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# Material Decomposition in Spectral CT using deep learning: A Sim2Real transfer approach

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**ABSTRACT** The state-of-the art for solving the nonlinear material decomposition problem in spectral computed tomography is based on variational methods, but these are computationally slow and critically depend on the particular choice of the regularization functional. Convolutional neural networks have been proposed for addressing these issues. However, learning algorithms require large amounts of experimental data sets. We propose a deep learning strategy for solving the material decomposition problem based on a U-Net architecture and a Sim2Real transfer learning approach where the knowledge that we learn from synthetic data is transferred to a real-world scenario. In order for this approach to work, synthetic data must be realistic and representative of the experimental data. For this purpose, numerical phantoms are generated from human CT volumes of the KiTS19 Challenge dataset, segmented into specific materials (soft tissue and bone). These volumes are projected into sinogram space in order to simulate photon counting data, taking into account the energy response of the scanner. We compared projection- and image-based decomposition approaches where the network is trained to decompose the materials either in the projection or in the image domain. The proposed Sim2Real transfer strategies are compared to a regularized Gauss-Newton (RGN) method on synthetic data, experimental phantom data and human thorax data.

**INDEX TERMS** Spectral CT, inverse problem, deep learning, transfer learning

## I. INTRODUCTION

The new generation of spectral computed tomography (SPCCT) scanners include photon-counting detectors (PCDs), which count single photons and resolve their energy [1]. With this extra dimension, SPCCT provides higher contrast with respect to conventional CT and allows for material decomposition, which opens up new diagnosis possibilities [2], [3]. PCDs can be ex-

ploited for material decomposition, including K-edge imaging, which uses the discontinuity at diagnostic energies of the linear attenuation coefficient of high-Z element-based contrast agents such as gadolinium, gold or bismuth. Material decomposition could be used to quantify calcium content to assess bone and teeth health, determine kidney stone composition, determine liver iron concentrations, determine bone marrow

composition, characterize plaques [3], [4], abdominal imaging [5], evaluating the risk of breast cancer [6], and k-edge contrast agent quantification, among others.

A variety of spectral CT image reconstruction methods have been proposed. Some of these methods have focused on compressed sensing and algorithms that promote sparsity in the image domain, using total variation (TV) [7], vector-valued generalization of TV [8], nonlocal TV [9], tight frames [10], dictionary learning methods [11], prior-based methods [12], and low-rank [13]–[15]. In this work, we focus on reconstruction algorithms that perform material decomposition.

Material reconstruction algorithms can be divided into projection-based [16], [17], image-based [18], [19], and one-step inversion approaches [20], [21]. Image-based methods reconstruct first each energy bin and then perform material decomposition on the image domain assuming that images are monochromatic, which may lead to beam hardening artefacts. Projection-based and one-step inversion methods are a natural choice as they take into account the inherent physics. One-step methods are mathematically the most elegant, as they solve the problem in one step, but they can be computationally expensive. Projection-based methods firstly decompose the energy-resolved sinograms into material-specific sinograms and then perform tomographic reconstruction of each of the decomposed sinograms [22]. An advantage of this approach is that it allows independent decomposition of each projection view, which can be parallelized, making the computational process more convenient [22].

State-of-the art for solving the material decomposition problem are optimization methods, also named variational approaches [20], [22]–[26]. Image-based material decomposition is a convex problem for a least squares functional [21]. Material decomposition in the projection domain is a nonlinear, nonconvex inverse problem although it is convex in a well defined region of the solution space [22], [26]. For projection-based algorithms, a previous work [22] proposed a regularized material-specific Gauss-Newton (RGN) method, which outperformed widely used unregularized maximum likelihood method. In [26], authors assessed an iterative regularization scheme based on the Bregman iteration.

While variational methods are robust and have shown improved results with respect to unregularized approaches, they present several disadvantages. First, they can be computationally slow, given their iterative nature. Second, their performances rely on the prior knowledge of the scanner energy response and the choice of the regularization functional. With regard to the adopted model, for instance, the detector response can be degraded by charge sharing, pulse pileup, and energy loss due to K-escape [27]. The effect of assum-

ing a perturbed detector response can have detrimental effects on image quality, as shown in [28]. With regard to the choice of the regularization functional, specific regularization for the decomposed materials have shown to improve image quality with respect to unregularized approaches [22], but the choice is far from being optimal.

Recently, deep convolutional neural networks (CNN) have shown outstanding results in several image processing tasks [29], [30]. CNNs have been also proposed for solving several inverse problems, including image restoration and image reconstruction [31]–[36]. Among the diverse CNN configurations, U-Net has shown outstanding results for image segmentation [37] and has been applied to postprocessing in CT [31] and to artifact removal of nonlinear CT images [38]. Several works have also proposed deep learning for solving the material decomposition, mainly in the image domain. In [39], the authors trained a U-Net network using simulated phantoms constructed from random combinations of materials and tested the model on mice data. In [9], the authors proposed a VGG-16 network and tested it on Shepp-Logan synthetic data and experimental cylindrical phantoms. The previously proposed neural networks approaches in the projection domain have been based on multilayer perceptrons (using fully connected layers) for decomposing materials in a pixel-by-pixel basis [40], [41], [42]. In [40], the authors used a neural network with two hidden layers followed by a denoising method to mitigate noise.

The recent success of CNNs for image processing tasks relies on large-scale annotated data sets such as ImageNet with millions of images [43], [29]. However, equivalent medical imaging data sets are not common. Transfer learning (TL) has emerged as a promising candidate technique to compensate the lack of large-scale medical imaging data sets. TL is the ability of a system or model to recognize and apply knowledge and skills learned in previous domains/tasks to novel domains/tasks. TL assumes that the model can generalize to new tasks or new domains by learning features or factors that are common between source and target tasks [44]. TL becomes relevant when labelled training data, time or computational power are limited, so it is particularly applicable to medical imaging. Different approaches for TL can be found in [45], [46]; most common is to pre-train a model on a large-annotated data set and then to fine tune the model on a more specific and smaller data set [47], [48]. Recent works proposed related TL approaches based on fine tuning for material decomposition [28], [42]. However, in this work we follow a Sim2Real transfer approach where the knowledge that one learns from synthetic data is transferred to a real-world scenario [49], [50]. The Sim2Real strategy is based on the fact that synthetic

data is almost infinitely accessible and diverse, and it becomes pertinent when experimental annotated data are very limited or non existent, which is the case of SPCCT. While learning-based approaches perform reasonably well given experimental training data, they may not necessarily work well when trained only on synthetic data. In cases in which synthetic data generalize poorly to real data, data augmentation strategies are generally followed.

In this work, we propose a deep learning strategy for solving the material decomposition problem based on a U-Net architecture and a Sim2Real transfer approach. In order for the Sim2Real approach to work, synthetic data must be realistic and representative of the experimental data. For this purpose, numerical phantoms are generated from human CT volumes of the KiTS19 Challenge dataset [51]. Numerical data are then computed by segmenting CT volumes into specific materials (soft tissue and bone), projecting the material volumes and simulating photon counting data, taking into account the energy response of the scanner. In order to compare projection- and image-based decomposition strategies, the U-Net is trained to decompose the materials either in the projection domain (U-Net-P) or in the image domain (U-Net-I). These are compared to a regularized Gauss-Newton (RGN) method in the projection domain [22] and all methods are assessed on both numerical and experimental data. The proposed approach combines a CNN model with training on human data, which allows to implicitly learn the real prior distribution of the decomposed materials [52]. This is particularly interesting from a Bayesian perspective to inverse problems as it motivates the choice of the regularization functional as a particular selection for the prior distribution of the unknown variable. Thus, our method differs from previous CNN methods based on the image domain and approaches that are trained on experimental phantom data only.

## II. FORWARD MODEL

We assume a 2D sensor with  $P$  pixels and  $I$  energy bins and an object with  $V$  voxels made of  $M$  materials. We image the object under  $\Theta$  projections. Let  $\mathbf{s} = (s_{1,1}^1, \dots, s_{i,p}^\theta, \dots, s_{I,P}^\Theta)^\top$  be the measurement vector, where  $s_{i,p}^\theta$  represents the photon counts measured in the  $i$ -th energy bin at the  $p$ -th pixel under the  $\theta$ -th projection, and  $\boldsymbol{\rho} = (\rho_{1,1}, \dots, \rho_{m,v}, \dots, \rho_{M,V})^\top$  be the (unknown) mass densities vector, where  $\rho_{m,v}$  is the mass density for the  $m$ -th material at the  $v$ -th voxel. The forward model in spectral CT can be represented as the mapping

$$\mathbf{s} = \mathcal{G}(\boldsymbol{\rho}). \quad (1)$$

The forward model  $\mathcal{G}$  can be seen as the composition of the linear X-ray transform and a non-linear spectral

mixing operator. The X-ray transform  $\mathcal{X}$  applies to each material independently, i.e.,

$$\mathbf{a}_m = \mathcal{X}(\boldsymbol{\rho}_m), \quad 1 \leq m \leq M \quad (2)$$

where  $\boldsymbol{\rho}_m = (\rho_{m,1}, \dots, \rho_{m,v}, \dots, \rho_{m,V})^\top$  and  $\mathbf{a}_m = (a_{m,1}^1, \dots, a_{m,p}^\theta, \dots, a_{m,P}^\Theta)^\top$  represent mass density and projected mass density for the  $m$ -th material, respectively. Spectral mixing applies to each view and detector pixel independently, i.e.,

$$\mathbf{s}^\theta = \mathcal{F}(\mathbf{a}^\theta), \quad 1 \leq \theta \leq \Theta \quad (3)$$

where  $\mathbf{a}^\theta = (a_{1,1}^\theta, \dots, a_{m,p}^\theta, \dots, a_{M,P}^\theta)^\top$  and  $\mathbf{s}^\theta = (s_{1,1}^\theta, \dots, s_{i,p}^\theta, \dots, s_{I,P}^\theta)^\top$ . In particular, we consider the following non linear mixing [23] (excluding pileup and charge sharing effects)

$$s_{i,p}^\theta = \int_{E \in \mathcal{E}} n_{0,p}(E) d_{i,p}(E) \exp \left[ - \sum_{m=1}^M a_{m,p}^\theta \tau_m(E) \right] dE \quad (4)$$

where  $\mathcal{E}$  is the range of energy delivered by the x-ray tube,  $n_{0,p}(E)$  is the x-ray source energy spectrum at the  $p$ -th pixel,  $d_{i,p}(E)$  is the energy-dependent detector response function at the  $p$ -th pixel for the  $i$ -th bin, and  $\tau_m(E)$  is the energy-dependent mass attenuation coefficient of the  $m$ -th material. This assumes that the local linear attenuation coefficient (LAC) of the object at energy  $E$  and the voxel  $\mathbf{x}$ ,  $\mu(E, \mathbf{x}_v)$ , can be decomposed as the sum of  $M$  basis functions that are separable in energy and space:

$$\mu(E, \mathbf{x}) = \sum_{m=1}^M \rho_m(\mathbf{x}) \tau_m(E), \quad (5)$$

where  $\rho_m(\mathbf{x}_v) = \rho_{m,v}$  and  $\mu_m(\mathbf{x}_v) = \mu_{m,v}$  for a voxel  $\mathbf{x}_v$ .

Data simulation involves solving the forward problem. For this, we first project the mass densities  $\boldsymbol{\rho}_m$  following (2) to get the projected mass densities  $\mathbf{a}_m$  and then we apply the spectral mixing operator (4) to get the photon-counting data at the different energy bins  $\mathbf{s}$ .

## III. SPECTRAL CT IMAGE RECONSTRUCTION

Solving the spectral CT image reconstruction problem in one step involves inverting the  $\mathbb{R}^{MP} \rightarrow \mathbb{R}^{I\Theta}$  non-linear mapping (1). In this work, we instead adopt two different two-step approaches: projection- and image-based decomposition approaches.

### A. PROJECTION-BASED APPROACH

The projection-based approach splits the problem into  $\Theta$  inversions of  $\mathbb{R}^{MP} \rightarrow \mathbb{R}^{IP}$  mappings (3), which decompose projections for different energy bins into projections for different materials, followed by  $M$  inversions of  $\mathbb{R}^V \rightarrow \mathbb{R}^{P\Theta}$  (2), which provide tomographic reconstructed images for the different materials. This



approach reduces the size of the subproblems, offering a natural parallelization scheme (e.g. decomposing all angles in parallel, reconstructing all materials in parallel), and allows to separate nonlinear (i.e. spectral) from linear (i.e. tomographic) mixing. Thus, the two-step approach allows to reduce the computational complexity with respect to the one-step method by first solving the material decomposition problem (3), projection by projection, and then solving the tomographic reconstruction problem for each material (2). Material decomposition is done projection by projection, which allows to include an explicit regularization functional or to implicitly learn the prior distribution. A previous work found that a regularization approach led to significant improvement with respect to an unregularized pixel-by-pixel decomposition, which was very sensitive to noise [22]. An alternative to solving the material decomposition problem projection by projection would be to decompose all projection views at once. While this could allow to introduce further regularization on the angle dimension, we chose single projection decomposition as it allows for parallelization across angles, reducing computational complexity.

For the first step (material decomposition in the projection domain), we consider two different methods: a regularized variational framework and a deep learning strategy, as described below.

#### 1) Projection-based material decomposition with a variational method

Using a variational framework, material decomposition has been previously formulated as the minimization of the following cost function [22]:

$$\Phi(\mathbf{a}^\theta) = \frac{1}{2} \|\mathbf{s}^\theta - \mathcal{F}(\mathbf{a}^\theta)\|_{W^\theta}^2 + \alpha \sum_m \mathcal{R}_m(\mathbf{a}^\theta), 1 \leq \theta \leq \Theta \quad (6)$$

where the data fidelity term is a weighted least square functional to approximate a Poisson distribution,  $W^\theta = \text{diag}(1/\sqrt{\mathbf{s}^\theta})$  is a weighting matrix,  $\alpha$  is a regularization parameter, and  $\mathcal{R}_m$  accounts for specific material regularization. We chose second-order and first-order Tikhonov regularization for soft tissue and bone, respectively, as suggested in [22]. While two different values of the regularization parameter could be used for different materials, it was previously found to not lead to significant improvement [22]. Cost function (6) is efficiently minimized by using a Gauss Newton algorithm (RGN); MATLAB code for RGN is available from the Spectral X-ray image reconstruction Spray toolbox [53].

#### 2) Projection-based material decomposition with U-Net (U-Net-P)

Deep learning has been recently proposed for inverse problems [31], [54]. In this work, we want to learn the

mapping

$$\mathcal{H}_\beta : \tilde{\mathbf{s}}^\theta \mapsto \tilde{\mathbf{a}}^\theta, \quad (7)$$

where  $\beta$  indicates the parameters of the neural network,  $\tilde{\mathbf{s}}^\theta$  corresponds to the normalized data defined as

$$\tilde{\mathbf{s}}^\theta = \ln(\hat{\mathbf{s}}/\mathbf{s}^\theta) \quad (8)$$

with  $\hat{\mathbf{s}} = \mathcal{F}(0)$  representing the measurement in the absence of the object, and  $\tilde{\mathbf{a}}$  corresponds to the normalized outputs. We normalize the output material per material across the entire training set, i.e.,  $\tilde{a}_{m,p}^{\theta,n} = a_{m,p}^{\theta,n} / \max_{p,\theta,n} a_{m,p}^{\theta,n}$ .

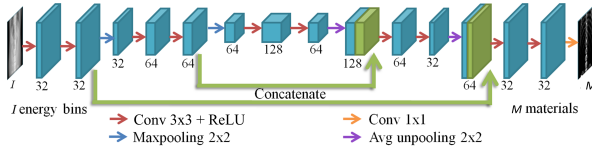
Normalization of input and output variables prior to training a neural network model is common practice to avoid a slow or unstable learning process. In this case, normalization of the outputs is motivated by the fact that different materials may have different range of values. For the inputs, photon-counting data have very large values; in addition, normalizing the data by the acquisition in the absence of the object,  $\hat{\mathbf{s}}$ , may decrease the sensitivity to modeling errors.

Learning means finding the parameters  $\beta$  of the network that minimizes the following loss function

$$\begin{aligned} \Xi(\beta) &= \sum_{n=1}^N \|\mathcal{H}_\beta(\tilde{\mathbf{s}}^n) - \tilde{\mathbf{a}}^n\|^2 \\ &= \sum_{n=1}^N \sum_{m=1}^M \|\mathcal{H}_{\beta,m}(\tilde{\mathbf{s}}^n) - \tilde{\mathbf{a}}_m^n\|^2, \end{aligned} \quad (9)$$

where  $(\tilde{\mathbf{s}}^n, \tilde{\mathbf{a}}^n)$  are  $N$  input-output vector pairs (3) that can be reshaped into input-output array pairs of size  $(P_x \times P_y \times I, P_x \times P_y \times M)$ ,  $N$  is the number of projection images in the training set, and each projection image is of size  $P_x \times P_y$ . Minimization of (9) was done with Adam method under TensorFlow, with learning rate  $10^{-4}$  and batch size of 16. Training and test losses were computed during training and early stopping was adopted to avoid overfitting.

We use a U-Net architecture [37], which consists in a contracting multi-scale decomposition path and a symmetric expanding path with skip connections at each scale. The contracting path comprises  $3 \times 3$  convolutions (with the zero-padding) each followed by a rectified linear unit (ReLU) and alternated with a  $2 \times 2$  max pooling operation with stride 2 for downsampling by half every two convolution operations. At each downsampling the number of feature channels is doubled, with 32 channels in the first scale and 128 channels in the last scale. The expansive path comprises the same convolution operations as in the contracting path but alternated with upsampling by two every two convolution operations. The final layer is a  $1 \times 1$  convolution used to map the 32 channel layer to the output with the desired  $M$  number of decomposed materials. This leads to a total of 14 hidden layers (figure 1).



**FIGURE 1.** U-Net architecture for material decomposition in the projection domain (U-Net-P) and in the image domain (U-Net-I). For U-Net-P, the input is a stack of photon counting projection images for  $I$  energy bins ( $P_x \times P_y \times I$ ), and output is a stack of the decomposed material projection images for  $M$  materials ( $P_x \times P_y \times M$ ) for a projection angle  $\theta$ . For U-Net-I, the input is a stack of reconstructed images for  $I$  energy bins ( $Q_x \times Q_y \times I$ ), and output is a stack of the decomposed material reconstructed images for  $M$  materials ( $Q_x \times Q_y \times M$ ) for a 2D slice.

### 3) Tomographic reconstruction of decomposed material mass densities

The second step corresponds to tomographic reconstruction for the different materials (2). For numerical data, we assume parallel geometry and perform tomographic reconstruction using filtered back-projection algorithm. For experimental data, tomographic reconstruction is done using a regularized conjugate gradient method within the Reconstruction Toolkit (RTK) [55], which minimizes the following cost function:

$$\Psi(\rho_m) = \|\mathcal{X}\rho_m - \mathbf{a}_m\|_2^2 + \gamma \|\nabla \rho_m\|_2^2, \quad (10)$$

where  $\gamma$  is a regularization parameter. The forward projection uses ray casting with trilinear interpolation and the backprojection is voxel-based with bilinear interpolation. Parameters were selected empirically as  $\gamma = 100$  and  $k = 25$ , where  $k$  is the number iterations of conjugate gradient.

## B. IMAGE-BASED APPROACH

The image-based approach is a widely used two-step approach for material decomposition in spectral CT [18], [19]. In the first step, images for the different energy bins,  $\mu_i^{\text{bin}}$ , are reconstructed by solving

$$\tilde{\mathbf{s}}_i = \mathcal{X}(\mu_i^{\text{bin}}), \quad 1 \leq i \leq I, \quad (11)$$

where  $\mu_i^{\text{bin}} = (\mu_{i,1}^{\text{bin}}, \dots, \mu_{i,v}^{\text{bin}}, \dots, \mu_{i,V}^{\text{bin}})^\top$ ,  $\mu_{i,v}^{\text{bin}}$  is the reconstructed image for the  $i$ -th energy bin at the  $v$ -th voxel, and  $\tilde{\mathbf{s}}_i$  corresponds to the normalized data (8). The first step (11) corresponds to  $I$  inversions of  $\mathbb{R}^V \rightarrow \mathbb{R}^{P\Theta}$  (11).

The second step is the material decomposition in the image domain

$$\mu^{\text{bin}} = \mathcal{M}(\rho), \quad (12)$$

where  $\mu^{\text{bin}} = (\mu_1^{\text{bin},\top}, \dots, \mu_i^{\text{bin},\top}, \dots, \mu_I^{\text{bin},\top})^\top$ ,  $\rho = (\rho_1^\top, \dots, \rho_m^\top, \dots, \rho_M^\top)^\top$  and  $\mathcal{M}$  is the spectral mixing operator in the image domain. We remark that  $\mathcal{M}$  cannot be analytically described in a simple manner without taking an approximation and that we are only interested in learning its inverse mapping. Step (12) requires one inversion of the mapping  $\mathbb{R}^{VM} \rightarrow \mathbb{R}^{VI}$ .

The implementation of the two-step approach used in this work is described as follows.

### 1) Tomographic reconstruction of energy bins

Tomographic reconstruction for the different energy bins (11) is solved using the same methods and same parameters as described in section III-A3. For experimental data, the regularized conjugate gradient method minimizes

$$\Psi(\mu_i^{\text{bin}}) = \|\mathcal{X}\mu_i^{\text{bin}} - \tilde{\mathbf{s}}_i\|_2^2 + \gamma \|\nabla \mu_i^{\text{bin}}\|_2^2. \quad (13)$$

### 2) Image-based material decomposition with U-Net (U-Net-I)

We solve the material decomposition problem in the image domain (12) using deep learning. For this, we aim to learn the mapping

$$\mathcal{M}_\omega^{-1} : \mu^{\text{bin},j} \mapsto \rho^j, \quad (14)$$

where  $\mathcal{M}^{-1}$  is the inversion of the mixing operator in the image domain and  $(\cdot)^j$  stands for the  $j$ -th slice in the volume. In this case, input and outputs are not normalized because mass densities are already naturally normalized to water.

Learning means finding the parameters  $\omega$  of the network that minimizes the following loss function

$$\begin{aligned} \Pi(\omega) &= \sum_{n=1}^N \|\mathcal{M}_\omega^{-1}(\mu^{\text{bin},n}) - \rho^n\|^2 \\ &= \sum_{n=1}^N \sum_{m=1}^M \|\mathcal{M}_{\omega,m}^{-1}(\mu^{\text{bin},n}) - \rho_m^n\|^2 \end{aligned} \quad (15)$$

where  $(\mu^{\text{bin},n}, \rho^n)$  are  $N$  input-output vector pairs (12) that can be reshaped into input-output array pairs of size  $(Q_x \times Q_y \times I, Q_x \times Q_y \times M)$ ,  $N$  is the number of image slices in the training set, and each image is of size  $Q_x \times Q_y$ . Minimization of (15) was done with the same method and the same U-Net architecture as described in the projection domain (figure 1).

## C. DATA AND IMAGE EVALUATION

### 1) Numerical human phantoms

Numerical human phantoms are made of soft tissue and bone and are built from CT volumes obtained from the KiTS19 challenge data set (2019 Kidney Tumor Segmentation Challenge, <https://kits19.grand-challenge.org/data/>) [51] (figure 2). We used 50 phantoms for training, 3 for evaluation, and 9 for test. CT volumes have voxel size  $0.96 \text{ mm} \times 0.96 \text{ mm} \times 1.8 \text{ mm}$ . In order to facilitate numerical simulations, we processed CT volumes to get the same dimension: volumes were cropped to have 640 voxels in  $x$ - and  $y$ -dimensions and 100 voxels along  $z$ -axis. CT volumes were semi-automatically segmented into bone and soft-tissue using a combination of thresholding and morphological operations. After segmentation, we created

mass density volumes by normalizing the segmented volumes to have median value in the kidneys equal to  $1.1 \text{ g}\cdot\text{cm}^{-3}$ . Then, mass densities for both materials were projected using the Radon transform (assuming parallel geometry) to create the projected mass densities.

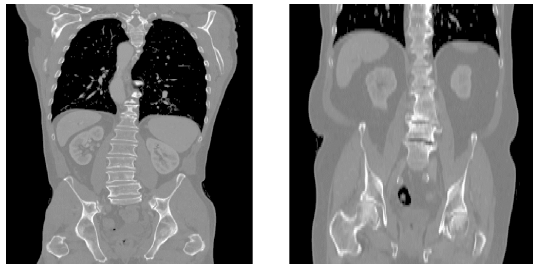


FIGURE 2. Two examples from the CT Kits19 data base.

Photon counting data were simulated taking into account the manufacturer source spectrum and detector response function and the linear attenuation coefficients (LACs) of the two materials. Both phantom creation and simulation were realized with the Spray toolbox [22], [53]. Noisy data was considered by assuming a Poisson distribution for a tube current of 200 mA, which corresponds to a total number of photons in a central pixel of the detector equal to  $N_0 = 6 \cdot 10^5$ . Projected data consisted of 360 projections over a 180 angle span and  $924 \times 8$  detector pixels.

In this work, we follow a Sim2Real transfer approach, so training data for the deep learning strategies are based on the numerical human phantoms. Training data for U-Net-P then consisted of 19440 projections (360 projections for 54 phantoms). In order to perform further data augmentation, projected volumes were randomly cropped along the  $z$ -dimension and data simulation and noise corruption were performed at runtime during training.

Training data for U-Net-I consisted of 5400 images (100 slices for 54 phantoms). Data augmentation was performed by random crop along all directions. In addition, data augmentation was performed to account for the appearance of bone tissue in the soft tissue image. For this, the bone image was first normalized and then scaled to have the maximum between 1.2 and 2.2 using random sampling from a uniform distribution. Then, this reference bone image was scaled again by  $\kappa_b$  to provide the final bone image. The reference bone image was also scaled by  $\kappa_s$  and added to the soft tissue image to provide the final soft tissue image. The values  $\kappa_b$  and  $\kappa_s$  were obtained from the ratios of the Gammex bone inserts ( $\kappa_b, \kappa_s$ ) as (0.77, 0.37), (0.01, 1.82), (0.80, 0.53), (0.45, 1.15). We remark that these ratios account only for the maximum values in the image but larger variations of bone values and

ratios are actually being considered because the bone image is not homogeneous. Given the computational cost of solving the two-step approach in the image domain, data augmentation and noise were done before training.

## 2) Experimental data

A SPCCT prototype system (Philips Medical Systems) installed at CERMEP, Lyon, was used for this study [56]. It is a 500 mm FOV system equipped with a conventional x-ray tube that can be set with a tube voltage at 80, 100, or 120 kVp and tube current values between 10 and 500 mA. Tube filtration absorbs low-energy x-rays so the subject is exposed to a spectrum that ranges from 35 to 120 keV. The system is based on photon counting detectors of 2-mm-thick cadmium zinc telluride with a pixel pitch of  $270 \mu\text{m} \times 270 \mu\text{m}$  at isocenter, ChromAIX2 application-specific integrated circuits combined with cadmium zinc telluride as sensor material, and operates in single photon-counting mode with energy discrimination. Photo-counting detectors allow up to 5 consecutive energy thresholds between 30 and 120 keV. The scan field of view is 500 mm in-plane, with a  $z$ -coverage of 17.5 mm in the scanner isocenter. Axial and helical scans over  $360^\circ$  are performed with 2400 projections per rotation.

We consider two data sets: an experimental phantom and human thorax data. For the experimental phantom, we used the CIRS (Computerized Imaging Reference Systems, Inc, USA) Electron Density Phantom [57], which is made of a cylinder of size  $330 \text{ mm} \times 270 \text{ mm} \times 50 \text{ mm}$  and a density of  $1.029 \text{ g}\cdot\text{cm}^{-3}$  and inserts as surrogates of different biological tissues. We used a mixture of inserts from the CIRS phantom and the GAMMEX Tissue Characterization Phantom Model 467 (Gammex Middleton, USA). Data were acquired using a tube voltage of 120 kVp and tube current of 198 mA using axial geometry, with a standard set of energy thresholds (30, 51, 62, 72, 81 keV). Data were binned to a final size of  $462 \times 16 \times 2400 \times 5$ . Final reconstructed voxel size was  $1 \text{ mm} \times 1 \text{ mm} \times 2 \text{ mm}$ . In order to compare the data SNR with previous work [28], we compute the total number of photons provided by the source in a central pixel of the detector. For this data set, the total number of photons was approximately  $N_0 = 6 \cdot 10^5$ .

The human thorax data set corresponds to an adult male volunteer. Data were acquired using a tube voltage of 120 kVp and exposure of 62 mAs using helical geometry (85 mA, 0.75 s rotation time and 1.03 pitch). Data were binned to a final size of  $924 \times 8 \times 24912 \times 5$ . This corresponded to a total number of photons of  $N_0 = 1.8 \cdot 10^5$ .

Image reconstruction of experimental data with both RGN and deep learning strategies take into account the source spectrum and the detector response function of

the scanner, following the spectral mixing definition (4). We have not included charge sharing and pulse pileup effects, which can lead to artefacts. We also remark that data calibrations and corrections included in the scanner manufacturer pipeline have not been included in this work.

### 3) Image evaluation

U-Net-P, U-Net-I and RGN were evaluated on synthetic data and on the two experimental data sets. The performance of RGN depends on the selection of the regularization parameter. Selecting the optimal regularization parameter in terms of MSE may lead to images with low noise but with loss of image details [26]. Thus, we provide results for RGN for two values of the regularization parameter:  $\alpha = 0.1$  (low regularization) and  $\alpha = 0.6$  (intermediate regularization). For the numerical test set, methods were assessed in terms of normalized Mean Squared Error (MSE) and Structural Similarity metric (SSIM) on both decomposed projections and reconstructed images, bias on reconstructed images for soft tissue and bone, and noise for soft tissue. Normalized MSE was computed for each material as follows:

$$\text{MSE}_m = \frac{\|\mathbf{a}_m - \mathbf{a}_m^{\text{Target}}\|_2}{\|\mathbf{a}_m^{\text{Target}}\|_2}. \quad (16)$$

Relative bias was computed for each material as follows:

$$\text{bias}_m = 100 \frac{|\bar{\rho}_m - \bar{\rho}_m^{\text{Target}}|}{\bar{\rho}_m^{\text{Target}}}, \quad (17)$$

where the mean was taken across a circular region in a homogeneous area (of radius equal to ten pixels) for soft tissue and in a mask for bone (comprised of pixels that belong to the support of bone in the phantom). Noise for soft tissue was computed as the standard deviation in the circular homogeneous region. In addition, methods were assessed by visual inspection.

For the experimental phantom data, methods were assessed in terms of quantification of soft tissue and bone inserts by computing the mean in a circular region with radius of 1 cm for a central slice. Both experimental phantom data and human thorax data were evaluated visually. For experimental data, we also computed a 'virtual' monochromatic image (for 60 keV) from the decomposed images in order to compare visually to the standard CT image provided by a conventional scanner. We chose 60 keV as a previous study found that monochromatic images between 60 and 70 keV could be considered as optimal surrogates of conventional CT images [58]. Monochromatic images were computed as the LACs at energy  $E$  and point  $\mathbf{x}$  in the reconstructed volume following (5).

## IV. RESULTS

### A. NUMERICAL THORAX PHANTOM DATA

Figure 3 shows decomposed images by RGN for two different values of  $\alpha$  and by U-Net-P. For  $\alpha = 0.1$ , which corresponds to little regularization, RGN provides accurate decomposition, recovering image details, but images are noisy. For  $\alpha = 0.6$ , RGN reduces noise but at the expense of excessive blurring, particularly in bone regions. This is well appreciated in the error images in figure 4. On the contrary, U-Net-P is able to reduce noise while maintaining image details, as can be appreciated in figure 5.

Tomographic reconstructions of decomposed data with RGN, U-Net-P and U-Net-I are shown in figure 6. These results are consistent with results obtained for the decomposed projections. For  $\alpha = 0.1$ , RGN recovers image details well but images are noisy. For  $\alpha = 0.6$ , RGN is able to remove noise but image details are lost. U-Net-P leads to similar reduction of noise than RGN for  $\alpha = 0.6$  while maintaining image quality, as it is well appreciated in the error images in figure 7. U-Net-I provides much higher image quality than projection-based methods, with less noise, better recovery of image details and excellent preservation of image texture.

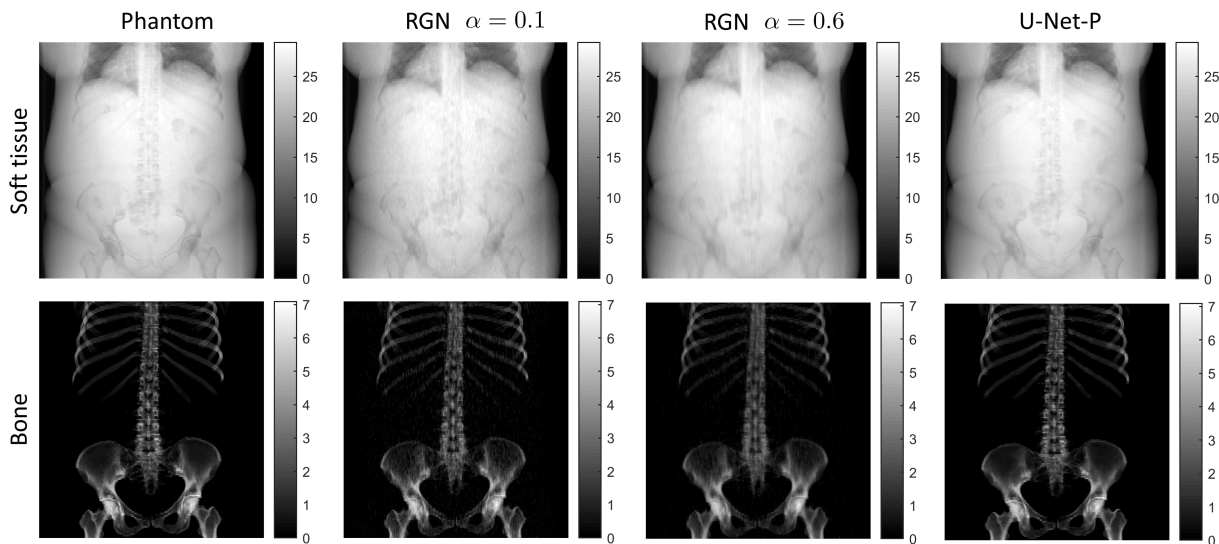
Figure 8 shows image details of the reconstructed images for soft tissue. RGN for  $\alpha = 0.6$  misses image details while U-Net-P presents better recovery than RGN for  $\alpha = 0.1$ . U-Net-I provides best results with almost perfect decomposition. The improved recovery of image details by U-Net-I can be explained by the presence of these details in the tomographic reconstructions of the different energy bins (figure 9), which constitute the input for U-Net-I.

Figure 10 (a, b) displays normalized MSE and SSIM for decomposed projections for RGN and U-Net-P. For soft tissue, U-Net-P presents a 29 % and 6 % decrease in normalized MSE on decomposed projections with respect to RGN for  $\alpha = 0.1$  and  $\alpha = 0.6$ , respectively. Normalized MSE for bone is larger than for soft tissue due to noise, as most part of the image corresponds to background. U-Net-P led to similar decrease in MSE for bone as for soft tissue. U-Net-P also led to increase in SSIM with respect to RGN for bone and soft tissue. For bone tissue, U-Net-P presents a 2.5- and 3-fold increase in SSIM on decomposed projections with respect to RGN for  $\alpha = 0.1$  and  $\alpha = 0.6$ , respectively.

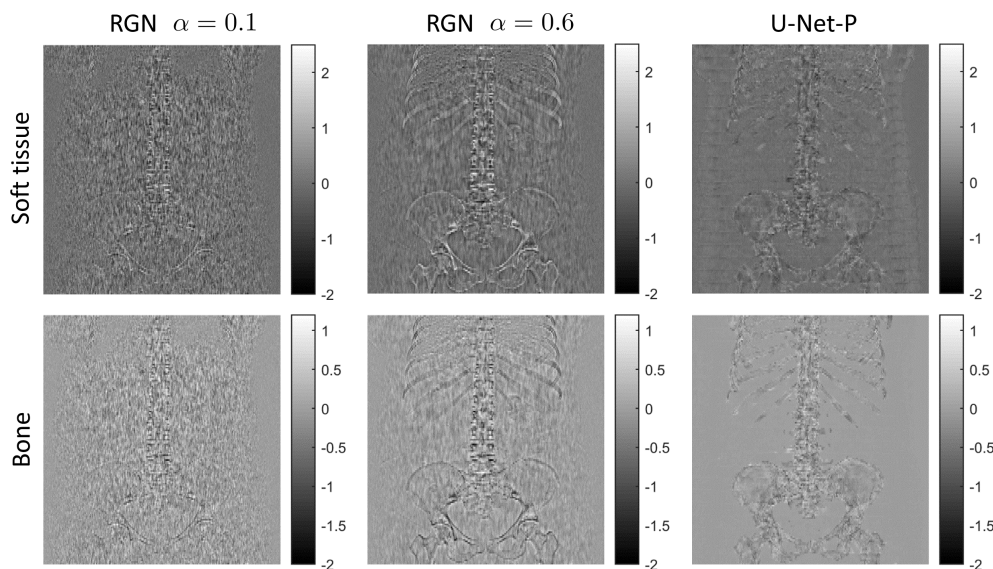
Figure 10(c, d) shows normalized MSE and SSIM for tomographic reconstructions for all methods. U-Net-P leads to better results than RGN, and U-Net-I leads to the best results overall, with up to 85 % and three-fold increase in SSIM with respect to RGN and U-Net-P, respectively.

Figure 10(e, f) show normalized bias for tomographic reconstructions for all methods. Among projection-based methods, RGN leads to lower bias





**FIGURE 3.** Phantom and decomposed projections (for  $0^\circ$  view) for RGN and U-Net-P for a synthetic phantom from the test set.



**FIGURE 4.** Error images of decomposed projections by RGN and U-Net-P for the same view as in figure 3.

for soft tissue but much higher bias for bone than U-Net-P. U-Net-I presents the lowest bias overall. For all methods, bias for soft tissue is smaller than for bone because it is computed over a larger region.

Figure 10(g) shows noise (SD) in soft tissue. Adopting RGN for  $\alpha = 0.6$  as reference, U-Net-P and U-Net-I lead to 27 % and 85 % decrease in noise, respectively.

## B. EXPERIMENTAL DATA

### 1) Experimental phantom data

Figure 11 shows tomographic reconstructions for the experimental phantom data. Methods lead to similar quantitative results, especially for soft tissue inserts. Decomposition of bone materials are slightly differ-

ent. U-Net-I leads to a clearer recovery and closer estimation for most inserts. In terms of image quality, U-Net-P presents less noisy images and slightly less ring artefacts than RGN. U-Net-I leads to high image quality with suppression of most ring artefacts. The 60 keV images provided by the two methods are very similar, with U-Net-P and U-Net-I presenting less noise.

Figure 12 shows quantification errors of the phantom inserts. Figures 12 (left and center) shows errors for all inserts for soft tissue and bone images. For soft tissue-like inserts, RGN leads to larger errors than deep learning methods, as it fails to provide zero densities for the bone image. For bone-like inserts, all methods



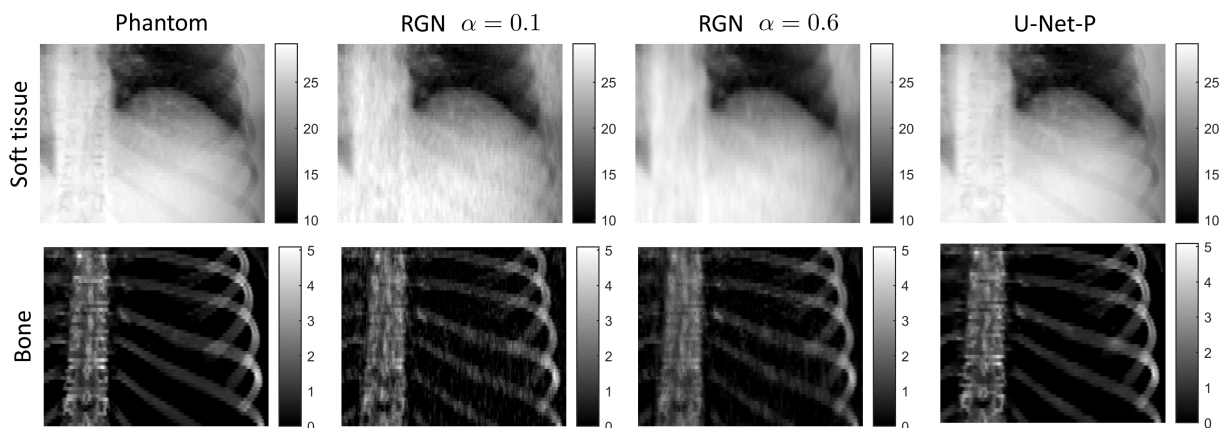


FIGURE 5. Image detail for phantom and decomposed projections for the images shown in figure 3.

tend to present a negative bias in the bone image (part of bone placed in the soft tissue image). Overall, U-Net-I leads to lowest quantification errors, as shown in figure 12 (right). Among the projection methods, U-Net-P provides lower median but larger variance (U-Net-P has almost zero error for soft tissue-like rods).

## 2) Human thorax data

Figure 13 shows tomographic reconstructions of the decomposed materials and the 60 keV image for RGN, U-Net-P and U-Net-I. Among the projection methods, RGN provides noisier decomposed images and appears more sensitive to ring artefacts than U-Net-P. U-Net-I provides higher image quality than projection-based methods, with better recovery of details for both soft tissue and bone images. Compared to the decomposed images, 60 keV images show highly reduced ring artefacts, with RGN presenting few artefacts, U-Net-P correcting for these artefacts, and U-Net-I providing the best image quality overall, with reduced noise and better recovery of texture for the soft tissue image.

## C. COMPUTATION TIME

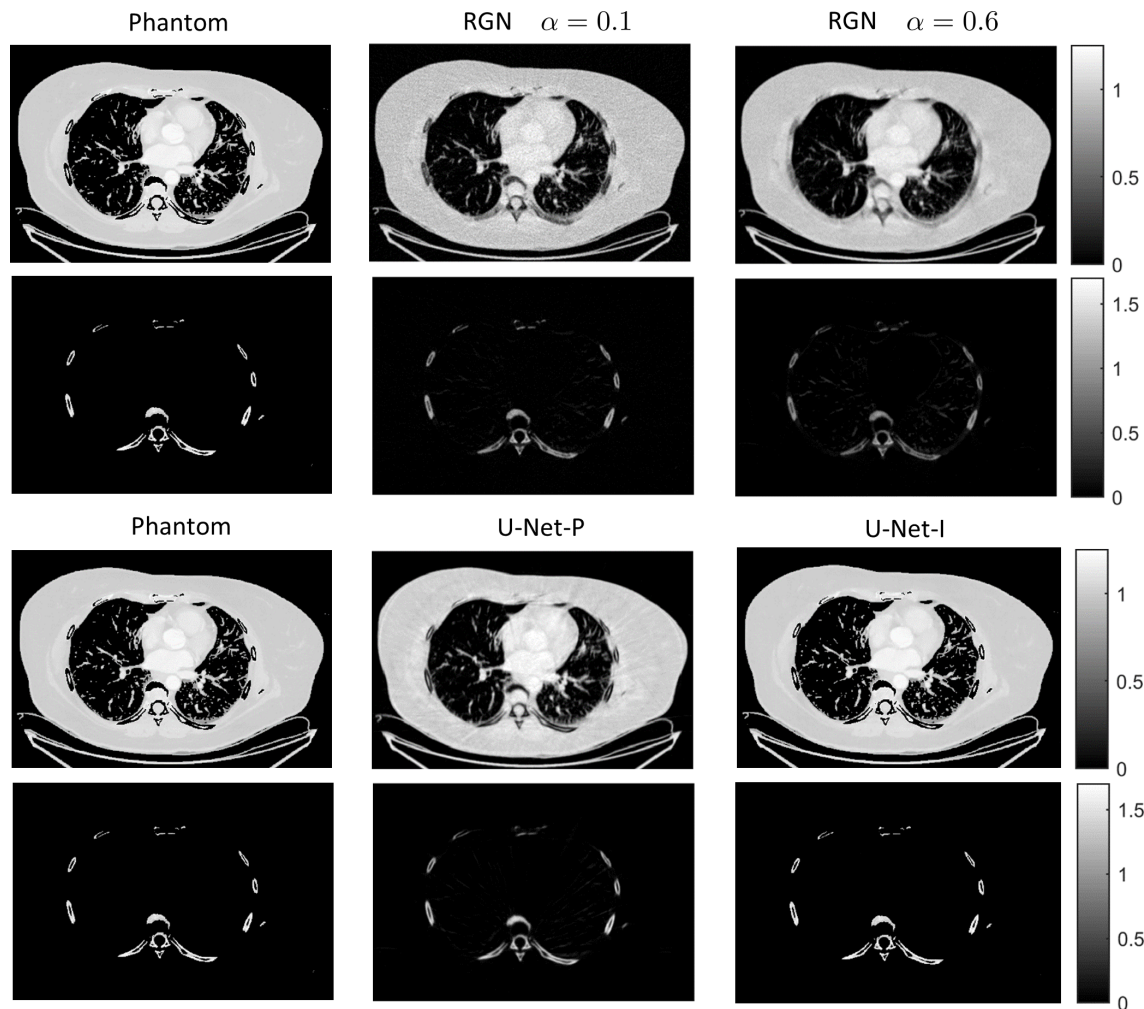
We run our code on a Windows computer with 64-bit operating system, Intel Xeon(R) E5-1650 v4 3.60 GHz CPU and 128 GB RAM. The U-Net is trained on a GeForce NVIDIA GTX 1080 Ti graphics card. U-Net-P requires 3.2 days for 1200 epochs and U-Net-I requires 33 hours for 600 epochs. Decomposition and tomographic reconstruction times for synthetic data and the human thorax data set are displayed in Table 1. Material decomposition with RGN is done on CPU by using straight-forward parallelization on 4 cores. For U-Net, we provide decomposition times on CPU and GPU. Tomographic reconstruction is done on CPU for synthetic data and on GPU with RTK for the human thorax data set. U-Net-I presents higher tomographic reconstruction times than projection based methods

because it requires reconstruction of five volumes (five energy bins) instead of two (two materials).

## V. DISCUSSION

We have proposed a deep learning method based on a Sim2Real approach and a U-Net architecture for solving the material decomposition problem in spectral CT. Given that medical imaging data and, specifically, spectral CT data are scarce, we have followed a Sim2Real approach by training on simulated human phantoms and assessing on experimental phantom data and human data. We compared projection- and image-based material decomposition by training the U-Net on either the projection domain (U-Net-P) or in the image domain (U-Net-I), and both approaches were compared to a RGN method in the projection domain. Among projection-based methods, we found that U-Net-P leads to improved image quality with respect to RGN, which presented a strong trade off between noise and regularization. Increasing the regularization parameter for RGN decreased noise but it led to loss of image details. On the contrary, for synthetic data, U-Net was able to remove noise while maintaining image quality. Differences in terms of image quality between U-Net-P and RGN were smaller for experimental data. In terms of quantification of decomposed materials, both methods led to similar results on the assessed experimental phantom data. However, U-Net-P was less affected by ring artefacts than RGN. Furthermore, U-Net led to a significant reduction in prediction time, specially for large data sets. U-Net-I presented a significantly superior improvement in image quality than projection based methods. For synthetic data, U-Net-I led to almost perfect material decomposition, and for experimental data, it removed noise and ring artefacts while recovering image details.

The superiority in terms of image quality of U-Net-P with respect to RGN must be discussed in detail. This can be explained by the fact that U-Net can learn



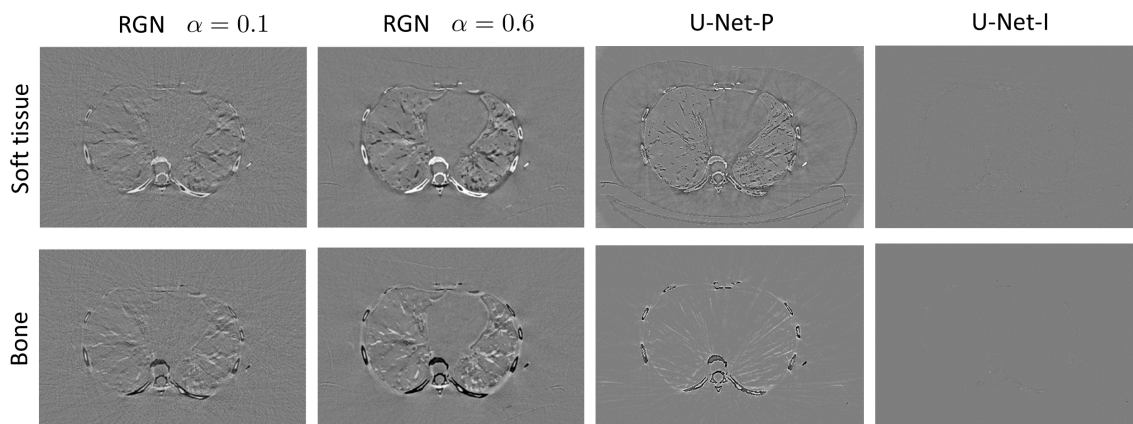
**FIGURE 6.** Tomographic reconstruction of a numerical human phantom for RGN, U-Net-P and U-Net-I. Image reconstruction corresponding to decomposed projections shown in figure 3.

**TABLE 1.** Material decomposition (Mat. Dec.) and tomographic reconstruction (Tomo. Rec.) times for synthetic data and for the human thorax data set. CPU, 4 cores: Parallelization using 4 cores. BS = Batch Size.

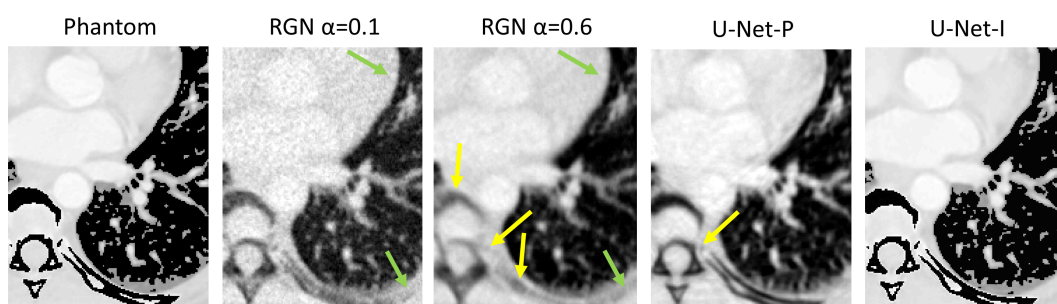
	Simulated data		Human thorax	
	Mat. Dec.	Tomo. Rec.	Mat. Dec.	Tomo. Rec.
RGN (CPU, 4 cores)	44 min	25 s	155 min	50 min (GPU)
U-Net-P (CPU)	70 s	""	25 min	""
U-Net-P (GPU)	6 s (BS = 16)	""	45 s (BS = 1024)	""
U-Net-I (GPU)	6.6 s (BS = 16)	63 s	45 s	125 min

implicitly the probability distribution of the decomposed materials. In fact, Bayesian deep learning interprets supervised learning as recovering the posterior distribution and it approximates the conditional mean when using the MSE loss [52]. This is particularly relevant for material decomposition in the projection domain, as in this case the choice of prior distributions is less clear. The RGN method included material specific regularization where regularization functionals for each material were selected as suggested in [22].

We used first- and second-order Tikhonov for bone and soft tissue, respectively. While this choice seems reasonable, it is not optimal. A second disadvantage of variational methods is the high dependence on the regularization parameter, which requires fine tuning. Here, we showed results for RGN for different values of the regularization parameter. For further insight into the selection of the regularization parameter for RGN, we refer to [22] and [26]. Although fine tuning can generally lead to an acceptable compromise between



**FIGURE 7.** Error images of tomographic reconstructions of a numerical human phantom (corresponds to figure 6).



**FIGURE 8.** Detail of tomographic reconstruction of soft tissue for the images shown in figure 6. Yellow arrow points where bone details are not well recovered. Green arrow points to the appearance of 'fake' details.



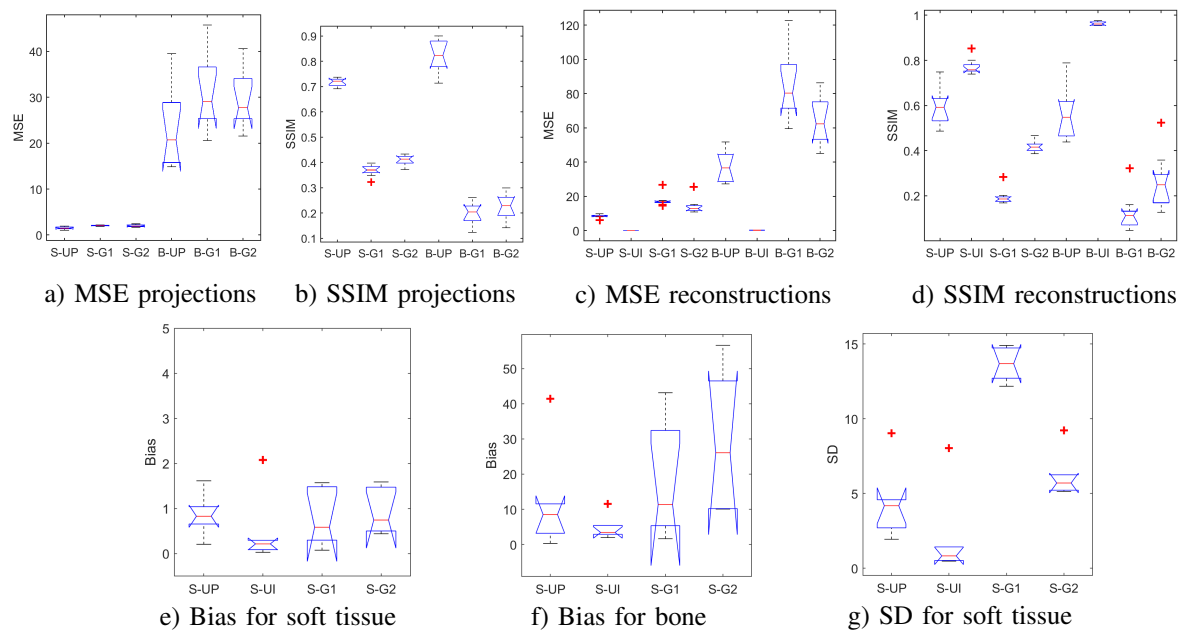
**FIGURE 9.** Tomographic reconstructed images for energy bins 1, 3 and 5. Images are displayed with the same colorbar (0, 0.53). Random crops of the five energy bins images are the input for U-Net-I. The output for these images are provided in figure 6.

noise and regularization for variational approaches, its benefits are mitigated by the fact that regularization functionals are not optimal.

The comparison between projection- and image-based methods is still an open question, particularly for deep learning approaches. In this work, we found that U-Net-I led to superior results than U-Net-P. Specifically, we found that U-Net-P led to high quality decomposition in the projection domain, as shown in the image detail in figure 5. However, this did not translate into an equivalent image quality after tomographic reconstruction. Tomographic reconstructed images suffered from some noisy structure or streak-like artefacts in the soft tissue image, a loss of small image details on bone parts and slightly blurred small details.

This can be due to several reasons. First, learning the probability distribution of the soft tissue and bone seems easier in the image domain than in the projection domain. In the image domain, distributions could be simplified to some given distributions centered around their mean values. In the projection domain, values depend on both material density and length. For a given value of a pixel in the projection domain, it is then not possible to distinguish between different densities or thickness. Using this reasoning, material decomposition taking into account other projections may improve results. Second, for imaged-based methods, tomographic reconstruction of the different energy bins provide images that are noisy but for which image details are preserved (figure 9). Thus, U-Net-I learns





**FIGURE 10.** Quantitative results on the numerical thorax test set. Boxplots for normalized MSE and SSIM of decomposed projections and tomographic reconstructed images, given by U-Net-P (UP), U-Net-I (UI), RGN for  $\alpha = 0.1$  (G1) and RGN for  $\alpha = 0.6$  (G2), for soft tissue (S) and bone (B). UI is provided only on reconstructions. Boxplots show the median, 25-th and 75-th percentiles, and minimum and maximum values excluding outliers, which are displayed with red crosses. When notches do not overlap, one can conclude, with 95% confidence, that the true medians do differ.

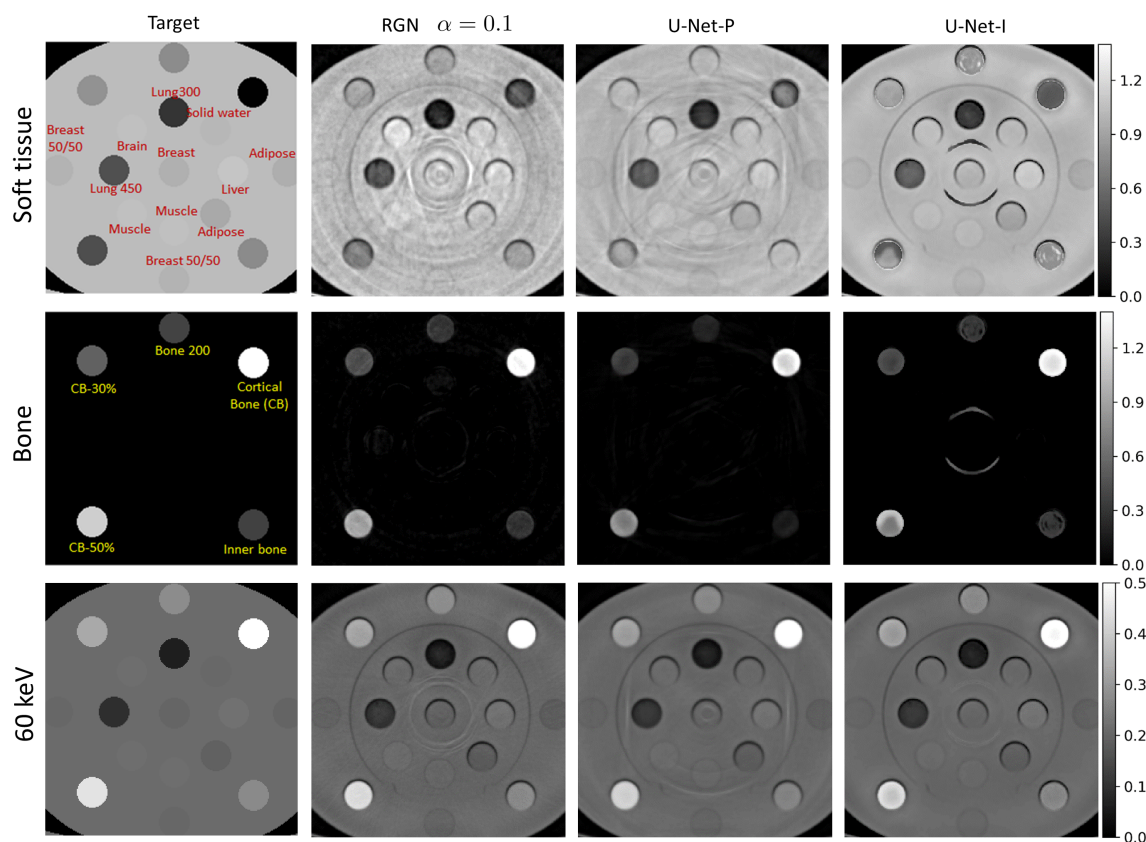
to simultaneously decompose materials and perform image restoration. Third, U-Net-I learns implicitly the prior distributions of the decomposed materials on the image domain while U-Net-P learns the prior distributions on the intermediate projection domain, on which small errors may translate in artefacts or noise in the image domain. Projection-based decomposition methods may thus require a further postprocessing step. In addition, we also found that training was easier in the image domain, requiring a lower number of epochs to start providing good results (results not shown).

For experimental data, projection-based algorithms were subject to ring and band artefacts. Interestingly, U-Net-P was more robust to the presence of artefacts than RGN. This may be because for U-Net-P we used normalized data while for RGN we used absolute data. Another explanation could be that U-Net-P learns the prior distribution of the decomposed materials, so it may penalize for these type of artefacts. In previous work, we also found this effect when decomposing simulated perturbed data [28]. More interesting, U-Net-I did not present ring artefacts on the experimental data.

Several deep learning approaches have been previously proposed for material decomposition. Most of them perform material decomposition in the image domain [9], [39]. Recently a multilayer perceptron was proposed for solving the material decomposition

problem in the projection domain [42]. In this work, we proposed a CNN approach to assess the potential of deep learning not only for solving the material decomposition problem but for implicit regularization. In addition, we have shown that a Sim2Real approach that learns on numerical human phantoms is feasible. This is particularly interesting for a CNN method, as it can implicitly learn the optimal regularization for human data. We remark that previous approaches have learned on experimental cylindrical-shape phantoms, which misses this feature of the CNN method.

The Sim2Real transfer approach belongs to the wider class of TL and domain adaptation approaches [45], [46], [59]. 'Transferability' has been shown to depend on the distance between source and target specific tasks [60]. In our case, the task is the same but domains may differ if the feature spaces or the marginal probability distributions between source and target are different. In the case of learning on numerical human phantoms and testing on human data, we do not expect large differences between source and target learned features and probability distributions, which may explain why we found positive results. In the case of testing on experimental phantoms, we found probability distributions to be different (results not shown). This could be expected as objects are different. For projection-based methods, we also remark that due to the fact that we are projecting mass densities, then the material decomposition problem in the projection



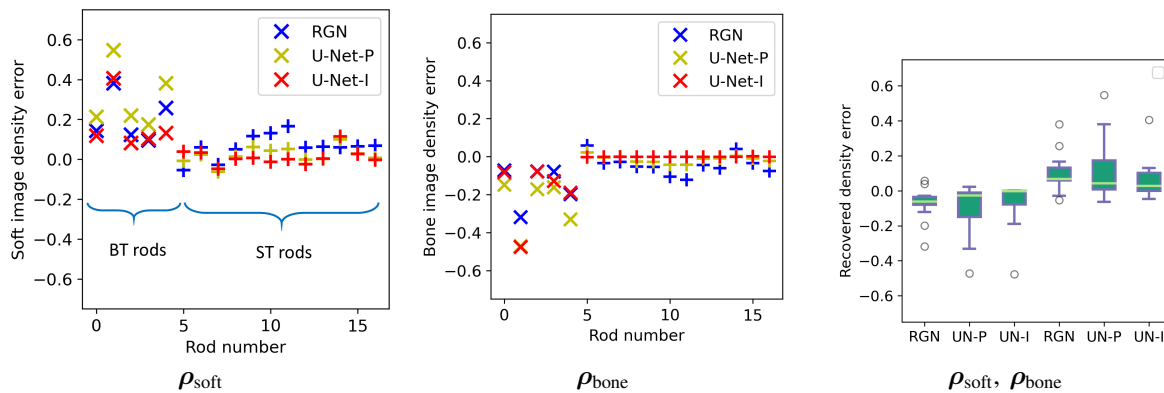
**FIGURE 11.** Experimental phantom with (Gammex and Cirs) inserts. Left: Estimated target images. Second to fourth columns: Tomographic reconstruction of soft tissue and bone and 60 keV image for RGN, U-Net-P and U-Net-I. We remark that data calibrations and corrections included in the scanner manufacturer pipeline have not been included in this work.

domain depends also on the object size. Although distributions were different, the range of values of the thorax data set comprised those of the experimental phantom, which may explain why it works. In order to achieve better generalization, we also tried further data augmentation by modifying sizes of the thorax phantoms. This led to similar results, with an increase in training time, but this techniques could lead to models with improved generalization. The features that are learned from a human phantom or from a phantom with inserts should be different, so including these type of phantoms in the training data may improve the performance on these type of experimental phantom data sets.

This work is subject to a few limitations. Results may depend on the learning model. Here we have used a U-Net architecture, which has led to outstanding results for diverse CT applications [31], [38]. However, for this problem a simpler architecture may be sufficient. The material decomposition has a pixel-wise nature, so it is possible that simpler ConvNets can learn the prior distributions of the materials without the need of a hierarchical-based architecture, which is more designed to interpret information across the entire

image. In order to assess this, we compared U-Net-P with two ConvNets without max-pooling operations, one with four convolutional layers, which corresponds to the main path or the first level of the U-Net, and a second one with the same number of convolutional layers as U-Net. We found that U-Net-P allows better removal of artefacts and provides improved image texture for soft tissue (results not shown). Besides the architecture, deep iterative methods, also called model-based learning methods, proposed for solving inverse problems could provide further benefits [33], [36], [61]. In particular, these iterative methods include a data consistency condition, which could mitigate the appearance of artefacts that can potentially lead to mislead diagnosis. Although U-Net leads to overall high image quality, deep iterative methods may be required to provide learning methods that are robust for the clinical use [62]. These methods can also reduce further the need of learning power, as well as the required amount of training data. Another interesting solution could be to consider Bayesian neural networks that also provide an uncertainty estimate [52]. With regard to the amount of training data, we found that using less than ten phantoms for training U-Net-





**FIGURE 12.** Quantification error of (Gammex and Cirs) inserts for RGN (blue) and U-Net-P (yellow) and U-Net-I (red) from decomposed soft tissue image  $\rho_{\text{soft}}$  (left) and decomposed bone image  $\rho_{\text{bone}}$  (center). Inserts are marked with the symbol + for soft tissue like materials (lung, breast, muscle, solid water, adipose tissue, brain, muscle) and with the symbol  $\times$  for bone like materials (cortical bone (CB), inner bone, CB 30%, CB 50%). Right: Boxplot of density errors where median and standard deviation are taken across all inserts for soft tissue and bone like inserts.

P led to lower image quality (results not shown); however, fewer data were not compensated for by more extensive data augmentation strategies such as translation and rotation. Further investigation could set the minimum amount of data for training this model. In addition, we have assumed that the energy response of the scanner is perfectly known. Although this has been provided by the manufacturer, some deviations from ideality conditions may occur. Further work could also fine tune a pretrained network using experimental phantom data as suggested in [28]. However, a previous work found only small improvements using a fully-connected network [42]. In this work, we have assessed the feasibility of the proposed method for material decomposition for two materials only. However, this methodology can be easily extended to three or more materials, including k-edge imaging, as shown on numerical data in [28].

In conclusion, deep learning methods show a great potential for spectral CT as they provide almost real time material decomposition and yield competitive results in comparison with current variational approaches.

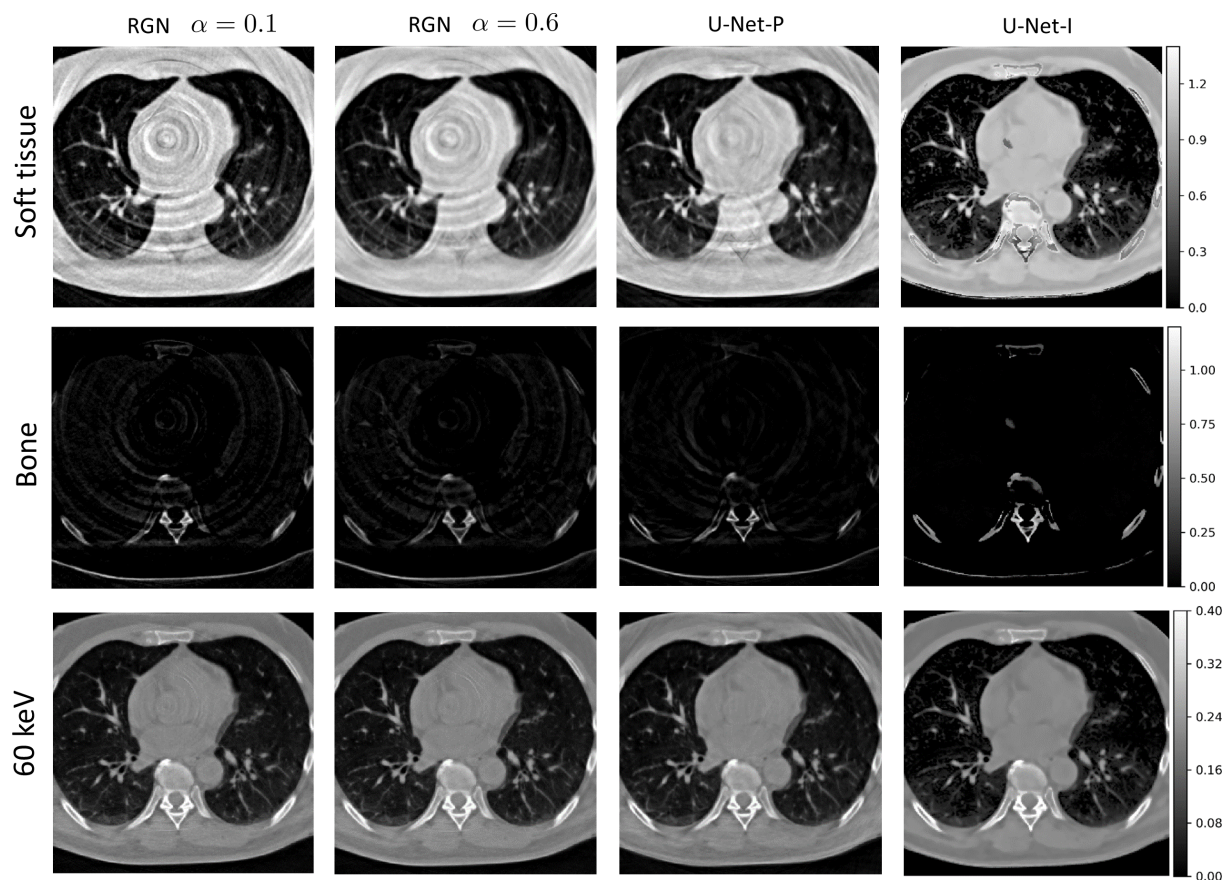
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**FIGURE 13.** Tomographic reconstruction of a human thorax for RGN, U-Net-P and U-Net-I.

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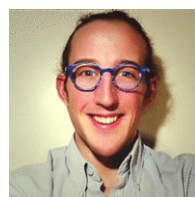
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