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## Recommended acetylene ${ }^{12} \mathrm{C}_{2} \mathbf{H}_{2}$ line list in $13.6 \mu \mathrm{~m}$ spectral region:

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#### Abstract

Following a previous work on recommended ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ line list for the $13-248 \mathrm{~cm}^{-1}$ and $390-634 \mathrm{~cm}^{-1}$ spectral regions, the present work is dedicated on new measurements between 638 and $820 \mathrm{~cm}^{-1}$. Line intensities have been measured for 18 bands: only four of them were previously reported. The measurements allowed validating predictions based on the global modeling of the line positions and intensities performed within the framework of the method of effective operators. Using the present new measurements as well as previous measurements from literature, new fittings of the line intensities for the $\Delta P=1$ series of transitions have been performed. A complete calculated line list of 200 bands belonging of the $\Delta P=1$ series of transitions is proposed as supplementary data in order to improve such spectroscopic databases as HITRAN or GEISA.


## 1. Introduction

The present work is the continuation of a previous paper [1] concerning calculation between 13 and $248 \mathrm{~cm}^{-1}$ and between 390 and $634 \mathrm{~cm}^{-1}$ with the aim to produce accurate ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ calculated line positions and intensities. The line list from Ref. [1] has been recently added in HITRAN2016 database. The calculation is based on the global modeling of the line positions and intensities within the framework of the method of effective operators [2-4] applied to various $\Delta P$ series [1,5-9] ( $P$ being polyad number defined in Section 3). In the present work new experimental spectra have been recorded and measurements of line intensities have been performed for 1020 transitions belonging to 18 vibrational bands between 638 and $820 \mathrm{~cm}^{-1}$. The positions and intensities of transitions (including those of 14 bands never measured before) are in very good agreement with acetylene line list presented in calculated acetylene database ASD-1000 [10]. This fact insures that the calculated line list in the region of the $\Delta P=1$ series is very close to the measuring data. As consequences, a set of 200 bands has been selected to generate the acetylene calculated line list of 40021 transitions between 389 and $893 \mathrm{~cm}^{-1}$. This line list is available to update atmospheric and planetary databases as HITRAN [11] and GEISA [12]

The experimental spectra recorded in MONARIS laboratory and their analysis will be presented in Section 2. The theoretical approach will be discussed in Section 3. In Section 4, the line intensity new fit for the $\Delta P=1$ series of bands will be described. Section 5 will be devoted to the description of the recommended ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ line list and comparisons of calculations with measurements and databases will be presented in Section 6 . Note that the reader is addressed to color version of this article for a complete readability of most of the figures.

## 2. New measurements in the $\mathbf{6 3 8 - 8 2 0} \mathbf{c m}^{-1}$ spectral region

The previous work [1] was dedicated to $\Delta P=0$ series, as well as the beginning of $\Delta P=$ 1 series with very weak bands recorded with absorption paths of around 150 m . To study weaker bands in the middle of the $\Delta P=1$ region $(13.6 \mu \mathrm{~m})$, such high absorption path is useless since the spectra will be totally saturated. An absorption path of 25.7 cm has been used to record three high resolution spectra with pressure of acetylene ranging from (2-10) $\times 10^{-3}$ atm allowing us to observe 4 bands already studied in literature as well as 14 bands never studied before. Experimental conditions are summarized in Table 1. For that, the Bruker IFS 125 in MONARIS has been equipped with a KBr beam splitter, and a MCT-D316 detector. A Globar source has been used. Temperature in the cell is measured with platinum probes inside the cell (accuracy of $\pm 0.1 \mathrm{~K}$ ). Pressure of natural acetylene inside the cell is measured with a $10 \mathrm{mbar}-\mathrm{full}$ scale Baratron gauge (stated accuracy of $\pm 0.25 \%$ ). A wavenumber calibration has been performed based on line position of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ transitions from HITRAN [11] as etalon. The average correcting factor $\varepsilon=\left(\sigma_{\text {ref }}-\sigma_{\text {obs }}\right) / \sigma_{\text {ref }}$ has been found equal to $-6.6(1) 10^{-7}$ (between parenthesis is 1 standard deviation 1 SD ). At $700 \mathrm{~cm}^{-1}$, it corresponds to a correction of $0.46(1) \times 10^{-3} \mathrm{~cm}^{-1}$. The accuracy of absolute line positions measurements is estimated to be equal to $0.1 \times 10^{-3} \mathrm{~cm}^{-1}$.

## (Table 1)

Figure 1 shows a portion around $705-706 \mathrm{~cm}^{-1}$, where the strongest saturated line is the $P_{e e}(10)$ transition of the $v_{5}{ }^{1}$ cold band of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$. Around $705.243 \mathrm{~cm}^{-1}$ the same transition is observed but corresponds to ${ }^{12} \mathrm{C}^{13} \mathrm{CH}_{2}$ isotopologue (marked with red stick in the upper panel of Fig. 1). Although only ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ transitions have been studied in the present work the parameters of such ${ }^{12} \mathrm{C}^{13} \mathrm{CH}_{2}$ transitions have been fitted together with nearby lines. HITRAN [11] and GEISA [12] databases contain the 5 most intense vibrational bands in the studying region coming from the Ref. $[13,14]$. All these bands were reconsidered here except the strongest $v_{5}{ }^{1}$ band which is saturated in our spectra. Note also that the two bands $\left(v_{4}+v_{5}\right)^{0}{ }_{+}-v_{4}{ }^{1}$ and $\left(v_{4}+v_{5}\right)^{0}{ }_{-}-v_{4}{ }^{1}$ present in HITRAN and GEISA from Ref. [13] correspond to only one band noted "000111-1 _ 0001010 " in the present work using vibrational assignment based on $V_{1} V_{2}$ $V_{3} V_{4} V_{5} \ell_{4} \ell_{5}$ quantum numbers (see Section 3.2 of Ref. [1] for more details).

The peak to peak signal-to-noise ratio of the spectra is almost constant with the wavenumber and is around 70. As it can be guessed in Fig. 1, a multiplicative channel spectrum is observed on all experimental spectra. This channel spectrum was modelled locally
as a background adjusted by a second order polynomial function within spectral domains around $0.04-0.1 \mathrm{~cm}^{-1}$.

## (Figure 1)

The multispectrum fitting procedure of Ref. [15] was used fixing the self-broadening coefficients at the values of Ref. [16] and using the Voigt profile. The apparatus function has been calculated with the maximum of optical path difference equal to 225 cm and the nominal value of the radius of the beam inside the interferometer equal to 1.0 mm together with the focal distance equal to 418 mm . An example of the result of the multispectrum fit is given in Fig. 2 for the $P_{e e}(24)$ transition of the $2 v_{5}{ }^{2}$ band of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ between 675.809 and $675.849 \mathrm{~cm}^{-1}$. Taking into account the signal to-noise ratio (which is close to 70), the residuals of the fit do not show any strong characteristic signature despite a kind of asymmetry in the profile that gives residuals slightly larger than the $1.5 \%$ peak to peak noise of the experimental spectra.
(Figure 2)

Absolute line intensities have been retrieved for 1220 transitions involving 18 vibrational bands. The accuracy of line intensities has been estimated to be around $5 \%$ for transitions deep enough in recorded experimental spectra (with intensities around $10^{-20}-10^{-21}$ $\mathrm{cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ ) whereas the accuracy may reach up to $10 \%$ for weaker transitions (with intensities around $10^{-22}-10^{-23} \mathrm{~cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ ). A sample of the results for the $2 v_{5}{ }^{0}-v_{5}{ }^{1}$ band is given in Table 2 (the whole set of the measurements is given in Supplementary material 1). A summary of the measurements performed in this work is presented in Table 3 for the 18 studied bands.

## 3. Theoretical approach

Measured line intensities were included in the simultaneous fit of the effective dipole moment parameters using approach describing in many previous publications (see for example [1-5]). The most important points of the approach are given below. The probability of a transition between two states $W_{b \leftarrow a}$ can be deduced from every line intensity expressed in $\mathrm{cm}^{-}$ $1 /\left(\right.$ molecule $* \mathrm{~cm}^{-2}$ ) using following conventional formula:

$$
\begin{equation*}
S_{b \leftarrow a}(T)=\frac{8 \pi^{3} g_{i} \sigma_{b \leftarrow a}}{3 h c Z_{t o t}(T)} e^{-\frac{h c E_{a}}{k_{B} T}}\left(1-e^{-\frac{h c \sigma_{b \leftarrow a}}{k_{B} T}}\right) W_{b \leftarrow a} \tag{1}
\end{equation*}
$$

where $h$ is the Planck's constant equal to $6.6260755 \times 10^{-27} \mathrm{erg}$.s ( $1 \mathrm{erg}=10^{-7} \mathrm{~J}$ ); $c$ is the vacuum velocity of light equal to $2.9979245810^{10} \mathrm{~cm} \mathrm{~s}^{-1} ; \sigma_{b \leftarrow a}$ is the transition wavenumber in $\mathrm{cm}^{-1}$; $E_{a}$ is the energy of the lower state (ground state) in $\mathrm{cm}^{-1}, k_{B}$ is the Boltzmann's constant equal to $1.380658 \times 10^{-16} \mathrm{erg} . \mathrm{K}^{-1} ; g_{i}$ is the statistical weight due to nuclear spin of the lower levels (equal $3 / 1$ for symmetry $a / s$ ), and T is the temperature of the measurements which was 296 K in our case. The total partition function $Z_{\text {tot }}$ used in this work is equal to 412.45 at 296 K [17]. The probability of a transition $W_{b \leftarrow a}$ is related to the dipole moment matrix element by the next expression ( $m$ is the projection of the angular moment on the Z axis of the space fixed system of axes):

$$
\begin{equation*}
\left.W_{b \leftarrow a}=3 \sum_{m m^{\prime}}\left|\left\langle\Psi_{b}\right| M_{Z}\right| \Psi_{a}\right\rangle\left.\right|^{2} \tag{2}
\end{equation*}
$$

In Ref. [4] the eigenfunctions of the effective Hamiltonian of acetylene molecule have been obtained in the form of expansion over products of harmonic oscillator and rigid rotator wavefunctions:
$\Psi \Psi_{N J M m_{\varepsilon}}^{\text {eff }}=\sum_{V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}} C^{V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}}\left|V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5} J m K ~ \delta\right\rangle$,
where $N$ identify the eigenstate inside of the polyad of interacting vibrational levels, $V_{i}$ are the harmonic oscillator quantum numbers, $\ell_{i}$ are the vibrational angular moments of the degenerate oscillators, $J$-angular moment quantum number, $K$ is the projection of the angular moment on
the axis of the molecule, $\varepsilon$ is the Wang combination symmetry ( $e / f$ ) and $C$ are the mixing coefficients. The sum is performed over all interacting basic functions forming one polyad which is defined by polyad number $P$. In the case of acetylene molecule, the harmonic oscillator quantum numbers of the interacting basic functions should satisfy the equation:

$$
\begin{equation*}
P=5 V_{1}+3 V_{2}+5 V_{3}+V_{4}+V_{5}=\text { const }, \tag{4}
\end{equation*}
$$

which expresses the approximate relations between normal mode frequencies in this molecule.
In order to use these functions in our calculation the dipole moment operator was transformed to the effective dipole moment operator using the same unitary transformation as the one transforming vibrational-rotational Hamiltonian to the effective:
where we denoted for simplicity the set of the harmonic oscillator quantum numbers $V_{i}$ by vector $\mathbf{V}$ and the vibrational angular moment quantum numbers $\ell_{i}$ by vector $\boldsymbol{\ell}$. The sum over these vectors assumes the sum over every quantum numbers separately, but satisfying Eq. (4). After developing effective dipole moment operator in series the calculations lead to the next expression for the probability of the transition:

The square of the function $\Phi_{\Delta J \Delta K}(J, K)$ multiplied by factor ( $2 J+1$ ) gives the Hönl-London factor in the case of isolated transitions. For $\Delta K=0, \pm 1$ this function coincide with Clebsch-Gordan coefficients and for $\Delta K= \pm 2, \pm 3$ can be found in Ref. [5,18]. The function $f_{\Delta V}^{\ell \mathcal{V}}(\mathrm{V}, \boldsymbol{\ell})$ is the square of vibrational matrix element and can be found in Ref. [5]. The combination of the Kronecker symbols appears due Wang basis functions and provides 2 when one of the basic functions has both vibrational angular moments equal zero. The Herman-Wallis type factor $F_{\Delta J\langle K}^{\Delta V}(J, K)$ describes the rotational dependence of the effective dipole moment operator. For $\Delta K= \pm 1$ it can be written as follows:
for $Q$ branch:
for $P$ and $R$ branches:

$$
\begin{aligned}
& F_{\Delta J \Delta K}^{\Delta V}(J, K)=-\frac{1}{4}\left(d_{J Q^{\Delta V}}^{\Delta \ell}-d^{\Delta V} J^{\ell \ell}\right)-\frac{1}{2}\left(b^{\Delta V} J^{\ell}+d^{\Delta V} \Delta^{\ell}\right)(2 K \Delta K+1)-d_{J Q^{\Delta V} Q^{\ell}} K^{2}+
\end{aligned}
$$

In the case $\Delta K=0$ for $P$ and $R$ branches, the Herman-Wallis type factor $F_{\Delta J \Delta K}^{4 V}(J, K)$ is:

The $m$ quantity in the Eqs. (9-10) and corresponds to $m=-J, J+1$ for $P, R$ branches respectively, and should not be confounded with the angular moment projection quantum number used in Eqs. $(2,3,6)$. The expression $F_{\Delta \Delta K}^{4 V}(J, K)$ for the $Q$ branch $(\Delta K=0)$ depends from $\ell_{4}$ and $\ell_{5}$ values and can be found in Ref. [3]. The set of the effective dipole moment
 the spectral domain defined by the value of $\Delta P$. Note, that the effective dipole moment parameters are the same for the vectors $\Delta \mathbf{V}$ and $\Delta \boldsymbol{\ell}$ differing only by signs except parameter $a^{\Delta V_{i}{ }^{\mathscr{\ell}}}$ which changes the sign when the sign of the vector $\Delta \boldsymbol{\ell}$ changes.

## 4. Line intensity fit ( $\Delta P=1$ series of transitions)

Based on the new measurements performed in this work (Section 2) and on the measurements published earlier $[1,13,14], 14$ effective dipole moment parameters have been fitted for the $\Delta P=1$ series of transitions to 1923 measured line intensities belonging to 28 different bands-(see Table 5). Most of the bands measured in this work (13 from 18) correspond to $\Delta V_{5}=1$, with $\Delta \ell_{4}=0$ and $\Delta \ell_{5}=1$, but also with $\Delta \ell_{4}=-2$ and $\Delta \ell_{5}=+1$ (3 bands), or with $\Delta \ell_{4}=-2$ and $\Delta \ell_{5}=+3(1$ band $)$, or with $\Delta \ell_{4}=+2$ and $\Delta \ell_{5}=+1(1$ band). No any new effective dipole moment parameter was required to reproduce the new measurements. The set of the fitted effective dipole moment parameters for $\Delta P=1$ is presented in Table 4 and the statistics of the fit is given in Table 5. For some transitions (weakest or blended), measurements of this work or from Ref. [1,13,14] become less accurate and can be off by more than $10 \%$ from calculations. Most of these measurements have been excluded from the fit of the parameters of Table 4 (representing 424 measurements from a total number of measurements equal to 2347). The present global model (using newly fitted parameters, see Table 4) reproduced $76 \%$ (1455 measurements) of the measurements included in the effective dipole moment parameters fit within $\pm 5 \%$, and $22 \%$ of measurements (430 measurements) within $\pm 5-10 \%$. The eigenfunctions of our global effective Hamiltonian [4] were used in the fit. The weighted dimensionless standard deviation $\chi=0.75$ and the root mean squares of the residuals $\mathrm{RMS}=4.4 \%$ were obtained in result of fit. The effective dipole moment parameters retrieved in this work are consistent with previous ones except for the $b_{J}$ parameter for $\Delta V_{4}=0, \Delta V_{5}=1$, $\Delta \ell_{4}=0$, and $\Delta \ell_{5}=1$ that converges to $-0.49(3) \times 10^{-3}$ in the present fit instead of $-0.76(5) \times 10^{-3}$ and $-0.72(5) \times 10^{-3}$ in Ref. [1] and Ref. [4] respectively (see Table 4). For bands measured in the present work, the 3 sets of effective dipole moment parameters in Table 4 lead to similar calculations able to reproduce the intensities of transitions never measured before.

> (Table 4)
(Table 5)
Examples of calculations and measurements for two newly measured bands are given in Figs. 3-4. Similar graphic comparisons are available for all measured bands in Supplementary material 2. As observed in Figs. 3-4, the differences between different calculations are negligible. Both calculations from effective parameters of Refs. [1,4] and of this work (see Table 4) are similar and reproduce the rotational dependence of $R^{2}$ for the 14 bands newly observed in this work. As observed in Figs. 3-4, the rotational dependence of measured $R^{2}$ values is quite smooth and well reproduced by all calculations (all calculations may not always
be distinguished because of the scale and of the similar calculated values). For some branches, one can clearly see that the measured rotational dependence of $R^{2}(m)$ cannot be reproduced by Herman-Wallis factors.
(Figure 3)

## (Figure 4)

## 5. Recommended acetylene $\left({ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}\right)$ line list for databases

Using the effective Hamiltonian parameters of Ref. [4] and effective dipole moment parameters (see Table 4) of $\Delta P=1$ series, the acetylene $\left({ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}\right)$ line list has been generated in the studding region with intensity cut off $10^{-28} \mathrm{~cm}^{-1} /\left(\right.$ molecule. $\mathrm{cm}^{-2}$ ). The spectral lines in this model do not have a unique vibrational labeling for all transitions belonging to a same band, but two principal contributors are given for upper and lower levels of transitions which can change inside a band. In order to have consistent vibrational labelling for a same series of transitions (with $P, Q$ and $R$ branches), an algorithm has been developed to reveal levels crossings. Indeed, as pointed out in Ref. [1], for some bands the main contributor to the eigenfunctions can change within a same series of transitions (band). When ro-vibrational levels of different series of transitions, considering as $J$ function, approach, some levels crossing can appear. As performed in Ref. [1], the vibrational assignment of the lowest $J$ transitions has been used to name the band. Inside a series of transitions, when crossings appear, the algorithm is looking for the next transition belonging to the series using such criteria as the difference of wavenumbers between transitions and the two largest contributions of the basic functions (for the upper and lower levels). Such transitions are noted with a star in the Table 6 and Supplementary material 3. The fact that the main contributor to the eigenfunctions is changing progressively (slowly or quickly depending on bands) affect line intensities in an unusual way so that Herman-Wallis factors are unable to reproduce the rotational dependence of transition dipole moment squared $R^{2}$. This problematic has been pointed out for example in Ref. [19] for $v_{1}+v_{3}+2 v_{4}{ }^{0}$ band (see Fig. 3 of Ref. [19]) and in Ref. [1] for 2 bands (see Figs. 10-11 of Ref. [1]) where the Herman-Wallis factors were not adapted to fit such unusual rotational dependence. Interesting case of band crossing is also presented in Ref. [20]. In the present work, several newly observed bands demonstrate such smooth rotational dependence of $R^{2}$ and are well predicted by previous calculations [1,4]. The effects of crossing levels can be drastic for line intensities calculation. The case of the $0003111-00030$ 10 band is discussed as an example. The line intensities and transition dipole moment squared
values in the $Q_{f e}$ branch are plotted in Figs. 5 and 6 respectively. Extract of the whole calculation (available as Supplementary material 4) with the two main contributors to the vibrational levels is given in Table 6 for the $Q_{f e}$ branch of the $0003111-0003010$ band. The first crossing appears in the $Q_{f e}$ branch at $J$ equal 17, the first contributor in the upper state becomes $000311-1$ instead of 0003111 . Then at $J$ equal 18, the first contributor in the upper state changes again to become 0003131 for the rest of the branch. Such crossings led to a change of slope for the $R^{2}$ values inside the branch (see Fig. 6). As written before, such rotational dependence within a branch cannot be correctly fitted by Herman-Wallis factors. In Fig. 5 one can observe the line intensities getting stronger after the crossing point $(J=18$, see Fig. 5). One can also notice in Fig. 5 the alternation of intensities versus $J$ with a ratio $3: 1$ for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ (due to the nuclear spins for symmetric isotopologues).
(Figure 5)
(Figure 6)
(Table 6)
From the complete calculation, 200 series of transitions forming vibrational bands have been defined and selected for databases. The whole line list contains 41021 transitions. Two cut-off procedures have been applied to select transitions. First a line intensity cut-off equal to $10^{-28} \mathrm{~cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ at 296 K has been used. Then, only bands with a sum of line intensities greater than $10^{-24} \mathrm{~cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ at 296 K have been selected. Note that the sum of line intensities has been halved when the band is affected by $\ell$-type doubling (leading to two series of $P, Q$ and $R$ branches). A summary of the present calculation for the 30 strongest bands is given in Table 7. The whole summary for the 200 bands calculated in the recommended line list is given as Supplementary material 4. Note, the recommended line list includes also most of bands proposed in Ref. [1] and already in HITRAN2016. These bands are marked by "H" letter in the Table 7 and corresponding Supplementary material 4. Because of the line intensity cut-off procedures performed in the present work, the 7 weakest bands from Ref. [1] are not included in the present line list.
(Table 7)
For all 200 bands a line list in HITRAN format has been generated and is available in Supplementary material 5 to this paper. As discussed in Section 6, the line positions from Refs. [21,22] present in HITRAN2016 have been used (when available) for the 5 strongest bands using same error code than in HITRAN2016: 4 (between $0.1 \times 10^{-3}$ and $1 \times 10^{-3} \mathrm{~cm}^{-1}$ ). For other
transitions, the calculated line positions of the present work (coming from effective Hamiltonian parameters of Ref. [4]) have been used with an error code equal to 3 (corresponding to $(1-10) \times 10^{-3} \mathrm{~cm}^{-1}$ ) for transitions with $J$ lower or equal to 40 and with an error code equal to 2 (corresponding to $(10-100) \times 10^{-3} \mathrm{~cm}^{-1}$ ) for transitions with $J$ higher than 40 (see discussion in Section 6). The set of effective dipole moment parameters from the present work (see Table 4) has been used to generate line intensities of all bands except the cold $v_{5}{ }^{1}$ band for which the set of effective dipole moment parameters from Ref. [1] has been used in order to be more consistent with measurements (see discussion in Section 6). For line intensities a code 5 (between 5 and 10\%) was used for the 18 measured bands (noted "Obs" in Table 7), whereas for a predicted band the error code 4 ( $\geq 10 \%$ and $<20 \%$ ) was chosen allowing to distinguish easily predicted and measured bands. Broadening coefficients (self and air), temperature dependence of air-broadening coefficients, air-shifting coefficients and associated error codes have been added following recommendations of Ref. [23] included in HITRAN2004 edition [24]. However, the error codes of air- and self-broadening coefficients have been degraded from 6 (between 2 and $5 \%$ ) to 4 (between $10-20 \%$ ) when $J \geq 35$ since a constant estimated value is used. Let us mention that in HITRAN 2016, error codes for broadening coefficients are all fixed to 6 even for transitions with $J$ greater than 35 .

Note that the vibrational labeling used in the present work has been described in Section 3.2 of Ref. [1]. We urge spectroscopic databases to note the fact that using $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{\text {tot }}$ quantum numbers instead of $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} l_{5}$ quantum numbers will lead to various transitions with identical assignments. The FORTRAN format A15 for vibrational assignment should change to ( $1 \mathrm{X}, 3 \mathrm{I} 1,4 \mathrm{I} 2, \mathrm{~A} 1, \mathrm{I} 1, \mathrm{~A} 1$ ) respectively for $V_{1}, V_{2}, V_{3}, V_{4}, V_{5}, \ell_{4}, \ell_{5}$, quantum numbers, the $u / g$ symmetry, a ranking number (noted $r$ in HITRAN, see Table 3 of Ref. [24]), and the $+/$ - symmetry. $V_{4}$ and $V_{5}$ being the lowest energy vibrational modes, two digits should be reserved for these modes for the possibility to have $V$ values greater than 9 . The ranking number is not used in the present line list and should not be useful anymore.

A sample of synthetic spectra using either HITRAN2016 or the present recommended line list are compared to experimental spectrum 3 in Fig. 7 between 703 and $706 \mathrm{~cm}^{-1}$. One can notice the many transitions of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ missing in HITRAN2016 [11] and GEISA2015 [12] but present in our line list. One can also observe some missing absorption features due to ${ }^{12} \mathrm{C}^{13} \mathrm{CH}_{2}$ isotopologue noted by symbols in Fig. 7 and assigned in Ref. [25].
(Figure 7)

## 6. Comparisons with spectroscopic databases

Since our aim is to update line positions and intensities already present in atmospheric databases and upgrade the line list with many hot bands, comparisons have been performed with HITRAN2016 edition. HITRAN2016 [11] or GEISA2015 [12] have same data for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ line positions and intensities of strong bands from Refs. [13,14], except for weak bands from Ref. [1] included in HITRAN2016 edition [11]. Calculations performed in Ref. [1] for the 29 bands in $\Delta P=1$ spectral region, and in the present work are based on same formalism [4] so no comparison is performed. Note that none of the bands measured in the present work is in common with the bands studied in Ref. [1]. Comparisons with EXOMOL database for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ [26] are also performed in term of line positions and intensities.

In the $\Delta P=1$ absorption region, line intensities of the 5 strongest bands at room temperature present in HITRAN are coming from Refs. [13,14]. Herman-Wallis factors and vibrational transition dipole moments squared from Refs. [13,14] have been used to generate calculated line intensities for updating HITRAN2004 edition [24]. Extrapolations for high $J$ values in HITRAN were performed using fixed $R^{2}$ values equal to the calculated one for the last measured transition in the branch. The present global calculation is consistent with HITRAN line intensities and improves extrapolations performed in HITRAN with fixed transition dipole moment squared values. Examples for the $v_{5}{ }^{1}$ and $2 v_{5}{ }^{0}-v_{5}{ }^{1}$ bands are given in Figs. 8-9 respectively. Figure 9 shows the very good consistency of present measurements and those from Ref. [13]. No measurement has been performed in this work for the strong $v_{5}{ }^{1}$ band, but calculations and measurements from literature plotted in Fig. 8 shows a slight discrepancy (up to $4 \%$ for highest $J$ values) between measurements and calculations in the $R$-branch, especially with parameters of the present work (see Table 4). The $R^{2}$ values deduced from EXOMOL line intensities are also given in Figs. 8 and 9. One can notice that EXOMOL line intensities worse reproduce measurements showing inaccurate rotational dependences especially for $P$ and $R$ branches. The whole set of graphic comparisons is available in Supplementary material 2.
(Figure 8)
(Figure 9)
Line positions of the 5 strongest bands from HITRAN2016 coming from calculation of Refs. [21,22] (believed to be a reference in the $\Delta P=1$ region for line positions) were compared with ASD-1000 calculated line positions [10] and with present measurements. Comparisons plotted in Fig. 10 versus line intensity show that for the weakest transitions the differences between HITRAN and ASD-1000 calculation can reach $\pm 0.03 \mathrm{~cm}^{-1}$ while present measurements and HITRAN2016 positions are in very good agreement. In order to better
understand the situation, the differences have been plotted versus $m$ for the $0000101-00000$ 00 and $0001111-0001010$ bands in Fig. 11 and 12 respectively, including also comparisons with EXOMOL line positions [26]. One can clearly observe in these figures increasing of deviations of ASD-1000 and EXOMOL line positions from HITRAN values for large rotational quantum numbers $J$. Moreover, while for the $0000101-0000000$ band (Fig.11) the differences increase on average in the same way for ASD-1000 and EXOMOL, for the 000111 $1-0001010$ band the trend is opposite (Fig.12). In term of line positions, the global model [4] does not allow to reach the accuracy of more simple models as those from Refs. [21,22] (used in HITRAN for the 5 strongest bands). These models consider several resonance interactions between ro-vibrational states and can well describe the rotational dependence of the energy of several interacting states. The models used in Refs. [21,22] allowed to reach estimated accuracy equal to $\pm 0.0001 \mathrm{~cm}^{-1}$ [21]. As consequences the line positions in HITRAN have been kept in our recommended line list for the 5 strongest bands as discussed in Section 5.
(Figure 10)
(Figure 11)
(Figure 12)

## 6. Conclusion

Recent measurements from Ref. [1] and from the present work allowed to demonstrate the predictive capabilities of global calculation [4] for $\Delta P=1$ series of bands. This calculation has been used to generate a complete line list in HITRAN format for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ isotopologue between 389 and $893 \mathrm{~cm}^{-1}$. The cut-off procedures used to select the most intense bands will allow to model acetylene absorption features with better accuracy for atmospheric temperature spectra, but also to model higher temperature spectra since the recommended line list contains many hot bands. The present recommended line list can be considered as a revised selection of bands from the high-temperature acetylene spectroscopic databank (ASD-1000) [10] in the $\Delta P$ $=1$ spectral region, adapted for spectroscopic databases such as HITRAN or GEISA. By performing measurements in higher $\Delta P$ spectral regions for weaker bands never measured, the validation of the predictive capabilities of global calculation for higher $\Delta P$ absorption regions is planned to improve higher spectral regions in spectroscopic databases.

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Fig. 1. Spectral range around $705-706 \mathrm{~cm}^{-1}$. Upper panel is a stick plot of HITRAN 2016 [11] for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ (black sticks) and ${ }^{12} \mathrm{C}^{13} \mathrm{CH}_{2}$ (red sticks). The line intensities (in log scale) are in $\mathrm{cm}^{-1}\left(\right.$ molecule. $\mathrm{cm}^{-2}$ ). In the lower panel the 3 experimental spectra are plotted (see experimental conditions in Table 1).


Fig. 2. Simultaneous fit of the $P_{e e}(24)$ transition of the $0000202-0000101$ band $\left(2 v_{5}{ }^{2}-v_{5}{ }^{1}\right)$ between 675.809 and $675.849 \mathrm{~cm}^{-1}$. In the lower panel are plotted the measured spectra \#1-3 (in black) and the respective simulated spectra (red for spectrum \#1, blue for \# 2, green for \#3) using multispectrum fitting procedure. In the upper panel are given the residuals of the fit where the same set of colors been used.


Fig. 3. Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}{ }^{-}$ branches of the $000212-1-0002020$ band plotted versus $m$ ( $m=-J, J, J+1$ for $P, Q, R$ branch respectively). Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas blue triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$ branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4).


Fig. 4. Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the $0002101-0002000$ band plotted versus $m(m=-J, J, J+1$ for $P, Q, R$ branch respectively) Red triangles are measurements from this work for the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches (open triangles for $Q$-branch and solid ones for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4).


Fig. 5. Calculated line intensities (in $\mathrm{cm}^{-1} /\left(\right.$ molecule. $\left.^{-2} \mathrm{~cm}^{-2}\right)$ at 296 K ) of transitions belonging to the $Q_{f e}$ branch of the 0003111-00030 10 band plotted versus $J$.


Fig. 6. Calculated transition dipole moment squared of transitions belonging to the $Q_{f e}$ branch of the $0003111-0003010$ band plotted versus $J$.

Fig.7. Synthetic spectra between 703 and $706 \mathrm{~cm}^{-1}$ using HITRAN 2016 or line list of this work. On the top in the first panel are plotted the transitions of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ from HITRAN2016 (red stick) and from the recommended line list of this work (black stick). In the main panel, experimental spectrum recorded at 9.3 matm of natural $\mathrm{C}_{2} \mathrm{H}_{2}$ is plotted in black. Synthetic spectra are plotted in blue (HITRAN 2016) and red (recommended line list + HITRAN2016 for ${ }^{12} \mathrm{C}^{13} \mathrm{C}_{2} \mathrm{H}_{2}$ transitions). The star symbol corresponds to the only ${ }^{12} \mathrm{C}^{13} \mathrm{C}_{2} \mathrm{H}_{2}$ transition present in HITRAN 2016 in the plotted spectral range. The + symbols correspond to missing ${ }^{12} \mathrm{C}^{13} \mathrm{C}_{2} \mathrm{H}_{2}$ transitions assigned from the work of Di Lonardo et al. [25].


Fig. 8. Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the $0000101-0000000$ band $\left(v_{5}{ }^{1}\right)$ plotted versus $m(m=-J, J, J+1$ for $P, Q, R$ branch respectively). Black line is from HITRAN [11]. Black triangles are measurements from Ref. [14] (open for $Q$-branch and solid for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Fig. 9. Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the $0000200-0000101$ band $\left(2 v_{5}{ }^{0}-v_{5}{ }^{1}\right.$ ) plotted versus $m(m=-J, J, J+1$ for $P, Q, R$ branch respectively). Black line is from HITRAN [11]. Black and red triangles are measurements from Ref. [13] and the present work respectively (open for $Q$-branch and solid for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Fig. 10. Line positions differences (HITRAN - Calculation (this work)) in red circles and (HITRAN measurements (this work)) in blue triangles plotted versus line intensities (in $\mathrm{cm}^{-1}\left(\right.$ molecule. $\mathrm{cm}^{-2}$ ) at 296 K ) in a log-scale.


Fig. 11. Line positions differences plotted versus $m$ ( $m=-J, J, J+1$ for $P, Q, R$ branch respectively) for the $0000101-0000000$ band $\left(v_{5}{ }^{1}\right)$. (HITRAN - Calculation (this work)) and (HITRAN - EXOMOL) are plotted in black and red symbols respectively. Solid up-triangles correspond to $P_{\text {ee }}$ and $R_{\text {ee- }}$-branches, open up-triangles for $Q_{\mathrm{fe}}$-branch.


Fig. 12. Line positions differences plotted versus $m(m=-J, J, J+1$ for $P, Q, R$ branch respectively) for the $0001111-0001010$ band. (HITRAN - Calculation (this work)) and (HITRAN - EXOMOL) are plotted in black and red symbols respectively. Solid up-triangles correspond to $P_{\mathrm{ee}}$ and $R_{\mathrm{ee}}$-branches, solid down-triangles to $P_{\mathrm{ff}}$ and $R_{\mathrm{ff}}$-branches, and open up- and down-triangles to $Q_{\mathrm{fe}}{ }^{-}$and $Q_{\mathrm{ef}}$-branches respectively.

Table 1: Experimental conditions and characteristics of the recorded spectra.

| Commercial sample (Air Liquide Alphagaz) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Natural $\mathrm{C}_{2} \mathrm{H}_{2}$ <br> Stated purity |  | $\begin{aligned} & 97.760 \% \text { of }{ }^{12} \mathrm{C}_{2} \mathrm{H}_{2} \\ & 99.55 \% \end{aligned}$ |  |  |
|  |  |  |
| Total absorption path |  |  |  | 25.7 (1) cm |  |  |
| Collimator focal length |  | 418 mm |  |  |
| Radius of the iris |  | 1.0 mm |  |  |
| Spectrum number | Total pressure (matm) | Temperature (K) | Brukerresolution ${ }^{\text {a }}$ $\left(\mathrm{cm}^{-1}\right)$ | Number of co-added scans |
| 1 | 2.396 | 294.0 | 0.004 | 598 |
| 2 | 4.916 | 294.5 | 0.004 | 600 |
| 3 | 9.319 | 294.3 | 0.004 | 600 |

[^0]Table 2. Measurements of line positions ( $\sigma_{\mathrm{Obs}}$ in $\mathrm{cm}^{-1}$ ) and intensities ( $S_{\mathrm{Obs}}$ in $\mathrm{cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ at 296 K in natural abundances) for the $2 v_{5}{ }^{0}-v_{5}{ }^{1}$ band.



Note: For assignment, the branch type is first given, then the e/f Wang symmetry of the upper and lower state, and finally the rotational quantum number $J$ of the lower state. Then are reported the vibrational assignment for the upper and lower states ( $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}$ ). Measured line positions ( $\sigma_{\text {Meas }}$ ) and energies of the lower state ( $E_{\text {low }}$ ) are given in $\mathrm{cm}^{-1}$. The transition dipole moments squared ( $R^{2}$ Obs) are given in debye ${ }^{2}$.

Table 3. Summary of measurements performed in this work.

|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Note: The band notation refers to the upper and lower vibrational state, see note of Table 2 . The line positions are given in $\mathrm{cm}^{-1}$ and the line intensities are in $\mathrm{cm}^{-1} /\left(\right.$ molecule. $\left.\mathrm{cm}^{-2}\right)$ at 296 K in natural abundance. The star marks the bands already measured in Ref. [13] and present in HITRAN and GEISA databases.
Table 4. Effective dipole moment parameters for the $\Delta P=1$ series of transitions.

| Parameter ${ }^{\text {a }}$ | $\Delta V_{1}$ | $\Delta V_{2}$ | $\Delta V_{3}$ | $\Delta V_{4}$ | $\Delta V_{5}$ | $\Delta \ell_{4}$ | $\Delta \ell_{5}$ | This work | Ref. [1] | Ref. [4] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M | 0 | 0 | 0 | 0 | 1 | 0 | 1 | -0.1583(2) | -0.1578(2) | -0.1579(2) |
| $\kappa_{5}$ | 0 | 0 | 0 | 0 | 1 | 0 | 1 | -0.0131(8) | -0.017(2) | $0.013(2)$ |
| $b_{J}$ | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $-0.49(3) \times 10^{-3}$ | $-0.76(5) \times 10^{-3}$ | $-0.72(5) \times 10^{-3}$ |
| $d_{J}$ | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $0.51(2) \times 10^{-4}$ | $0.45(3) \times 10^{-4}$ | $0.47(3) \times 10^{-4}$ |
| M | 0 | 0 | 0 | 2 | -1 | 2 | -1 | $-0.3361(4) \times 10^{-2}$ | $-0.3343(5) \times 10^{-2}$ |  |
| $\kappa_{4}$ | 0 | 0 | 0 | 2 | -1 | 2 | -1 | 0.028(4) | 0.020 (3) |  |
| $b_{J}$ | 0 | 0 | 0 | 2 | -1 | 2 | -1 | $-0.211(8) \times 10^{-2}$ | $-0.244(9) \times 10^{-2}$ |  |
| $d_{J}$ | 0 | 0 | 0 | 2 | -1 | 2 | -1 | $-0.66(5) \times 10^{-4}$ | $-0.63(6) \times 10^{-4}$ |  |
| M | 0 | 0 | 0 | 2 | -1 | 0 | 1 | $0.669(2) \times 10^{-2}$ | $0.665(2) \times 10^{-2}$ |  |
| $\kappa_{4}$ | 0 | 0 | 0 | 2 | -1 | 0 | 1 | $0.060(2)$ | $0.059(2)$ |  |
| $a_{5}$ | 0 | 0 | 0 | 2 | -1 | 0 | 1 | 0.030(2) | 0.026(2) |  |
| $b_{J}$ | 0 | 0 | 0 | 2 | -1 | 0 | 1 | $-0.109(7) \times 10^{-2}$ | $-0.119(8) \times 10^{-2}$ |  |
| $d_{J}$ | 0 | 0 | 0 | 2 | -1 | 0 | 1 | $-0.55(4) \times 10^{-4}$ | $-0.61(4) \times 10^{-4}$ |  |
| M | 0 | 0 | 0 | 2 | -1 | -2 | 3 | $-0.36(3) \times 10^{-3}$ | $-0.30(3) \times 10^{-3}$ |  |

[^1]${ }^{\mathrm{b}}$ Confidence intervals ( 1 SD , in unit of the last quoted digit) are given between parentheses.

Table 5. Statistics of the fitted bands of the $\Delta P=1$ series.

| Measured bands | Spectral range <br> in cm | $N^{a}$ | $J_{\text {max }}{ }^{b}$$\mathrm{MR}^{c}$ <br> in \%$\mathrm{RMS}^{d}$ <br> in \% |
| :--- | :---: | :---: | :---: | :---: | :---: |

## Band measured in Ref. [14]

0000101 - $0000000644.5-820.2 \quad 7738$-1.10 0.01

## Bands measured in Ref. [13]

| 00002 | 0 | $0-00001$ | 0 | 1 | $661.0-800.2$ | 64 | 32 | -1.13 | 3.79 |
| :--- | :--- | :--- | :--- | :--- | :--- | ---: | :--- | :--- | :--- |
| 00002 | 0 | $2-00001$ | 0 | 1 | $674.7-794.8$ | 79 | 30 | -1.01 | 2.67 |
| 00011 | $1-1-00010$ | 1 | 0 | $655.8-787.5$ | 109 | 31 | -0.13 | 3.31 |  |
| 00011 | 1 | $1-00010$ | 1 | 0 | $669.4-798.8$ | 98 | 28 | -0.15 | 4.19 |

## Bands measured in Ref. [1]

| 00020 | 20 | 0 | -00001 | 0 | 1 | $434.6-564.0$ | 107 | 33 | -1.08 | 5.82 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: | ---: |
| 00020 | 0 | 0 | -00001 | 0 | 1 | $429.6-586.8$ | 84 | 34 | 1.77 | 4.72 |
| 00030 | 1 | 0 | -00011 | 1 | 1 | $449.7-583.9$ | 77 | 27 | -1.08 | 4.56 |
| 00030 | 1 | 0 | -00011 | $1-1$ | $478.9-580.6$ | 37 | 22 | 1.41 | 6.29 |  |
| 00030 | 3 | 0 | -00011 | 1 | 1 | $468.3-559.8$ | 40 | 25 | 0.85 | 5.54 |
| 00021 | 0 | $1-00002$ | 0 | 0 | $457.4-568.3$ | 33 | 23 | 0.93 | 5.80 |  |
| 00021 | 0 | $1-00002$ | 0 | 2 | $458.6-527.2$ | 52 | 25 | -0.11 | 3.45 |  |
| 00021 | 2 | $1-00002$ | 0 | 2 | $456.8-555.6$ | 20 | 21 | 4.73 | 8.88 |  |
| 00021 | 2 | $1-00002$ | 0 | 0 | $555.7-565.6$ | 2 | 21 | 6.89 | 6.92 |  |

## Bands measured in this work

| 00002 | 0 | 0 | -00001 | 0 | 1 | $643.0-804.9$ | 72 | 34 | -0.13 | 2.69 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: | ---: |
| 00002 | 0 | $2-00001$ | 0 | 1 | $651.0-819.6$ | 87 | 37 | 0.48 | 3.33 |  |
| 00011 | $1-1$ | -00010 | 1 | 0 | $638.3-806.0$ | 119 | 35 | 0.27 | 3.54 |  |
| 00011 | 1 | 1 | -00010 | 1 | 0 | $657.5-812.6$ | 85 | 34 | -0.51 | 3.74 |
| 00003 | 0 | 1 | -00002 | 0 | 0 | $660.2-784.7$ | 47 | 29 | 1.49 | 3.99 |
| 00003 | 0 | 1 | -00002 | 0 | 2 | $649.4-779.4$ | 64 | 29 | -1.20 | 4.48 |
| 00003 | 0 | $3-00002$ | 0 | 2 | $675.3-784.7$ | 40 | 22 | -0.95 | 3.59 |  |
| 00012 | 1 | 0 | -00011 | 1 | 1 | $654.5-765.9$ | 46 | 23 | -0.96 | 4.53 |
| 00012 | 1 | 0 | -00011 | $1-1$ | $638.3-795.6$ | 65 | 34 | 1.92 | 4.99 |  |
| 00012 | 1 | $2-00011$ | 1 | 1 | $673.8-795.8$ | 50 | 26 | -0.15 | 4.46 |  |
| $00012-1$ | $2-00011$ | 1 | 1 | $668.9-779.7$ | 54 | 26 | 2.27 | 4.29 |  |  |
| $00012-1$ | 2 | -00011 | $1-1$ | $652.3-805.3$ | 48 | 33 | 3.29 | 6.72 |  |  |
| 00021 | 0 | 1 | -00020 | 0 | 0 | $674.3-774.0$ | 28 | 23 | 3.49 | 4.72 |
| 00021 | 0 | 1 | -00020 | 2 | 0 | $676.3-802.1$ | 28 | 28 | 6.32 | 8.16 |
| 00021 | 2 | 1 | -00020 | 0 | 0 | $662.1-810.6$ | 22 | 33 | 0.95 | 6.06 |
| 00021 | 2 | $1-00020$ | 2 | 0 | $674.0-809.8$ | 64 | 30 | 0.30 | 3.86 |  |
| 00021 | $2-1-00020$ | 0 | 0 | $673.2-754.7$ | 26 | 27 | -1.42 | 3.80 |  |  |
| 00021 | $2-1-00020$ | 2 | 0 | $649.5-794.5$ | 99 | 32 | -0.19 | 3.72 |  |  |

[^2]Table 6. Calculation based on parameter of Table 4 (this work) for the $Q_{f e}$ and $R_{e e}$ branches of the $0003111-0003010$ band. The
first column corresponds to the vibrational labeling used for a whole series of transition. Then the type of branch, the Wang symmetry
e/f of the upper and lower state, $J$ of lower state, calculated line positions in $\mathrm{cm}^{-1}$, calculated line intensities at 296 K for natural
abundances in $\mathrm{cm}^{-1} /\left(\right.$ molecule.cm ${ }^{-2}$ ), the lower state energy $\mathrm{cm}^{-1}$, then, for upper and lower levels, the two main contributors to the
eigenfunctions (with percentages, see text). A star at the beginning of the line means that the main contributors to the eigenfunctions
are different from the vibrational labeling used for a whole series of transition.

| Vibrational labeling of the band | B | r $J$ |  | Position | Intensity | $E_{\text {Low }}$ | Upper main contributors |  |  |  | Lower main contributors |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | First | per | Second | p | First | per | Second |  |  |



Table 7. Summary of calculation for the 30 first strongest bands in the $\Delta P=1$ series of bands. The first column corresponds to the vibrational labeling used for series of transitions (bands). $N$ is the total number of transitions belonging to band. Minimum and maximum wavenumbers of calculated transitions belonging to the band are given in $\mathrm{cm}^{-1}, S u m_{-} S$ is the sum of calculated line intensities (see text) in $\mathrm{cm}^{-1} /\left(\right.$ molecule. $\mathrm{cm}^{-2}$ ) at 296K for natural abundances. Smin and Smax are respectively the minimum and maximum calculated line intensities in the band. Minimum and maximum values of $J$ in the band are given.

| Vibrational labeling of the band |  |  | $\begin{gathered} N \\ \hline 195 \end{gathered}$ | $\begin{aligned} & \text { Wavenumbers } \\ & \min -\max \\ & \hline 577.0-881.5 \end{aligned}$ | Sum_S$2.46 \mathrm{E}-17$ | Smin <br> 1.36E-28 | Smax$1.18 \mathrm{E}-18$ | $\begin{gathered} J \\ \min \max \end{gathered}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H | H 0000101 | 0000000 |  |  |  |  |  | 0 | 65 | Obs |
| H | 0000202 | 0000101 | 343 | 589.8-887.6 | $6.94 \mathrm{E}-19$ | 1.32E-28 | 3.59E-20 | 1 | 61 | Obs |
| H | 000020 | 0000101 | 176 | 583.5-869.8 | $6.89 \mathrm{E}-19$ | 1.40E-28 | 3.01E-20 | 1 | 62 | Obs |
| H | 0001111 | 0001010 | 345 | 588.7-892.7 | $6.33 \mathrm{E}-19$ | $1.09 \mathrm{E}-28$ | $3.18 \mathrm{E}-20$ | 1 | 62 | Obs |
| H | 00011 1-1 | 0001010 | 355 | 579.9-866.0 | $6.23 \mathrm{E}-19$ | $1.08 \mathrm{E}-28$ | $3.11 \mathrm{E}-20$ | 1 | 61 | Obs |
|  | 0000301 | 0000200 | 167 | 585.7-853.8 | 4.07E-20 | $1.07 \mathrm{E}-28$ | $1.87 \mathrm{E}-21$ | 0 | 57 | s |
| * | 0002101 | 0002000 | 149 | 604.2-846.0 | 3.62E-20 | $1.13 \mathrm{E}-28$ | $1.80 \mathrm{E}-21$ | 0 | 51 | Obs |
|  | 0001212 | 0001111 | 315 | 603.8-871.6 | $3.49 \mathrm{E}-20$ | $1.00 \mathrm{E}-28$ | $1.63 \mathrm{E}-21$ | 2 | 58 | Obs |
|  | 0000303 | 0000202 | 313 | 598.9-868.5 | $2.89 \mathrm{E}-20$ | 1.02E-28 | $1.36 \mathrm{E}-21$ | 2 | 57 | Obs |
| * | 0001210 | 00011 1-1 | 319 | 587.1-854.9 | $2.79 \mathrm{E}-20$ | $1.01 \mathrm{E}-28$ | $2.54 \mathrm{E}-21$ | 0 | 58 | Obs |
| * | 00012-1 2 | 00011 1-1 | 302 | 601.6-862.4 | 2.69E-20 | $1.18 \mathrm{E}-28$ | $2.54 \mathrm{E}-21$ | 0 | 57 | Ob |
| * | 0002121 | 0002020 | 282 | 627.2-881.0 | 2.58E-20 | $1.01 \mathrm{E}-28$ | $1.40 \mathrm{E}-21$ | 2 | 54 | Obs |
| * | 00021 2-1 | 0002020 | 321 | 582.9-853.7 | $2.26 \mathrm{E}-20$ | 1.10E-28 | 1.02E-21 | 2 | 57 | Obs |
|  | 00021 2-1 | 0002000 | 126 | 630.2-798.0 | 1.49E-20 | $1.16 \mathrm{E}-28$ | $1.20 \mathrm{E}-21$ | 0 | 53 | Obs |
| * | 0002101 | 0002020 | 310 | 612.6-879.5 | 1.27E-20 | $1.25 \mathrm{E}-28$ | $1.46 \mathrm{E}-21$ | 2 | 57 | Obs |
| * | 0002121 | 0002000 | 162 | 600.1-865.0 | $1.05 \mathrm{E}-20$ | $1.06 \mathrm{E}-28$ | $4.70 \mathrm{E}-22$ | 2 | 57 | Obs |
|  | 0000301 | 0000202 | 298 | 590.2-854.8 | 9.41E-21 | 1.02E-28 | 5.07E-22 | 2 | 56 | Obs |
| * | 00012-1 2 | 0001111 | 307 | 594.9-859.1 | 8.56E-21 | $1.25 \mathrm{E}-28$ | 3.92E-22 | 2 | 57 | Obs |
| * | 0001210 | 0001111 | 297 | 578.7-843.6 | 8.46E-21 | $1.01 \mathrm{E}-28$ | $4.44 \mathrm{E}-22$ | 2 | 53 | Obs |
|  | 0100101 | 0100000 | 151 | 608.3-847.6 | 1.69E-21 | $1.15 \mathrm{E}-28$ | 8.11E-23 | 0 | 51 |  |
| * | 0002200 | 0002101 | 143 | 620.0-838.9 | 1.65E-21 | $1.19 \mathrm{E}-28$ | $8.28 \mathrm{E}-23$ | 1 | 51 |  |
| * | 0002222 | 0002121 | 277 | 616.6-854.1 | 1.64E-21 | $1.34 \mathrm{E}-28$ | $9.87 \mathrm{E}-23$ | 3 | 51 |  |
|  | 00022 2-2 | 00021 2-1 | 297 | 590.6-839.7 | 1.64E-21 | $1.08 \mathrm{E}-28$ | $8.05 \mathrm{E}-23$ | 1 | 52 |  |
| * | 0002202 | 0002101 | 284 | 621.7-854.5 | 1.45E-21 | $1.05 \mathrm{E}-28$ | $7.59 \mathrm{E}-23$ | 1 | 52 |  |
|  | 0001313 | 0001212 | 278 | 619.9-855.5 | 1.42E-21 | $1.11 \mathrm{E}-28$ | 8.36E-23 | 3 | 52 |  |
| * | 0001311 | 0001210 | 282 | 598.9-855.5 | 1.35E-21 | $1.07 \mathrm{E}-28$ | $7.41 \mathrm{E}-23$ | 1 | 52 |  |
| * | 00031 1-1 | 0003010 | 254 | 598.1-840.2 | 1.27E-21 | 1.05E-28 | 1.02E-22 | 1 | 51 |  |
| * | 00013-1 3 | 00012-1 2 | 280 | 609.4-844.8 | 1.27E-21 | 1.12E-28 | $6.78 \mathrm{E}-23$ | 1 | 51 |  |
|  | 0000400 | 0000301 | 146 | 597.2-837.8 | 1.18E-21 | $1.18 \mathrm{E}-28$ | $5.00 \mathrm{E}-23$ | 1 | 52 |  |
| * | 00031 3-1 - | 0003030 | 283 | 590.6-837.0 | $1.18 \mathrm{E}-21$ | $1.05 \mathrm{E}-28$ | $5.09 \mathrm{E}-23$ | 3 | 52 |  |

Note: The vibrational labeling for upper and lower state corresponds to $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}$. A star at the beginning of the line means that the main contributor to the eigenfunctions of the upper or lower states (or both) is changed within the series of transitions (bands). Letter H shows bands present in HITRAN2016 [11]. In the last column "Obs" means that the band was measured in this work or reported in literature (see Section 2).

## Declaration of interests

— The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

CThe authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

David Jacquemart: Visualization, Analysis, Investigation, Methodology, Data Curation, Writing - Original Draft. Pascale Soulard: Investigation. Oleg Lyulin: Methodology, Software, Validation, Formal analysis, Data Curation, Writing - Original Draft.

## Supplementary material 2:

Comparisons of $R^{2}$ experimental values with $R^{2}$ values from HITRAN/EXOMOL/Global model [1,4,present work].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 000010 $1-0000000$ band $\left(v_{5}{ }^{1}\right)$ plotted versus $m$. Black line is from HITRAN [11]. Black triangles are measurements from Ref. [14] (open for $Q$-branch and solid for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00011 $1 \mathbf{1 - 0 0 0 1 0} 1 \mathbf{0}$ band plotted versus $m$ (noted $\left.\left(v_{4}+v_{5}\right)^{2}-v_{4}{ }^{1}\right)$ in Ref. [13] as well as in HITRAN and GEISA databases). Black line is from HITRAN [11]. Black and red triangles are measurements from Ref. [13] and the present work respectively (open for $Q$-branch and solid for $P$-and $R$-branches). Upside triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas downside triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4).


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 000020 $\mathbf{0}-0000101$ band $\left(2 v_{5}{ }^{0}-v_{5}{ }^{1}\right)$ plotted versus $m$. Black line is from HITRAN [11]. Black and red triangles are measurements from Ref. [13] and the present work respectively (open for $Q$-branch and solid for $P$ and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00002 $02-0000101$ band plotted versus $m$ (noted $2 v_{5}{ }^{2}-v_{5}{ }^{1}$ in Ref. [13] as well as in HITRAN and GEISA databases). Black line is from HITRAN [11]. Black and red triangles are measurements from Ref. [13] and the present work respectively (open for $Q$-branch and solid for $P$-and $R$-branches). Upside triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas downside triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00011 1-1 - 0001010 band plotted versus $m$ (noted $\left.\left(v_{4}+v_{5}\right)^{0}{ }_{+}-v_{4}{ }^{1}\right)$ and $\left(v_{4}+v_{5}\right)^{0}{ }_{-}-v_{4}{ }^{1}$ in Ref. [13] as well as in HITRAN and GEISA databases). Black line is from HITRAN [11]. Black and red triangles are measurements from Ref. [Jac2001] and the present work respectively (open for $Q$-branch and solid for $P$ and $R$-branches). Upside triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas downside triangles are for $P_{f f}$, $R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $000212-1-0002020$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 000030 $1-0000200$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$ branch and solid for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $0000301-0000202$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $0000303-0000202$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}$ and $R_{e e}$-branches whereas blue triangles are for $P_{f f}$ and $R_{f f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Not Found in EXOMOL.


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 000210 $\mathbf{1 - 0 0 0 2 0} 000$ band plotted versus $m$. Red triangles are measurements from this work for the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches (open triangles for $Q$-branch and solid ones for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00021 0 1-00020 20 band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 000212 $\mathbf{1 - 0 0 0 2 0} 0 \mathbf{0}$ band plotted versus $m$. Red triangles are measurements from this work for the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches (open triangles for $Q$-branch and solid ones for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Not Found in EXOMOL.


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $0002121-0002020$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas blue triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Not Found in EXOMOL.

I checked by plotting synthetic spectra around the R20f quite visible in our exp spectra at $783.8717 \mathrm{~cm}^{-1}$, the most intense below (in blue EXOMOL, green HITRAN 2016, red ASD).



Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches of the 00021 2-$\mathbf{1}-\mathbf{0 0 0 2 0} \mathbf{0} \mathbf{0}$ band plotted versus $m$. Red triangles are measurements from this work for the $P_{e e}, R_{e e}$ and $Q_{f e}$-branches (open triangles for $Q$-branch and solid ones for $P$-and $R$-branches). Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].
Line P27e at 641.4486 has strange R2 value around 0.06 D2. And indeed the EXOMOL synthetic spectrum (in blue) presents a line that is not observed.



Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $0001210-00011 \mathbf{1 - 1}$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00012-1 2-00011 1-1 band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00012 $12-0001111$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas blue triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Not Found in EXOMOL.

Below at $750.378 \mathrm{~cm}-1$, the Rff7 of this band observed in exp spectrum (black line) is reproduced by our line list (ASD in red), but not by HITRAN or EXOMOL. Around 750.56, two lines are also missing in EXOMOL, the Ree 8 and Rff8 of 0000303 _u 0000202 g band also missing in EXOMOL. The transitions with stars correspond to ${ }^{12} \mathrm{C}^{13} \mathrm{H}_{2}$ transitions.



Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the $0001210-0001111$ band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas blue triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


Transition dipole moment squared of transitions belonging to the $P_{e e}, R_{e e}, P_{f f}, R_{f f}, Q_{e f}$ and $Q_{f e}$-branches of the 00012-1 2-00011 11 band plotted versus $m$. Triangles are measurements from the present work (open for $Q$-branch and solid for $P$-and $R$-branches). Red triangles are for $P_{e e}, R_{e e}$ and $Q_{f e}$-branches whereas black triangles are for $P_{f f}, R_{f f}$ and $Q_{e f}$-branches. Calculations obtained using parameters of effective dipole moment are in blue line when using parameters from Ref. [4], in green line when using parameters from Ref. [1], and in red line when using parameters from this work (see Table 4). Plotted in blue symbols (open triangles for $Q$ branch and solid triangles for $P$ and $R$ branches) are transition dipole moment squared from EXOMOL [26].


[^0]:    ${ }^{a}$ Bruker-resolution $=0.9 / \Delta_{\max } . \Delta_{\max }$ being the maximum optical path difference.

[^1]:    ${ }^{\text {a }}$ Parameters $M$ are given in Debye while the other parameters are dimensionless.

[^2]:    Note: The band notation refers to the upper and lower vibrational states ( $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}$ ).
    ${ }^{a}$ Number of the fitted line intensities for a given band.
    ${ }^{b}$ Maximum value of the angular momentum quantum number for a given band.
    ${ }^{c}$ Mean residuals.
    ${ }^{d}$ Root mean squares of the residuals.

