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Vortex-induced vibrations of a flexible cylinder at subcritical Reynolds number

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The flow past a fixed, rigid cylinder becomes unsteady beyond a critical Reynolds number close to 47, based on the body diameter and inflow velocity. The present paper explores numerically the vortex-induced vibrations (VIV) that may develop for a flexible cylinder at subcritical Reynolds number (Re), i.e. for Re < 47. Flexible cylinder VIV are found to occur down to Re ≈ 20 , as previously reported for elastically mounted, rigid cylinders. A detailed analysis is carried out for Re = 25, in two steps: the system behavior is examined from the emergence of VIV to the excitation of the first structural modes and then, focus is placed on higher mode responses. In all cases, a single vibration frequency is excited in each direction. The cross-flow and in-line responses exhibit contrasted magnitudes (peak amplitudes of 0.35 vs. 0.01 diameters), as well as distinct symmetry properties and evolutions (e.g. standing/traveling waves). The flow, unsteady once the cylinder vibrates, is found to be temporally and spatially locked with body motion. The synchronization with the cross-flow, standing wave responses is accompanied by the formation of cellular wake patterns, regardless the modes involved in the vibrations. Body trajectory varies along the span but dominant orbits can be identified. Despite the low amplitudes of the in-line responses, connections are uncovered between orbit orientation and flow-structure energy transfer, with different trends in each direction.

1. Introduction

Vortex-induced vibrations (VIV) of flexible bodies with bluff cross-section are encountered in many natural and industrial systems, e.g. plants and trees in wind, cables and mooring lines exposed to ocean currents. Due to their impact on engineering structures and their fundamental interest as a paradigm of fluid-structure interaction involving a synchronization, or lock-in, between body motion and flow unsteadiness, VIV have been the object of a number of studies, as reviewed for example by Williamson & Govardhan (2004). VIV have often been investigated through the canonical problem of a rigid circular cylinder mounted on an elastic support. When the rigid cylinder is fixed, the flow becomes unsteady beyond a critical Reynolds number close to 47, with the formation of the alternating von Kármán vortices (Mathis et al. 1984). The Reynolds number (Re) is based on the body diameter (D) and inflow velocity (U); the above critical value is denoted by Re_{c} in the following. If the rigid cylinder is elastically mounted, previous works have shown that VIV may occur in the subcritical-Re range, i.e. for $Re < Re_c$, possibly down to Re ≈ 20 , depending on the system parameters (Cossu & Morino 2000; Mittal & Singh 2005; Kou et al. 2017; Dolci & Carmo 2019). A typical case of rigid cylinder VIV in the subcritical-Re range (Re = 33) is presented in figure 1. The maximum amplitude of cross-flow vibration, normalized by D, is plotted in figure 1(a) as a function of the reduced velocity, U^* , defined as the inverse of the oscillator natural frequency

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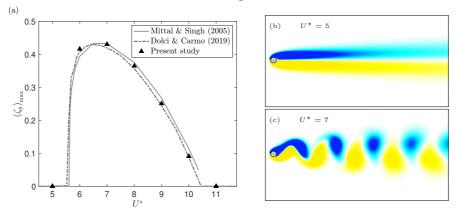


FIGURE 1. Vortex-induced vibrations of a rigid cylinder at Re = 33: (a) maximum amplitude of cross-flow displacement as a function of the reduced velocity; (b,c) instantaneous iso-contours of spanwise vorticity ($\omega_z \in [-0.3, 0.3]$), for (b) $U^* = 5$ and (c) $U^* = 7$. In (a), the present simulation results are compared to the amplitudes reported by Mittal & Singh (2005) and Dolci & Carmo (2019).

non-dimensionalized by D and U. Structural responses emerge over a well-defined range of U^* . The flow, which is steady in the absence of vibration, becomes unsteady and synchronizes with body motion within this range of U^* (figure 1(b,c)).

The present work aims at extending the analysis of subcritical-Re VIV to flexible cylinders. Flexible cylinder VIV have been well documented for $\text{Re} > \text{Re}_c$ (Chaplin *et al.* 2005; Bourguet et al. 2011; Wu et al. 2012; Huera-Huarte et al. 2014; Gedikli et al. 2018; Seved-Aghazadeh et al. 2019). They are still driven by the lock-in mechanism but the flexibility of the body and its distributed interaction with the flow may lead to an increased complexity of the system behavior. For example, several structural wavelengths may be excited, sometimes simultaneously (Bourguet et al. 2013). The vibrations often consist of a mixture of standing and traveling wave patterns and so does the wake (Newman & Karniadakis 1997). The phase difference between the streamwise and cross-flow vibrations may vary along the span, leading to diverse trajectory shapes, more or less favorable to body excitation/damping by the flow (Fan et al. 2019). These different aspects remain to be explored in the subcritical-Re range. An attempt is made here on the basis of three-dimensional numerical simulations. The question of the critical value of Re for the onset of flexible cylinder VIV is briefly addressed, then a constant value, Re = 25 (i.e. close to half Re_{c}), is selected and the investigation is carried out in two steps. First, focus is placed on the evolution of the system behavior with U^{\star} (based on the fundamental natural frequency), from the emergence of VIV to the excitation of the first structural modes; a cylinder of length to diameter aspect ratio equal to 50 is considered and U^{\star} is progressively varied from 1 to 35 (\S 3). Second, higher mode vibrations are examined for a cylinder of aspect ratio 400 and two high values of U^{\star} , 80 and 110 (§4).

2. Formulation and numerical method

A sketch of the physical system is presented in figure 2. The cylinder has a circular cross-section, is pinned at both ends and aligned with the z axis in the absence of deformation (fluid at rest). Its length and diameter are denoted by L and D, respectively. The cylinder is placed in an incompressible, uniform cross-current, parallel to the x axis. The Reynolds number is based on the inflow velocity (U) and D, Re = $\rho_f UD/\mu$, where

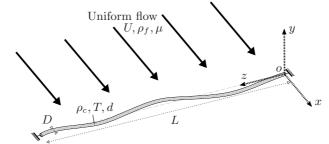


FIGURE 2. Sketch of the physical system.

 ρ_f and μ denote the fluid density and viscosity, respectively. The flow dynamics is predicted by the three-dimensional Navier–Stokes equations. The cylinder can oscillate in the in-line (IL, x axis) and cross-flow (CF, y axis) directions. All the physical variables are non-dimensionalized by D, U and ρ_f . The non-dimensional structural mass, tension and damping are defined as $m = \rho_c/(\rho_f D^2)$, $\tau = T/(\rho_f D^2 U^2)$ and $\xi = d/(\rho_f DU)$, where ρ_c denotes the cylinder dimensional mass per unit length, T and d are its dimensional tension and damping. The IL and CF displacements, non-dimensionalized by D, are denoted by ζ_x and ζ_y . The sectional IL and CF force coefficients are defined as $C_{\{x,y\}} = 2F_{\{x,y\}}/(\rho_f DU^2)$, where F_x and F_y are the dimensional sectional fluid forces aligned with the x and y axes. The body dynamics is governed by forced vibrating string equations (Newman & Karniadakis 1997; Bourguet *et al.* 2011):

$$m\ddot{\zeta}_{\{x,y\}} - \tau \zeta''_{\{x,y\}} + \xi \dot{\zeta}_{\{x,y\}} = \frac{C_{\{x,y\}}}{2}, \qquad (2.1)$$

where ' and ' denote the time and space (z) derivatives. The non-dimensional natural frequency associated with the n^{th} sine Fourier mode (i.e. $\sin(\pi nzD/L)$) is obtained via the dispersion relation $f_{\text{nat}}(n) = n\sqrt{\tau/m}/(2L/D)$, in vacuum. The reduced velocity is defined as the inverse of the fundamental natural frequency $(n = 1), U^* = 1/f_{\text{nat}}(1)$.

The structural damping ratio is defined as $\gamma = \xi(L/D)/(2\pi\sqrt{\tau m})$. Different values of Re, L/D, m, γ and U^* are examined.

The numerical method is the same as in previous studies concerning comparable systems at higher Re (Bourguet et al. 2011, 2013). It is briefly summarized here and some additional validation results are presented. The coupled flow-structure equations are solved by the parallelized code Nektar, which is based on the spectral /hp element method (Karniadakis & Sherwin 1999). The computational domain (50D downstream and 20D in)front, above, and below the cylinder), boundary conditions (no-slip condition on the cylinder surface, flow periodicity on the side boundaries) and discretization (2175 elements in the (x, y) plane) are the same as in the above mentioned studies. A convergence study was carried out in a typical case of subcritical-Re VIV (Re = 25, L/D = 50, m = 6, $\gamma = 0, U^{\star} = 32$) in order to select the non-dimensional time step (0.005), polynomial order in the (x, y) plane (5) and number of Fourier modes in the z direction (128). In particular, the relative differences on force/vibration amplitudes and frequencies were lower than 0.05% when increasing the polynomial order from 5 to 6. For the larger aspect ratio configuration (L/D = 400), 1024 Fourier modes are employed. In figure 1(a), a comparison of the CF vibration amplitudes of a rigid cylinder subjected to VIV at Re = 33 (two-degree-of-freedom oscillator), with those reported in prior works, confirms the validity of the present numerical method. Each simulation is initialized with a lowamplitude $(10^{-4}D)$, random asymmetrical deformation of the cylinder. The analysis is based on time series of more than 30 oscillation cycles, collected after convergence.

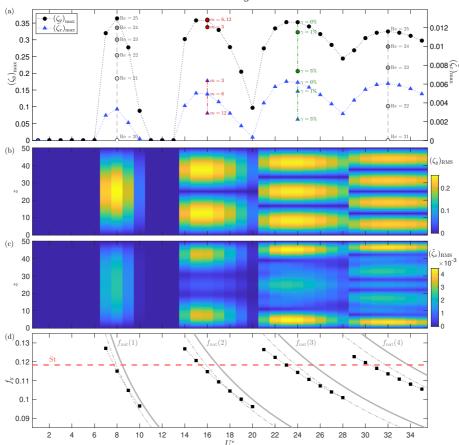


FIGURE 3. Responses of the flexible cylinder (L/D = 50) at Re = 25, for m = 6 and $\gamma = 0$, as functions of U^* : (a) maximum amplitudes of displacement fluctuations in the CF (left axis; black circles) and IL (right axis; blue triangles) directions; (b,c) RMS values of the (b) CF and (c) IL displacement fluctuations along the span; (d) CF vibration frequency (IL vibration frequency is equal to twice this frequency). In (a), the maximum amplitudes of CF displacement for Re $\in [20, 24]$ are also represented at $U^* = 8$ and $U^* = 32$ (grayscale circles); the maximum amplitudes of CF and IL displacement fluctuations are added for Re = 25, at $U^* = 16$ for $m \in \{3, 12\}$ and $\gamma = 0$ (red symbols), and at $U^* = 24$ for m = 6 and $\gamma \in \{0.01, 0.05\}$ (green symbols). In (d), the natural frequencies of the first four structural modes in vacuum ($f_{\rm nat}$) are indicated by plain gray lines; the corrected natural frequencies, with an added mass coefficient of 1, are denoted by gray dashed-dotted lines; the vortex shedding frequency identified by Buffoni (2003) is indicated by a red dashed line.

3. Emergence of VIV and first mode responses

The emergence of VIV and their evolution with U^* are examined for a cylinder of aspect ratio L/D = 50. The maximum amplitude of CF vibration along the span for $\text{Re} \in [20, 25]$, m = 6 and $\gamma = 0$, is plotted at $U^* = 8$ and $U^* = 32$ in figure 3(a). Vibrations arise between Re = 20 and 21 at $U^* = 8$ and between Re = 21 and 22 at $U^* = 32$; these values of Re are close to those reported for rigid cylinder VIV (Dolci & Carmo 2019). Considering the possible influence of the other structural parameters, no attempt was made to determine the value of Re for the onset of vibration for all U^* . The value Re = 25 is selected as a typical value to explore subcritical-Re VIV and it is kept constant in the rest of the paper. To illustrate the existence of vibrations at

this Re for different non-dimensional structural masses and when structural damping is added, the maximum amplitudes of CF and IL responses are represented at $U^* = 16$ for $m \in \{3, 6, 12\}$ and $\gamma = 0$, and at $U^* = 24$ for m = 6 and $\gamma \in \{0, 0.01, 0.05\}$ ($\tilde{}$ denotes the fluctuation about the time-averaged value). In the following, γ is set to 0 to allow maximum amplitude vibrations and m is set to 6.

An overview of the structural responses occurring at Re = 25, for m = 6 and $\gamma = 0$, is presented in figure 3. The maximum vibration amplitude exhibits similar trends in each direction as a function of U^{\star} but contrasted magnitudes since the peak amplitudes are close to 0.35 diameters in the CF direction and lower than 0.01 diameters in the IL direction (figure 3(a)). Comparable amplitudes were reported in the rigid cylinder case (Mittal & Singh 2005). The successive bell shapes in the evolution of the vibration amplitudes are associated with successive changes in their spatial structures. They are visualized in figure 3(b,c) via the root mean square (RMS) values of the displacement fluctuations along the span. Well-defined sine modes $(1^{st} to 4^{th})$ can be identified in the CF direction. Less regular patterns develop in the IL direction but it can be noted that the instantaneous response is always symmetrical about the midspan point, while it may be either symmetrical (odd modes) or anti-symmetrical (even modes) in the CF direction. Such phenomenon was also observed at higher Re for symmetrical systems (Gedikli et al. 2018). At higher Re, both mono-frequency and multi-frequency vibrations were reported for a flexible cylinder placed in a uniform current (e.g. Seyed-Aghazadeh et al. 2019). Here, a single frequency is excited in each direction, with a ratio of 2 between the IL and CF responses as usually observed for circular bodies. As shown in figure 3(d), the CF vibration frequency (f_y) remains lower than the natural frequency of the corresponding structural mode in vacuum (plain gray lines). It is relatively close to the natural frequency corrected by considering the potential added mass coefficient $C_m = 1$, i.e. $f_{\text{nat}} \sqrt{m/(m + C_m \pi/4)}$ (gray dashed-dotted lines; Williamson & Govardhan (2004)). This is not always the case at higher Re (Bourguet et al. 2011). The vibration frequency ranges from 0.1 to 0.13 approximately. This range includes the subcritical Strouhal frequency found by Buffoni (2003) by triggering the flow (St = 0.118, red dashed line).

In the absence of vibration, the flow is steady and similar to that depicted in figure 1(b). When the body vibrates, the frequencies of flow unsteadiness and body CF motion coincide along the entire span, as illustrated in figure 4 by the power spectral densities (PSD) of the CF component of flow velocity sampled at (x, y) = (10, 0), in four typical cases (f_y is indicated by a vertical dashed-dotted line); an example is selected for each mode excited in the CF direction (1st to 4th). The lock-in condition is thus established. This justifies the term VIV employed to designate the present vibrations. The absence of response up to $U^{\star} = 6$ and around $U^{\star} = 12$ (figure 3(a)) suggests that the admissible range of wake frequencies (i.e. deviation from the subcritical Strouhal frequency) is not compatible with the possible vibration frequencies. In addition, the spanwise structures of the flow and body response are found to coincide, with the same wavelengths and the minima of flow velocity PSD matching CF vibration nodes (horizontal dashed lines in figure 4). This coincidence shows that the flow and the body are not only temporally locked but also spatially locked. In all cases, the wake exhibits a cellular pattern where each cell ends near the nodes of the CF vibration. Instantaneous visualizations of the flow are presented in figure 4. Within each cell, two counter-rotating vortices are formed per oscillation cycle (2S pattern; Williamson & Govardhan (2004)) and the flow is comparable to that depicted in figure 1(c).

To further analyze the system behavior, the synchronization of the IL and CF responses and its possible link with flow-structure energy transfer are examined in the following.

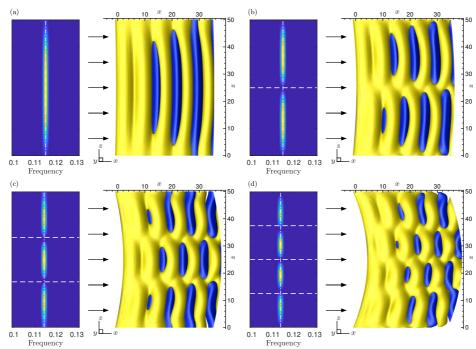


FIGURE 4. Flow patterns downstream of the flexible cylinder subjected to VIV at Re = 25 (L/D = 50): PSD of the CF component of flow velocity along the span at (x, y) = (10, 0) and instantaneous iso-surfaces of spanwise vorticity ($\omega_z \pm 0.07$), for (a) $U^* = 8$, (b) $U^* = 16$, (c) $U^* = 24$ and (d) $U^* = 32$. The PSD are normalized by the peak magnitude; the color code ranges from blue (0) to yellow (1). A vertical dashed-dotted line indicates the CF vibration frequency and horizontal dashed lines denote CF vibration nodes. Arrows represent the oncoming flow. Part of the computational domain is visualized (35D downstream of the cylinder).

With a frequency ratio of 2 between the IL and CF responses, the cylinder exhibits figureeight trajectories in the plane perpendicular to the span. The shape and orientation of these trajectories are monitored at each spanwise location, by the phase difference $\Phi_{xy} = \phi_x - 2\phi_y$, where ϕ_x and ϕ_y are the local phases of the IL and CF responses. A nomenclature is adopted where the cylinder moves downstream when reaching CF oscillation maxima for $\Phi_{xy} \in]-180^\circ, 0^\circ[$ and upstream for $\Phi_{xy} \in]0^\circ, 180^\circ[$; these two types of trajectories are referred to as clockwise and counter-clockwise. The cases $\Phi_{xy} = 0^{\circ}$ and $\Phi_{xy} = \pm 180^{\circ}$ correspond to crescent-shaped orbits, bent downstream and upstream, respectively. A systematic analysis, for each $U^* \in [1, 35]$ where vibrations occur, shows that body motion is dominated (73%) by counter-clockwise trajectories and that the most frequent phase difference is $\Phi_{xy} \approx 20^{\circ}$, i.e. counter-clockwise orbit close to a crescent bent downstream. Comparable phasing properties were reported at much higher Re (Dahl et al. 2010). The time-averaged power coefficients, $C_{e\{x,y\}} = C_{\{x,y\}}\zeta_{\{x,y\}}$, are used to identify, in each direction, the spanwise regions of excitation $(C_{e\{x,y\}} > 0)$ and damping $(C_{e\{x,y\}} < 0)$ of the structure by the flow (⁻ denotes time-averaged values). Histograms of Φ_{xy} and $C_{e\{x,y\}}$ gathering all the cases are plotted in figure 5. The probability (P) associated with each histogram quadrant is specified in the plots and the most frequent trajectory is represented in figure 5(a). In spite of the low amplitudes of the IL responses, some connections appear between body trajectory and energy transfer. Counter-clockwise orbits are associated with excitation and damping of the structure in both directions, with a deviation towards damping in the CF direction versus excitation in the IL direction.

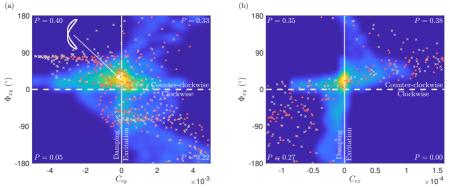


FIGURE 5. Flexible cylinder trajectory and flow-structure energy transfer at Re = 25 (L/D = 50): histogram of the IL/CF response phase difference and time-averaged power coefficient, in the (a) CF and (b) IL directions. Each histogram is normalized by the peak magnitude; the color code ranges from blue (0) to yellow (1). A vertical solid line separates the regions of excitation and damping of the structure by the flow (i.e. positive/negative values of $C_{e\{x,y\}}$) while a horizontal dashed line denotes the limit between clockwise and counter-clockwise orbits $(\Phi_{xy} = 0^{\circ})$; the probability (P) associated with each histogram quadrant is specified. The most frequent trajectory shape $(\Phi_{xy} \approx 20^{\circ})$ is represented in (a). The results obtained for L/D = 400 (§4) are superimposed on the histograms (gray crosses/red triangles for $U^* = 80/U^* = 110$).

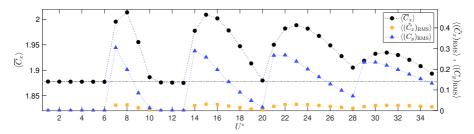


FIGURE 6. Force statistics at Re = 25 (L/D = 50), as functions of U^* : span-averaged values of the time-averaged IL force coefficient (left axis) and RMS values of the force coefficient fluctuations (right axis). A gray dashed-dotted line denotes the value of the IL force coefficient for a fixed rigid cylinder.

Clockwise orbits are less frequent but involved in more contrasted energy transfer trends. At higher Re, such orbits were often connected to vibration damping (e.g. Fan *et al.* 2019). Here, they are associated with IL vibration damping but CF vibration excitation.

Some statistics of fluid forces are reported in figure 6. The structural vibrations are accompanied by a slight amplification of the span- and time-averaged IL force, compared to the fixed, rigid cylinder case (gray dashed-dotted line) and by the emergence of force fluctuations which are quantified by their span-averaged, RMS values ($\langle \rangle$ denotes span-averaged values). As also observed for the structural responses, force fluctuations present substantially different magnitudes in each direction.

The principal features of the flexible cylinder, subcritical-Re VIV have been described from their emergence to the excitation of the first structural modes. Higher mode vibrations are examined in the next section.

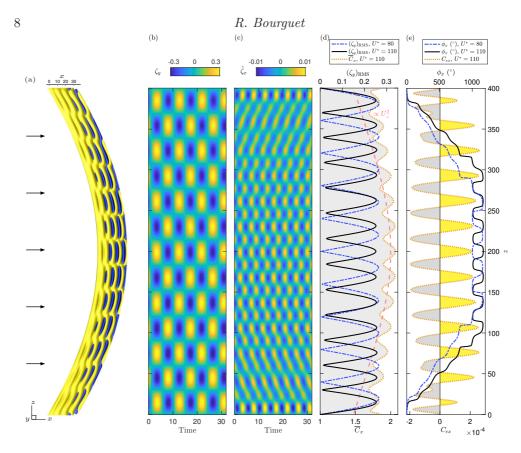


FIGURE 7. Flow-structure system behavior for L/D = 400 at Re = 25: (a) instantaneous isosurfaces of spanwise vorticity ($\omega_z \pm 0.07$) for $U^* = 110$ (arrows represent the oncoming flow; part of the computational domain is visualized, i.e. 35D downstream of the cylinder); (b,c) time series of the (b) CF and (c) IL displacement fluctuations along the span for $U^* = 110$; (d) spanwise evolution of the RMS value of the CF displacement for $U^* = 80$ and $U^* = 110$ (top axis) and time-averaged IL force coefficient for $U^* = 110$ (bottom axis; gray area); (e) spanwise evolution of the local phase of the IL response (ϕ_x) for $U^* = 80$ and $U^* = 110$ (top axis) and time-averaged power coefficient (C_{ex}) for $U^* = 110$ (bottom axis; regions of excitation/damping of the structure by the flow are represented by yellow/gray areas). In (d), a red dashed line indicates a possible trend of the mean force due to the cylinder streamwise deflection.

4. Higher mode responses

In order to extend the above analysis to higher mode vibrations, a flexible cylinder of aspect ratio L/D = 400 is considered in this section, for two high values of U^* , 80 and 110. The values of Re, m and γ are kept equal to 25, 6 and 0.

The cylinder is found to vibrate for both values of U^* . Figure 7(a-c) represents an instantaneous visualization of the wake, as well as selected time series of the CF and IL displacement fluctuations along the span, for $U^* = 110$. The vibration amplitudes are similar for both U^* values and are also comparable to those reported in §3, i.e. maxima close to 0.35 and 0.01 diameters in the CF and IL directions. Within the range of vibration frequencies identified in figure 3(d) and based on the natural frequencies in vacuum, 4 and 7 structural modes could be excited in the CF and IL directions for $U^* = 110$. However, it appears that in both studied cases, a single frequency is excited in each direction, with an IL/CF response frequency ratio of 2, as previously observed.

The CF responses remain essentially composed of standing waves. Their spatial struc-

tures are close to the 10th and 13th sine modes, as shown in figure 7(d) which represents the spanwise evolutions of the displacement RMS values (top axis). In the IL direction, as illustrated in figure 7(c), the central region of the cylinder ($z \in [100, 300]$) is characterized by dominant standing wave patterns while traveling waves develop on each side. The excited wavelengths correspond to the 19th and 25th modes for $U^* = 80$ and $U^* = 110$. The instantaneous IL responses remain symmetrical about the midspan point which is not necessarily the case for the CF responses (anti-symmetrical for $U^* = 80$). Another persistent trend in the IL responses, also visible in figure 3(c), is the presence of amplitude peaks near the body ends. As also reported for lower mode responses, the vibration frequencies ($f_y = 0.115$ and $f_y = 0.109$ for $U^* = 80$ and $U^* = 110$) are lower than the corresponding natural frequencies in vacuum ($f_{nat}(10) = 0.125$ and $f_{nat}(13) = 0.118$) and close to the corrected natural frequencies with $C_m = 1$ (0.118 and 0.111).

For both values of U^* , the flow and the body remain temporally and spatially locked, since the frequencies and spanwise structures of the flow and CF vibration coincide. The wakes exhibit cellular patterns comparable to those visualized in figure 4.

A complementary vision of the mixed standing-traveling waves identified in the IL vibrations is proposed in figure 7(e) which represents the response local phases (ϕ_x) for both U^* values. These plots confirm the transition from standing waves in the central region, with regular jumps near response nodes, to traveling waves moving towards cylinder ends on each side. This orientation of the traveling waves relates to the spanwise distribution of flow-structure energy transfer, as previously observed at higher Re (Bourguet *et al.* 2013). The energy transfer is quantified via C_{ex} in figure 7(e) (for $U^* = 110$). The structural waves propagate from the main region of excitation (central part) towards the regions where damping dominates (side parts). The global distribution of C_{ex} along the span appears to be determined by the profile of the inflow velocity component locally normal to the body (U_{\perp}) . This profile is sheared due to the streamwise deflection of the cylinder (visible in figure 7(a)), which is caused by the mean IL force. The main excitation region is found to be located in the area of maximum U_{\perp} , i.e. the central part.

The present VIV cases exhibit a wider variety of trajectory shapes than those examined in §3. IL/CF response synchronization remains however dominated (60%) by counterclockwise, figure-eight orbits. The values of Φ_{xy} and $C_{e\{x,y\}}$ obtained for $U^* = 80$ and $U^* = 110$ are superimposed on the histograms in figure 5 (gray crosses/red triangles). The general trends previously identified are found to persist and are even more clearly defined for the higher mode responses, in particular the excitation of CF vibrations through clockwise orbits while this orientation is associated with IL vibration damping.

Force statistics are comparable to those reported for lower mode responses, e.g. $\langle \overline{C}_x \rangle =$ 1.90 for $U^* = 110$. The local peaks of \overline{C}_x along the span coincide with CF response antinodes as shown in figure 7(d) (bottom axis); such coincidence is also observed for lower mode responses. The decreasing trend of \overline{C}_x towards the body ends can be connected to a scaling of the force by the inflow velocity component locally normal to the deflected body, i.e. $\propto U_{\perp}^2$ (red dashed line in figure 7(d)).

5. Conclusions

The subcritical-Re VIV of a flexible cylinder, pinned at both ends and immersed in a uniform current, have been investigated on the basis of numerical simulations. Vibrations were observed down to Re ≈ 20 , as previously reported for rigid cylinders. A constant value, Re = 25, was selected and the analysis was carried out in two steps: a monitoring of the system behavior as a function of U^* , from the emergence of VIV to the excitation

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of the first structural modes and then, a focus on higher mode responses. The typical features of the subcritical-Re VIV uncovered in this work can be summarized as follows.

A single vibration frequency is excited in each direction, with a ratio of 2 between the IL and CF responses. The flow, which is steady in the absence of vibration, becomes unsteady and its frequency coincides with CF vibration frequency. The peak amplitudes of the CF and IL vibrations are of the order of 0.35 and 0.01 body diameters, respectively. The CF vibrations are essentially composed of standing waves and their spatial structures are close to sinusoidal modes. The spanwise structure of the unsteady flow matches that of the CF vibration, i.e. the flow and the flexible body are not only temporally locked but also spatially locked. This synchronization is accompanied by the formation of cellular wake patterns. The IL responses exhibit less-regular evolutions, in particular with the development of traveling waves propagating from the central part of the cylinder towards its ends; this orientation can be related to the streamwise deflection of the body through the spanwise distribution of the regions of excitation/damping. The instantaneous IL responses are however found to remain symmetrical about the midspan point, which is not necessarily the case in the CF direction. The cylinder describes preferentially counter-clockwise figure-eight orbits, especially for the low mode responses where these orbits are generally close to a crescent-shaped trajectory, bent downstream. In spite of the low amplitudes of the IL responses, the orbit orientation appears to be connected to flow-structure energy transfer and different trends arise in the CF and IL directions.

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