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A systematic study of radiative torque grain alignment in the diffuse interstellar medium

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ABSTRACT

Context. Analyses of *Planck* data have demonstrated that the grain alignment efficiency is almost constant in the diffuse and translucent interstellar medium (ISM).

Aims. We aim to test whether the radiative torque (RAT) theory is compatible with these new observational constraints on grain alignment.

Methods. We combine a numerical magnetohydrodynamical simulation with a state-of-the-art radiative transfer post-processing code POLARIS which incorporates a physical dust model and the detailed physics of grain alignment by RATs. A dust model based on two distinct power-law-sized distributions of spherical graphite grains and oblate silicate grains was designed to reproduce the mean spectral dependence of extinction and polarization observed in the diffuse ISM. From a simulation of interstellar turbulence obtained with the adaptive-mesh-refinement code RAMSES, we extracted a data cube with physical conditions representative of the diffuse ISM. We post-process the RAMSES cube with POLARIS to compute the grain temperature and alignment efficiency in each cell of the cube. Finally, we simulate synthetic dust emission and polarization observations.

Results. In our simulation, the grain alignment efficiency is well-correlated with the gas pressure, but not with the radiative torque intensity. Because of the low dust extinction in our simulation, the magnitude of the radiative torque varies little, decreasing only for column densities larger than 10^{22} cm^{-2} . In comparing our synthetic maps with those obtained assuming a uniform alignment efficiency, we find no systematic difference and very small random differences. The dependencies of the polarization fraction p with the column density N_{H} or with the dispersion in polarization angle S are also similar in both cases. The drop of grain alignment produced by the RAT model in the denser cells of the data cube does not significantly affect the patterns of the synthetic polarization maps, the polarization signal being dominated by the line-of-sight and beam integration of the geometry of the magnetic field. If a star is artificially inserted at the center of the simulation, the polarization fraction is increased everywhere, with no specific pattern around the star. The angle-dependence of the RAT efficiency is not observed in simulated maps and where the magnetic field is artificially set to a uniform configuration in the plane of the sky, it is only seen to be very weak in the optimal configuration.

Conclusions. The RAT alignment theory is found to be compatible with the *Planck* polarization data for the diffuse and translucent ISM in the sense that both uniform alignment and RAT alignment lead to very similar simulated maps. To further test the predictions of the RAT theory in an environment where an important drop of grain alignment is expected, high-resolution polarization observations of dense regions must be confronted with numerical simulations sampling high-column densities ($N_{\text{H}} > 10^{22} \text{ cm}^{-2}$) through dense clouds, given a sufficient statistical basis.

Key words. submillimeter: ISM – magnetic fields – radiative transfer – polarization – dust, extinction

1. Introduction

Polarization of starlight and of dust thermal emission are commonly used as observational tracers of interstellar magnetic field orientation within the Milky Way as well as in external galaxies (see e.g., Hiltner 1949; Chapman et al. 2011; Sadavoy et al. 2018; Planck Collaboration XII 2020; Lopez-Rodriguez et al. 2020). This polarization is produced by the dichroism of the solid phase of the ISM and composed of elongated dust grains that are spinning and precessing around the local magnetic field.

A variety of mechanisms have been proposed to explain how the spin axis of dust grains can become aligned with interstellar magnetic fields, overcoming the random torques produced by impinging gas particles which tend to disalign them. Shortly after the discovery of starlight polarization (Hall 1949; Hiltner 1949), grain alignment was suggested to be the result of magnetic relaxation (Davis & Greenstein 1951, DG hereafter).

The interstellar magnetic field strength is too low, however, for the DG mechanism to function in the diffuse ISM. Furthermore, grain alignment by magnetic relaxation works like a heat

engine, requiring a temperature difference between gas and dust. It must fail in dense cores, where $T_{\text{dust}} \approx T_{\text{gas}}$. Hence, the DG mechanism cannot account for the observed level of dust polarization on lines of sight (LOS) passing through dense molecular regions. Jones & Spitzer (1967) demonstrated that these limitations of the DG mechanism could be overcome if grains had the superparamagnetic properties that the presence of ferromagnetic inclusions in the grain matrix provides. Purcell (1979) found that the formation of molecular hydrogen on the grain surface might spin-up the grain to superthermal velocities, allowing for grain alignment even though $T_{\text{dust}} \approx T_{\text{gas}}$.

The radiative torques (RATs) exerted onto grains by the absorption and scattering of photons can also spin-up and align grains with the magnetic field, provided that grains have a certain asymmetry called helicity (Dolginov & Mitrofanov 1976; Draine & Weingartner 1996, 1997). Through a number of studies published in a series of papers, a model of grain alignment by RATs was constructed (Lazarian & Hoang 2007a, 2008, 2019; Hoang & Lazarian 2008, 2014, 2016), opening the pathway towards quantitative comparisons with the observations (Bethell et al. 2007; Seifried et al. 2019).

Several studies have looked for the distinctive signatures of the RAT mechanism in polarization observations. The observed variations of the polarization fraction in the optical or in the submillimeter are found to be in qualitative agreement with what is expected from the RAT theory: a strong drop in starless cores (Alves et al. 2014; Jones et al. 2015), an increase with the radiation field intensity in dense clouds with embedded YSOs (Whittet et al. 2008) or around a star (Andersson et al. 2011), a modulation by the angle between the magnetic field and the direction of anisotropy of the radiation field (Andersson & Potter 2010; Vaillancourt & Andersson 2015), or a correlation with the wavelength λ_{max} where starlight polarization peaks (Andersson & Potter 2007). For a review of observational constraints favouring grain alignment by RATs, see Andersson et al. (2015). On the contrary, studies where the polarization fraction was corrected for the effect of the magnetic field before the analysis have not found any drop in the grain alignment efficiency, whether in the diffuse and translucent ISM (Planck Collaboration XII 2020) or in dense cores (Kandori et al. 2018, 2020). Clearly, more work is needed to solve this discrepancy and to reach conclusions that are statistically significant.

The purpose of this paper is to confront the predictions of the RAT theory to observations in a quantitative way through synthetic dust polarized emission maps built from a magnetohydrodynamic (MHD) simulation of interstellar turbulence with state-of-the-art grain alignment physics and an accurate treatment of radiative transfer. In our new modeling we post-process the MHD simulation of Hennebelle et al. (2008) used in Planck Collaboration Int. XX (2015) with the radiative transfer (RT) code POLARIS¹ (Reissl et al. 2016), using a physical dust model designed to reproduce the mean extinction and polarization curves observed in the diffuse ISM. The POLARIS tool, which incorporates the detailed physics of the RAT alignment theory was also applied to predict line emission including the Zeeman effect (Brauer et al. 2017a,b; Reissl et al. 2018; Pellegrini et al. 2019), as well as galactic radio observations (Reissl et al. 2019). Contrary to other dust emission codes, POLARIS is a full Monte-Carlo dust heating and polarization code solving the RT problem in the Stokes vector formalism for dichroic extinction and thermal re-emission by dust, simultaneously. Furthermore, POLARIS keeps track of each of the photon packages in order to simulate

the radiation field in complex environments, allowing for the determination of the parameters required by the grain alignment physics. In essence, this paper stands as a follow-up to Planck Collaboration Int. XX (2015) in which the modeling was done based on the simplifying assumption of uniform grain alignment, in addition to that of Seifried et al. (2019), where grain alignment was properly computed with POLARIS but lacked a well-constrained dust model.

In this article, we use the numerical model of the RAT theory outlined by Hoang & Lazarian (2014) to estimate the relative importance of the radiation field properties and of the gas pressure in establishing the level of grain alignment under physical conditions representative of the diffuse and translucent ISM. The alignment of dust grains with the magnetic field by mechanical torques (MAT; Lazarian & Hoang 2007b; Das & Weingartner 2016; Hoang et al. 2018) is also of great interest for our purpose. However, MAT is not yet a predictive theory, as RAT is, and, thus, it cannot be integrated into our modeling. Nonetheless, further in this paper, we discuss some implications of the possible grain alignment by mechanical torques.

The paper is structured as follows. In Sect. 2, we introduce the MHD simulation used in this study and the radiative transfer that is applied to it. The modeling of dust is described in Sect. 3 and that of grain alignment in Sect. 4. The output data cubes and maps from the POLARIS modeling are presented in Sects. 5 and 6 for two different setups of the radiation field. Our results are discussed in Sect. 7 and summarized in Sect. 8.

2. MHD simulations and radiative transfer

2.1. The RAMSES MHD simulation

As a model for a volume of neutral ISM material, including both diffuse and dense gas on the way to forming molecular clouds, we consider a single snapshot from an MHD simulation computed with the adaptive-mesh-refinement code RAMSES (Teyssier 2002; Fromang et al. 2006). This particular simulation of interstellar MHD turbulence is the same as the one that is used in Planck Collaboration Int. XX (2015) and we refer the reader to that paper and to Hennebelle et al. (2008), where the simulation was originally presented, for further details. To give its essential characteristics, it follows the formation of structures of cold neutral medium gas (CNM, $n_{\text{gas}} \sim 100 \text{ cm}^{-3}$, $T_{\text{gas}} \sim 50 \text{ K}$) within head-on colliding flows of warm neutral medium (WNM, $n_{\text{gas}} \sim 1 \text{ cm}^{-3}$, $T_{\text{gas}} \sim 8000 \text{ K}$). The colliding flow setup provides a convenient way to form such a mixture of diffuse and dense structures that reproduce several observational properties of turbulent molecular clouds (see, e.g., Hennebelle & Falgarone 2012), although cloud formation may actually proceed through other mechanisms, such as spiral density waves (Dobbs et al. 2006). The simulation volume is threaded by a magnetic field that is initially aligned with the direction of the flows. From this simulation, we extract data over a cubic subset 18 pc along each side, located near the center of the full 50 pc box. The extracted data comprise total gas density n_{gas} , pressure P_{gas} , and components B_x , B_y , and B_z of the magnetic field. Unlike in Planck Collaboration Int. XX (2015), however, we performed this extraction using the full resolution of the simulation (0.05 pc per pixel) instead of the coarser 0.1 pc per pixel resolution that was used in Planck Collaboration Int. XX (2015). The average total gas density in the simulation cube is about 15 cm^{-3} leading to a total gas mass of $\approx 3400 M_{\odot}$, assuming a molecular weight $\mu = 1.4$. The components of the magnetic field have a dispersion

¹ <http://www1.astrophysik.uni-kiel.de/~polaris/>

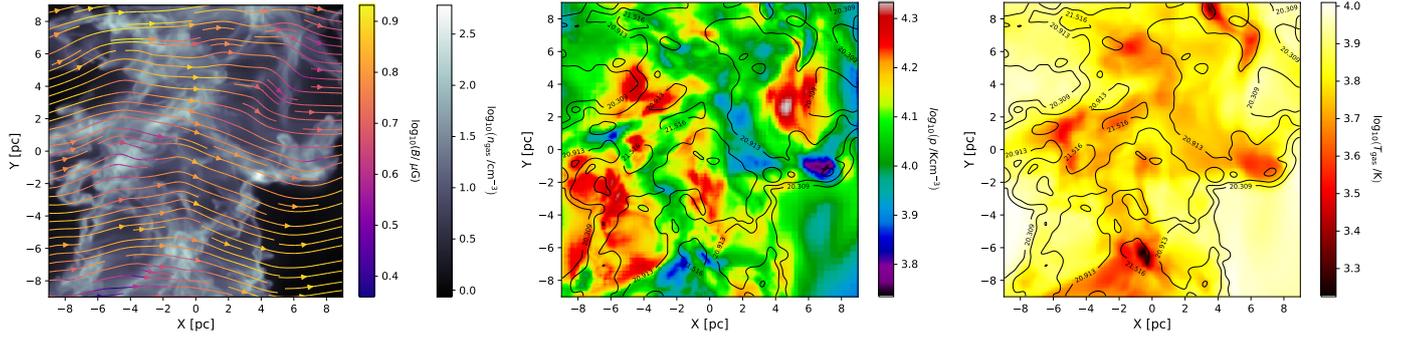


Fig. 1. RAMSES MHD parameters averaged cell by cell along the Z axis of the MHD cube: gas density n_{gas} (left), gas pressure P_{gas} (center), and gas temperature T_{gas} (right). The vector field shows the averaged magnetic B_x and B_y components and the colorbar shows $B = (B_x^2 + B_y^2)^{1/2}$. Contour lines indicate the logarithm of column density N_{H} .

Table 1. Properties of the radiation field setups for the MC dust grain heating and alignment simulations.

Setup	Description
ISRF	Diffuse and isotropic ISRF with the SED from Mathis et al. (1983) with $G_0 = 1$
STAR	ISRF plus one additional star at the very center of the grid with $R_* = 15 R_{\odot}$ and $T_* = 15000$ K

of $3 \mu\text{G}$ and a mean value of about $5 \mu\text{G}$ with a direction that is typically aligned with the flow (Planck Collaboration Int. XX 2015, Fig. 15).

We used this simulation, first, to allow for a direct comparison of our results with those obtained with the same simulation assuming a uniform alignment of dust grains along the magnetic field lines (Planck Collaboration Int. XX 2015) and, second, because it is representative of the diffuse ISM, while still harboring dense cores ($n_{\text{gas}} \sim 10^4 \text{ cm}^{-3}$) where the drop in the grain alignment efficiency may be more pronounced. From this simulation, we utilize the gas density n_{gas} , the gas temperature T_{gas} , and the magnetic field magnitude as well as its direction as input for our subsequent RT post-processing. In Fig. 1 we show the gas density, temperature, pressure as well as the magnetic field direction. The maps show direct, unweighted average quantities over the LOS, that is, along the z -axis of the simulation cube, for each direction.

2.2. Monte-Carlo photon propagation scheme of POLARIS

The post-processing steps of the MHD data consist of two parts. First, the radiation field is calculated with a Monte-Carlo (MC) approach in order to derive the necessary quantities for dust heating and grain alignment. In a second step we create synthetic dust emission and polarization maps. For all the RT simulations we make use of the RT code POLARIS (Reissl et al. 2016).

The local radiation field is determined by the 3D distribution of the dust and of the photon emitting sources. Commonly, the radiation field is quantified by the dimensionless parameter (Habing 1968):

$$G_0 = \frac{1}{5.29 \times 10^{-14} \text{ erg cm}^{-2}} \int_{6 \text{ eV}}^{13.6 \text{ eV}} u_E dE, \quad (1)$$

where u_E is the spectral energy density of the radiation field within the energy band where photoelectric heating is most relevant.

In this study, we considered two separate setups relating to the sources of radiation. For the ISRF setup, we only used a

parametrization of the spectral energy distribution (SED), as presented in Mathis et al. (1983) (see Table 1) for the MC sampling of wavelengths.

We note that we kept track of both the wavelength and direction \hat{k} of each photon package per grid cell. For the ISRF setup, photon packages are injected into the MHD simulation from a sphere surrounding the grid with a randomly sampled \hat{k} unit vector.

Since the grain alignment considered (see Sect. 4) is sensitive to the radiation field, we investigated a second case with an additional source of radiation. For this STAR setup, we considered a star (see Table 1) at the very center of the grid, in addition to the ISRF radiation, in order to quantify the influence of the radiation field on dust heating and grain alignment. Here, the photon packages start with a random direction \hat{k} from the very position of the star whereas the wavelengths of the photons are samples from the Planck function.

We note that the STAR setup is not entirely self-consistent since the star is added in post-processing and does not form in the MHD simulation itself, so that the magnetic field and the gas do not respond accurately to the stellar feedback. Hence, our model lacks the expected density cavity and the deformation of field lines in the vicinity of the star. Moreover, dust grains may get spun-up in close proximity to the star up to such a rate that the grains may rationally be disrupted by centrifugal forces (Hoang 2019). However, with a star with a luminosity of $L = 10^4 L_{\odot}$, a redistribution of the grains sizes may only happen at a maximum distance of ≈ 1 pc from the star (Hoang et al. 2019). Nevertheless, we provide the STAR setup in order to explore the influence of the radiation field and subsequent RAT alignment on ISM polarization patterns in a controlled environment. In this way, we can ensure that any deviation compared to the ISRF setup is purely due to radiation since the properties of the magnetic field and gas remain the same.

All MC RT simulations are performed with 100 wavelength bins logarithmically distributed over a spectrum of $\lambda \in [92 \text{ nm} - 2 \text{ mm}]$. For the photon package propagation scheme we apply a combination of the continuous absorption

technique introduced by [Lucy \(1999\)](#) to keep track of the photons per grid cell and the temperature correction of [Bjorkman & Wood \(2001\)](#) to ensure the correct spectral shift when a photon package gets absorbed and re-emitted. Assuming thermal equilibrium between the absorbed and emitted energy, the dust temperature per cell can be calculated with (see [Lucy 1999](#); [Bjorkman & Wood 2001](#); [Reissl et al. 2016](#), for details):

$$\int \bar{C}_{\text{abs},\lambda} J_{\lambda} d\lambda = \int \bar{C}_{\text{abs},\lambda} B_{\lambda}(T_{\text{dust}}) d\lambda, \quad (2)$$

where $\bar{C}_{\text{abs},\lambda}$ is the size averaged cross section of absorption. Here, we keep track of each of the temperatures corresponding to the distinct grain populations (silicate and graphite) individually as well as an average dust temperature. In detail, we solve Eq. (2) with $\bar{C}_{\text{abs},\lambda} = \bar{C}_{\text{abs},\lambda,\text{silicate}}$, $\bar{C}_{\text{abs},\lambda} = \bar{C}_{\text{abs},\lambda,\text{graphite}}$, and $\bar{C}_{\text{abs},\lambda} = \bar{C}_{\text{abs},\lambda,\text{silicate}} + \bar{C}_{\text{abs},\lambda,\text{graphite}}$ separately once the radiation field per cell is known (see also [Appendix A](#)). Consequently, all the dust polarization simulations performed in this work are for an average dust grain and ignore the possible size dependence of the dust temperature. For the MC simulations of the radiation field, we consider the dust grains to be spherical since the dust shape and orientation has, for moderate elongations, only a minor influence on the grain absorption and scattering cross-sections (see e.g., [Draine & Fraisse 2009](#), their Fig. 2).

The local spectral energy density u_{λ} is defined as the sum over the directions of intensity J_{λ} of all photon packages that crossed a particular grid cell,

$$u_{\lambda} = \frac{4\pi}{c} \sum |J_{\lambda}|, \quad (3)$$

and the spectra anisotropy factor of the radiation field γ_{λ} can be defined as the vector sum of all radiation normalized by the total energy density,

$$\gamma_{\lambda} = \frac{|\sum J_{\lambda}|}{\sum |J_{\lambda}|}. \quad (4)$$

Consequently, $\gamma_{\lambda} = 1$ stands for an anisotropic radiation per wavelength, that is, a plane wave and $\gamma_{\lambda} = 0$ for a totally diffuse, in other words, a fully isotropic radiation field.

The total energy density per cell u_{rad} is then defined by:

$$u_{\text{rad}} = \int u_{\lambda} d\lambda, \quad (5)$$

where we integrate over the full wavelength range, from which we derive the normalized quantity $U_{\text{rad}} = u_{\text{rad}}/u_{\text{ISRF}}$, where $u_{\text{ISRF}} = 8.64 \times 10^{-13} \text{ erg cm}^{-3}$ is the total energy of the ISRF per unit volume in our solar neighborhood as introduced by [Mezger et al. \(1982\)](#). For a subsequent analysis and discussion, we define for each position in the MHD cube, the average anisotropy factor of the radiation field (e.g., [Bethell et al. 2007](#); [Tazaki et al. 2017](#)) as:

$$\langle \gamma \rangle = \frac{1}{u_{\text{rad}}} \int \gamma_{\lambda} u_{\lambda} d\lambda, \quad (6)$$

and the average $\cos \vartheta$ as:

$$\langle \cos \vartheta \rangle = \frac{1}{u_{\text{rad}}} \int \cos \vartheta_{\lambda} u_{\lambda} d\lambda, \quad (7)$$

where $\vartheta_{\lambda} = \angle(\mathbf{k}_{\lambda}, \mathbf{B})$ is the angle between the direction \mathbf{k}_{λ} of the radiation field per wavelength bin and the direction \mathbf{B} of the local magnetic field lines.

The quantification of polarized radiation can be done in the Stokes vector formalism with $S = (I, Q, U, V)^T$, where I is the total intensity, Q and U are the components of the linear polarization, and V is the circularly polarized part. For the subsequent ray-tracing we make use of the full set of RT equations in the Stokes vector formalism in order to carry the full information of dust emission and extinction including polarization through the grid. We use a Runge-Kutta solver to project the rays onto a detector that stores each of the Stokes components as well as optical depth and column density. For the intensity I , we handle the contribution of silicate and graphite grains separately. Finally, the fraction of linear polarization is defined as:

$$p = \frac{\sqrt{Q^2 + U^2}}{I}. \quad (8)$$

The orientation angle of the polarization vectors can be derived by:

$$\psi = \frac{1}{2} \text{atan2}(U, Q) \quad (9)$$

in the IAU convention for angles, as in [Planck Collaboration Int. XIX \(2015\)](#).

We use the polarization angle dispersion function \mathcal{S} introduced by [Serkowski \(1958\)](#) and [Hildebrand et al. \(2009\)](#). This function is a measure of the local dispersion of magnetic field orientations within an annulus δ around each position \mathbf{r} . The dispersion function reads

$$\mathcal{S}(\mathbf{r}, \delta) = \sqrt{\frac{1}{N} \sum_{i=1}^N [\psi(\mathbf{r}) - \psi(\mathbf{r} + \delta_i)]^2}, \quad (10)$$

where N is the number of pixels within the annulus. Following [Planck Collaboration Int. XX \(2015\)](#), we place the MHD cube at a distance of $D = 100 \text{ pc}$, use $\delta = FWHM/2$, here with a FWHM of $5'$, and a pixellization of three pixels per beam.

2.3. Radiative transfer post-processing of the RAMSES simulation

Since the MC method is based on stochastic sampling, derived quantities are inherently prone to noise ([Hunt et al. 1995](#)); a qualitative analysis of the noise is provided in [Appendix B](#). Hence, we perform the MC simulation with 5×10^8 photon packages per wavelength for the ISRF setup. For the STAR simulation we apply 5×10^8 photon packages per wavelength for the ISRF and 2×10^7 photon packages for the star in the very center of the MHD cube constituting a balance between noise reduction and run-time.

The quantity G_0 seems to be particularly sensitive to the number of photons. For low photon numbers G_0 stays far below unity, whereas $G_0 = 1$ is expected at the borders of the MHD grid considering the [Mathis et al. \(1983\)](#) ISRF. These photons are emitted towards the computational domain from a sphere of radius twice the sidelength of the MHD cube. Only this combination of amount of photons and sphere radius guarantees a $G_0 \approx 1$ and an anisotropy factor $\gamma_{\lambda} \approx 0$, on average, over all the photons entering the simulation domain. Photons permanently scatter or become absorbed and are subsequently re-emitted in the POLARIS RT simulations. Photons newly injected into the grid may be deflected out of the grid already after a few such events and cannot carry their energy deeper inside. Consequently, the average energy density u_{rad} is about 2–5% lower

than the expected u_{ISRF} towards the center of the RAMSES MHD domain. As we discuss below, such a loss of energy only results in a modification of the polarization fractions by a fraction of a percent.

3. The dust model

3.1. Grain properties

Dust models compatible with observational constraints in the diffuse ISM in extinction, emission and polarization require distinct dust populations (Draine & Fraisse 2009; Siebenmorgen et al. 2014; Guillet et al. 2018): one population of very small grains to reproduce the UV bump and the mid-IR emission bands; one population of non-spherical silicate grains to account for the observed polarization in the optical, in the mid-IR silicate bands and in the FIR and sub-millimeter; and one population of carbonaceous grains (graphite or amorphous carbon; spherical or not) to complete the fit.

To confront the predictions of the RAT theory (Lazarian & Hoang 2007a; Hoang & Lazarian 2014) to the statistics of dust-polarized emission at 353 GHz obtained by the Planck collaboration (Planck Collaboration Int. XX 2015; Planck Collaboration XII 2020), we use a simplified dust model adapted to the POLARIS code. It is composed of two distinct size distributions of graphite ($\rho_G = 2.24 \text{ g.cm}^{-3}$) and silicate ($\rho_S = 3.0 \text{ g.cm}^{-3}$) grains. Graphite grains are assumed to be spherical, while silicate grains are spheroidal with an oblate shape. We note a_{\parallel} (resp. a_{\perp}) the size of the oblate silicate grain along (resp. perpendicular to) its symmetry axis, and $s = a_{\parallel}/a_{\perp} = 0.5$ its aspect ratio. The sphere of equal volume has a radius $a = a_{\parallel}^{1/3} a_{\perp}^{2/3}$.

Each size distribution follows a power-law of index q , with cut offs at a_{\min} and a_{\max} , and mass per H m [g/H]:

$$\frac{dn(a)}{da} = \frac{3m(q+4)}{4\pi\rho(a_{\max}^{q+4} - a_{\min}^{q+4})} a^q, \quad (11)$$

where a is the radius of the grain for spherical grains, and the radius of the sphere of equal volume for spheroidal grains.

The absorption, scattering and polarization coefficients of spheroidal grains are calculated with the DDSCAT 7.3 code (Draine & Flatau 2013). DDSCAT provides the differential cross sections for extinction, absorption, and circular polarization required for an all-encompassing radiative transfer (RT) scheme, but has numerical limitations for large dust grains and small wavelengths. For this reason, we do not calculate those cross-sections for $\lambda < 0.25 \mu\text{m}$, a domain of the UV that is not of interest for our study.

The absorption and scattering coefficients for spherical dust grains are calculated on the fly at all wavelengths by POLARIS itself with Mie theory, based on the refractive indices of the silicate and graphite grains (Weingartner & Draine 2001). Following the RAT theory, as outlined in Lazarian & Hoang (2007a) and Hoang & Lazarian (2014), we assume that grains larger than a certain threshold-size a_{align} are aligned along magnetic field lines, while other grains are not aligned, meaning that they do not present any preferred orientation. The value of a_{align} , which depends on the local physical conditions, is determined using the RAT theory implemented in the POLARIS code. However, to be able to compare our results with those obtained by neglecting variations in the grain alignment efficiency (Planck Collaboration Int. XX 2015), we also define a FIXED alignment setup in which $a_{\text{align}} = 100 \text{ nm}$ for silicate grains throughout

Table 2. Definition of the considered grain alignment mechanisms.

Alignment	Description
FIXED	$a_{\text{align}} = 100 \text{ nm}$
RAT	a_{align} calculated by RATs (see Sect. 4)

the cube, independently of the local physical conditions (see Table 2). We outline the physics of grain alignment later in Sect. 4 in more detail.

3.2. Radiative transfer with spherical grains

A few arguments favor using the optical properties of spherical grains, and not that of spheroidal grains, to compute the radiation transfer and dust temperature with POLARIS (see Sects. 2.3 and 4 for details). First, the dust shape and orientation has, for moderate elongations, only a minor influence on the grain absorption and scattering cross-sections (see, e.g., Draine & Fraisse 2009, their Fig. 2). Second, only silicate grains are spheroidal in our model, contributing to $\sim 50\%$ of the dust extinction in the optical (Weingartner & Draine 2001). Third, we are not able to compute correctly the radiation transfer by oblate grains in the far-UV ($\lambda < 0.25 \mu\text{m}$) because the dust cross-sections for oblate grains could not be calculated for large grains at these wavelengths (see Sect. 3.1), and would impose an extrapolation of those cross-sections down to the geometrical limit. Fourth, in the RAT theory the properties of the radiation field in each cell must be known to determine the grain alignment efficiency. As a consequence, the POLARIS code must first make an assumption on the grain alignment - random or perfect alignment for example - when computing the radiation transfer and dust temperature. Therefore, for the radiation transfer calculations leading to the determination of the characteristic of the radiation field and dust temperature in each cell, and for this purpose only, we replace oblate silicate grains by spherical grains of the same equivalent size.

3.3. Fitting extinction and polarization curves in the optical

Our dust model must reproduce the mean extinction and polarization curves observed in the diffuse interstellar medium for moderate extinction ($A_V \sim 1$). Polarization curves in extinction are usually modeled by the Serkowski law (Serkowski et al. 1975; Whittet et al. 1992),

$$p(\lambda) = p_{\max} \exp\left\{-K[\ln(\lambda/\lambda_{\max})]^2\right\}, \quad (12)$$

where λ_{\max} is the wavelength at which $p(\lambda)$ peaks, and K controls the width at half maximum of the curve. The mean values observed in the diffuse ISM are $\lambda_{\max} = 0.55 \mu\text{m}$, and $K = 0.92$ (Whittet et al. 1992). The maximal value of $p_{\max}/E(B-V)$ was long considered to be 9% (Serkowski et al. 1975). It was recently reevaluated to be at least 13% (Planck Collaboration XII 2020; Panopoulou et al. 2019), corresponding to a polarization fraction of $p_V/\tau_V \simeq 4.5\%$, with $\tau_V = 1.086 A_V$.

For simplicity, lacking further constraints, we fix the power-law index of the silicate size distribution to $q_S = -3.5$ (Mathis et al. 1977). The value of λ_{\max} severely constrains the minimal size of aligned grains a_{align} , while the value of K provides a looser constraint on the upper cut-off a_{\max}^S of the silicate size distribution, which, in this case, is the only aligned population. We adapt a_{\max}^S and a_{align} to reproduce the overall shape

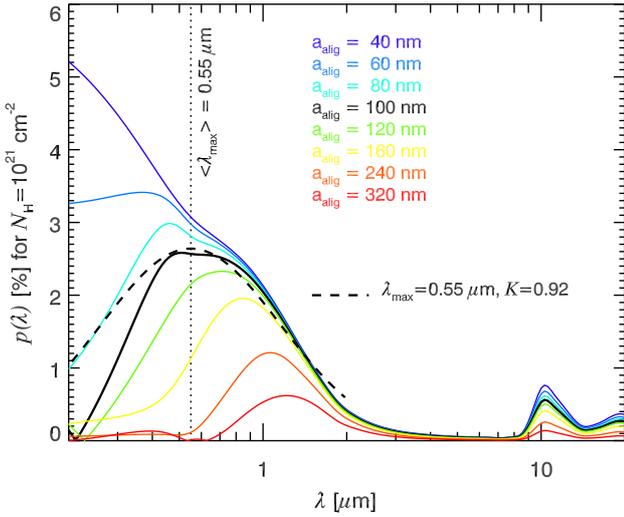


Fig. 2. Starlight polarization percentage for a column density $N_{\text{H}} = 10^{21} \text{ cm}^{-2}$, as a function of the wavelength, for increasing values of the alignment parameter a_{align} . Silicate grains are assumed to be aligned, while graphite grains are not. The dashed curve is the mean polarization curve observed in the diffuse ISM ($A_{\text{V}} \sim 1$), which constrains both the upper limit $a_{\text{max}}^{\text{S}}$ of the silicate size distribution and the minimal size of aligned grains a_{align} . Using our model, it is best fitted in the optical and near-infrared (NIR) for $a_{\text{align}} = 100 \text{ nm}$ (see Sect. 3.3 for a discussion of the poor fit in the UV).

of Serkowski’s curve. Figure 2 shows that a reasonable fit is obtained for $a_{\text{max}}^{\text{S}} = 400 \text{ nm}$ and $a_{\text{align}} = 100 \text{ nm}$. A better correspondence could not be obtained in the UV ($\lambda < 400 \text{ nm}$) using oblate grains if we imposed a peak close to 550 nm . This weakness is, however, of little importance for our investigation; first, because we do not study this part of the polarization spectrum and second, because the weak UV polarization in the mean polarization curve is known to be entirely produced by large ($a \geq 0.1 \mu\text{m}$) aligned grains (Kim & Martin 1995), whose abundance is constrained by the optical and NIR part of the spectrum. Therefore, we do not expect any change in our conclusions with a better fit of the UV polarization spectrum using more complex size distributions as per Draine & Fraisse (2009) or a power-law-sized distribution with prolate grains replacing oblate grains as per Guillet et al. (2018).

The remaining parameters can be constrained with the mean extinction curve observed in the diffuse ISM. We use the Mathis (1990) extinction curve per hydrogen, between 0.1 and $1 \mu\text{m}$ with $a_{\text{amin}}^{\text{S}} = 8 \text{ nm}$, $a_{\text{amin}}^{\text{G}} = 400 \text{ nm}$, $a_{\text{amin}}^{\text{M}} = 10 \text{ nm}$, $a_{\text{amax}}^{\text{G}} = 170 \text{ nm}$, $q_{\text{G}} = -3.9$, $m_{\text{S}} = 0.0034$ and $m_{\text{G}} = 0.0021$. This makes a total dust mass to gas mass ratio $m_{\text{dust}}/m_{\text{gas}} = 0.55\%$. Figure 3 shows a comparison of the resulting output of the POLARIS code with the Mathis (1990) mean extinction curve per H. The fit is correct in the UV and optical, but not in the NIR, as expected in a silicate-graphite model with power-law size distributions. Replacing spheres by oblate grains only marginally affects the resulting extinction curve (Fig. 3). In Sect. 7.1, we further discuss the potential impact on our results of the extinction curve in the NIR used for this particular MHD simulation. Figure 4 presents the resulting dependence of the polarization fraction in the optical (V band) and at 353 GHz as a function of our alignment parameter, a_{align} . Figure 2 demonstrates that the mean value of λ_{max} observed in the diffuse ISM can be obtained with our model for $a_{\text{align}} \approx 100 \text{ nm}$. According to Fig. 2, the observed range of variation of λ_{max} through the ISM ($0.4 \geq \lambda_{\text{max}} \geq 0.8 \mu\text{m}$, Whittet et al. 1992; Voshchinnikov et al. 2016) translates into a range of values

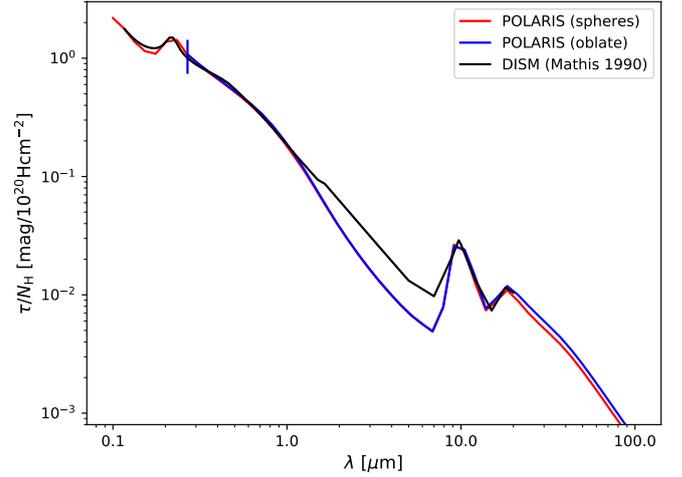


Fig. 3. Extinction curve from the UV to the mid-IR of the applied POLARIS dust models of spherical (red line) and non-spherical (blue line) grains in comparison with the measurements (black line) of Mathis (1990).

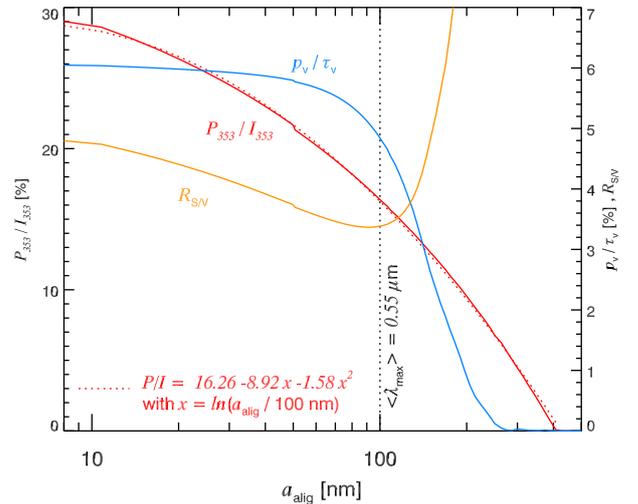


Fig. 4. Left axis: polarization fraction at 353 GHz , P/I , as a function of the alignment parameter a_{align} . Right axis: same for the polarization fraction in the V band $p_{\text{V}}/\tau_{\text{V}}$ and the polarization ratio, $R_{\text{S/V}} = P/I/(p_{\text{V}}/\tau_{\text{V}})$. The vertical dotted line indicates the value of a_{align} needed to reproduce the mean value of the Serkowski’s parameter λ_{max} of $0.55 \mu\text{m}$ observed in diffuse and translucent LOS. An empirical fit to the dependence of P/I on a_{align} is provided for convenience.

for a_{align} , between 75 and 150 nm . Between these two values λ_{max} , we expect of drop of the polarization fraction by a factor of two in the optical and only by a factor 1.4 at 353 GHz . This figure makes it clear that the dependence of the polarization fraction on the grain alignment efficiency differs in emission at 353 GHz and in extinction in the optical. A drop in grain alignment would therefore be easier to observe in the optical than at 353 GHz , because of a steeper dependence on a_{align} . For the mean $\lambda_{\text{max}} = 0.55 \mu\text{m}$, our model predicts $p_{\text{V}}/\tau_{\text{V}} = 4.8\%$, thereby reproducing the highest polarization fraction $p/E(B-V) > 13\%$ observed in the optical (Planck Collaboration XII 2020; Panopoulou et al. 2019). The situation is different with regard to emission where, with $P/I = 16.3\%$, our model is 20% below the highest polarization fraction at 353 GHz ($p_{\text{max}} = 20\text{--}22\%$, Planck Collaboration Int. XIX 2015; Planck Collaboration XII 2020). Correspondingly, the value of the polarization ratio $R_{\text{S/V}} = P/I/(p_{\text{V}}/\tau_{\text{V}}) \approx 3.4$,

is weaker than the value of $R_{S/V} \simeq 4.2$ observed in the diffuse and translucent ISM (Planck Collaboration XII 2020), but it is as expected within the range of the values obtained with compact astrosilicates (see Guillet et al. 2018, for a discussion of dust optical properties adapted to *Planck* observations). These small discrepancies have no impact on our conclusions as we do not attempt to reproduce the absolute value of the polarization fraction at 353 GHz but, rather, its relative variations with the environment, especially with the column density.

4. Insights on the radiative spin-up model

Simulating dust polarization by means of extinction and emission not only requires non-spherical dust grains but also a detailed knowledge of the grain alignment efficiency with the magnetic field orientation. Here, we focus explicitly on the RAT alignment physics as it is outlined in Hoang & Lazarian (2014).

4.1. The fiducial radiative torque (RAT) physics

Abandoning the notion of perfectly aligned dust grains requires us to model the physics of non-spherical spinning dust grains having their minor principle axis precessing around the magnetic field direction. In the RATs framework, a non-spherical irregular dust grain of equivalent radius a can gain angular momentum through the torques Γ_{rad} exerted by an anisotropic radiation field (Hoang & Lazarian 2014):

$$\Gamma_{\text{rad}} = \pi a^2 \int \left(\frac{\lambda}{2\pi} \right) \gamma_{\lambda} \cos(\vartheta_{\lambda}) Q_{\Gamma}(a, \lambda) u_{\lambda} d\lambda, \quad (13)$$

where γ_{λ} is the spectra anisotropy factor (Eq. (4)), and Q_{Γ} is the RAT efficiency (Draine & Weingartner 1996; Hoang & Lazarian 2014):

$$Q_{\Gamma} = \begin{cases} Q_{\Gamma}^{\text{ref}} & \text{if } \lambda \leq 1.8a \\ Q_{\Gamma}^{\text{ref}} \times \left(\frac{\lambda}{1.8a} \right)^{\alpha_Q} & \text{otherwise.} \end{cases} \quad (14)$$

Parameters Q_{Γ}^{ref} and α_Q depend on the grain shape and grain material. We note that the exact values of the parameters Q_{Γ}^{ref} and α_Q are not well constrained. Numerical calculations show that Q_{Γ}^{ref} can present a range of values comprised between 0.01 and 0.4, and that α_Q is between -2.6 and -4 (Hoang & Lazarian 2014; Herranen et al. 2019). We take an average of $\alpha_Q = -3$ as a reference value, and the exact value of Q_{Γ}^{ref} is determined for our dust model in Sect. 4.2.

Spinning grain tends to be disaligned by the random momentum transferred in collisions with gas particle (Davis & Greenstein 1951), as well as by the emission of IR photons (Draine & Lazarian 1998). The gas drag on dust grains acts on a characteristic timescale of

$$\tau_{\text{gas}} = \frac{3}{4\sqrt{\pi}} \frac{I_{\parallel}}{\mu m_{\text{H}} n_{\text{gas}} v_{\text{th}} a^4 \Gamma_{\parallel}} = \frac{2\sqrt{\pi}}{5} \frac{\rho_S s^{-2/3}}{\mu m_{\text{H}} \Gamma_{\parallel}} \frac{a}{n_{\text{gas}} v_{\text{th}}}, \quad (15)$$

where $v_{\text{th}} = (2k_{\text{B}}T_{\text{gas}}/(\mu m_{\text{H}}))^{1/2}$ is the thermal velocity of the gas particles (of mean mass μm_{H}), $\Gamma_{\parallel} \approx 1.1$ is a geometrical factor for oblate grains of aspect ratio $s = 0.5$, and $I_{\parallel} = \frac{8\pi}{15} \rho_S a_{\parallel} a_{\perp}^4 = \frac{8\pi}{15} \rho_S s^{-2/3} a^5$ is the moment of inertia of the oblate grain with respect to the minor axis. The drag timescale τ_{FIR} by IR photon emission can be accounted for by a single

parameter $\text{FIR} \equiv \tau_{\text{gas}}/\tau_{\text{FIR}}$ (Draine & Lazarian 1998; Lazarian & Hoang 2019)

$$\text{FIR} = 0.4 \left(\frac{0.1 \mu\text{m}}{a} \right) \left(\frac{30 \text{ cm}^{-3}}{n_{\text{gas}}} \right) \sqrt{\frac{100 \text{ K}}{T_{\text{gas}}}} \left(\frac{u_{\text{rad}}}{u_{\text{ISRF}}} \right)^{2/3}, \quad (16)$$

Combining gas drag and FIR photon emission, this leads to a total drag timescale for the dust grain of:

$$\tau_{\text{drag}} = \frac{\tau_{\text{gas}}}{1 + \text{FIR}}. \quad (17)$$

The alignment of dust grains with their minor axis parallel to the magnetic field direction is closely connected to overcoming the randomization of the rotation axis by gas bombardment and emission of IR photons. In the absence of any aligning torques, dust grain rotation is at thermal equilibrium with the gas, leading to a grain angular momentum of

$$J_{\text{th}} = \sqrt{k_{\text{B}}T_{\text{gas}}I_{\parallel}} \propto a^{2.5} \sqrt{T_{\text{gas}}}. \quad (18)$$

We note that the magnitude of J_{th} becomes constant as the dust grains thermalize with the gas and the orientation remains randomized over time.

In order to ensure the alignment of dust with the magnetic field direction, the spin-up process by RATs needs to dominate over gas collision and IR photon emission and bring grains to suprathermal rotation (Hoang & Lazarian 2014). Following Hoang & Lazarian (2008), we assume that dust grains are aligned in a stable configuration for:

$$\frac{J_{\text{rad}}}{J_{\text{th}}} = \frac{\tau_{\text{drag}} \Gamma_{\text{rad}}}{J_{\text{th}}} \geq 3. \quad (19)$$

This condition defines the minimal grain size a_{align} for dust grains to be aligned. If we use the approximate expression $Q_{\Gamma} \propto a^{-2.7}$ (Hoang & Lazarian 2014), and momentarily restrict our study to the case where the disaligning effect of IR photon emission can be neglected with respect to collisions with gas particles ($\text{FIR} \ll 1$), this minimal grain size follows the scaling:

$$a_{\text{align}}^{\text{FIR} \ll 1} \propto \left(\frac{Q_{\Gamma}^{\text{ref}} \langle \gamma \rangle \langle \cos \vartheta \rangle U_{\text{rad}}}{n_{\text{gas}} T_{\text{gas}}} \right)^{-1/3.2}. \quad (20)$$

This expression shows that the grain alignment radius is a slowly varying function of the ratio between the gas pressure and an effective intensity $Q_{\Gamma}^{\text{ref}} \langle \gamma \rangle \langle \cos \vartheta \rangle U_{\text{rad}}$ of the anisotropic component of the radiation field.

The final condition for grains to be aligned with the magnetic field direction requires a stable Larmor precession around the magnetic field. This condition can be estimated by comparing the Larmor precession timescale τ_{larm} (Lazarian & Hoang 2007a)

$$\tau_{\text{larm}} \propto \frac{a^2 s^2 \rho T_{\text{dust}}}{\chi B}, \quad (21)$$

accounting for the interplay of field strength and the paramagnetic properties of the grain, with the gas drag timescale τ_{gas} (Eq. (15)). If the grain can complete its precession before any gas-grain interaction significantly affects its angular momentum, we may consider it to be aligned with the magnetic field direction. Consequently, for $\tau_{\text{larm}} < \tau_{\text{gas}}$ a grain is considered to be aligned with the magnetic field direction, which defines the

maximal grain radius, a_{larm} , where grains cease to be aligned along the magnetic field lines (Lazarian & Hoang 2007a),

$$a_{\text{larm}} = 2.71 \times 10^5 \frac{s^2 (\chi/10^{-4}) (B/5 \mu\text{G})}{(n_{\text{gas}}/30 \text{ cm}^{-3}) (T_{\text{dust}}/15 \text{ K}) (\sqrt{T_{\text{gas}}/100 \text{ K}})} \text{ cm}. \quad (22)$$

Here, χ is the paramagnetic susceptibility of the grain material. Graphite grains have a magnetic susceptibility of about $\chi = 9.6 \times 10^{-10}$ (Weingartner 2006), whereas for ordinary paramagnetic silicate, we have $\chi = 4.2 \times 10^{-4}$ (Hunt et al. 1995; Hoang et al. 2014). In essence, graphite can barely perform a stable Larmor precession for the range of parameters of the RAMSES simulation (see Eq. (22)) due to this difference of about six orders of magnitude.

Laboratory experiments also suggest that most of the iron is bound within the silicate component of the ISM dust (see e.g., Davoisne et al. 2006; Demyk et al. 2017), providing superparamagnetic properties to the silicate populations for which a much better alignment is predicted (Jones & Spitzer 1967), if not perfect (Lazarian & Hoang 2008; Hoang & Lazarian 2016). In our model, we therefore assume that only silicate grains are aligned with the magnetic field direction, a choice that is consistent with observations of dust polarization (Mathis 1986; Costantini et al. 2005; Draine & Fraisse 2009; Vaillancourt & Matthews 2012).

The nutation of the grain during its precession tends to reduce polarization. This can be quantified by the Rayleigh reduction factor $R = \langle Q_J Q_X \rangle$ (Greenberg 1968; Roberge & Lazarian 1999, see also Appendix A). Q_J characterizes the degree of alignment of the angular momentum, J , with the magnetic field direction, whereas Q_X describes the internal degree of alignment between the minor principle axis a_{\parallel} of the dust grain and J . The average is then done over the time on the distribution function of the angle between the spin axis and the minor axis (for Q_X) and between the spin axis and the magnetic field (for Q_J). Radiative torques can align grains with the magnetic field \mathbf{B} in two distinct attractor points. One is characterized by $J \gg J_{\text{th}}$ (highJ hereafter) and the other one where J is of the same order as J_{th} (lowJ), respectively. While highJ corresponds to a perfect alignment, meaning $Q_J \approx 1$ and $Q_X \approx 1$, the lowJ attractor point is less well constrained. For paramagnetic materials, such as pure silicate without iron inclusions, the fraction of highJ to lowJ alignment, together with the values for Q_J and Q_X in the lowJ case, are not well determined by the RATs theory (Hoang & Lazarian 2014).

As discussed in Hoang & Lazarian (2016), a significant fraction of dust grains in the lowJ attractor would prevent the model from reproducing the highest polarization fractions observed by *Planck* in the diffuse ISM ($p_{\text{max}} \approx 20\%$, Planck Collaboration Int. XIX 2015). Alternatively, the polarization fraction could also be increased by introducing larger grains (Bethell et al. 2007) because this would increase the mass fraction of aligned grains. However, the presence of a significant fraction of large grains would prevent the dust model introduced in Sect. 3 from reproducing the mean Serkowski’s law and extinction curve of the diffuse ISM.

Thus, we make the assumption that silicate grains have ferromagnetic inclusions. Consequently, silicate grains align only at the highJ attractor point, and the Rayleigh reduction factor for RAT alignment is:

$$R(a) = \begin{cases} 1 & \text{if } a_{\text{align}} < a < a_{\text{larm}} \\ 0 & \text{otherwise} \end{cases}. \quad (23)$$

Assuming that silicates settle only at highJ would also prevent a so-called “wrong” alignment, that is, the alignment of the minor principal grain axis with the magnetic field direction (see Lazarian & Hoang 2007a). Thus, we do not model or discuss the implications of a possible “wrong” alignment of dust grains. Nevertheless, we note that POLARIS is, in principle, capable of calculating the internal alignment efficiency (Reissl et al. 2016) at lowJ. Furthermore, a_{larm} is only of minor relevance for silicate grains in our dust model since $a_{\text{max}} \ll a_{\text{larm}}$ even for ordinary paramagnetic grains let alone superparamagnetic ones (see also Appendix C.2).

Altogether, the exact parametrization of $R(a)$ (i.e., with or without internal alignment) is of minor relevance for the dust polarization calculations presented in this article since more sophisticated assumptions would scale down the overall degree of linear polarization, without affecting the polarization patterns at the smaller scales (see e.g., Brauer et al. 2016).

4.2. Calibrating the RAT efficiency Q_{Γ} on observational data

Our Eq. (14) involves the physical parameter Q_{Γ}^{ref} that controls the efficiency of radiative torques. The higher Q_{Γ}^{ref} , the better grains are aligned. The value of Q_{Γ}^{ref} must be determined using numerical tools like DDSCAT by calculating the radiative torques efficiency for a particular grain shape and material that constitutes the aligned dust population; here, oblate silicate grains of axis ratio $s = 1/2$. Herranen et al. (2019) carried out the most recent and extensive study of the dependence of Q_{Γ} on the ratio λ/a , for various grain shapes and materials. Although Q_{Γ} is not strictly constant at low λ/a according to these calculations, a constant value for Q_{Γ}^{ref} between 0.05 and 0.4 appears to be a reasonable model owing to the scatter in the calculations presented for different shapes (Herranen et al. 2019, Fig. 20).

This theoretical value for Q_{Γ}^{ref} can be compared to the value that is needed to obtain an alignment parameter a_{align} of 100 nm, the value necessary for our model to reproduce the mean Serkowski’s curve observed in the diffuse and translucent ISM (see Sect. 3). Using our RAMSES simulation with POLARIS, we find $Q_{\Gamma}^{\text{ref}} = 0.14$, a value that we use going forward.

4.3. Phase diagram for the grain alignment efficiency

It has long been established that the suprathermal rotation can allow for grain alignment (Purcell 1975, 1979). In the RAT modeling of Hoang & Lazarian (2014), grains are assumed to be aligned if the local physical conditions make them rotate three times faster than in thermal equilibrium with the gas. Given any efficient spin-up process (Lazarian et al. 2015), this necessary prerequisite allows for dust grains to align with the magnetic field direction because of paramagnetic effects acting on a microscopic level (see e.g., Barnett 1915; Davis & Greenstein 1951; Jones & Spitzer 1967; Purcell 1979, for details).

Figure 7 presents a synthetic view on the dependence of a_{align} on the local physical conditions in the Hoang & Lazarian (2014) RAT theory, in the form of a phase-diagram for the diffuse ISM. The y axis is the spin-up parameter $Q_{\Gamma}^{\text{ref}} \langle \gamma \rangle \langle \cos \vartheta \rangle U_{\text{rad}} / (n_{\text{gas}} T_{\text{gas}})$ (see Eq. (20)). The x axis is the FIR ratio (Eq. (16)) calculated for the reference value $a = 100$ nm. This phase diagram allows to estimate the grain alignment radius predicted by RATs for any physical conditions, as long as the wavelength-dependence of the radiation field can be reasonably described by the ISRF with a scaling factor U_{rad} . At low FIR ratio, $\tau_{\text{drag}} \approx \tau_{\text{gas}}$, and the alignment radius becomes

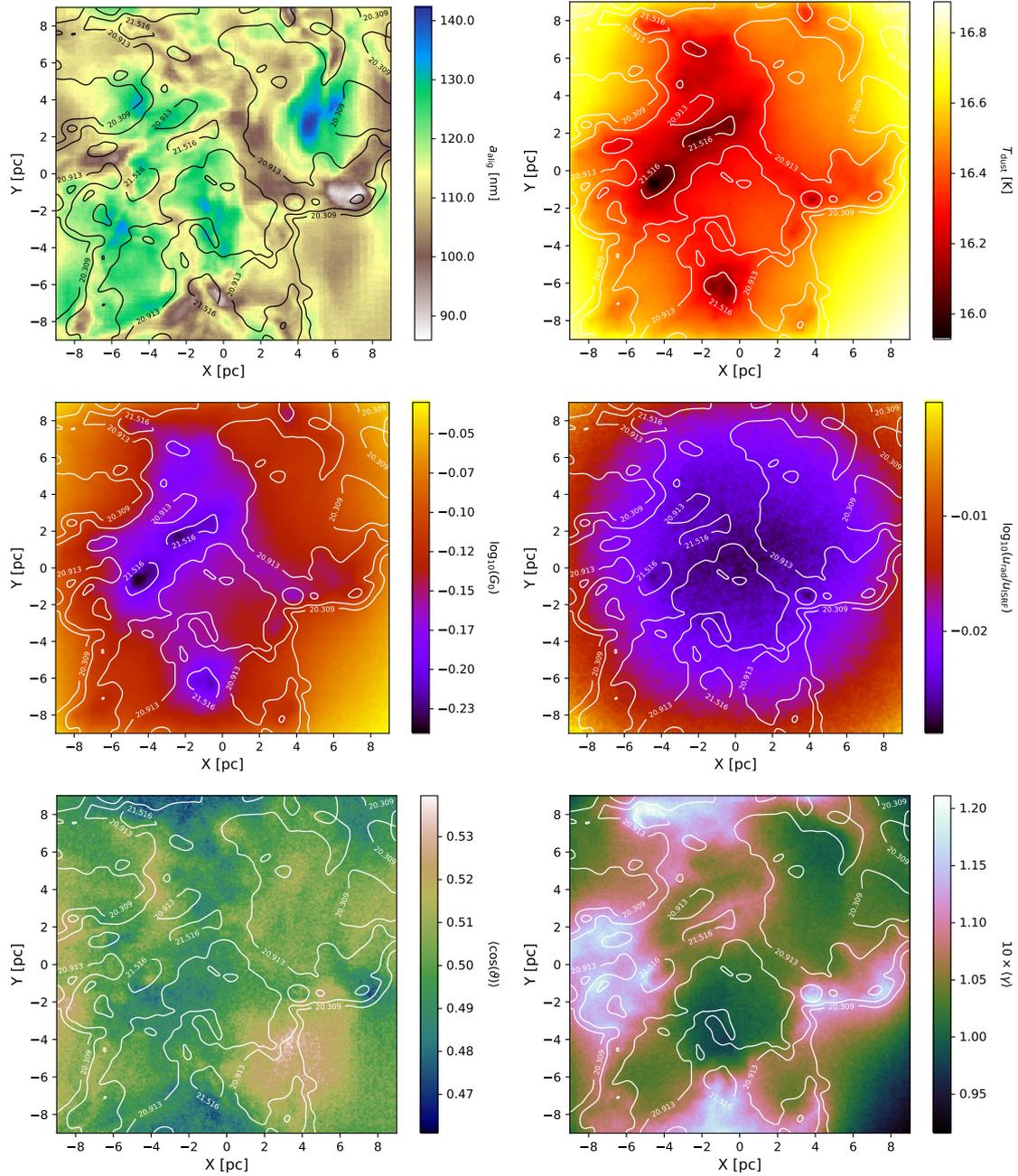


Fig. 5. Quantities averaged along the LOS derived by POLARIS MC simulations for the ISRF-RAT setup. Here, direct averages are done, without any weighting by another parameter. The individual panels show the alignment radius a_{alig} (top left), average dust temperature T_{dust} (top right), G_0 (middle left), the radiation field U_{rad} (middle right), the average angle $\langle \cos \vartheta \rangle$ (bottom left), and the anisotropy factor $\langle \gamma \rangle$ (bottom right), respectively.

independent of the FIR ratio. At a high FIR ratio, $\tau_{\text{drag}} \simeq \tau_{\text{FIR}} \propto a^2 U_{\text{rad}}^{-2/3}$ and the alignment efficiency a_{alig} becomes independent of the gas density.

Arrows indicate how a_{alig} varies when the corresponding parameter increases by a factor of ten. Because of the exponent $-1/3.2$ in Eq. (20), variations by orders of magnitude of any of these parameters are needed to significantly affect the value of a_{alig} .

5. Grain alignment in the translucent and diffuse ISM

In this section, we present the results of our calculations with POLARIS. Our MHD cube is representative of the diffuse and

translucent ISM. We start by presenting the statistics of the radiation field in the MHD cube, which controls the radiative torque efficiency. Then, we look for the physical variables that, under these conditions, control the variations of the grain alignment efficiency under the RAT theory. Finally, we compare the dust polarization maps when grains are aligned by radiative torques, and when the grain alignment is uniform, to test if the alignment model leaves some imprint in the polarization maps calculated with this MHD simulation.

5.1. Characteristics of the radiation field

Figure 5 presents the set of derived MC quantities for the case ISRF-RAT. All maps show the average of grid cells along the z

axis of the MHD cube, that is, along the LOS (histograms over the complete 3D domain are provided in Appendix C). For clarity regarding the parameters characteristic for the radiation field, the maps are not weighted by any quantity, for example, by density. Otherwise, characteristic features of the model ISRF would get modulated by the weighting, making it harder to discuss the different quantities on an individual basis. The map of the alignment radius a_{align} has a range of 80–145 nm. The map of a_{align} clearly correlates with the pressure map presented in Fig. 1, not with the density map.

The dust temperature is rather uniform in the entire simulation, between 16 and 17 K. Here, we show the combined temperatures averaged over the materials of silicate and graphite (individual temperatures are provided in Appendix C). Even with such a small temperature variation, a correlation with the column density stands out. Dust grains in the densest regions are colder because of the shielding by the surrounding dust. As expected, the small variations of G_0 coincide with the column density structure, as photons become more likely absorbed in dense regions. In contrast to G_0 , the total energy density u_{rad} is integrated over the entire spectrum and should be almost constant independently of the density because the total energy within the system remains conserved while being shifted towards longer wavelength by dust emission. Still, we see that u_{rad} is slightly (2% at most) smaller than u_{ISRF} . This is a small artifact of the MC method associated with the loss of photons (see Sect. 2.2).

The average angle $\langle \cos \vartheta \rangle$ between the radiation field and the magnetic direction draws the same picture of a totally diffuse radiation field. The values of $\langle \cos \vartheta \rangle$ in Fig. 5 cluster around a value of 0.5. We acknowledge that the quantity $\langle \cos \vartheta \rangle$ does not strictly correspond to a particular angle ϑ but represents an average over an ensemble of angles weighted by the cosine function and the radiation field (see Eq. (7)). However, we note that a $\cos \vartheta = 0.5$ would correspond to an angle of $\vartheta = 60^\circ$. This is exactly the value one obtains when averaging over a large ensemble of pairs of randomly orientated vectors. Hence, a value of 0.5 is consistent with a mostly isotropic radiation field (see also Appendix C).

Finally, the anisotropy factor $\langle \gamma \rangle$ has a trend with higher values in denser regions and amounts to an average value of 0.11 comparable with the value of 0.1 usually given in the literature (see e.g. Lazarian & Hoang 2007a; Hoang & Lazarian 2014) for the ISM. We run simulations with no dust at all, that is, at a ratio of $m_{\text{dust}}/m_{\text{gas}} = 0\%$ in the RAMSES cube. These test simulations show that $\langle \gamma \rangle > 0$ (see Appendix C). Even with more photons and for different radii of the source sphere, the anisotropy factor cannot be pushed below $\langle \gamma \rangle < 0.045$. We speculate that this may be a numerical limitation of the applied MC techniques.

5.2. What drives the variations of the grain alignment parameter a_{align} ?

Figure 6 presents the way in which the alignment parameter calculated by POLARIS for our RAMSES simulation depends on the local physical conditions, using the same phase diagram as in Fig. 7. The density, temperature, and radiation field characterizing this simulation only occupies a small surface in our phase diagram. The density of points in this phase diagram allows to separate the WNM phase (high temperature, low density) from the CNM phase (high density, low temperature) where grains are not well aligned in a small fraction of cells (red points). Comparing Figs. 7 and 6, we see that our simple analytic derivation of a_{align} (see Sect. 4) reproduces the numerical results of POLARIS quite well.

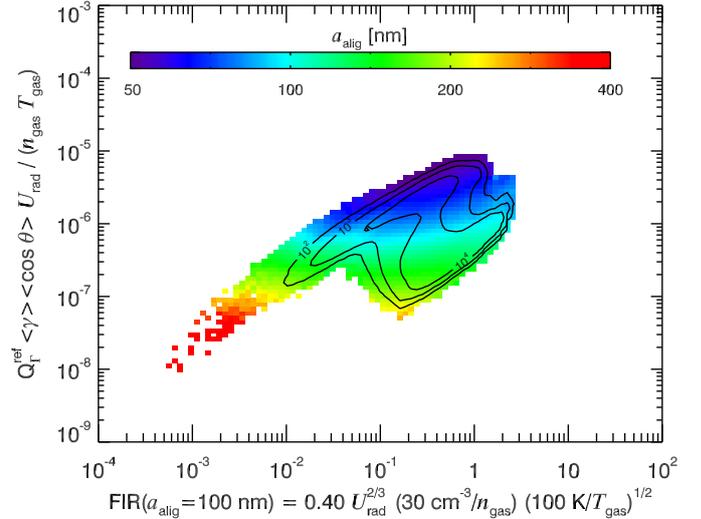


Fig. 6. Alignment parameter a_{align} calculated by POLARIS for the ISRF-RAT simulation in the phase diagram of Fig. 7. Contour lines indicate the density of points, delimitating two valleys of points corresponding to the cold (CNM, upper branch) and warm (WNM, lower branch) phases in the simulation.

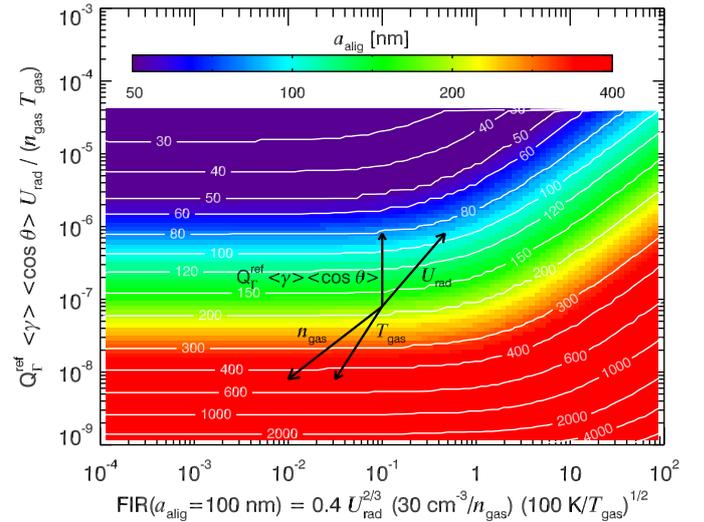


Fig. 7. Alignment parameter, a_{align} in nm, as a function of the spin-up parameter, $Q_{\gamma}^{\text{ref}} \langle \gamma \rangle \langle \cos \vartheta \rangle U_{\text{rad}} / (n_{\text{gas}} T_{\text{gas}})$ (see Eq. (20)), and of the FIR ratio at $a = 100$ nm (Eq. (16)), following Hoang & Lazarian (2014). Black arrows indicate the displacement in that frame when the corresponding physical quantity increases by a factor of ten.

Figure 8 shows the dependence of the mean density-weighted, a_{align} parameter as a function of the column density, for any LOS along the three axes of the cube. The value of $\langle a_{\text{align}} \rangle$ is rather uniform on a large range of column densities, from 4×10^{20} to $2 \times 10^{21} \text{ cm}^{-2}$, but increases at the lowest and highest column densities. A trend of a similar shape is reported in Seifried et al. (2019) for the dependency of the alignment radius a_{align} on gas density n_{gas} . However, their MHD data set has about a one order of magnitude lower gas densities and temperate and a $G_0 > 0$ leading to values of a_{align} that are up to a factor of 6.5 smaller than ours.

To understand what drives grain alignment, we plot on Fig. 9 how the mean, density-weighted, gas pressure $n_{\text{gas}} T_{\text{gas}}$ (responsible for grain disalignment) and radiative torque Γ_{rad} (responsible

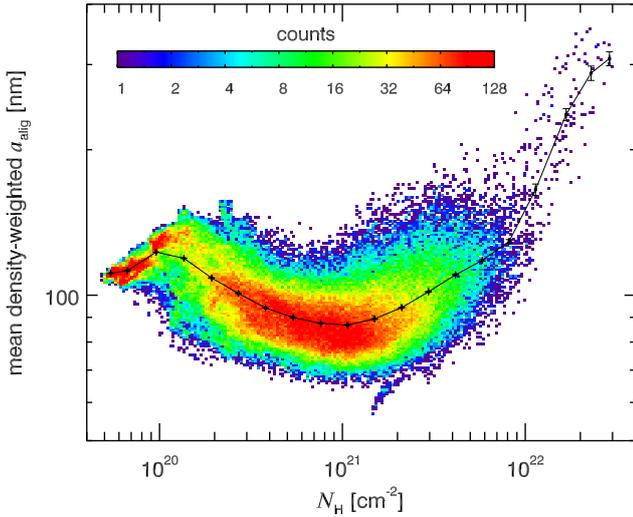


Fig. 8. Mean, density-weighted a_{align} parameter for our ISRF case as a function of the column density for our simulated cube, combining viewing angles along x , y , and z .

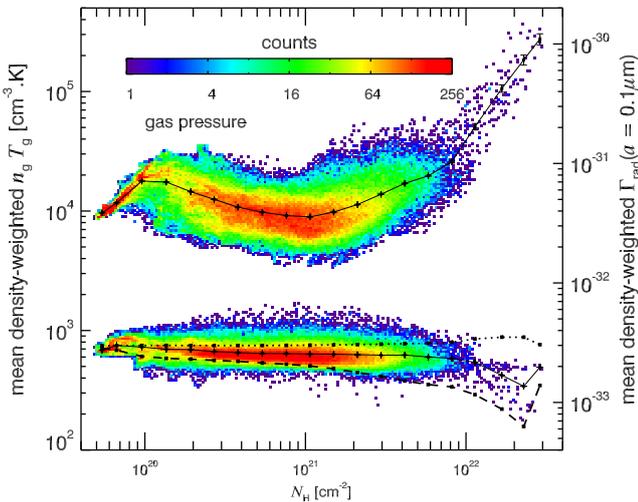


Fig. 9. Mean, density-weighted gas pressure $n_{\text{gas}} T_{\text{gas}}$ (left axis), and radiative torque Γ_{rad} (right axis) as a function of the column density for our simulated cube, combining viewing angles along x , y , and z . To avoid a biased comparison, both axes share the same amplitude in log. This figure is to be compared with Fig. 8. A comparison with our simple model using u_{rad} (dotted) and G_0 (dashed) for the calculation of Γ_{rad} is overplotted.

for grain alignment) calculated for a grain size $a = 0.1 \mu\text{m}$ depend on the column density.

The comparison of Figs. 9 with 8 makes it clear that, in opposition to what is usually assumed, it is the variations in the gas pressure that drive the variations of grain alignment, and not the variations of the radiative torques through dust extinction. The latter is almost constant, slightly decreasing with N_{H} . The decrease of the radiative torques intensity cannot therefore be invoked to explain the decrease of the alignment efficiency within the range of column densities present in our simulation.

Table 3 quantifies this interpretation by presenting the value of the Pearson correlation coefficient between the alignment parameter a_{align} and different physical quantities characterizing the local ISM in our simulation, such as the density, temperature, gas pressure, radiation field intensity. A positive (resp. negative)

Table 3. Pearson coefficients for the correlation of $\log(a_{\text{align}})$ with the log of different physical quantities.

G_0	0.21
$1/(n_{\text{gas}} T_{\text{gas}})$	0.91
$G_0/(n_{\text{gas}} T_{\text{gas}})$	0.86
$\langle \gamma \rangle \langle \cos \vartheta \rangle G_0/(n_{\text{gas}} T_{\text{gas}})$	0.90

Notes. In the diffuse and translucent ISM, a_{align} is primarily driven by the gas pressure, not by the characteristics of the radiation field (direction, anisotropy factor, or intensity). An increasing intensity of the radiation field even tends to disalign grains by increasing FIR photon emission.

correlation coefficient means that an increase of the quantity tends to increase (resp. decrease) a_{align} , and therefore to disalign (resp. align) grains. The correlation between the radiation field intensity as measured by G_0 and the grain alignment parameter a_{align} is weak but, surprisingly, positive. This results from two competing effects of the radiation field on the RATs efficiency. These are the spin-up effect of radiative torques, expressed by Eq. (19), and the disaligning effect of FIR emission, described by Eq. (16). In the WNM phase of the diffuse ISM, where the gas temperature is high and dust extinction remains weak everywhere, it is the latter effect that dominates over the former. This implies that in the WNM, an increase in the radiation field intensity makes the grain alignment efficiency decrease, not increase, due to the damping of grain rotation by the emission of IR photons.

Grain alignment in the diffuse ISM is, therefore, primarily driven by gas pressure and, thus, by disalignment, while the alignment capacity of RATs is almost constant. The anisotropy of the radiation field γ , or the cosine of the angle ϑ between the radiation field anisotropy and the magnetic field only act as secondary factors, which are not able to produce any significant patterns in the correlation of a_{align} with N_{H} .

5.3. Statistical analysis of dust polarization maps

In Fig. 10 we show the resulting polarization maps for the ISRF setup with RAT alignment, and for the FIXED alignment setup. The general polarization pattern resembles the maps presented in Planck Collaboration Int. XX (2015), with peak values about 10% lower. The cases of RAT and FIXED are almost identical, with some minor amplification in the overall magnitude of polarization fraction p in the latter case. The characteristic hallmarks of RAT alignment (angular dependency of p with the radiation and magnetic field direction as well as the increase of p with a higher radiation) do not seem to cause any signature in the polarization signal shown in Fig. 10. A comparison of the polarization vectors (rotated by 90°) with the averaged magnetic field orientation presented in Fig. 1 shows that they do not perfectly match over the entire map. This demonstrates that dust polarization patterns cannot be simply interpreted as a projection of the magnetic field direction onto a plane. Hence, quantitative interpretation requires modeling by means of RT simulations which include proper dust alignment physics.

Figure 11 shows how the polarization fraction varies with the column density in our simulation, for all LOS along the three axes of the cube. The mean trend is compared for the RAT and FIXED alignment cases. The RAT case starts to depart from the FIXED case for $N_{\text{H}} > 2 \times 10^{21} \text{ cm}^{-2}$ (or $A_{\text{V}} = 1$), predicting systematically lower polarization fractions. As discussed

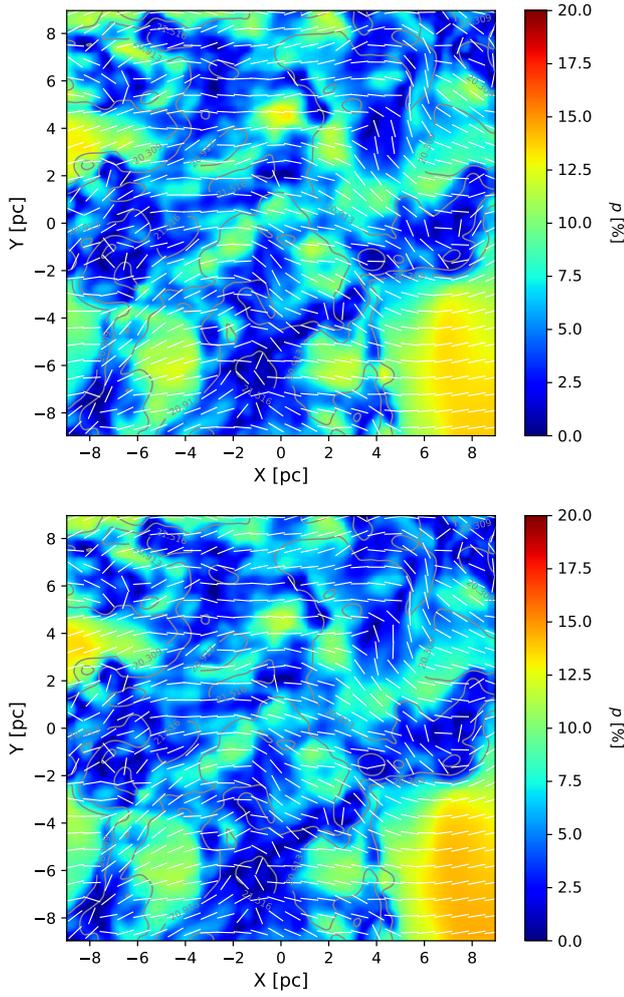


Fig. 10. Simulated maps of the polarization fraction at 353 GHz for the RAT (*top*) and FIXED (*bottom*) alignment cases. The contour lines show the column density. The white segments give the orientation of the magnetic field derived from the polarization angle.

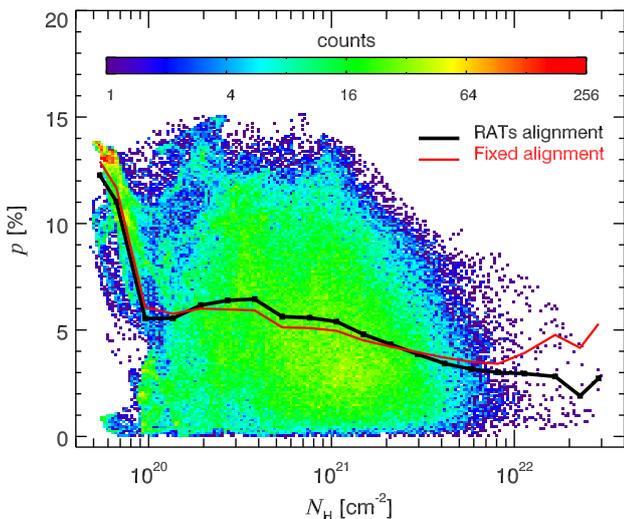


Fig. 11. Polarization fraction p at 353 GHz at 5 arcmin of resolution, as a function of the column density for the ISRF-RAT simulation. The mean trend is overplotted for RATs alignment case (black) and for the FIXED alignment case (red).

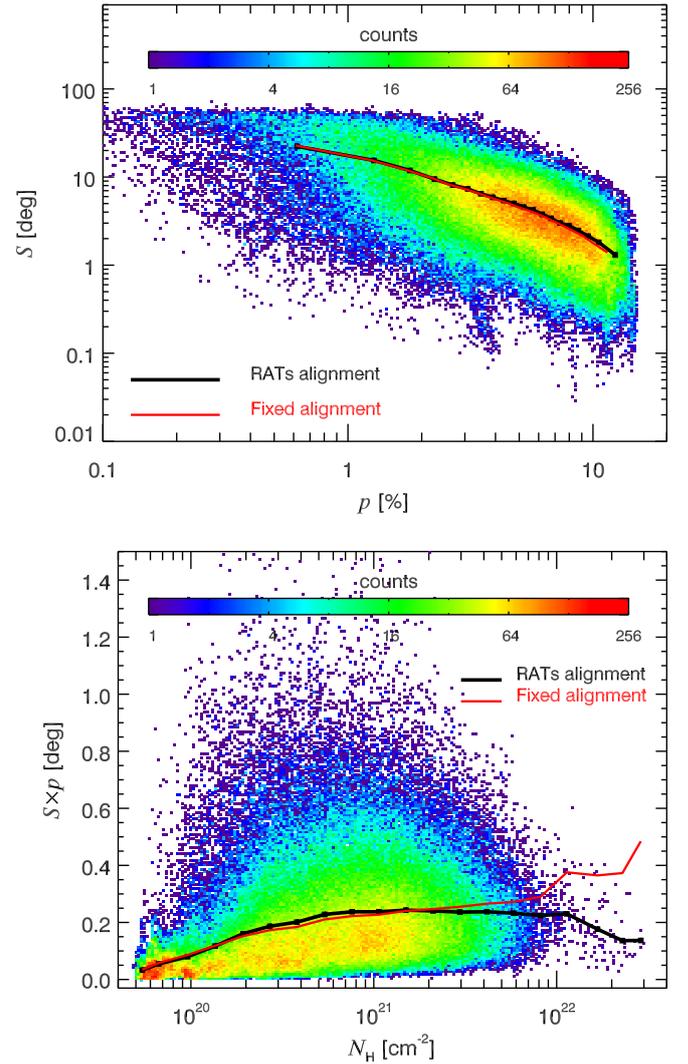


Fig. 12. *Top:* dispersion of polarization angles S as a function of the polarization fraction p all taken at 353 GHz, combining viewing angles along x , y , and z . *Bottom panel:* same for the product $S \times p$ considered as a tracer of grain alignment efficiency. Mean trends for RAT alignment (black) and FIXED alignment (red) are overlotted.

in Sect. 5.2, this is not due to dust extinction but, rather, to the higher pressure encountered in denser environments. This departure is, nonetheless, quite small given the range of column densities covered with a sufficient statistics through our simulation.

Figure 12 allows us to extend our analysis by studying the product $S \times p$ which was proposed in Planck Collaboration XII (2020), as a tracer of the grain alignment efficiency. The top panel shows that S and p are anti-correlated, whether we align grains uniformly or following the RATs model. The bottom panel, which presents the variations of the $S \times p$ product with the column density, confirms that the grain alignment predicted by RATs decreases with N_H in our simulation from $N_H = 2 \cdot 10^{21} \text{ cm}^{-2}$. The value of the mean trend of $S \times p$ is however harder to interpret. As discussed in Planck Collaboration Int. XX (2015), this particular RAMSES simulation does not reproduce perfectly the observed inverse correlation $S \propto 1/p$. As a consequence, and unlike in Planck data (see Planck Collaboration XII 2020), we do not observe a constant $S \times p$ with N_H .

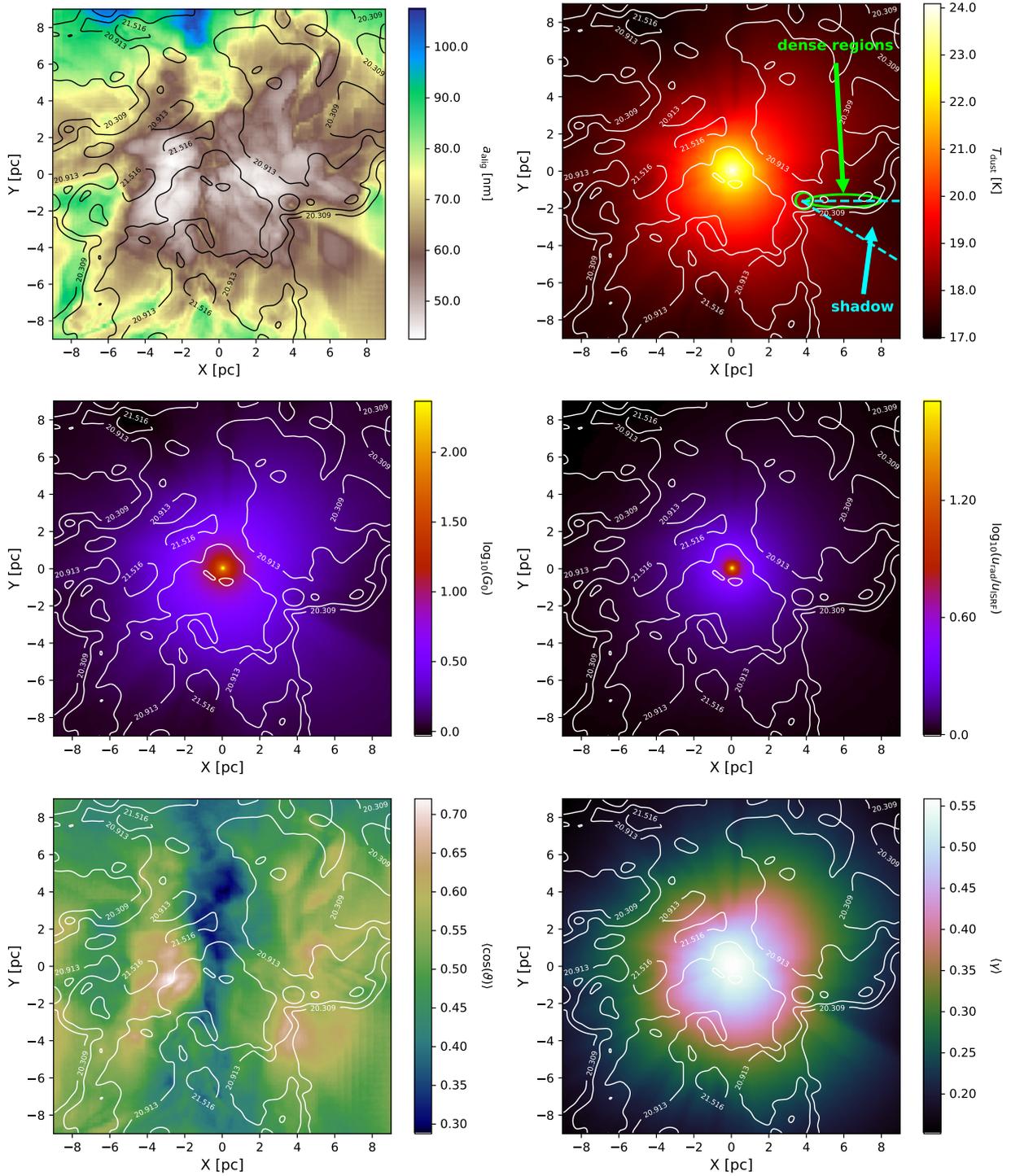


Fig. 13. Same as Fig. 5 for the STAR-RAT setup.

6. Looking for signatures of RATs

In this section, we modify the physical conditions in the cube so as to favour the observation of characteristic signatures of RATs, such as its dependence on the radiation field intensity and its angle-dependence (Lazarian & Hoang 2007a).

6.1. Results with a star at the center of the MHD simulation

In Fig. 13 we show the output of our MC simulation for the STAR setup where a star is introduced at the center of the cube

without changing the MHD simulation (see Sect. 2.3). For the STAR setup the radiation field is clearly dominated by the central star, both in magnitude and direction. Consequently, the RAT alignment is most efficient in the center of the MHD cube with a minimum of the alignment parameter a_{align} down to 45 nm, a maximum of about 250 nm and an average of 55 nm.

Here, the averaged map of a_{align} barely shows any resemblance to the gas distribution. The only exception is at $X = 4$ pc and $Y = -2$ pc where the clump with the highest density within the RAMSES simulation is situated. However, this effect is a result of the radiation from the star being shielded by the clump. Here

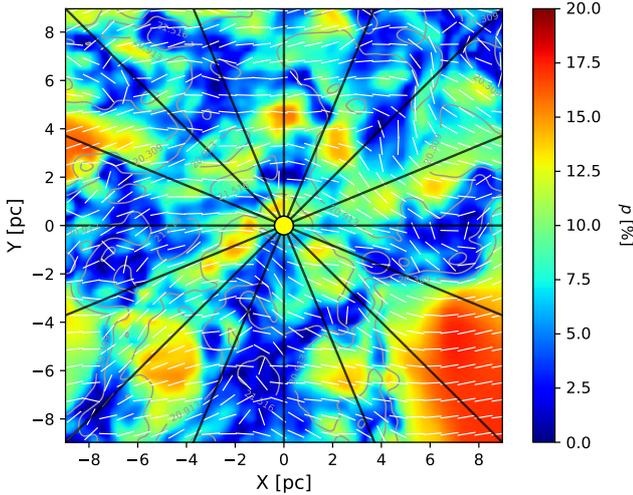


Fig. 14. Map of the polarization fraction in the STAR-RAT case, to be compared with the ISRF setup (Fig. 10, top panel). Black solid lines are the projected direction of the radiation field \mathbf{k} while the central yellow dot indicates the position of the star and the contour lines represent the column density N_{H} .

we note a lane of minimal grain alignment size starting at this clump going radially outwards. Such a shadowing effect is due to extinction of radiation in the densest regions of the cube (compare with Fig. 1).

This shadowing is even more obvious for the average dust temperature T_{dust} map of Fig. 13. Here, we highlight the densest regions and the resulting shadow by lines and arrows. As for the alignment efficiency, we report a decreased dust temperature in regions that are shielded from radiation. Several similar features can be observed e.g. directly above the star. This shadowing effect can also be seen in the maps of G_0 , u_{rad} , and $\langle \gamma \rangle$, respectively. In detail, the anisotropy factor $\langle \gamma \rangle$ reaches values up to 0.56, meaning that the radiation field has a stronger unidirectional component compared to the ISRF setup, where we have $\langle \gamma \rangle \approx 0.1$ in the center of the map. The same is true of the quantity $\langle \cos(\vartheta) \rangle$: on average the alignment angles cluster around $\vartheta \approx 60^\circ$, but the STAR setup has much smaller values of $\langle \cos(\vartheta) \rangle$ along the Y-axis through the center, where the radiation is perpendicular to the direction of the large scale magnetic field. Hence, radiation and magnetic field direction are not randomly oriented with respect to each other in that region, with an anisotropic radiation field that is much stronger at the center. This configuration of the STAR setup represents a significantly different set of parameters regarding the radiation field compared with the ISRF setup.

In Fig. 14, we show the resulting polarization maps for the STAR setup with RAT alignment. The map shows the idealized direction of the radiation field drawn on it for later analysis (see Sect. 7.2). Regarding the polarization pattern, Fig. 14 does not significantly differ from Fig. 10, or from the one presented in Planck Collaboration Int. XX (2015). We compare polarization angles pixel by pixel between all combinations of ISRF and STAR setups with RAT or FIXED alignment (see Tables 1 and 2). Despite a significant change in the radiation field and subsequent RAT alignment between all these setups, the resulting polarization angles only differ by about 2° on average. There is also no variation in p that can be attributed to the shadowing effect observed in Fig. 13. For the radiation field coming from the STAR setup the magnitude of the polarization p increases only by about 3%. However, this increase is a general

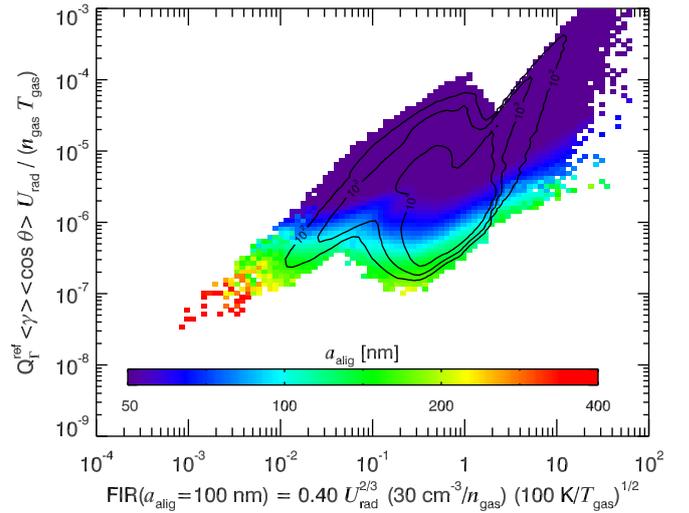


Fig. 15. Same as Fig. 6 for the STAR-RAT case.

trend throughout the p map and not only limited to the center region where the star is situated. We analyze and discuss this phenomenon in the following sections in further detail.

Figure 15, similarly to Fig. 6, illustrates how the alignment parameter a_{align} varies in the phase diagram of Fig. 7. With a star illuminating the cube, the whole physical quantities are driven toward the top right corner of the phase diagram. As a consequence, the alignment efficiency is globally increased everywhere in the cube, increasing the mean value of the polarization fraction on any LOS (Fig. 14) without modifying the patterns observed for the ISRF case (Fig. 10).

Despite the presence of a strong radiation field emitted by the star at the center of the cube, Fig. 16 show that we do not observe any systematic relation expected from the RATs theory, namely, a decrease of the polarization fraction with the distance to the star, or a sinusoidal dependence of the polarization fraction on the 2D-angle $\theta_{\text{pos}} = \angle(\mathbf{k}, \mathbf{B})$ between the projected directions of the magnetic field, \mathbf{B} (estimated from the rotated polarization vectors), and the assumed radiation field, \mathbf{k} . This is explained by two main factors. First, the physical quantities that characterize the RAT alignment, namely the intensity, the direction, and the anisotropy of the radiation field, do not vary at small scales by a factor that is strong enough to dominate over the other factors affecting the polarization fraction: the structure of the magnetic field on the line sight and within the beam, and the grain alignment randomization by gas collisions. Second, when the alignment is very efficient (as is the case when grains are irradiated by a star: $a_{\text{align}} \sim 10$ nm, see Fig. 15), strong variations in a_{align} do not produce a corresponding strong variation in the intrinsic polarization fraction of dust polarized emission because the dependence of p on a_{align} is not steep when a_{align} is small (see Fig. 4). As a consequence, p at 353 GHz does not trace the alignment efficiency very well even though the alignment is very efficient (low value of a_{align}). Figure 17 is similar to Fig. 12 and shows that the $S \times p$ barely responds to increase in the radiation field caused by the central star.

The polarization fraction does not reflect only the variations in the alignment efficiency, but also the structure of the magnetic field. Studying the statistics of $S \times p$ instead of p , we can get rid of the influence of the magnetic field structure (Planck Collaboration XII 2020). However, as presented in Fig. 16, the mean dependency of $S \times p$ with the distance and 2D-angle θ_{pos} does not show any of the expected systematic trends either.

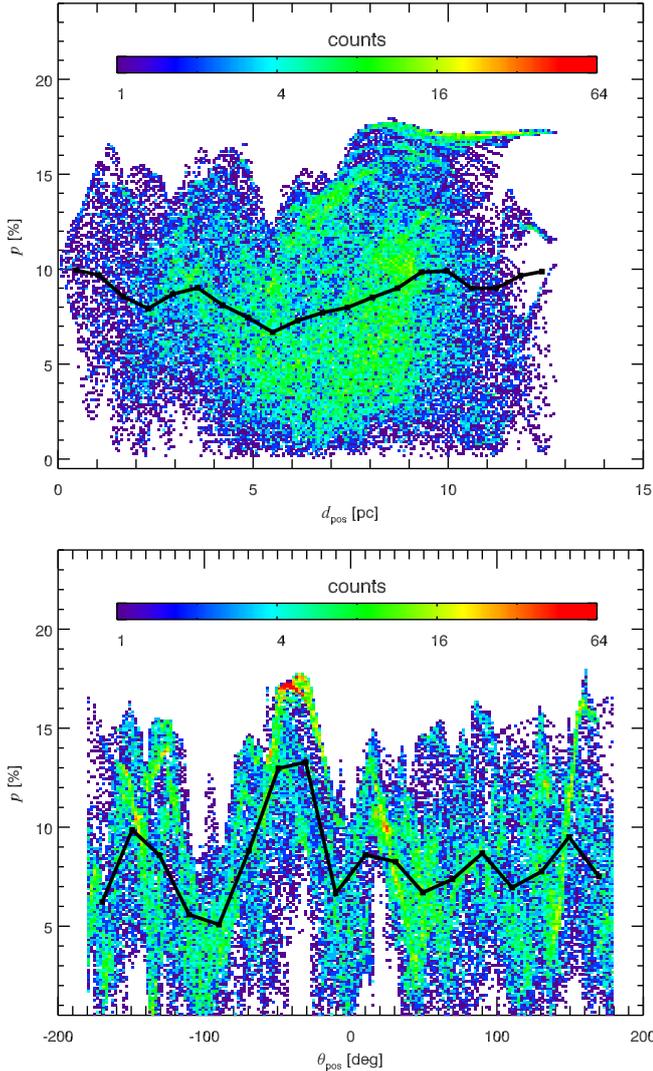


Fig. 16. Polarization fraction as a function of the distance to the star projected on the plane of the sky (*top*) and of the angle between the projected magnetic field and starlight direction (*bottom*), for the STAR-RAT setup.

We conclude that, under normal circumstances, the angle-dependence or distance-dependence of dust polarization with respect to a star is not present in simulated observations. However, this only holds true for the diffuse ISM case presented here, whereas models of molecular clouds (Bethell et al. 2007; Hoang & Lazarian 2014; Reissl et al. 2016) and circumstellar disks (Tazaki et al. 2017) do indeed reproduce the telltale signs for the presence of ongoing RAT alignment.

6.2. Optimal configuration for detecting the angle dependence of RATs

We pursue our analysis of the STAR case by studying a simple configuration where the distance and angle-dependence effect of RATs should be optimal. We run POLARIS for our RAMSES simulation, with a star at the center still, but with the magnetic field from the RAMSES simulation replaced by a magnetic field direction everywhere uniform in the X direction in the plane of the sky.

Figure 18 presents the resulting maps of a_{align} , anisotropy $\langle \gamma \rangle$, and polarization p . Comparing these maps to those of the

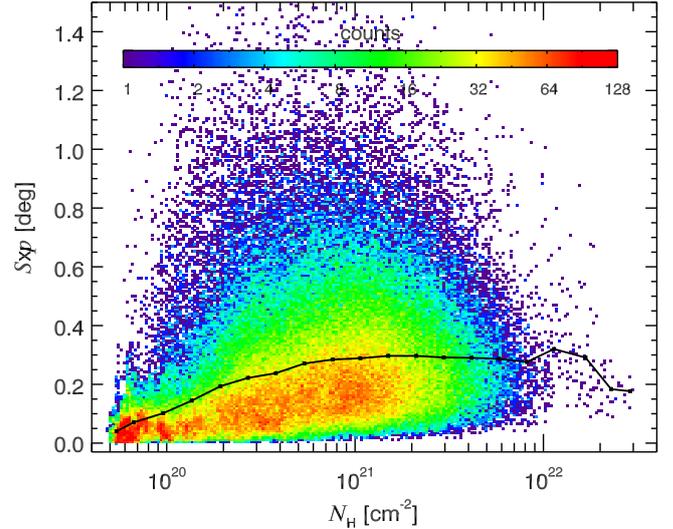


Fig. 17. Same as the bottom panel of Fig. 12 but for the STAR-RAT case.

ISRF-RAT setup and the STAR-RAT setup presented in Figs. 5 and 13, respectively, the dust grains along $X = 0$ pc become severely depolarized with alignment radii $a_{\text{align}} \gtrsim 100$ nm while we find $a_{\text{align}} \lesssim 90$ nm for the rest of the map. Yet again, we observe the characteristic shadowing effect at $X = 4$ pc and $Y = -2$ pc caused by the densest clump in the RAMSES simulation (see Fig. 1). The average angle between the direction of radiation and magnetic field orientation $\langle \gamma \rangle$, is also characteristic of RAT alignment with lower values along the line $X = 0$ pc. However, this influence is less obvious in the map of p which results from physical quantities integrated along the LOS and is also dependent on other quantities, such as the magnetic field orientation (see Appendix A). Overall, the magnitude of p in Fig. 18 shows less variations compared to those of in Figs. 5 and 13. This demonstrates that a good part of depolarization is a result of the turbulent component of the magnetic field and not grain alignment physics itself. This finding is also consistent with the interpretation of synthetic dust polarization maps presented in Seifried et al. (2019).

The dependence of p on the distance and on the angle θ_{pos} , presented in Fig. 19, do indeed present small trends expected from RATs. However, the decrease of p with the distance, as well as its sinusoidal modulation by θ_{pos} , are so small (by 1 and 2%, respectively), so that they would most probably not be observable once noise and background contamination are added, even in this optimal configuration of the magnetic field.

7. Discussion

In this section, we discuss the implications and limits of our model as well as the observational possibilities of testing alignment theories.

7.1. Impact of the fitted size distributions on our results

In Sect. 3.3, we mentioned that our simple oblate² grain shape and size distributions (power-laws) do not allow for a precise

² Using prolate grains instead of oblate grains imposes to compute the grain optical properties integrated over the grain spinning dynamics (see Guillet et al. 2018, for a detailed description).

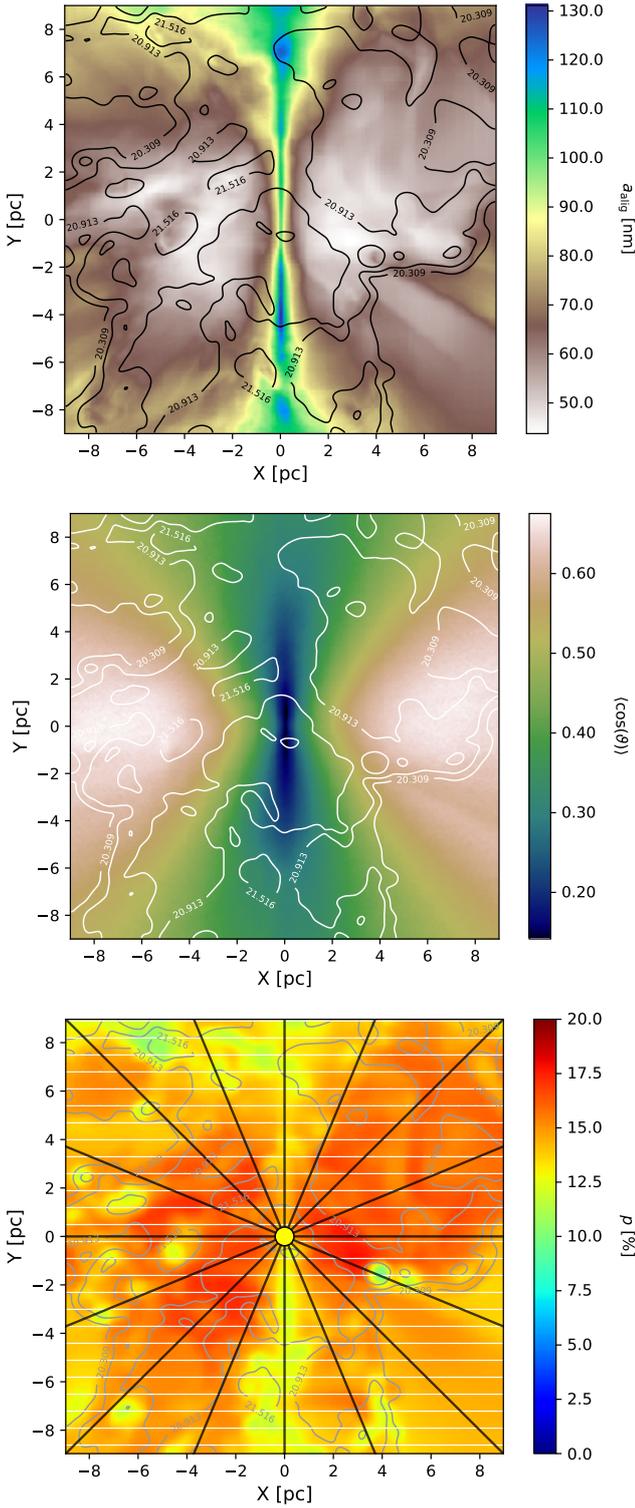


Fig. 18. Same case as the STAR-RAT setup, but with a uniform magnetic field along the X direction. *Top panel:* projected alignment radius a_{align} . *Middle panel:* projected average angle ($\cos \theta$). *Bottom panel:* linear polarization fraction overlaid with polarization vectors (white) rotated by 90° tracing the magnetic field orientation \mathbf{B} .

fit to the polarization and extinction curves (see Figs. 2 and 3). Let us first discuss the NIR extinction, which is not well reproduced by our dust model for $\lambda > 1.5 \mu\text{m}$. According to Fig. 3, we systematically underestimate the NIR extinction by a factor ~ 2 . With the same figure, we see that NIR extinction is significant ($\tau \geq 1$) only for column densities higher than 10^{22}cm^{-2}

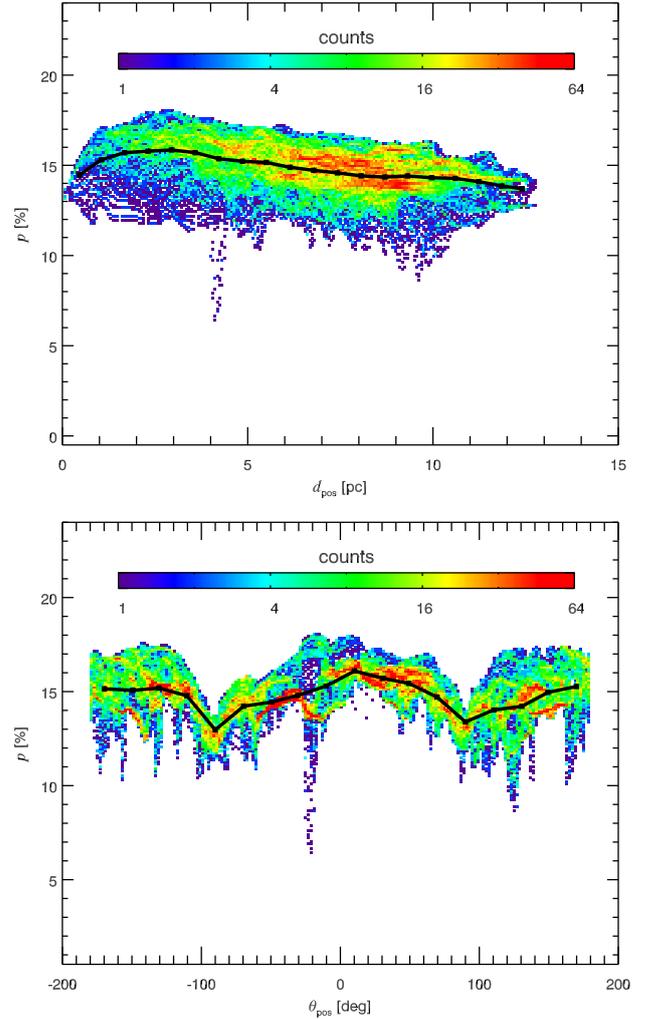


Fig. 19. Polarization fraction p as a function of the distance in the plane of the sky (*top*) and as a function of the projected angle θ_{pos} between the magnetic field and starlight (*bottom*), for the STAR-RAT case with a uniform magnetic field in the plane of the sky. The image corresponds to Fig. 18 and is to be compared with Fig. 16.

at $\lambda = 2 \mu\text{m}$, and higher than $5 \times 10^{22} \text{cm}^{-2}$ at $\lambda = 4 \mu\text{m}$. For these LOS, our calculations overestimate the number of NIR photons that are present. Our model tends, therefore, to overestimate grain alignment at the highest column densities, in the densest clumps of our simulation, which are rare. Second, we inferred a maximal size $a_{\text{max}}^{\text{S}} = 400 \text{nm}$ for the silicate distribution from a fit of the polarization curve, particularly its NIR part. A lower (resp., higher) value for $a_{\text{max}}^{\text{S}}$ would have increased (resp. decreased) the mass of dust grains above the mean alignment radius a_{align} in the diffuse ISM, which is of the order of 100nm . As a consequence, a loss of alignment would have had more (resp., less) impact on the local polarization fraction, that is, the relation between p and a_{align} would have been steeper (resp. less steep) than described in Fig. 4. All in all, our model may slightly overestimate the alignment of grains by RATs and it certainly does not underestimate it.

7.2. Can the angle-dependence of the RATs alignment efficiency be tested observationally?

Section 6 has demonstrated that one of the characteristic effects expected from the RATs theory, namely the angle-dependence

of the grain alignment efficiency, is too weak to be observed in realistic conditions. However, [Vaillancourt & Andersson \(2015\)](#) claimed to detect this effect, analyzing polarization data for the OMC-1 ridge with a star at its center: the IRC2 source. Their Fig. 2, which shows how the polarization fraction varies with the angle θ_{pos} , indeed exhibits a sinusoidal variation that looks like what we expect from the RATs theory.

We propose an alternative explanation for these observations. It was established long ago that the maximal polarization fraction, whether in extinction or in emission, tends to systematically decrease with the column density (e.g., [Jones 1989](#)). The origin for this effect, whether it is due to the magnetic field tangling or to a drop in the alignment efficiency, is still under debate and depends on the authors. More recently, [Planck Collaboration Int. XXXV \(2016\)](#) demonstrated a systematic variation of the orientation of the magnetic field with respect to the gas structures, from parallel in the diffuse ISM to rather perpendicular to dense filaments. Such variations were observed in almost all regions of the Gould Belt. Both of these effects, which are observed all through the ISM, are present in the OMC-1 polarization maps of [Vaillancourt & Andersson \(2015\)](#). If we combine these two effects and start our analysis at the position of the heating source IRC2, we can predict, without invoking any RAT physics, that the polarization fraction observed along the direction of the ridge is weak and corresponds to θ_{pos} close to 90° , while the polarization fraction observed perpendicular to the ridge, and therefore toward the less dense ISM, is higher and correspond to θ_{pos} closer to 0° .

We speculate that such a correlation should also be observed toward dense filaments even without embedded stars, as long as the external magnetic field is observed to be perpendicular to the filaments, as is the case for the Musca filament ([Pereyra & Magalhães 2004](#)) or for the B213 filament in Taurus ([Chapman et al. 2011](#)). In summary, the characteristic effects of RAT alignment seem to be usually too weak to be observed, and can be mimicked by other physical effects, in particular those deriving from the orientation of the magnetic field with respect to the gas filaments.

We note that there is an additional factor that needs to be taken into account for testing the RAT theory observationally. In [Hoang & Lazarian \(2016\)](#), it was demonstrated that for superparamagnetic grains of size $a > 100$ nm, the angular-dependency with ϑ may get lost entirely. The criterion for the loss of angular dependency of RAT alignment goes with $1/(n_{\text{gas}} T_{\text{gas}}^{1/2}) > C$, where C is some constant (see [Hoang & Lazarian 2016](#), for details). Hence, a dependency with ϑ can still be expected in dense molecular clouds while in the DISM it may become void. However, we already can barely report any angular-dependency in our setups ISRF-RAT as well as STAR-RAT (see Fig. 19) so that this additional criterion is of minor relevance within the scope of this paper.

In essence, to test the angle-dependency of RATs, optimal conditions, such as a uniform \mathbf{B} in the plane of the sky around a hot star and avoiding dense regions where other effects may dominate, should be applied. We also suggest to test this effect in the optical, where dust models predict steeper variations of the polarization fraction with the grain alignment efficiency (see Fig. 4).

7.3. Testing grain alignment theories in dense cores

This article aims to demonstrate that it is necessary to provide quantitative tests of the RATs theory and not only qualitative evidence, as is usually done. The dependence of the polarization

fraction on the dust properties or on the magnetic field structure is so degenerate that it is hard to disentangle the different effects at work only based on maps of the polarization fraction. In [Planck Collaboration XII \(2020\)](#), we advocated that using the statistics of the polarization angles, through the quantities \mathcal{S} and $\mathcal{S} \times p$, could be useful to that end.

In the present article, we have demonstrated that the efficiency of the radiative torques is constant in the diffuse and translucent ISM and that all variations of the alignment efficiency are solely due to variations of the disalignment by gas collisions measured by the gas pressure and not to the decrease of the radiation field intensity by dust extinction. The ISRF is dominated in energy by NIR ($\sim 1 \mu\text{m}$) photons ([Mathis et al. 1983](#), their Fig. 1). Comparing Eqs. (19) with (13), in particular its factor of $\lambda \times u_\lambda$, shows that it is the total number of photons, not their total energy, that is involved in grain alignment by RATs. The UV photons are unimportant for RAT alignment in the diffuse ISM, both in energy and – even more so – in number. As a consequence, the efficiency of the aligning torque is expected to be rather constant under the ISRF radiation field as long as extinction in the NIR is not important. This could justify why no dependence of alignment on the grain temperature could be found in *Planck* diffuse ISM data ([Planck Collaboration Int. XIX 2015](#); [Planck Collaboration XII 2020](#)). On the contrary, the disaligning torques exerted by gas collisions vary a great deal through the diffuse and translucent ISM, because of pressure variations. In particular, the pressure increases by orders of magnitude between the diffuse and dense ISM, as soon as the gas temperature gets stabilized around a few tens of Kelvin. This dimension is underestimated when one interprets the difference in the polarization patterns in distinct environments through the prism of the radiation field alone.

To test the decrease of RAT efficiency, we therefore need to move to very dense environments where extinction in the NIR starts to be significant ($N_{\text{H}} \gg 10^{22} \text{ cm}^{-2}$). The key issue that remains is explaining the level of polarization observed in dense cores, where we expect a huge increase in pressure combined with a severe drop in the RAT efficiency due to extinction of optical and NIR photons which are driving the grain alignment. Such data analysis is not possible with the five arcmin resolution of *Planck*, but it is accessible to the new generation of polarization instruments working at subarcmin resolutions, such as JCMT/SCUBA-2/POL-2 ([Holland et al. 2013](#)), SOFIA/HAWC+ ([Dowell et al. 2010](#); [Harper et al. 2018](#)), or NIKA2 ([Monfardini et al. 2011, 2014](#); [Calvo et al. 2016](#)). Maintaining a high level of grain alignment by RATs in cores requires a significant grain growth (e.g., [Pelkonen et al. 2009](#)). This hypothesis, which is indeed reasonable, ignores, however, the fact that grain growth automatically changes both the grains' shapes and optical properties and, therefore, their polarization capabilities. Altogether, modeling such scenarios requires that we further build on our understanding of grain alignment physics and dust evolution (in particular grain-grain coagulation), and a comparison of observations with numerical results obtained with MHD simulations and tools such as POLARIS.

In this paper, we focus on the spin-up of dust grains by RATs. Alternatively, irregularly-shaped dust grains may spin up by means of mechanical torques (MATs, [Hoang et al. 2018](#)). Originally, such a theory was proposed for regular grain shapes by [Gold \(1952a,b\)](#). It was later extended to a magneto-mechanical alignment theory by [Lazarian \(1995, 1997\)](#). Here, a supersonic gas-dust drift velocity is required. In principle such a drift may be driven by cloud–cloud collisions, winds (e.g., [Habing et al. 1994](#)), or MHD turbulence ([Yan & Lazarian 2003](#)).

Although cloud–cloud collisions and winds cannot account for the large scale alignment of grains, MHD turbulence seems to be ubiquitous in the ISM (Xu & Zhang 2016). However, it remains to be seen if MHD turbulence can provide a supersonic drift.

More recent studies indicate that mechanical grain alignment may be efficient for helical grains even in the case of a subsonic drift (Lazarian & Hoang 2007b; Das & Weingartner 2016; Hoang et al. 2018). In the MAT theory, the mechanical torque efficiency is proportional to the gas pressure (Das & Weingartner 2016; Hoang et al. 2018). This means that the grain alignment radius is independent of the gas pressure, therefore of the gas density, unlike that of RATs. We suggest that this property, which implies high level of grain alignment in dense cores (though not a systematically high level of polarization because of magnetic field tangling and possible dust coagulation), could be used to disentangle between alignment by RATs and alignment by MATs.

8. Summary

In this paper, we present a quantitative analysis of the impact of RAT alignment on dust polarimetry. This particular alignment theory predicts a sensitivity of the grain alignment efficiency with respect to the magnitude of the radiation field, as well as an angular dependency on the direction of the radiation with respect to the magnetic field orientation. We aim to model these dependencies for the diffuse and translucent ISM. For this, we used a MHD cube representative of the diffuse ISM simulated with the RAMSES code. We post-processed the MHD data with the RT code POLARIS to produce synthetic dust polarization observations. The latest version of the POLARIS code solves the full four Stokes parameters matrix equation of the RT problem, including RAT alignment, simultaneously. For the dust, we developed a best-fit model consisting of two populations of silicate and graphite grains following a power-law size distribution, which reproduce the mean Serkowski’s law as well as the mean extinction curve in the diffuse ISM.

We first performed Monte-Carlo dust heating and grain alignment calculations assuming a diffuse ISRF. The resulting radiation field and grain alignment efficiency is consistent with the alignment theory of RATs.

We analyze the polarization maps and reproduce the anti-correlation of polarization fraction with gas column density as well as with the angular dispersion known from *Planck* observations. However, we cannot trace any of the characteristic predictions of RAT alignment in the synthetic polarization data. Our scientific findings are summarized as follows:

- (i) Correlating the different parameters relevant for RATs reveals that the grain alignment efficiency in the diffuse and translucent ISM is primarily driven by the gas pressure (which tends to disalign grains and varies by orders of magnitude through the ISM) and not by the radiation field intensity (which varies only moderately in the diffuse and translucent ISM).
- (ii) Anisotropy $\langle \gamma \rangle$ of the radiation field and its orientation $\langle \cos(\theta) \rangle$ with respect to the magnetic field only have a minor effect on grain alignment in the diffuse ISM.
- (iii) Despite the local drop of grain alignment in denser regions due to the increase in the gas pressure, the RATs alignment mechanism leaves no trace in the anti-correlation of gas column density N_{H} with polarization fraction p ; nor in the anti-correlation of the angular dispersion \mathcal{S} with p the possible signposts of RATs being washed out by LOS integration

and variations of the magnetic field structure on the LOS and within the beam.

We then considered a second setup to investigate the RAT alignment behavior for different variations of the radiation field, by placing a B-type star in the very center of the RAMSES MHD cube in addition to the ISRF, and repeating our RT simulations. We find that grain alignment efficiency is highest in close proximity of the star in concordance with RAT theory. Our findings in that case comprise the following:

- (i) Even under optimal conditions, fingerprints of RATs would be barely observable. In particular, the predicted dependency of grain alignment by RATs with the angle between the radiation field and the magnetic field direction would not be detectable by observations of dust emission.
- (ii) Even close to a star, the variations in the magnetic structure along the LOS and within the beam are much more important for dust polarization than the variation in the characteristics of the radiation field.

Altogether, our modeling of synthetic dust polarization observations indicates that the effects of RAT alignment are barely detectable in the diffuse and translucent ISM, but are predicted to be stronger in the optical (i.e., on starlight polarization) than in submillimetre polarized emission.

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Appendix A: Radiative transfer of polarized radiation with POLARIS

Performing RT simulations with the full Stokes vector transforms the RT problem into a matrix equation (Martin 1974; Lee & Draine 1985; Whitney & Wolff 2002). Rotating the reference frame of the polarized light from the lab frame into the frame of the dust grain by a matrix $\hat{R}(\varphi)$ allows to eliminate some of the transfer coefficients (Mishchenko 1991). It follows from the Stokes vector formalism for the rotation matrix

$$\hat{R}(\varphi) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(2\phi) & -\sin(2\phi) & 0 \\ 0 & \sin(2\phi) & \cos(2\phi) & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \quad (\text{A.1})$$

where the angle ϕ is defined to be between the coordinate system of the Stokes vector and the magnetic field direction (see Reissl et al. 2016, for details). The full RT equation along a path element $d\ell$ of the LOS reads then:

$$\frac{d}{d\ell} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} = - \begin{pmatrix} k_I & k_Q & 0 & 0 \\ k_Q & k_I & 0 & 0 \\ 0 & 0 & k_I & -k_V \\ 0 & 0 & k_V & k_I \end{pmatrix} \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} + \begin{pmatrix} j_I \\ j_Q \\ 0 \\ 0 \end{pmatrix}. \quad (\text{A.2})$$

Here, k_I , k_Q , and k_V are the transfer coefficients associated to extinction, linear, and circular polarization while j_I and j_Q are the coefficients of total and polarized emission, respectively. We note that the emission coefficient for the Stokes U parameter is zero here. The polarization by emission of the Stokes U comes with the back rotation $\hat{R}(-\phi)$ into lab frame. The POLARIS code deals with Eq. (A.2) by applying the Runge-Kutta-Fehlberg (RKF45) solver. This solver selects the step size $d\ell$ variably by comparing the fourth order solution to the fifth order solution. This ensures that the maximal error in each integration step for each of the Stokes parameters is kept below a certain error level. In POLARIS this allowed error level is defined to be $\leq 10^{-6}$ by default.

The RT coefficients are dependent on the dust cross sections in extinction C_{ext} , absorption C_{abs} , and circular polarization C_{circ} . The cross sections are in turn dependent on grain material, wavelength, grain size, and shape. Dealing with oblate dust grains is sufficient to calculate the cross sections C_{\parallel} and C_{\perp} parallel and perpendicular, respectively, to the minor principle axis a_{\parallel} . We define the radiation to propagate along the Z axis whereas the state of polarization is determined with respect to the $X - Y$ plane, perpendicular to Z . In this reference frame the radiation experiences an extinction cross section

$$C_{\text{ext},X}(a) = \langle C_{\text{ext}}(a) \rangle + \frac{1}{3}R(a) \times (C_{\text{ext},\parallel}(a) - C_{\text{ext},\perp}(a)) \quad (\text{A.3})$$

along the X axis and an extinction cross section,

$$C_{\text{ext},Y}(a) = \langle C_{\text{ext}}(a) \rangle + \frac{1}{3}R(a) \times (C_{\text{ext},\parallel}(a) - C_{\text{ext},\perp}(a)) (1 - 3 \sin^2(\vartheta)), \quad (\text{A.4})$$

along the Y axis, corrected for grain orientation and grain incomplete alignment with the magnetic field direction. Here, ϑ is defined to be between the LOS and the magnetic field direction and R is the Rayleigh reduction factor (see Sect. 4). The quantity

$$\langle C_{\text{ext}}(a) \rangle = \frac{1}{3} (2C_{\text{ext},\parallel}(a) + C_{\text{ext},\perp}(a)), \quad (\text{A.5})$$

denotes the cross section of a randomized oblate dust grain. In this paper we perform the RT simulations with size-averaged cross sections for different materials (marked by the index i) for extinction

$$\bar{C}_{i,\text{ext}} = \int_{a_{\text{min}}}^{a_{\text{max}}} N(a) (C_{i,\text{ext},X}(a) + C_{i,\text{ext},Y}(a)) da \quad (\text{A.6})$$

and

$$\Delta \bar{C}_{i,\text{ext}} = \int_{a_{\text{min}}}^{a_{\text{max}}} N(a) (C_{i,\text{ext},X}(a) - C_{i,\text{ext},Y}(a)) da, \quad (\text{A.7})$$

weighted by the size distribution function $N(a)$ (see Sect. 3). The same geometrical considerations apply also for the cross sections of absorption $\bar{C}_{i,\text{abs}}$ and $\Delta \bar{C}_{i,\text{abs}}$, respectively, as well as for circular polarization $\Delta \bar{C}_{i,\text{circ}}$. Consequently, the total RT coefficient of extinction reads

$$k_I = \frac{1}{2} \sum_{i=1}^2 n_{i,\text{dust}} \bar{C}_{i,\text{ext}} \quad (\text{A.8})$$

and the coefficient of linear polarization by extinction is defined by

$$k_Q = \sum_{i=1}^2 n_{i,\text{dust}} \Delta \bar{C}_{i,\text{ext}}, \quad (\text{A.9})$$

where the sum accounts for the distinct cross sections and number densities for silicate and graphite grains, respectively. An already polarized radiation may also accumulate a small amount of circular polarization due to the differential phase lag along the distinct grain axes leading to a transfer coefficient of:

$$k_V = \sum_{i=1}^2 n_{i,\text{dust}} \Delta \bar{C}_{i,\text{circ}}. \quad (\text{A.10})$$

For the RT coefficient of emission, we also account for individual dust temperatures for each of the grain materials. Assuming the dust grain to be in equilibrium with its environment leads to the following emission coefficients

$$j_I = \frac{1}{2} \sum_{i=1}^2 n_{i,\text{dust}} B_{\lambda}(T_{i,\text{dust}}) \bar{C}_{i,\text{abs}}, \quad (\text{A.11})$$

and

$$j_Q = \sum_{i=1}^2 n_{i,\text{dust}} B_{\lambda}(T_{i,\text{dust}}) \Delta \bar{C}_{i,\text{abs}}. \quad (\text{A.12})$$

Appendix B: Monte-Carlo noise estimation

Due to its stochastic nature, a certain amount of noise is the inevitable drawback in MC RT simulations. In this section we quantify the noise in the MC runs for dust heating and grain alignment. The MC noise depends on the number of applied photons and the quality of the random number generator. In POLARIS we implemented the random number generator scheme KISS (Marsaglia & Zaman 1993; Marsaglia 2003) with a period of roughly 10^{75} . We repeated the MC runs as outlined in Sect. 2.3 with ten different random seeds. From these runs, we calculated the average $\langle E \rangle$ for each of the grid cells where E can stand

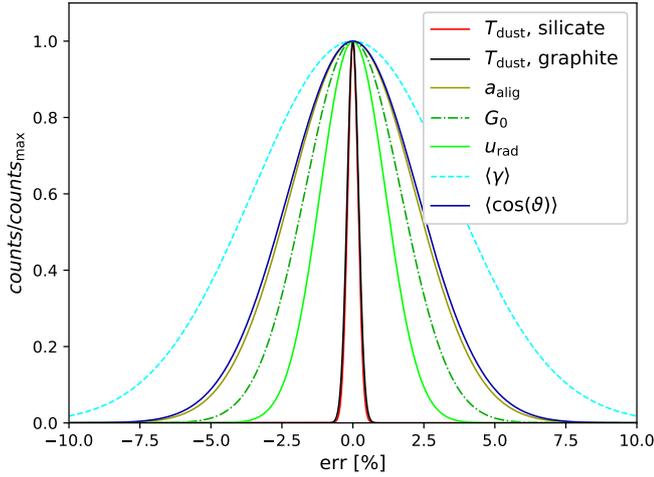


Fig. B.1. Histogram of the MC error distribution.

Table B.1. Mean values and standard deviations (STD) of the MC noise for the different parameters derived MC RT simulations.

Parameter	Mean [%]	STD [%]
$T_{\text{dust, silicate}}$	-6.33×10^{-6}	0.18
$T_{\text{dust, graphite}}$	-8.44×10^{-7}	0.20
a_{align}	5.43×10^{-5}	2.18
G_0	-9.07×10^{-5}	1.69
u_{rad}	1.07×10^{-6}	1.15
$\langle \gamma \rangle$	-7.22×10^{-5}	3.53
$\langle \cos(\vartheta) \rangle$	-5.65×10^{-5}	2.27

for each of the quantities T_{dust} , a_{align} , G_0 , u_{rad} , $\langle \gamma \rangle$, and $\langle \cos(\vartheta) \rangle$ derived from the POLARIS MC run. Consequently, $\langle E \rangle$ provides a noise reduced baseline for the error estimation. We use an error based on the quantity E per run and grid cell with respect to the average over all ten runs defined as

$$\text{err} = (E - \langle E \rangle) / \langle E \rangle. \quad (\text{B.1})$$

In Fig. B.1 we show the distribution of deviations from the average as a measurement of the MC noise and the corresponding mean values and the standard deviations (STD) are listed in Table B.1. The dust temperatures are the least affected by the MC noise with a mean close to zero and a STD less than a quarter of a percent. However, even the anisotropy factor $\langle \gamma \rangle$, although it is the quantity most affected by MC noise, barely exceeds a STD of 3.5%. The subsequent ray-tracing scheme of POLARIS has an excellent signal to noise ratio. Thus, we estimate the maximal numerical error to be not larger than 3.6% for the entire POLARIS RT pipeline and subsequent polarization maps presented in this paper.

Appendix C: Histograms of Monte-Carlo quantities

In this section, we briefly present the 3D distributions of the physical quantities derived with our POLARIS MC simulations.

C.1. The radiation field

In Fig. C.1, we show the histograms of the 3D distributions of different quantities. The average angle $\langle \cos(\vartheta) \rangle$ for both the

ISRF and STAR cases shows a similar distribution as the projected images (see Sects. 5.1 and 6). The average values for ISRF, STAR, as well as the case with no dust at all in the cube, are almost identical at 0.5, indicating a large degree of random orientation between radiation field and magnetic field direction. The distributions in the ISRF and “no dust” cases are almost the same, while values down to zero and up to unity for the STAR case and the regions surrounding the central star are present.

The anisotropy factor $\langle \gamma \rangle$ clusters around mean values of 0.09 and 0.27 for the ISRF and the STAR setups, respectively. However, the “no dust” case does not reach lower values than 0.04 with an average of about 0.05. As outlined in Sect. 2.3, we inject photons with random directions into the grid to mimic a completely isotropic ISRF. Hence, one could expect a value of 0.0 for this case, indicating a minor numerical bias in the MC method.

The magnitude of the radiation field quantified by G_0 and u_{rad} peaks around unity for the “no dust” case, whereas the ISRF setup reaches unity only at the very borders of the grid. For the STAR case we find the radiation field on average to be increased by roughly a factor of two with peak values up to 100 times larger than the $G_0 = 1$ ISRF, close to the star.

C.2. Dust temperatures and characteristic grain alignment radii

In Fig. C.2, we show the histograms of dust temperatures and grain alignment radii. For the ISRF case, the dust temperatures for silicate and graphite reach mean values of 15 and 18 K, respectively. For the STAR case we get mean temperatures of about 17 K for silicates and 18 K for graphite, while we report temperatures up to 118 K for a few grid cells in close proximity to the star.

For silicates, the mean values of the alignment radius are $a_{\text{align}} = 68$ nm for the STAR setup and $a_{\text{align}} = 114$ nm for the ISRF setup. Only a marginal amount of all grid cells reaches the upper grain size of $a_{\text{amax}}^{\text{S}} = 400$ nm. Furthermore, the Larmor limit (see Eq. (22)) is $a_{\text{larm}} \gg a_{\text{amax}}^{\text{S}}$ and is therefore not shown in Fig. C.2. Consequently, the window $a_{\text{align}} < a < a_{\text{larm}}$ of stable RAT alignment with the magnetic field direction (see also Eq. (23)) falls within the size range of silicate grains. Hence, all cells of the MHD grid do contribute to dust polarization.

In this paper we assume that graphite grains are completely randomized, independently of local conditions. In Fig. C.2 we show also the radius a_{align} of graphite. For these grains, the mean values of the alignment radius are $a_{\text{align}} = 71$ nm for the STAR setup and $a_{\text{align}} = 120$ nm for the ISRF setup. However, we find the condition $a_{\text{align}} < a_{\text{amax}}^{\text{G}}$ to be fulfilled for some rare cases in the MHD grid. Hence, a marginal amount of graphite grains can in principle spin-up to a stable alignment. Moreover, the Larmor limit a_{larm} is of the same order as the graphite size range. Thus, we note that the condition $a < a_{\text{larm}}$ is breached for a small size range of the parameter set provided by the RAMSES simulation.

Indeed, we report that graphite grains may possibly align within a small range of grain sizes for about 0.7% of all cells for the ISRF setup and 2.0% for the STAR setup. For the ISRF, an alignment with the magnetic field is possible, in principle, for some regions of the diffuse ISM. However, these regions are sparsely distributed over the entire grid and should not influence the polarization pattern in a detectable way. For the STAR setup, the regions of possible graphite alignment are clustered around the very position of the central star. Hence, graphite might also trace the magnetic field in close proximity

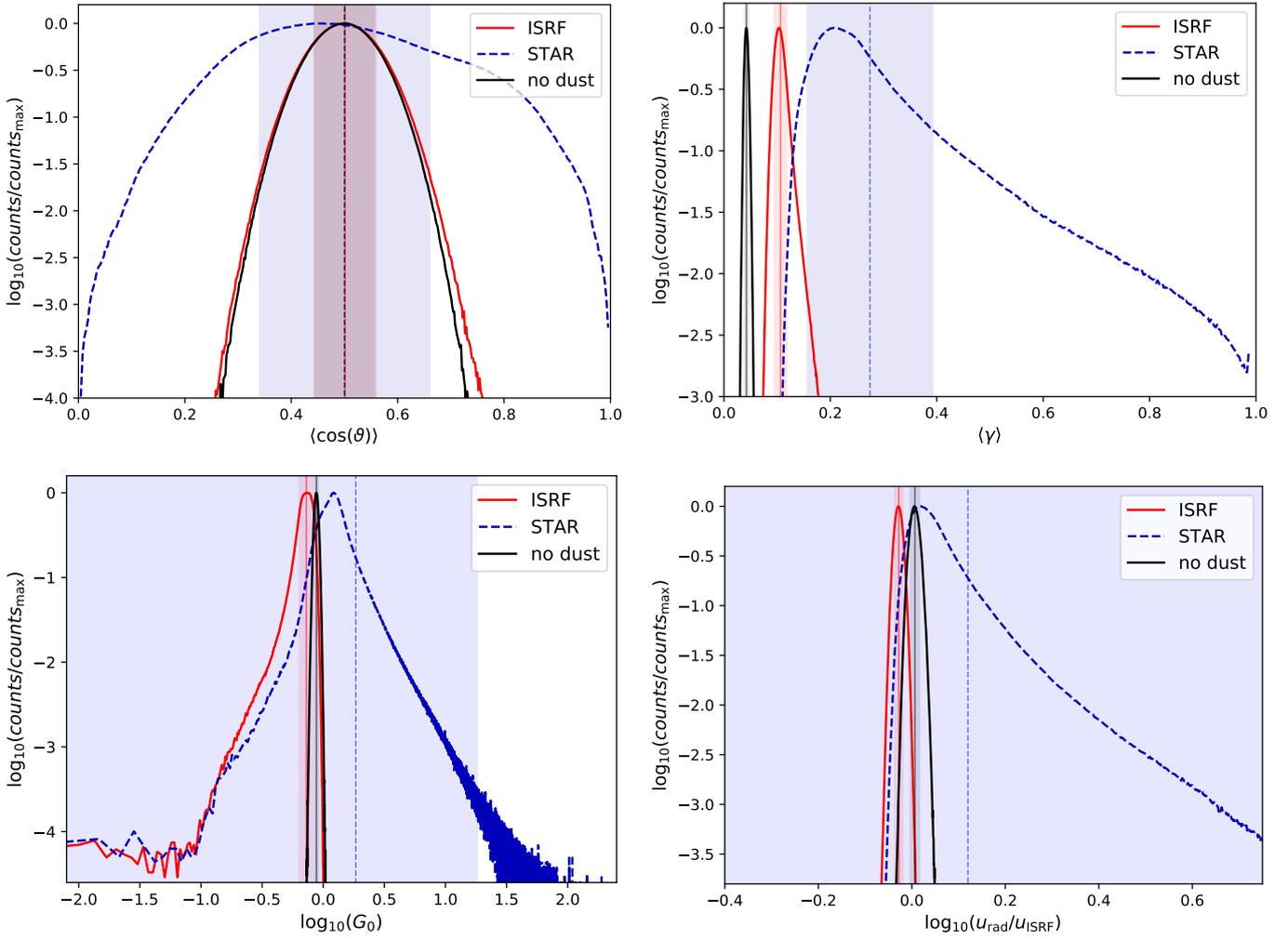


Fig. C.1. Histograms considering all cells within the RAMSES cube for the setups ISRF and STAR, respectively, as well as a test run with the ISRF and no dust. The individual panels are the average angle $\langle \cos(\vartheta) \rangle$ between magnetic field direction and radiation field (*upper left*) and the anisotropy factor $\langle \gamma \rangle$ (*upper right*), G_0 (*bottom left*), and the average energy density, u_{rad} , of the radiation field (*bottom right*). All histograms are normalized to their respective peak values. Vertical lines and bars represent the corresponding mean values and the standard deviations, respectively.

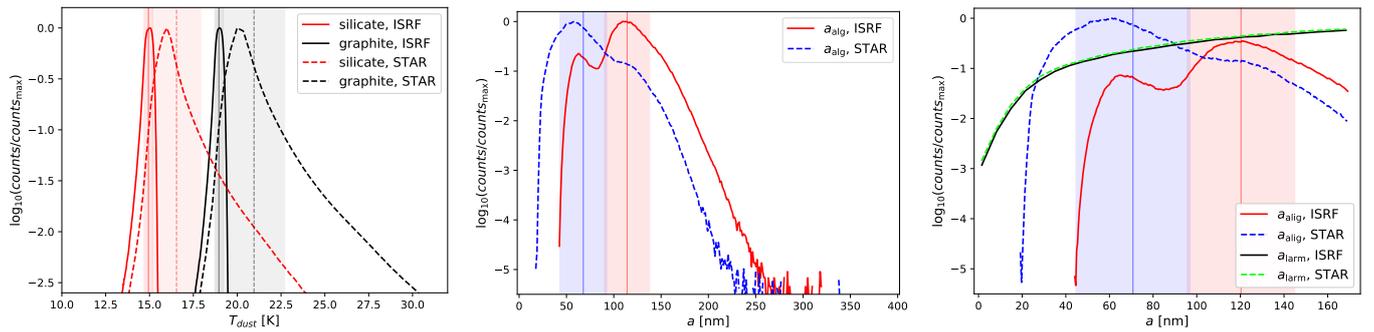


Fig. C.2. Same as Fig. C.1. *Left panel:* individual dust temperatures T_{dust} of silicate and graphite grains for the setups ISRF and STAR, respectively. *Center panel:* alignment radius a_{align} for silicate grains. The Larmor limit is not plotted because $a_{\text{larm}} \gg 400$ nm. *Right panel:* distribution of the radii a_{align} and a_{larm} for graphite grains.

to the star. A second possibility is the alignment of graphite with the radiation field. Pure graphite grains as well graphite-silicate composites may align with the predominant direction of the radiation field (Lazarian & Hoang 2007a, 2019) for a distance that is several AU away from the star. However, this distance is much smaller than the resolution of the RAMSES

simulation. Furthermore, charged dust grains may be randomized while drifting with respect to the magnetic field. This effect affects carbonaceous grains more than silicate grains (Weingartner 2006). Overall, the assumption that graphite grains do not align at all remains justified within the scope of this paper.