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Proton Exchange Membrane Fuel Cell behavioral model suitable for prognostics

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Abstract

Prognostics and Health Management (PHM) is a discipline that enables the estimation of the Remaining Useful Life (RUL) of a system and is not yet much applied to Proton Exchange Membrane Fuel Cell PEMFC. However it could permit the definition of adequate conditions allowing extending PEMFC's too short life duration. For that purpose, a model that can reproduce the behavior of a PEMFC is needed. This paper presents a model of a PEMFC that could serve for a prognostics purpose. The model is composed of a static part and a dynamic parts that are independent. On one side, the static part is developed thanks to equations describing the physical phenomena and is based on the Butler-Volmer law. On the other side, the dynamic part is an electrical equivalency of physical phenomenon. The models are validated thanks to experimental data gathered in long term tests. For that purpose the parameters are successively updated based on characterization measurements (polarisation curves and EIS (electrochemical impedance spectroscopy)). Then the results of the model are compared to the ageing data in order to evaluate if the model is able to reproduce the behavior of the fuel cell. The usefulness of this model for prognostics is finally discussed.

Keywords: Proton Exchange Membrane Fuel Cell, Prognostics and Health Management, Behavioral Model, Static, Dynamic,

Nomenclature

η_a	Voltage drop at the anode	[V]
η_c	Voltage drop at the cathode	[V]
τ_{Oc}	Time constante of the diffusion convection impedance	[s]
b_a	Tafel anode parameter	V^{-1}
b_c	Tafel cathode parameter	$[V^{-1}]$
b_{Oc}	Parameter of the variation law of R_{Oc}	$[V^{-1}]$
C_{dca}	Double layer capacity at the anode	$[F/cm^2]$
C_{dcc}	Double layer capacity at the cathode	$[F/cm^2]$
E_n	Nernst Potential	[V]
i	Number of EIS realized at each characterizations	
j_{0a}	Exchange current density at the anode	$[A/cm^2]$
j_{0c}	Exchange current density at the cathode	$[A/cm^2]$
j_{0Oc}	Parameter of the variation law of R_{Oc}	$[A/cm^2]$
J_{AC}	Dynamic current density	$[A/cm^2]$
J_{DC}	Static current density	$[A/cm^2]$
J_{EIS}	Vector of the current densities for the EIS	$[A/cm^2]$
J_{pola}	Vector of the current densities for the polarization curve	$[A/cm^2]$
j_{Lc}	Limit current density at the cathode	$[A/cm^2]$
k	Number of characterizations	
k_{Oc}	Parameter of the variation law of τ_{Oc}	$[A.s/cm^2]$
L	Connectors' inductance	$[H.cm^2]$
R_m	Membrane resistance	$[\Omega.cm^2]$
r	Internal resistance (Static and Global model)	$[\Omega.cm^2]$
R_{Oc}	Module of the diffusion convection impedance	$[\Omega.cm^2]$
R_{ta}	Transfert resistance at the anode	$[\Omega.cm^2]$
R_{tc}	Transfert resistance at the cathode	$[\Omega.cm^2]$
U	Stack Voltage	[V]
U_{AC}	Dynamic stack Voltage normalised per cell	[V]
U_{DC}	Static stack Voltage normalised per cell	[V]
U_n	Stack voltage normalized per cell	[V]
W_{Oc}	Diffusion convection impedance	$[\Omega.cm^2]$

1. Introduction

PEMFC is a promising alternative to the actual production of energy but has got technical bolts as the distribution and the storage of dihydrogen as

well as a too short life duration [1]. In order to postpone the end of life, the development of Prognostics and Health Management (PHM) seems to be an adapted solution. The part of PHM that is highlighted here and that has not been investigated much in literature is Prognostics. The idea is to estimate the Remaining Useful Life of a system. For that purpose, as a starting point, a behavioral model, including ageing, of a PEMFC is needed. For modeling the behavior, different kinds of approaches can be highlighted, like data-based [2] or model-based [3], both largely present in the literature. However, neither of these models seems to fit the diagnostics purpose. Indeed, for examples, the ageing phenomena can hardly be added if only the micro phenomenon happening in the fuel cell are modeled [4]. For that purpose, a model-based approach is developed in this paper in order to have a good precision and even to model some important internal parameters of the fuel cell. A combination of a static and a dynamic model is proposed and fulfills the need of a model in an efficient way. Indeed, added to the positive aspects of a model-based approach, this model is rather easy to implement, has a high enough accuracy with the description of internal parameters, and the ageing can be easily included.

This paper is structured as follows. First a presentation of the path made toward a behavioral model usable for prognostics is drawn, then the model developed is presented. Next the updating procedure, i.e. the tuning of parameters' values is explained for finally studying the validation thanks to the comparison between the simulated behavior and experimental results.

2. Backgrounds

2.1. Prognostics and Health Management (PHM)

Every machine or system is deteriorating with time until reaching a faulty state. It can happen at an unsuitable time and trigger negative consequences as it prevents the system to ensure its mission. The maintenance could take a lot of time, and meanwhile, all the dependent systems are not able to carry on. Some loss of money or time and even security troubles can be triggered by this situation. PHM appears to be a solution to face this kind of problems [5]. Among the aims of PHM, the principals are:

- To improve the decision making process in order to increase the life duration of the system;
- To improve the availability and reduce the operational cost;

- To improve the security of the system.

PHM is described as composed of seven modules (figure 1) that allow defining the different steps followed in the process [6] . With a first part of observation composed by the data acquisition (module 1) obtained thanks to the sensors and by the data processing (module 2) which allows extracting some features. Then the analysis part is composed by modules 3, 4 and 5. Module 3 (condition assessment) aims defining the state of health of the system by detecting faults. Then, the module 4, diagnostic, assesses the origins of the faults. Module 5, prognostics, predicts the future state of health of the monitored system thanks to previous modules. It allows estimating the remaining useful life (RUL). The action part of PHM is composed by the last two modules. First, the decision support provides recommendations about the actions that should be taken to fulfill the mission while optimizing criteria like cost or time to failure. And then, the human-machine interface that allows the communication with the user but also the overall link between the modules.

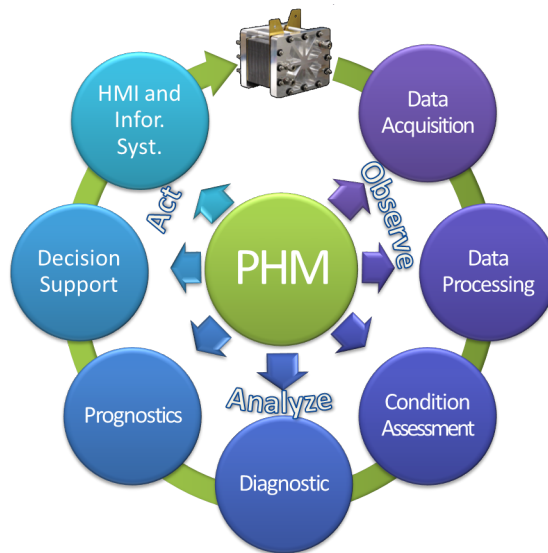


Figure 1: PHM modules adapted from[7]

2.2. PHM of fuel cell

Even though the PHM, under its denomination, has not been applied a lot to the fuel cell, but papers dealing with the different modules of PHM can be found in the literature. For example different authors [8, 9, 10, 11, 12, 13] develop the modules of the observation part and even diagnostics [12, 13, 14, 15, 16]. There is a lot of paper already dealing with diagnostics for the PEMFC and the previous steps. However, there are only few paper dealing with the step further which is PEMFC pronostics [17], on which focus this paper.

The ISO definition of prognostics is: “estimation of the operating time before failure and the risk of existence or later appearance of one or more failure modes”. It allows defining the Remaining Useful Life (RUL) that is according to the ISO standard [18] : “estimation of the time past between the current moment and the moment when the monitored machine is considered as failed”. So, prognostics aims at predicting the time left for the system to be functional. In this objective, approaches for prognostics [19] can be distinguished as follows:

- Data-driven [20, 21, 22] approaches aim at approximating and predicting the behavior of the system thanks to experimental data and without an analytical model of the underlying phenomena. Those approaches are usually performed thanks to machine learning tools like neural network. This kind of approaches is generally simple to implement but has no link with the internal phenomenon. It is then not possible to correlate the state of health observed or predicted with the real physic happening. These approaches are effective if a large amount of data is available, which is not always the case.
- Model-based approaches are based on the description of the physical phenomena happening. Equations developed thanks to a precise study of the behavior based on global knowledge as for exemple, chemistry or electronics is the startpoint of this approach. Indeed, the failure criteria developed in this approach are the description of the failure mechanisms by explicit mathematical representation. This approaches are reliable but require a precise knowledge of the physics phenomenon happening in order to be able to model it.
- Hybrid approaches are based on the two last approaches. The idea is, here, to try to combine the first two methods in order to have a more

accurate and reliable result. Effort has to be made to avoid a too high computational cost and to reach a satisfying applicability.

The classification of the physic-based approach can be discussed. Indeed, even though the model is based on the description of the physical phenomenon, data are needed in order to obtain appropriate parameters of the model.

The models of PEMFC that can be found in the literature cover different approaches from physic-based to data-based. Data driven approaches won't model any physic phenomenon and will need a significant amount of data for the learning phase. They can be represented as black boxes [20]. They presents more or less the same drawbacks than the data-driven approach of prognostics and don't comply with our needs. Then it was chosen to study only the physical-based as this kind of approaches has not been developed yet for our purpose but also because it would allow keeping a strong link with the actual physical phenomenon. The physic-based model describe the physic phenomenon happening. Some are formalized thanks to an electrical equivalency [23, 24, 25, 26], while others directly exploit the physical and chemical equations [27, 28, 29, 4, 30].

The black box modeling has already been investigated [21, 31]. The physical based approach is developed with this first step of modeling. It would allow gaining in precision and even adding some possible analysis as some internal parameters with a physical meaning are represented. In this work, we choose to develop a physics-based approach applied on a PEMFC stack as the stack is defined as the object of the study (excluding the other components of the PEMFC system).

3. Literature review: Towards an analytical behavior model

Numerous works has been analyzed in order to define and identify a model that would comply with the PHM needs. A synthesis is shown thanks to the table 1.

3.1. Aims of the models

The goal of the model should be convenient for a prognostics use. A comprehensive model could be usable, but the development should present a capacity of adaptation as allowing the addition of a new input without too much burden. A model for comprehensive purpose is a model which

aims understanding the interaction between different electrochemical mechanisms. The claimed objectives are variables: Fouquet et al. [23] developed their model for diagnostic purpose, while Siegel et al. [27] objective is comprehension whereas for Hinaje et al. [32] it is a development that would allow the control. In other references, the underlying aim is not always given, even if it is a capital fact, as a model developed for purpose of design [33] won't fit most of the time for another application.

3.2. Boundaries of the model

The boundaries of the expected model are the terminal of the stack as it is the stack's RUL which is here investigated. The modeled objects differ also among the papers. The ones that model the whole system or a part of it [34] haven't been retained as it is beyond the scope of this study. Some models concern a single cell [4, 24, 27, 28, 29, 32]. Fouquet et al [23] use a model of a single cell, and extend it for modeling a stack. It is the same for Shan et al. [35] that presents a cell model and then use it for modeling a stack. So, some models of single cell can match with our needs, if they can be extended to a stack, implying a few assumptions or modifications. Finally some authors model directly stacks [3, 25, 36].

3.3. Static or dynamic models

A static model would be convenient as the objective is to model the behavior for a long time scale under a constant load in a first step. But a dynamic model would be convenient as it brings more precision on the behavior's description and would make the model more reliable under variable load. However it is an open question. Defining a model as static or dynamic is not an easy task. Indeed, there is no clear agreement in the literature about a definition. A model with a time dependency can be considered as dynamic regardless to the value of the time constant, while for some authors a model with a low time constant is a static model. Thus, some models are labeled as dynamic as [4, 25, 30, 35] whereas other as static [23] but not always with the same definition. However a lot of authors don't even define the nature of their model, and some can appear static [24, 27] or dynamic [36] with the analysis of their work face to our definition.

3.4. Space and time scale

The space scale of the phenomenon described in the models is also variable as well as the dimension of the model. A thin granularity, down to the

nanometer, is often linked to a high dimension description and suits more the design purposes. A review of this kind of models is available [37], with detailed models of precise phenomena. For prognostics purposes, a 1D or even 0D model should be precise enough and have a compatible computing cost [23, 24, 27, 28, 29, 36]. Furthermore, the time scale of the phenomena retained in the description doesn't need to be low as thousands of hours as simulated time might be necessary to forecast the RUL. However, the fastest phenomena can be kept then neglected in a second step if necessary.

3.5. Degradation already included in the model

As our final final need is to model the ageing, a model that includes some degradation would present advantages. For example Fouquet et al. [23] characterize the flooding and drying of the membrane in order to classify the degraded operating modes of the fuel cell. Lee et al. [24] as well as Laffly [38] did try to model the ageing by fitting parameters' evolution with polynomial function. In their work, Robin et al. [3] tried to model the Pt surface degradation mechanism.

3.6. Validation of the models

The model should have been validated with experiments to be reliable enough.

The validation strategies are variable too, as some authors validate their models thank to experimentations [33, 36], some others thanks to comparison done with other publication [39], or even with equations solver results [32]. Lee et al. [24] validate their model by evaluating the fitting of their curve with the real data, it means that it is the evaluation of the parameters and the shape of the model that are validated on the example not its predictive ability. Hou et al. [36] evaluate the parameters thanks to experiments and then, validate them thanks to another test on another stack.

3.7. Synthesis and discussion

Table 1 presents the characteristics of each model versus all the criterion. At the first sight, on table 1, some model appear to fulfil the criteria but a deeper analysis is needed:

1. The model of Robin et al. [3] presents a combination of an analytical model and a semi-empirical one. A degradation : the Pt surface degradation is included in this model. But the need of the local partial pressure is a strong limitation of this model.

2. The model of Fouquet et al. [23] is an electrical equivalent circuit that is based on Randles model but improved with a Constant Phase Element. However in this model the two electrodes are not separated, which decreases the level of information.
3. The model of Reggiani et al. [25] is a model based on an electrical equivalent circuit. This model doesn't present enough precision for the purpose here as the model proposed doesn't go really deep in the the phenomenon modeled, for example, there is not differentiation between anode and cathode. The gain of using a physics-based approach would not be as great as expected because the hypothesis of simplification are pushed too far.
4. The model of Hou et al. [36] is a model that has an objective really focused, indeed, models for the voltage overshoot and undershoot are developed here. So these models are not complete enough for the purpose of this paper.

As no model that could be found in literature complies with each criterion (table 1), a new model is presented in this paper that is more adapted to our need of prognostics purpose.

4. Behavioral model description

4.1. Overall presentation

The proposed behavioral model is depicted in figure 2. The only input of this model is the current which is then normalized in the current density to be decomposed in direct and alternating current densities thanks to a low pass filter. These current densities are then used as the inputs of the models in order to furnish the output that are direct and alternating voltage per cell which are finally recomposed in voltage per cell to be denormalized in voltage.

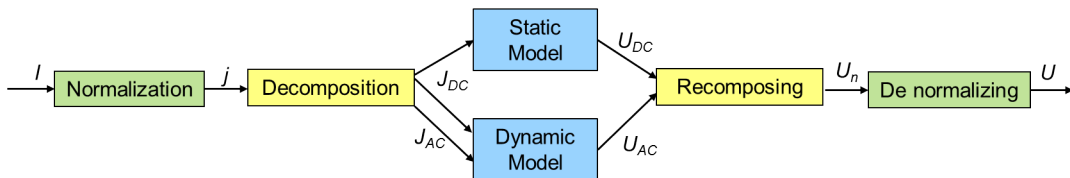


Figure 2: Scheme of the model

Ref.	First author	Model type	Aim	Object modeled	Static or dynamic	Degradation
[3]	Robin	Physical & chemical desc.	Comprehensive	Stack	Dynamic	Modeled
[39]	Asl	Phys. & chem. des. & electrical eq. circuit	Not clearly defined	Stack	Dynamic	No
[23]	Fouquet	Electrical equivalent circuit	Diagnostic	Cell → stack	Dynamic	Characterized (Classified)
[24]	Lee	Electrical eq. circuit	Diagnostic	Cell	Static	Modeled
[25]	Reggiani	Electrical eq. circuit	Not clearly defined	Stack	Dynamic	No
[26]	Lazarou	Electrical eq. circuit	Not clearly defined	Cell → stack	Dynamic	No
[27]	Siegel	Physical & chemical des.	Comprehensive	Cell	Static	No
[28]	Martins	Physical & chemical des.	Not clearly defined	Cell	Static	No
[29]	Chevalier	Physical & chemical des.	Diagnostic	Cell	Static	Modeled
[4]	Ceraolo	Physical & chemical des.	Not clearly defined	Cell	Dynamic	No
[30]	Philipps	Physical & chemical des.	Not clearly defined	Cell → stack	Dynamic	No
[32]	Hinaje	Phys. & chem. des. & electrical eq. circuit	Control	Cell	Dynamic	No
[33]	Park	Phys. & chem. des. & electrical eq. circuit	Conception	Cell → stack	Dynamic	No
[35]	Shan	Physical & chemical des.	Conception	Cell → stack	Dynamic	No
[36]	Hou	Logarithmic & semi-empirical	Not clearly defined	Stack	Dynamic	No

Table 1: Synthesis table of the literature study

The objective of a prognostic approach is to be able to reproduce the behavior of the system in order to obtain information estimated like the state of health (SOH) or the remaining useful life (RUL). It is in this frame that this model appears to be exploitable for prognostics (figure 3). Indeed, thanks to the model and to ageing data, the prognostic approach can be developed, this would allow providing the informations needed for the next steps of PHM, i.e. the decision process.

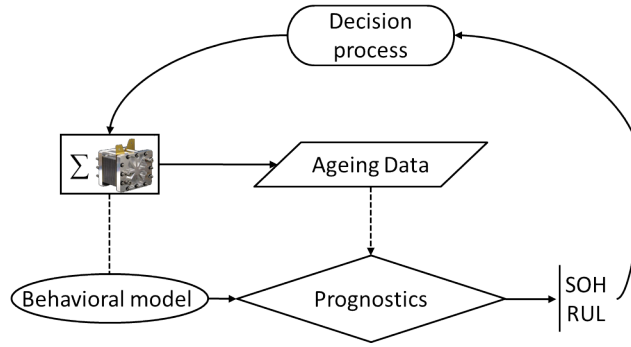


Figure 3: Insertion of the model in prognostics

4.2. Static part of the model

The static model based on the Butler-Volmer law is in a first step a variation law that takes into account the activation phenomenon at the cathode and at the anode by the two voltage drop η_a et η_c .

$$U_{DC} = E_n - r \cdot J_{DC} - \eta_a - \eta_c \quad (1)$$

Where r is the internal resistance of the fuel cell, J_{DC} the static current density and E_n the Nernst potential.

With the hypothesis that the influence of the hydrogen diffusion can be neglected face to the oxygen ones, the final expression is (2). Indeed during measurements it can be noticed that the diffusion at the cathode has a bigger influence than the diffusion on the anode side [38]. With at the anode and cathode :

- b_a, b_c the Tafel parameters;
- j_{0a}, j_{0c} the exchange current density;

- j_{Lc} the limit current density at the cathode only.

$$U_{DC} = E_n - r \cdot J_{DC} - \frac{1}{b_a} \cdot \operatorname{asinh} \left(\frac{J_{DC}}{2 \cdot j_{0a}} \right) - \frac{1}{b_c} \cdot \operatorname{asinh} \left(\frac{J_{DC}}{2 \cdot j_{0c} \cdot \left(1 - \frac{J_{DC}}{j_{Lc}} \right)} \right) \quad (2)$$

4.3. Dynamic part of the model

Here, the aim is to link the voltage variation to the current variation, with the hypothesis that the variations are around a static operating point.

4.3.1. Summary of the model

The phenomena that are represented in the dynamic model are expressed thanks to an electrical equivalency (figure 4). Indeed, the multi-physical phenomena are represented by electrical impedances with a similar behavior :

- A part of the diffusion convection of the different gases at the cathode is modeled by a Warburg impedance.
- The double layer capacities at the interface electrode-electrolyte on the anode and cathode are modeled respectively by capacitor C_{dca} and C_{dcc} .
- Two transfer resistances R_{ta} and R_{tc} represent the electrons transfer at the electrodes.
- The ionic conductance of the membrane is modeled by an equivalent resistance R_m . A different writing than the internal resistance on the static part as they are here not linked yet.
- And finally, the inductive behavior due to the connectors is taken into account by an inductance L_{con} .

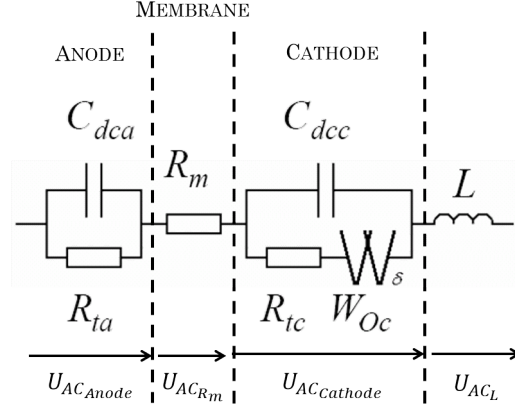


Figure 4: Electrical equivalency of the dynamic model

4.3.2. Warburg impedance

The Warburg W_{Oc} is defined by its module R_{Oc} and its time constant τ_{Oc} expressed in the Laplace space(eq. (3)).

$$W_{Oc}(p) = R_{Oc} \cdot \frac{\tanh(\sqrt{\tau_{Oc} \cdot p})}{\sqrt{\tau_{Oc} \cdot p}} \quad (3)$$

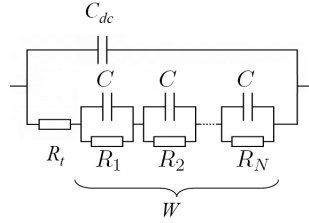


Figure 5: Electrical equivalent circuit of an electrode with a Warburg represented by N RC filter in series

An equivalence for this impedance is a network of n RC filters in series (figure 5). The values of the parameters R_n (eq. (4)) and C (eq. (5)) are as follows.

$$R_n = \frac{8 \cdot R_{Oc}}{(2 \cdot n - 1)^2 \cdot \pi^2} \quad (4)$$

$$C = \frac{\tau_{Oc}}{2 \cdot R_{Oc}} \quad (5)$$

The equivalent impedance then have for expression (eq. 6), with R_n developed on (eq. (4)) and N_{eq} the number of RC filters :

$$W_{O_{ceq}}(p) = \sum_{n=1}^{N_{eq}} \frac{R_n}{1 + R_n \cdot C \cdot p} \quad (6)$$

When using more than 5 RC filters the error between the model and the measures is under 4%. Yet the experiment measures error have the same order of value, we can consider that 5 filters are enough as up to 5 filters.

4.3.3. State space representation

The equivalent electrical circuit is then expressed thanks to a state space representation in which each electrode has a state space representation. We consider that the current density is well separated in its static J_{DC} and dynamic part J_{AC} as they are the different input for the static and the dynamic model.

A state space representation is expressed as :

$$\dot{X} = A \cdot X + B \cdot U \quad (7)$$

$$Y = C \cdot X + D \cdot U \quad (8)$$

For the anode (figure 4), with no diffusion convection impedance, the state vector is (eq. (9)) and the matrix of the representation are (eq. (10), (11), (12) and (13)) :

$$X = [I_{R_{ta}}] \quad (9)$$

$$A = \left[-\frac{1}{R_{ta} \cdot C_{dca}} \right] \quad (10)$$

$$B = \left[\frac{1}{R_{ta} \cdot C_{dca}} \right] \quad (11)$$

$$C = [R_{ta}] \quad (12)$$

$$D = [0] \quad (13)$$

The state space representation at the anode is thus finally (eq. (14)):

$$\begin{cases} \left[\dot{I}_{Rta} \right] &= \left[-\frac{1}{R_{ta} \cdot C_{dca}} \right] \cdot \left[I_{Rta} \right] + \left[\frac{1}{R_{ta} \cdot C_{dca}} \right] \cdot \left[j_{AC} \right] \\ \left[U_{AC_{Anode}} \right] &= \left[R_{ta} \right] \cdot \left[I_{Rta} \right] \end{cases} \quad (14)$$

For the cathode, with one diffusion convection impedance, the state vector and the matrix of representation are given bellow on equations (15), (16), (17), (18) and (19). Where V_i is the voltage across the i^{th} RC cell of the equivalent circuit of the Warburg.

$$X = \begin{bmatrix} V_1 \\ V_2 \\ \dots \\ V_N \\ I_{Rtc} \end{bmatrix} \quad (15)$$

$$A = \begin{bmatrix} \frac{-1}{R_1 \cdot C_{eq}} & 0 & \dots & 0 & \frac{1}{C_{eq}} \\ 0 & \frac{-1}{R_2 \cdot C_{eq}} & \dots & 0 & \frac{1}{C_{eq}} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \dots & \frac{-1}{R_N \cdot C_{eq}} & \frac{1}{C_{eq}} \\ \frac{-1}{R_{tc} \cdot R_1 \cdot C_{eq}} & \frac{-1}{R_{tc} \cdot R_2 \cdot C_{eq}} & \dots & \frac{-1}{R_{tc} \cdot R_N \cdot C_{eq}} & -\frac{N}{R_{tc} \cdot C_{eq}} - \frac{1}{R_{tc} \cdot C_{dca}} \end{bmatrix} \quad (16)$$

$$B = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ \frac{1}{R_{tc} \cdot C_{dca}} \end{bmatrix} \quad (17)$$

$$C = [1 \quad 1 \quad \dots \quad 1 \quad R_{tc}] \quad (18)$$

$$D = [0] \quad (19)$$

Finally the whole state space representation at the cathode is given by equation (20).

in order to take into account their evolution due to ageing. This would also enable the model to be applied to different stacks. For that are used the characterization results considered as composed of one polarization curve and i ($i = 3$ in the reported data) EIS realised at different currents.

The global process can be seen on figure 6. A quick description of the *tuning of the static model* and *tuning of the dynamic model* is proposed here with a complete development in the two next subsections.

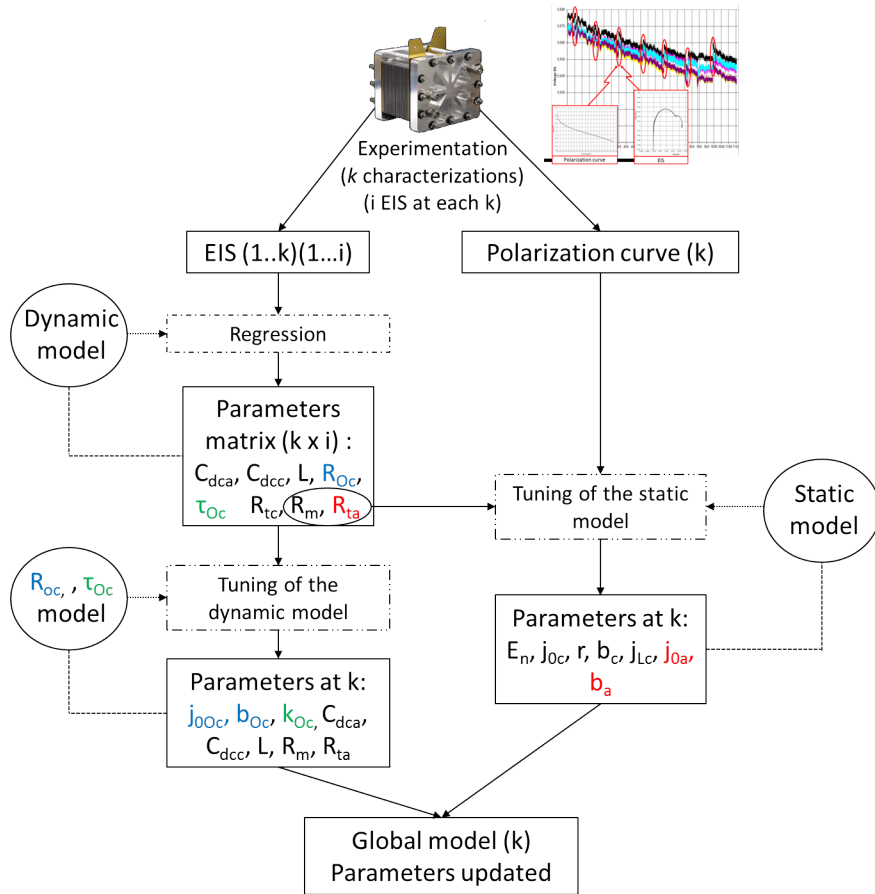


Figure 6: Parameters tuning procedure

On a first step non linear regressions are realized on the i Nyquist plots at the k characterizations. The regressions permit to obtain a first set of the following parameters. As k.i. EIS are used, k.i. values are obtained for each

of these parameters.

- The impedance module R_{Oc} and the time constant τ_{Oc} of diffusion convection of the oxidant at the cathode
- The double layer capacities at the anode and the cathode C_{dca}, C_{dcc}
- The transfer resistance at the anode and the cathode R_{ta}, R_{tc}
- The membrane resistance r
- The connector inductance L

Then the *tuning of the static model* is realized on each polarization curve, the matrix of parameters calculated on the previous step being necessary. This step allows defining the values of the other static parameters (which have not been tuned in the first step and listed below) for each considered characterization :

- Nernst potential E_n
- Exchange current density at cathode and anode $j_{0c} j_{0a}$
- Membrane resistance r (that takes the mean value of R_m)
- Tafel parameters at cathode and anode $b_c b_a$
- Limit current density at the cathode j_{Lc}

Next as τ_{Oc} and R_{Oc} depends on the current, the parameters of their time function are regressed thanks to the current at which the EIS is done. This last tuning will provide for the concerned characterization (and not only for each EIS of this characterization) the following parameters:

- The impedance module R_{Oc} and the time constant τ_{Oc} of the diffusion convection's under parameters (j_{0Oc}, b_{Oc} and k_{Oc})
- The double layer capacities at the anode and the cathode C_{dca}, C_{dcc}
- The transfer resistance at the anode and the cathode R_{ta}
- The membrane resistance named r for the global model
- The connector inductance L

All of the needed parameters are obtained for tuning the global model. However R_{tc} 's value has not been defined for the global model. It is also dependent on the current and the cathode parameters values obtained on the static tuning procedure are used. The expression of R_{tc} is developed in equation (22).

$$R_{tc} = \frac{1}{b_c} \cdot \frac{1}{\sqrt{\left(\frac{J_{DC}}{2 \cdot j_{0c} \cdot 1 - \frac{j_{DC}}{j_{Lc}}}\right)^2 + 1}} \cdot \frac{1}{2 \cdot j_{0c} \cdot \left(1 - \frac{j_{DC}}{j_{Lc}}\right)^2} \quad (22)$$

The parameter values obtained by the update of the static and dynamic model permit to define the model. However, as it is based on a given characterization set, the model updated only concerns the evolution around or after the used characterization.

5.2. Tuning of the static model

Here is developed the block *update of the static model*. A more precise description can be seen on figure 7.

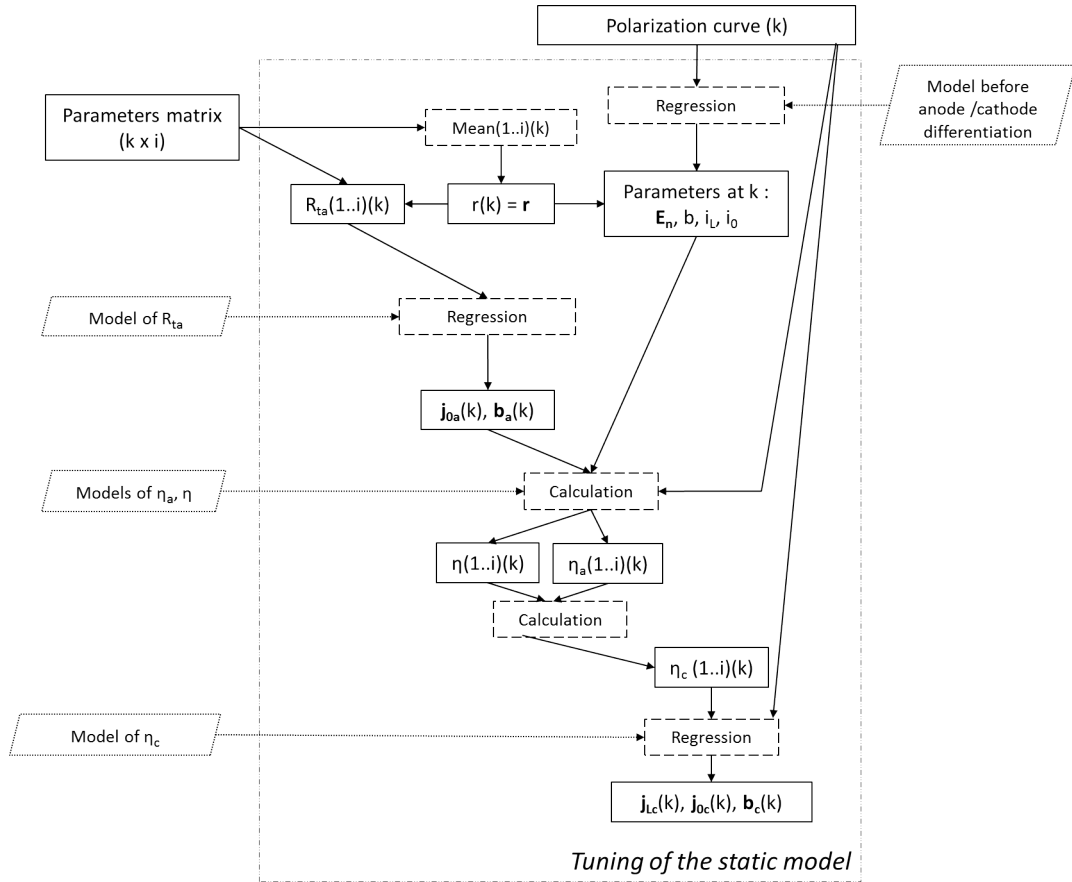


Figure 7: Static model update

For each characterization k , a unique value is necessary for R_m , because only one is needed on the static equation at each characterization as R_m shouldn't depend on the current level. The mean of all the values obtained for this parameter at each characterization is thus considered, this parameter is then written r .

The value of R_{ta} at each EIS are already obtained. Yet the transfer resistance at the anode evolve with the current thanks to the equation (eq. (23) with the exchange current density at the anode j_{0a} and the anode tafel parameter b_a . A regression is then realized with the value of R_{ta} , the values of the level current density at which are done the EIS, and the analytic

equation.

$$R_{ta} = \frac{1}{\left(b_a \cdot 2 \cdot j_{0a} \cdot \sqrt{\left(\frac{J_{EIS}}{2 \cdot j_{0a}} \right)^2 + 1} \right)} \quad (23)$$

Meanwhile, on an other side an other regression is done on the data of the k^{th} polarization curve with a model of the fuel cell "before" the differentiation anode/cathode (eq. (24)) i.e. the voltage drop is for the whole cell.

$$U_{pola} = E_n - r \cdot J_{pola} - \frac{1}{b} \cdot a \cdot \sinh \left(\frac{J_{pola}}{2 \cdot i_0 \cdot \left(1 - \frac{J_{pola}}{i_L} \right)} \right) \quad (24)$$

All the parameters necessary to obtain the values of the global and anode voltage drops are then known. Thanks to their expressions (eq. (25) and (26)) it is now possible to calculate them for all the currents of the polarization curve.

$$\eta = \frac{1}{b} \cdot a \cdot \sinh \left(\frac{J_{pola}}{2 \cdot i_0 \cdot \left(1 - \frac{J_{pola}}{i_L} \right)} \right) \quad (25)$$

$$\eta_a = \frac{1}{b_a} \cdot a \cdot \sinh \left(\frac{J_{pola}}{2 \cdot j_{0a}} \right) \quad (26)$$

From the previous values the cathode voltage drop can be deduced as $\eta = \eta_a + \eta_c$. As the expression of η_c is also know (eq. (27)), a regression on its values is done in order to obtain the tafel parameter (b_c) and the exchange and limit current density (j_{0c}) at the cathode at this characterization.

$$\eta_c = \frac{1}{b_c} \cdot a \cdot \sinh \left(\frac{J_{pola}}{2 \cdot j_{0c} \cdot \left(1 - \frac{J_{pola}}{j_{Lc}} \right)} \right) \quad (27)$$

With this process, the static model is completely tuned as all the parameters in equation (2) are updated. The model is finally usable after the characterization that allows tuning it.

5.3. Tuning of the dynamic model

The dynamic updating procedure is described on figure 8. For L , C_{dca} , C_{dcc} , and R_m the average value is calculated. It is done on all values obtained at the characterization k considered. Indeed, only one value is needed, taking the i values obtained on the EIS and calculating the mean also permits to smooth if there is errors on the measures.

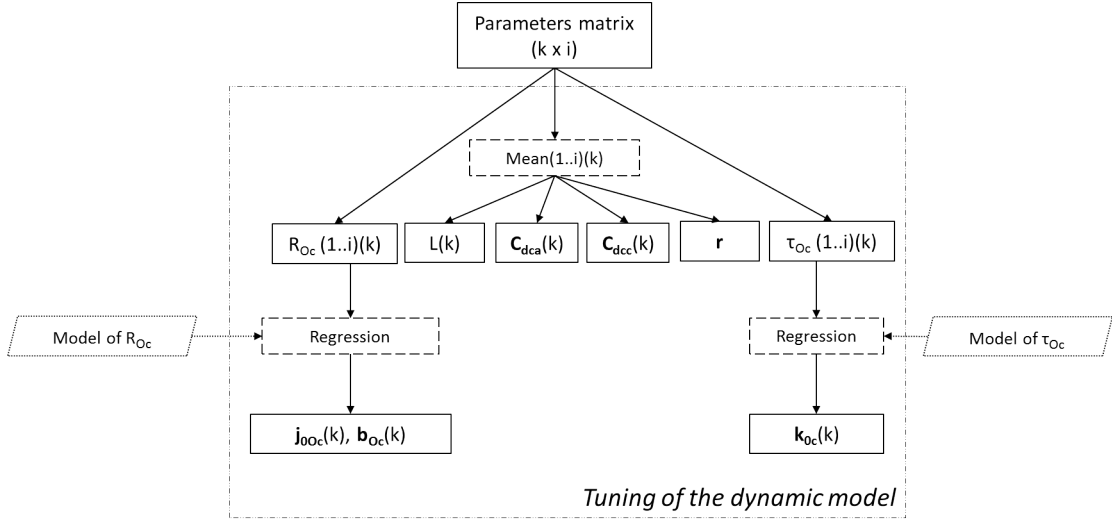


Figure 8: Dynamic part update

For the development of the diffusion convection parameters, R_{Oc} and τ_{Oc} some regressions are realized too thanks to their expressions (eq. (28) and (29)). As the i values obtained of the parameters at the characterization k are already known thanks to the very first step of the global tuning process, a regression can be realized. Indeed, their variation laws depend on the current density. For the regression, the current densities at which are realized the i EIS are used.

$$R_{Oc} = \frac{1}{\left(b_{Oc} \cdot 2 \cdot j_{0Oc} \cdot \sqrt{\left(\frac{J_{EIS}}{2 \cdot j_{0Oc}} \right)^2 + 1} \right)} \quad (28)$$

$$\tau_{Oc} = \frac{k_{Oc}}{J_{EIS}} \quad (29)$$

6. Experiments, results and discussion

6.1. Experimental setup

The model is validated thanks to two long-term tests carried out on two different stacks of similar technology (PEMFC composed of 5 cells with an active area of 100cm^2).

- A first stack (named FC1) is operated in stationary regime, with a constant load expressed by a current of 70A , at roughly nominal operating conditions during 1000 hours.
- A second stack (named FC2) is operated under dynamic current testing conditions, i.e. with high-frequency triangular current ripples. The current is 70A with a ripple part of more or less 10% at a 5kHz frequency. The operating conditions are set constant. The test lasted 1000 hours.

The latter experiment has been realized in order to estimate the perturbations caused by a power converter usually connected to the fuel cell compared to a constant current in the first experiment. It permits to ensure that the model can still be accurate with the current oscillations caused by the power converter.

For both tests, some values as the voltage, current, or humidity were monitored all along the 1000 hours in order to obtain global historic curves (i.e. evaluating the evolution over time of voltage levels). Besides, characterizations were carried out once per week (around every 160 hours) according to an identical protocol:

- Polarization curve test (i.e. measuring the static I/V curve of the fuel cell stack)
- Electrochemical Impedance Spectroscopy (EIS) measurement (i.e. plotting the Nyquist diagram of the fuel cell stack over a frequency range from 50 mHz to 10 kHz) at three different current density $0.70\text{A}/\text{cm}^2$, $0.45\text{A}/\text{cm}^2$ and $0.20\text{A}/\text{cm}^2$.

All along the 1000 hours test, 8 characterizations were performed.

6.2. Static part tuning validation

In order to validate the model, the whole updating procedure described on figure 7 was realized for each characterization. Indeed, the objective is here to confirm that the model reproduces the behavior of a PEMFC stack. The results presented are the results of the experiment on the fuel cell 2, as this is the more complex load.

On figure 9 an exemple of the results of this procedure, at the third characterization (after around 182 hours of test) can be seen. The fitting of the polarization curve simulated with the static model is in plain line and the experimental data is in dots for the fuel cell under ripple solicitation. The fitting appears to be satisfying.

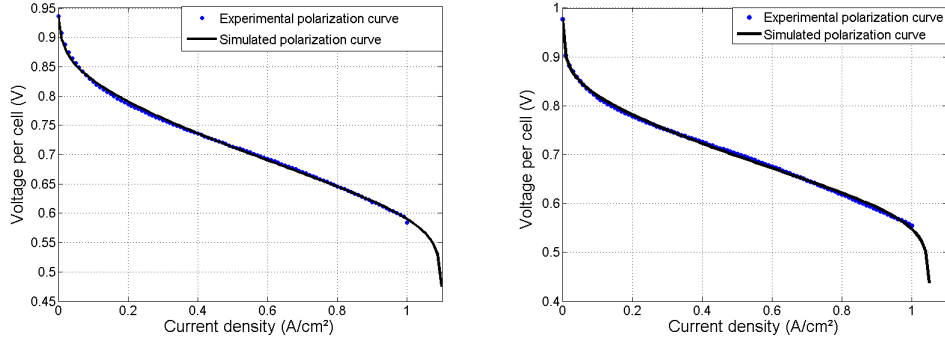


Figure 9: Fitting of a polarization curve during the tuning of the static model for the FC2 at the third (182h) and the eight (1016h) characterization

In order to discuss further the accuracy of the model, the results errors MAPE (Mean Absolute percent error) and RMSE (Root Mean Square Error) between the simulated polarization curve and the real data are calculated. As the updating of the static model is realized for each characterization the evolution of the error versus time can be drawn. That allows studying if the model is still adapted when the stack ages. There is no clear evolution with the time (figure 10). It is validated on the experiment under stabilized load as the calculations of error were similar and with no clear tendency. The model is as well adapted at the start of the life of a stack than at its end of life. It is a convenient point, as the goal is to use this model for modeling the ageing.

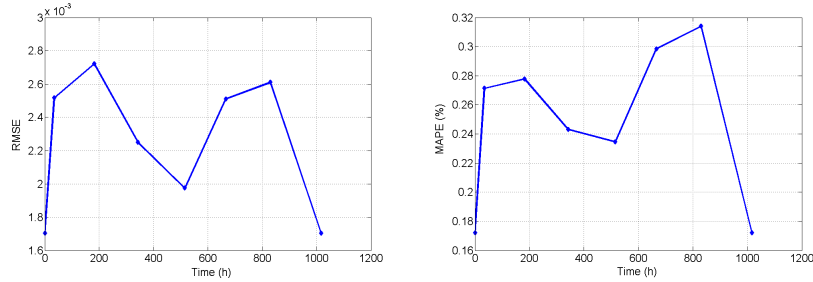


Figure 10: Evolution of the RMSE and MAPE of the difference between the model and the data with the time for the FC2

The global errors MAPE and RMSE of the static tuning on the two experiments is then calculated. This value is obtained by taking the average of all the errors obtained on each characterization. The results are gathered on table 2. The good quality of the fitting is one more time validated. The static part of the model reproduces the behavior that can be seen on the experimental data and stay accurate during the 1000 hours of the two tests and for each polarization curve of each test.

	With stabilized current	With ripple current
Mean MAPE %	0,19	0,25
Mean RMSE	1,66E-03	2,25E-03

Table 2: Mean of errors on all the characterization phases for polarization curve fitting

6.3. Dynamic part tuning validation

During the update of the dynamic part, the fitting with the Nyquist plot is drawn and studied. Figure 11 depicts a Nyquist plot extracted from the experimental data at 35 hours and at 70A for the FC2 and the simulated results obtained thanks to the dynamic model. The mean errors for the two experiments and the simulation of fitting can be found on the table 3. It can be seen that there is one more time no clear evolution of the error with the time or even with the current at which is realized the EIS. This is confirmed as, the same calculation of errors was made on the dynamic part than on the static one, and nor the aging time nor the current has an effect on the performance of the dynamic model.

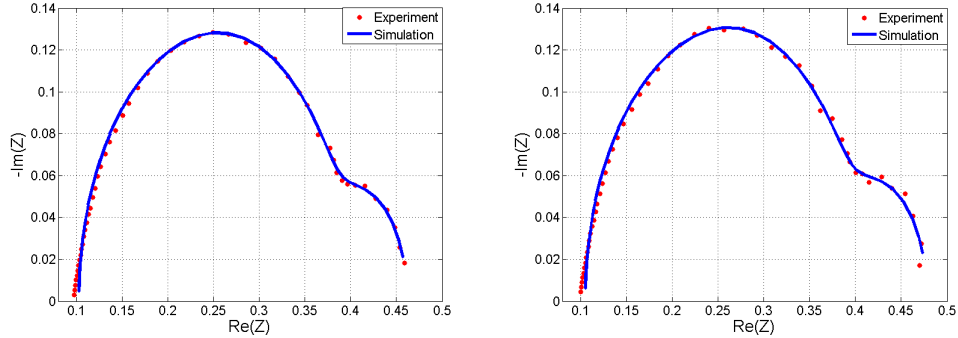


Figure 11: Fitting of a Nyquist plot at 20 A at the third (182h) and seventh (830h) characterization for the FC2

	With stabilized current		With ripple current	
	Real part	Imaginary part	Real part	Imaginary part
Mean MAPE	0,90 %	8,22 %	0,19 %	0,25 %
Mean RMSE	1,025	12,6	0,0027	0,0026

Table 3: Mean of errors on all the characterization phases for the Nyquist Plot fitting

6.4. Global model simulation

Finally, the global model that can be seen in figure 2 is validated. For that purpose, the model was completely updated with the data from the third characterization (after 182 hours of test) for the FC2. The parameters values obtained thanks to this procedure are gathered in table 4.

The time constant applied to the low pass filter that allows decomposing the current density in a dynamic and a static part is 0.2s.

The global model is then completely updated, it can finally be validated. For that purpose, the load of the experiment is imposed to the model; the simulation and the experiment are then compared.

An example taken after 182 hours around the third characterization can be seen in figure 12. In this figure, it is obvious that the global model responds with the same trend than the fuel cell that was experimented.

Symbol	Name	Value	Unit
r	Internal resistance	0.0989	$\Omega.cm^2$
E_n	Nernst potential	0.937	V
j_{0a}	Exchange current density at the anode	0.1454	A/cm^2
b_a	Tafel anode parameter	36.43	V^{-1}
j_{0c}	Exchange current density at the cathode	0.0018	A/cm^2
b_c	Tafel cathode parameter	44.64	V^{-1}
j_{Lc}	Limit current density at the cathode	1.099	A/cm^2
C_{dca}	Double layer capacity at the anode	0.0404	F/cm^2
C_{dcc}	Double layer capacity at the cathode	0.0472	F/cm^2
L	Connector inductance	$1.23.10^{-6}$	H
j_{0Oc}	Parameter of the variation law of R_{Oc}	5223	A/cm^2
b_{Oc}	Parameter of the variation law of R_{Oc}	0.0012	V^{-1}
k_{Oc}	Parameter of the variation law of τ_{Oc}	0.0918	$A.s/cm^2$

Table 4: Values of the parameters after the model updating process with the third characterization data around 182h on FC2

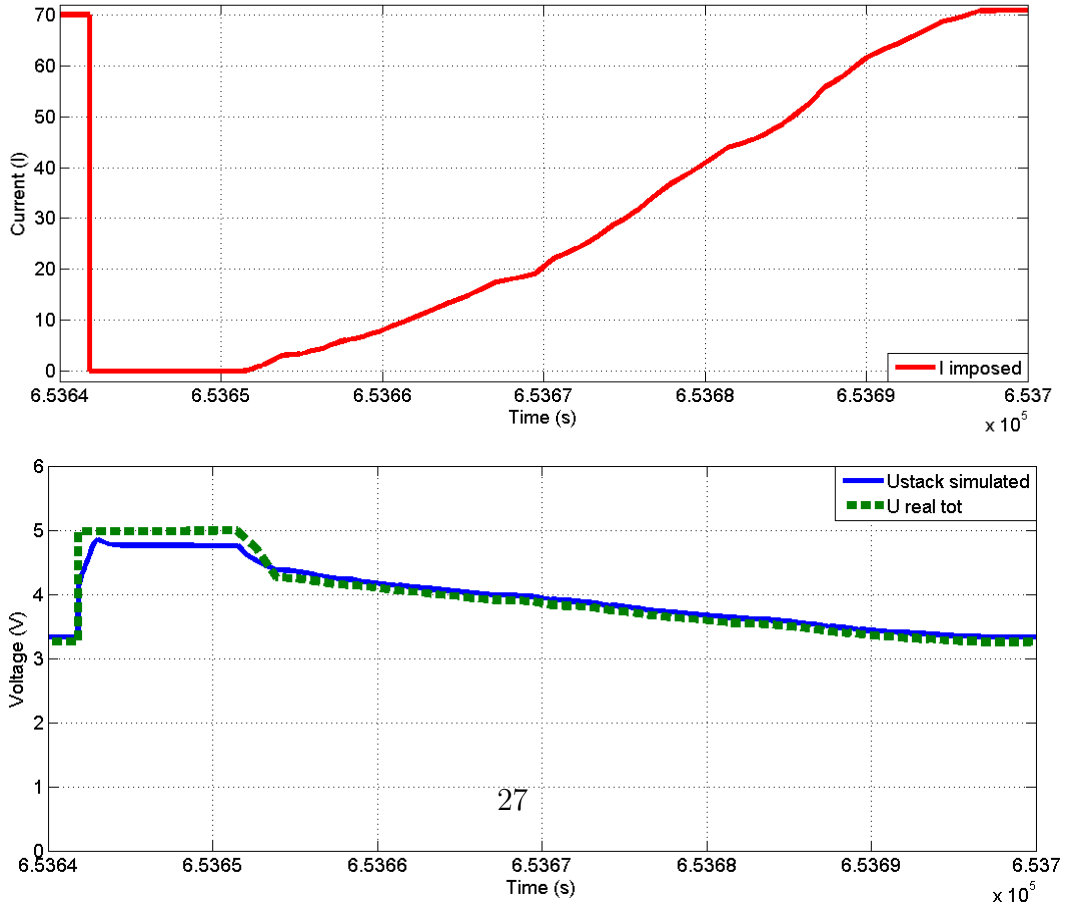


Figure 12: Simulation and experiment comparison (bottom curves) under the same load (top curve) just after the third characterization

However, there is a small difference of a constant value between the two curves when the current is evolving. This can be explained by the change of operating conditions. Indeed, during the polarization curve measurement the operating conditions are different than during the ageing test. For example, the temperature is not stable on this experiment as it exhibits a variation of fifteen degrees. This is due to the poor control of the temperature on the test bench in this specific experiment. So, the hypothesis of constant operating conditions is not completely verified.

At the open circuit voltage, this difference is bigger and a peak can be observed. It is due to the decomposing block that split the static and the dynamic current. Indeed, this block is a low-pass filter and it is not enough adapted for our needs. Here, the time constant in this block is $0.2s$. The influence of this value is interesting. Indeed, if this value is decreased, the peak would rise higher, on an other hand, if this value is augmented, the time the model would take to gain the top of the step, would be too important to face the real behavior of the fuel cell.

The model reproduces well the behavior of the fuel cell as we can see in the figure 12. On this part the error RMSE is 0.5103, a good performance.

7. Conclusion

The objective is to define and validate a model that can accurately reproduce the behavior of a PEMFC in order to be applied for prognostics. For that purpose, in this paper a model composed of a static and a dynamic part is proposed and validated thanks to experimental data. In a first step, the static model is studied by the comparison of experimental polarization curve and simulated one. The errors have been calculated and prove that this part of the model is very satisfying. In a second step, but in the same way, the dynamic part has been examined, the results show a good fitting independently of the time or of the current. Finally, the whole model has been simulated, and it shows good hope for the future application. Indeed, the model is as good on a young stack than on an stack aged of a thousand hours. The model presents the exact same answer to the solicitation that the fuel cell itself under the same solicitation: the behavior is well reproduced. It means that the structure of the model can be kept during the ageing. However, the difference between the operation conditions during the polarization curve and the ageing process is an issue that has to be fixed; the integration of other input might be necessary. The decomposition block would also have

to be improved because it triggers a response not as good as hoped as the decomposition of the current is not well adapted.

This model fits well for the prognostics, and is going to be the starting point of the following work. Indeed, the ageing can be modeled by giving to some parameters a dependency to the time.

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