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1 **EXPLORATORY TESTS ON A BIAXIAL COMPRESSION HOPKINSON BAR SET-UP**

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7 **Abstract:**

8 Background: Multiaxial dynamic loadings occur in many industrial cases and multiaxial
9 dynamic test development is thus a crucial issue. Objective: To meet this challenge, a biaxial
10 compression Hopkinson bar set-up is designed. Methods: The set-up consists of a striker, an
11 input bar, an internal output bar and a co-axial external output tube (surrounding the internal
12 bar). The internal output bar measures the axial loading of the cross sample whereas the external
13 output bar measures the transverse one via a mechanism. This mechanism uses two intermediate
14 parts with inclined sliding surfaces. Results: Gauges on the bars enable for force measurements
15 in the set-up, and the sample displacement field is obtained by digital image correlation. Simple
16 compression tests on cuboid samples inserted between the input bar and the internal output bar
17 give the sample material behavior. Then, to determine the friction at the mechanism sliding
18 surfaces, identical samples are inserted between the input bar and the external output bar, and
19 are compressed. Conclusions: Finally, the consistency of the measurements obtained during a
20 biaxial compression test on a cross sample can be checked from the previously measured
21 parameters and from numerical simulations.

22 **Keywords:** biaxial compression dynamic test, Hopkinson bars

1 Introduction

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Multiaxial dynamic loadings usually occur in many industrial cases such as automotive impacts [1], high-speed forming [2] or high-speed machining [3]. Multiaxial dynamic test development is therefore a crucial issue. Unfortunately, most of the dynamic tests are uniaxial. For instance, the very common Hopkinson bar test (which enables for accurate measurements at high strain rates) uses the uniaxial compression loading generated by the impact of a projectile.

In order to perform multiaxial tests, many set-ups have thus been designed to obtain multiaxial loadings from an initial uniaxial loading device. For example, a radial pressure can be applied to a cylindrical sample mounted on Hopkinson bars thanks to a confinement device. One can use a pressure vessel that enables for a controlled quasi-static pressure to be applied from a fluid [4]. Inserting the cylindrical sample inside a rigid tube can generate a dynamic radial loading even though the ratio between the radial pressure and the axial stress strongly depends on the sample material, in particular on its Poisson's ratio [5]. Using a confinement tube made of a perfect plastic behavior material makes it possible to maintain a constant radial pressure [6]. A rigid confinement can also be imposed to a cruciform sample with a pre-loading system [7].

Another idea is to combine shear and compressive loadings. An inclined shear/compression specimen [8] or pressure bars with beveled ends [9] can be used to apply such combined loadings. The combined torsion-compression Hopkinson bar technique using torsional and compressive bars at each side of specimen was also reported [10]. It can also be carried out by blocking a brake on the input bar and by applying both compression/tension and torsion on the input boundary of the bar. Then the sudden fracture of the brake generates both

46 torsion and tension/compression waves [11]. Unfortunately, the difference between the wave
47 celerities does not enable simultaneous loadings to be obtained [12].

48 In order to apply biaxial loadings, two perpendicular Hopkinson bar devices have been
49 built [13]. An explosive is used to obtain simultaneous loadings. The system is rather expensive
50 and difficult to use. Recently, biaxial Hopkinson bar systems using two impactors were reported
51 to generate biaxial compression states on samples [14], but obtaining two simultaneous impacts
52 remains difficult. Another simple way to apply an equi-biaxial loading is the bulge-test using
53 Hopkinson bars described in [15]. In this test, the external boundary of a circular sheet is leant
54 against the tubular boundary of the output bar while the other side of the sheet is submitted to
55 the pressure of a fluid compressed by the input bar. A biaxial tensile state is thus obtained at
56 the center of the sheet. Unfortunately, only sheets can be tested and the displacement field on
57 the sample cannot be easily measured.

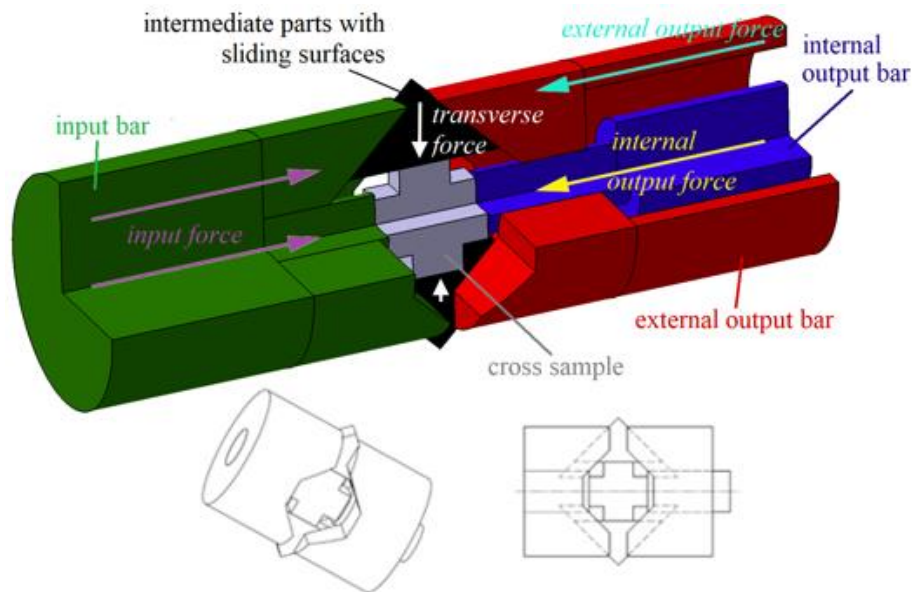
58 From the short review above, it can be seen that the multiaxial testing design is still a
59 tough issue. There are no commonly admitted testing set-ups and the design of such a test
60 depend on the aimed loading state and on specimens. This paper is focused on biaxial
61 compression and a new concept of Hopkinson bar system has been designed and tested. Its
62 principle and its characteristics are described in Section 2. Then, Sections 3 and 4 present
63 respectively the raw experimental results obtained from calibration tests and the analysis of a
64 bi-axial test thanks to numerical simulations.

65 **2 Design of the new set-up**

66 2.1 Set-up characteristics

67 The designed bi-axial set-up uses a mechanism with intermediate parts with sliding
68 surfaces and a cruciform specimen. This mechanism with sliding surfaces at 45° with respect

69 to the axial direction was placed between the single input bar, the internal output bar and the
 70 co-axial external output tube (Figure 1). After the striker impact on the input bar, the internal
 71 output bar measures the axial loading of the cross sample whereas the external output bar (the
 72 single tube that surrounds the internal output bar) measures the transversal one via the
 73 mechanism.



74
 75 Figure 1: Schematic of the experimental configuration (cut view) with the relative motion of
 76 each part and the applied forces (up). Three-dimensional (down, left) and uncut (down, right)
 77 views without the three bars.

78 Using a single loading impulse avoids the difficulty due to non-simultaneous impacts
 79 occurring with perpendicular Hopkinson bar devices [13], [14]. Another advantage of such a
 80 design lies in the fact that the ratio between the axial and the transverse loadings is imposed by
 81 the ratio between the external and the internal output bar impedances and by the sliding surface
 82 angle of the mechanism.

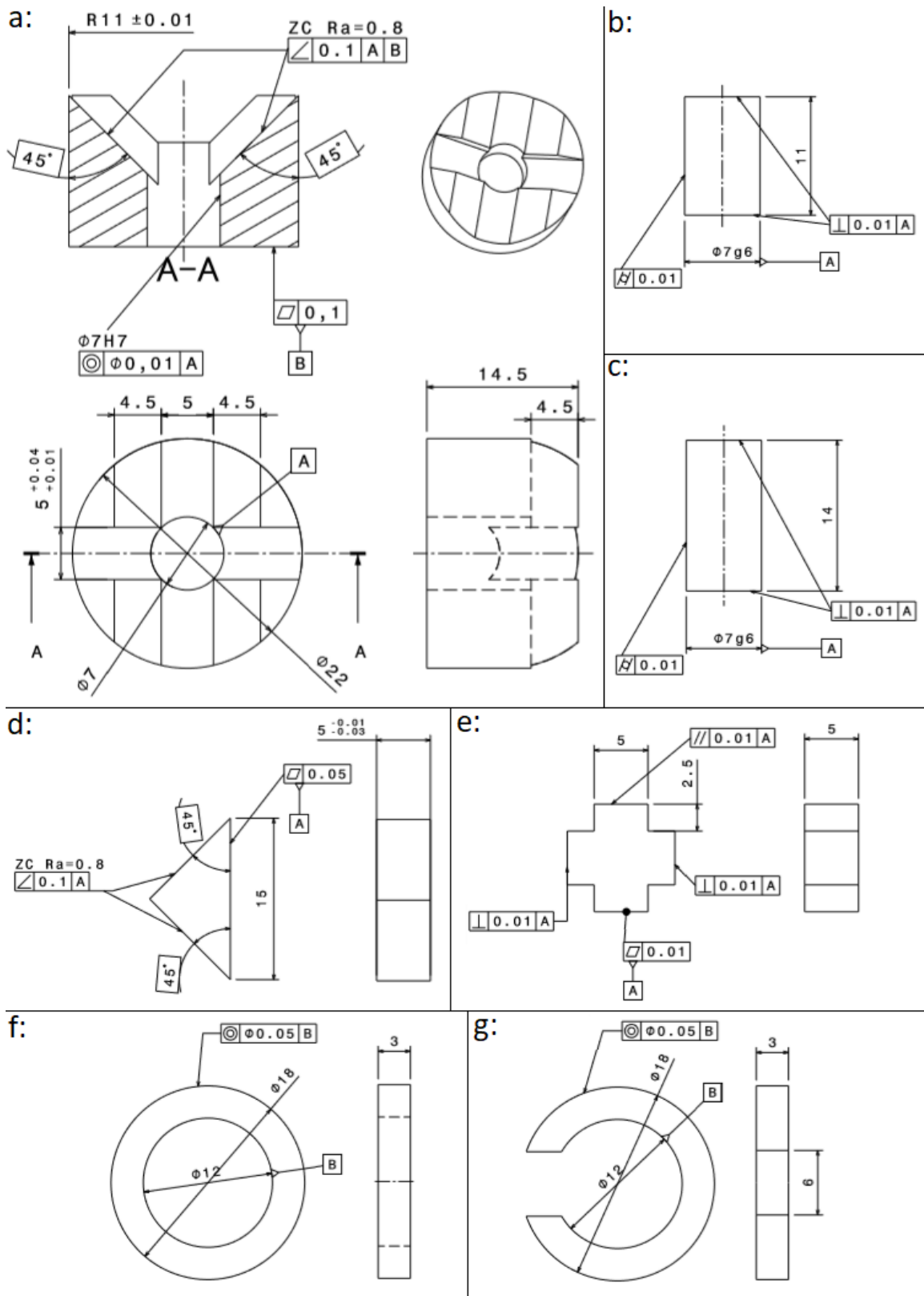
83 The pressure bars are made of steel and their characteristics are given in Table 1. The
 84 external and the internal output bars have nearly the same impedance in order to ensure, on an

85 isotropic sample, an approximate equality between the internal and the external loadings, and
 86 therefore between the axial and the transverse loadings, thanks to the mechanism. The
 87 difference between the internal radius of the external output bar (R_{ieo}) and the internal output
 88 bar radius (R_{io}) is 3 mm, which is sufficient to place the gauges glued on the internal bar and
 89 their cables. These electrical cables exit from the external bar at the output end (i.e. at the
 90 opposite of the set-up). Nylon bearings are inserted between the two co-axial output bars and
 91 some of them are opened (Figure 2g) to let a passage to the cables.

bar	density	wave celerity	radius		length
			external	internal	
striker	$\rho_i = 8050 \text{ kg.m}^{-3}$	$C_i = 4600 \text{ m.s}^{-1}$	$R_i = 11 \text{ mm}$		1.25 m
input					4 m
internal output	$\rho_{io} = 7800 \text{ kg.m}^{-3}$	$C_{io} = 5100 \text{ m.s}^{-1}$	$R_{io} = 6 \text{ mm}$		2 m
external output	$\rho_{eo} = 7400 \text{ kg.m}^{-3}$	$C_{eo} = 5200 \text{ m.s}^{-1}$	$R_{eoo} = 11 \text{ mm}$	$R_{ieo} = 9 \text{ mm}$	2 m

92 Table 1: Mass densities, tensile-compressive wave celerities, radii and lengths of the bars.

93 The detailed drawings of the set-up parts are given in Figure 2. The sample size
 94 (boundary to boundary) is $10 \text{ mm} \times 10 \text{ mm}$ and its thickness is 5 mm (Figure 2e). The shape of
 95 the parts with the two sliding surfaces (noted “a” in Figure 2) has been chosen to maximize the
 96 stiffness. One of this part (the left-hand one in Figure 1, in green) is inserted between the input
 97 bar and the two transverse triangular parts (noted “d”) and the other (the right-hand one in
 98 Figure 1, in red) is inserted between the two transverse triangular parts and the external output
 99 bar.



100

101 Figure 2: Part drawings (general tolerances: 0.1 mm); a: parts with the sliding surfaces, b: left-

102 hand cylinder, c: right-hand cylinder, d: transverse triangular parts, e: sample, f: bearings, g:

103 opened bearings.

104 The cylinder noted “b” in Figure 2 is inserted between the input bar and the sample, and
105 the cylinder “c” is inserted between the sample and the internal output bar (see Figure 1). Both
106 cylinders apply the axial loading on the cross sample and the right-hand one in Figure 1 (the
107 “c”) is free to have an axial motion relatively to the right-hand part with the sliding surfaces
108 (“a”).

109 2.2 Forces and velocities in the set-up

110 Strain gauges are glued at the middle of the input bar and on the two output bars close
111 to the sample but far enough from the ends (at 0.374 m on the external bar and at 0.612 m on
112 the internal one) to be within the Saint-Venant conditions.

113 After the striker impact, the input bar gauge measures an incident compressive wave ε_i
114 followed by a reflected tensile wave ε_r . Moreover, the external output gauge measures a
115 transmitted wave in the external output bar, ε_{et} and the internal output gauge also measures a
116 transmitted wave in the internal output bar, ε_{it} . ε_i can be seen as a loading imposed to the biaxial
117 set-up whereas ε_r , ε_{et} and ε_{it} can be seen as the set-up response to the imposed loading.

118 These strain waves have to be virtually transported from the gauge positions to the
119 interfaces between the bars and the set-up presented in Figure 1, down. Thus, ε_i has to be
120 delayed and ε_r , ε_{et} and ε_{it} have to be shifted forward of the duration necessary for the waves to
121 propagate from the measurement gauge to the corresponding interface. Then the Hopkinson
122 formulae enable for the determination of the forces and of the velocities at the interfaces from
123 these transported waves and from the bar parameters given in Table 1:

$$124 \quad (1) \quad F_i = -\rho_i C_i^2 \pi R_i^2 (\varepsilon_i + \varepsilon_r)$$

$$125 \quad (2) \quad V_i = C_i (\varepsilon_r - \varepsilon_i)$$

126 (3) $F_{eo} = -\rho_{eo} C_{eo}^2 \pi (R_{eoo}^2 - R_{ieo}^2) \varepsilon_{et}$

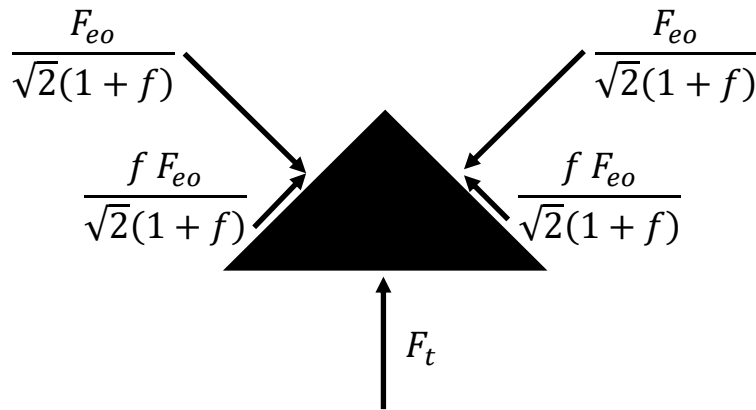
127 (4) $V_{eo} = -C_{eo} \varepsilon_{et}$

128 (5) $F_{io} = -\rho_{io} C_{io}^2 \pi R_{io}^2 \varepsilon_{it}$

129 (6) $V_{io} = -C_{io} \varepsilon_{it}$

130 F_i and V_i are the force and the velocity at the interface between the input bar and the set-
 131 up shown in Figure 1, F_{eo} and V_{eo} are the force and the velocity at the external output bar
 132 interface and F_{io} and V_{io} are the force and the velocity at the internal output bar interface.

133 Under the assumption of an equilibrium state in the set-up, the axial force in the sample
 134 can be assumed to be equal to the internal output force F_{io} and the transverse force F_t can be
 135 deduced from the external output force F_{eo} . Indeed, each transverse triangular part of the
 136 mechanism is axially submitted to half F_{eo} and by taking account of friction, the mechanical
 137 equilibrium of a transverse triangular part leads to Figure 3.



138

139 Figure 3: Equilibrium of a transverse triangular part axially submitted to half F_{eo} .

140 As the Figure 3 upper triangle moves from top to bottom, the applied friction forces are
141 oriented from bottom to top. Besides, according to the Coulomb's laws, the friction force over
142 normal force ratio is imposed to be equal to the friction coefficient at the mechanism sliding
143 interfaces, noted f . The axial projection of the force transmitted by a sliding surface corresponds
144 to half F_{eo} (the axially applied force) and the transverse projection corresponds to F_t , which
145 leads to:

$$146 \quad (7) \quad F_t = \frac{1-f}{1+f} F_{eo}$$

147 **3 Experimental results**

148 **3.1 Strain gauge measurement and image processing**

149 Axial strain gauges are glued on each of the three bars and the measurement frequency
150 is 500 kHz. The Hopkinson formulae (equations (1), (3) and (5)) permit for the calculation of
151 the forces at the interfaces between the bars and the set-up from these measurements. The
152 camera trigger signal is measured in the same time-basis as the gauge voltages. The image
153 which was being recorded in the camera at the arrival of the trigger signal being known, both
154 measurements can be time shifted.

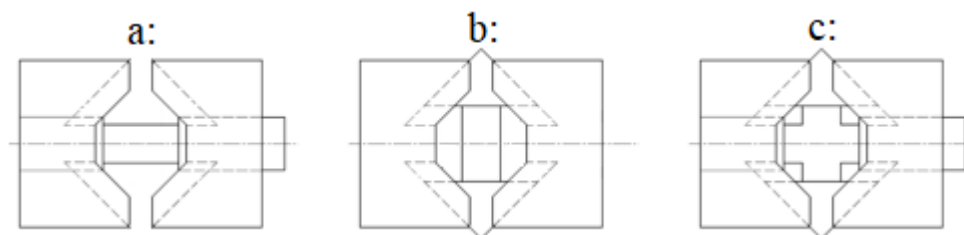
155 The speckled samples are observed during the tests thanks to an SA5 high-speed camera
156 whose frequency is 50 kHz at a definition of 512 pixels \times 272 pixels. Images of the samples are
157 acquired during the tests. The first one is called reference image and the displacement between
158 each image and the reference is calculated thanks to Digital Image Correlation (DIC). DIC is
159 performed by using the in-house Correli RT3 software [16], [17]. The displacement field is
160 defined over a finite-element mesh made of triangular 3-noded elements (T3). The chosen
161 element size is 10 pixels. The mean displacements on the four sample interfaces and the
162 resulting axial and transverse elongations are determined from DIC. The displacement is given

163 in pixels, which are converted into millimeters knowing the sample dimension. In order to
164 control the uncertainty of the DIC calculation, an elastic regularization is used [16], [17].

165 The relative weight applied to the reference solution can be seen as the fourth power of
166 a length called the regularization length. A too high regularization length may lead to erroneous
167 estimations of the experimental displacement field because this field is thus constrained to be
168 close to an elastic solution. As a result, the DIC calculations are processed with a regularization
169 length decreasing from a value corresponding to 3 times the element size (30 pixels) to a value
170 equal to the element size (10 pixels). DIC gives identical results when the length varies from
171 30 to 20 pixels but the results obtained with a 10 pixel length are sometimes a bit noisy and
172 slightly different from the previous ones. To reduce the noise, a 20-pixel length is thus chosen
173 for the processing.

174 3.2 Identification of the sample material behavior

175 The samples are made of an AW-2017A aluminum. The material stress-strain law is
176 identified from simple compression tests on cuboid samples ($5\text{ mm} \times 5\text{ mm} \times 10\text{ mm}$) inserted
177 between the input bar and the internal output bar (the external output bar being removed, see
178 Figure 4a).



179

180 Figure 4: Schematics of the tests; a: cuboid sample axially compressed, b: cuboid sample
181 transversally compressed, c: cross sample bi-axially compressed.

182 The compression force in the sample (Figure 4, case a) thus corresponds to the internal
183 output force F_{io} . The sample axial and transverse elongations in the image plan are determined
184 from DIC. The real cross section (which increases because of compression), and then the true
185 stress, can thus be calculated. Meanwhile, the axial logarithmic strain is deduced from the
186 corresponding axial elongation. These measurements lead to repeatable axial behaviors.

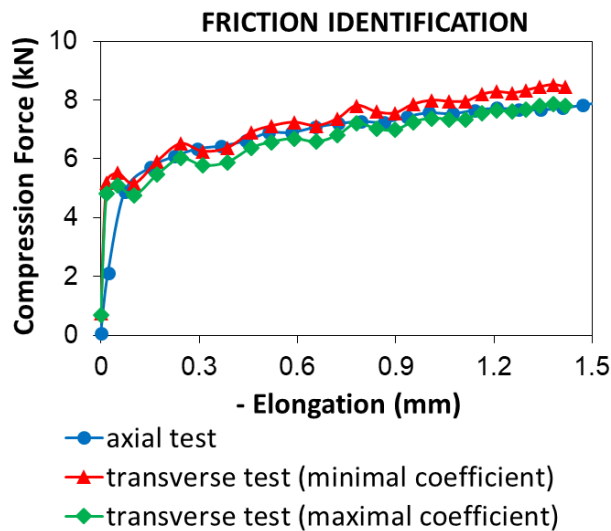
187 3.3 Identification of the friction at the mechanism sliding interfaces

188 The friction coefficient in the mechanism of this new bi-axial testing device is a key
189 parameter which has to be determined under the bi-axial test conditions. In order to reproduce
190 the reached sliding velocities at the sliding interfaces, identical AW-2017A cuboid samples are
191 inserted between the input bar and the external output bar, and are compressed via the
192 mechanism (the internal output bar being removed, see Figure 4b). The ratio between the
193 transverse compression force F_t and the external output force F_{eo} is thus friction dependent
194 according to relation (7).

195 The set-up being far too small to insert a cell able to measure the compression force in
196 the sample, this force will be deduced from relation (7) and from the F_{eo} measurement. The
197 friction coefficient f will be estimated knowing that the force-elongation laws identified during
198 the axial (Figure 4a) and the transverse (Figure 4b) tests must be the same because the tested
199 cuboid samples are the same too.

200 According to Figure 5, by multiplying the external output force F_{eo} measured during the
201 transverse test by a constant ratio, a satisfactory fit can be obtained between the transverse and
202 the axial tests when the displacements become high enough. However, for low displacements,
203 the ratio should be a bit lower to obtain a satisfactory fit. It implies that the friction is first higher
204 (adhesion phase) and then decreases when the displacements become high enough (sliding
205 phase), which is finally consistent with the Coulomb's law.

206 Figure 5 represents typical curves obtained from an axial test and from a transverse one,
 207 chosen as average behaviors. The transverse curve shows that the adhesion phase is not
 208 stationary, unlike the sliding one. The friction will thus be identified only during the sliding
 209 phase. The noise of the transverse force-elongation curve will lead to an uncertainty on the
 210 friction. By fitting, in the sliding phase, the transverse curve points with the minimal forces and
 211 the axial curve, a lower bound of the friction coefficient is obtained. Inversely, by fitting, in the
 212 sliding phase, the transverse curve points with the maximal forces and the axial curve, an upper
 213 bound of the coefficient is obtained. One obtains $0.05 < f < 0.09$. Such values are consistent
 214 with Vaseline lubricated interfaces. It finally leads to a 0.87 average F_v/F_{eo} ratio with a 4 %
 215 relative uncertainty.



216
 217 Figure 5: Friction identification by fitting the transverse test and the axial one.

218 The friction coefficient magnitude and the corresponding uncertainty knowledge does
 219 not matter in itself, but it will enable for the determination of the transverse force and of the
 220 corresponding uncertainty during the bi-axial test.

221 Without clearances and without intermediate strains in the set-up, the corresponding
 222 interface sliding velocity should be equal to the difference between the input velocity and the

223 external output one, or to the opposite of the transverse sample elongation rate, both divided by
224 $\sqrt{2}$ (because of the 45° angle):

$$225 \quad (8) \quad V_{int,bars} = \frac{V_i - V_{eo}}{\sqrt{2}}$$

$$226 \quad (9) \quad V_{int,sample}(t) = \frac{\Delta l(t-\Delta t) - \Delta l(t+\Delta t)}{2\sqrt{2} \Delta t}$$

227 $V_{int,bars}$ is the interface sliding velocity estimated from the bar interface velocities
228 (relations (2) and (4)) whereas $V_{int,sample}$ is the same quantity estimated from the sample
229 elongation Δl . Formula (9) corresponds to a numerical differentiation, t being a measurement
230 instant and Δt the elongation acquisition time (given by the camera).

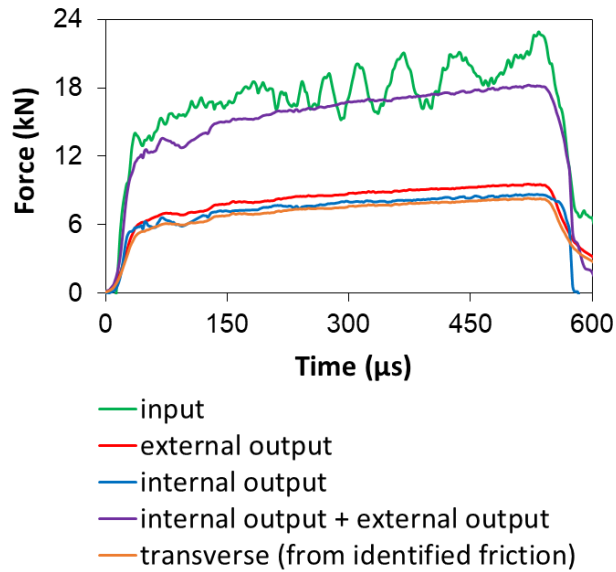
231 These velocity estimations show that a stationary phase with an interface sliding
232 velocity of around 1 to 3 m/s begins for an elongation of approximately 0.1 mm, which is
233 consistent with the beginning of the phase with a constant friction identified in Figure 5.

234 3.4 Analysis of the bi-axial test measurements

235 An AW-2017A cross sample is tested by using the whole bi-axial mechanism and the
236 two output bars (see Figure 1 or Figure 4c). The forces applied by the bars on the bi-axial set-
237 up are determined from the strain gauge measurements and from the Hopkinson formulae and
238 are shown in Figure 6.

239 Figure 6 shows that the input force and the total output force are in satisfactory
240 equilibrium, despite of the complex 3-dimensionnal wave propagation phenomena occurring in
241 the bi-axial mechanism. According to Section 2.2, the axial compression force in the sample
242 corresponds to F_{io} whereas the transverse compression force F_t is lower than F_{eo} but almost
243 equal because of the low friction (in Section 3.3, the estimated F_t/F_{eo} ratio is roughly 0.87). The

244 obtained transverse and axial forces (F_t and F_{io}) being very close, Figure 6 thus displays that
245 the force loading path in the sample is rather equi-bi-axial.

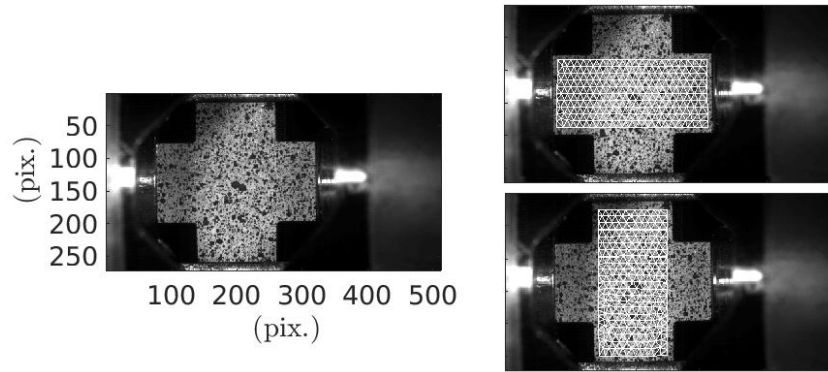


246

247 Figure 6: Time evolutions of the forces at the interfaces.

248 As the external and the internal output bars have nearly the same impedance, the
249 velocities, and thus the displacements, at the external and the internal output bar boundaries are
250 also very similar. If there were no clearances and no strains occurring in the mechanism
251 intermediate parts, the transverse displacement of each of the two triangular parts would be half
252 the difference between the input bar and the external output bar displacements. The triangular
253 parts moving symmetrically, the sample elongations, in both directions, would thus be exactly
254 equal to the difference between the displacements at the input bar and at the output bar
255 interfaces. It displays that the elongation loading path may be also rather equi-bi-axial.

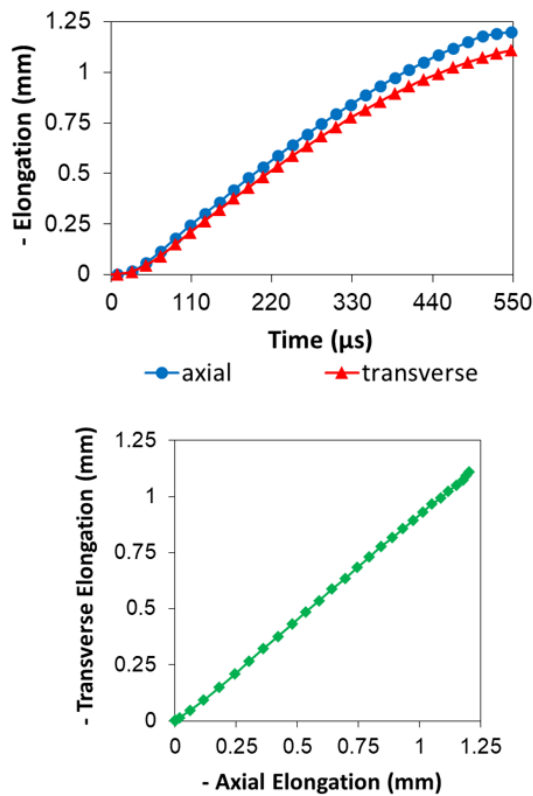
256 The cross sample axial and transverse elongations are determined from the images and
257 from DIC. The DIC reference image and the corresponding meshes on the sample are shown in
258 Figure 7.



259

260 Figure 7: Reference image (left), mesh used to determine the axial displacements (right, up)

261 and mesh used to determine the transverse displacements (right, down).



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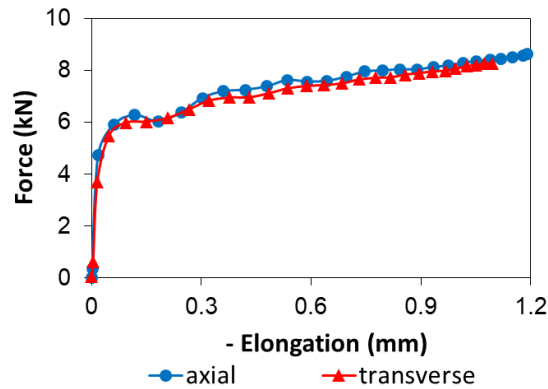
263 Figure 8: Time-evolutions of (the opposite of) the elongations in both directions (up) and

264 corresponding loading path (down).

265 The obtained elongation time-evolutions and the corresponding transverse-axial loading

266 path can be seen in Figure 8, which clearly confirms that an almost equi-bi-axial loading is

267 imposed to the sample. This bi-axial state can also be seen in Figure 9, which also shows the
268 set-up capacities in both directions.



269

270 Figure 9: Sample force-elongation curves in axial and transverse directions.

271 Formulae (8) and (9) show that the sliding velocity reached at the interface during the
272 stationary phase is of the order of 1 to 3 m/s, like during the friction identification test. It
273 confirms the relevance of the friction coefficient value used for data processing.

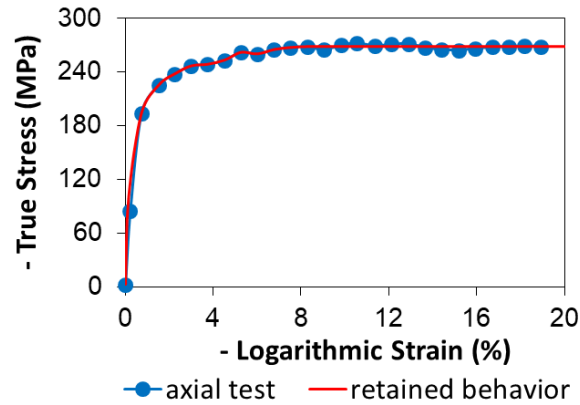
274 **4 Check of the measurement consistency thanks to simulations**

275 4.1 Material modelling

276 A typical result obtained from an axial compression test on a cuboidal sample (Figure
277 4a), and chosen as a reference is reported in Figure 10.

278 As there are few measurement points in the elastic phase, a 70 GPa Young modulus and
279 a 0.3 Poisson's ratio are assumed (AW-2017A characteristics). A yield stress - plastic strain
280 law with a 100 MPa elastic threshold, and which exactly fits the measurements is then chosen
281 (see retained behavior in Figure 10). To simplify the modelling, the stress is supposed to
282 saturate at a 268 MPa threshold value, which also well fits the measurements. In practice, the
283 axial curves are reproducible for strains lower than 3 %, but a 4 % dispersion is observed for

284 the threshold value. These parameters are implemented in a Von-Mises elastic-plastic model
285 with an isotropic hardening. The used software is ABAQUS.



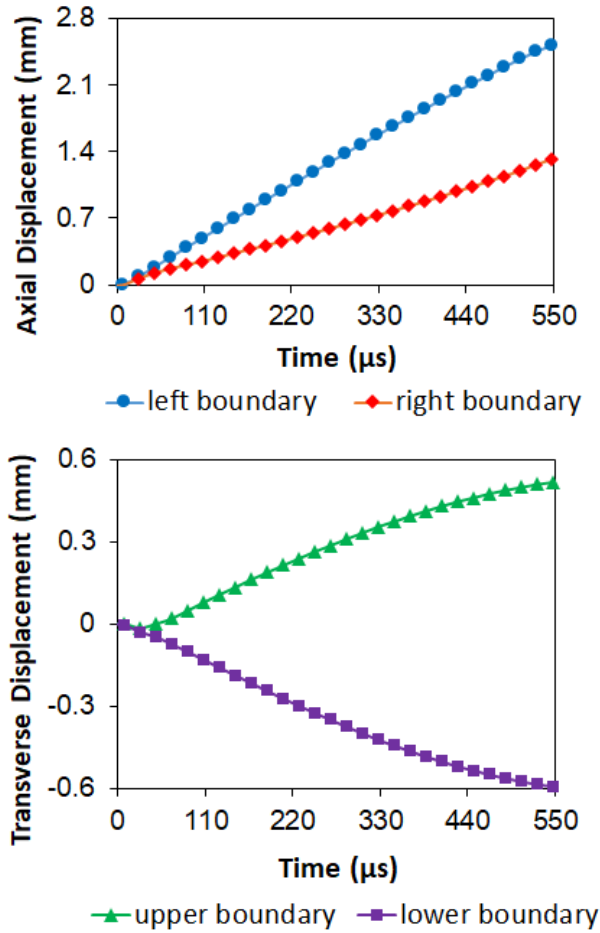
286

287 Figure 10: Stress-strain law identified from a test.

288 4.2 Simulation of the sample behavior

289 Because of its cross-shape, the stress and the strain states in this sample are
290 heterogeneous. So, to check the force and elongation measurement consistency, a finite-element
291 simulation must be performed. The calculations are performed with the Figure 10 retained
292 behavior. The fact that the model identification test has been carried out in the same dynamic
293 conditions as the bi-axial test implies that the method remains valid with a strain rate dependent
294 behavior. If any contact occurs between the arm free boundaries, it will be supposed frictionless.
295 According to Figure 6, the bi-axial set-up, and therefore the cross sample, are in a satisfactory
296 equilibrium. This equilibrium state can be accurately verified by processing a dynamic explicit
297 calculation. The chosen density is 2800 kg.m^{-3} .

298 The displacements estimated thanks to DIC calculations are directly imposed to the
299 sample interfaces (Figure 11). Because of the image plan symmetry, only half the sample has
300 to be modelled (Figure 12). 8-node linear brick elements are used. The chosen brick size is
301 0.25 mm, which leads to the Figure 12 mesh.



302

303

Figure 11: Imposed boundary displacements (axial ones oriented from left to right and

304

transverse ones oriented from top to bottom).

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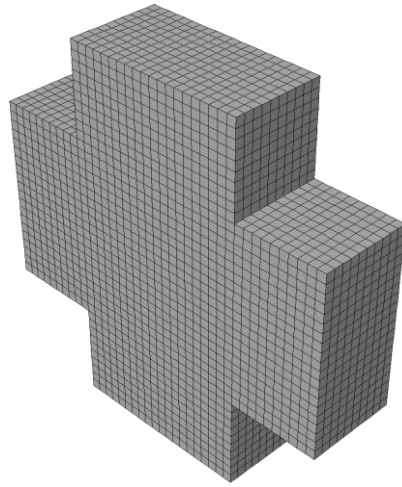
The dynamic explicit calculations display that the forces applied at opposite boundaries are almost equal until 60 μs, and become exactly the same after this duration. The sample equilibrium assumption being checked, the axial force is defined as the left and right boundary force average and the transverse force as the upper and lower boundary force average.

309

The numerical and the experimental forces in both directions can then be compared to check the measurement consistency. Because of the behavior dispersion (see Section 4.1), a 4 % relative uncertainty must be considered for the numerical forces. The friction is taken into account by determining the measured transverse force with the 0.87 estimated F_t/F_{eo} ratio (see end of section 3.3). The 4 % relative uncertainty of this ratio also leads to a 4 % uncertainty of

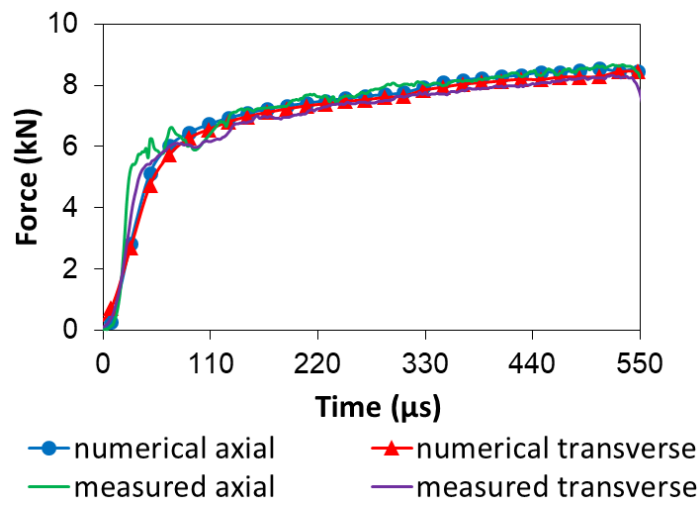
313

314 the measured transverse force. It could be noted that the uncertainty due to friction is not so
315 high.



316

317 Figure 12: Meshed sample model accounting of the symmetry plan.



318

319 Figure 13: Comparison between the experimental forces and the numerical forces obtained
320 from the measured displacements and from the identified model.

321 In Figure 13, the numerical forces are obtained at the displacement measurement
322 frequency (i.e. every 20 μs). As expected, the fit is not perfect at the very beginning of the test
323 because of the following reasons:

- 324 - These is a too weak number of acquisition points in the elastic phase to accurately
325 measure the brutal increase of the forces.
- 326 - The sample equilibrium being not perfect during the first 60 μs , the axial and the
327 transverse forces in the cross sample do not exactly correspond to measured forces at
328 the output bar interfaces (i.e. F_{io} and F_{eo} multiplied by the friction dependent ratio).
- 329 - The transverse force is determined from the sliding friction coefficient, and as explained
330 in section 3.3, this method overestimates the force at the very beginning of the test, i.e.
331 in the adhesion phase.

332 However, during the stationary phase, the measurement consistency is clearly proven.
333 It validates the identified sample model. Although this processing is not performed to measure
334 the friction, it also shows that the friction coefficient used to process the data is consistent.

335 4.3 Simulation of the whole apparatus behavior

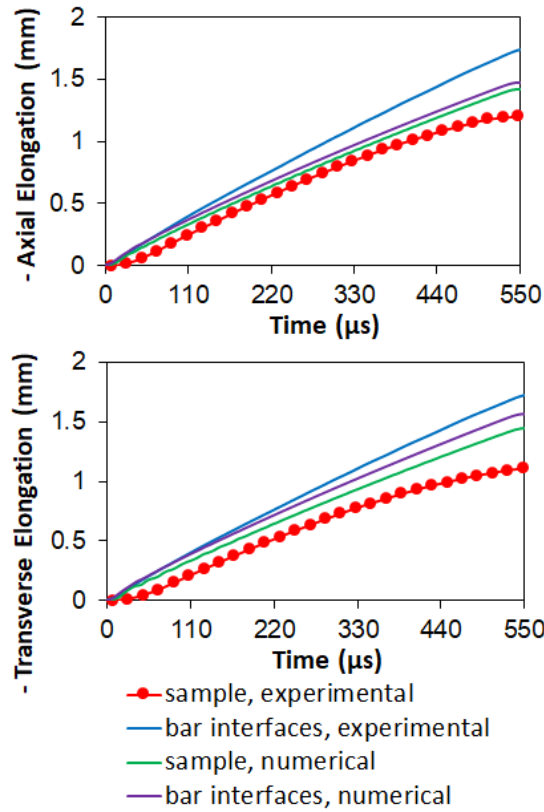
336 The axial and transverse forces in the sample are both determined from the forces at the
337 interfaces between the output bars and the set-up. This determination is based on the
338 equilibrium assumption, which actually implies a quick enough transmission of the wave
339 through the mechanism. A satisfactory, but not perfect, equilibrium is experimentally shown in
340 Figure 6. However, the incident strain wave ε_i and the reflected one ε_r being rather opposite, as
341 shown in Figure 15, the input force F_i determination from formula (1) is very noise sensitive.
342 A simulation of the whole bar set-up has thus been performed to study this equilibrium. The
343 used software is still ABAQUS in its explicit version.

344 The aluminum sample is supposed to have the properties given in Sections 4.1 and 4.2.
345 The bi-axial mechanism parts are supposed to be made of the input bar steel (it is actually the
346 case) whose Poisson's ratio is 0.3 (density and wave celerity given in Table 1), and to remain
347 purely elastic. The same assumptions are used to model the output bars (densities and wave

348 celerities also given in Table 1). The striker initial velocity is $6 \text{ m}\cdot\text{s}^{-1}$, which is consistent with
349 experimental measurements (Figure 15). The selected friction coefficient at the contact surfaces
350 is 0.07, as measured in Section 3.3. The static and the dynamic coefficients are supposed to be
351 the same.

352 Because of the two symmetry planes (the cutting plane in Figure 1 and the one normal
353 to the section plane and containing the axis), only a quarter of the system is studied. The bars
354 and the projectile are modelled by 6-node linear triangular prism elements (ABAQUS
355 terminology) whose approximate size is 5 mm. The two parts with the sliding surfaces and the
356 tubes inserted between the sample and the input bar and between the sample and the internal
357 output bar are modelled by the same elements but their rough sizes are respectively 10 mm and
358 2.5 mm. The triangular part is composed of two triangular prism elements separated by the
359 symmetry plane. The sample is merely composed of four 8-node linear brick elements: one
360 corresponding to the center and three corresponding to the three arms represented in the
361 simplified model. As shown in Figure 15, element sizes are thin enough to roughly fit the
362 measurements. The chosen time increment is $0.1 \mu\text{s}$.

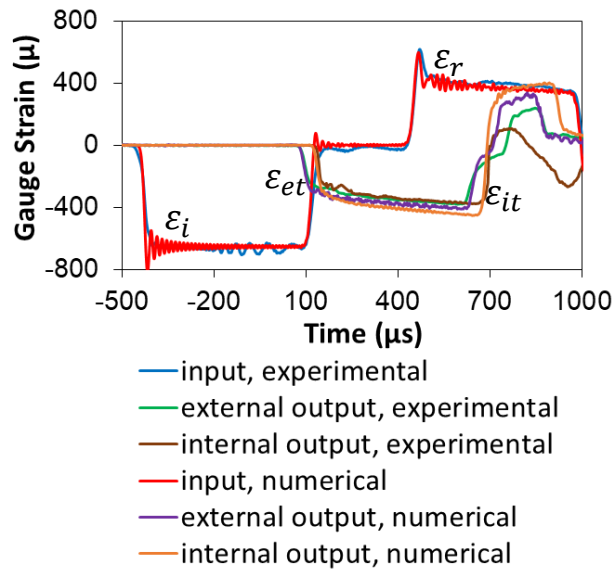
363 The experimental results display that the contacts in the bi-axial mechanism are not
364 perfect. In Figure 14, a non-negligible gap can be seen between the sample elongations and the
365 differences between the input and the output bar displacements. As explained in Section 3.4,
366 these quantities would be identical if there was neither clearances nor intermediate strains. The
367 numerical equivalent of this gap is lower, and only due to the elastic strains of the mechanism
368 parts. It implies that the numerical set-up is a little bit stiffer than the real one. However, the
369 stiffness remaining in the same order, it enables to check the general relevance of the set-up.



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371 Figure 14: Comparisons between the sample elongations and the differences between the bar
 372 displacements.

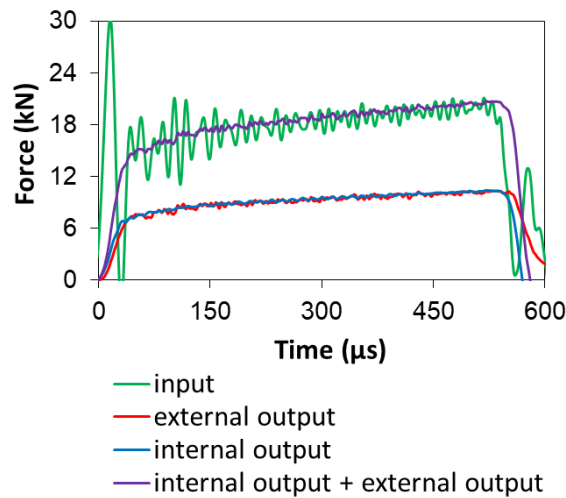
373 The gauges are glued at the middle of the input bar and on the two output bars at 0.374 m
 374 from the interface with the set-up on the external bar, and at 0.612 m on the internal one. The
 375 experimental and the numerical strain time-evolutions are compared in Figure 15. The input
 376 gauge first measures the incident wave ε_i , and then the reflected wave ε_r . The external output
 377 gauge and the internal one measure the external transmitted wave ε_{et} and the internal transmitted
 378 wave ε_{it} . ε_i can be seen as a loading imposed to the bi-axial set-up whereas ε_r , ε_{et} and ε_{it} can be
 379 seen as the set-up response to the imposed loading. Figure 15 shows that the simulated ε_i
 380 (proportional to the striker initial velocity) rather fits the experimental one, despite some
 381 spurious oscillations. The numerical transmitted waves are a little bit higher than the
 382 experimental ones, which is fully consistent with a modelled set-up stiffer than the real one.



383

384 Figure 15: Experimental and numerical strain time evolutions at the gauge positions.

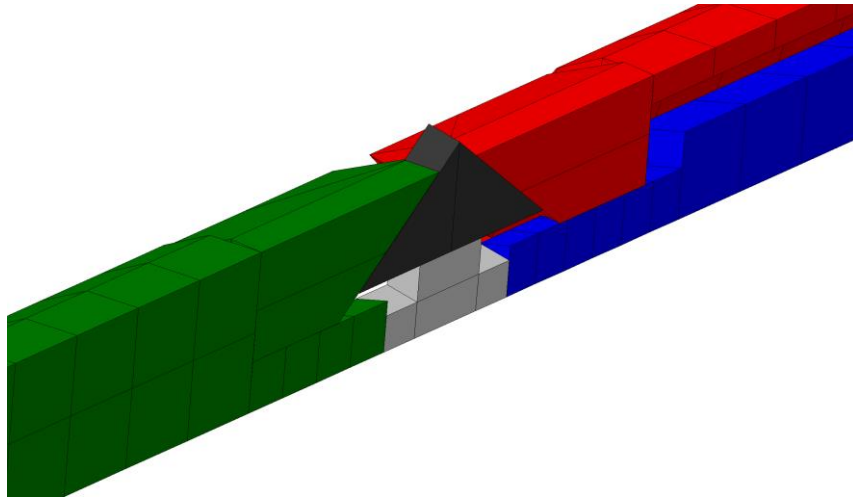
385 Figure 16 finally shows that, in spite of numerical oscillations, the input force and the
 386 total output force are in mean equilibrium and that both output forces are the same.



387

388 Figure 16: Time evolutions of the numerical forces at the interfaces.

389 The finite element mesh can be seen in Figure 17. As the contacts are not perfectly
 390 modeled, using a smaller mesh would be useless to better fit the measurements.



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Figure 17: Finite element mesh.

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5 Conclusion

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The aim of the study was to check the relevance of a newly designed Hopkinson bi-axial compression set-up. The sample axial compression is directly generated by an internal output bar whereas the transverse compression is indirectly generated by an external output bar via a mechanism. The friction in the mechanism is identified in the relevant dynamic conditions from comparisons between axial and transverse compression tests on cuboid samples. To reproduce the sliding velocities reached at the mechanism sliding interfaces during the bi-axial test, these cuboid samples are made of the bi-axial sample material. The friction being identified, any sample can now be tested.

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A calibration bi-axial test has been performed on a cross sample with a simple shape, and therefore easy to model. The measurements show that the device ensures an approximate equality between the axial and the transverse loadings, and the experimental result reliability is proven by a numerical modelling of the bi-axial sample. The set-up can therefore be used in the future for characterization on more complex samples and materials (which was not the aim of this first study).

408 Finally, the design of an easily buildable set-up generating and measuring a rather
409 isotropic dynamic bi-axial loading has been achieved.

410 **Conflict of Interest**

411 The authors declare that they have no conflict of interest.

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