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1 Independent Reaction Times method in Geant4-DNA: implementation

2 and performance.

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18 Abstract.

Purpose: The simulation of individual particle tracks and the chemical stage following water radiolysis in biological tissue is an effective means of improving our knowledge of the physicochemical contribution to the biological effect of ionizing radiation. However, the step-by-step simulation of the reaction kinetics of radiolytic species is the most time-consuming task in Monte
Carlo track-structure simulations, with long simulation times that are an impediment to research.
In this work, we present the implementation of the independent reaction times (IRT) method in
Geant4-DNA Monte Carlo toolkit to improve the computational efficiency of calculating G-values,

26 defined as the number of chemical species created or lost per 100 eV of deposited energy.

27 Methods: The computational efficiency of IRT, as implemented, is compared to that from 28 available Geant4-DNA step-by-step simulations for electrons, protons and alpha particles 29 covering a wide range of linear energy transfer (LET). The accuracy of both methods is verified using published measured data from fast electron irradiations for 'OH and e-aq for time-30 31 dependent G-values. For IRT, simulations in the presence of scavengers irradiated by cobalt-60 32 y-ray and 2 MeV protons are compared with measured data for different scavenging capacities. 33 In addition, a qualitative assessment comparing measured LET-dependent G-values with Geant4-34 DNA calculations in pure liquid water is presented.

Results: The IRT improved the computational efficiency by three orders of magnitude relative to step-by-step while differences in G-values by 3.9% at 1 μ s were found. At 7 ps, *OH and e⁻_{aq} yields calculated with IRT differed from recent published measured data by 5%±4% and 2%±4%, respectively. At 1 μ s, differences were 9%±5% and 6%±7% for *OH and e⁻_{aq}, respectively. Uncertainties are one standard deviation. Finally, G-values at different scavenging capacities and LET-dependent G-values reproduced the behavior of measurements for all radiation gualities.

41 **Conclusion**: The comprehensive validation of the Geant4-DNA capabilities to accurately simulate
42 the chemistry following water radiolysis is an ongoing work. The implementation presented in
43 this work is a necessary step to facilitate performing such a task.

45 1 Introduction.

46 Modeling the reaction kinetics of chemical species produced by radiolysis has important 47 applications in radiobiology and medical physics. At the cellular level, this modeling complements 48 the quantification of biological damage by accounting for the indirect contributions from the 49 radiolytic species, extending the knowledge of the effects of ionizing radiation in biological tissue. 50 Chemical reaction kinetics constitute a stochastic process that is in alignment with the capabilities of track-structure simulations using the Monte Carlo method. Together they 51 52 encompass the physical and chemical processes of the interaction of ionizing radiation with 53 biological tissue. Along the years, sophisticated Monte Carlo track-structure (MCTS) codes have been developed, including KURBUC¹, PARTRACK², RITRACKS³, TRAX-chem⁴, IONLYS-IRT⁵, and 54 Geant4-DNA ^{6–9}. In some cases, the codes have the capability to integrate geometry models, like 55 56 DNA in the cell nucleus, allowing the sampling of clustered DNA strand-breaks, which are the input of DNA repair models ^{1,10–14}. Until recently, MCTS codes have been restricted to the 57 58 laboratories where they were developed, and then, their use in biology or medical physics fields 59 have been limited, averaging only a few publications annually, as shown in Figure 1.



Figure 1 : Number of publications per year in biomedical science listed in PubMed. Search parameters: Geant4-DNA or Monte
Carlo track-structure. Search criteria: appeared in the abstract of publications. Search date: February 10, 2020.

More than 10 years have passed since the Geant4 Collaboration ^{15–17} released Geant4-DNA, today 64 the first open-source and multithreaded MCTS code ^{6–9}. Since 2013, this open source toolkit 65 66 provides models and tools to simulate the water radiolysis process, including the physical, prechemical, and chemical stages ^{18–20}. Geant4-DNA is under active development (e.g.,⁹). This work 67 is being done in parallel with the development of TOPAS-nBio, a wrapper to the toolkit to 68 69 facilitate track structure and chemistry simulation of complex geometries incorporating cell structures, including DNA²¹. The impact of Geant4-DNA in the medical physics field since its 70 71 introduction continues to increase (Figure 1). The development of Geant4-DNA is an ongoing 72 work that includes further refinement and validation of physical models, radiation chemistry 73 models, geometry models, damage scoring algorithms and computational efficiency improvement methods. 74

75 It is well known that MCTS codes demand a high computational cost. The overload is intrinsic due
76 to the calculation of each and every ionization along the track of charged particles through

77 matter. In addition, the use of the step-by-step method (SBS) for the realization of chemical 78 reactions between radiolysis products increases dramatically the computing time for the 79 simulation of biological effects (>99% of the execution time for an alpha particle of 4 MeV/u 80 simulated with Geant4-DNA). To mitigate this overload, at the physical stage the use of variance reduction techniques ²² and the combination of condensed-history and track-structure transport 81 82 ²³ have shown significant enhancement of the computational efficiency of Geant4-DNA 83 applications. For the chemical stage, the independent reaction times (IRT) technique has been 84 developed to reduce the computational burden of simulating the reaction kinetics of chemical species ^{24–26}. IRT has been implemented in several MCST codes, mainly for the calculation of time-85 dependent radiolytic yields ^{3,5,21,26–28}. Given its flexibility, the algorithm can also accommodate 86 87 the reaction of DNA molecules with reactive chemical species which leads to the estimation of 88 early DNA damage, as shown in plasmid models ²⁹ or the cell nucleus ¹². The high efficiency of IRT 89 relative to step-by-step, and its flexibility to simulate biological damage, make this method a 90 powerful tool with potential benefits to the research community. However, the availability of IRT, 91 like open source MCTS, has been limited. For these reasons, the Geant4 collaboration has started 92 to work actively on the implementation of this method in the code, either in its 93 original/traditional version, using synchronous algorithm adapted to the calculation of DNA 94 damage (Tran et al, submitted to Medical Physics), and an extended version that considers behavior of chemical species at boundaries ³⁰. A collective effort is also performed for comparing 95 96 all these variants in order to specify the limits and advantages of each of them, which strongly 97 depend on the applications.

In this work, we present details of the implementation and characterization of the IRT method in
 Geant4-DNA. We report the computational efficiency compared to SBS simulations and accuracy
 compared to experimental radiolytic yields. The implementation will be publicly released in
 forthcoming Geant4 version 10.7 Beta.

102

103 2 Methods.

104 2.1 The Independent Reaction Times.

105 The IRT method was developed to simulate reaction times in the diffusion kinetics process, as 106 part of the simulation of the diffusion and reaction of radiolytic species and their reactive 107 products following water radiolysis. The high computational efficiency of IRT compared to the 108 alternative SBS method is achieved by avoiding the burden of simulating the detailed trajectory 109 of each diffusing chemical species. In counterpart, this approach has the drawback of losing the 110 spatial information of each individual chemical species. Instead, an iterative process is performed 111 that begins at radiolysis and completes after all reactive species have reacted or an upper time 112 limit has been reached. Following the independent pairs approximation, the initial positions of 113 all the diffusive species produced at the end of the pre-chemical stage are used to simulate the 114 reaction times between reactive pairs using probability functions. These functions represent 115 solutions to the diffusion equation from the theory of diffusion kinetics. All the reactive pairs 116 along with their reaction times are assembled into an array that is sorted out in an ascendant 117 way according to reaction times. Subsequently, the realization of the reactions is performed by 118 removing from the array each reactive pair, starting with the pair with the shortest reaction time,

119 and inserting the reactive products, if any. Each time a product is created, the corresponding 120 reaction times with the remaining species in the array are sampled and resorted in an ascendant 121 way. The process is finished when all the possible combinations are exhausted or an upper time limit is achieved, typically the 10⁻⁷-10⁻⁶ s, signaling the end of the chemical stage, when the spatial 122 distribution of species are considered as homogeneous ³¹. Reactions with background solutions 123 124 can be simulated as pseudo-first-order reactions with the continuum approach, assuming they 125 are uniformly distributed in the background. In the continuum approach, each reactive species 126 reacts with the background following an exponential distribution probability given by 1 – exp(-127 k[B] t), where k[B] is the scavenging capacity of the solution ²⁶. For the implementation, the reaction times are obtained as $t = -\log(U)/k[B]$, where U is a random number uniformly 128 129 distributed between 0 and 1.

130 *2.1.1 Reaction schemes.*

140

131 The implementation presented in this work, extends the previous scheme for SBS simulations of Geant4-DNA ^{18,19} developed on top of totally diffusion-controlled reactions (when two chemical 132 133 species recombine with each other immediately at encounter), by incorporating the IRT method 134 including partially diffusion-controlled reactions (when two chemical species do not recombine 135 immediately when they encounter, ³²). The scheme to simulate the reaction times is based on the formalism developed^{25,33}, and later presented elsewhere^{3,5,26}. The reader is referred to these 136 137 publications for the mathematical details. The main probability functions are summarized below. 138 For totally diffusion-controlled reactions, the reaction times are sampled using the inverse of the 139 probability functions solved for time t, given by Equations 1 and 2 for reactions where at least

one chemical specie is neutral, and between charged particles, respectively.

141
$$P_{\rm I}(t \mid r_0) = \frac{\sigma}{r_0} {\rm Erfc}\left(\frac{r_0 - \sigma}{\sqrt{4Dt}}\right)$$
(1)

142 and,

143
$$P_{\rm III}(t \mid r_0) = \frac{\sigma_{\rm eff}}{r_{\rm eff}} \operatorname{Erfc}\left(\frac{r_{\rm eff} - \sigma_{\rm eff}}{\sqrt{4Dt}}\right)$$
(2)

144 where r_0 is the initial separation between chemical species, σ is the reaction radius and D is the 145 sum of the diffusion coefficients. For charged particles, r_{eff} and σ_{eff} are the effective separation 146 distance and effective reaction radius, respectively. These values are scaled from the natural 147 separation and reaction radius to consider a Coulomb potential and are related by the Onsager's 148 radius r_c as follows

149
$$r_{\rm eff} = \frac{-r_c}{1 - \exp(r_c/r_0)}$$
, and $\sigma_{\rm eff} = \frac{-r_c}{1 - \exp(r_c/\sigma)}$ (3)

150

For partially diffusion-controlled reactions, the probability functions are assigned to a random number U uniformly distributed between 0 and 1 (i.e. $P_{II}(r, t|r_0) = U$) and solved numerically to obtain the time, t. Equation 4 corresponds to reactions where at least one chemical species is neutral, rewritten in terms of the diffusion k_{diff} and activation k_{act} reaction rate coefficients for computational implementation.

156
$$P_{\rm II}(t \mid r_0) = \frac{k_{\rm act}}{k_{\rm diff} r_0 \alpha} \left[{\rm Erfc}\left(\frac{r_0 - \sigma}{\sqrt{4Dt}}\right) - W\left(\frac{r_0 - \sigma}{\sqrt{4Dt}}, -\alpha\sqrt{4Dt}\right) \right]$$
(4)

158 where, $\alpha = -(k_{act} + 4\pi\sigma D)/(4\pi\sigma^2 D)$ with k_{act} the activation reaction rate coefficient and 159 $W(x,y) = \exp(2xy + y^2) \operatorname{Erfc}(x + y)$. Equation 5 corresponds to reactions between charged 160 particles, rewritten in terms of k_{diff} and the observed reaction rate coefficient k_{obs} :

161

162
$$P_{\rm IV}(t \mid r_0) = \frac{\sigma_{\rm eff} k_{\rm obs}}{r_{\rm eff} k_{\rm diff}} [{\rm Erfc}(b) - W(b, a)]$$
(5)

163 where,

164
$$a = \frac{4\sigma^2 \alpha'}{r_c^2} \sqrt{\frac{t}{D} \sinh^2\left(\frac{r_c}{2\sigma}\right)}, \quad \text{and} \quad b = \frac{r_c}{4\sqrt{Dt}} \left[\coth\left(\frac{r_c}{2r}\right) - \coth\left(\frac{r_c}{2\sigma}\right) \right]$$
(6)

165 with α' given by,

166
$$\alpha' = \frac{k_{\rm act}}{4\pi\sigma^2} + \frac{r_c D}{\sigma^2 (1 - \exp(-r_c/\sigma))} \quad (7)$$

167

168 2.1.2 Implementation in Geant4-DNA.

Geant4-DNA, an extension of the Geant4 toolkit, is an object-oriented simulation toolkit written in C++ for the simulation of the passage of particles through the matter, the subsequent radiolysis and the reaction kinetics of chemical species. The software provides the tools distributed in C++ classes^a which include functionalities to build geometry models, specify particle sources, invoke physics process and chemistry process, scoring capabilities, etc. In this way, Geant4-DNA allows building sophisticated simulations for radiobiology research. Details of the architecture of Geant4

^a A C++ class is a user-defined concrete representation of a concept (i.e. a type), designed to provide a new type that has no direct counterpart among the built-in C++ types.⁶⁷

- and Geant4-DNA can be found elsewhere 6-9,17-20,34. Details of the implementation of IRT in
- 176 Geant4-DNA are presented here.
- 177
- 178



179

Figure 2 : Flowchart of IRT implemented in Geant4-DNA (version 10.7 beta, June 2020). G4ITTrackHolder, G4ITReactionSet,
 G4DNAMolecularReactionTable and G4MoleculeCounter classes are developments already available from the step-by-step
 implementation ¹⁹, ³⁵.

- 183 Figure 2 shows the flowchart diagram of the implementation of IRT in Geant4-DNA developed in
- this work (version 10.7 beta, June 2020). The dissociation channels of the pre-chemical stage
- 185 (Table 1) and the chemical reactions are declared and initialized in the chemistry class

constructor^b G4EmDNAChemistry option3, which includes the list of molecular chemical 186 187 species, chemical reactions and their type. The set of reactions implemented are those listed for the RITRACKS software elsewhere ³, see appendix A. Provisions are made within the class 188 189 constructor to facilitate activating or deactivating individual reactions in Geant4-DNA 190 applications. Parameters for the chemical reactions are pre-calculated in the 191 G4DNAMolecularReactionTable class. By the end of pre-chemical stage, the initial chemical 192 species are automatically stored in a vector defined in the **G4ITTrackHolder** class. From this class, 193 a loop is performed to identify all possible reactive pairs from all the initial chemical species. Subsequently, reactions at contact are evaluated using equation 8^{3,5,36} which overcomes the 194 195 cases when the interparticle distance is smaller than the effective reaction radius and hence the 196 IRT method cannot be used, for example in equation 1 the probability is greater than one if $r_0 < r_0$ 197 σ.

198
$$P_{\text{react}} = \frac{-\exp\left(-\frac{r_c}{\sigma + \varrho}\right)}{\exp\left(-\frac{r_c}{\sigma}\right) - \exp\left(-\frac{r_c}{\sigma + \varrho}\right) - \left(\frac{k_{\text{diff}}}{k_{\text{act}}}\right)\left(1 - \exp\left(-\frac{r_c}{\sigma}\right)\right)}$$
(8)

199 In equation 8, $\rho = 0.29$ nm, the approximate distance between neighboring water molecules; 200 and $P_{\text{react}} = 1$ for totally diffusion-controlled reactions ($k_{\text{act}} \rightarrow \infty$) as expected.

The identified remaining reactive pairs, defined internally as "reactions", are stored in the reaction list defined in the **G4ITReactionSet** class with their corresponding reaction time, called random reaction time (RRT in figure 2). The RRT values are sampled depending on the type of reaction using equations 1, 2, 4 and 5, whereas the adopted acceptance-rejection methods are

^b A constructor is a function with the explicit purpose of initializing objects (i.e. construct) of a give type.⁶⁷

described in detail elsewhere³. G4ITReactionSet uses an ordered multiset container to sort in 205 206 ascending order the RRT values. Subsequently, one more loop is performed for the realization of 207 reactions, that is, to remove from the reaction list the reactive pairs (named speciesA and 208 speciesB in Figure 2), starting with the pairs having the shortest RRT value. All remaining 209 "reactions" that include any of the reactive species involved are also removed. If chemical species 210 are produced by the reaction, then all of the possible reactive pairs along with the remaining 211 chemical species in G4ITTrackHolder are identified and inserted in the reaction list with the 212 corresponding RRT value. The spatial positions of the products are calculated with the position approach described elsewhere²⁴. Finally, the **G4MoleculeCounter** class counts the number of 213 214 chemical species and calculates G-values (number of chemical species produced or lost per 100 215 eV of deposit energy) as a function of time.

216



Figure 3 : A schematic illustration of the voxelization of the chemical track into cubic voxels of side length σ_{off} . The black points represent chemical species at the end of the pre-chemical stage, the yellow star indicates a target molecule, and the red voxels represent scanned regions, searching for the target molecule.

To reduce the computational burden of searching reactive pairs separated by long distances, we limit the search range for a reactive chemical species among its neighbors based on a confidence level for reaction. To this end, the simulation medium is voxelized into cubic voxels of side length σ_{off} (Figure 3), the searching range described elsewhere ¹⁹. The parameter σ_{off} was set to 550 nm, giving a 95% confidence level for the species with higher reaction rate (H₃O⁺, table 2). Thus, for a given chemical species, shown with a yellow star in Figure 3, all the possible reactions are searched within the 27 voxels around it (in 3-dimensions).

To incorporate the IRT method within the chemistry framework of Geant4-DNA, new classes have been developed among the Geant4 kernel classes. In this way, the users can easily swap between the SBS method or the IRT method in any physics list (e.g. selecting **G4EmDNAChemistry_option3** for IRT or **G4EmDNAChemistry up to option 2** for SBS), taking advantage of the features previously developed for the SBS method, described elsewhere ^{18,19}.

233

234 2.2 Verification.

235 2.2.1 Physical models and water dissociation scheme.

The simulation of the physical stage is done on a history-by-history basis, starting with a source particle traversing the geometry, ionizing atoms in its wake, followed by water radiolysis with diffusion and reaction of the reactive chemical species. For the simulation of physical interactions in liquid water (e.g. electronic excitation, ionization, elastic scattering, etc.), Geant4-DNA adopts a discrete approach ("track structure") in which all interactions are explicitly simulated, without the use of cuts for the control of the production of secondary particles. Such an approach ensures a better accuracy, particularly adapted to low energy (< 100 eV) and small dimension (< micrometer) particle tracking ³⁷. Geant4-DNA provides different sets of models for the simulation of physical interactions, assembled in "physics constructors" which assign each particle type to a list of physical interactions they can undergo along with the corresponding models needed to simulate such interaction. We previously described in detail the three alternative constructors currently available in Geant4-DNA, differing only by the theoretical approaches they adopt for the description of electron interactions and by their energy range coverage ⁹

250 For this study, we selected the "G4EmDNAPhysics_option2" physics constructor, which 251 provides the largest energy coverage for electrons in Geant4-DNA (7.4 eV to 1 MeV). In brief, this 252 constructor describes the interactions of electrons, photons, protons, neutral hydrogen, alpha particles and their charged states and heavier ions (⁷Li, ⁹Be, ¹¹B, ¹²C, ¹⁴N, ¹⁶O, ²⁸Si and ⁵⁶Fe). 253 254 Regarding electron interactions, this constructor describes inelastic processes based on the 255 formalism of the complex dielectric response function of liquid water, considering four ionization shells and five discrete electronic excitation states ³⁸. Ionization of the K-shell is calculated from 256 the Binary-Encounter-Approximation-with-Exchange model ³⁹. Regarding the modeling of elastic 257 258 scattering for electrons, for this work we have replaced the default model based on the partial wave theory by a newly developed model calculated using the ELSEPA code ^{40,41}. Regarding the 259 260 thermalization distance of sub-excited electrons, the model adopted is derived from Monte Carlo simulations using cross-sections of Michaud et al ⁴² for amorphous ice, scaled by Meesungnoen 261 et al ⁴³ to consider the difference between amorphous and liquid-phase water. The model is 262 applied with an upper energy limit of 7.4 eV. In the case of electrons induced by auto-ionization 263 264 of excited water molecules at the pre-chemical stage, the thermalization distance is obtained as if the electron has 1.7 eV of kinetic energy, based on empirical data. The effect of different
 thermalization models available in Geant4-DNA has been described elsewhere ²⁰.

267 The different parameters needed for the simulation of the physico-chemical and chemical stages of water radiolysis are gathered in a "chemistry constructor", which contains all 268 269 information available for simulation of the water molecule dissociation scheme, definition of 270 molecular species (including charge, mass, diffusion constant and van der Waals radius) and 271 chemical reactions they can undergo (including reaction rate coefficients). This constructor is 272 named "G4EmDNAChemistry_option3" and is designed exclusively for this IRT approach, 273 opposed to the other chemistry constructors available in Geant4-DNA, which are only used for 274 the SBS approach. The list of available constructors dedicated to the chemical stage simulation 275 are summarized in the table 1. The dissociation scheme of water molecules, following physical 276 ionizations or electronic excitations, and corresponding branching ratios implemented in this constructor, from ²⁰, are presented in the appendix (Table A1). In this constructor, for a complete 277 278 simulation of water radiolysis, 15 molecular species listed in Table A2 are available (instead of 7 for the SBS constructors ⁴⁴). In addition, the 72 chemical reactions listed in tables A3-A7 are 279 available (instead of 9 for the step-by-step constructors ^{45,46}). 280

28	2 Та	able 1	Chemistry	constructors	available	in Geant4-DNA
----	------	--------	-----------	--------------	-----------	---------------

Geant4-DNA Constructor	Description
G4EmDNAChemistry	First constructor implemented in Geant4-DNA for the chemistry processes with parameter values from Karamitros et al ^{18,19}
G4EmDNAChemistry_option1	Implements a revisited set of chemistry parameters used in Shin et al ²⁰
G4EmDNAChemistry_option2	Includes chemistry parameters for simulating reactions with DNA components.

	G4EmDNAChemistry_option3	Implements the IRT approach presented in this work.	
283			
284	2.2.2 Computational efficiency.		
285	The computational efficiency $arepsilon$, i	s a figure-of-merit that relates the computation time $ au$ spent	to
286	achieve a statistical variance, σ^2 :		
287			
288	$\varepsilon = (T\sigma^2)^{-1}.$	(8)	
289			
290	In this work, $arepsilon$ was used	to compare the computational efficiency of SBS and our IF	RT
291	methods for the calculation of ra	adiolytic yields, both implemented in Geant4-DNA as explaine	ed
292	above. Simulations using both	methods were performed to reach the same σ^2 for G-value	ue
293	calculations. We assume this car	n be achieved by simulating the same number of histories ar	nd

using the same processes to model the physical (particle tracks) and pre-chemical (radiolysis) stages. The computational efficiency enhancement of the IRT over the SBS method was quantified by the reduced ratio ε_R , defined as the ratio between the computation times to simulate only the chemical stages, T_{SBS} and T_{IRT} with $\sigma^2_{SBS} = \sigma^2_{IRT}$, calculated as follows:

298

$$\varepsilon_R = T_{SBS} T_{IRT}^{-1} \tag{9}$$

300

301 The quantity ε_R is reported as a function of the unrestricted linear energy transfer (LET), 302 averaged over simulated short track segments of electrons, protons or alpha particles. LET was 303 calculated as the accumulated energy deposited in the scoring region, including all secondary

electrons, divided by the primary track length ⁴⁷. For electrons, the simulation consisted of short 304 305 track segments of initially monoenergetic electrons positioned at the center of a water cube of 1 306 cm side. The transport of each primary electron was terminated immediately after its 307 accumulated energy loss exceeds a specific energy cut. Secondary electrons produced by inelastic 308 interactions were transported down to the lower energy cut of Geant4-DNA model limits, see 309 section 2.2.1. That criteria and energy cut values are given elsewhere ^{20,46}. For protons and alpha 310 particles, short tracks segments were generated by terminating the transport of the primary 311 particle at a pre-defined length. For protons, the track lengths ranged from 2.5 µm for the lowest energy value (0.5 MeV) to 20 µm for the highest energy value (100 MeV). For alpha particles, a 312 313 2.5 µm length was used for all the energy values (1 MeV/u to 12.5 MeV/u). The secondary 314 electrons were simulated down to the energy limits of the Geant4-DNA's ELSEPA model for elastic 315 scattering at 7.4 eV, section 2.2.1 and ⁴⁰. Reference simulations, in terms of computational 316 efficiency, were performed using the SBS method. For both IRT and SBS methods, 24 statistically 317 independent simulations were run using the same CPU unit and the same number of primary histories, which ranged from 5 to 600 per simulation job for the highest-LET (alpha 4 MeV/u) and 318 319 lowest-LET (electrons 1 MeV), respectively. Finally, ε_R was calculated using equation 9 and 320 reported as the mean with its statistical uncertainty at one standard deviation. In all the 321 simulations, the statistical uncertainty of the chemical yields was better than 0.5%, one standard 322 deviation.

324 *2.2.3 Time-dependent and LET-dependent G-values.*

The set of reactions used are listed in the Appendix section; see also section 2.1.1. Simulations performed to compare SBS with IRT used only those reactions available in SBS, as marked in the appendix section. The branching ratios for the dissociation of water molecules and electron attachment are described in section 2.2.1. The simulation setups are described in section 2.2.2.

The time evolution of chemical yields was calculated using the first 10 keV of energy loss from 1 MeV electron tracks, which is a conventional method to perform G-values calculation for fast electrons $^{20,46-48}$. At the sub nanosecond scale, calculated results were presented along with direct measurements of G-values in water for 'OH and e_{aq}^{-} from electron beams obtained with picosecond pulse radiolysis reported by 49 50 51 and 52. At the microsecond scale, G-values were calculated for comparison to those measured for electron beams from Muroya et al ⁵⁰ and ⁶⁰Co irradiation from LaVerne ⁵³ and Yoshida et al. ⁵⁴

For LET-dependent yields, G-values at 1 µs were calculated for comparison to compiled experimental data. In most of the experimental LET data, measurements were obtained in the presence of scavengers, while the calculations were performed in pure water. A suitable comparison requires reproducing the experimental conditions in the simulation as best as possible, for example, simulating the same scavenger system used in each experiment. The objective of this work was to verify the reproducibility of the behavior of the chemical yields as the ionization density increases.

344 *2.2.4 G-value calculation in the presence of scavengers.*

345 The capability of the IRT implementation to model the presence of scavengers was verified for 1 346 MeV electrons (first 10 keV of energy deposited) and 2 MeV protons. The feature to simulate 347 scavengers with the Geant4-DNA SBS was not available at this point. Simulations of the system containing glycylglycine at concentrations ranging from 10^{-4} M to 1 M (1 M = 1 mol dm⁻³) were 348 349 performed by adding the set of reactions (R1-R3). The bulk medium was made of liquid water (p 350 = 1 g cm⁻³) at neutral pH and ambient temperature. The yield of produced ammonium cation NH_4^+ from the scavenging of e⁻aq was calculated at the end of the chemical stage and compared with 351 experimental values for a range of scavenger capacities from Yoshida et at. ⁵⁴ for y-rays and from 352 LaVerne ⁵⁵ for protons. 353

354

 $^{+}NH_{3}CH_{2}CONHCH_{2}CO_{2}^{-} + e_{aq}^{-} + H_{2}O \rightarrow ^{-}CH_{2}CONHCH_{2}CO_{2}^{-} + NH_{4}^{+} + OH^{-}$ 355 356 $k_1 = 3.0 \times 10^8 / M/s$ (R1) 357 ⁺NH₃CH₂CONHCH₂CO₂⁻ + H[•] \rightarrow ⁺NH₃CH₂CONH[•]CHCO₂⁻ + H₂ $k_2 = 2.4 \times 10^6 / M/s$ 358 (R2) 359 ⁺NH₃CH₂CONHCH₂CO₂⁻ + [•]OH \rightarrow ⁺NH₃CH₂CONH[•]CHCO₂⁻ + H₂O $k_3 = 1.6 \times 10^8 / M/s$ 360 (R3) 361

362 3 Results.



363

Figure 4: LET-dependent computational efficiency of IRT implemented in Geant4-DNA relative to the SBS method. Results are
shown for electrons (red), protons (black) and alpha particles (blue). Error bars represent one standard deviation of statistical
uncertainty.

367

368 3.1 Computational efficiency.

In Figure 4, ε_R is shown as a function of LET for simulations with the IRT method implemented in Geant4-DNA, calculated as the ratio of time taken in the chemistry portion of the simulation using SBS and IRT for the same calculation precision (Equation 9). A substantial efficiency improvement of three orders of magnitude was achieved with the IRT method implemented in Geant4-DNA for the lower LET electron and proton simulations. As the LET increases for the electron source, ε_R is reduced to a still significant factor of two.



Figure 5: Calculated time dependent ratio between oxidative and reductive G-Values from the first 10 keV energy deposited by 1
MeV electrons (left) from Geant4 IRT (black points) and SBS (light gray points). Error bars represent combined statistical
uncertainty, one standard deviation. Time-depended G-values for *OH radical (center) and solvated electron (right) from IRT (black
lines) and SBS (light gray lines). Experimental data from pulse radiolysis are shown at shorter times with filled triangles⁵¹, empty
circles and dotted-dashed lines ⁵², dot-dashed lines ⁴⁹ (using a time correlation method) and filled circles ⁵⁰. At longer times, data
from ⁶⁰Co irradiations are shown with empty squares⁵³, filled circles ⁵⁰ and empty triangles⁵⁴. Experimental errors represent one
standard deviation.

385 3.2 Time-dependent and LET-dependent G-value.

386 *Time-dependent G-values.*

Figure 5 shows the time-dependent yields for the first 10 keV of energy deposited along 1 MeV
electron tracks. From the graph on the left of the figure, it is shown that the material balance
equation for oxidizing (•OH and H₂O₂) and reducing (e⁻_{aq}, H• and H₂) species is (almost) fulfilled
with a statistically significant systematic deviation of 0.3% for both IRT and SBS implementations.
Figure 5 also shows the time-dependent G-value for •OH radical and e⁻_{aq}. At the shorter
times, IRT and SBS calculations agreed within combined statistical uncertainties, as the same

393 physics models and pre-chemical dissociative channels were used. At longer times, IRT differed 394 from SBS by up to -3.8% \pm 0.1%, and -3.9% \pm 0.1% for •OH and e_{aq}^{-} , respectively.

For *OH, direct measurements from irradiations of electrons in pure water for the shorter time range (< 10 ns) from El Omar et al. ⁵¹ and Wang et al. ⁵² are shown. The magnitude of the experimental error is shown at a single time of 10^{-2} ns for clarity. The obtained decay of *OH yields from 7 x 10^{-3} ns to 8 ns for both IRT and SBS methods exceed the more recent experimental yields from Wang et al. ⁵² at 7 x 10^{-3} ns by 0.3 ± 0.12 molec./100 eV, one standard deviation. At 10^{3} ns, IRT and SBS exceed the experimental data by 0.22 ± 0.12 molec./100 eV and 0.32 ± 0.12 molec./100 eV, one standard deviation, respectively.

For solvated electrons, at the earliest times both IRT and SBS calculations agreed with direct measurements from Bartels et al⁴⁹, El Omar et al⁵¹ and Wang et al⁵², within one standard deviation of the experimental error. At longer times, calculated data from both methods agreed with the experimental data from Yoshida et al ⁵⁴ within one standard deviation.



Figure 6: Unrestricted LET-dependent G-values at 1 μs for electrons (black), protons (red) and alpha particles (blue). IRT
calculations are shown with solid lines connecting crosses and SBS are shown with dotted lines connecting empty circles.
Experimental data from γ-rays (black), proton or deuteron (red) and alpha particles (blue) are shown with symbols: filled square⁵⁶,
filled circle⁵⁷, filled triangle⁵⁸, filled diamond⁵⁹, star⁶⁰, inverted triangle⁶¹, filled polygon⁶², and semi filled circle⁶³. Experimental
error bars represent one standard deviation. The LET-dependent ratio between oxidative and reduction species is shown at the
bottom right panel. Error bars represent combined statistical uncertainty, one standard deviation.

413 *LET-dependent G-values.*

406

Figure 6 shows the LET-dependent G-value for electrons, protons and alpha particles calculated with IRT and SBS. The material balance equation, represented as the ratio between oxidative to reduced species as a function of the LET, is shown in the bottom right of Figure 6. The ratio reaches unity within statistical uncertainties for protons and alpha particles, but deviates from unity by 0.3% for electrons, as seen in Figure 6. Measured data from the literature are also displayed from different particles. For the chemical species displayed in Figure 6, the calculated
yields reproduce the change in the experimental data as the LET increases. That is, although the
yield of H[•] and H₂O₂ are significantly higher in the simulation than the experiments, the slope of
the yield with LET is in reasonable agreement.

- 423
- 424 *G*-value calculation in the presence of scavengers.

425 Modeling the presence of scavengers is shown in Figure 7 for the yield of NH₄⁺ produced by 426 electrons and protons as a function of the scavenging capacity. For electrons, calculated data 427 from LaVerne et al ⁵⁵ using IRT is also shown. The experimental data from cobalt-60 y-rays 428 irradiation, which result in a scavenging capacity comparable to electrons, is from Yoshida et al 429 ⁵⁴. As shown, a consistent agreement of the behavior of NH₄⁺ yields is fairly reproduced by the 430 Geant4-DNA implementation of IRT. For low energy protons, measured data are reported as track-averaged G-values while the IRT calculation is typically calculated with track-segment G-431 432 value, which is calculated over an almost constant LET across a short track-segment. The 433 comparison of both track-segment and track-averaged G-values are shown in Figure 7. The track-434 averaged G-values were obtained by integrating the G-values from short proton track-segments 435 from 2 MeV to 0.1 MeV, the limit of the Geant4-DNA models for protons. Results are consistent with calculated data from LaVerne et al ⁵⁵ where the G-values are also reported as a track-436 437 averaged quantity.



Figure 7 : Calculated NH₄⁺ yields with Geant4-DNA IRT (empty squares connected with solid lines) and from LaVerne ⁵⁵ (dashed
lines) at different scavenging capacities of glycylglycine. Electron irradiation (black) simulations are compared to measured data
for cobalt-60 from Yoshida et al ⁵⁴ (solid diamonds). Data for 2 MeV proton (red) simulations are compared to measured data
from LaVerne ⁵⁵ (filled circles.) For protons, both track-segment and track-averaged G-values are shown.

443

444 4 Discussion.

445 In this work, an implementation of the independent reaction times (IRT) in Geant4-DNA was 446 presented. A substantial improvement in the computational efficiency was achieved, up to three 447 orders of magnitude at low LET, decreasing as the particle LET increases. This decrease was 448 caused by the increase in the density of ionized and excited events from high LET particles 449 compared to low LET particles. As a consequence, the increased number of neighbor initial 450 chemical species looked by the IRT searching algorithm, as implemented, demanded more 451 operations as the complexity of this algorithm is O(N(N-1)/2). Thus, degrading in the efficiency 452 with increasing the LET was expected. Implementing a neighbor searching algorithm, for example, by adopting the kd-tree algorithm available in Geant4-DNA¹⁹, and the implementation 453

454 of a cutoff distance ²⁵ as a function of the LET, will potentially mitigate such reduction in 455 efficiency.

A systematic deviation of 0.3% from unity was found for the ratio between oxidative species to reduced species for electron tracks calculated with both SBS and IRT. The difference might be caused by the lack of dissociation scheme of the double ionized water molecules induced by Auger electrons produced by our implementation of the physics list, but are currently considered as single ionized water molecules in our simulation. However, this discrepancy is well below the experimental uncertainty of 5% typically reported, shown in the center and right panels of Figure 5, and is thus results in a negligible systematic error.

For time-dependent G-values a clear difference was found between IRT and SBS at longer 463 464 times, hence, also reflected in LET-dependent G-values. The differences might be attributed in 465 part to the independent pair approximation taken by the IRT approach whereas the SBS considers a multiparticle system ⁶⁴. Nevertheless, it has been shown that the yields calculated with SBS are 466 equivalent to IRT when using two-particle systems ^{3,24,65}. In addition, the G-values calculated with 467 468 the SBS approach depended to some extent on the minimum time step which is implemented in a dynamic time partition¹⁹. To quantify this effect, we calculated G-values for *****OH produced by 1 469 470 MeV electrons using a fixed minimum time step to 0.1 ps. While the G-value for solvated 471 electrons remained unaffected, our results showed that the G-value for 'OH reduced by 2.6% at 472 1 µs when the fixed minimum time step was used instead of the default values used by the dynamic time step (see table 4 in Karamitros et al ¹⁸). However, we kept the latter time step 473 configuration in all the simulations because the systematic difference, smaller than reported 474

475 experimental errors, was tolerated given the computational overhead of four-fold introduced by476 the use of a small-time step.

A significant overestimate of G-values, outside the experimental error of the latest 'OH 477 measurements from Wang et al ⁵², was found for both SBS and IRT at 10⁻² ns. The data from Wang 478 479 et al is the most recent data obtained at the shortest time following irradiation (7 ps). To resolve 480 this mismatch, a comprehensive revision of the current physical and water dissociative schemes 481 implemented in Geant4-DNA, following Wang et al ⁵² data, is encouraged. That revision task is an 482 ongoing work within our group that began with the revision of the physical models as reported recently²⁰. We expect that the revision of physical and pre-chemical processes also has a good 483 484 impact in the Geant4-DNA accuracy at the steady state (10³ ns), where currently a reasonable 485 agreement is found. Nevertheless, for e-aq a satisfactory agreement was found within the 486 experimental error over the entire time domain.

487 The evolution of G-values as a function of the particle LET were reproduced by both SBS 488 and IRT. The magnitude of the calculated yields was in reasonable agreement with measured 489 data for most of the species, considering the experimental uncertainties, and considering that 490 the measurements were performed in the presence of scavengers, while calculations were 491 performed in pure liquid water. A strict comparison between calculated and measured data 492 requires strict adherence to the experimental conditions in the simulations, including the 493 presence of scavengers, the comparison of track-averaged and track-segment G-values (Figure 494 5), and the implementation of the multiple ionization process, shown to improve the accuracy for H_2O_2 in the high LET range ^{28,66}. 495

496 5 Conclusions.

497 In this work, the Independent Reaction Times method that simulates the reaction kinetics 498 following the interaction of ionizing radiation was successfully implemented in Geant4-DNA. The 499 implementation achieves a substantial computational efficiency over the existing step-by-step 500 method (SBS) of Geant4-DNA by up to three orders of magnitude. Both methods achieve similar 501 accuracy when compared to experimental data of time-dependent and LET-dependent G-values. 502 The lack of consideration of partially diffusion-controlled reactions in the SBS with the selection 503 of a dynamic time step resolution causes a difference in G-values by 3.9% with respect to IRT data 504 at 1 µs. The capabilities of simulating systems with scavengers was demonstrated and showed 505 satisfactory agreement with experimental data. However, for 'OH radical yields, there was a 506 significant overestimate of 5% at the earliest time (7 ps) from recently measured yields. Further 507 work to resolve such differences is ongoing within our group. The implementation presented 508 here is a step forward to facilitate such studies.

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- 520 Appendix A
- 521 The list of reactions available in the Geant4-DNA IRT implementation are shown in Tables A1 to
- 522 A4. The classification is that proposed by Frongillo et al ⁵. The reaction rate coefficients are
- 523 from Plante and Devroye ³. The molar concentration M is equal to 1 mol dm⁻³
- 524
- 525

Table A1 Molecular dissociation scheme and branching ratios available in the "G4DNAChemistry_option3" chemistry constructor
 ²⁰.

Physical interaction	Scheme	Dissociation products	Probability
lonization	Dissociation	H ₃ O ⁺ + OH	1
Excitation	Dissociation	.0Н + Н.	0.65
(A1B1)	Relaxation	$H_2O + \Delta E$	0.35
Excitation	Auto-	$\mathrm{H_{3}O^{+}+^{\cdot}OH}+\mathrm{e_{aq}^{-}}$	0.55
(B1A1)	ionization		
	Dissociation	[•] OH + [•] OH + H ₂	0.15
	Relaxation	$H_2O + \Delta E$	0.3
Excitation	Auto-	$H_3O^+ + OH + e_{aq}^-$	0.5
(Rydberg,	ionization		
diffuse bands)	Relaxation	$H_2O + \Delta E$	0.5
Dissociative	Dissociation	$OH + OH^{-} + H_{2}$	1
attachment			
(H ₂ O ⁻)			

Recombination	Dissociation	'OH + 'OH + H ₂	0.15
electron-hole	Dissociation	.0Н + Н.	0.55
	Relaxation	$H_2O + \Delta E$	0.3

- 530 Table A2 Molecular species, diffusion coefficients and radii used for radiolysis simulation with IRT, from ³. *Available in the SBS
- 531 constructors and used also in IRT for the comparison studies of this work.

Molecular species	Diffusion	Radius (nm)
	coefficient	
	(10 ⁹ nm ² s ⁻¹)	
Н•	7.0*	0.19
•OH	2.2*	0.22
H ₂ O ₂	2.3*	0.21
H ₂	4.8*	0.14
e ⁻ aq	4.9*	0.50
H₃O⁺	9.46*	0.25
OH⁻	5.3*	0.33
O ₂	2.4	0.17
0 ₂ •-	1.75	0.22
HO [•] 2	2.3	0.21
HO ₂ -	1.4	0.25
O(³ P)	2.0	0.20
0•-	2.0	0.25
O ₃ •-	2.0	0.20
O ₃	2.0	0.20

- 534 Table A3 Totally-diffusion controlled reactions where at least one neutral particle is involved. Shaded reactions are used for the
- 535 comparison studies of this work.

Reaction type I	k _{obs} (/M/s)
$H^{\bullet} + e^{-}_{aq} \rightarrow H_2 + OH^{-}$	2.50 x 10 ¹⁰
$H^{\bullet} + H^{\bullet} \to H_2$	5.03 x 10 ⁹
H• + O(³ P) → •OH	2.02 x 10 ¹⁰
•OH + O(³ P) \rightarrow HO ₂	2.02 x 10 ¹⁰
H• + O• [_] → OH [_]	2.00 x 10 ¹⁰
$HO_2 + O(^{3}P) \rightarrow O_2 + ^{\bullet}OH$	2.02 x 10 ¹⁰
$O(^{3}P) + O(^{3}P) \rightarrow O_{2}$	2.20 x 10 ¹⁰

- 537 Table A4 Partially-diffusion controlled reactions where at least one neutral particle is involved. Shaded reactions are used for the
- 538 comparison studies of this work.

Reaction type II	k _{obs} (/M/s)	k _{diff} (/M/s)	k _{act} (/M/s)
•OH + $e^{-}_{aq} \rightarrow OH^{-}$	2.95 x 10 ¹⁰	3.87 x 10 ¹⁰	1.24 x 10 ¹¹
$^{\circ}OH + ^{\circ}OH \rightarrow H_2O_2$	5.50 x 10 ⁹	7.33 x 10 ⁹	2.21 x 10 ¹⁰
$^{\bullet}OH + OH^{-} \rightarrow O^{\bullet-} + H_2O$	6.30 x 10 ⁹	3.12 x 10 ¹⁰	7.89 x 10 ⁹
$^{\circ}\text{OH} + \text{HO}_2^- \rightarrow \text{HO}_2^{\circ} + \text{OH}^-$	8.32 x 10 ⁹	1.28 x 10 ¹⁰	2.38 x 10 ¹⁰
$^{\circ}OH + O^{\circ-} \rightarrow HO_2^{-}$	1.00 x 10 ⁹	1.49 x 10 ¹⁰	1.07 x 10 ⁹
$^{\bullet}\text{OH} + \text{HO}_{2}^{\bullet} \rightarrow \text{O}_{2} + \text{H}_{2}\text{O}$	7.90 x 10 ⁹	1.46 x 10 ¹⁰	1.72 x 10 ¹⁰
$^{\bullet}OH + H_2O_2 \rightarrow HO_2^{\bullet} + H_2O$	2.88 x 10 ⁷	1.46 x 10 ¹⁰	2.89 x 10 ⁷
$^{\bullet}OH + H_2 \rightarrow H^{\bullet} + H_2O$	3.28 x 10 ⁷	1.91 x 10 ¹⁰	3.29 x 10 ⁷
$^{\bullet}\text{OH} + \text{O}_2^{\bullet-} \rightarrow \text{O}_2^{+} \text{OH}^{-}$	1.07 x 10 ¹⁰	1.32 x 10 ¹⁰	5.74 x 10 ¹⁰
$^{\bullet}OH + O_{3}^{\bullet-} \rightarrow O_{2}^{\bullet-} + HO_{2}^{\bullet}$	8.50 x 10 ⁹	1.34 x 10 ¹⁰	2.34 x 10 ¹⁰
$H^{\bullet} + {}^{\bullet}OH \rightarrow H_2O$	1.55 x 10 ¹⁰	2.86 x 10 ¹⁰	3.39 x 10 ¹⁰
$H^{\bullet} + OH^{-} \rightarrow e^{-}_{aq} + H_2O$	2.51 x 10 ⁷	4.84 x 10 ¹⁰	2.51 x 10 ⁷
$e_{aq}^- + H_2O_2 \rightarrow OH^- + OH$	1.10 x 10 ¹⁰	3.87 x 10 ¹⁰	1.54 x 10 ¹⁰

$e^{-}_{aq} + HO_2^{\bullet} \rightarrow HO_2^{-}$	1.29 x 10 ¹⁰	3.87 x 10 ¹⁰	1.94 x 10 ¹⁰
$e^{-}_{aq} + O_2 \rightarrow O_2^{\bullet-}$	1.74 x 10 ¹⁰	3.70 x 10 ¹⁰	3.28 x 10 ¹⁰
$\mathrm{H_2O_2} + \mathrm{OH^-} \rightarrow \mathrm{HO_2^-} + \mathrm{H_2O}$	4.71 x 10 ⁸	3.11 x 10 ¹⁰	4.78 x 10 ⁸
$H_2O_2 + O_3(P) \rightarrow HO_2^{\bullet} + {}^{\bullet}OH$	1.60 x 10 ⁹	1.33 x 10 ¹⁰	1.82 x 10 ⁹
$\mathrm{H}_{2}\mathrm{O}_{2}\text{+}\mathrm{O}^{\bullet-} \rightarrow \mathrm{HO}_{2}^{\bullet} + \mathrm{OH}^{-}$	5.55 x 10 ⁸	1.50 x 10 ¹⁰	5.76 x 10 ⁸
$H^{\bullet} + HO_2^{\bullet} \rightarrow H_2O_2$	1.00 x 10 ¹⁰	2.82 x 10 ¹⁰	1.55 x 10 ¹⁰
$H^{\bullet} + H_2O_2 \rightarrow {}^{\bullet}OH + H_2O$	3.50 x 10 ⁷	2.82 x 10 ¹⁰	3.50 x 10 ⁷
$H^{\bullet}+O_2 \rightarrow HO_2^{\bullet}$	2.10 x 10 ¹⁰	2.56 x 10 ¹⁰	1.17 x 10 ¹¹
$H^{\bullet}+O_2^{-} \rightarrow HO_2^{-}$	1.00 x 10 ¹⁰	2.72 x 10 ¹⁰	1.58 x 10 ¹⁰
$H_2 + O_3(P) \rightarrow H^{\bullet} + {}^{\bullet}OH$	4.77 x 10 ³	1.75 x 10 ¹⁰	4.77 x 10 ³
$H_2 + O^{\bullet-} \rightarrow H^{\bullet} + OH^{-}$	1.21 x 10 ⁸	2.01 x 10 ¹⁰	1.22 x 10 ⁸
$OH^- + HO_2^{\bullet} \rightarrow O_2^{\bullet-} + H_2O$	6.30 x 10 ⁹	3.11 x 10 ¹⁰	7.90 x 10 ⁹
$OH^- + O_3(P) \rightarrow HO_2^-$	4.20 x 10 ⁸	2.93 x 10 ¹⁰	4.26 x 10 ⁸
$O_2 + O_3(P) \rightarrow O_3$	4.00 x 10 ⁹	1.23 x 10 ¹⁰	5.92 x 10 ⁹
$O_2 + O^{\bullet-} \rightarrow O_3^{\bullet-}$	3.70 x 10 ⁹	1.40 x 10 ¹⁰	5.03 x 10 ⁹
$\mathrm{HO}_{2}^{\bullet} + \mathrm{HO}_{2}^{\bullet} \rightarrow \mathrm{H}_{2}\mathrm{O}_{2} + \mathrm{O}_{2}$	9.80 x 10⁵	7.31 x 10 ⁹	9.80 x 10⁵
$\mathrm{HO}_{2}^{\bullet} + \mathrm{O}_{2}^{\bullet-} \rightarrow \mathrm{HO}_{2}^{-} + \mathrm{O}_{2}$	9.70 x 10 ⁷	1.32 x 10 ¹⁰	9.77 x 10 ⁷
$HO_2^- + O_3(P) \rightarrow O_2^{\bullet-} + {}^{\bullet}OH$	5.30 x 10 ⁹	1.16 x 10 ¹⁰	9.77 x 10 ⁹

540 Table A5 Totally-diffusion controlled reactions between charged chemical species. Shaded reactions are used for the comparison

541 studies of this work.

Reaction type III	k _{obs} (/M/s)
$e^{-}_{aq} + e^{-}_{aq} \rightarrow H_2 + OH^{-}$	6.36 x 10 ⁹
$H_3O^+ + OH^- \rightarrow H_2O$	1.13 x 10 ¹¹
$H_3O^+ + O_3^{\bullet-} \rightarrow {}^{\bullet}OH + O_2$	8.99 x 10 ¹⁰

- 543 Table A6 Partially-diffusion controlled reactions between charged chemical species. Shaded reactions are used for the
- 544 comparison studies of this work.

Reaction type IV	k _{obs} (/M/s)	k _{diff} (/M/s)	k _{act} (/M/s)
$e^{-}_{aq} + H_{3}O^{+} \rightarrow H^{\bullet}$	2.11 x 10 ¹⁰	1.26 x 10 ¹¹	2.53 x 10 ¹⁰
$e^{-}_{aq} + O^{-} \rightarrow 2 \text{ OH}^{-}$	2.31 x 10 ¹⁰	2.35 x 10 ¹⁰	1.44 x 10 ¹²
$e^{-}_{aq} + O_2^{\bullet-} \rightarrow H_2O_2 + 2 \text{ OH}^-$	1.29 x 10 ¹⁰	2.12 x 10 ¹⁰	3.29 x 10 ¹⁰
$e^{-}_{aq} + HO_2^{-} \rightarrow O^{\bullet-} + OH^{-}$	3.51 x 10 ⁹	2.14 x 10 ¹⁰	4.20 x 10 ⁹
$\mathrm{H_3O^+} + \mathrm{HO_2^-} \rightarrow \mathrm{H_2O_2}$	5.00 x 10 ¹⁰	7.71 x 10 ¹⁰	1.42 x 10 ¹¹
$H_3O^+ + O^- \rightarrow ^{\bullet}OH$	4.78 x 10 ¹⁰	8.13 x 10 ¹⁰	1.16 x 10 ¹¹
$H_3O^+ + O_2^{\bullet-} \rightarrow HO_2^{\bullet}$	4.78 x 10 ¹⁰	7.74 x 10 ¹⁰	1.25 x 10 ¹¹
$O^{\bullet-} + O^{\bullet-} \rightarrow H_2O_2 + 2 \text{ OH}^-$	1.00 x 10 ⁸	3.42 x 10 ⁹	1.03 x 10 ⁸
$0^{\bullet-} + 0_3^{\bullet-} \rightarrow 2 \ 0_2^{\bullet-}$	7.01 x 10 ⁸	5.58 x 10 ⁹	8.00 x 10 ⁸
$O^{\bullet-} + O_2^{\bullet-} \rightarrow O_2 + 2 \text{ OH}^-$	6.00 x 10 ⁸	5.70 x 10 ⁹	6.71 x 10 ⁸
$O^{\bullet-} + HO_2^- \rightarrow O_2^{\bullet-} + OH^-$	3.50 x 10 ⁸	5.81 x 10 ⁹	3.72 x 10 ⁸

546 Table A7 Reactions with H_2O , H_3O^+ and OH^- (scavenging capacity is provided), and first order reactions (reaction rate constant

547 *k*_{obs} provided) available in Geant4-DNA, but not used in comparison studies of this work.

Reaction	Scavenging capacity (s ⁻¹)
	or k _{obs}
$e^{-}_{aq} + H_2O \rightarrow H^{\bullet} + OH^{-}$	1.58 x 10 ¹
$O^- + H_2O \rightarrow OH + OH^-$	1.36 x 10 ⁶
$\mathrm{HO}_{2^{-}} + \mathrm{H}_{2}\mathrm{O} \rightarrow \mathrm{H}_{2}\mathrm{O}_{2} + \mathrm{OH}^{-}$	1.36 x 10 ⁶
$O_2^- + H_2O \rightarrow HO_2^{\bullet} + OH^-$	1.50 x 10 ⁻¹
$\mathrm{H}^{\bullet} + \mathrm{H}_{2}\mathrm{O} \rightarrow \mathrm{e}^{-}_{\mathrm{aq}} + \mathrm{H}_{3}\mathrm{O}^{+}$	5.94
$O_3(P) + H_2O \rightarrow 2 \cdot OH$	1.90 x 10 ³
$O_2^{\bullet-} + H_3O^+ \rightarrow HO_2^{\bullet-}$	4.73 x 10 ³
$O_3^{\bullet-} + H_3O^+ \rightarrow {}^{\bullet}OH + O_2$	8.90 x 10 ³
$e_{aq}^{-} + H_3O^{+} \rightarrow H^{\bullet}$	2.09 x 10 ³
$\mathrm{HO}_{2}^{-}\mathrm{+}\mathrm{H}_{3}\mathrm{O}^{+}\mathrm{\rightarrow}\mathrm{H}_{2}\mathrm{O}_{2}$	4.95 x 10 ³
$OH^- + H_3O^+ \rightarrow H_2O$	1.12 x 10 ⁴
$0^{\bullet-} + H_3 O^+ \rightarrow {}^{\bullet}OH$	4.73 x 10 ³

$H^{\bullet} + OH^{-} \rightarrow e^{-}_{aq} + H_2O$	2.49
$^{\bullet}OH + OH^{-} \rightarrow O^{\bullet-} + H_{2}O$	6.24 x 10 ²
$\mathrm{H_2O_2} + \mathrm{OH}^- \!$	4.66 x 10 ¹
$\mathrm{HO}_{2}^{\bullet} + \mathrm{OH}^{-} \rightarrow \mathrm{O}_{2}^{\bullet-} + \mathrm{H}_{2}\mathrm{O}$	6.24 x 10 ²
$O_3(P) + OH^- \rightarrow HO_2^-$	4.16 x 10 ¹
$0_3^{\bullet-} \rightarrow 0^{\bullet-} + 0_2$	2.66 x 10 ³
$\mathrm{HO}_{2}^{\bullet} \rightarrow \mathrm{H}_{3}\mathrm{O}^{+} + \mathrm{O}_{2}^{\bullet-}$	7.15 x 10⁵

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