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Maulik K Patel, Kurt E Sickafus, Gianguido Baldinozzi. Divergent short-and long-range behavior in ion-irradiated  $\delta$ -Sc<sub>4</sub> Hf<sub>3</sub> O<sub>12</sub>. Physical Review Materials, 2020, 10.1103/PhysRevMaterials.4.093605 . hal-02939779

**HAL Id: hal-02939779**

**<https://hal.science/hal-02939779>**

Submitted on 15 Sep 2020

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# Divergent short and long-range behaviour in ion-irradiated $\delta$ -Sc<sub>4</sub>Hf<sub>3</sub>O<sub>12</sub>

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Ion irradiation experiments and quantitative x-ray diffraction analysis were used to demonstrate that the lattice and structure behave very differently in a complex oxide,  $\delta$ -Sc<sub>4</sub>Hf<sub>3</sub>O<sub>12</sub>, under irradiation. Analysis of the structure reveals that with increasing fluence, the characteristic  $c/a$  ratio for  $\delta$ -phase converges to that of an ideal fluorite phase, whereas locally it produces a metaphase consisting of frozen nanoscale structures having bixbyite-like flavor that increase the overall stability and radiation response of the apparent long-range oxygen-deficient average fluorite structure.

## I. INTRODUCTION

Non-stoichiometric fluorite-related oxides are model systems to address fundamental questions in inorganic compounds, and in particular the mechanisms of solid state reactions and transformations in solids. Systematic analysis of the thermodynamic properties of heterogeneous equilibria shows that singularities of the physical properties (melting point, conductivity, thermoelectricity, etc) do not necessarily occur for compositions with simple rational ratios. Wagner and Schottky [1] discussed the statistical thermodynamics of real compounds and proved the stoichiometry of ideal crystals has no special position, though the extent to which different substances may display a departure from stoichiometry depends on specific characteristics like the energies of lattice disorder and charge transfer. Oxygen deficient fluorites are grossly non-stoichiometric compounds and lattice energy calculations can lead to the conclusion that many of the observed non-stoichiometric phases can exhibit a high degree of metastability [2]. Indeed, in these systems, short-range interactions between defects, clusters and complex atomic arrangements can be strong and they can explain the observed variety of long-range structures encountered in these compounds. The delicate balance between order, disorder, and metastability present in these systems makes them an interesting playground for studying their resilience to external perturbations, and in particular, to ion irradiation. Though the questions raised are fundamental, their impact on properties is also important. Structural stability is of particular interest in these complex oxides because these systems provide fascinating in-

sights into the behavior of advanced nuclear ceramics and the long-term behaviour of spent fuels and nuclear waste-forms. The technological interest in these oxides also spans other areas as they find applications as solid-state electrolytes in fuel cells, and have interesting features that can be exploited in the engineering of thermal barrier coatings.

As the structures disorder, they become more complicated and difficult to describe. But disorder and complexity by themselves are neither good nor bad. It is the lack of precision in their description that often prevents us from navigating and managing this complexity. A complete description of all the phenomena occurring in fluorite-related materials disordered by ion irradiation is still out-of-reach.

The study of radiation effects in fluorite compounds and in fluorite derivative phases, including pyrochlore, weberite, and bixbyite systems is not a recent trend, though it is still expanding. Pyrochlore and weberites [3] with A<sub>2</sub>B<sub>2</sub>O<sub>7</sub> generic chemical formula are perhaps the simplest and least substoichiometric compounds in the AO<sub>2-x</sub> system where there is a significant tendency for cations and anions to order. Several studies highlight the impact of the A- and B-site cation radii on the resistance to disorder or amorphisation produced by high pressure or radiation [4–10]. Bixbyite oxides (B<sub>2</sub>O<sub>3</sub>), generally consist of a single-type of rare earth cation. These systems exhibit a consistent ordering of O vacancies in their ground state. Moreover, these structures display the highest oxygen deficiency among the fluorite-related systems. While recent structural studies using diffraction techniques assess the structural changes occurring in these single-element oxides [11–13], little is structurally known about multi-cation bixbyites [14, 15].

In between these two substoichiometric compositions of the oxygen-deficient fluorite systems, another simple system that exhibits a consistent anion vacancy ordering,

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not necessarily involving cation ordering, is the  $\delta$ -phase structure. The radiation resistance of these structures has already been investigated using diffraction techniques but the details of the structural changes are not yet clear as there is no extensive and systematic study of these systems using x-ray or neutron diffraction.  $\delta$ -phases are interesting systems in the large family of oxygen deficient fluorites [16]. The  $\delta$ -phase structure consists of edge and corner-sharing oxygen octahedra and oxygen vacancies are located in the ideal fluorite anion sublattice. These vacancies are generally found to order onto specific sites of the structure, leading to the appearance of superstructure reflections in the x-ray diffraction patterns. These weak reflections are produced by the combined effect of the composition modulation and of the displacive relaxation of the metal ions surrounding the anion vacant sites. The ideal oxygen stoichiometry (O/M) in  $\delta$ -phases is close to 1.714. Direct structural determination has found that the cations order only when the stoichiometry is  $A_6^{+3}B^{+6}O_{12}$  [17, 18], whereas the cations cannot order in compounds with stoichiometry  $A_4^{+3}B_3^{+4}O_{12}$ . The common characteristic symmetry of these phases is  $R\bar{3}$ , and they typically exhibit a moderate deviation (few %) from the ideal  $c/a$  ratio 0.9258 of a cubic fluorite described in this same lattice frame.

The structural characteristics of several irradiated  $\delta$ -phases [19–26] were studied and the common conclusion was the observation of a phase transformation towards an apparent disordered fluorite phase. The most comprehensive among these studies [20, 21] also discuss the qualitative formation of a bixbyite-like phase in low-energy irradiated  $\delta$ - $Sc_4Zr_3O_{12}$ . This transformation to bixbyite was in some way a mystery since group-subgroup analysis does not allow for a direct transformation from the  $\delta$ -phase to a bixbyite. However, if one compares the polyhedral networks in these two structures, then one can find a slight similarity in the polyhedral networks. The bixbyite structure is only comprised of octahedra (slightly distorted octahedra [27]), while the  $\delta$ -phase is typically described as having 6-fold and 7-fold polyhedra. However, one of the M-O bond lengths in the 7-fold polyhedra is significantly longer such that the polyhedra resemble capped octahedra [28].

The aim of this work is not to provide a definitive blueprint for the global changes occurring in all fluorite-derived structures, but rather to offer a fresh explanation for the following phenomena: (1) the critical structural changes involved; (2) how structure supports radiation resistance; (3) how to find a balance between global long-range and diverse local structural features; and (4) how this can lead to effective engineering of fluorite-related materials. In order to establish these quantitative features, we analyze structural characteristics of a the swift heavy ion irradiated  $\delta$ -phase compound, namely  $Sc_4^{+3}Hf_3^{+4}O_{12}$  using high-resolution x-ray powder diffraction.

## II. EXPERIMENTAL PROCEDURES

Powders of scandium sesquioxide ( $Sc_2O_3$ , 99.99%) and hafnium oxide ( $HfO_2$ , 99.95%) purchased from Alfa Aesar were calcined at 700 °C and weighed to obtain a 4:3:12 stoichiometric ratio of Sc:Hf:O. The mixture was ball milled in a high energy SPEX<sup>®</sup> 8000D dual mixer/mill using zirconia ceramic vial set and two 12.7 mm zirconia ceramic balls in an isopropanol medium for 8 hours. The powder mixture was cold pressed into pellets of 13 mm in diameter and a thickness of 10 mm using a stainless steel die and plunger. The pellets were then sintered in air, first at 1200 °C for 48 hours and then again at 1600 °C for 72 hours. The heating and cooling rates during both sintering cycles were kept at 5 °C/min. Samples were ground again between the two sintering cycles. The as-synthesized pellets were close to 95% of the theoretical density and x-ray powder diffraction was performed to assess their phase purity. Qualitative analysis of the diffraction patterns showed formation of a rhombohedral  $\delta$ -phase that matched closely with structures reported in the literature [16, 29].

The rest of the pellets were used for irradiation experiments. Prior to irradiations, these pellets were cut into discs of 2 mm thickness and polished with diamond lapping films down to 1  $\mu$ m. The final polishing was performed using colloidal silica to remove residual damage due to polishing. To study the radiation response of  $\delta$ - $Sc_4Hf_3O_{12}$ , samples were irradiated at room temperature with 92 MeV  $Xe^{26+}$  ions at the IRRSUD beamline in GANIL, France, using time-integrated fluxes (fluences) ranging from  $10^{11}$  to  $10^{14}$  ions/cm<sup>2</sup>. The flux of ions during irradiation was  $10^9$  ions/cm<sup>2</sup>/s and the sample surface was kept normal to the ion beam direction. Fig. 1a shows the partitioning of energy loss for each Xe ion into nuclear and electronic stopping power components, as a function of depth in the  $\delta$ - $Sc_4Hf_3O_{12}$  target material. The integrated energy losses from electronic and nuclear components calculated from their respective stopping powers are 87.5 and 3.4 MeV. It is important to observe in Fig. 1a that electronic stopping far exceeds nuclear stopping over nearly the entire range of the Xe ions in the  $Sc_4Hf_3O_{12}$  target (at least until the depth of 7.5  $\mu$ m in the target where the ion implantation occurs).

X-ray powder diffraction measurements were performed on samples irradiated with fluences exceeding  $10^{12}$  ions/cm<sup>2</sup>, that correspond to the conditions of a uniformly irradiated surface due to multiple ion-track overlaps. Diffraction measurements were performed using a Bruker D8 Advance diffractometer equipped with a Göbel mirror for Cu  $K\alpha$  radiation and a NaI scintillation detector. Data collections were performed in a  $\theta - \theta$  geometry performing symmetric step scans of the detector and the x-ray source ( $\Delta 2\theta = 0.02^\circ$ ) with a step time of 2 sec/step.  $\delta$ - $Sc_4Hf_3O_{12}$  presents a significant advantage for the x-ray diffraction analysis compared to other compounds belonging to this same family because of the excellent scattering contrast between Sc and Hf ions.

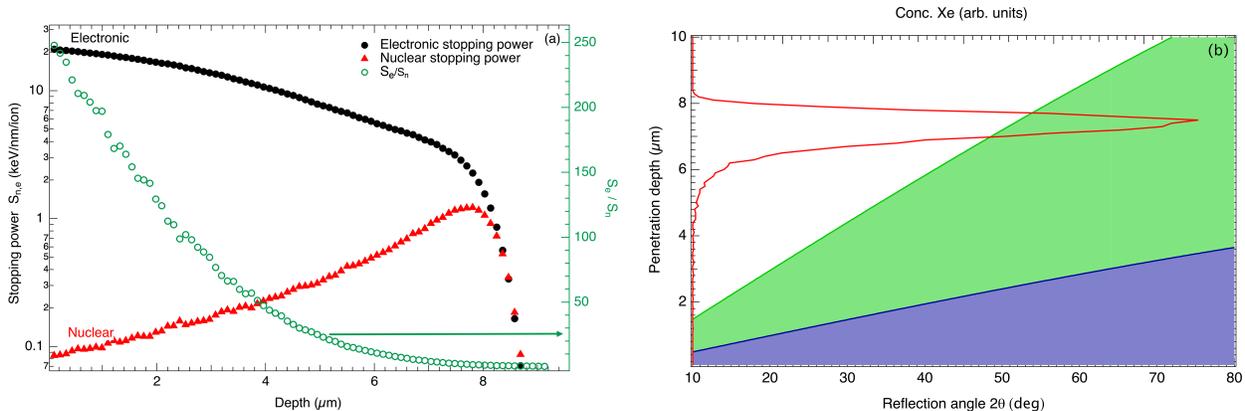


FIG. 1. (a) Electronic versus nuclear energy loss for 92 MeV Xe ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ . The abscissa indicates distance into the target, specifically distance normal to the target surface. The ordinate (longitudinal) range of the incident Xe ions is approximately  $8\mu\text{m}$ . The ordinate on the left shows incident ion energy loss (due to either electronic (black circles) or nuclear (ballistic) (red triangles) mechanisms) on the logarithmic scale, while that on the right shows the ratio of electronic to nuclear energy loss (green open circles). Calculations were performed using the so-called "quick SRIM" calculations option within the SRIM code for ion stopping in solids [30]. (b) Comparison of the penetration depth of Cu-K $\alpha$  x-rays in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  as a function of the scattering angle (blue,  $2\theta$ , bottom scale) and Xe implantation profile (red line, top scale): according to the Beer-Lambert law and for a Bragg-Brentano experiment geometry, 63.2% of the scattered signal at a given angle comes from a shallow region below the sample surface whose depth is below the blue line. The green line is intended to indicate that 95% of the signal arises from depths below this line. Below  $2\theta = 45^\circ$ , more than 95% of the scattered x-ray photons come from a region where no implantation occurs.

Fig. 1b shows the depth profile of implanted Xe ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , calculated using SRIM [30] for  $10^{14}$  ions/cm $^2$ . Based on SRIM, the projected range,  $R_p$ , of 92 MeV Xe ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  is  $8\mu\text{m}$ , with a longitudinal straggling of  $0.7\mu\text{m}$ . Fig. 1b also shows the penetration depth of Cu-K $\alpha$  x-rays in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ . The x-ray diffracted signal in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  comes from a variable penetration depth not exceeding  $5\mu\text{m}$ . Clearly, over this range in target depth, no significant Xe ion implantation occurs. In summary, Fig. 1 shows that electronic energy loss dominates significantly over nuclear energy loss for 92 MeV Xe in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , over nearly the entire range of the implanted Xe ions; additionally, x-ray diffraction measurements at low angles ( $2\theta < 45^\circ$ ) are only sensitive to electronic radiation damage effects (essentially, no nuclear radiation damage effects contribute to the measurements performed in this study). Rietveld refinements were performed using the software Jana2000 [31] and 3D structure visualization models were obtained using the software VESTA [32].

### III. LOCAL ORDER

The interaction of an impinging x-ray beam with a crystal produces a discrete set of scattered beams forming a periodic lattice of sharp reflections (Bragg reflections), the so-called reciprocal space of the crystal. Any kind of crystal imperfection (stacking faults, chemical disorder, lattice vibrations, ...) perturbing the long-range crystalline order reduces the intensity of the Bragg reflections

by a large attenuation factor. But the overall scattered intensity is conserved, and this loss of intensity of the Bragg reflections is, however, recovered under the form of a very weak and broad diffuse intensity that adds to the background and it is spread over particular positions in the reciprocal space. This broad x-ray scattering intensity is called diffuse scattering. The deviation from the perfect crystalline order can occur because of atomic displacements or related to atomic substitutions, or due to a combination of the two effects. When the diffracted beam is measured without energy resolution, it is not possible to discriminate between a dynamic origin of the diffuse scattering (lattice vibrations) or a static origin (crystal imperfections). In this setup, the diffuse scattering intensity, gives directly the instantaneous spatial correlations of the order parameter  $\xi$ :  $S(\mathbf{q}, t = 0) = |\xi_q|^2$  where  $\xi_q$  is the  $q$ -th component of the Fourier transform of a spatially-dependent atomic displacement wave or density concentration wave occurring in the crystal [33–35]. The spatial correlation length of the  $q$ -th component of the order parameter can be obtained from the breadth of the diffuse scattering within the Ornstein-Zernike formalism [36, 37]. Using a correlated microdiffraction model developed by Neder et al. [38] it is possible to model the diffuse scattering produced by correlated nanodomains introducing a difference structure where the atoms represent the difference between the average structure and the nanodomain structure. Scherrer-type peak broadening can be included in this "correlated-model" structure, and it describes the characteristic long-range correlation length of the average structure and the shorter-range av-

eraged size of the correlation domains responsible for the diffuse scattering. Eventually, a microstrain-type peak broadening can also be introduced to account for defect-induced elastic fluctuations of the lattice parameter.

#### IV. PRISTINE $\delta$ - $\text{Sc}_4\text{Hf}_3\text{O}_{12}$

The Rietveld refinement of the pristine diffraction pattern uses the prototype  $\delta$ -phase model for  $\text{A}_6\text{BO}_{12}$  [17, 18] as a starting point. In these structures, the hexavalent metal ion occupies consistently the 3a positions of the  $R\bar{3}$  space group. The trivalent metal ions occupy the 18f Wyckoff positions. O vacancies are localized at 6c positions. In  $\delta$ - $\text{Sc}_4\text{Hf}_3\text{O}_{12}$ , Sc and Hf cannot order in the same way as their relative ratio is different, and they were evenly distributed over each of these two cation sites in such a way as to maintain the 4:3 cation stoichiometry.

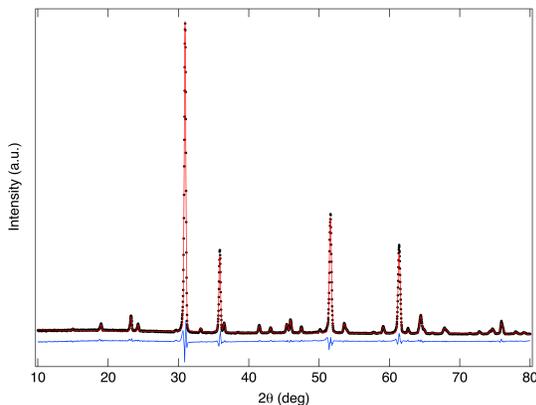


FIG. 2. Observed (black dots), calculated (red solid line) XRD pattern for pristine  $\delta$ - $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  showing a good Rietveld refined fit with the structural model shown in table I. The blue solid line indicates the difference between the observed and calculated patterns.

The refinement of this initial model against the pristine sample data allows us to check the validity of the assumption that O vacancies are confined to the 6c Wyckoff position. See Note I in supplementary material for further explanation [39]. Also, the relative occupancy of Sc and Hf was refined independently for the 3a and 18f Wyckoff positions occupied by cations. The refined and experimental patterns display a very good agreement as displayed in Fig. 2. The refined model provides the calculated stoichiometry of  $\text{Sc}_{4.01}\text{Hf}_{2.99}\text{O}_{12}$ , in excellent agreement with the desired 4:3:12 stoichiometry. The metal distributions onto the two families of metal sites are not random as initially expected: scandium ions display a mild preference for the 18f sites, while the hafnium ions display a preference for the 3a sites. The refined structural parameters are summarized in Table I. To reduce the overall number of parameters, a common isotropic thermal displacement parameter was used for all the atoms. See Note II in supplementary material for details on the model for profile

function used in the refinements [40]

TABLE I. Structural parameters of the refined  $\delta$ -phase model for ( $R\bar{3}$ ,  $a=b=9.3626(4)$ ,  $c=8.6920(7)$  Å,  $Z=3$ ).  $R_{wp}=9.64\%$ ,  $\text{GoF}=2.3$ ,  $R_B=2.4\%$ .

Site	$x$	$y$	$z$	Occ	$U_{iso}(\text{Å}^2)$
(Hf, Sc) <sub>1</sub> 3a	0	0	0	0.54(1), 0.46(1)	0.003(1)
(Hf, Sc) <sub>2</sub> 18f	0.2568(2)	0.0426(3)	0.3523(2)	0.409(8), 0.591(8)	0.003(1)
O <sub>□</sub> 6c	0	0	1/4	0	
O <sub>1</sub> 18f	0.815(2)	0.789(2)	0.617(2)	1	0.003(1)
O <sub>2</sub> 18f	-0.160(2)	-0.462(2)	0.226(2)	1	0.003(1)

For the purpose of this study we refer to the  $\text{A}_4^{+3}\text{B}_3^{+4}\text{O}_{12}$  stoichiometry as  $\delta$ -phase. The diffraction pattern consists of two types of reflections, strong intense peaks belonging to an average fluorite lattice, and weak super-lattice peaks whose intensity depends on the specific ordering of anion vacancies and the corresponding relaxation of the cations from the ideal fluorite positions.

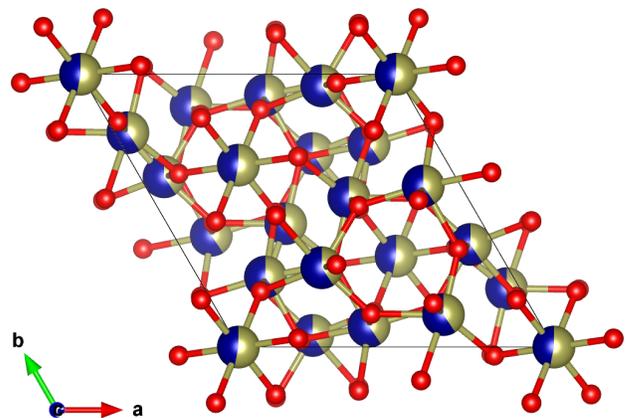


FIG. 3. 3D ball and stick structural model of  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  projected along the  $c$ -axis. The dual colored atoms display cations with a fractional occupancy of Sc (Blue) and Hf (Gold).

The  $c/a$  ratio obtained from the refinement of the pristine  $\delta$ -phase is 0.92837(9), which is more elongated than the corresponding value for an ideal fluorite structure. In addition, the atomic volume for pristine  $\delta$ - $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  was determined to be  $11.5765 \text{ Å}^3/\text{atom}$ .

Fig. 3 displays a projection of the refined structure showing the occupancy of cations over the 3a and 18f Wyckoff positions and the atomic relaxations. The metal ions at 3a positions are 6-fold coordinated with the O2 anions forming a regular octahedron with 6 identical metal-oxygen bonds ( $2.019(11) \text{ Å}$ ). Here, the environment of the 3a site is very compact as outlined by the large values of the Hf and Sc bond valence sums that are 4.63(7) and 3.79(6) respectively. On the other hand, a distorted polyhedron (capped octahedron) with 7 different bonds ranging from  $2.022(16)$  to  $2.476(14) \text{ Å}$  is formed by the cations at the 18f positions with O1 and O2 anions. These bonds are much shorter than what can be expected for Sc and Hf, suggesting that these atoms are actually in an environment much smaller than desirable and more adapted to cations with smaller sizes

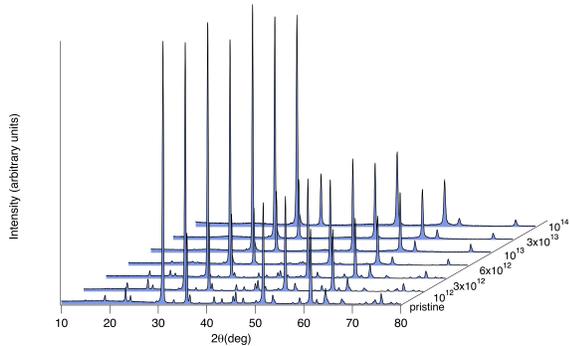


FIG. 4. x-ray diffraction patterns obtained from pristine and 92 MeV Xe irradiated  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  at fluences ranging from  $10^{11} - 10^{14}$   $\text{Xe}/\text{cm}^2$ . The vanishing of superlattice reflections characteristic of the trigonal  $\delta$ -phase occurs above  $6 \times 10^{12}$   $\text{Xe}/\text{cm}^2$ . Before that apparent long-range symmetry changes, the intensity of those superlattice reflections decreases continuously due to a progressive change in the crystal structure.

and/or higher formal valence. It is useful to point out that the longest bond is demonstrably longer than the other six, and it contributes effectively only for 6% to the overall bond valence sum of the cations at 18f positions. This long bond is formed with an O2 atom. For that reason, the cations at 18f positions can be approximately described as a 6-fold coordinated distorted octahedron. The volume of the polyhedron at 3a is  $10.356 \text{ \AA}^3$  while that at 18f is  $11.581 \text{ \AA}^3$  (it would be  $15.281 \text{ \AA}^3$ , should the longest bond be taken into account in the capped octahedron description). The octahedron at the 3a position has a corner-sharing connectivity with the 6 neighbouring 6-fold coordinated polyhedra of the second type (18f), whereas the 18f polyhedra display an edge-sharing connectivity among themselves in addition to the corner sharing connectivity already described. This description is adopted in the rest of this paper. (If the 18f polyhedra were assumed to be 7-fold coordinated capped octahedra, the connectivity would be exclusively edge sharing for all polyhedra, but the analysis of the volumes of these capped octahedra is quantitatively less convenient, though it leads to the same conclusions.) Figure S1 in the supplementary information file is included to display the conventional building block of  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  consisting of 7 polyhedra [41].

## V. IRRADIATED $\delta - \text{Sc}_4\text{Hf}_3\text{O}_{12}$

Fig. 4 shows the measured diffraction patterns of the pristine and irradiated  $\delta$ -phase samples. A gradual decrease of the superlattice reflections characteristic of the  $\delta$ -phase is observed in the initial stages of the irradiation. These superlattice reflections are also increasingly broadened while the reflections corresponding to

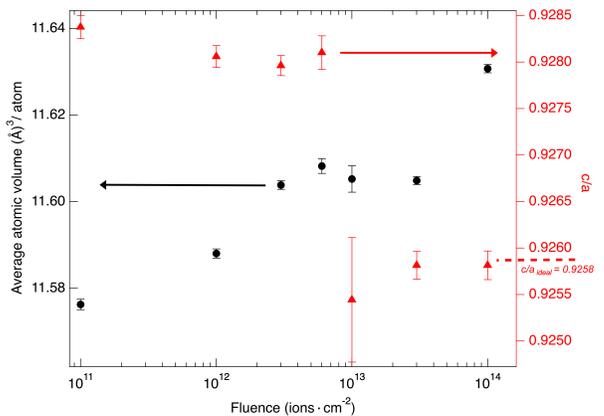


FIG. 5. Changes in the average atomic volume (black circles) and  $c/a$  lattice parameter (red triangles) as a function of Xe fluence. The average atomic volume displays a monotonic increase as a function of the fluence, regardless of the symmetry changes. The  $c/a$  on the other hand shows an abrupt change above  $6 \times 10^{12}$  ions/cm<sup>2</sup> marking a change in the long-range symmetry. Ideal  $c/a$  for fluorite is shown as dotted line. For comparison purposes, the lattice parameters were always calculated in the trigonal symmetry of the pristine phase, though above  $10^{13}$  ions/cm<sup>2</sup> the lattice becomes cubic. Note that the  $c/a$  ratio and atomic volume for pristine  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  (not shown here) are 0.92837(9) and  $11.5765 \text{ \AA}^3/\text{atom}$ , respectively and are extremely close to those obtained for the sample irradiated with  $1 \times 10^{11}$  ions/cm<sup>2</sup>.

a fluorite average structure are only marginally affected by a microstrain effect related to an inhomogeneous defect buildup. This suggests the characteristic correlation length of the  $\delta$ -phase, is continuously reduced as the irradiation proceeds. The underlying mechanism controlling these changes is not clear, but partial healing of the defects can be achieved by the significant atomic transport occurring in the anion sublattice. The corresponding correlation length of the damaged  $\delta$ -phase remains much larger than the transverse dimension of the region impacted by a single ion track as long as these superlattice reflections are observed. Above  $6 \times 10^{12}$   $\text{Xe}/\text{cm}^2$ , these superlattice reflections vanish, leaving behind only the parent fluorite peaks and diffuse scattering. This indicates that irradiation-induced defects cause the ordered  $\delta$ -phase structure to transition to something resembling a defect fluorite phase that still possesses residual short-range order. Rietveld refinements of diffraction patterns up to the fluence of  $6 \times 10^{12}$   $\text{Xe}/\text{cm}^2$  were carried out using the  $\delta$ -phase model obtained from the pristine sample. The refinement of the pattern at  $10^{13}$   $\text{Xe}/\text{cm}^2$  does not provide the proper feedback for determining the phases of the atomic displacements and this leads to larger thermal displacement parameters in the average fluorite structure. Hence, from here onward, the observed reflections were only refined using a fluorite average structure while the diffuse scattering can be modeled using a correlated microdomain approach.

Ion irradiation in this  $\delta$ -phase produces two different

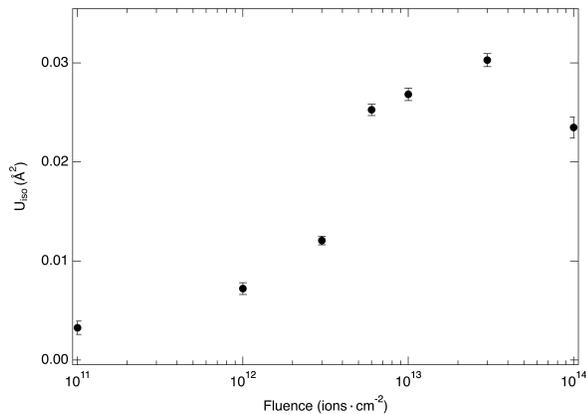


FIG. 6. Thermal displacement parameters ( $U_{iso}$ ) as a function of fluence for pristine and 92 MeV Xe irradiated  $Sc_4Hf_3O_{12}$ .  $U_{iso}$  parameters were obtained after Rietveld refinement and indicates an increase of disorder in the  $\delta$ -phase which gradually saturates when the structure is transformed to a defect fluorite phase.

types of observable changes. The first type of modification concerns long-range perturbation of the lattice related to elastic and polar interactions among structural defects. These changes alter the volume of the reference cell and its shape that was characterised by the  $c/a$  ratio in this present case. The second type of modifications are short-range and affect more directly the relaxation of the atomic structure characterized by composition and relaxation of the atomic positions. They can then also induce polymorphism of the structural motifs, and change the polyhedra connectivity's thus building-up competition between local configurations.

Changes in the average atomic volume and  $c/a$  lattice parameter obtained from these refinements are displayed in Fig. 5. The atomic volume and the  $a$ -lattice parameter increase with increasing fluence. At lower fluences, a progressive convergence of  $c/a$  towards the ideal fluorite ratio (0.9258) is observed. Then, at  $10^{13}$  Xe/cm<sup>2</sup>, a sudden decrease in the  $c$ -lattice parameter occurs, pinning the  $c/a$  to the ideal value. This change is concomitant with the disappearance of the superlattice reflections.

On the other hand, the thermal displacement parameter ( $U_{iso}$ ) displayed in Fig. 6 shows a gradual increase before practically saturating after the transformation to long-range fluorite. This indicates a high degree of displacive disorder in the long-range average fluorite structure. The overall atomic displacement parameter ADP( $U_{iso}$ ) is  $0.003 \text{ \AA}^2$  for the pristine sample and it increases steadily at higher fluences to saturate around  $0.03 \text{ \AA}^2$ . Note III and Figure S2 in the supplementary information file is included to display the evolution of ADP ( $U_{iso}$ ) as a function of the fluence on a linear scale which shows the value for the pristine sample [42].

The six identical metal to oxygen bond lengths for 3a octahedra (those at the corners of Fig. 3) increase from  $2.019(11) \text{ \AA}$  to  $2.164(16) \text{ \AA}$  while the average of the 6

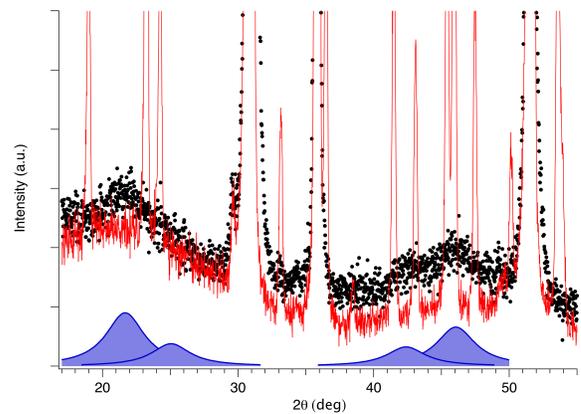


FIG. 7. XRD patterns obtained from  $Sc_4Hf_3O_{12}$ , pristine delta phase (solid red) and irradiated with  $10^{14}$  Xe/cm<sup>2</sup> (black dots) showing emergence of diffuse scattering (blue peaks) at the angular positions corresponding to (211), (220), (332), and (413) superlattice reflections of bixbyite-related structures ( $Ia\bar{3}$ ,  $a_B=2a_F$ )

shorter bond lengths for the cations at 18f positions decreases from  $2.15 \text{ \AA}$  to  $2.13 \text{ \AA}$ . It can be seen that the shared edges among 18f octahedra are shortened after irradiation, which is a result of the swelling of 3a-type octahedra. These modifications to the structural motif cause an overall increase in the distortion of the structure that is not akin to the convergence toward a long-range fluorite as observed for the lattice parameters. At lower fluence, a quantitative evolution of polyhedral volumes can be obtained in the  $\delta$ -phase structure. A 23% increase in the volume of octahedra around the 3a site is observed between the pristine and the sample irradiated at a fluence of  $6 \times 10^{12}$  Xe/cm<sup>2</sup>, whereas a decrease of 10% in the octahedral volume around the 18f site is also observed. The change in volume of these polyhedra at  $6 \times 10^{12}$  Xe/cm<sup>2</sup> converges to the volumes observed in the two bixbyite polyhedra ( $10.42$  and  $12.95 \text{ \AA}^3$ ). Hence, the local and long-range changes are thus divergent and the local structure is not averaging to an ideal fluorite where cation and anion vacancies are distributed at random.

Indeed, at  $10^{13}$  Xe/cm<sup>2</sup> a diffuse scattering signal appears (Fig. 7). The angular positions of the diffuse scattering components of the scattering do not change at fluences above  $10^{13}$  Xe/cm<sup>2</sup>. These positions do not overlap with the positions of the pristine  $\delta$ -phase superlattice peaks but rather correspond to new positions compatible with superlattice reflections of a bixbyite-type structure. In spite of the O stoichiometry, these positions are not compatible with a pyrochlore structural arrangement because they do not satisfy the F-center extinction rules. Also, the diffuse signal at (211) is not compatible with a  $a_W = \sqrt{2}a_F, b_W = 2a_F, c_W = \sqrt{2}a_F$  Imma weberite arrangement.

The bixbyite-like arrangement hypothesis is also in agreement with the observation of diffuse spots at the bixbyite reciprocal lattice points by TEM in low-energy

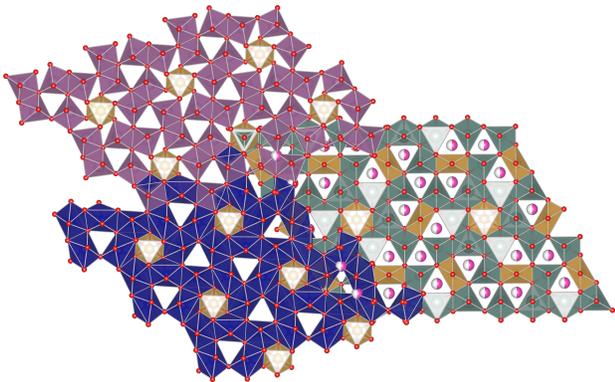


FIG. 8. Schematic changes induced by the ion irradiation on the occupancies of the anion sublattice. The blue and purple structures represent the pristine structure with the two polyhedra descriptions, the green structure on the right the bixbyite-like arrangement where half of the oxygen vacant sites are on average randomly filled (displayed as half coloured pink spheres).

irradiation experiments on  $\delta$ -phase samples [20, 21]. While pyrochlore and weberite structures are characterized by a cation site preference onto the A and B sites of the generic  $A_2B_2O_7$  chemical formula, in the bixbyite-related structures  $M_2O_{3.5}$  a pronounced cation selectivity is not expected and the bixbyite order displayed schematically in Fig. 8 is only given by the stacking of the O vacancies and the atom position relaxation they induce. This particular order might be related to the moderate cation selectivity and the pronounced O vacancy ordering already observed in the pristine  $\delta$ -phase of this compound. The correlation length of this local structure is about 4 nm, as derived from the integral breadth of the diffuse signal. Previously, ion tracks consisting of a disordered fluorite core with 3–4 nm in diameter were reported in swift heavy ion irradiated  $\delta$ - $Sc_4Zr_3O_{12}$  [22]. The corresponding lattice parameter of the present bixbyite-related local phase is about 9.99(3) Å. Therefore, this phase is almost 2.4 % denser than the average long-range radiation-induced oxygen deficient fluorite phase and also 1.9 % denser than the pristine  $\delta$ -phase, marking another departure from the evolution in volume of the long-range average-fluorite phase.

We note here that the damage evolution revealed by our XRD measurements is also not compatible with conventional radiation-induced phase transformation models, such as the "Gibbons" cascade overlap models [43, 44]. These models require that the latent damage in the cascade regions produces a second phase that is not correlated and generally incoherent with the pristine (unirradiated) material. On the contrary, our latent damage regions are likely coherent with the undamaged regions (evidence for this is provided in TEM images in Tang et al. [22], where they observed coherence between latent tracks and pristine material in swift heavy ion-irradiated  $Sc_4Zr_3O_{12}$  (the oxide structure and irradiation condi-

tions in Tang et al. are very similar to the compound and experimental conditions used in this study). Furthermore, were we to have coexisting delta and disordered fluorite phases in our low-fluence microstructures (i.e., fluences ranging from  $10^{11} - 6 \times 10^{12}$  ions/cm<sup>2</sup>), we should expect to resolve two sets of XRD peaks: one from the rhombohedrally-distorted  $\delta$ -phase ( $c/a$  greater than ideal), the second from the cubic disordered fluorite phase (with the ideal  $c/a$  ratio). We do not observe this hypothetical mixture at any fluence, based on our XRD measurements.

## VI. DISCUSSION AND CONCLUSION

According to the previous work of Ishimaru et al. [20] low energy ion irradiation (300 keV Kr and up to a fluence of  $3 \times 10^{16}$  ions/cm<sup>2</sup>) induces structural changes in the  $\delta$ -phase compound  $Sc_4Zr_3O_{12}$ . Using cross section TEM, two different phases were observed in the sample. These phases occur in two separate layers located above the pristine sample substrate: the diffraction pattern from the layer immediately above the substrate only presented spots characteristic of a fluorite phase, while the layer closer to the surface presented additional diffuse spots obeying the selection rules of  $Ia\bar{3}$  space group. This was then indexed with a bixbyite-type structure. The authors concluded that this phase was likely formed by some sort of re-arrangements of oxygen vacancies within the fluorite layer. The existence of the two layers seems related to the characteristics of the low energy irradiation, where damage occurs in the absence of implanted ions in the bixbyite-type layer, where as damage coincides with significant ion implantation in the fluorite-like layer. In the present experiment, no implantation occurs within the layer probed by x-rays and indeed, only a disordered fluorite with bixbyite local flavour is observed.

Group-subgroup analysis establishes that there is no direct compatibility relation between bixbyite and  $\delta$ -phase, thus preventing the existence of an order parameter describing the direct transformation. The only possible pathway to connect the two phases is through an intermediate fluorite phase that shares the specific symmetry elements of bixbyite and  $\delta$ -phase. Bixbyite and  $\delta$ -phase share a unique feature among the phases observed in the pseudo binary phase diagrams of type  $A_2^{+3}O_3 - B^{+4}O_2$ : these two phases are the only ones where the metal ions are 6-fold coordinated with O anions.

The  $\delta$ -phase can also be viewed as having a capped octahedra which is found in the A-type  $M_2O_3$  compounds. A known high temperature phase transformation occurs from the A-type into a C-type bixbyite in some of these rare earth oxides. Hence it is possible to change from 7-fold to 6-fold in these sesquioxides and the same is likely to occur in the  $\delta$ -structure. Therefore, it is likely that these two phases actually exhibit some sort of competition. Though the two phases have qualitatively similar polyhedra, they do not have exactly the same connectiv-

ity, and this explains the different O stoichiometries.

The bixbyite phase generally presents an extended domain of existence in the oxygen-excess range, as for instance in  $\text{CeO}_{2-x}$ ,  $\text{TbO}_{2-x}$ , and  $\text{PrO}_{2-x}$  [45, 46] ( $0.28 \leq x \leq 0.5$ ). Thus, the bixbyite signature from a structure with extra O atoms filling the bixbyite O vacancies would translate into weak superstructure peaks, similar to the diffuse scattering observed, as the amplitudes of the cation relaxations near the O vacancies would be smaller. This observation suggests that the bixbyite phase acts possibly as a chemical attractor, having some kind of exotic dynamics for local chaotic fluctuations of the oxygen stoichiometry. The bixbyite local configuration reached after ion irradiation is then a frozen metastable steady state where the phase trajectories evolving away from the  $\delta$ -phase composition remain in the vicinity of the bixbyite

attractor. This particular characteristic of the bixbyite phase seems effective in supporting radiation tolerance, by creating a very large number frozen local configurations of lower symmetry: preserving a very large number of configurations that maximize and thereby stabilize the apparent long-range cubic symmetry. Systems exhibiting these characteristics can then be exploited to effectively engineer radiation resistant materials.

## ACKNOWLEDGMENTS

The authors would like to acknowledge Dr. Isabelle Monnet and Dr. Jean-Claude Pivin for their help in performing the ion irradiation experiment at GANIL.

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- [1] C. Wagner and W. Schottky, Theorie der geordneten mischphasen. *Z. Physik. Chem.* **B11**, 163, 1930.
- [2] O. Toft Sørensen, *Nonstoichiometric oxides* Academic Press, 1981, ISBN 9780126552805.
- [3] L. Cai and J. C. Nino. Complex ceramic structures. I. Weberites. *Acta Cryst. B*, **65**, 269–290, 2009.
- [4] K.E. Sickafus, L. Minervini, R. W. Grimes, J. A. Valdez, M. Ishimaru, F. Li, K. J. McClellan and T. Hartmann, Radiation tolerance of complex oxides *Science*, **289**: 748, 2000.
- [5] B.J. Wuensch, and K.W. Eberman, Order-disorder phenomena in  $\text{A}_2\text{B}_2\text{O}_7$  pyrochlore oxides. *JOM* **52** 19–21 2000.
- [6] M. Lang, et al., Review of  $\text{A}_2\text{B}_2\text{O}_7$  pyrochlore response to irradiation and pressure. *Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms* **268** 2951–2959 2010
- [7] Y. H. Li, B. P. Uberuaga, C. Jiang, S. Choudhury, J. A. Valdez, M. K. Patel, J. Won, Y.-Q. Wang, M. Tang, D. J. Safarik, D. D. Byler, K. J. McClellan, I. O. Usov, T. Hartmann, G. Baldinozzi, and K. E. Sickafus *Phys. Rev. Lett.* **108**, 195504, 2012.
- [8] J. Shamblin, M. Feyngenson, J. Neufeind, C. L. Tracy, F. Zhang, S. Finkeldei, D. Bosbach, H. Zhou, R. C. Ewing and M Lang, Probing disorder in isometric pyrochlore and related complex oxides *Nat. Mater.*, **15**: 507, 2016.
- [9] D. Simeone, G. J. Thorogood, D. Huo, et al. Intricate disorder in defect fluorite/pyrochlore: a concord of chemistry and crystallography. *Sci Rep* **7**, 3727 2017.
- [10] Pilania, G., B. Puchala, and B. Uberuaga, Distortion-stabilized ordered structures in  $\text{A}_2\text{BB}'\text{O}_7$  mixed pyrochlores. *npj Comput. Mater.*, **5**, 7 2019.
- [11] M. Tang, J. A. Valdez, K.E. Sickafus and P. Lu, Order-disorder phase transformation in ion-irradiated rare earth sesquioxides *Appl. Phys. Lett.*, **90**: 151907, 2007.
- [12] C. L. Tracy, M. Lang, F. Zhang, C. Trautmann, and R. C. Ewing, Phase transformations in  $\text{Ln}_2\text{O}_3$  materials irradiated with swift heavy ions *Phys. Rev. B*, **92**: 174101, 2015.
- [13] G. Sattonnay, S. Bilgen, L. Thome, C. Grygiel, I. Monnet, O. Plantevin, C. Huet, S. Miro, and P. Simon, Structural and microstructural tailoring of rare earth sesquioxides by swift heavy ion irradiation *Phys. Status Solidi B*, **253**: 2110, 2016.
- [14] G. Baldinozzi, J.-F. Berar, M. Gautier-Soyer, and G. Calvarin. Segregation and site selectivity in Zr-doped  $\text{Y}_2\text{O}_3$ . *J. Phys.: Condens. Matter* **9** 9731–9744, 1997.
- [15] G. Baldinozzi, J.-F. Berar, and G. Calvarin. Rietveld Refinement of Two-Phase Zr-Doped  $\text{Y}_2\text{O}_3$ . *Materials Science Forum*, **278281**, 680-685, 1998.
- [16] H.J. Rossell, Crystal structures of some fluorite-related  $\text{M}_7\text{O}_{12}$  compounds. *J. Solid State Chem.*, **19**: 103, 1976.
- [17] Y. Hinatsu, N. Masaki, and T. Fujino, The crystal structure of  $\text{La}_6\text{UO}_{12}$ . *J. Solid State Chem.* **73**: 567, 1988.
- [18] R. M. Rojas, P. Herrero, P. J. Garcia Chain, and J. Rodriguez-Carvajal, Structural study of the rhombohedral fluorite-related  $\text{R}_{III}$  Phase  $\text{U}_{1-y}\text{La}_y\text{O}_{2\pm x}$ ,  $0.56 \leq y \leq 0.67$  *J. Solid State Chem.* **112**: 322, 1994.
- [19] J.A. Valdez, M. Tang and K.E. Sickafus, Radiation damage effects in  $\delta$ - $\text{Sc}_4\text{Zr}_3\text{O}_{12}$  irradiated with  $\text{Kr}^{2+}$  ions under cryogenic conditions. *Nucl. Instrum. and Meth. Phys. Res.*, **250**: 148, 2006.
- [20] M. Ishimaru, Y. Hirotsu, M. Tang, J. A. Valdez, and K.E. Sickafus, Ion-beam-induced phase transformations in  $\delta$ - $\text{Sc}_4\text{Zr}_3\text{O}_{12}$ . *J. Appl. Phys.*, **102**: 063532, 2007.
- [21] K. E. Sickafus, M. Ishimaru, Y. Hirotsu, I. Usov, J. A. Valdez, P. Hosemann, A. L. Johnson and T. T. Thao, Compositional analyses of ion-irradiation-induced phases in  $\delta$ - $\text{Sc}_4\text{Zr}_3\text{O}_{12}$ . *Nucl. Instrum. and Meth. Phys. Res.*, **266**: 2892, 2008.
- [22] M. Tang, P. Kluth, J. Zhang, M. K. Patel, B. P. Uberuaga, C.J. Olson Reichhardt and K.E. Sickafus, Swift heavy ion irradiation-induced microstructure modification of two delta-phase oxides:  $\text{Sc}_4\text{Zr}_3\text{O}_{12}$  and  $\text{Lu}_4\text{Zr}_3\text{O}_{12}$ . *Nucl. Instrum. and Meth. Phys. Res.*, **268**: 3243, 2010.
- [23] J. Zhang, Y. Wang, M. Tang, J. Won, J. A. Valdez, and K. E. Sickafus, Order-to-disorder transformation in  $\delta$ -phase  $\text{Sc}_4\text{Zr}_3\text{O}_{12}$  induced by light ion irradiation. *J. Mater. Res.*, **25**: 248, 2010.
- [24] J. Wen, C. Gao, Y. H. Li, Y. Q. Wang, L. M. Zhang, B.T. Hu, L.J. Chen and X. Su, Ion irradiation induced order-to-disorder transformation in  $\delta$ -phase  $\text{Lu}_4\text{Hf}_3\text{O}_{12}$ . *Nucl. Instrum. and Meth. Phys. Res.*, **310**: 1, 2013.

- [25] J. Wen, Y.H. Li, M. Tang, J. A. Valdez, Y.Q. Wang, M. K. Patel, K.E. Sickafus, Heavy and light ion irradiation damage effects in  $\delta$ -phase  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$ . *Nucl. Instrum. and Meth. Phys. Res.*, **365**: 325, 2015.
- [26] J. Zhang, M. K. Patel, Y. Q. Wang, M. Tang, J. Won, J. A. Valdez and K.E. Sickafus, Strong irradiation tolerance to amorphization in delta- $\text{Sc}_4\text{Ti}_3\text{O}_{12}$ . *Nucl. Instrum. and Meth. Phys. Res.*, **459**: 265, 2015.
- [27] B. H. O'Connor and T. M. Valentine, A neutron diffraction study of the crystal structure of the C-form of yttrium sesquioxide. *Acta Cryst.*, **B25**: 2140, 1969.
- [28] M. R. Thornber, D. J. M. Bevan and J. Graham, Mixed oxides of the type  $\text{MO}_2$  (Fluorite)-  $\text{M}_2\text{O}_3$  - III: Crystal structures of the intermediate phases  $\text{Zr}_5\text{Sc}_2\text{O}_{13}$  and  $\text{Zr}_4\text{Sc}_3\text{O}_{12}$ , *Acta Cryst. B*, **24**: 1183, 1968.
- [29] G. A. Kalinovskaya, F. M. Spiridonov and L. N. Komissarova, Phase equilibria in the  $\text{HfO}_2$ - $\text{Sc}_2\text{O}_3$ . *J. Less-Common Metals*, **17**: 151, 1969.
- [30] J. F. Ziegler and J. P. Biersack, *The stopping and range of ions in matter*, Volume **2-6**. Pergamon Press 1977-1985.
- [31] V. Petricek, M. Dusek and L. J. F. Palatinus, Crystallographic computing system JANA2006: General features. *Z. Kristallogr.*, **229**: 345, 2014.
- [32] K. Momma and F. Izumi, VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Cryst.*, **44**: 1272, 2011.
- [33] E. Rosshirt, F. Frey, H. Boysen, and H. Jagodzinski, Chain ordering in  $\text{E}_2\text{PI}_{1.6}$  (5,10-Diethylphenazinium Iodide). *Acta Cryst. B*, **41**: 66–76, 1985.
- [34] R. J. Nelmes, D. R. Allan, M. I. McMahon, and S. A. Belmonte, Self-hosting incommensurate structure of barium IV. *Phys. Rev. Lett.*, **83**: 4081, 1999.
- [35] T. R. Welberry and B. D. Butler, Interpretation of diffuse x-ray scattering via models of disorder. *J. Appl. Cryst.*, **27**: 205–231, 1994.
- [36] H. Jagodzinski, and F. Frey, Disorder diffuse scattering of x-rays and neutrons. *International tables for crystallography volume B: Reciprocal space* Ed. U Shmueli 407–442, 2006.
- [37] J. Brunet, and K. E. Gubbins, General theory of the long-range pair-correlation function. *The Journal of Chemical Physics*, **49**, 5265-5269, 1968.
- [38] R. B. Neder, F. Frey, and H. Schulz, Diffraction theory for diffuse scattering by correlated microdomains in materials with several atoms per unit cell. *Acta Cryst. A* **46**, 792–798 1990.
- [39] Supplementary material Note I on occupancy of vacant 6c site.
- [40] Supplementary material Note II on profile function model.
- [41] Supplementary material Figure S1 shows the polyhedral model for  $\delta$ -phase.
- [42] Supplementary material Note III on atomic displacement parameter and Figure S2.
- [43] J. F. Gibbons, Ion implantation in semiconductors - Part I: range distribution theory and experiments. *Proceedings of the IEEE* **56**: 295–319 1968.
- [44] J. F. Gibbons, Ion implantation in semiconductors - Part II: Damage production and annealing. *Proceedings of the IEEE* **60**: 1062–1096 1972.
- [45] J. W. McMurray, Thermodynamic assessment of the Pr–O system. *J. Am. Ceram. Soc.* **99** 1092, 2016.
- [46] B. G. Hyde, D. J. M. Bevan and L. Eyring, On the praseodymium oxygen system. *Phil. Trans. Royal Soc. Lond.: A* **259** 583, 1966.