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Q. Bizot, O. Politano, A. Nepapushev, S. Vadchenko, A. Rogachev, et al.. Reactivity of the Ti–Al system: Experimental study and molecular dynamics simulations. Journal of Applied Physics, 2020, 127 (14), pp.145304. 10.1063/5.0004550 . hal-02995065

HAL Id: hal-02995065 https://hal.science/hal-02995065

Submitted on 10 Nov 2020

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(Dated: 10 November 2020)

The reactivity of the Ti-Al system was investigated experimentally in the case of reactive laminated particles produced by High Energy Ball Milling. The ignition temperature for self-sustaining reaction was measured as a function of the heating rate. By means of the Kissinger analysis, two activation energies were evaluated. The first one is associated to the solid state transformation at interface below the melting point of Al. The second one corresponds to the exothermic dissolution of Ti into Al liquid together with the formation of TiAl₃. A complementary microscopic approach was developed in order to detect all elemental processes associated the reactivity of the Ti-Al system in composite materials. Above the melting temperature of Al, the exothermic dissolution of Ti into the liquid layer starts and induces a self-sustaining behavior until the reaction is complete. The dissolution step is limited by the low solubility of Ti in Al. The formation of the intermetallic compound TiAl₃was observed. The microscopic analysis of the dissolution at interface explains some specific features of reactive particles.

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I. INTRODUCTION

Research on Ti-Al based intermetallic alloys is an active research field due to their possible use in aircraft engines, industrial gas turbines, and automotive industries. These materials exhibit unique physical and mechanical properties such as very good strength, high specific yield strength and stiffness, good oxidation resistance combined with good creep properties at high temperatures, low density, high thermal capability and biocompatibility, ...¹. Actually, titanium aluminides is an important class of materials that could provide a promising alternative to nickel alloys. In the last decades, the class of Ti-rich Ti-Al based intermetallic materials has replaced many usual alloys for applications up to 900 °C (1173 K). For instance, the Ti lamellar alloys (γ -TiAl+ α_2 -Ti₃Al) are already used in industrial applications due to strength and ductility requirements at high temperature.

A major issue is to use refractory Ti-Al intermetallic alloys in additive technologies. This is actually challenging because 3D printing by SLM (Selective Laser Melting) and SLS (Selective Laser Sintering) uses a local heating that must be close to the high melting point of refractory powder particles. In order to overcome the technological bottleneck, an alternative is the fabrication of composite reactive particles Ti+Al that react at low temperature and lead to the direct formation of intermetallic alloys². In parallel, a new method for fabricating Ti-Al intermetallic compounds by cold spraying was proposed in³.

Reactive multilayer nanofoils (RMNF) present very close similarities with reactive laminated particles (RLP). They are often used as model systems to study the processes occurring at the atomic scale in metallic nano-systems presenting a huge amount reactive interfaces. RMNFs are composed of hundreds of stacked thin metallic layers, varying in thickness from 4 to 100 nm. In such bimetallic Ti/Al nanofoils, a short-term local heating will induce a rapid and self-sustaining reaction⁴. The exothermic reaction propagates along the foil without any further energy supply. The propagation velocity of the reaction is up to 3 m/s^{5,6}. The overall reaction temperature is higher than the

melting temperature of Al ($T_m = 660 \,^{\circ}\text{C}$ (933 K)) and lower than the melting temperature of Ti ($T_m = 1650 \,^{\circ}\text{C}$ (1923 K)). Thus, the reaction proceeds in a liquid/solid system. A Ti-Al foil is transformed in intermetallics in less than 50 ms. The kinetics of intermetallic phase formation in the Ti/Al multilayers has been investigated using differential scanning calorimetry and time-resolved X-ray diffraction^{7,8}.

Many questions arise concerning the reactivity of the Ti-Al system in RMNFs. In order to address this issue, we adopted a molecular dynamics approach that gives a full microscopic description. This approach has been extensively applied in the case of Ni/Al RMNFs (for a review, see⁹). Molecular dynamics simulations (MDS) reveal the elemental mechanisms that occur at nanoscale: melting, dissolution, mixing, phase transformations, microstructure formation, nucleation and growth of intermetallics, ... Such analysis allows us to describe the complex kinetics occurring in metallic systems provided a satisfactory interatomic potential is available. There exists a limited number of studies of the Ti-Al system by means of molecular dynamics. The alloying reaction in Ti-coated Al nanoparticle (4.8 nm of diameter in equiatomic fraction) was studied by means of MDS in combination with an Embedded Atom Method (EAM) potential¹⁰. The alloying reaction occurs as a metastable solid-state alloying process that completes after the melting of the Al core. After an heating up to 900 K, the exothermic alloying reaction heats up the system to an adiabatic temperature of 1352 K. The final product is an undercooled liquid $Ti_{50}Al_{50}$ alloy. The Al-coated Ti nanoparticle is much less reactive because of pre-alloying in the vicinity of the interface¹¹. The synthesis of the intermetallic γ -TiAl was studied by means of MDS in the thermal explosion regime¹². Heterogeneous crystallization from the melt was observed at 1550 K when the system is submitted to $cooling^{13}$. The heterogeneous nucleation of solid Al from the melt by TiAl₃was investigated¹⁴. It appears that the intermetallic TiAl₃is a powerful nucleant for the solidification of aluminum.

A recent experimental work² demonstrates the peculiar features of Ti-Al RLPs produced by High Energy Ball Milling. First, a preliminary heating is required for the onset of a self-sustaining reaction. The ignition temperature is close to the melting point of Al. Actually, the formation of liquid Al promotes the exothermic dissolution of Ti into Al liquid that induces a temperature rise. The combustion of Ti-Al RLPs leads to the formation of Ti-TiAl₃composites.

In this work, we focused on the reactivity of composite Ti-Al systems by combining an experimental investigation and MD study. In the experimental part, the aim is to detect the key aspects of the exothermic reaction as the reaction onset temperature and the characteristic activation energy. In the MD part, the understanding of the reaction mechanism is directly related to the question of phase transformations associated with the self-propagating reactive wave. To handle this problem by means of molecular dynamics, the atomic and microstructure evolution inside the stacked layers was simulated at a fixed temperature. Two representative systems were prepared: a small system (reference system) and a thick system. Different initial temperatures close to the melting temperature of Al were imposed for the same stoichiometry $N_{\text{Ti}}/N_{\text{Al}} \sim 3$ with an excess of Ti. This allowed accurate description of reactive dissolution and crystallization of intermetallic compound during the progress of the reaction.

II. METHODS

A. Experimental methods

Composite Ti/Al powders were produced by means of High Energy Ball Milling (HEBM) technique in the planetary mill "Activator-2S" ("Activator", Russia), from the mixture of Ti and Al elemental powders. The powders were placed in the steel jars together with steel balls. Volume of the jar was 250 ml (filled with Ar at 4 bar), diameter of the steel balls 6 mm, balls to mixture mass ratio 20:1, the rotation speed of Sundisc 200 rpm, milling time 120 min. After HEBM, the powder consisted of bimetallic particles, were Ti flattened inclusions were embedded into Al matrix: thus, Al layers separated Ti islands in each bimetallic particle. Reactivity of the composite powders

were evaluated by heating up mini-pellets (3 mm in diameter, 0.3 - 1.0 mm thick), consolidated from the composite powder, in Ar atmosphere, and measuring reaction onset temperature T_i . Details of the methods were published earlier². Microstructure and elements distribution inside the bimetal particles were studied using SEM and EDS analyses. Basing on the Kissinger method¹⁵, energy of activation *E* was evaluated from the formula

$$\ln\left(\frac{b}{T_i^2}\right) = \operatorname{const} - E/(RT_i) \tag{1}$$

where b = dT/dt - heating rate, T_i - reaction onset temperature, R - gas constant. We used T_i instead of the temperature corresponding to maximum reaction rate, T_m , because, as distinct from differential scanning calorimetry, temperature in our experiments increased very sharply after reaction initiation. Thus, value of Ti was close to Tm, which allowed evaluation of E from eq. (1).

B. Simulation details

The molecular dynamics (MD) simulations were performed with the LAMMPS MD software¹⁶. The system was analyzed at the atomistic level using the EAM interatomic potential developed by Zope and Mishin in 2003¹⁷. The potential of Zope and Mishin was initially fitted for Al, α -Ti and γ -TiAl using extended experimental and ab-initio databases and its transferability was then tested by considering other intermetallic compounds (i.e., $L1_0$ -TiAl, $L1_2$ -TiAl₃and $D0_{22}$ -TiAl₃). A preliminary step consisted in computing the melting temperature (see Table 1) using a classical liquid-solid coexistence (two-phase) method¹⁸. Thermal expansion coefficient was also determined to characterize the behavior of the system as a function of temperature (see Appendix).

In order to model the Ti-Al reactive interfaces in RLPs, a simplified bilayer Ti-Al-Ti system was considered. The initial system (see Fig. 1), referred to here as the small sample, is made of an inner layer of fcc-Al (7 atomic planes containing 10 188 Al atoms) in between two outer layers of hcp-Ti (8 and 9 atomic planes each containing all together



FIG. 1. Initial configuration of the simulated system with one slice of Al in between two Ti layers. Al and Ti are shown as blue and red spheres, respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

	Melting	temperatures	Cohesive energies (eV/atom)	
metal/phase	two-phase method	other works	experimental	EAM potential vs. experimental
Al	870	870	933	3.36 / 3.36
Ti	1531	-	1941	4.85 / 4.85
TiAl	1510	1494	1713	4.51 / 4.51
$TiAl_3(DO_{22})$	1175	-	1388	4.02 / 4.06

TABLE I. Melting temperatures and cohesive energies evaluated using the Zope and Mishin EAM potential and experimental values.

31 280 atoms) with $N_{\text{Ti}}/N_{\text{Al}} \sim 3$. The size of the simulation box is $L_x = L_y = 11.8$ nm in the *x*-direction and $L_z = 6$ nm in the *z*-direction. The interface is oriented normal to the [002] direction of the Ti layers and to the [111] direction of Al layer. Periodic boundary conditions are applied in all directions. The empty space around the Al layer allows the system to avoid any artificial constraint due to the application of periodicity on the Al and Ti¹⁹.

Both Al and Ti lattice parameters were determined as a function of temperature on bulk systems. Hence, the Ti-Al-Ti system was created with the appropriate lattice pa-

	$N_{ m Ti}/N_{ m Al}\sim 3$				
sample	$L_x = L_y \text{ (nm)}$	L_z (nm)	Al atomic planes	# atoms	
Reference system	11.8	6.1	7	41 468	
Thick sample	17.5	13.4	15	211 710	

TABLE II. Summary of the simulation details

rameter corresponding to the initial temperature (see Appendix). The simulation is thermalized in the canonical statistical ensemble (NVT) over 400 ps at the initial temperature using a Nosé-Hoover thermostat (damping parameter of 0.1). The simulation is then carried out in the microcanonical statistical ensemble (NVE) over more than 15 ns. NVE simulation corresponds to adiabatic conditions: no external reservoir is interacting with the system. This procedure allows us to observe the spontaneous dynamics of the system that may imply a variety of elemental mechanisms. The time step to integrate the equation of motions with a Verlet algorithm was fixed at 0.001 ps.

A thick sample was also considered (see Table II). Initially, an inner layer of fcc-Al with of 15 atomic planes ($N_{Al} = 51\ 230$) was placed in between two outer layers of hcp-Ti with 40 atomic planes each ($N_{Ti} = 160\ 480$) with $N_{Ti}/N_{Al} \sim 3$. The size of the simulation box is $L_x = L_y = 17.5$ nm in the x-direction and $L_z = 134$ nm in the zdirection. The orientations of Ti and Al at interface was (002)/(111) as in the previous simulations. The simulation procedure is in two parts:

- The system is thermalized in the NVT ensemble before the simulation in adiabatic conditions (NVE ensemble).
- The system is then cooled down by step of 5 K in the NPT ensemble (Parrinello and Rahman scheme with a damping parameter of 0.1) during 300 ps and the NVT ensemble during 100 ps. After each step, the simulation is carrying out in the microcanonical ensemble (NVE) in order to observe the spontaneous dynamics of the system. The cooling process begins at 1315 K and ends at 1200 K.

Different indicators are used to follow the evolution of the system. The number density profiles along the *z*-axis gives a good indication of the crystallinity state and of the local composition in Ti or Al in each slice. Well-defined peaks are associated with a system structured in atomic planes. Each atom was labeled by two indices: one associated with the chemical species (type) and one with its local lattice structure (Ackland and Jone's indicator)²⁰. It is also useful to compute the potential energy per atom, which is very sensitive to the local environment of a given atom. Global indicators were also followed during the evolution of the system: temperature and the stoichiometry in the inner layer. The stoichiometry is defined as the ratio $\xi = N_{\text{Ti}}/(N_{\text{Ti}} + N_{\text{Al}})$. The microscopic configurations were visualized with the open-source software (OVITO)²¹.

III. RESULTS AND DISCUSSIONS

A. Experimental results

After HEBM, both metals (Ti and Al) formed bimetal particles (Fig. 2a). More ductile metal Al forms matrix, where Ti layers (inclusions) have irregular shape. No intermetallic phases were observed at the boundaries between Al and Ti (Fig. 2b). At the same time, some intermixing of these two metals was revealed due to line-scan mode of EDS microanalysis (Fig. 3). A typical microstructure of the intermixed areas looks similar to metastable phases that formed in the Ni-Al systems during HEBM due to intense friction²². It allows us to assume that metastable phases (perhaps, solid solutions) can be formed due to HEBM also in the Ti-Al system, which should decrease temperature of the reaction initiation in this system.

In order to measure the reaction initiation temperature, the mini-pellets were placed in the h-BN crucible and heated up using carbon-strip heater with average rate from 18 K/s up to 119 K/s. Typical temperature - time profile of the process is shown in Fig. 4. When the temperature of the sample achieved some value T_i , exothermal reaction started and increased temperature sharply. The heating regime below T_i does not follow



FIG. 2. Microstructure of the bimetal particle after HEBM (a) and boundaries between Ti and Al layers (b). SEM, backscattered electrons. Dark phase is Al, white - Ti.



FIG. 3. SEM and results of the EDS scanning along the line. Dark phase - Al, white - Ti, grey - intermediate metastable phase.

strictly a linear law, however, average heating rate can be calculated for the sake of rough approximation as

$$b = \langle dT/dt \rangle = (T_i - T_0)/t_i,$$
 (2)

where T_i - the reaction onset temperature, T_0 - initial temperature of the sample, and t_i - heating time. The carbon heater was switched-off in 1 s after exothermic reaction initiation, and the sample cooled down.



FIG. 4. Temperature-time profile of the heating up and reaction in Ti/Al composite powder sample measured with WRe5/WRe20 thermocouple.

The value of T_i increased continuously with increasing heating rate *b* (Fig. 5). Based on these data, the Kissinger equation (1) was applied to evaluate activation energy of the process:

$$E \sim -R \, \frac{d \left[\ln(b/T_i^2) \right]}{d(1/T_i)} \tag{3}$$

Two linear regions were appeared at the Kissinger plot (Fig. 6) that correspond to the values of activation energy $E_1 = (28.4 \pm 7.3)$ kJ/mol for higher temperature, and $E_2 = (92.1 \pm 14.4)$ kJ/mol for lower temperature regions. A transition point between these two regions corresponds to a temperature of about 950 - 960 K, which is close to the melting point of Al (933.5 K). Thus, we can assume that limiting stage of the process changes, when T_i exceeds melting temperature of Al. Probably, under slow heating conditions (smaller *b*), reaction has enough time to form some solid intermetallic product on the boundary between Ti and Al, which later limits the reaction rate even after Al melts. At fast heating (larger *b*), no solid product appears, and the reaction is limited only by diffusion in the melt, with small energy of activation.

Although the two measured values of E definitely indicate two different mechanisms of interaction, it remains a challenge to reveal these mechanisms. Diffusion coefficient and activation energy of Ti atoms in the Al melt are not available up to now. The activa-



FIG. 5. Reaction onset temperature as function of heating rate.



FIG. 6. Evaluation of activation energy in Kissinger coordinates.

tion energies of Ti and Al solid state diffusion in different phases of the Ti-Al systems, such as α -Ti, β -Ti, Ti₃Al, and TiAl, fall in the range 2.59-4.08 eV (250-394 kJ/mol)²³. These values are much higher than the values measured in this work. From the other hand, some experimental study of interfacial reactions in Ti/Al multilayers during diffusion welding, shown that effective activation energy of diffusion decreases dramatically with decreasing atomic fraction of Ti²⁴. Thus, the activation energy for diffusion in the TiAl phase was determined as 250 kJ/mol, while diffusion in the TiAl₃ phase had activation energy about 100 kJ/mol. Moreover, TiAl₃ was a major phase formed dur-

ing the diffusion welding²⁴. Recent works confirmed the leading role of TiAl₃ in the interface reaction between Ti and Al below melting point of Al^{25,26}. Measurements of the linear growth rate of TiAl₃ layer in the temperature range 823 - 923 K gave activation energy 128.7 kJ/mol²⁶. Since the forming has polycrystalline structure with well-developed grain boundaries network²⁵, the grain boundary diffusion must be also taken into account. Basing on to the normal parabolic growth of the TiAl₃ layer (which was the only phase appeared on the Ti/Al boundary at 823-923 K), activation energy of 33.1 kJ/mol was obtained for the low temperature grain boundary diffusion controlled growth, and 296.2 kJ/mol - for the high temperature bulk diffusion controlled growth²⁷. Overall activation energy of 76.8 kJ/mol was accepted for the whole region of the applied annealing temperatures. It is worth noting that all these data were obtained using isothermal annealing method. Comparison with our data measured at non-isothermal conditions allows assumptions that the value of 92.1 kJ/mol corresponds to combination of solid-state bulk and grain boundary diffusion, while 28.4 kJ/mol may correspond to grain diffusion solely or to liquid phase diffusion in the Al melt. From analogy with other metallic melts, we may expect that activation energy of diffusion in the Al melt is approximately 5 times smaller that that for the solid-state diffusion²⁸. The following MDS results allow deeper insight in the mechanism of interaction.

B. Numerical results

1. Reference sample

The reference system was prepared at different initial temperatures, close to the melting temperature of Al, $T_m(Al) = 870$ K (see Table I). For initial temperatures below the melting temperature of Al, the system remains stable. Just a small number of defects appear in the inner layer. The stability of the interface is quite unexpected as compared to prior works on Ni-Al system where exothermic phase transformations already appear in solid-state¹⁹. This is probably due to the very low misfit between (002) Ti-plane and

(111) Al-plane (see Fig. 7).



FIG. 7. Atomic arrangement of Ti and Al at the interface.



FIG. 8. (a): Temperature T (scale in K, on the right) and number of atoms in at% (on the left) as a function time (scale in ns). The number of atoms in fcc, hcp and unknown configuration are represented. The different stages in the evolution are indicated by the dashed lines. (b): Temperature T (scale in K, on the right) and stoichiometry (on the left) as a function time (scale in ns).

For an initial temperature of 950 K, the situation is completely different. During the thermalization at 950 K, the Al inner melts and wets the Ti-free surface. During the simulation in adiabatic conditions, the temperature is followed as well as the fraction (at%) of atoms in the different local configurations (fcc, hcp or unknown). The typical shape of curves in Fig. 8 suggests that the dynamics of the system can be divided into 4

stages:

- I Just after thermalization, from t = 0.4 to 11 ns (stage I), the number of amorphous atoms (unknown) and fcc atoms is more or less constant. Amorphous atoms correspond to liquid atoms. The fcc-atoms are located at free surfaces or interfaces. The temperature slowly increases up to 1050 K and ξ reaches 0.18.
- II During stage II (from t = 11 to 12 ns), the number of hcp-atoms starts to decrease. The temperature reaches 1100 K and ξ exceeds 0.2. This stage corresponds to a rapid dissolution of Ti in the inner layer.
- III The stage III is short (less than 0.2 ns, from t = 12.24 to 12.46 ns). More hcp-Ti atoms disappear together with a sudden and short decrease in amorphous atoms. This corresponds to a reorganisation of the inner layer in fcc atoms. The burst in temperature is associated with the crysallization of the inner layer with a stoi-chiometry around 0.23.
- IV In the last stage (IV), the temperature reaches a plateau. Other indicators are stable. The system is completely crystallized and its structure doesn't changes over time.

The number density profile at t = 0.4 ns in Fig. 9a shows the amorphization of Al atoms in the inner layer due to melting. Although the temperature was larger than the melting temperature of Al, the Al atoms remained arranged in layers close to the interface. During the adiabatic evolution of the system, the Ti atoms invade the inner layer as the stoichiometric factor ξ progressively increases while the Al are reorganized in planes (see Fig. 9b). At the interfaces, the transient formation of a solid solution (Ti+Al)_{ss} was observed. Figure 9c demonstrates the recrystallization of the inner plane (6 planes) with a well-defined ratio between Al and Ti atoms. This ratio is slightly less than 0.25, the one expected for the formation of TiAl₃. The Ackland and Jones' analysis shows formation of a fcc-like structure except a twin defect formed by planes in hcp-like structure.

The increase in temperature is associated with two processes: the reactive dissolution between Ti and Al and the spontaneous crystallization of a new phase. The reactive dissolution plays an important role in the catalytic character of the reaction because an increase in temperature favors further dissolution of Ti in Al. In this simulation, the process of dissolution was interrupted by the phase transformation in an intermetallic compound. Indeed, the stoichiometry in the inner layer increases up to a plateau with a value of 22 at% of titanium.

The phase transformation could be associated with an exothermic reaction giving rise to the formation of a new compound. If we suppose that TiAl₃is formed:

$$3Al + Ti \rightarrow TiAl_3$$
 (4)

The energy balance expressed in terms of cohesive energies reads

$$\frac{1}{4}[3 \times E_0(\text{Al}) + E_0(\text{Ti})] = E_0(\text{TiAl}_3) + q$$
(5)

where q = 0.30 eV is the excess energy released by the atomic rearrangement or, equivalently, the formation energy of the compound TiAl₃. The intermetallic TiAl₃is characterized by a $D0_{22}$ structure at high temperature. But the potential developed by Zope and Mishin¹⁷ gives a very small difference between the two structures $D0_{22}$ and $L1_2$ of the TiAl₃. The structure $L1_2$ is 0.001 eV/atom smaller than the structure $D0_{22}$. According to this observation, the distinction between these two structures can't be really established in the context of the simulation.

Another simulation was carried out with an initial temperature of 1000 K. The number of atoms and the geometry remained the same. The system was created with the appropriate lattice parameter corresponding to 1000 K. As shown in Fig. 10, the dynamics follows the four stages described previously. During stage II, the temperature rise is even more pronounced. The dissolution is here more important and the stoichiometry reaches a plateau value of 34 at% and a maximum temperature $T_{ad} = 1300$ K. The evolution towards the final temperature is done in a shorter time.



FIG. 9. Number density profiles at t = 0.4, 12.24, 12.46 ns in the *z*-direction, perpendicular to the interfaces. The dashed lines indicate the limits of the inner layer in the initial configuration. Corresponding snapshots of the system. Position is measured in Angstroms.

2. Thick sample

In order to investigate the size effect, a thick sample was created at 1000 K. We performed the same analysis as previously. In this case, Fig. 11a shows only 3 stages: (I) slow increase in temperature and no configuration change, (II) rapid dissolution of Ti in the inner layer and (III) saturation toward the adiabatic temperature. The dissolution of Ti in the inner layer produces a release of heat. The adiabatic temperature is 1315 K and the saturation of the liquid solution is $\xi = 0.35$ as shown in Fig. 11b. No spontaneous crystallization was observed. After the NVE simulation in adiabatic conditions, the inner layer is a liquid solution (0.35 Ti+ 0.65 Al)_{liq}. Figure 12 at t = 5 ns gives the



FIG. 10. Initial temperature of 1000 K. (a): Temperature T (scale in K, on the right) and number of atoms in at% (on the left) as a function time (scale in ns). The number of atoms in fcc, hcp and unknown configuration are represented. The different stages in the evolution are indicated by the dashed lines. (b): Temperature T (scale in K, on the right) and stoichiometry (on the left) as a function time (scale in ns).

number density profile and the corresponding snapshot of the system during stage (I). Although the inner layer is Al liquid, a structural ordering close to the interfaces was noticed. Figure 12 at t = 20 ns corresponds to the coexistence of solid outer layers surrounding the liquid solution of Ti and Al. As shown in Fig. 12, 3.5 ns after the start of the cooling demonstrates the complete reorganization in atomic planes with a constant ratio between Ti and Al in each plane. All atoms of the inner layer have a fcc local configuration as proven in Fig. 11c.

Dissolution is the main process in the self-sustained character of the reaction in the Ti-Al system. Above the melting point of Al, Ti dissolve in the liquid Al layer. Figure 13 gives the coverage of 4 planes below the lower interface. A similar behavior was observed for the upper interface. The following features were identified:

- 1. The Ti atoms close to the interfaces leave the solid substrate more easily than atoms located deeper. Nevertheless, the number of liquid atoms (marked as amorphous atoms) doesn't significantly increase.
- 2. The vacancies liberated by outgoing Ti atoms are occupied by incoming Al atoms



FIG. 11. Thick sample. Initial temperature of 1000 K. (a): Temperature T (scale in K, on the right) and number of atoms in at% (on the left) as a function time (scale in ns) during the heating. The number of atoms in fcc, hcp and unknown configuration are represented. (b) Stoichiometry (on the left) as a function time (scale in ns). (c): Temperature T (scale in K, on the right) and number of atoms in at% (on the left) as a function time (scale in ns) during the cooling.

very quickly. Most Al atoms adopt a local fcc arrangement while Ti atoms are becoming liquid. The Al atoms occupy substitutional positions in the first atomic plane (# -1) below the interface.

- 3. The mobility of Al atoms is limited in outer layers because of the lack of local defects and the inefficient diffusion in solid-phase. As shown in Fig.13, the first plane below the interface is completely depleted by Ti atoms and progressively covered by Al atoms. Defects (vacancies and line defects) are created in plane (# -1).
- 4. In about 10 ns, 50 at% of Ti of the first atomic plane below the interface are dissolved. At 12 ns, the number of Ti reaches a minimum value. Remaining Ti (< 20 at%) are located on the free surfaces.
- 5. When the number of Ti in the plane (# -1) is significantly reduced, the second plane (# -2) starts to be depleted and the number of Ti in the plane (# -1) increases again and reaches a value of 32 at%. The dissolution process operates plane by plane as shown in Fig. 13.



FIG. 12. Number density profiles at t = 5, 20 ns in the *z*-direction, perpendicular to the interfaces, and 3.5 ns after the start of the cooling. The dashed lines indicate the limits of the inner layer in the initial configuration. Corresponding snapshots of the system. Position is measured in Angstroms.

6. After the dissolution of 70 at% of Ti atoms in 3 planes, the system reaches a state Ti_{sol} - $(Ti_x + Al_{1-x})_{ss}$ - $(Ti_y + Al_{1-y})_{liq}$

In the case of liquid mixtures, Titanium and Aluminum are characterized by a negative mixing enthalpy:

$$\Delta H_{\rm mix}(T) = H_{\rm Ti-Al}(T) - [(1 - x_{\rm Ti})H_{\rm Al}(T) + x_{\rm Ti}H_{\rm Ti}(T)]$$
(6)

At the atomistic level, the scheme (Fig. 14) shows the elemental process associated with dissolution: a liquid atom Al will be exchanged with a solid Ti atom. As an example, a set of atoms were followed. For instance, the potential energy of the Al atom in the



FIG. 13. Number of Ti atoms (at%) in the atomic planes close to the interface. The plane (# -1) is the plane just below the interface, the plane (# -2) is below the plane (#-1),



FIG. 14. Number of Ti atoms (at%) in the atomic planes close to the interface. The plane (# -1) is the plane just below the interface, the plane (# -2) is below the plane (#-1),

liquid layer is around - 3.28 eV and decreases to -5.28 eV when it substitutes a Ti in the outer solid layer. The Ti atom in the solid has a potential energy of -4.31 eV and increases to -3.38 eV when it disolves in the inner liquid layer. The energetic balance reads:

$$E(Al_{liq}) + E(Ti_{sol}) = E(Al_{Ti-sol}) + E(Ti_{Al-liq}) + q_{diss}$$
(7)

where $q_{\rm diss}$ represents the excess of energy release by the dissolution process: the heat

of dissolution $q_{\text{diss}} = 1.27$ eV. The energy transfer associated with all dissolved atoms induces the increase of *T* up to 1315 K.

During the exchange between Al and Ti atoms, a single incoming Al atom surrounded by Ti atoms induces a slight change in the potential energy of Ti nearest neighbours (Fig. 15a). The substitution of several Al atoms in a vicinity induces a significant modification of neighbouring atoms (Fig. 15b). Such group of atoms will play the role of a nucleus for further dissolution.



FIG. 15. Snapshot of atomic plane #-1. (a): potential energy /atom. (b): species index (Al is blue and Ti is red). Time t = 2ns.

IV. CONCLUSIONS

The reactivity of the Ti-Al system has been studied by means of molecular dynamics simulations and experiments. The main features are as follows:

- No reaction occurs at a temperature below the melting point of Al. The interface between (002)-Ti plane and (111)-Al plane is very stable due to the small mismatch between the two structures. In addition, the metallic radius of Ti is slightly larger than the Al metallic radius:

$$r_{\text{metal}}(\text{Ti}) = 1.47 \text{ pm} \quad r_{\text{metal}}(\text{Al}) = 1.43 \text{ pm}$$
 (8)

This fact explains the lack of solubility of Ti in Al solid.

- When the system is heated above the melting temperature of Al, we observed an exothermic self-sustained dynamics until a plateau value of T is reached. The behavior is similar to the phenomenon of adiabatic explosion.
- The first phase transformation to occur at high temperature is the amorphization of the Al inner layer, except close the interfaces where Al exhibits a structural ordering.
- The dissolution of Ti in Al is associated with an exothermic mixing of the two metals. The heat released due to dissolution is the main heat source.
- The dissolution operates as an exchange of Ti and Al atoms at interfaces. There is no net flux at the interface.
- The adiabatic temperature depends on the initial temperature value. The same is true for the saturation value of the liquid solution.
- The spontaneous formation of an intermetallic compound was only observed in the small systems. The phase transformation is very rapid (less than 0.2 ns).
- In the large system, the crystallization of the intermetallic compound occurs during the cooling simulation at 2988 K. The growth of the intermetallic develops plane by plane starting from the interface.
- The intermetallic compound is $(Ti_y Al_{1-y})$ with $y \sim 0.3$. The interatomic potential developed by Zope and Mishin predicts a single Al-rich phase $Ti_{0.25}Al_{0.75} \equiv$ TiAl₃. The simulation results demonstrate the formation of an intermetallic with a well-defined composition and a local fcc configuration, close to the TiAl₃compound. As shown in Fig.16, the TiAl₃intermetallic can easily grow on a Ti plane. Substitution of Ti atoms by Al ones and a slight displacement of

Ti gives the specific structure. Moreover the $D0_{22}$ structure is based on a face centered cubic structure.



FIG. 16. $D0_{22}$ crystallographic structure of TiAl₃ and two consecutive (111) planes in TiAl₃. The (002) plane of pure Ti is shown in dashed. Al in blue and Ti in red.

ACKNOWLEDGMENTS

This work is supported by the International Russian-French PHC Kolmogorov "RECIPES" (Campus France no. 41144SG), the Ministry of Science and Higher Education of the Russian Federation in the framework of the Federal Target Program "Research and Development on Priority Directions of the Scientific and Production Complex of Russia for 2014-2020", agreement no. 14.587.21.0051, project RFMEFI58718X0051. The use of computational facilities at the Computing Center of the University of Bourgogne, PSIUN-CCUB, is gratefully acknowledged.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Thermal expansion								
metal/phase	A(Å)	B(Å/K)	$C(Å/K^2)$					
Al	4.05	4.868×105	4.237×108					
Ti	2.951	3.377 × 106	9.929 × 109					
TiAl	3.998	4.273 × 105	1.811 × 108					
TiAl ₃	4.049	5.638 × 105	2.688×108					

TABLE III. Coefficients *A*, *B* and *C* for the parabolic fit $a(T) = A + BT + CT^2$ giving the lattice parameter dependences on temperature for pure Ti and Al metals, and for the intermetallic compounds. These values were computed for the Zope and Mishin EAM potential¹⁷.

Appendix

The temperature evolution of the lattice parameter was investigated to determine the thermal expansion coefficient $\alpha = [a(T) - a(298K)]/a(298K) \times 100\%$, where a(T) is the lattice parameter at *T*. The method used to calculate the thermal expansion is in 3 steps. (1) the system is heated in the NVT ensemble during 50 ps with a temperature ramp of 10. (2) The system is relaxed in the NPT ensemble during 50 ps at a constant temperature. During this stage, the system adjust its volume. (3) The system is then simulated in the NVE ensemble during 10 ps. All the measurements are done in this part. The 3 steps making up one cycle are repeated during the simulation. The temperature is heated from 10 K to the melting point in order to get the thermal expansion in the solid phase. The temperature dependence of the lattice parameter was approximated by using a parabolic fit $a(T) = A + BT + CT^2$. The corresponding values of the coefficients *A*, *B*, and *C* are reported in Table III.

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