Extensive empirical analyses were performed, in this study, using single modality and multi-traits/multimodal (two fingers and three fingers and all finger fusion) based on min and sum score level fusion rules. The obtained results demonstrated that DRB classifier is a powerful tool in person identification biometrics systems, especially in the case of multi-trait. The proposed method was able to attain accuracy comparable with existing schemes. Future work aims to realize a modified DRB classifier in computing similarities between features based on map diffusion. Also, the effectiveness of the proposed method under adversarial attacks will be studied.

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