



## **Electric field control of interfacial Dzyaloshinskii-Moriya interaction in Pt/Co/AlO<sub>x</sub> thin films**

Marine Schott, Laurent Ranno, Hélène Béa, Claire Baraduc, Stéphane Auffret,  
Anne Bernand-Mantel

### **► To cite this version:**

Marine Schott, Laurent Ranno, Hélène Béa, Claire Baraduc, Stéphane Auffret, et al.. Electric field control of interfacial Dzyaloshinskii-Moriya interaction in Pt/Co/AlO<sub>x</sub> thin films. *Journal of Magnetism and Magnetic Materials*, 2021, 520, pp.167122. <10.1016/j.jmmm.2020.167122>. <hal-02944910>

**HAL Id: hal-02944910**

**<https://hal.science/hal-02944910v1>**

Submitted on 15 Dec 2022

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons CC BY-NC 4.0 - Attribution - Non-commercial use - International License

# Electric field control of interfacial Dzyaloshinskii-Moriya interaction in Pt/Co/AlO<sub>x</sub> thin films

Marine Schott and Laurent Ranno

*Univ. Grenoble Alpes, CNRS, Grenoble INP,  
Institut Néel, 38000 Grenoble, France*

Hélène Béa, Claire Baraduc, and Stéphane Auffret

*Univ. Grenoble Alpes, CEA, CNRS, Grenoble INP\*,  
IRIG-Spintec, 38000 Grenoble, France*

Anne Bernand-Mantel\*

*Université de Toulouse, Laboratoire de Physique et Chimie des Nano-Objets,  
UMR 5215 INSA, CNRS, UPS, 135 Avenue de Rangueil, F-31077 Toulouse Cedex 4, France*

## Abstract

We studied electric field modification of magnetic properties in a Pt/Co/AlO<sub>x</sub> trilayer via magneto-optical Kerr microscopy. We observed the spontaneous formation of labyrinthine magnetic domain structure due to thermally activated domain nucleation and propagation under zero applied magnetic field. A variation of the period of the labyrinthine structure under electric field is observed as well as saturation magnetization and magnetic anisotropy variations. Using an analytical formula of the stripe equilibrium width we estimate the variation of the interfacial Dzyaloshinskii-Moriya interaction under electric field as function of the exchange stiffness constant.

---

\*Electronic address: [bernandm@insa-toulouse.fr](mailto:bernandm@insa-toulouse.fr)

## I. INTRODUCTION

Electric-field (EF) control of magnetism in metals is currently an actively expanding field of study, motivated by potential applications in low power spintronics devices. The magnetization of metallic magnetic materials in spintronics devices can be manipulated using magnetic field or spin-polarized currents flow. The ability to control the magnetic properties of a system using a gate voltage is a promising technique which could lead to the development of EF-assisted magnetization switching devices. Since the first experimental demonstration of EF control of coercive field in a FePt thin film by Weisheit et al. [1], lots of studies have been conducted with the final intention of finding the best conditions for functional devices. Significant variations in the magnetic anisotropy energy under EF application have been observed by many groups [2–7], as well as EF variation of  $T_c$  in ultrathin films [8–10]. Recently, the EF impact on the exchange stiffness parameter  $A_{\text{ex}}$  has been addressed experimentally [11, 12] and theoretically [13]. In these systems, a dielectric oxide layer is present at the top surface of the ferromagnet to allow the application of an EF in a capacitor geometry. This induces a broken spatial inversion symmetry for the ferromagnetic thin film. The presence of these non-identical interfaces is the source of an antisymmetric type of exchange, the Dzyaloshinskii-Moriya interaction (DMI), which has been shown to be a source of chiral spin textures in Pt/Co/ $\text{AlO}_x$  for instance [14]. DMI has been recently shown to be tuneable using strain [15], or using the current flowing in the heavy metal [16, 17]. The interfacial origin of this DMI and its consequences in spin textures in ultrathin films make also DMI an interesting EF tunable parameter. However, distinguishing EF modulation on DMI from other contributions is not straightforward as direct access to DMI is difficult. In addition to theoretical predictions for ultra-thin samples [18], several experimental studies have reported a change in the DMI factor under EF application [18–23]. This control was shown for relatively thick layers of Fe (20 nm) [19, 23], or a material presenting a weak DMI, Ta/FeCoB/ $\text{TaO}_x$ , as demonstrated by Srivastava et al. [20]. More recently, Zhang et al. [22] and Koyama et al. [21] showed larger EF induced variation of DMI in Pt/Fe/MgO and Pt/Co/Pd/MgO systems presenting intermediate DMI values.

In this work, we analyzed labyrinthine domains (also referred to as stripe domains) in samples of Pt/Co/ $\text{AlO}_x$  presenting large DMI values [14, 24]. A reversible evolution of the

labyrinthine magnetic domain configurations under EF is observed. We also report an EF variation of the saturation magnetization and anisotropy field. The analysis of the variation of equilibrium stripe width allowed us to estimate the EF variation of the DMI term  $D$ . We stress here that this estimation strongly depends on the assumptions made on the exchange constant value.

## II. SYSTEM DESCRIPTION AND CHARACTERIZATION

Our system is a Pt(3 nm)/Co(0.6 nm)/AlO<sub>x</sub> sputtered trilayer, presenting a gradient of oxidation at the Co/AlO<sub>x</sub> interface. This was induced by the post-oxidation of a wedged-shaped Al top layer (Fig. 1(a)). Using this technique, we get access to a low thicknesses range for Co due to the Co partial oxidation in the region where the deposited Al is thin. The sample has been covered by about 50 nm of a high- $k$  insulator, HfO<sub>2</sub>, deposited using atomic layer deposition. Then an Indium Tin Oxide (ITO) layer was DC sputtered and patterned in electrodes. These transparent electrodes allow to obtain magneto-optical Kerr effect (MOKE) images of the magnetic domains in the Co layer under a gate voltage (Fig. 1(d)). Voltages of different magnitudes were applied between this top electrode and the Co layer. Here a positive voltage application induces electrons accumulation at the surface of the Co layer (Fig. 1(a)). We used MOKE in polar geometry and recorded images and magnetic hysteresis loops on a single position on the sample through the ITO electrode under different applied voltages (Fig. 1(d)). To determine the EF variation of the saturation magnetization  $M_s$ , we measured the variation of the p-MOKE signal between the two opposite saturated states, for out-of-plane applied magnetic field. The average value of magnetization of the wedged sample has been obtained by measuring  $M_s$  with a Vibrating Sample Magnetometer-Superconducting Quantum Interference Device (VSM-SQUID). A  $T_c$  of 366 K was estimated from VSM-SQUID measurements on the sample under study which possesses an averaged Co thickness of 0.49 nm due to partial oxidation of the deposited Co (see Fig. 1(a)).

A strong EF dependence of  $M_s$  is shown in Fig. 1(e). Such sensitivity of the saturation magnetization is due to the proximity of the  $T_c$  to the measurement temperature (room temperature). Similar EF control of  $T_c$  associated with strong  $M_s$  variations were observed

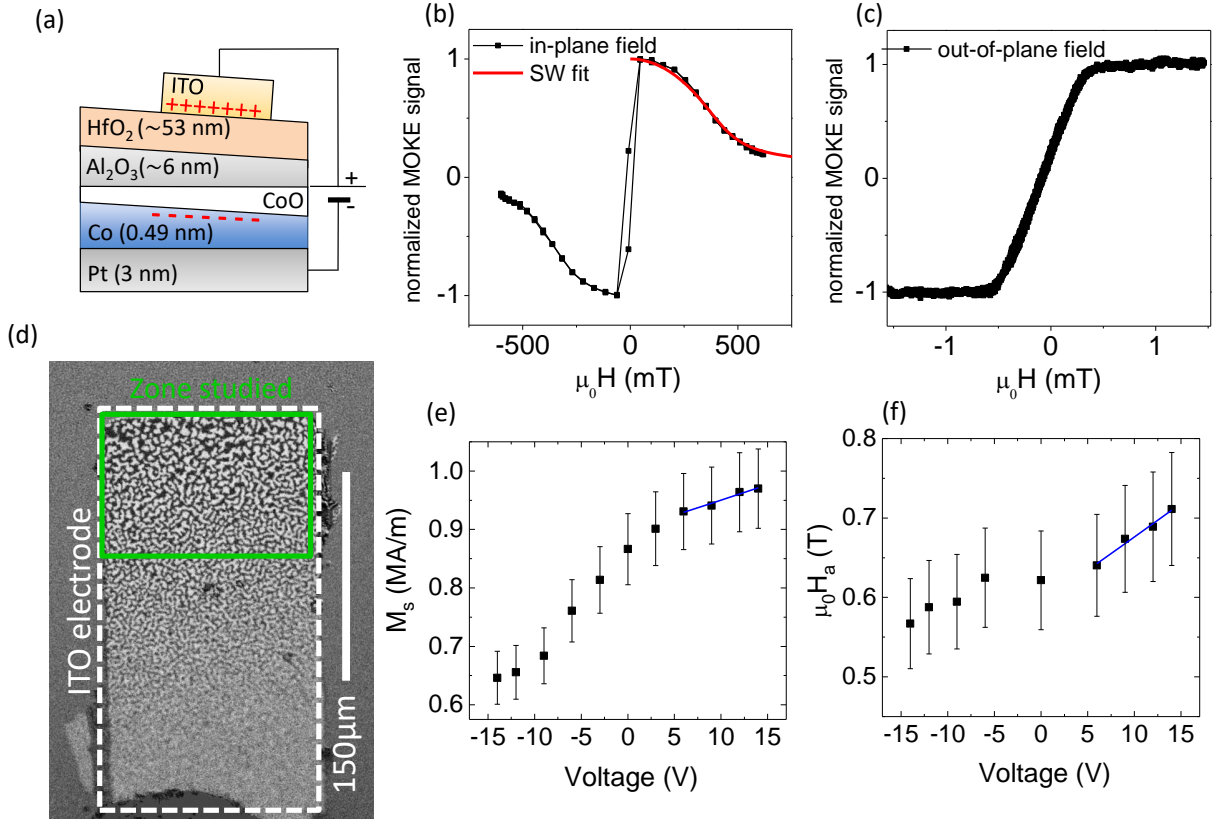


FIG. 1: (a) Schematics of the wedge sample and of the set-up used for EF application: the Pt/Co/AlO<sub>x</sub> trilayer is covered by a  $\sim 50$  nm of dielectric layer (HfO<sub>2</sub>) and a transparent top electrode (ITO). (b) p-MOKE hard axis (in-plane field) hysteresis loop (black squares) and Stoner-Wohlfarth fit (red line). (c) p-MOKE easy axis (out-of-plane field) hysteresis loop (black squares). (d) p-MOKE image of the demagnetized state taken at 0 T, after saturation with an out-of-plane field of 0.4 mT for +12 V applied gate voltage. (e) Evolution of saturation magnetization with gate voltage. A systematic error of 7%, was estimated from the error on the VSM-SQUID measurement. (f) Evolution of anisotropy field with voltage measured from p-MOKE hysteresis loops with in-plane field. A systematic error of 10%, was estimated from fluctuations in the field calibration of the p-MOKE measurement with in-plane applied magnetic field. The blue solid lines in c and d show the regions where the EF-efficiencies have been extracted.

in recent studies [11, 25]. The EF variation of the anisotropy field  $\mu_0 H_a$  is presented in Fig. 1(f). The anisotropy field  $\mu_0 H_a$  is extracted using Stoner-Wohlfarth fit of the magnetization rotation toward the hard axis direction, on p-MOKE hysteresis loops, for in-plane applied magnetic field (see Fig. 1(b)). From the measurements of  $\mu_0 H_a(V)$ , we deduced the variations of the effective magnetic anisotropy energy from the formula  $\mu_0 H_a = 2K_{eff}/M_s$ , where  $K_{eff} = K_s/t - \frac{1}{2}\mu_0 M_s^2$  is the effective magnetic anisotropy and  $K_s$  is the surface magneto crystalline anisotropy. A voltage controlled magnetic anisotropy (VCMA) coefficient [26]  $\beta_{PMA} = \Delta K_s/\Delta E = 562 \pm 102 \text{ fJ}/(\text{V}\cdot\text{m})$  is obtained. This is larger compared to the usual range obtained for a charge accumulation effect (10-290 fJ/(V·m)) [3, 6, 27, 28]. The enhanced effect is again likely due to the proximity of  $T_c$  to the measurement temperature.

### III. EF VARIATION OF EQUILIBRIUM LABYRINTHINE DOMAINS

As discussed earlier, the analysis of the equilibrium domain configuration has been shown to be one of the ways to study the influence of the EF on different magnetic properties [11, 12]. At zero and negative gate voltages, the domains are blurry due to a very strong thermally induced domain wall motion, as observed in previous works [29]. Thus, in the following we focus our study on positive gate voltages, for which the labyrinthine domains are stable, between 6 V and 14 V. To record the images of labyrinthine states and their variation with the EF, we proceed as follow: under a constant EF, we first saturate the sample with an applied magnetic field, then we turn off the magnetic field and record an image after a waiting time of a few seconds. The images presented in Fig. 2(a)-(d) correspond to the labyrinthine domains which spontaneously appear due to thermally activated nucleation and domain wall propagation. The labyrinthine domains are clearly and reversibly influenced by the application of an EF, similarly to what we observed in our previous experiments [30]. The characteristic labyrinthine domain width  $L_{eq}$  is estimated using a 2D Fourier transform of the images in Fig. 2(a)-(d). In Fig. 2(e) we present  $L_{eq}$  as function of the applied voltage, which shows an increase as a positive voltage is applied to the top ITO electrode. To understand in which way the EF is influencing the domain periodicity, we used an analytical model to describe the domain width  $L_{eq}$  in ultrathin films:

$$L_{eq} = C \cdot t \cdot \exp\left(\frac{\pi\sigma_\omega}{2K_d t}\right), \quad (1)$$

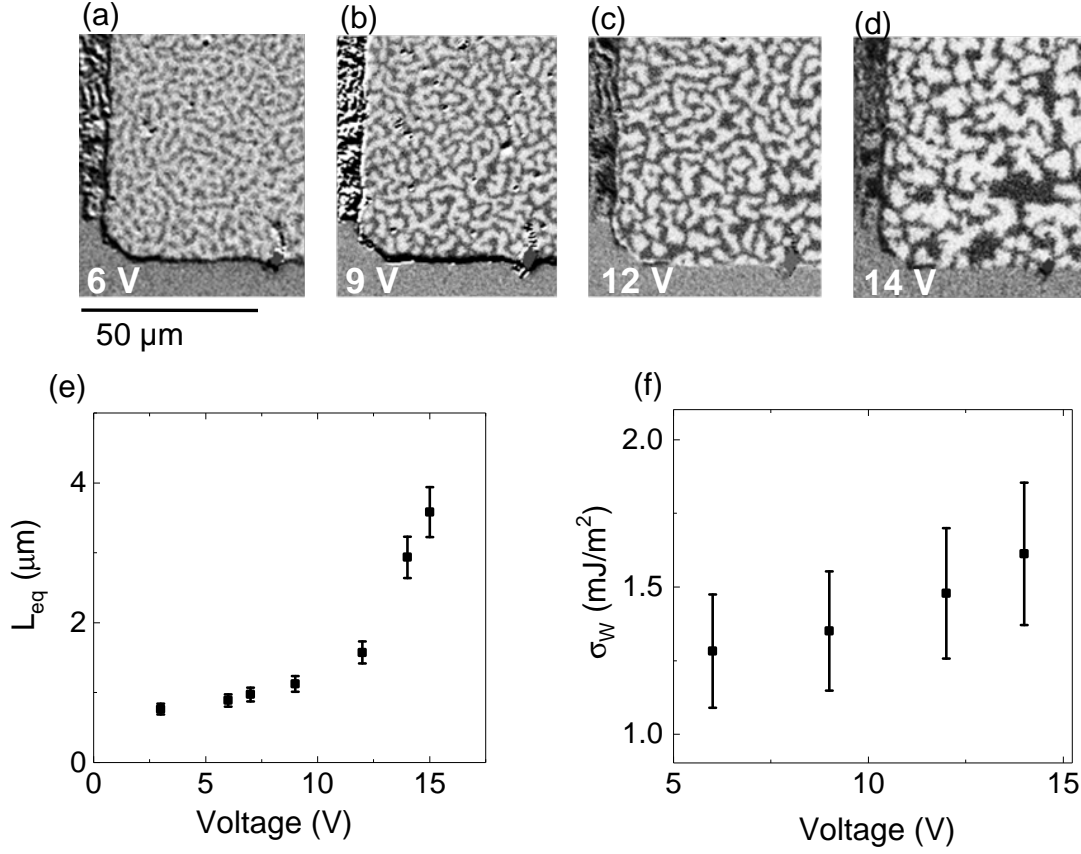


FIG. 2: (a)-(d) p-MOKE images of the evolution of equilibrium stripe width  $L_{eq}$  with gate voltage. (e) Equilibrium stripe width  $L_{eq}$  as a function of gate voltage. We estimated from repeated measurements a  $\sim 10\%$  error on  $L_{eq}$  due to imperfect demagnetization. (f) Deduced domain wall energy as function of gate voltage. The error bars correspond to a 16% error calculated from the propagation of the errors in  $M_s$ ,  $t$  and  $L_{eq}$ .

where  $t$  is the cobalt thickness (which is fixed here to 0.49 nm),  $K_d$  the dipolar constant  $K_d = \frac{1}{2}\mu_0 M_s^2$  and  $C$  is a model-dependent constant [31, 32] of order unity. The experimental domain wall energy  $\sigma_w$  in Fig. 2(f) is deduced using the measured  $L_{eq}$  and  $M_s$  values. We find domain wall energies  $\sigma_w$  around 1.3 – 1.6  $\text{mJ/m}^2$  for the range of voltages under study, which is consistent with earlier studies [30].

#### IV. EF VARIATION OF DMI

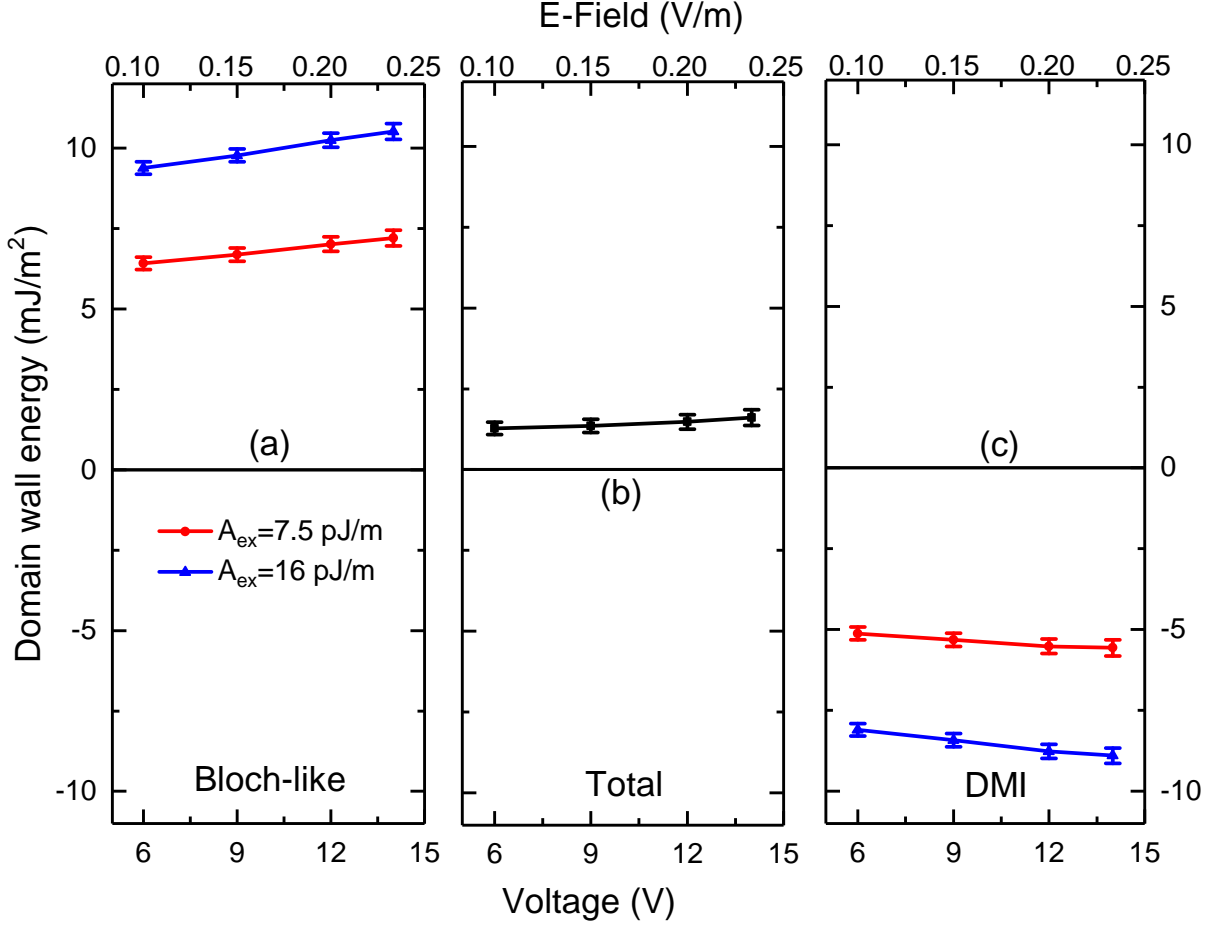


FIG. 3: Different components of the wall energy  $\sigma_w$  as a function of applied EF : (a) Bloch wall energy  $\sigma_w^{Bloch}$ . (b) Total energy  $\sigma_w$ . (c) DMI contribution  $\sigma_w^{DMI}$ .

In the presence of sufficiently strong DMI, the domain wall is of Néel type with a sense of rotation which lowers the domain wall energy [33]:  $\sigma_w = \sigma_w^{Bloch} + \sigma_w^{DMI} = 4\sqrt{A_{ex}K_{eff}} - \pi D$ , where  $D = D_s/t$  stands for the bulk DMI constant and is expressed in J/m², while the surface DMI value  $D_s$  is expressed in J/m. We see that in order to extract  $D$  using the measured  $\sigma_w$  and  $K_{eff}$  values it is necessary to know the exchange constant  $A_{ex}$ . We have used two values for  $A_{ex}$ . The first value  $A_{ex} = 7.5$  pJ/m (for  $V = 0$  V) was deduced from a fit using Kuzmin formula [34] of the temperature dependence of  $M_s$  in our sample measured by VSM-SQUID. This reduced value is coherent with recent studies [35]. The second value



$A_{ex}=16$  pJ/m (for  $V=0$  V) is a value corresponding to bulk thin Co films [36]. The fact that the value of  $A_{ex}$  extracted from our VSM-SQUID measurements is lower than the bulk Co value is linked to the low  $T_c$  of our sample (366 K) and coherent with the low  $M_s$  value. For the same reason we can expect  $A_{ex}$  to be influenced by EF as it was already suggested by previous studies [11–13, 37, 38]. We present the different deduced energy terms and their EF variation in Fig. 3. The total domain wall energy  $\sigma_w$ , also shown in Fig. 2(f) is presented in Fig. 3(b). In Fig. 3(a) we present two values and variations of the Bloch wall energy  $\sigma_w^{Bloch} = 4\sqrt{A_{ex}K_{eff}}$  deduced from the measured  $H_a$  and  $M_s$  and the two values of  $A_{ex}$  discussed earlier.  $A_{ex}$  is considered to vary with EF as  $\Delta A_{ex}/A_{ex} = 2\Delta M_s/M_s$ , as the general tendency described by mean field approximation is that  $A_{ex} \propto M_s^2$  near  $T_c$  [39]. Other theoretical studies have found a scaling law of  $A_{ex} \propto M_s^{2-\epsilon}$ , with  $\epsilon$  being close to 0.2 for low temperatures [40–42]. Fixing  $\Delta A_{ex}/A_{ex} = 2\Delta M_s/M_s$  is then a good approximation and will give us an upper limit for the variation we can expect for  $D(V)$ . From these assumptions we deduce the DMI value and EF variations which are presented in Fig. 3. The  $D$  value at 6 V is ranging between 1.3-2.4 mJ/m<sup>2</sup> depending on the chosen  $A_{ex}$  value. We see that EF variation of  $\sigma_w^{Bloch}$  (Fig. 3(a)) is stronger than the variation of the total wall energy  $\sigma_w$  (Fig. 3(b)) and that an EF variation of  $D$  is necessary to compensate this variation (Fig. 3(c)).

To discuss the DMI variations under EF, we use the voltage-control DMI (VCDMI) coefficient [18, 20]), defined as  $\beta_{DMI} = \Delta D/\Delta E$  (in J/(V·m), with  $\Delta E = \Delta V/t_{Ox}$ , where  $\Delta V$  is the voltage variation and  $t_{Ox}$  the dielectric thickness. The coefficient  $\beta_{DMI}$  is plotted versus  $A_{ex}$  in Fig. 4. It is in the range of  $\beta_{DMI} = 1100 - 2000 \pm 700$  fJ/(V·m). In order to compare this result with previous works we give a summary of the different values in Table 1. Very spread  $\beta_{DMI}$  values between 3.2 and 2000 fJ/(V·m) are obtained. However, these values are not directly comparable, as in addition to different materials and material quality, different thickness ranges of the ferromagnetic layer and different dielectric oxide layers have been used. To obtain comparable values of the (VCDMI) coefficient, we define a new normalized coefficient  $\eta_{DMI}$ , which we introduce as the variation of surface DMI constant  $D_s$  per surface charge provided at the interface of the ferromagnet:  $\eta_{DMI} = \Delta D_s/(\epsilon_e \Delta E)$ , where  $\epsilon_e$  is the effective permittivity equal to  $\epsilon_e = \epsilon_0 \epsilon_r$  in the case of a single dielectric layer, where  $\epsilon_0$  is the permittivity of vacuum and  $\epsilon_r$  the relative permittivity of the dielectric. This new normalized  $\eta_{DMI}$  coefficient takes into account the fact that the DMI is of interfacial

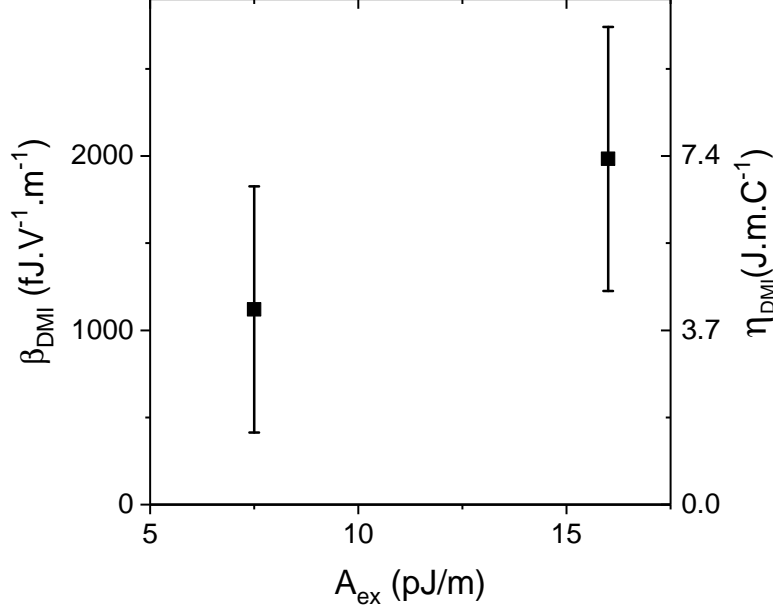


FIG. 4:  $\beta_{DMI}$  coefficients deduced from the experimental  $M_s$ ,  $t$ ,  $L_{eq}$  and  $K_{eff}$  values as a function of the chosen  $A_{ex}$  value. The error bars are calculated from the standard error on the slope on a linear fit of  $D(V)$ .

origin, and consequently it is the variation of surface DMI constant  $D_s$  which should be compared. In addition, as high-k oxides have been used in order to allow smaller EF for a similar effect on DMI we also have to take into account the effective permittivity of the (possibly multilayered) oxide and compare the effect for a given induced surface charge density and not a given electric field (assuming that the EF effect is induced by electron displacement). After performing this renormalization of the EF changes on DMI, we can now compare the  $\eta_{DMI}$  values corresponding to different studies from several teams. The obtained values lie within the range  $0.6$  to  $14.5 \times 10^{-12}$  J.m/C. We first see that the two studies with long time scale measurements (made by Brillouin light Spectroscopy (BLS) [20, 22]) provide much larger  $\eta_{DMI}$ . This is potentially due to the ion migration contribution from these long measurements. Long (days or hours) and short time (seconds or minutes) measurements present a factor of 5 ratio in  $\eta_{DMI}$  [20]. Our present result obtained within minute-timescale in ultrathin Co gives intermediate  $\eta_{DMI}$ . For the case of the theoretical paper by Yang et al., we have reported two values for the  $\eta_{DMI}$ , considering or not that

seed nm	FM nm	MOx nm	$\Delta D$ mJ/m <sup>2</sup>	$\Delta E$ MV/m	$\beta_{DMI}$ fJ/(V·m)	$\eta_{DMI}$ 10 <sup>-12</sup> J·m/C	ref
Pt 3	Co 0.49	AlO <sub>x</sub> /HfO <sub>x</sub> 6-53	0.14-0.26 ±0.2	133	1100-2000 ±700	3.9-7.2	here
Ta 3	FeCoB 0.65	TaO <sub>x</sub> /AlO <sub>x</sub> /HfO <sub>x</sub> 1-10-50	0.1	167	600	3.2	[20]*
Ta 3	FeCoB 0.65	TaO <sub>x</sub> /AlO <sub>x</sub> /HfO <sub>x</sub> 1-10-50	0.105	667	158	0.61	[20]
Au 50	Fe 20	MgO/SiO <sub>2</sub> 10-270	$4 \times 10^{-5}$	12.5	3.2	1.72	[19]
Pt 4	Fe 2	MgO 367	0.06	800	75	2.65	[22]*
Ta/Pt 2.6-2.4	Co/Pd 0.78-0.4	MgO/HfO <sub>x</sub> 2-50	0.038	577	67	0.38	[21]
V/Fe 20-20	Co 0.14	MgO/SiO <sub>2</sub> 5-50	$1.8 \times 10^{-3}$	18	100	5.5	[23]
V/Fe 20-20	Co 0.26	MgO/SiO <sub>2</sub> 5-50	$1.2 \times 10^{-3}$	18	65	14.5	[43]
Pt	Co 0.6	MgO			26	0.6-1.76	[18]

TABLE I: Summary of DMI variations under EF. The long time scale studies (hours or days) have a star \* in the last column.

the EF calculated corresponds to an applied EF or takes into account the effect of  $\epsilon_r$  in the oxide, which is still debated in the community, in particular due to the underestimation of the dielectric permittivity of MgO. These two values are thus giving ranges for theoretical  $\eta_{DMI}$  in the Pt/Co/MgO system. The relatively small dispersion in the extracted  $\eta_{DMI}$  values is noticeable, as all these studies have been performed in different teams with samples with different ferromagnetic materials, seed layers and oxides, grown with different techniques (magnetron sputtering or molecular beam epitaxy), measured with different methods (BLS, DW asymmetric motion under in-plane magnetic field, analysis of the labyrinthine domain

structures, excitation of magneto-static surface spin-waves) with EF ranging from 18 to 800 MV/m. This indicates that the underlying physics is similar for all these samples despite the very different  $\beta_{DMI}$  proposed. In order to carefully compare interface effect and optimize the EF effect on DMI, one should thus perform calculation of this renormalized, thickness and oxide-independent  $\eta_{DMI}$ .

## Conclusion

In conclusion, we were able to deduce a strong EF variation of the magnetic anisotropy energy ( $\beta_{PMA} = 562 \pm 102$  fJ/(V·m)) and of the *DMI* term ( $\beta_{DMI} \sim 1100 - 2000 \pm 700$  fJ/(V·m)). The observed variation of domain size  $L_{eq}$  is a result of the combination of variations of every magnetic parameter. The strong  $\beta$  coefficients we were able to deduce for PMA and DMI energies are the result of significantly increased EF effects for measurement temperatures close to  $T_c$ .

## Acknowledgements

The authors thank M. Chshiev and A. Thiaville for fruitful discussions and C. Mahony for his contribution to the editing of the manuscript. This work was supported by the French ANR via Contract No. ELECSPIN ANR-16-CE24-0018), the DARPA TEE program through Grant MIPR No. HR0011831554 and the EUR Grant NanoX No. ANR-17-EURE-0009 in the framework of the Programme des Investissements d’Avenir.

- 
- [1] M. Weisheit, S. Fähler, A. Marty, Y. Souche, C. Poinsignon, D. Givord, Electric field-induced modification of magnetism in thin-film ferromagnets, *Science* 315 (2007) 349–351. doi:10.1126/science.1136629.
  - [2] T. Maruyama, Y. Shiota, T. Nozaki, K. Ohta, N. Toda, N. Mizuguchi, A. A. Tulapurkar, T. Shinjo, M. Shiraishi, S. Mizukami, Y. Ando, Y. Suzuki, Large voltage-induced magnetic anisotropy change in a few atomic layers of iron, *Nature Nanotechnology* 4 (2009) 158.
  - [3] W.-G. Wang, M. Li, S. Hageman, C. L. Chien, Electric-field-assisted switching in magnetic tunnel junctions, *Nature Materials* 11 (2012) 64.

- [4] M. K. Niranjana, C.-G. Duan, S. S. Jaswal, E. Y. Tsybal, Electric field effect on magnetization at the Fe/MgO(001) interface, *Applied Physics Letters* 96 (2010) 222504. doi:10.1063/1.3443658.
- [5] K. Nakamura, R. Shimabukuro, Y. Fujiwara, T. Akiyama, T. Ito, A. J. Freeman, Giant Modification of the Magnetocrystalline Anisotropy in Transition-Metal Monolayers by an External Electric Field, *Physical Review Letters* 102 (2009) 187201. doi:10.1103/PhysRevLett.102.187201.
- [6] M. Endo, S. Kanai, S. Ikeda, F. Matsukura, H. Ohno, Electric-field effects on thickness dependent magnetic anisotropy of sputtered MgO/CoFeB/Ta structures, *Applied Physics Letters* 96 (2010) 212503. doi:10.1063/1.3429592.
- [7] K. Yamada, H. Kakizakai, K. Shimamura, M. Kawaguchi, S. Fukami, N. Ishiwata, D. Chiba, T. Ono, Electric Field Modulation of Magnetic Anisotropy in MgO/Co/Pt Structure, *Applied Physics Express* 6 (2013) 073004.
- [8] H. Ohno, D. Chiba, F. Matsukura, T. Omiya, E. Abe, T. Dietl, Y. Ohno, K. Ohtani, Electric-field control of ferromagnetism, *Nature* 408 (2000) 944–946. doi:10.1038/35050040.
- [9] D. Chiba, S. Fukami, K. Shimamura, N. Ishiwata, K. Kobayashi, T. Ono, Electrical control of the ferromagnetic phase transition in cobalt at room temperature, *Nature Materials* 10 (2011) 853.
- [10] K. Shimamura, D. Chiba, S. Ono, S. Fukami, N. Ishiwata, M. Kawaguchi, K. Kobayashi, T. Ono, Electrical control of Curie temperature in cobalt using an ionic liquid film, *Applied Physics Letters* 100 (2012) 122402. doi:10.1063/1.3695160.
- [11] F. Ando, H. Kakizakai, T. Koyama, K. Yamada, M. Kawaguchi, S. Kim, K. J. Kim, T. Moriyama, D. Chiba, T. Ono, Modulation of the magnetic domain size induced by an electric field, *Applied Physics Letters* 109 (2016) 22401. doi:10.1063/1.4955265.
- [12] T. Dohi, S. Kanai, A. Okada, F. Matsukura, H. Ohno, Effect of electric-field modulation of magnetic parameters on domain structure in mgo/cofeb, *AIP Advances* 6 (2016) 075017. doi:10.1063/1.4959905.
- [13] M. Oba, K. Nakamura, T. Akiyama, T. Ito, M. Weinert, A. J. Freeman, Electric-Field-Induced Modification of the Magnon Energy, Exchange Interaction, and Curie Temperature of Transition-Metal Thin Films, *Physical Review Letters* 114 (2015) 107202. doi:10.1103/PhysRevLett.114.107202.

- [14] M. Belmeguenai, J.-P. Adam, Y. Roussigné, S. Eimer, T. Devolder, J.-V. Kim, S. M. Cherif, A. Stashkevich, A. Thiaville, Interfacial dzyaloshinskii-moriya interaction in perpendicularly magnetized ultrathin films measured by brillouin light spectroscopy, *Physical Review B* 91 (2015) 180405. doi:10.1103/PhysRevB.91.180405.
- [15] N. S. Gusev, A. V. Sadovnikov, S. A. Nikitov, M. V. Sapozhnikov, O. G. Udalov, Manipulation of dzyaloshinskii-moriya interaction in co/pt multilayers with strain, 2020. *arXiv:2002.05042*.
- [16] G. V. Karnad, F. Freimuth, E. Martinez, R. Lo Conte, G. Gubbiotti, T. Schulz, S. Senz, B. Ocker, Y. Mokrousov, M. Kläui, Modification of dzyaloshinskii-moriya interaction-stabilized domain wall chirality by driving currents, *Phys. Rev. Lett.* 121 (2018) 147203. URL: <https://link.aps.org/doi/10.1103/PhysRevLett.121.147203>. doi:10.1103/PhysRevLett.121.147203.
- [17] N. Kato, M. Kawaguchi, Y.-C. Lau, T. Kikuchi, Y. Nakatani, M. Hayashi, Current-induced modulation of the interfacial dzyaloshinskii-moriya interaction, *Phys. Rev. Lett.* 122 (2019) 257205. URL: <https://link.aps.org/doi/10.1103/PhysRevLett.122.257205>. doi:10.1103/PhysRevLett.122.257205.
- [18] H. Yang, O. Boulle, V. Cros, A. Fert, M. Chshiev, Controlling Dzyaloshinskii-Moriya Interaction via Chirality Dependent Atomic-Layer Stacking, Insulator Capping and Electric Field, *Scientific Reports* 8 (2018) 12356. doi:10.1038/s41598-018-30063-y.
- [19] K. Nawaoka, S. Miwa, Y. Shiota, N. Mizuochi, Y. Suzuki, Voltage induction of interfacial DzyaloshinskiiMoriya interaction in Au/Fe/MgO artificial multilayer, *Applied Physics Express* 8 (2015) 063004. doi:10.7567/apex.8.063004.
- [20] T. Srivastava, M. Schott, R. Juge, V. Kizáková, M. Belmeguenai, Y. Roussigné, A. Bernand-Mantel, L. Ranno, S. Pizzini, S. M. Chérif, A. Stashkevich, S. Auffret, O. Boulle, G. Gaudin, M. Chshiev, C. Baraduc, H. Béa, Large-Voltage Tuning of Dzyaloshinskii-Moriya Interactions: A Route toward Dynamic Control of Skyrmion Chirality, *Nano Letters* 18 (2018) 4871–4877. doi:10.1021/acs.nanolett.8b01502.
- [21] T. Koyama, Y. Nakatani, J. Ieda, D. Chiba, Electric field control of magnetic domain wall motion via modulation of the Dzyaloshinskii-Moriya interaction, *Science Advances* 4 (2018). doi:10.1126/sciadv.aav0265.
- [22] W. Zhang, H. Zhong, R. Zang, Y. Zhang, S. Yu, G. Han, G. L. Liu, S. S. Yan, S. Kang, L. M. Mei, Electrical field enhanced interfacial Dzyaloshinskii-Moriya interaction in MgO/Fe/Pt

- system, *Applied Physics Letters* 113 (2018) 122406. doi:10.1063/1.5050447.
- [23] J. Suwardy, M. Goto, Y. Suzuki, S. Miwa, Voltage-controlled magnetic anisotropy and Dzyaloshinskii-Moriya interactions in CoNi/MgO and CoNi/pd/MgO, *Japanese Journal of Applied Physics* 58 (2019) 060917. doi:10.7567/1347-4065/ab21a6.
  - [24] M. Vanatka, J.-C. Rojas-Snchez, J. Vogel, M. Bonfim, M. Belmeguenai, Y. Roussign, A. Stashkevich, A. Thiaville, S. Pizzini, Velocity asymmetry of dzyaloshinskii domain walls in the creep and flow regimes, *Journal of Physics: Condensed Matter* 27 (2015) 326002.
  - [25] D. Chiba, T. Ono, Control of magnetism in Co by an electric field, *Journal of Physics D: Applied Physics* 46 (2013) 213001.
  - [26] B. Dieny, M. Chshiev, Perpendicular magnetic anisotropy at transition metal/oxide interfaces and applications, *Review of Modern Physics* 89 (2017) 25008. doi:10.1103/RevModPhys.89.025008.
  - [27] K. Kita, D. W. Abraham, M. J. Gajek, D. C. Worledge, Electric-field-control of magnetic anisotropy of Co<sub>0.6</sub>Fe<sub>0.2</sub>B<sub>0.2</sub>/oxide stacks using reduced voltage, *Journal of Applied Physics* 112 (2012) 33919. doi:10.1063/1.4745901.
  - [28] T. Nozaki, A. Koziol-Rachwał, W. Skowroński, V. Zayets, Y. Shiota, S. Tamaru, H. Kubota, A. Fukushima, S. Yuasa, Y. Suzuki, Large voltage-induced changes in the perpendicular magnetic anisotropy of an mgo-based tunnel junction with an ultrathin fe layer, *Physical Review Applied* 5 (2016) 044006. doi:10.1103/PhysRevApplied.5.044006.
  - [29] N. Bergeard, J. P. Jamet, A. Mougin, J. Ferré, J. Gierak, E. Bourhis, R. Stamps, Dynamic fluctuations and two-dimensional melting at the spin reorientation transition, *Physical Review B* 86 (2012) 094431. doi:10.1103/PhysRevB.86.094431.
  - [30] M. Schott, A. Bernand-Mantel, L. Ranno, S. Pizzini, J. Vogel, H. Ba, C. Baraduc, S. Auffret, G. Gaudin, D. Givord, The skyrmion switch: Turning magnetic skyrmion bubbles on and off with an electric field, *Nano Letters* 17 (2017) 3006–3012. doi:10.1021/acs.nanolett.7b00328.
  - [31] B. Kaplan, G. A. Gehring, The domain structure in ultrathin magnetic films, *Journal of Magnetism and Magnetic Materials* 128 (1993) 111–116. doi:10.1016/0304-8853(93)90863-W.
  - [32] V. Gehanno, Y. Samson, A. Marty, B. Gilles, A. Chamberod, Magnetic susceptibility and magnetic domain configuration as a function of the layer thickness in epitaxial fepd(0 0 1) thin films ordered in the llo structure, *Journal of Magnetism and Magnetic Materials* 172

- (1997) 26 – 40. doi:10.1016/S0304-8853(97)00089-9.
- [33] M. Heide, G. Bihlmayer, S. Blügel, Dzyaloshinskii-moriya interaction accounting for the orientation of magnetic domains in ultrathin films: Fe/w(110), *Physical Review B* 78 (2008) 140403. doi:10.1103/PhysRevB.78.140403.
  - [34] M. D. Kuz'min, Shape of Temperature Dependence of Spontaneous Magnetization of Ferromagnets: Quantitative Analysis, *Physical Review Letters* 94 (2005) 107204. doi:10.1103/PhysRevLett.94.107204.
  - [35] I. A. Yastremsky, O. M. Volkov, M. Kopte, T. Kosub, S. Stienen, K. Lenz, J. Lindner, J. Fassbender, B. A. Ivanov, D. Makarov, Thermodynamics and Exchange Stiffness of Asymmetrically Sandwiched Ultrathin Ferromagnetic Films with Perpendicular Anisotropy, *Physical Review Applied* 12 (2019) 64038. doi:10.1103/PhysRevApplied.12.064038.
  - [36] P. J. Metaxas, J. P. Jamet, A. Mougin, M. Cormier, J. Ferré, V. Baltz, B. Rodmacq, B. Dieny, R. L. Stamps, Creep and flow regimes of magnetic domain-wall motion in ultrathin Pt/Co/Pt films with perpendicular anisotropy, *Physical Review Letters* 99 (2007) 217208. doi:10.1103/PhysRevLett.99.217208.
  - [37] T. Dohi, S. Kanai, F. Matsukura, H. Ohno, Electric-field effect on spin-wave resonance in a nanoscale CoFeB/MgO magnetic tunnel junction, *Applied Physics Letters* 111 (2017) 72403. URL: <https://doi.org/10.1063/1.4999312>. doi:10.1063/1.4999312.
  - [38] J. Cho, S. Miwa, K. Yakushiji, H. Kubota, A. Fukushima, C.-Y. You, S. Yuasa, Y. Suzuki, Effect of electric field on the exchange-stiffness constant in a  $\text{Co}_{12}\text{Fe}_{72}\text{B}_{16}$  disk-shaped nanomagnet 65 nm in diameter, *Phys. Rev. Applied* 10 (2018) 014033. URL: <https://link.aps.org/doi/10.1103/PhysRevApplied.10.014033>. doi:10.1103/PhysRevApplied.10.014033.
  - [39] U. Atxitia, D. Hinzke, O. Chubykalo-Fesenko, U. Nowak, H. Kachkachi, O. N. Mryasov, R. F. Evans, R. W. Chantrell, Multiscale modeling of magnetic materials: Temperature dependence of the exchange stiffness, *Physical Review B* 82 (2010) 134440. doi:10.1103/PhysRevB.82.134440.
  - [40] R. Moreno, R. F. L. Evans, S. Khmelevskyi, M. C. Muñoz, R. W. Chantrell, O. Chubykalo-Fesenko, Temperature-dependent exchange stiffness and domain wall width in co, *Physical Review B* 94 (2016) 104433. doi:10.1103/PhysRevB.94.104433.
  - [41] Y. O. Kvashnin, W. Sun, I. Di Marco, O. Eriksson, Electronic topological transition and noncollinear magnetism in compressed hcp co, *Physical Review B* 92 (2015) 134422. doi:10.



1103/PhysRevB.92.134422.

- [42] I. Turek, J. Kudrnovsk, V. Drchal, P. Bruno, S. Blgel, Ab initio theory of exchange interactions in itinerant magnets, *physica status solidi (b)* 236 (2003) 318–324. doi:10.1002/pssb.200301671.
- [43] J. Suwardy, K. Nawaoka, J. Cho, M. Goto, Y. Suzuki, S. Miwa, Voltage-controlled magnetic anisotropy and voltage-induced dzyaloshinskii-moriya interaction change at the epitaxial fe(001)/mgo(001) interface engineered by co and pd atomic-layer insertion, *Physical Review B* 98 (2018) 144432. doi:10.1103/PhysRevB.98.144432.