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► To cite this version:

Olivier Bouaziz. An original unified approach for the description of phase transformations in steel during cooling: first application to binary Fe–C. Metallurgical Research & Technology, 2019, 116 (6), pp.615. 10.1051/metal/2019037 . hal-02968667

HAL Id: hal-02968667

<https://hal.science/hal-02968667v1>

Submitted on 16 Oct 2020

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An original unified approach for the description of phase transformations in steel during cooling: first application to binary Fe–C

Olivier Bouaziz*

Laboratoire d'Étude des Microstructures et de Mécanique des Matériaux (LEM3), CNRS, Université de Lorraine, Arts et Métier Paris Tech, F 57000, Metz, France

Received: 7 September 2018 / Accepted: 9 August 2019

Abstract. Exploiting Landau's theory of phase transformations, defining an original order parameter and using the phenomenological transformation temperatures, it is reported that it is possible to describe in a global approach the conditions for the formation of each constituent (ferrite, bainite, martensite) from austenite during cooling in steel. It allowed to propose a new rigorous classification of the different thermodynamic conditions controlling each phase transformation. In a second step, the approach predicts naturally the effect of cooling rate on the bainite start temperature. Finally, perspectives are assessed to extend the approach in order to take into account the effect of an external field such as applied stress.

Keywords: phase transformation / steel / austenite / ferrite / bainite / martensite / Landau / order parameter

1 Introduction

In the field of solid-state phase transformation in metallic alloys [1], the transformation of austenite in steel on cooling can occur by a variety of mechanisms including the formation of ferrite, bainite and martensite. The bainitic transformation occurs in a range between purely diffusional transformation to ferrite or pearlite and low temperature transformation to martensite by a displacive mechanism. Thus, the bainite transformation exhibits features of both diffusional and displacive transformations and has given rise to a large amount of research activity (see [2,3] for reviews). A major part of the research has concerned modelling of the kinetics of the transformations by detailed descriptions of the thermodynamic conditions operating at the interface [4–7]. However, the crucial understanding of the physically based conditions of the start of each phase transformation is less understood, especially for bainite.

Usually the Ar_3 temperature is defined as the maximum temperature for any phase transformation of austenite to ferrite during cooling [8]:

$$Ar_3(^{\circ}C) = 910 - 230C - 21Mn - 15Ni \quad (1) \\ + 45Si + 32Mo.$$

For temperature lower than Ar_3 , the basic tools of physical metallurgy are the definition of the martensite start temperature M_s and the bainite start temperature B_s expressed phenomenologically as functions of chemical composition as:

$$M_s(^{\circ}C) = 539 - 423C - 30.4Mn - 17.7Ni \quad (2) \\ - 12.1.Cr - 11Si,$$

where alloying element are expressed in weight(%) [9], and [10]:

$$B_s(^{\circ}C) = 870 - 270C - 90Mn - 37Ni \quad (3) \\ - 70Cr - 83Mo.$$

In addition, another characteristic temperature is defined as the temperature where austenite and ferrite has the same thermo-chemical free energy determined as [2,11]:

$$T_0(^{\circ}C) = 835 - 198.C - 91Mn - 36Ni \quad (4) \\ - 73Cr - 15Si - 87Mo.$$

In this publication, it is showed that it is possible to describe in a global approach the conditions for each phase transformation exploiting completely Landau's theory

* e-mail: olivier.bouaziz@univ-lorraine.fr

[12–15] of phase transformations including an original order parameter and to propose a new classification of the different phase transformation in steel during cooling and to predict naturally the effect of cooling rate on bainite start temperature.

2 The proposed approach

In the framework of Landau's theory [12–14], for a second order phase transition, the free energy is expressed as:

$$F(\chi, T) = F_0(T) + A(T) \cdot \chi^2 + C \cdot \chi^4, \quad (5)$$

where T is the temperature, χ the order parameter, $F_0(T)$ the thermo-chemical free energy, $A(T)$ a function of temperature and C a positive constant.

The simplest expression for $A(T)$ is:

$$A(T) = A_0(T - T_c), \quad (6)$$

with A_0 a positive constant and T_c a critical temperature where $A(T)$ changes of sign.

Usually in phase transformation of steels, $F_0(T)$ is known [2,3,7]. So, the identification of the total free energy $F(\chi, T)$ requires the determination of three parameters: A_0 , T_c , C .

For $T > T_c$, $F(\chi, T)$ exhibits one minimum as a function of χ :

$$\frac{\partial F(\chi, T)}{\partial \chi} = 0, \quad (7)$$

for $\chi = 0$

For $T \leq T_c$, $F(\chi, T)$ exhibits two minima as a function of χ :

$$\frac{\partial F(\chi, T)}{\partial \chi} = 0, \quad (8)$$

for

$$\chi = \pm \sqrt{\frac{A_0(T_c - T)}{2C}}. \quad (9)$$

In order to exploit this approach to a classification of phase transformations in steel, it is now assumed that:

$$T_c = B_s, \quad (10)$$

where B_s is the bainite start temperature.

By convention, it is chosen to have an order parameter for martensite:

$$\chi = \sqrt{\frac{A_0(B_s - M_s)}{2C}} = 1. \quad (11)$$

Giving a first relationship:

$$\frac{A_0}{2C} = \frac{1}{B_s - M_s}. \quad (12)$$

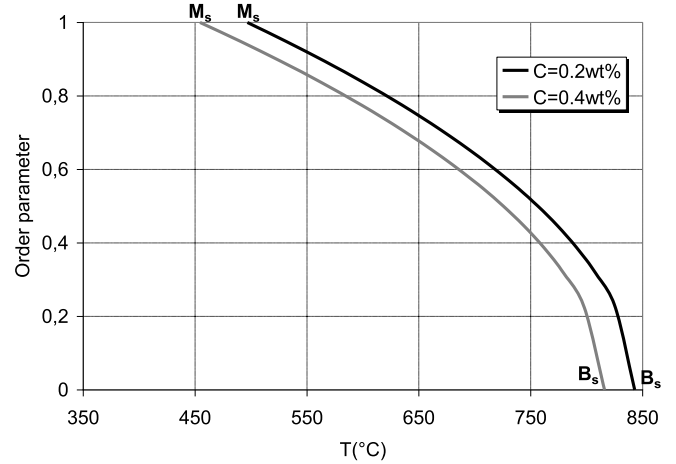


Fig. 1. Evolution of the order parameter from B_s to M_s temperatures for two different Fe–C compositions.

Therefore, the order parameter is:

$$\chi = \sqrt{\frac{B_s - T}{B_s - M_s}}. \quad (13)$$

As B_s to M_s temperatures depends on the carbon content, this one controls the order parameter.

In order to illustrate quantitatively this law, the evolution of the order parameter from B_s to M_s temperatures for two different Fe–C compositions has been plotted in Figure 1.

It is now proposed to define clearly what could be the parameter of order for phase transformation in steels. If C_f is the carbon content of the phase appearing, it is reasonable to propose that:

$$\chi = \frac{C - C_{\alpha,eq}}{C_\gamma - C_{\alpha,eq}}, \quad (14)$$

Where $C_{\alpha,eq}$ is the solubility of carbon in ferrite at equilibrium and C_γ is the carbon in austenite. So, the order parameter can be a sursaturation in carbon in the binary Fe–C system.

In addition, chemical free energy at M_s has been determined as [14]:

$$F_0(M_s, T) = F_0(M_s) + S_0 \cdot (T - M_s), \quad (15)$$

with $F_0(M_s) = 1250 \text{ J/mol}$ and $S_0 = -6.8 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$, which are independent of the composition.

The energy value $F_0(M_s)$ should correspond to the maximum at M_s for $\chi = 0$. As for any $T < B_s$ this maximum exists for the same value of $\chi = 0$, it is written for $M_s \leq T < B_s$:

$$F(0, T) = F_0(T - M_s) + F_0(M_s), \quad (16)$$

with

$$F_0(T - M_s) = S_0 \cdot (T - M_s), \quad (17)$$

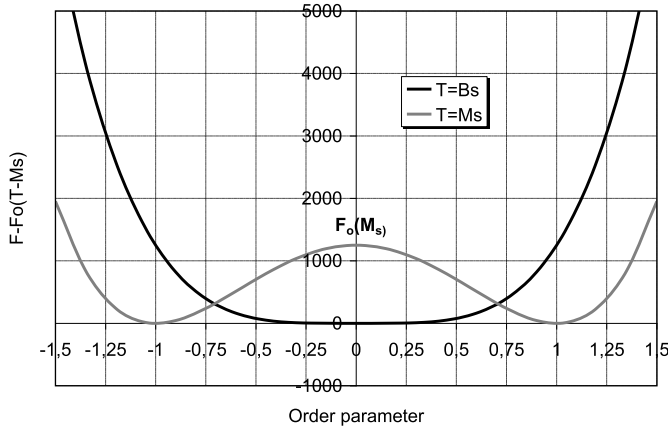


Fig. 2. Evolution of the $F(\chi, T) - F_0(T - M_s)$ as a function of the order parameter at B_s and at M_s temperatures.

when T is near M_s but it can be completely different for higher temperature.

In order to determine A_0 and C , as the total free energy at M_s for $\chi = 1$ has to be zero, it comes:

$$F_0(M_s) + A_0(M_s - B_s) + C = 0, \quad (18)$$

or

$$C = 2C - F_0(M_s), \quad (19)$$

and

$$C = F_0(M_s). \quad (20)$$

Consequently:

$$A_0 = \frac{2 \cdot F_0(M_s)}{B_s - M_s}. \quad (21)$$

Finally it is possible to express completely the free energy:

$$F(\chi, T) = F_0(T - M_s) + F_0(M_s) + \frac{2 \cdot F_0(M_s)}{B_s - M_s} (T - B_s) \cdot \chi^2 + F_0(M_s) \cdot \chi^4, \quad (22)$$

or

$$F(\chi, T) = F_0(T - M_s) + F_0(M_s) + F_0(M_s) \cdot \chi^2 \left(2 \cdot \frac{(T - B_s)}{B_s - M_s} + \chi^2 \right). \quad (23)$$

In order to highlight the key role of the order parameter, it has been drawn in [Figure 2](#). The evolution of the right-end side term of the expression:

$$F(\chi, T) - F_0(T - M_s) = F_0(M_s) + F_0(M_s) \cdot \chi^2 \left(2 \cdot \frac{(T - B_s)}{B_s - M_s} + \chi^2 \right). \quad (24)$$

Table 1. Classification of phase transformation conditions from austenite during cooling.

Phase	Free energy	Order parameter
Ferrite	$\frac{\partial F(\chi, T)}{\partial \chi} = 0$	$\chi = 0$
Bainite	$\frac{\partial F(\chi, B_s)}{\partial \chi} = 0$ $\frac{\partial^2 F(\chi, B_s)}{\partial \chi^2} = 0$	$T < B_s, \chi = \sqrt{\frac{B_s - T}{B_s - M_s}}$
Martensite	$F(\chi, M_s) = 0$ $\frac{\partial F(\chi, M_s)}{\partial \chi} = 0$	$\chi = 1$

Finally, the quantitative developed approach can be used in order to summarize the thermodynamic conditions for the formation of each phase, as it is summarized in [Table 1](#), providing more rigorous occurrence criterion especially to distinguish ferrite, bainite or martensite formation.

3 Extended approach including cooling rate

It is well known that B_s decreases if the cooling rate is increased. In order to capture this effect using the previous approach, it is assumed that a kinetic equation for the order parameter can be written for $T < B_s$ as:

$$\frac{\partial \chi}{\partial t} = -\eta \cdot \frac{\partial F(\chi, T)}{\partial T}, \quad (25)$$

where η is independent of χ and of T , giving for $T < B_s$:

$$\frac{\partial \chi}{\partial t} = \eta \cdot A_0 \cdot \chi^2. \quad (26)$$

Using equation (13), it is also possible to express:

$$\frac{\partial \chi}{\partial T} = \frac{-\sqrt{\frac{1}{B_s - M_s}}}{2 \cdot \sqrt{B_s - T}} = -\frac{1}{2 \cdot \sqrt{(B_s - T) \cdot (B_s - M_s)}}. \quad (28)$$

Therefore:

$$\frac{dT}{dt} = \frac{\partial \chi}{\partial t} / \frac{\partial \chi}{\partial T}. \quad (27)$$

It comes using equations (26) and (28):

$$\frac{dT}{dt} = -2 \cdot \eta \cdot A_0 \cdot \frac{(B_s - T)^{3/2}}{\sqrt{B_s - M_s}} \quad (30)$$

Combining with equation (21), we have:

$$\frac{dT}{dt} = -2 \cdot \eta \cdot F_0(M_s) \cdot \left(\frac{B_s - T}{B_s - M_s} \right)^{3/2} \quad (32)$$

Thus, the temperature T respecting equation (32) is:

$$T = B_s - (B_s - M_s) \cdot \left(\frac{-1}{2 \cdot \eta \cdot F_0(M_s)} \frac{dT}{dt} \right)^{2/3}, \quad (33)$$

with $\frac{dT}{dt} \leq 0$ during cooling. This temperature is the bainite start temperature affected by the cooling rate.

As $T \geq M_s$, equation (33) gives a critical cooling rate for $T = M_s$:

$$\frac{dT}{dt} = -2 \cdot \eta \cdot F_0(M_s) \quad (34)$$

In addition, a formula has been determined for the critical cooling rate in order to form 1% of martensite from austenite [16]:

$$\text{Log}(-C_r) = 4.5 - 2.7C - 0.95\text{Mn} - 0.18\text{Si} - 0.38\text{Cr} - 1.29(C \cdot \text{Cr}), \quad (35)$$

where C_r is expressed in °C/s.

Moreover, using equation (34) and (35), it is consistent to impose that:

$$2 \cdot \eta \cdot F_0(M_s) = C_r, \quad (36)$$

and

$$\eta = \frac{C_r}{2 \cdot F_0(M_s)}. \quad (37)$$

Finally, the law predicting the evolution of the bainite start temperature as a function of cooling rate is:

$$T = B_s - (B_s - M_s) \cdot \left(\frac{-1}{C_r} \frac{dT}{dt} \right)^{2/3}. \quad (38)$$

In order to illustrate quantitatively this law, the evolution of the bainite start temperature as a function of cooling rate for two different Fe–C compositions has been plotted in Figure 3.

4 Conclusions

Exploiting Landau's theory of phase transformations, defining an original order parameter and using the phenomenological transformation temperatures, it is reported that it is possible to describe in a global approach the conditions for the formation of each phase (ferrite,

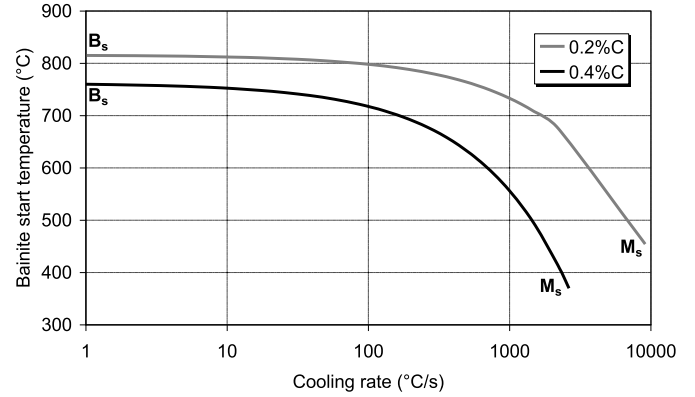


Fig. 3. Evolution of the bainite start temperature as a function of cooling rate for two different Fe–C compositions.

bainite, martensite) from austenite during cooling in steel. It allowed to propose a new rigorous classification of the different thermodynamic conditions controlling each phase transformation. In a second step, the approach predicts naturally the effect of cooling rate on the bainite start temperature. In perspectives, the approach can be extended to take into account external fields by adding a linear term in free energy linearly proportional to the order of parameter and proportional to the potential energy of the external field [12–14]. For instance, in the case of an uniaxial applied stress σ , the contribution to the free energy is expressed as:

$$F(\chi, \sigma) = \pm \frac{\sigma^2}{2 \cdot E} \cdot \chi, \quad (39)$$

where E is the elastic modulus and the sign depends on the compressive or tensile stress.

This term breaks the symmetry of the total free energy as a function of the parameter of order and it can change the occurrence conditions of each phase. A lot of experimental data are available in the literature in order to validate this last point which will be investigated in a next future.

Acknowledgement. The author thanks Dr. F. Levy for stimulating discussions.

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Cite this article as: Olivier Bouaziz, An original unified approach for the description of phase transformations in steel during cooling: first application to binary Fe–C, *Metall. Res. Technol.* **116**, 615 (2019)